

# Bosenova collapse of axion cloud around a rotating black hole

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# Axions

• Candidates of massive scalar fields.  $\nabla^2 \Phi - \mu^2 \Phi = 0$

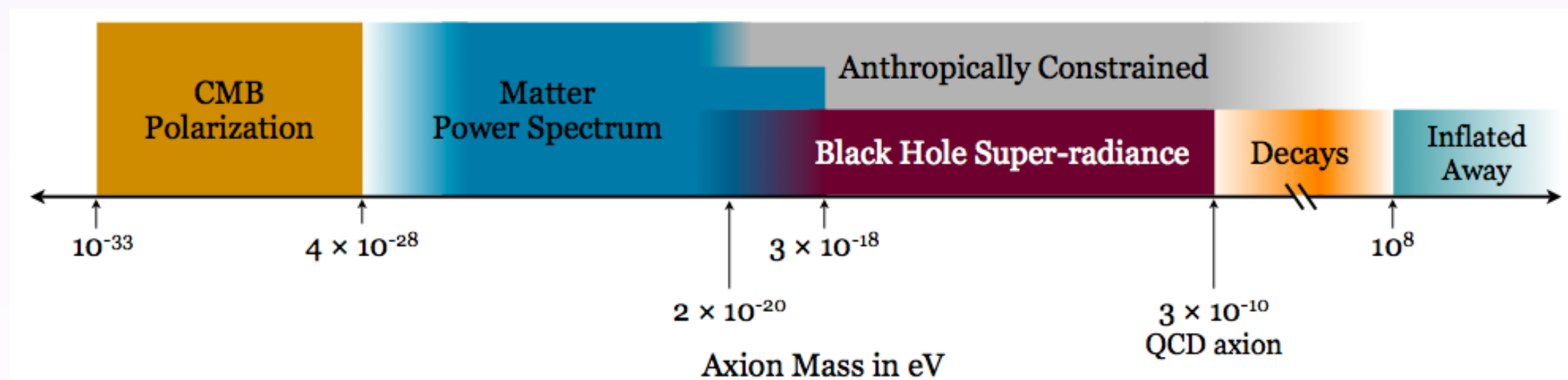
## • QCD axion

- QCD axion was introduced to solve the Strong CP problem.
- It is one of the candidates of dark matter.

## • String axion

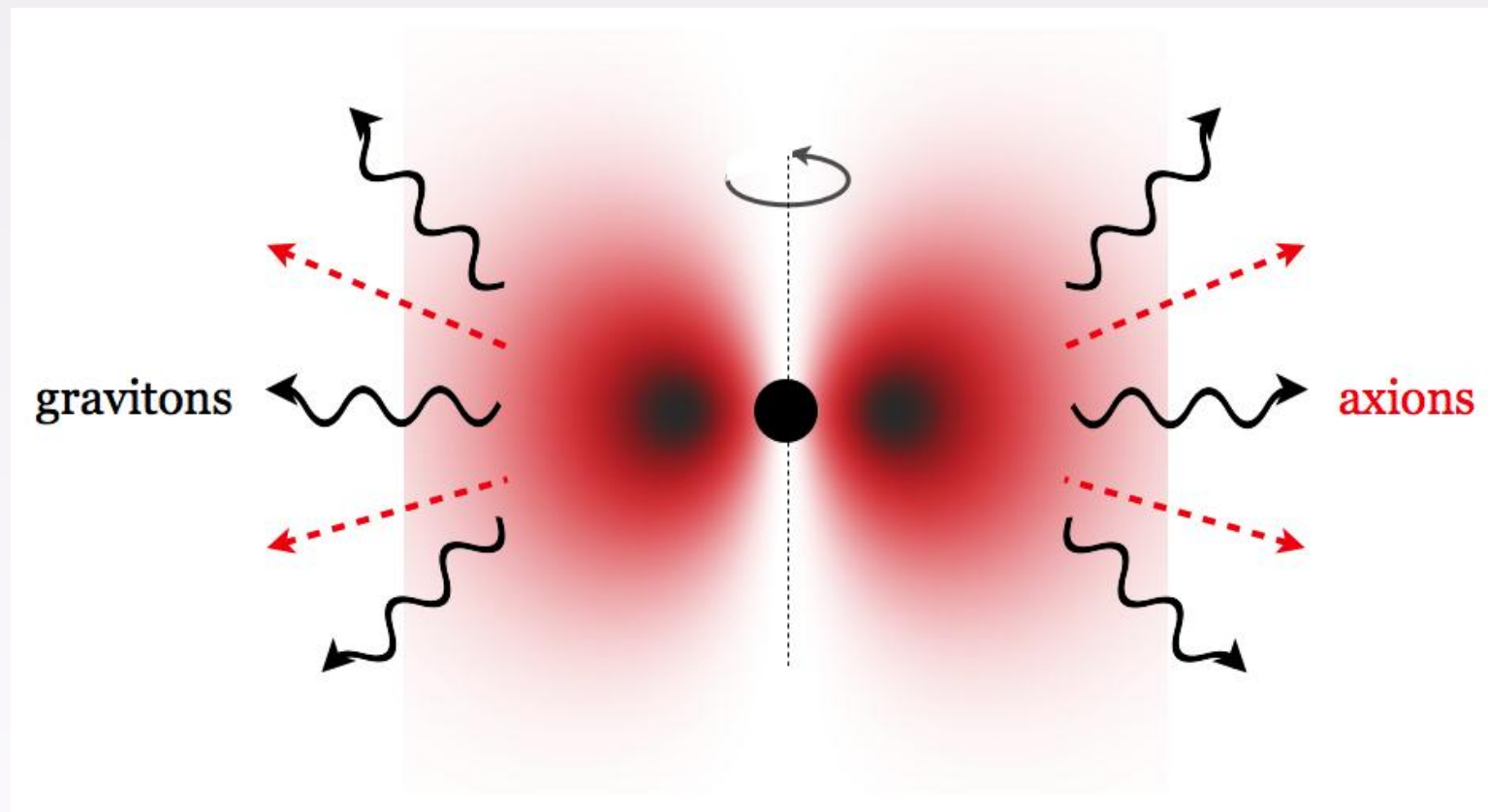
Arvanitaki, Dimopoulos, Dubvosky, Kaloper, March-Russel, PRD81 (2010), 123530.

- String theory predicts the existence of 10-100 axion-like massive scalar fields.
- There are various expected phenomena of string axions.



# Axion field around a rotating black hole

- Axion field makes a bound state and causes the superradiant instability

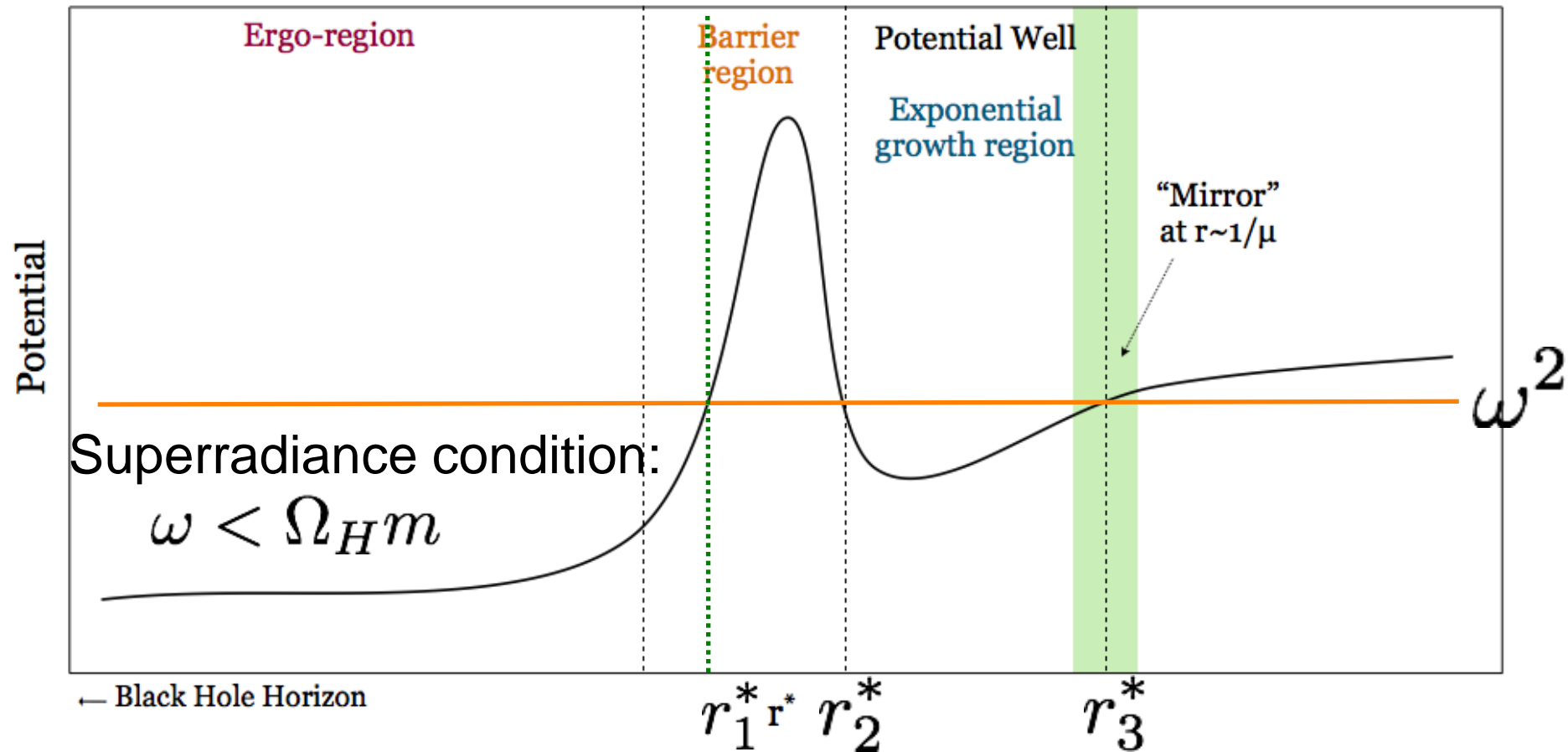


Detweiler, PRD22 (1980), 2323.

Zouros and Eardley, Ann. Phys. 118 (1979), 139.

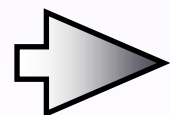
# Bound state

Zouros and Eardley, Ann. Phys. 118 (1979), 139.



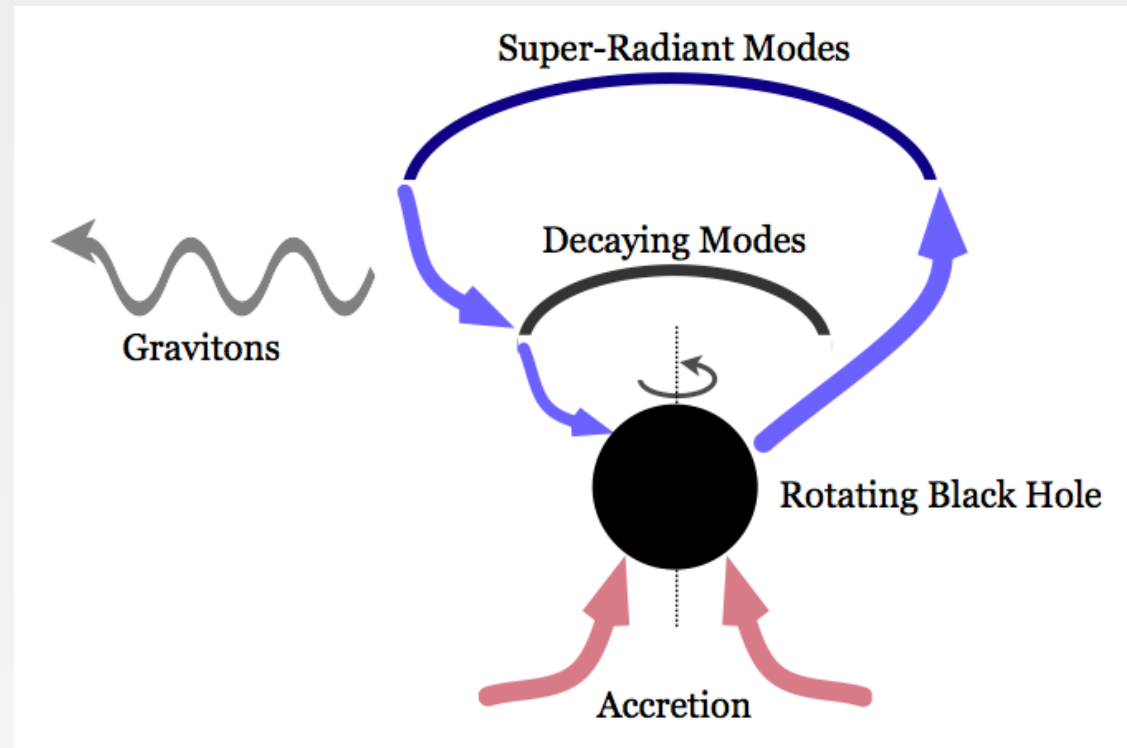
$$\Phi = e^{-i\omega t} R(r) S(\theta) e^{im\phi}$$

$$R = \frac{u}{\sqrt{r^2 + a^2}}$$



$$\frac{d^2 u}{dr_*^2} + [\omega^2 - V(\omega)] u = 0$$

# BH-axion system



Arvanitaki and Dubovsky, PRD83 (2011), 044026.

- Superradiant instability

- - Emission of gravitational waves
  - Pair annihilation of axions

- Effects of nonlinear self-interaction

- - Bosenova
  - Mode mixing

## Nonlinear effect

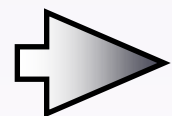
- QCD axion

break

U(1)PQ symmetry  $\rightarrow$  Z(N) discrete symmetry

$V(\Phi)$  becomes periodic.  $\Delta\Phi = 2\pi v_a/N = 2\pi f_a$

$$V = f_a^2 \mu^2 [1 - \cos(\Phi/f_a)]$$



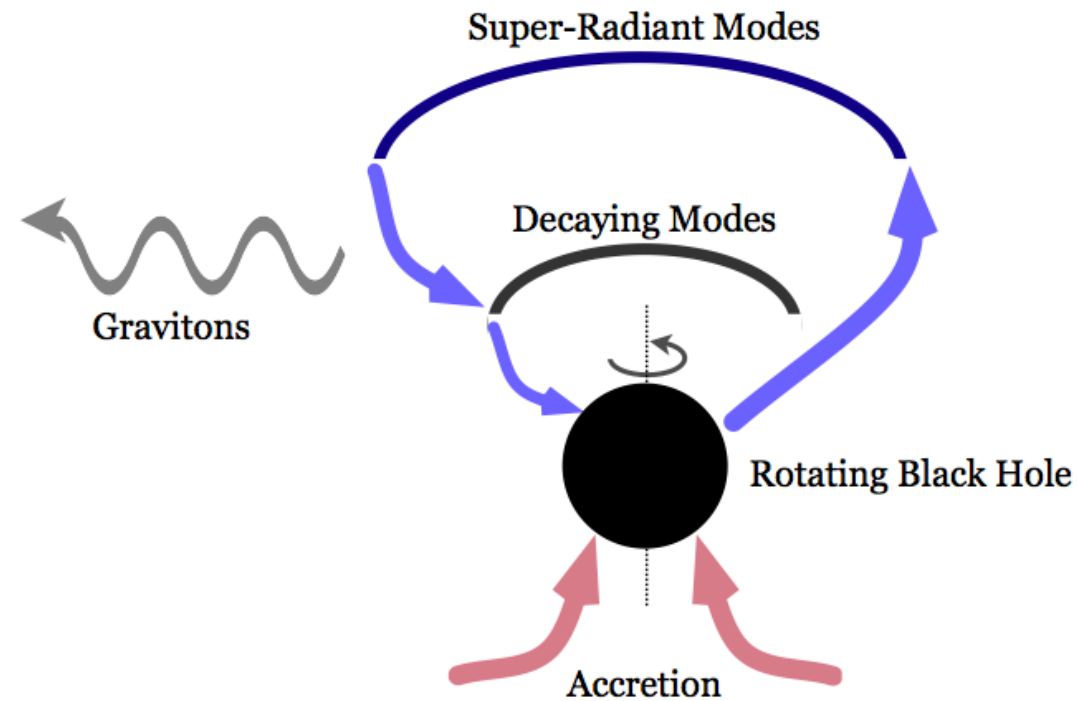
$$\nabla^2 \Phi - \mu^2 f_a \sin\left(\frac{\Phi}{f_a}\right) = 0$$

$$\nabla^2 \varphi - \mu^2 \sin \varphi = 0 \quad \varphi \equiv \frac{\Phi}{f_a}$$

- The similar statement holds also for string axions.



# BH-axion system



Arvanitaki and Dubovsky, PRD83 (2011), 044026.

- Superradiant instability

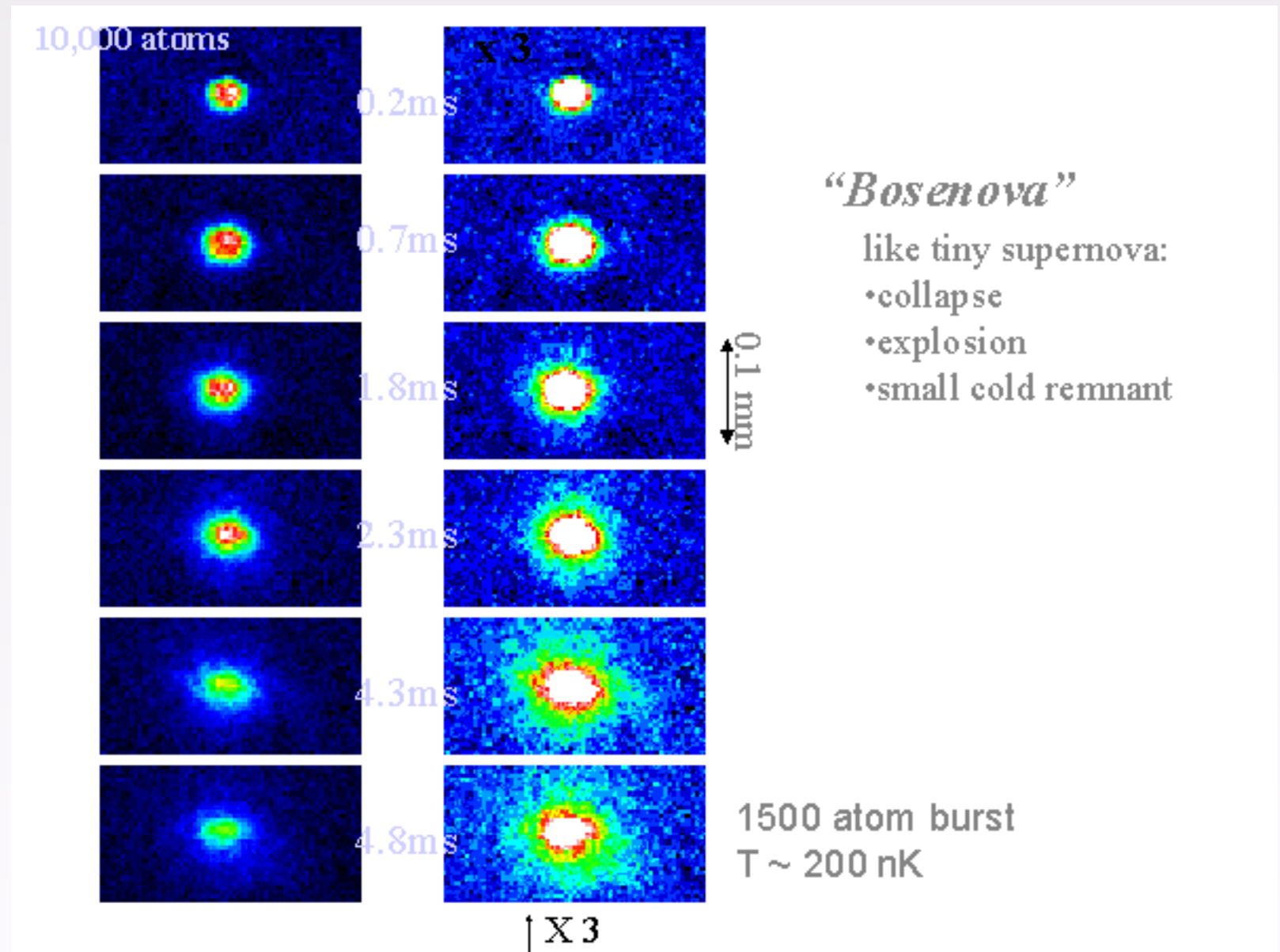
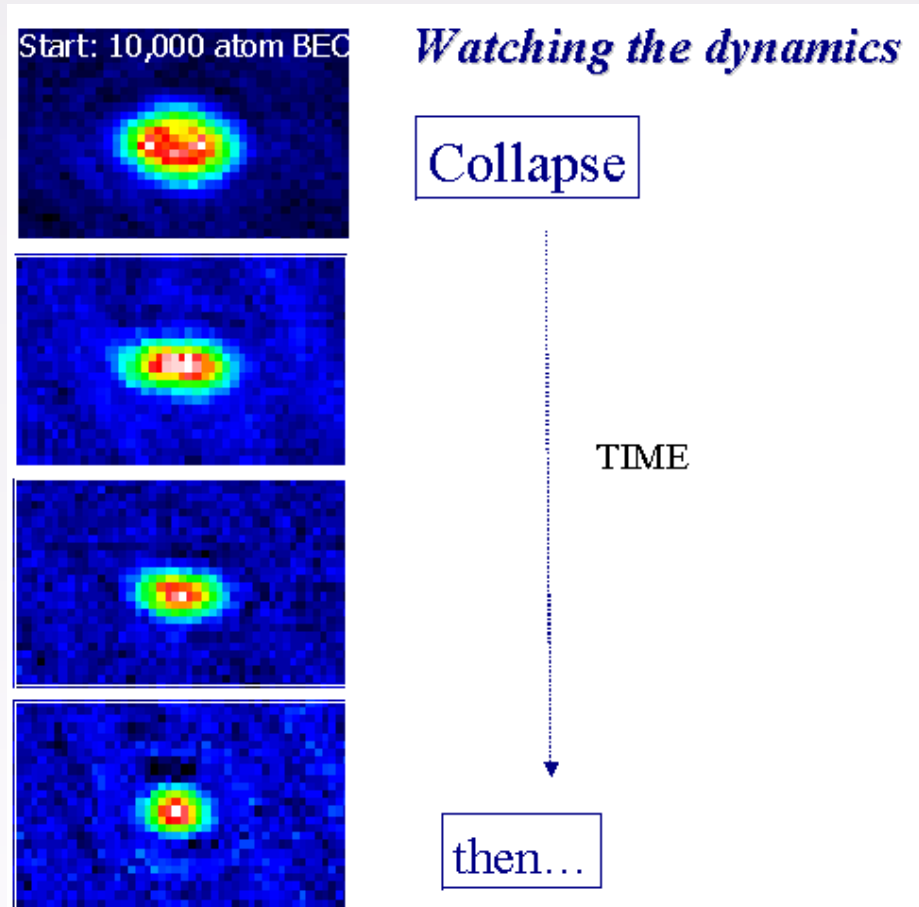
- - Emission of gravitational waves
  - Pair annihilation of axions

- Effects of nonlinear self-interaction

- - Bosonova
  - Mode mixing

# Bosenova in condensed matter physics

<http://spot.colorado.edu/~cwieman/Bosenova.html>



BEC state of Rb85 (interaction can be controlled)

Switch from repulsive interaction to attractive interaction

Wieman et al., Nature 412 (2001), 295

## What we would like to do

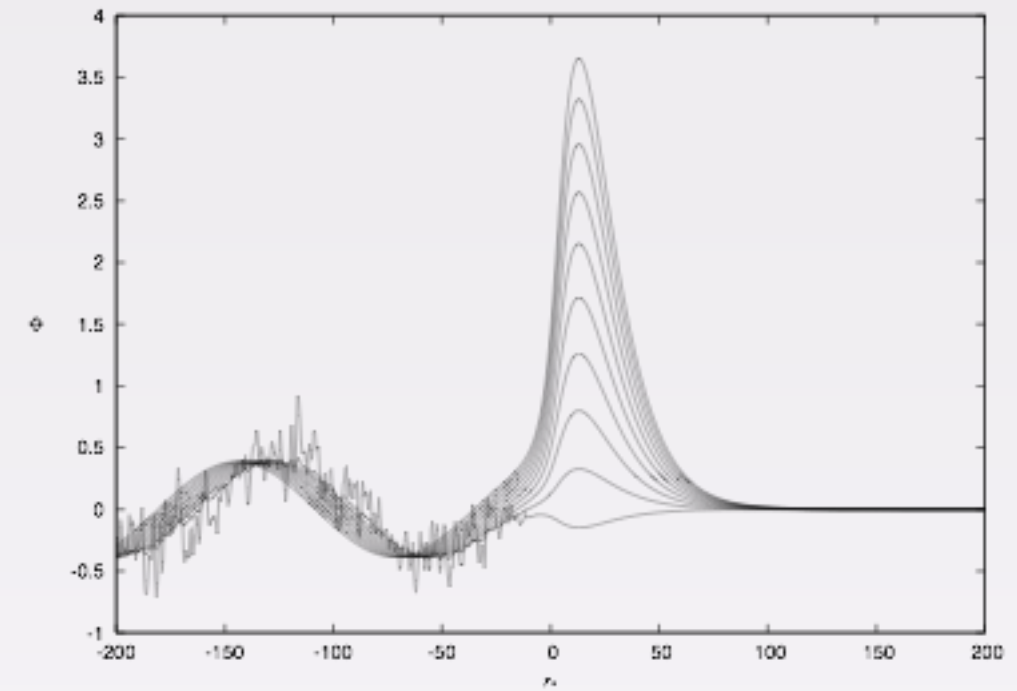
- We would like to study the phenomena caused by axion cloud generated by the superradiant instability around a rotating black hole.
- In particular, we study numerically whether “Bosenova” happens when the nonlinear interaction becomes important.
- We adopt the background spacetime as the Kerr spacetime, and solve the axion field as a test field.

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## First difficulty

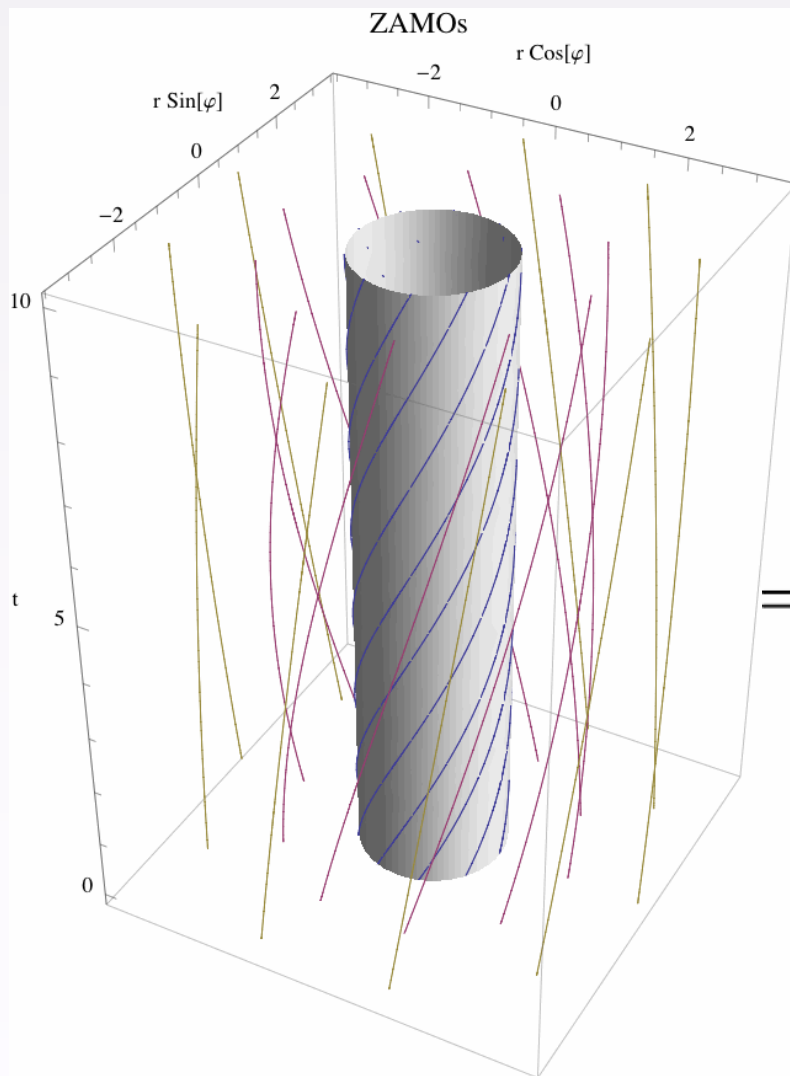
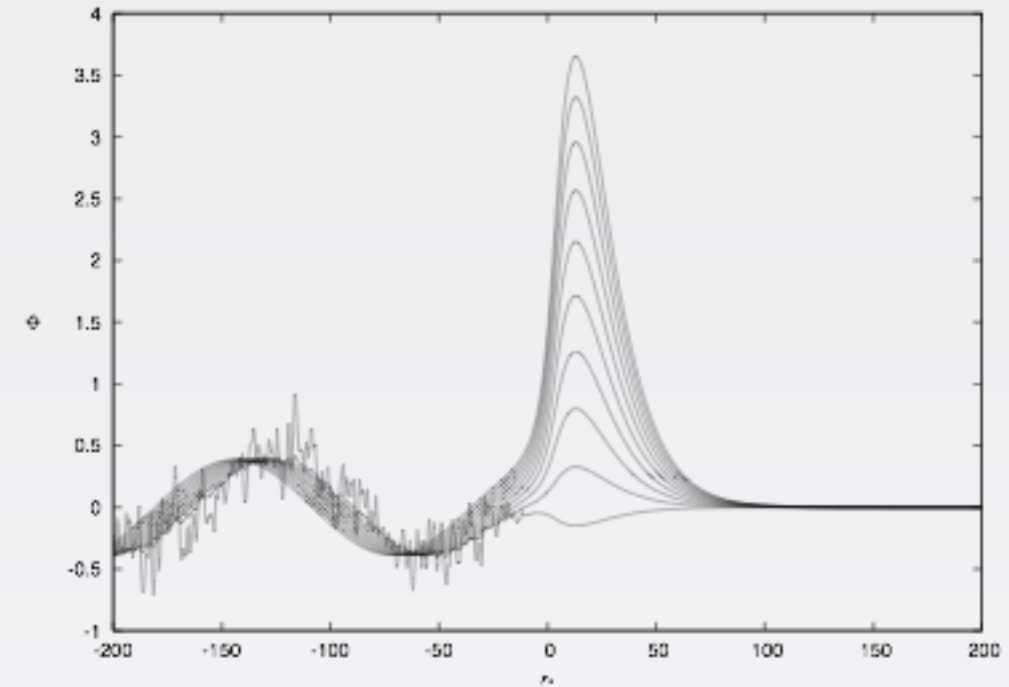
- Stable simulation cannot be realized in Boyer-Lindquist coordinates.



# First difficulty

- Stable simulation cannot be realized in Boyer-Lindquist coordinates.

➔ We use ZAMO coordinates.



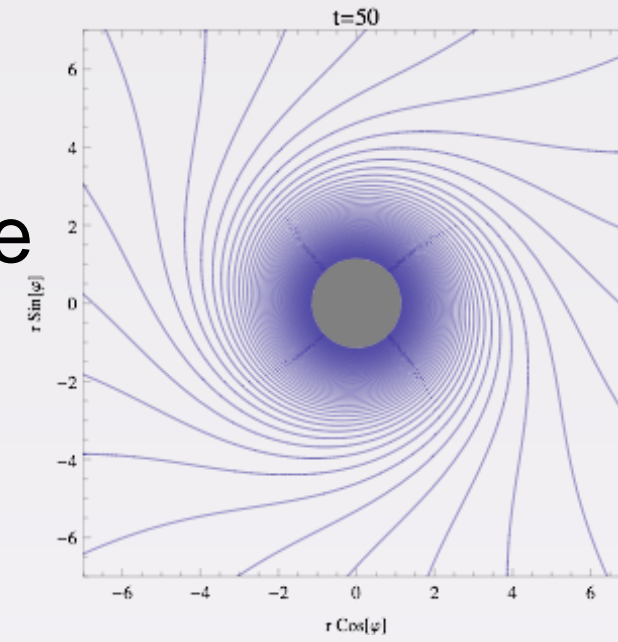
$$\Omega = \frac{d\phi}{dt} = \frac{u^\phi}{u^t} = -\frac{g_{t\phi}}{g_{\phi\phi}}$$

$$= \frac{2Mar}{(r^2 + a^2)^2 - \Delta a^2 \sin^2 \theta}$$

$$\begin{aligned} \tilde{t} &= t, \\ \tilde{\phi} &= \phi - \Omega(r, \theta)t, \\ \tilde{r} &= r, \\ \tilde{\theta} &= \theta, \end{aligned}$$

## Second difficulty

- ZAMO coordinates becomes more and more distorted in the time evolution



## Second difficulty

- ZAMO coordinates becomes more and more distorted in the time evolution

➡ We “pull back” the coordinates

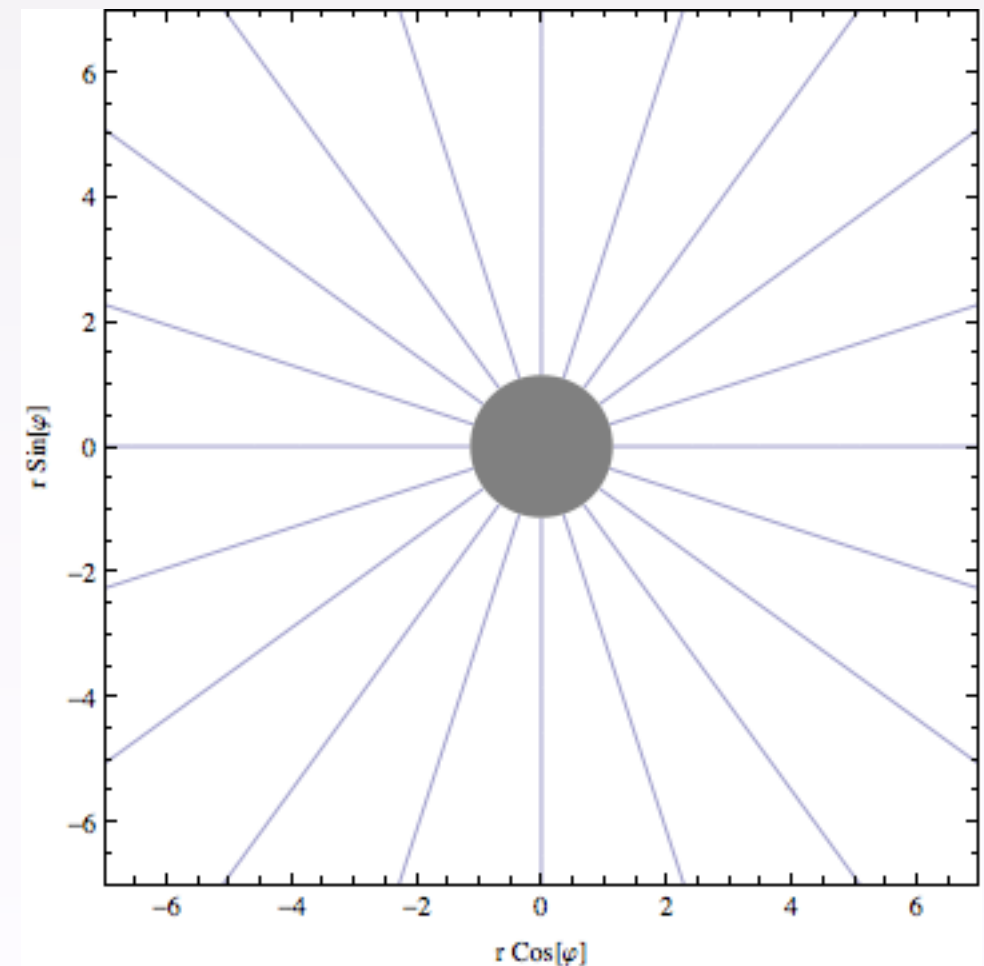
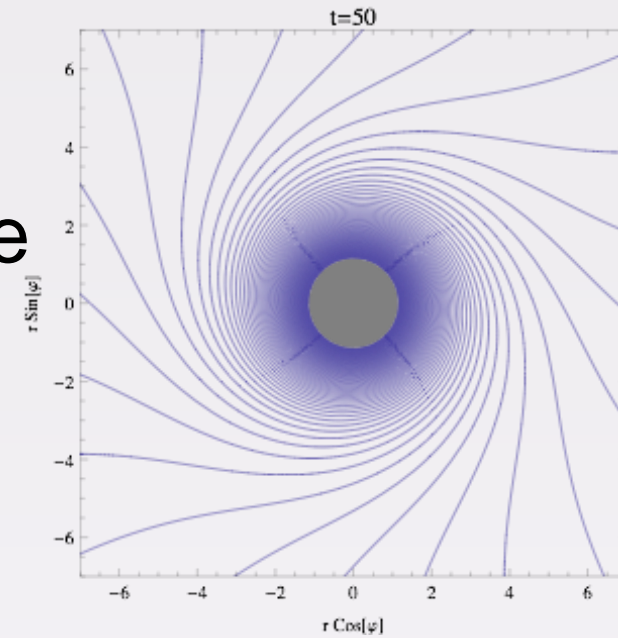
$$nT_P \leq t \leq (n+1)T_P :$$

$$t^{(n)} = t,$$

$$\phi^{(n)} = \phi - \Omega(r, \theta)(t - nT_P),$$

$$r^{(n)} = r,$$

$$\theta^{(n)} = \theta.$$





## Our 3D code

- Space direction : 6th-order finite discretization

- Time direction : 4th-order Runge-Kutta

- Grid size:  $\Delta r_* = 0.5 \quad (M = 1)$   
 $\Delta\theta = \Delta\phi = \pi/30$

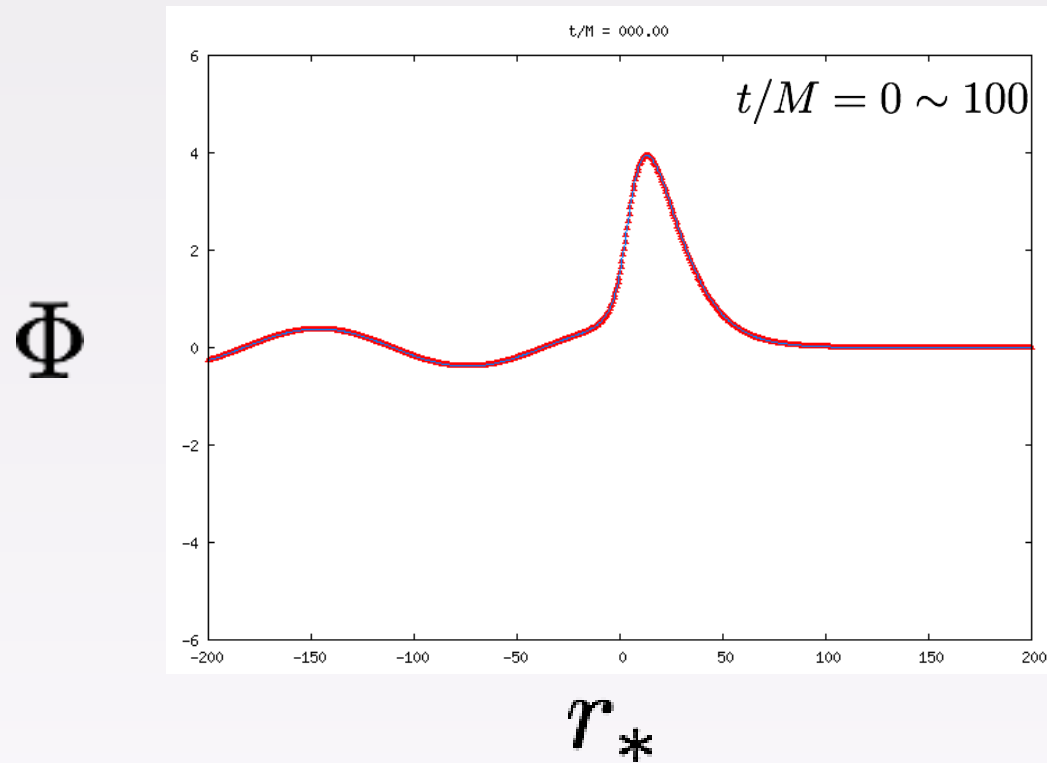
- Courant number:  $C = \frac{\Delta t}{\Delta r_*} = \frac{1}{20}$

- Pure ingoing BC at the inner boundary,  
Fixed BC at the outer boundary

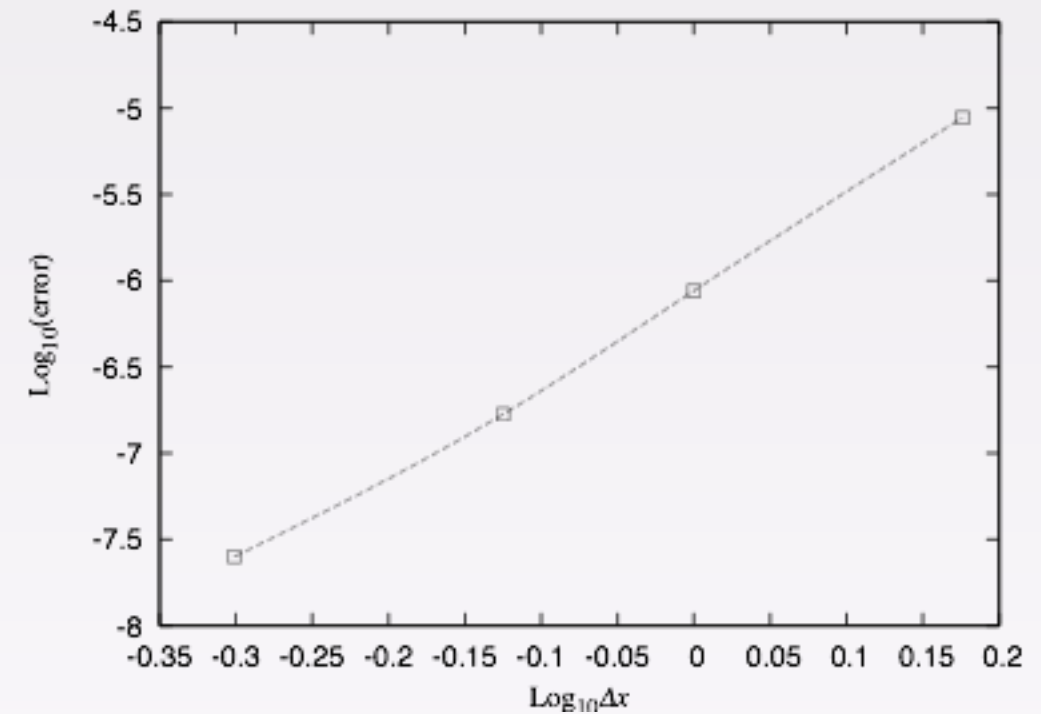
- Pullback: 7th-order Lagrange interpolation

# Code check

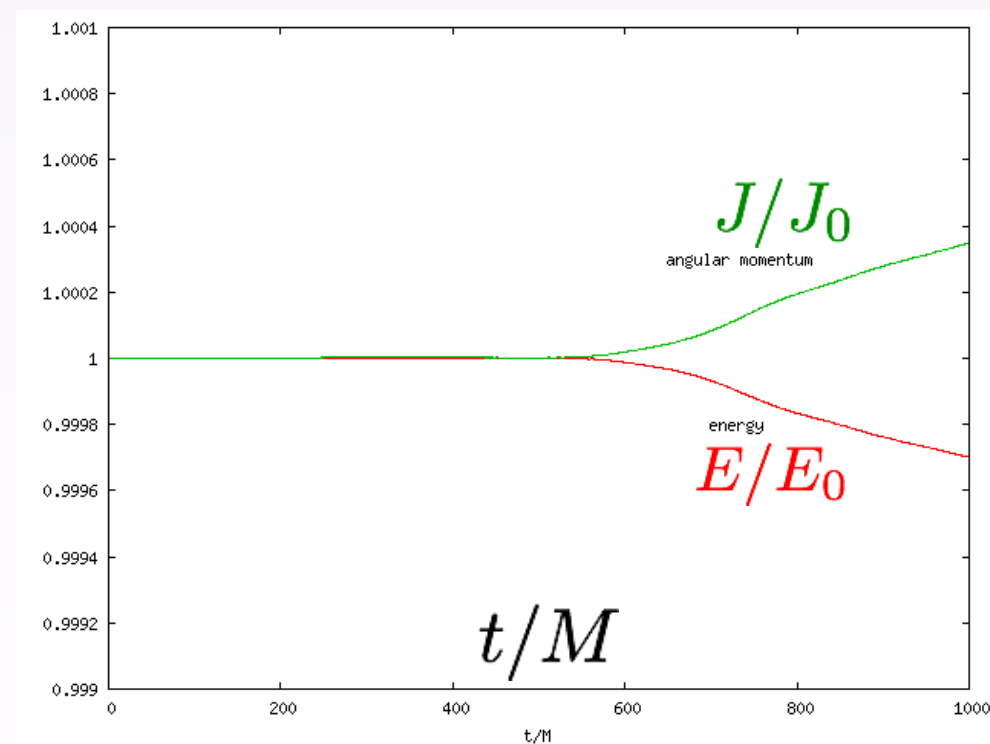
- Comparison with semianalytic solution in the Klein-Gordon case



- Convergence



- Conserved quantities



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# Numerical simulation

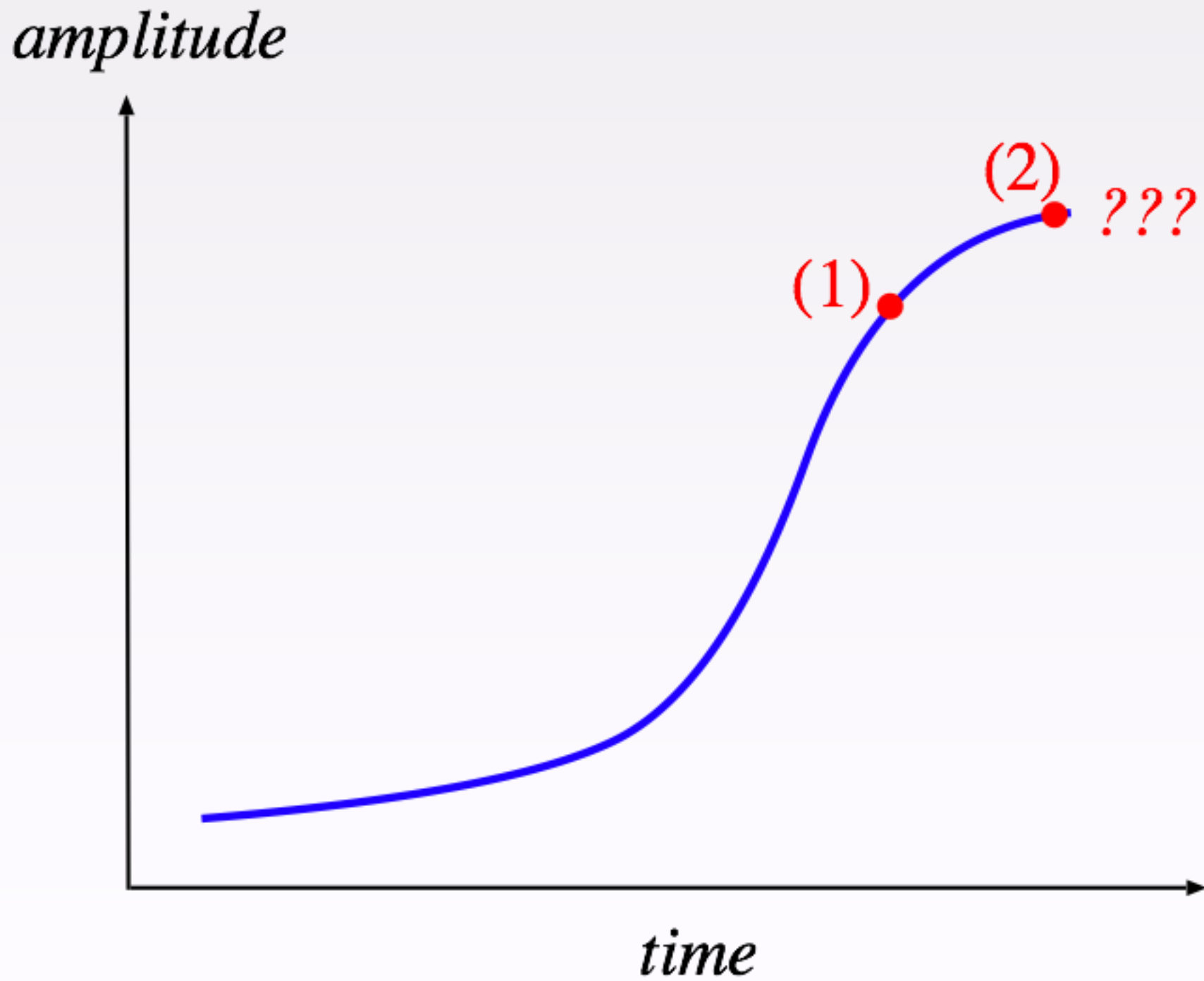
- Sine-Gordon equation

$$\nabla^2 \varphi - \mu^2 \sin \varphi = 0$$

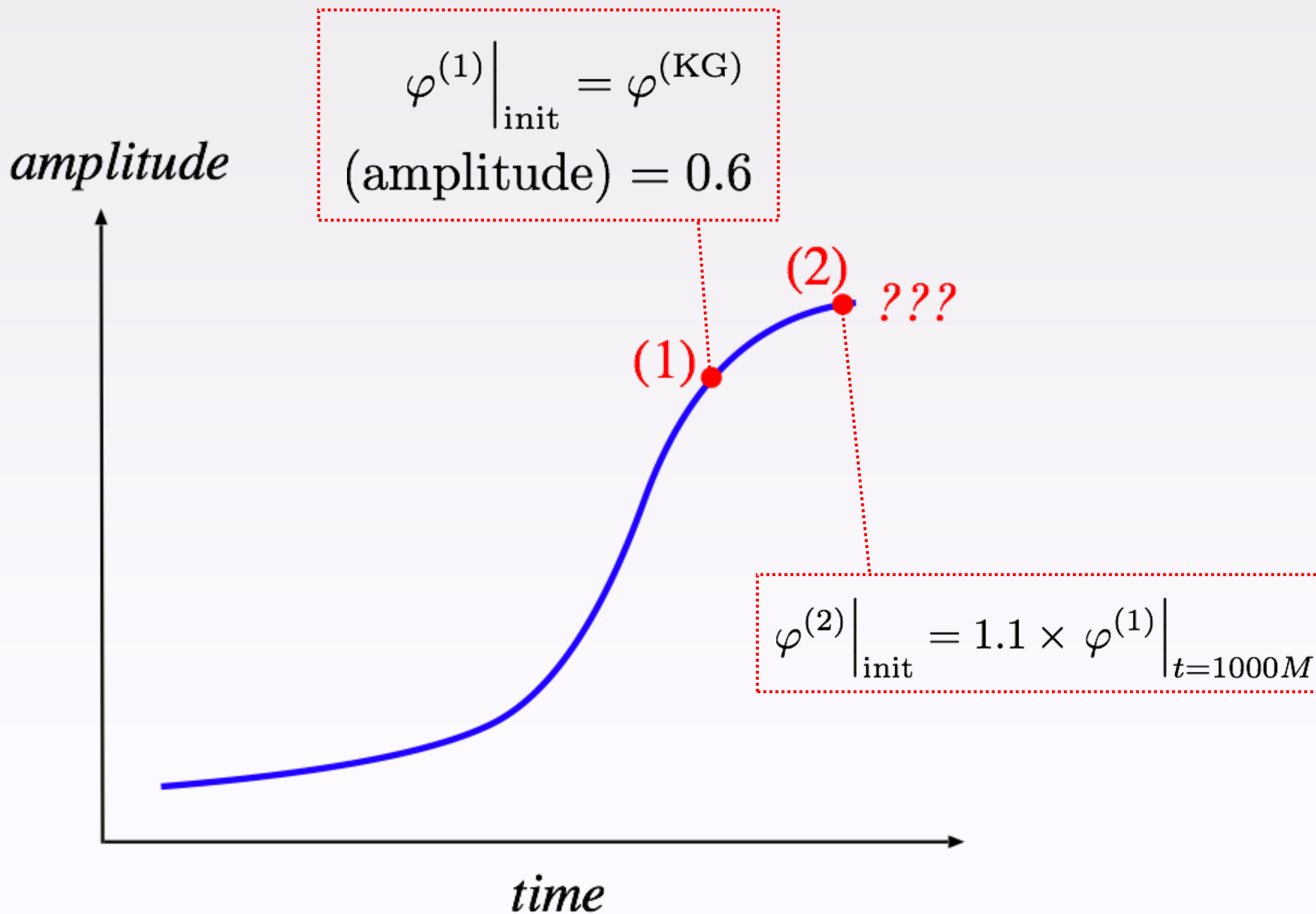
- Setup  $a/M = 0.99, \quad M\mu = 0.4$

- We choose the state of axion cloud that has grown by superradiant instability of  $l = m = 1$  mode.

# Expected evolution

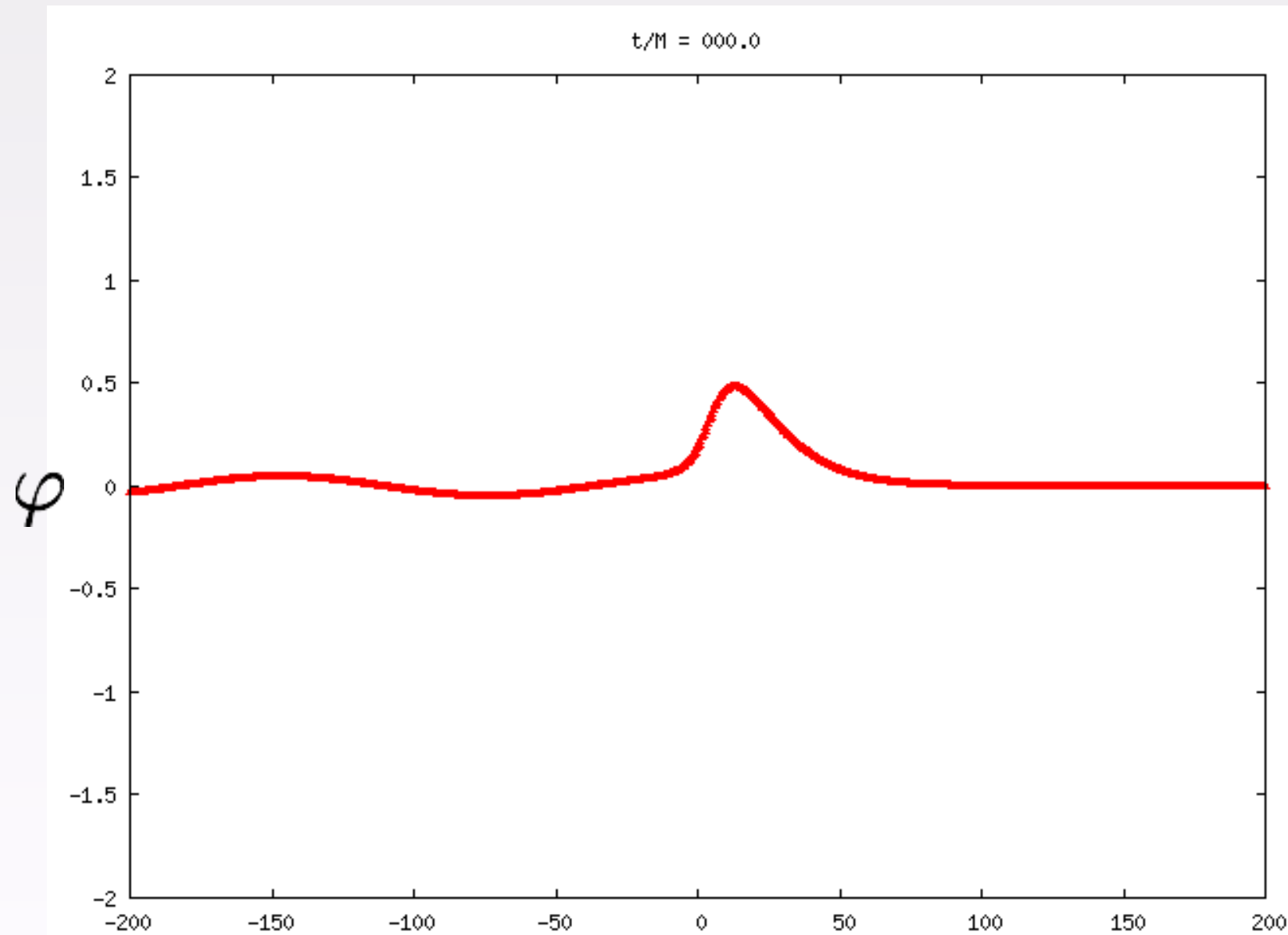


# Expected evolution



# Simulation (1)

- Axion field on equatorial plane ( $\phi = 0$ )



$$-200 \leq r_*/M \leq 200$$

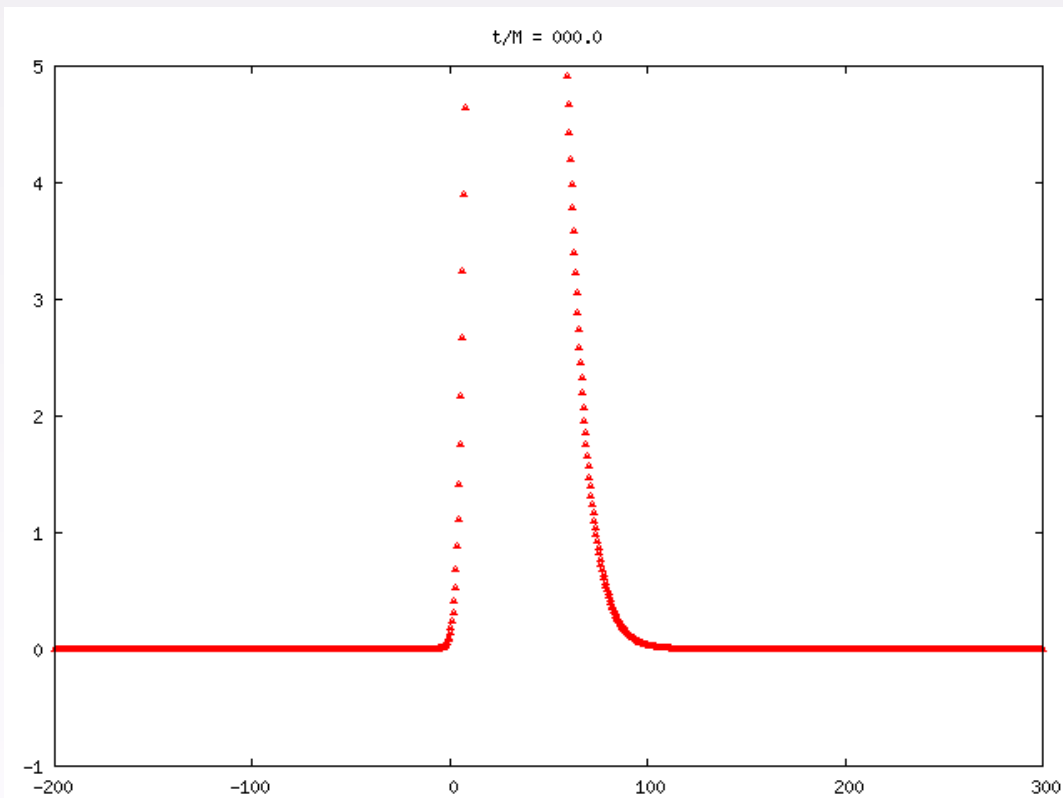
# Simulation (1)

- Energy density with respect to the tortoise coordinate

$$t/M = 0$$

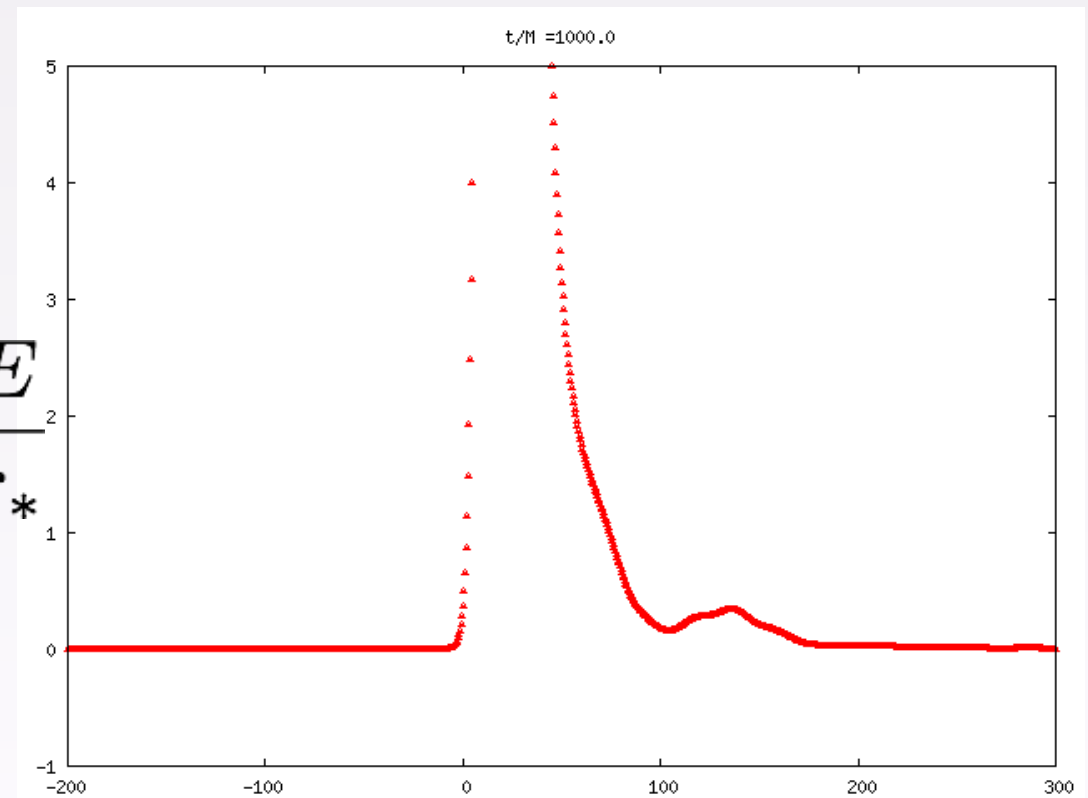
$$t/M = 1000$$

$$\frac{dE}{dr_*}$$



$$-200 \leq r_*/M \leq 300$$

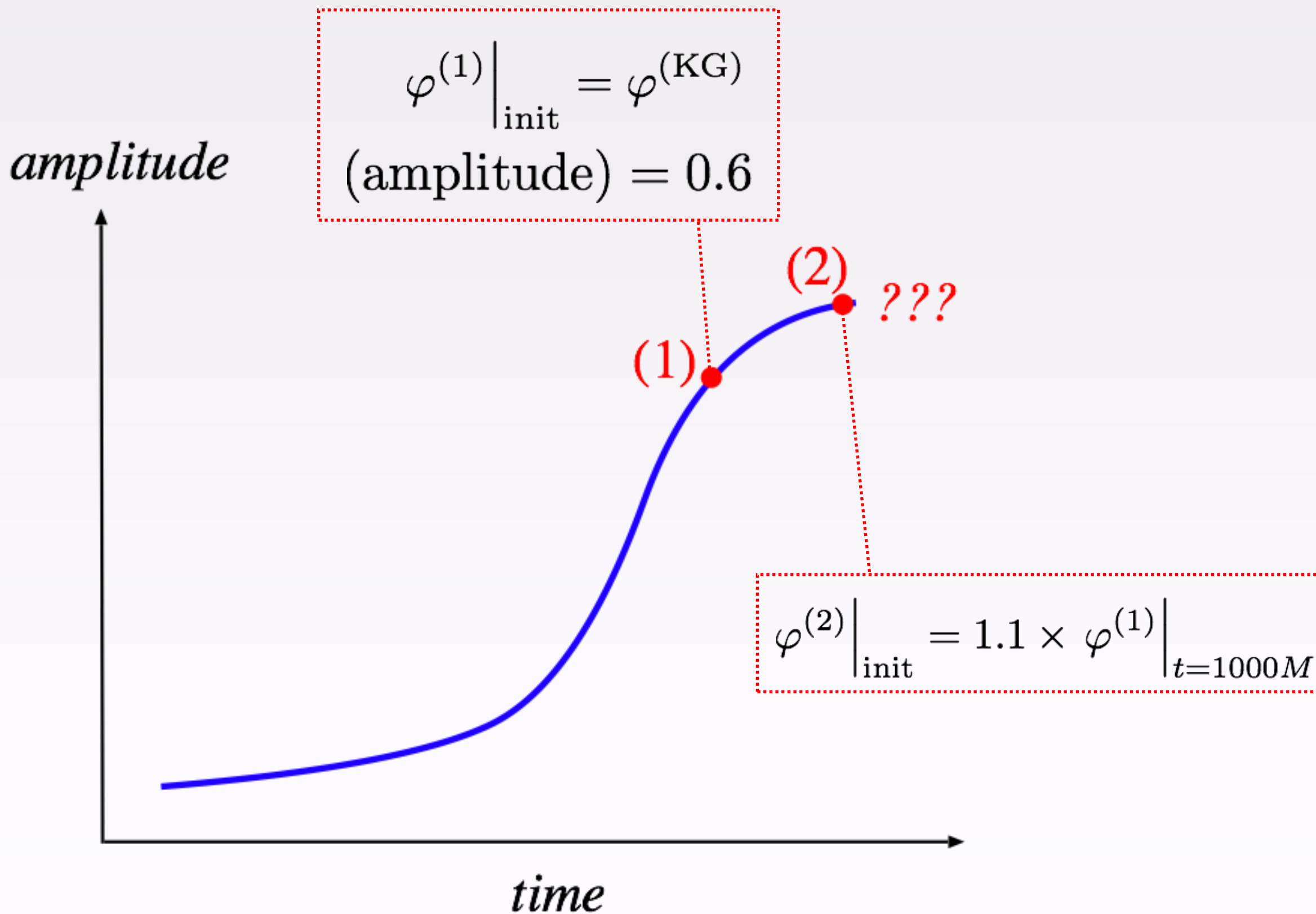
$$\frac{dE}{dr_*}$$



$$-200 \leq r_*/M \leq 300$$

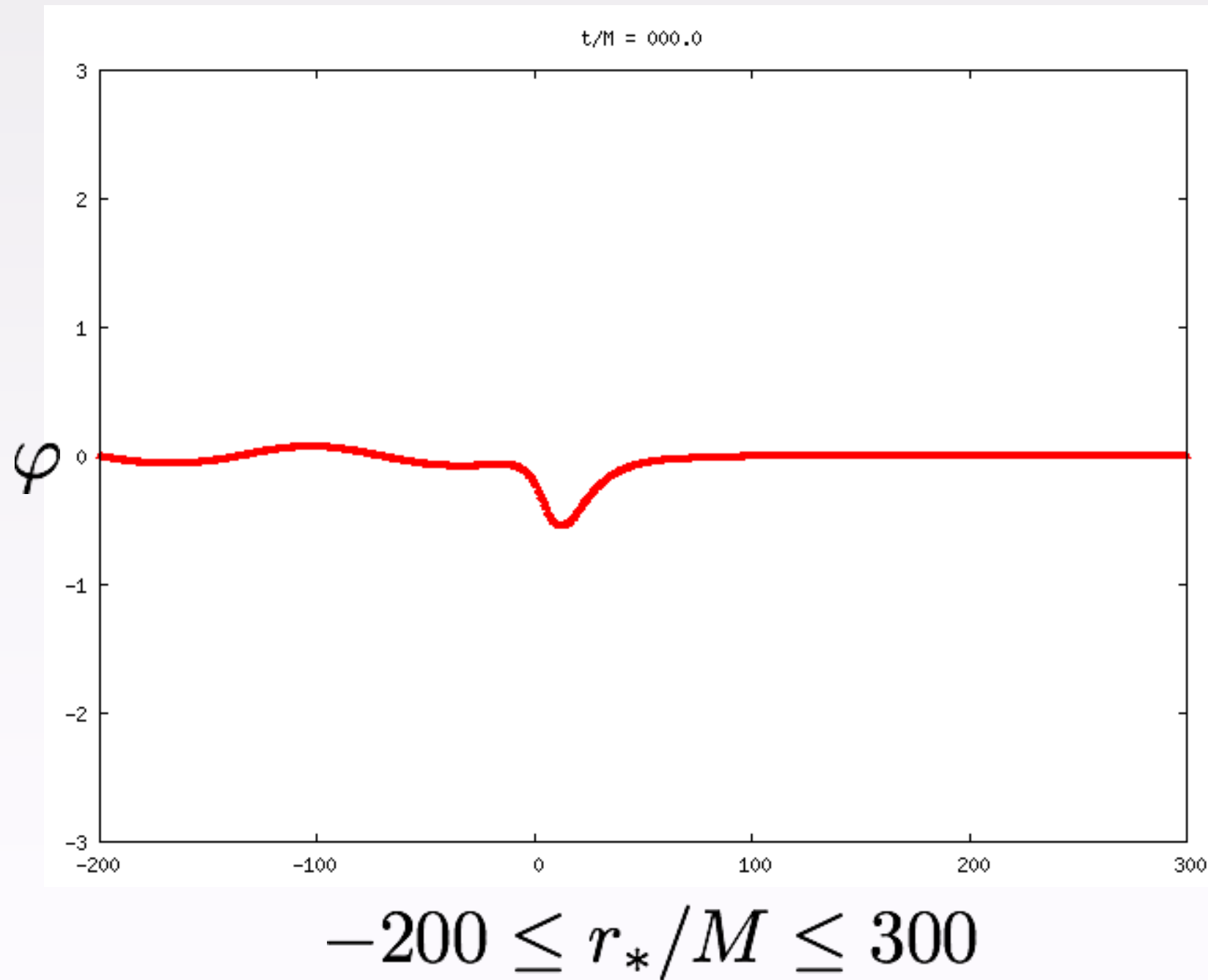


# Expected evolution



## Simulation (2)

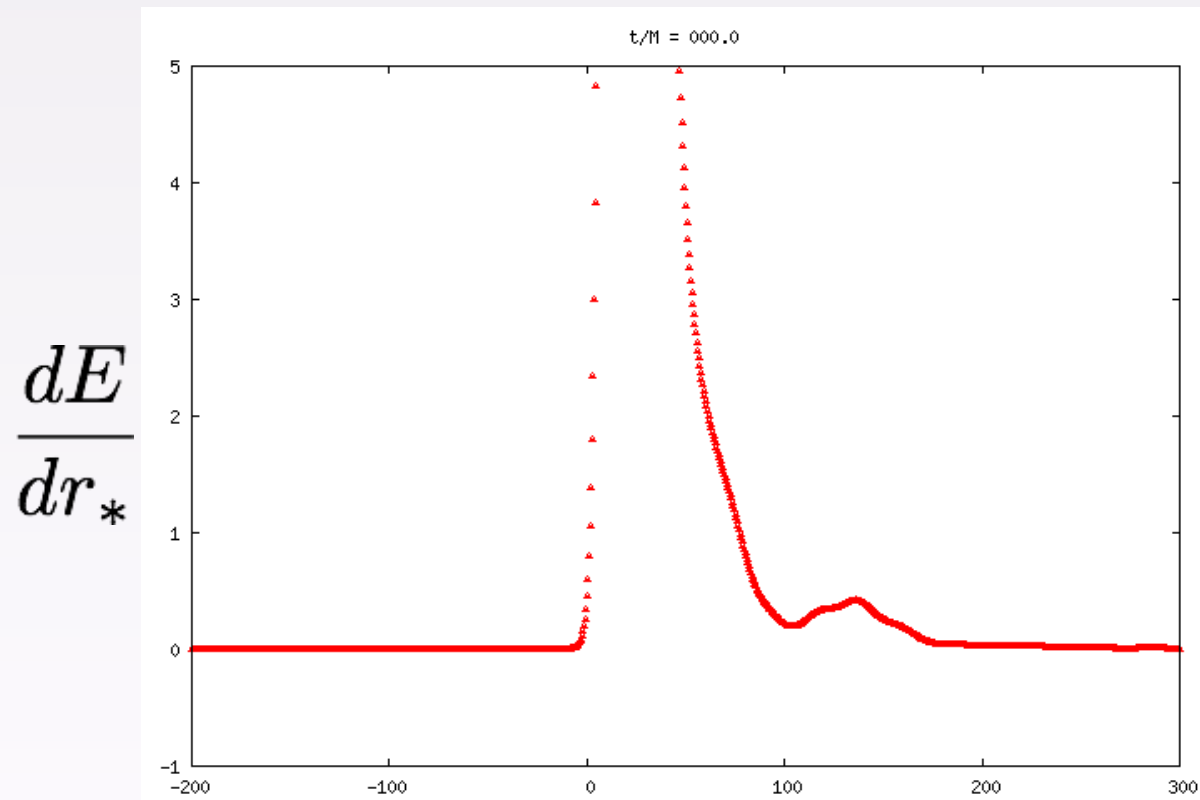
- Axion field on equatorial plane ( $\phi = 0$ )



# Simulation (2)

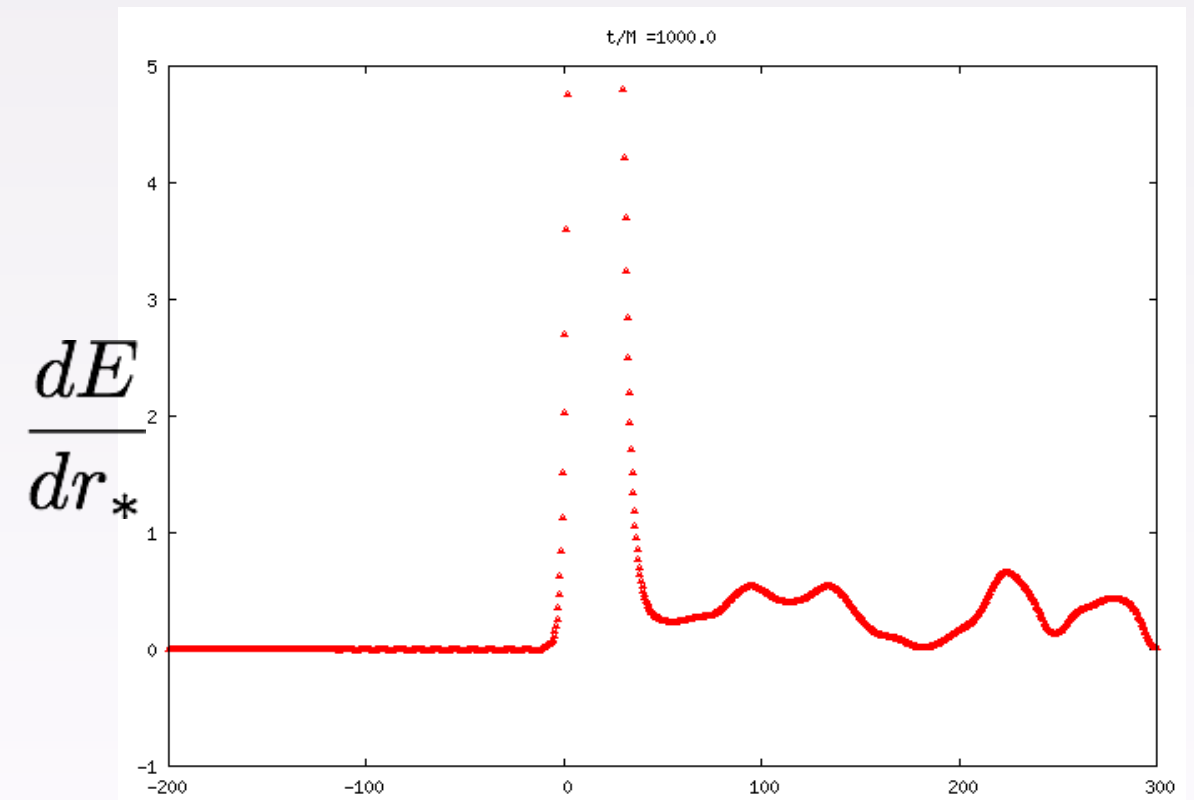
- Energy density with respect to the tortoise coordinate

$$t/M = 0$$



$$-200 \leq r_*/M \leq 300$$

$$t/M = 1000$$



$$-200 \leq r_*/M \leq 300$$

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# Summary

- We developed a reliable code and numerically studied the behaviour of axion field around a rotating black hole.
- When the nonlinear self-interaction becomes relevant, the “bosenova collapse” can be seen, but not very violent.
- The final state of superradiant instability would be a quasi-stationary state.

## Issues for future

- Calculation of the gravitational waves emitted in bosenova.
- The case where axions couple to magnetic fields.