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**Boundary Value Problems
and Symplectic Algebra
for Ordinary Differential
and Quasi-Differential
Operators**

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Contents

Preface	ix
I. Introduction: Fundamental algebraic and geometric concepts applied to the theory of self-adjoint boundary value problems	1
1. Survey of problems, methods, goals: organization of results	1
2. Review of basic definitions and standard results for quasi-differential expressions, and basic concepts of symplectic geometry and symplectic algebra	8
II. Maximal and minimal operators for quasi-differential expressions, and GKN-theory	17
III. Symplectic geometry and boundary value problems	25
1. Symplectic and Lagrangian spaces	25
2. Symplectic geometry applied to boundary value problems	51
IV. Regular boundary value problems	65
V. Singular boundary value problems	79
1. Partition spaces and deficiency indices	79
2. The deficiency index conjecture	85
3. Symplectic invariants of partition and endpoint spaces	90
4. Realizations of deficiency indices: Tabulation of self-adjoint boundary conditions	99
Appendix A. Constructions for quasi-differential operators	109
Appendix B. Complexification of real symplectic spaces, and the real GKN-theory	137
References	179
Notation Index	181
Index	185