

# Broadband MIMO-OFDM Wireless Communications

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**Abstract**—Orthogonal frequency division multiplexing (OFDM) is a popular method for high data rate wireless transmission. OFDM may be combined with antenna arrays at the transmitter and receiver to increase the diversity gain and/or to enhance the system capacity on time-variant and frequency-selective channels, resulting in a multiple-input multiple-output (MIMO) configuration. This paper explores various physical layer research challenges in MIMO-OFDM system design, including physical channel measurements and modelling, analog beam forming techniques using adaptive antenna arrays, space-time techniques for MIMO-OFDM, error control coding techniques, OFDM preamble and packet design, and signal processing algorithms used for performing time and frequency synchronization, channel estimation, and channel tracking in MIMO-OFDM systems. Finally, the paper considers a software radio implementation of MIMO-OFDM.

**Keywords:** OFDM, broadband wireless, multiple-input multiple-output, synchronization, space-time coding, adaptive antennas, software radio

## I. INTRODUCTION

Orthogonal frequency division multiplexing (OFDM) has become a popular technique for transmission of signals over wireless channels. OFDM has been adopted in several wireless standards such as digital audio broadcasting (DAB), digital video broadcasting (DVB-T), the IEEE 802.11a [1] local area network (LAN) standard and the IEEE 802.16a [2] metropolitan area network (MAN) standard. OFDM is also being pursued for dedicated short range communications (DSRC) for road side to vehicle communications and as a potential candidate for the fourth generation (4G) mobile wireless systems.

OFDM converts a frequency selective channel into a parallel collection of frequency flat sub-channels. The subcarriers have the minimum frequency separation required to maintain orthogonality of their corresponding time domain waveforms, yet the signal spectra corresponding to the different subcarriers overlap in frequency. Hence, the available bandwidth is used very efficiently. If knowledge of the channel is available at the transmitter, then the OFDM transmitter can adapt its signaling strategy to match the channel. Due to the fact that OFDM uses a large collection of narrowly spaced subchannels, these adaptive strategies can approach the ideal water pouring capacity of a frequency selective channel. In practice this is achieved by using adaptive bit loading techniques, where

different sized signal constellations are transmitted on the subcarriers.

OFDM is a block modulation scheme where a block of  $N$  information symbols is transmitted in parallel on  $N$  subcarriers. The time duration of an OFDM symbol is  $N$  times larger than that of a single carrier system. An OFDM modulator can be implemented as an inverse discrete Fourier transform (IDFT) on a block of  $N$  information symbols followed by an analog to digital converter (ADC). To mitigate the effects of intersymbol interference (ISI) caused by channel time spread, each block of  $N$  IDFT coefficients is typically preceded by a cyclic prefix (CP) or a guard interval consisting of  $G$  samples, such that the length of the CP is at least equal to the channel length,  $M$ . Under this condition, a linear convolution of the transmitted sequence and the channel is converted to a circular convolution. As a result, the effects of the ISI are easily and completely eliminated. Moreover, the approach enables the receiver to use fast signal processing transforms such as a fast Fourier transform (FFT) for OFDM implementation [3]. Similar techniques can be employed in single carrier systems as well, by preceding each transmitted data block of length  $N$  by a cyclic prefix of length  $G$ , while using frequency domain equalization at the receiver.

Multiple antennas can be used at the transmitter and receiver, an arrangement called a multiple-input multiple-output (MIMO) system. A MIMO system takes advantage of the spatial diversity that is obtained by spatially separated antennas in a dense multipath scattering environment. MIMO systems may be implemented in a number of different ways to obtain either a diversity gain to combat signal fading, or to obtain a capacity gain. Generally there are three categories of MIMO techniques. The first aims to improve the power efficiency by maximizing spatial diversity. Such techniques include delay diversity, space-time block codes (STBC) [4], [5] and space-time trellis codes (STTC) [6]. The second class uses a layered approach to increase capacity. One popular example of such a system is V-BLAST suggested by Foschini *et al.* [7] where full spatial diversity is usually not achieved. Finally, the third type exploits the knowledge of channel at the transmitter. It decomposes the channel coefficient matrix using Singular Value Decomposition (SVD) and uses these decomposed unitary matrices as pre and post filters at the transmitter and the receiver to achieve near capacity [8].

OFDM has been adopted in the IEEE802.11a LAN and IEEE802.16a LAN/MAN standards. OFDM is also being considered in IEEE802.20a, a standard-in-the-making for maintaining high-bandwidth connections to users moving at speeds

This research was supported in part by the Yamacraw Mission, of the State of Georgia, U.S.A., <http://www.yamacraw.org> and in part by the National Science Foundation under Grant CCR-0121565.



up to 60 mph. The IEEE802.11a LAN standard operates at raw data rates up to 54 Mb/s (channel conditions permitting) with a 20 MHz channel spacing, thus yielding a bandwidth efficiency of 2.7 bits/s/Hz. The actual throughput is highly dependent on the medium access control (MAC) protocol. Likewise, IEEE802.16a operates in many modes depending on channel conditions with a data rate ranging from 4.20 Mb/s to 22.91 Mb/s in a typical bandwidth of 6 MHz, translating into a bandwidth efficiency of 0.7 to 3.82 bits/s/Hz. Recent developments in MIMO techniques promise a significant boost in performance for OFDM systems. Broadband MIMO-OFDM systems with bandwidth efficiencies on the order of 10 bits/s/Hz are feasible for LAN/MAN environments. The PHY layer techniques described in this paper are intended to approach 10 bits/s/Hz bandwidth efficiency.

This paper discuss several physical (PHY) layer aspects broadband MIMO-OFDM systems. Section II describes the basic MIMO-OFDM system model. All MIMO-OFDM receivers must perform time synchronization, frequency offset estimation and correction and parameter estimation. This is generally carried out using a preamble consisting of one or more training sequences. Once the acquisition phase is over, receiver goes into the tracking mode. Section III provides an overview of the signal acquisition process and investigates sampling frequency offset estimation and correction in Section IV. The issue of channel estimation is treated in Section V. Section VI considers space-time coding techniques for MIMO-OFDM, while Section VII discusses coding approaches. Adaptive analog beam forming approaches can be used to provide the best possible MIMO link. Section VIII discusses various strategies for beamforming. Section IX very briefly considers medium access control issues. Section X discusses a software radio implementation for MIMO-OFDM. Finally, Section XI wraps up with some open issues concluding remarks.

## II. MIMO-OFDM SYSTEM MODEL

A multicarrier system can be efficiently implemented in discrete time using an Inverse Fast Fourier Transform (IFFT) to act as a modulator and a Fast Fourier Transform (FFT) to act as a demodulator. The transmitted data are the “frequency” domain coefficients and the samples at the output of the IFFT stage are “time” domain samples of the transmitted waveform. Figure 1 shows a typical MIMO-OFDM implementation.

Let  $\mathbf{X} = \{X_0, X_1, \dots, X_{N-1}\}$  denote the length- $N$  data symbol block. The IDFT of the data block  $\mathbf{X}$  yields the time domain sequence  $\mathbf{x} = \{x_0, x_1, \dots, x_{N-1}\}$ , i.e.,

$$x_n = \text{IFFT}_N\{X_k\}(n) \quad (1)$$

To mitigate the effects of channel delay spread, a guard interval comprised of either a cyclic prefix or suffix is appended to the sequence  $\mathbf{X}$ . In case of a cyclic prefix, the transmitted sequence with guard interval is

$$x_n^g = x_{(n)_N}, \quad n = -G, \dots, -1, 0, 1, \dots, N-1 \quad (2)$$

where  $G$  is the guard interval length in samples, and  $(n)_N$  is the residue of  $n$  modulo  $N$ . The OFDM complex envelope is obtained by passing the sequence  $\mathbf{x}^g$  through a pair of

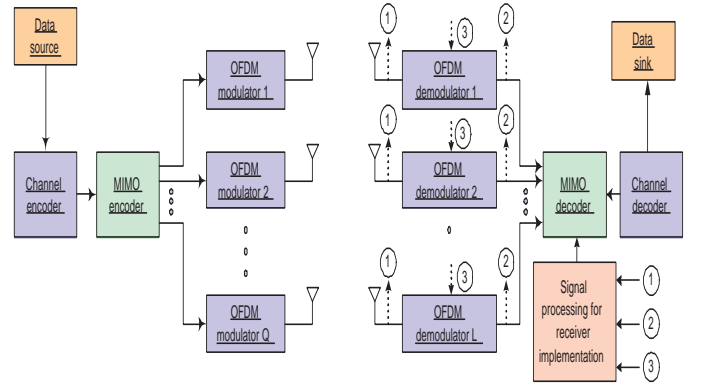
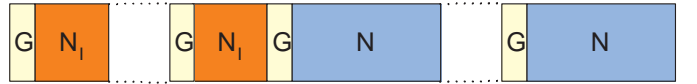


Fig. 1.  $Q \times L$  MIMO-OFDM system, where  $Q$  and  $L$  are the number of inputs and outputs, respectively.

analog-to-digital converters (to generate the real and imaginary components) with sample rate  $1/T$  seconds, and the analog  $I$  and  $Q$  signals are upconverted to an RF carrier frequency. To avoid intersymbol interference (ISI), the cyclic prefix length  $G$  must equal or exceed the length of the discrete-time channel impulse response,  $M$ . The time required to transmit one OFDM symbol,  $T_s = NT + GT$ , is called the OFDM symbol time. The OFDM signal is transmitted over the passband RF channel, received and downconverted to base band. Due to the cyclic prefix, the discrete linear convolution of the transmitted sequence with the channel impulse response becomes a circular convolution. Hence, at the receiver the initial  $G$  samples from each received block are removed, followed by an  $N$ -point discrete Fourier transform (DFT) on the resulting sequence.

Antenna 1



Antenna Q

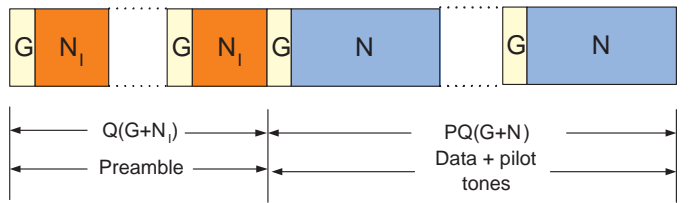


Fig. 2. Frame structure for the  $Q \times L$  OFDM system.

The frame structure of a typical MIMO-OFDM system is shown in Fig. 2. The OFDM preamble consists of  $Q$  training symbols of length  $N_I + G$ , where  $G \leq N_I \leq N$ ,  $N_I = N/I$  and  $I$  an integer that divides  $N$ . Often the length of the guard interval in the training period is doubled, for example in IEEE802.16a [1], to aid in synchronization, frequency offset estimation and equalization for channel shortening in cases where the length of the channel exceeds the length of the



guard interval.

First consider the preamble portion of the OFDM frame. The length- $N_I + G$  preamble sequences are obtained by exciting every  $I$ th coefficient of a length- $N$  frequency domain vector with a non-zero training symbol from a chosen alphabet (the remainder are set to zero). The frequency domain training sequences transmitted from the  $i$ th antenna are  $\{S_k^{(q)}\}_{k=1}^N$ , where  $q = (c-1)Q + i$  and  $c = 1, 2, \dots, Q$ . The individual length- $N_I$  time domain training sequences are obtained by taking an  $N$ -point IDFT of the sequence  $\{S_k^{(q)}\}_{k=1}^N$ , keeping the first  $N_I$  time-domain coefficients and discarding the rest. A cyclic prefix is appended to each length- $N_I$  time-domain sequence. Let  $\mathbf{H}_{ij}$  be the vector of sub-channel coefficients between the  $i$ th transmit and the  $j$ th receive antenna and let  $\{R_k^{(l)}\}_{k=0}^{N_I-1}$  be the received sample sequence at the  $l$ th receiver antenna. After removing the guard interval, the received samples  $\{R_k^{(l)}\}_{k=0}^{N_I-1}$  are repeated  $I$  times and demodulated using an  $N$ -point FFT as

$$R_k^{(l)} = \text{FFT}_N\{r^{(l)}\}(k) \quad (3)$$

$$= \sum_{q=1}^Q H_k^{(q,l)} S_k^{(q)} + W_k^{(l)} \quad (4)$$

where  $k = 0, \dots, N-1$ . The demodulated OFDM sample matrix  $\mathbf{R}_k$  of dimension  $(Q \times L)$  for the  $k$ th subcarrier can be expressed in terms of the transmitted sample matrix  $\mathbf{S}_k$  of dimension  $(Q \times Q)$ , the channel coefficient matrix  $\mathbf{H}_k$  of dimension  $(Q \times L)$  and the additive white Gaussian noise matrix  $\mathbf{W}_k$  of dimension  $(Q \times L)$  [24] as

$$\mathbf{R}_{k,Q \times L} = \mathbf{S}_{k,Q \times Q} \cdot \mathbf{H}_{k,Q \times L} + \mathbf{W}_{k,Q \times L} \quad (5)$$

where  $\mathbf{R}$ ,  $\mathbf{H}$  and  $\mathbf{W}$  can be viewed as either a collection of  $N$  matrices of dimension  $Q \times L$ , or as a collection of  $Q \times L$  vectors of length  $N$ .

#### A. Preamble Design for MIMO OFDM Systems

Least square channel estimation schemes require that all  $Q \times N_I$  training symbol matrices  $\mathbf{S}^{(q)}$ ,  $q = (c-1)Q + k$ ,  $k = 1, \dots, N_I$  be unitary so that only  $Q$  OFDM symbols are needed for channel estimation [25]. A straight forward solution is to make each  $\mathbf{S}_k$  a diagonal matrix. However, the power of the preamble needs to be boosted by  $10 \log_{10} Q$  dB in order to achieve a performance similar to the case when the preamble signal is transmitted from all the antennas. This has the undesirable effect of increasing the dynamic range requirements of the power amplifiers. Hence, methods are required so that sequences can be transmitted from all the antennas while still having unitary  $\mathbf{S}_k$  matrices. One approach adapts the work by Tarokh *et al.* on space-time block codes [5], [26]. For  $Q = 2, 4$  and  $8$ , orthogonal designs exist. For example, for  $Q = 2$  and  $4$  we can choose the preamble structures of the form

$$\mathbf{S}_{AS} = \begin{bmatrix} \mathbf{S}_1 & \mathbf{S}_1 \\ -\mathbf{S}_1 & \mathbf{S}_1 \end{bmatrix}, \quad (6)$$

$$\mathbf{S}_{TS} = \begin{bmatrix} \mathbf{S}_1 & \mathbf{S}_1 & \mathbf{S}_1 & \mathbf{S}_1 \\ -\mathbf{S}_1 & \mathbf{S}_1 & -\mathbf{S}_1 & \mathbf{S}_1 \\ -\mathbf{S}_1 & \mathbf{S}_1 & \mathbf{S}_1 & -\mathbf{S}_1 \\ -\mathbf{S}_1 & -\mathbf{S}_1 & \mathbf{S}_1 & \mathbf{S}_1 \end{bmatrix}, \quad (7)$$

where  $\mathbf{S}_1$  is the length- $N_I$  vector  $S_k$ ,  $k = 1 \dots N_I$ . This results in unitary  $\mathbf{S}_k$  matrices. As it turns out, transmitting the same sequence from all the antennas in this fashion is advantageous when performing synchronization. A similar structure for  $Q = 8$  exists. For other values of  $Q$ , a LS solution for the channel estimates can be obtained by either transmitting more than  $Q$  training sequences, or by making the training symbol matrices unitary by using a Gram Schmidt orthonormalization procedure as described in [24].

#### B. Pilot insertion

Channel coefficients require constant tracking. This is aided by inserting known pilot symbols at fixed or variable sub-carrier positions. For example, the IEEE 802.16a standard recommends the insertion of 8 pilot tones at fixed positions on subcarriers [12, 36, 60, 84, 172, 196, 220, 244] (assuming  $N = 256$ ). Fig. 3 shows the method for generating the pilot sequences used in the IEEE 802.16a standard. In the downlink (DL) and the uplink (UL), the shift register is initialized with sequences as shown. A '0' at the output  $P_n$  is mapped to +1 and a '1' is mapped to -1. For a MIMO system with  $Q = 2$  and 4 antennas, the pilot sequences  $p_n$  can be coded over space and time to form structures in (6) and (7), respectively, thereby admitting a simple least squares channel estimate. For more information on the pilot sequence construction, readers can refer to [27].

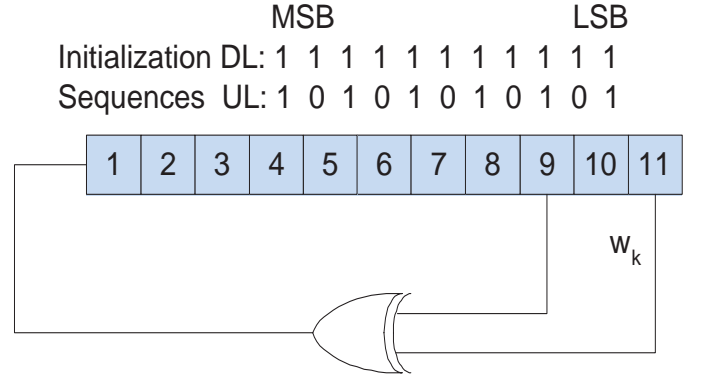


Fig. 3. Pilot tone generation.

### III. SYNCHRONIZATION IN THE ACQUISITION MODE

Time and frequency synchronization can be performed sequentially in the following steps [28].

*Step I: Coarse Time Synchronization and Signal Detection* - Coarse time acquisition and signal detection locates the start of an OFDM frame over an approximate range of sample values. Due to the presence of the cyclic prefix (or suffix), coarse time acquisition during the preamble can be performed by



correlating the received samples that are at a distance of  $N_I$  from each other over a length- $G$  window ([25], [29]), viz.

$$n_{j,\text{coarse}} = \arg \max_n \{\phi_{j,n}\}. \quad (8)$$

where  $\phi_{j,n} = \sum_{k=0}^{G-1} (r_{j,n+k}^* \cdot r_{j,n+k+N_I})$ . In addition to maximizing  $\phi_{j,n}$ , it should also exceed a certain threshold to reduce the probability of false alarm ( $P_{\text{FA}}$ ). We chose the threshold to be 10% of the incoming signal energy of the correlation window.

*Step II: Frequency Offset Estimation in the Time Domain-* Any frequency offset between the transmitter and the receiver local oscillators is reflected in the time domain sequence as a progressive phase shift  $\theta = 2\pi\gamma N_I/N$ , where  $\gamma$  is the frequency offset and is defined as the ratio of the actual frequency offset to the inter-carrier spacing. A frequency offset estimate of up to  $\pm I/2$  subcarrier spacings can be obtained based on the phase of the autocorrelation function in (8) as follows:

$$\hat{\gamma}_j = \frac{I}{2\pi} \angle \{\phi_{n_{j,\text{coarse}}}\}, \quad (9)$$

where  $n_{j,\text{coarse}}$  is the optimum coarse timing acquisition instant and  $I = N/N_I$ . The frequency offset can then be removed from the received sample sequence by multiplying it with  $\exp\{-j2\pi\hat{\gamma}_j n/N_I\}$  during the preamble and  $\exp\{-j2\pi\hat{\gamma}_j n/N\}$  during the data portion. Note that by reducing the length of the training symbol by a factor of  $I$ , the range of the frequency offset estimate in the time domain can be increased by a factor of  $I$ .

*Step III: Residual Frequency Offset Correction* - Should the range of the time domain frequency offset estimation be insufficient, frequency domain processing can be used. Suppose that the same frequency domain training sequence  $\{S_k^{(q)}\}_{k=1}^N$  is transmitted from all the antennas. The residual frequency offset, that is an integer multiple of the subcarrier spacing, can be estimated by computing a cyclic cross-correlation of  $\{S_k^{(q)}\}_{k=1}^N$  with the received, frequency corrected (from Step II), demodulated symbol sequence, viz.,

$$\chi_k = \sum_{n=0}^{N-1} S_k^{(q)*} (r_{k+n}^{(1)})^c R_n^{(1)c} \quad k = 0, 1, \dots, N-1, \quad (10)$$

where

$$R_n^{(1)c} = \text{FFT}_N \left\{ r_n^{(1)} e^{j2\pi\hat{\gamma}_{\text{ML}} n/N_I} \right\}. \quad (11)$$

The residual frequency offset is estimated as  $\hat{\Gamma} = \arg \max_k \{|\chi_k|\}$ ,  $k = 0, 1, \dots, N-1$ . Note that the fractional part of the relative frequency offset is estimated in the time domain in Step II while the integer part is estimated in the frequency domain in Step III.

*Step IV: Fine Time Synchronization* - Fine time acquisition locates the start of the useful portion of the OFDM frame to within a few samples. Once the frequency offset is removed, fine time synchronization can be performed by cross-correlating the frequency corrected samples with the

transmitted preamble sequences. The fine time synchronization metric is

$$n_{j,\text{fine}} = \arg \max_n \{\psi_{j,n}\}, \quad (12)$$

where  $\psi_{j,n} = \sum_{q=1}^Q \left| \sum_{k=0}^{N_I-1} (s_{q,k}^* \cdot r_{j,n+k}) \right|$ . For systems using 2 and 4 and 8 transmit antennas using the orthogonal designs discussed earlier = only one cross correlator is needed per receiver antenna. Once again the threshold is set at 10% of the energy contained in  $N_I$  received samples. Since fine time synchronization is computationally expensive process, it is carried out for a small window centered around the coarse time synch. instant  $n_{j,\text{coarse}}$ .

Finally the net time synchronization instant for the entire receiver is selected to be  $n_{\text{opt}} = \frac{1}{L} \sum_{j=1}^L n_{j,\text{fine}}$ . An added negative offset of a few samples is applied to the fine time synchronization instant in order to ensure that the OFDM windows for all the receivers falls into an ISI free zone.

#### A. Example

Consider a  $2 \times 2$  and a  $4 \times 4$  broadband MIMO-OFDM system [2] operating at a carrier frequency of 5.8 GHz on the SUI-4 channel shown below. The OFDM signal occupies a bandwidth of 4.0 MHz. The uncorrected frequency offset ( $\Gamma + \gamma$ ) is 1.25 subcarrier spacings. The OFDM blocksize is

TABLE I  
SUI-4 CHANNEL MODEL

	Tap 1	Tap 2	Tap 3	Units
Delay	0	1.5	4.0	$\mu\text{s}$
Power (omni ant.)	0	-4	-8	dB
Doppler $f_m$	0.2	0.15	0.25	Hz

$N = 256$ , and the guard interval is kept at  $N/4 = 64$ . Out of 256 tones, the dc tone and 55 other tones at the band edges are set to zero. Hence, the number of used tones  $N_u = 200$ . The length of the sequences used in the preamble is varied from  $N$  to  $N/2$  to  $N/4$ . The preamble insertion period,  $P$ , is chosen to be 10. STBCs are used to encode the data. For a  $2 \times 2$  system, the Alamouti STBC is used with code rate 1, whereas for a  $4 \times 4$  system, code rate is  $3/4$  [26]. In the data mode, each of the tones is modulated using a 16-QAM constellation and no channel coding is employed. Least squares channel estimates obtained using the preamble are used to process the entire frame [28]. For training sequences of length  $N_I < N$ , frequency domain linear interpolation and extrapolation are used. Afterwards, frequency domain smoothing is used, such that channel estimates at the band-edges are kept as they are, whereas all the other channel estimates are averaged using

$$\hat{H}_k^{(q,j)} = \frac{\bar{H}_{k-1}^{(q,j)} + \bar{H}_{k+1}^{(q,j)}}{2}. \quad (13)$$

Figure 4 shows the coarse and fine time synchronization performance for a  $4 \times 4$  MIMO-OFDM system with  $N_I = 128$ ,  $I = 2$ , and signal-to-noise ratio (SNR) of 10 dB.



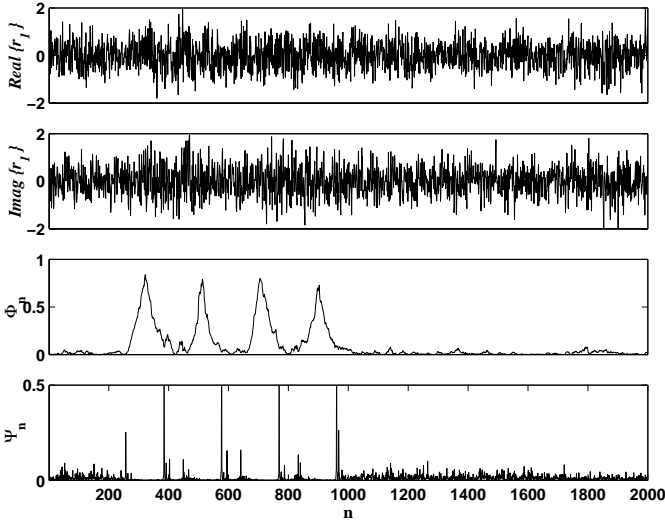


Fig. 4. Coarse and fine time synchronization for a  $4 \times 4$  system with  $N_I = 128$ , SNR=10 dB, freq. off.  $\Gamma + \gamma = 1 + 0.25$ . Steps IB, IIIB.

Figure 5 shows the overall bit error rate (BER) performance of a  $2 \times 2$  MIMO-OFDM system using the suggested algorithms.

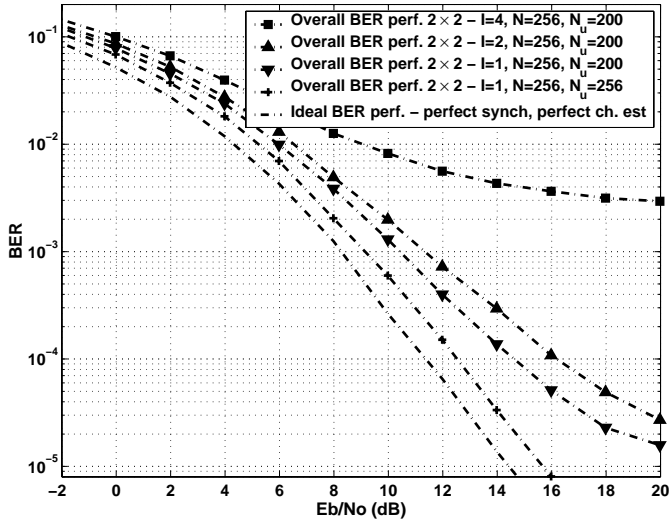


Fig. 5. Uncoded BER as a function of SNR for a  $2 \times 2$  system using 16-QAM modulation,  $P = 10$ .

#### IV. SAMPLE FREQUENCY OFFSET CORRECTION AND TRACKING

MIMO-OFDM schemes that use coherent detection need accurate channel estimates. Consequently, the channel coefficients must be tracked in a system with high Doppler. In the broadband fixed wireless access (BFWA) system IEEE 802.16a, the channel is nearly static. However, channel variations are still expected due to the presence of sampling frequency offset between transmitter and the receiver RF oscillators. Generally the components in the customer premises equipment (CPE) have a low tolerance with typical drift of 20 parts per million (ppm). This means a signal with a BW of 4

MHz produces an offset of 80 samples for every one second of transmission. Sample frequency offset causes phase rotation, amplitude distortion and loss in synchronization.

Even after successful signal acquisition and synchronization, the OFDM system must guard against sample frequency offset (SFO) and phase offset. It must also guard against drift in the RF local oscillator and sampling clock frequency with time [30].

Let  $T' \neq T$  be the sampling time at the receiver and let  $\beta = (T' - T)/T$  be the normalized offset in the sampling time. The received and demodulated OFDM symbol with the sampling time offset can be approximated by

$$R_{g,k}^{(l)} = \sum_{q=1}^Q \exp \{j2\pi\beta gk(N+G)/N\} \text{sinc}(\beta k) \times H_{q,k}^{(l)} S_k^{(q)} + W_{k,\text{AWGN}}^{(l)} + W_{k,\text{ICI}} \quad (14)$$

where  $k = 0, \dots, N-1$ ,  $l = (j-1)Q + g$  and  $g = 1, 2, \dots, Q$  is the running index of the OFDM symbol in time, and  $\text{sinc}(x) = \sin(\pi x)/\pi x$ .

Due to the sampling frequency offset  $\beta$ , the received demodulated symbol suffers phase rotation as well as amplitude distortion. In general, the value of  $\beta$  is very small. For example, for a sampling clock tolerance of 20 ppm and sampling frequency  $f_s = 8$  MHz,  $\beta = 2 \times 10^{-5}$ . Hence,  $\text{sinc}(k\beta) \approx 1$  and its effect is negligible. With this assumption, the demodulated OFDM sample matrix  $\mathbf{R}_k$  in (5) becomes

$$\mathbf{R}_{k,Q \times L} = \mathbf{\Lambda}_{k,Q \times Q} \cdot \mathbf{S}_{k,Q \times Q} \cdot \mathbf{H}_{k,Q \times L} + \mathbf{W}_{k,Q \times L}. \quad (15)$$

where  $\mathbf{\Lambda}_{k,Q \times Q}$  is diagonal matrix representing the phase rotations of the received demodulated samples due to the presence of sampling frequency offset.

##### A. Sample Frequency Offset Estimation

If the MIMO OFDM transmission is being carried out in blocks of  $Q$  OFDM symbols, then phase rotation between consecutive blocks of OFDM symbols increases in a linear fashion. Hence let the received sample matrix corresponding to the preamble be given by

$$\mathbf{R}_k^{\text{preamble}} = \mathbf{\Lambda}_k^{\text{preamble}} \cdot \mathbf{S}_k^{\text{preamble}} \cdot \mathbf{H}_k + \mathbf{W}_k. \quad (16)$$

The received sample matrix for the next block of  $Q$  OFDM symbols corresponding to the pilot tones is then given by

$$\mathbf{R}_k^{\text{p}} = \exp \{j2\pi Qk\beta(N+G)/N\} \times \mathbf{\Lambda}_k^{\text{preamble}} \cdot \mathbf{S}_k^{\text{p}} \cdot \mathbf{H}_k + \mathbf{W}_k. \quad (17)$$

If the channel does not change much for  $2Q$  consecutive blocks of OFDM symbols as is the case for wireless LAN/MAN applications, then we can correlate  $\mathbf{R}_k^{\text{preamble}}$  and  $\mathbf{R}_k^{\text{p}}$  to obtain an initial estimate of  $\beta$  per subcarrier as

$$\begin{aligned} \hat{\beta}_k^{\text{initial}} &= \frac{\angle \text{trace}[\mathbf{R}_k^{\text{H preamble}} \mathbf{R}_k^{\text{p}}]}{2\pi Qk(N+G)/N} \\ &= \frac{\angle \sum_{l=1}^L |R_{l,l}|^2 \exp \{j2\pi\beta Qk(N+G)/N\}}{2\pi Qk(N+G)/N} \end{aligned} \quad (18)$$

This estimate of the sampling frequency offset estimate is then averaged over all the sub-carriers.



### B. Channel Estimation

Once initial estimates of  $\beta$  are obtained, channel estimation can be carried out using the Least Squares (LS) technique as

$$\hat{\mathbf{H}}_k = \mathbf{B}_k^H (\mathbf{B}_k \mathbf{B}_k^H)^{-1} \mathbf{R}_k, \quad (19)$$

where  $\mathbf{B}_k = \mathbf{\Lambda}_k \mathbf{S}_k$ . This ensures that the initial effect of the sampling frequency offset is taken into account when the channel is estimated. More elaborate channel estimation schemes are considered in the Section V.

### C. Sampling Frequency Offset Tracking

Once initial estimates of  $\beta$  are obtained, open loop sampling frequency offset estimation is obtained by minimizing the metric

$$\min (\text{trace} [(\mathbf{R}_k - \mathbf{\Lambda}_k \mathbf{C}_k^p)^H (\mathbf{R}_k - \mathbf{\Lambda}_k \mathbf{C}_k^p)]), \quad (20)$$

where  $\mathbf{C}_k^p = \mathbf{S}_k^p \mathbf{H}_k$ . This results in the LS solution of the type

$$\hat{\mathbf{\Lambda}}_k = \mathbf{R}_k \mathbf{C}_k^{pH} (\mathbf{C}_k^p \mathbf{C}_k^{pH} + \delta \mathbf{I})^{-1}, \quad (21)$$

where  $\delta$  is a small number of the order of  $1 \times 10^{-5}$  introduced to guard against ill-conditioned matrices and  $\mathbf{I}$  is the identity matrix. If the variance of the noise at the receiver is known then this factor can be applied instead of  $\delta$ . From  $\hat{\mathbf{\Lambda}}_k$ , the new value of sampling frequency offset may be extracted by correlating the diagonal elements of the  $\hat{\mathbf{\Lambda}}_k$  matrix as

$$\hat{\beta}_k^{\text{new}} = \frac{\angle \left\{ \sum_{q=1}^{Q-1} \hat{\mathbf{\Lambda}}_{q,q,k}^* \hat{\mathbf{\Lambda}}_{q+1,q+1,k} \right\}}{2\pi k(N+G)/N}. \quad (22)$$

The new value of  $\hat{\beta}_k^{\text{new}}$  is then passed through a first order low pass filter and the output of the filter is used to obtain the filtered estimate of  $\beta$ . This then is used to form the new estimate  $\hat{\mathbf{\Lambda}}_k^{\text{new}}$ . The sampling frequency offset in the tracking mode is then compensated for as  $\hat{\mathbf{R}}_k^{\text{new}} = (\hat{\mathbf{\Lambda}}_k^{\text{new}})^{-1} \mathbf{R}_k$ .

### D. Example

Simulations are carried out for the same  $4 \times 4$  broadband fixed wireless access system described in Section III. The sampling frequency offset  $\beta$  is 10 parts per million (ppm) and is allowed to vary around that value in a random walk. Hence  $\beta = 10\text{ppm} + \mathcal{N}(0, 1/10^6\text{ppm})$ . Figure 6 shows the BER results. The bottom curve is the ideal results with perfect synchronization and channel estimation and zero sampling frequency offset. The next curve up shows the performance with synchronization and channel estimation, but without any sampling frequency offset present in the system. The next curve up shows the performance with synchronization, channel estimation, and sample frequency offset correction. The top curve shows the performance when an uncorrected sample frequency offset is present.

## V. MIMO-OFDM CHANNEL ESTIMATION

Channel state information is required in MIMO-OFDM for space-time coding at the transmitter and signal detection at receiver. Its accuracy directly affects the overall performance of MIMO-OFDM systems. In this section, we present several approaches for MIMO-OFDM channel estimation.

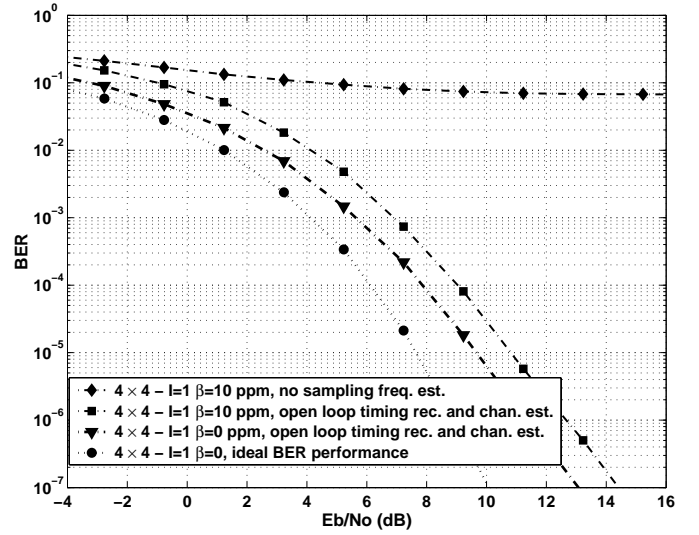


Fig. 6. BER performance for a  $4 \times 4$  system with  $\beta = 0$  and 10 ppm, with frame length of 80 OFDM symbols.

### A. Basic Channel Estimation

Channel estimation for OFDM can exploit time and frequency correlation of the channel parameters. A basic channel estimator has been introduced in [31].

As discussed before, for a MIMO system with  $Q$  transmit antennas, the signal from each receive antenna at the  $k$ th subchannel of the  $n$ th OFDM block can be expressed as<sup>1</sup>,

$$R_{n,k} = \sum_{q=1}^Q H_{n,k}^{(q)} X_{n,k}^{(q)} + W_{n,k},$$

where  $H_{n,k}^{(q)}$  is the channel frequency response at the  $k$ th subchannel of the  $n$ th OFDM block corresponding to the  $q$ th transmit antenna, and  $W_{n,k}$  is the additive white Gaussian noise. The challenge with MIMO channel estimation is that each received signal corresponds to several channel parameters.

Since the channel response at different frequencies is correlated, channel parameters at different subcarriers can be expressed as

$$H_{n,k}^{(q)} = \sum_{m=0}^{N_o-1} h_{n,m}^{(q)} W_N^{km}, \quad (23)$$

for  $k = 0, 1, \dots, N-1$  and  $q = 1, \dots, Q$ . The parameter  $N_o$  depends on the ratio of the delay span of wireless channels and the OFDM symbol duration, and  $W_N = \exp(-j\frac{2\pi}{N})$ . Hence, to obtain  $H_{n,k}^{(q)}$ , we only need to estimate  $h_{n,m}^{(q)}$ .

If the transmitted signals,  $X_{n,k}^{(q)}$  from the  $q$ th transmit antenna are known for  $q = 1, \dots, Q^2$ , then  $\tilde{h}_{n,m}^{(q)}$ , a temporal estimation of  $h_{n,m}^{(q)}$ , can be found by minimizing the following

<sup>1</sup> We omit the index for receive antenna here since channel estimation for each receive antenna is performed independently.

<sup>2</sup> During the training period, transmitted signals are known to the receiver; In the data transmission mode, a decision-directed approach can be used



cost function,

$$\sum_{k=0}^{N-1} \left| R_{n,k} - \sum_{q=1}^Q \sum_{m=0}^{N_o-1} \tilde{h}_{n,m}^{(q)} W_K^{km} x_{n,k}^{(q)} \right|^2. \quad (24)$$

Direct calculation in [31] yields

$$\begin{pmatrix} \mathbf{A}_n^{(11)} & \dots & \mathbf{A}_n^{(Q1)} \\ \vdots & \dots & \vdots \\ \mathbf{A}_n^{(1Q)} & \dots & \mathbf{A}_n^{(QQ)} \end{pmatrix} \begin{pmatrix} \tilde{\mathbf{h}}_n^{(1)} \\ \vdots \\ \tilde{\mathbf{h}}_n^{(Q)} \end{pmatrix} = \begin{pmatrix} \mathbf{b}_n^{(1)} \\ \vdots \\ \mathbf{b}_n^{(Q)} \end{pmatrix}, \quad (25)$$

or

$$\begin{pmatrix} \tilde{\mathbf{h}}_n^{(1)} \\ \vdots \\ \tilde{\mathbf{h}}_n^{(Q)} \end{pmatrix} = \begin{pmatrix} \mathbf{A}_n^{(11)} & \dots & \mathbf{A}_n^{(Q1)} \\ \vdots & \dots & \vdots \\ \mathbf{A}_n^{(1Q)} & \dots & \mathbf{A}_n^{(QQ)} \end{pmatrix}^{-1} \begin{pmatrix} \mathbf{b}_n^{(1)} \\ \vdots \\ \mathbf{b}_n^{(Q)} \end{pmatrix}, \quad (26)$$

where  $\tilde{\mathbf{h}}_n^{(q)}$  is the temporal estimation of channel parameter vector, defined as

$$\tilde{\mathbf{h}}_n^{(q)} = \left( \tilde{h}_{n,0}^{(q)}, \dots, \tilde{h}_{n,N_o-1}^{(q)} \right)^T,$$

and  $a_{n,m}^{(ij)}$ ,  $\mathbf{A}_n^{(ij)}$ ,  $b_{n,m}^{(i)}$ , and  $\mathbf{b}_n^{(i)}$  are defined as

$$a_{n,m}^{(ij)} = \sum_{k=0}^{N-1} x_{n,k}^{(i)} x_{n,k}^{(j)*} W_N^{-km}, \quad (27)$$

$$\mathbf{A}_n^{(ij)} = \left( a_{n,m_1-m_2}^{(ij)} \right)_{m_1, m_2=0}^{N_o-1}, \quad (28)$$

$$b_{n,m}^{(i)} = \sum_{k=0}^{N-1} r_{n,k} x_{n,k}^{(i)*} W_N^{-km},$$

and

$$\mathbf{b}_n^{(i)} = \left( b_{n,0}^{(i)}, \dots, b_{n,N_o-1}^{(i)} \right)^T,$$

respectively.

From the temporal estimation of channel parameters, robust estimation can be obtained using the approach developed in [32], which exploits the time correlation of channel parameters. Robust estimation of channel parameter vectors at the  $n$ th OFDM block can be obtained by

$$\hat{\mathbf{h}}_n^{(i)} = \sum_{l \geq 0} f_l \tilde{\mathbf{h}}_{n-l}^{(i)},$$

where  $f_l$ 's ( $l \geq 0$ ) are the coefficients for the robust channel estimator [31], [32].

Figure 7 illustrates the block diagram of the basic channel estimator for a MIMO-OFDM system with two transmit antennas. To calculate temporal estimation in the figure, a  $2N_o \times 2N_o$  matrix inversion is needed to get the temporal estimation of  $h_{n,m}^{(1)}$  and  $h_{n,m}^{(2)}$ . In general, a  $QN_o \times QN_o$  matrix inversion is required for a MIMO-OFDM system with  $Q$  transmit antennas, which is computationally intensive. To reduce the computational complexity, the significant-tap-catching estimator has been proposed in [31].

To study the impact of channel estimation error on MIMO-OFDM performance, a  $2 \times 2$  MIMO-OFDM system with space-time coding is simulated. The parameters of the simulated OFDM system are similar to those in [31], [32]. The OFDM signal consists of 128 tones, including 8 guard tones on each

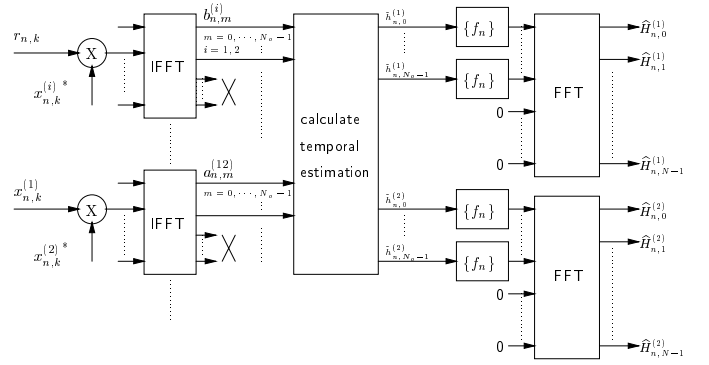


Fig. 7. Basic channel parameter estimator for MIMO-OFDM with 2 transmit antennas.

side, and with 160  $\mu\text{sec}$  symbol duration. A 40  $\mu\text{sec}$  guard interval is used, resulting in a total block length  $T_f = 200$   $\mu\text{sec}$  and a subchannel symbol rate  $r_b = 5$  kbaud. A 16-state 4-PSK space-time code is used. In brief, the overall system can transmit data at a rate of 1.18 Mb/s/sec over an 800 kHz channel, i.e., the bandwidth efficiency is 1.475 bits/s/Hz.

Figure 8 compares the performance between channels with the two-ray and the COST207 HT delay profiles with  $f_d=40$  Hz. From the figure, the system has the same performance when the ideal parameters of the previous OFDM block are used for decoding. However, when estimated parameters are used, the system has better performance for the two-ray delay profile than for the HT profile since the estimator has lower MSE for the two-ray delay profile as we can see from Fig. 8(b). When the 7-tap or 9-tap significant-tap-catching technique in [31] is used, the required SNR for a 10% WER is 8 dB for the two-ray delay profile and about 8.6 dB for the COST207 HT delay profile, respectively.

### B. Optimum Training Sequences for Channel Estimation

In this section, we describe optimum training that can simplify initial channel estimation and optimize estimation performance.

For simplicity, we assume that modulation results in constant-modulus signals, that is,  $|x_{n,k}^{(q)}| = 1$ . From (27),

$$a_{n,m}^{(ii)} = N\delta[m],$$

where  $\delta[m]$  denotes the unit impulse function. Consequently,  $\mathbf{A}_n^{(ii)} = N\mathbf{I}$ , where  $\mathbf{I}$  is a  $N_o \times N_o$  identity matrix. If the training sequences,  $\{x_{1,k}^{(q)}\}$ 's, are chosen such that  $\mathbf{A}_1^{(ij)} = \mathbf{0}$  for  $i \neq j$ , then, from (26),  $\tilde{\mathbf{h}}_1^{(i)} = \frac{1}{N}\mathbf{b}_1^{(i)}$ , and no matrix inversion is required for channel estimation.

To find  $x_{1,k}^{(q)}$  for  $q \geq 2$  with  $|x_{1,k}^{(q)}| = 1$  and  $\mathbf{A}_1^{(ij)} = \mathbf{0}$  for  $i \neq j$ , it is sufficient to find  $a_{1,m}^{(ij)} = 0$  for  $|m| \leq N_o - 1$  since  $\mathbf{A}_1^{(ij)}$  only consists of  $a_{1,m}^{(ij)}$ 's for  $|m| \leq N_o - 1$ , where  $m \equiv N + m$  if  $m < 0$ .

To construct training sequences such that  $\mathbf{A}_1^{(ij)} = \mathbf{0}$ , let the training sequence for the first antenna  $\{x_{1,k}^{(1)}\}$  be any sequence that is *good* for time and frequency synchronization and other properties, such as low PAPR. For a MIMO-OFDM system



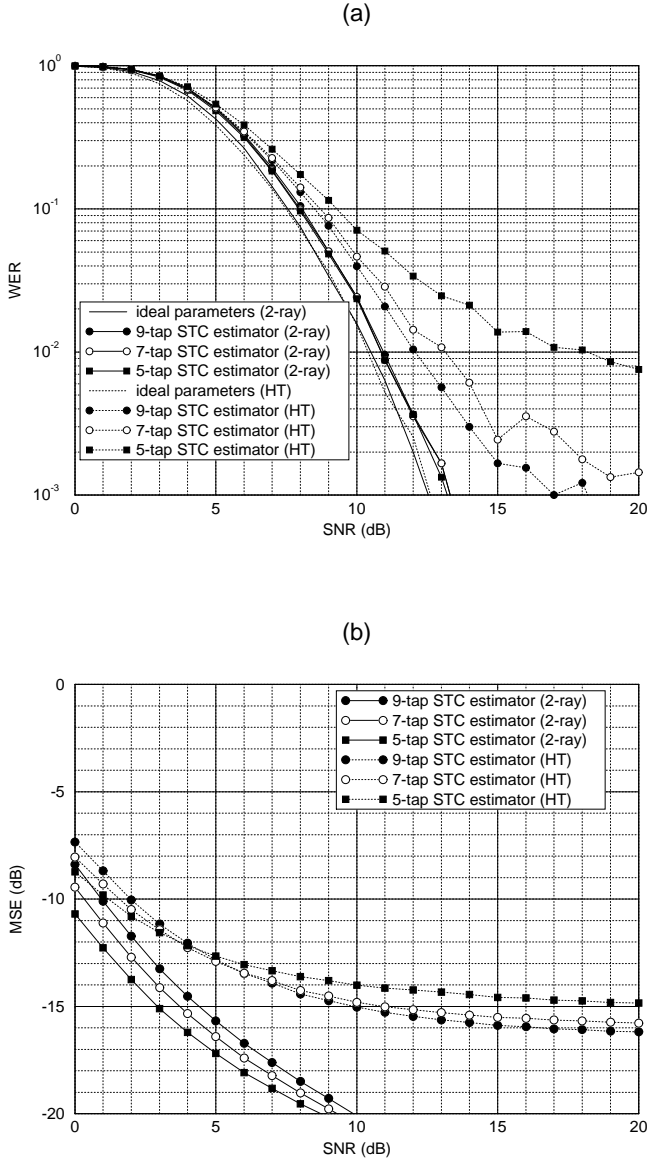


Fig. 8. (a) WER and (b) MSE of a  $2 \times 2$  MIMO-OFDM system when a wireless channel with 40 Hz Doppler frequency and the two-ray and the COST207 HT delay profiles, respectively.

with the number of transmit antennas,  $Q$ , less than or equal to  $N/N_o$ , let

$$x_{1,k}^{(q)} = x_{1,k}^{(1)} W_N^{-\bar{N}_o(q-1)k}, \quad (29)$$

for  $q = 2, \dots, Q$ , where  $\bar{N}_o = \lfloor N/Q \rfloor \geq N_o$  and  $\lfloor z \rfloor$  denotes the largest integer no larger than  $z$ . Then for any  $i \leq j$ ,

$$a_{n,m}^{(ij)} = N\delta[m - \bar{N}_o(j-i)]. \quad (30)$$

Note that  $1 \leq j-i \leq p-1$ ; therefore,

$$\bar{N}_o(j-i) \geq \bar{N}_o \geq N_o, \quad (31)$$

and

$$\bar{N}_o(j-i) \leq \bar{N}_o(p-1) = \bar{N}_o p - \bar{N}_o \leq N - N_o. \quad (32)$$

Consequently,  $a_{1,m}^{(ij)} = 0$  for  $0 \leq m \leq N_o - 1$  or  $N - N_o + 1 \leq m \leq N - 1$  (equivalent to  $|m| \leq N_o - 1$ ), which results in  $\mathbf{A}_1^{(ij)} = \mathbf{0}$  for all  $i < j$ . If  $i > j$ ,  $\mathbf{A}_1^{(ij)} = (\mathbf{A}_1^{(ji)})^H = \mathbf{0}$ . Hence,  $\mathbf{A}_1^{(ij)} = \mathbf{0}$  for all  $i \neq j$ .

It should be indicated that the above optimum training sequence design approach is not applicable to those MIMO-OFDM systems with more than  $N/N_o$  transmit antennas.

It is proved in [31] that the MSE of the basic temporal channel estimation reaches the low bound when  $\mathbf{A}_1^{(ij)} = \mathbf{0}$  for  $i \neq j$ . Therefore, optimum training sequence can not only reduce the complexity of channel estimation but also improve the performance of temporal channel parameter estimation during training period.

### C. Simplified Channel Estimation

In the above section, we have introduced optimum sequences for channel estimation, which not only improve the initial channel estimation during the training period but also simplify channel estimation. During the data transmission period ( $n > 1$ ), transmitted symbols are random; therefore, we cannot control  $\mathbf{A}_n^{(ij)}$ . Here, we introduce an approach that simplifies channel estimation during data transmission mode.

From (25), for the  $n$ th OFDM block, we have

$$\mathbf{A}_n^{(ii)} \tilde{\mathbf{h}}_n^{(i)} = \mathbf{b}_n^{(i)} - \sum_{j=1, j \neq i}^Q \mathbf{A}_n^{(ji)} \tilde{\mathbf{h}}_n^{(j)}, \quad (33)$$

for  $i = 1, \dots, Q$ . In the above expression, the subscript  $n$  has been added to indicate that those vectors and matrices are related to the  $n$ th OFDM block. From the discussion in the previous section, for an OFDM system with constant modulus modulation,  $\mathbf{A}^{(ii)} = N\mathbf{I}$  for  $i = 1, \dots, Q$ , and therefore,

$$\tilde{\mathbf{h}}_n^{(i)} = \frac{1}{N} \left( \mathbf{b}_n^{(i)} - \sum_{j=1, j \neq i}^Q \mathbf{A}_n^{(ji)} \tilde{\mathbf{h}}_n^{(j)} \right), \quad (34)$$

for  $i = 1, \dots, Q$ . From the above equations, if  $\tilde{\mathbf{h}}_n^{(i)}$ 's for  $j = 1, \dots, i-1, i+1, \dots, Q$  are known, then  $\tilde{\mathbf{h}}_n^{(i)}$  can be estimated without any matrix inversion.

If robust estimation of channel parameter vectors at previous OFDM block,  $\hat{\mathbf{h}}_{n-1}^{(i)}$ 's for  $i = 1, \dots, Q$  are used to substitute  $\tilde{\mathbf{h}}_n^{(i)}$  on the right side of (34), then

$$\tilde{\mathbf{h}}_n^{(i)} = \frac{1}{N} \left( \mathbf{b}_n^{(i)} - \sum_{j=1, j \neq i}^p \mathbf{A}_n^{(ji)} \hat{\mathbf{h}}_{n-1}^{(j)} \right), \quad (35)$$

for  $i = 1, \dots, Q$ , and the matrix inversion in (26) can be avoided.

The simplified channel estimation described above significantly reduces the computational complexity of channel estimation; it may also cause some performance degradation. However, it is demonstrated by theoretical analysis and computer simulation in [33] that the performance degradation is negligible.



#### D. Enhanced Channel Estimation

In [31], [33], Sections V-A, V-B, and V-C, we have introduced channel parameter estimators and optimum training sequences for OFDM with multiple transmit antennas. Furthermore, for a MIMO-OFDM system where many independent channels with the same delay profile are involved, the channel delay profile can be more accurately estimated. By exploiting the estimated channel delay profile, channel parameter estimation can be further improved.

From the above discussion, for the  $n$ th OFDM block, channel parameters corresponding to the  $q$ th transmit and the  $l$ th receive antenna pairs,  $h_{n,m}^{(q,l)}$  in (23), can be estimated using the correlation of channel parameters at different times and frequencies. With  $\hat{h}_{n,m}^{(q,l)}$ , the estimated  $h_{n,m}^{(q,l)}$ , the channel frequency response at the  $k$ th tone of the  $n$ th OFDM block can be reconstructed by

$$\hat{H}_{n,k}^{(q,l)} = \sum_{m=0}^{N_o-1} \hat{h}_{n,m}^{(q,l)} W_N^{km}. \quad (36)$$

The estimated channel parameter,  $\hat{h}_{n,m}^{(q,l)}$ , can be decomposed into the true channel parameter,  $h_{n,m}^{(q,l)}$ , and an estimation error,  $e_{n,m}^{(q,l)}$ , that is

$$\hat{h}_{n,m}^{(q,l)} = h_{n,m}^{(q,l)} + e_{n,m}^{(q,l)}. \quad (37)$$

From [33],  $e_{n,m}^{(q,l)}$  can be assumed to be Gaussian with zero-mean and variance  $\sigma^2$ , and independent for different  $q$ 's,  $l$ 's,  $n$ 's, or  $m$ 's. If the parameter estimation quality is measured by means of the normalized MSE (NMSE), which is defined as

$$\text{NMSE} = \frac{E \left| \hat{H}_{n,k}^{(q,l)} - H_{n,k}^{(q,l)} \right|^2}{E \left| H_{n,k}^{(q,l)} \right|^2},$$

then it can be calculated directly that the NMSE for the estimation in (36) is

$$\text{NMSE}_r = N_o \sigma^2, \quad (38)$$

where we have used the assumption that

$$\sum_{l=0}^{N_o-1} E \left| h_{n,m}^{(q,l)} \right|^2 = \sum_{l=0}^{N_o-1} \sigma_m^2 = 1,$$

with  $\sigma_m^2 = E \left| h_{n,m}^{(q,l)} \right|^2$ .

If the channel's delay profile, that is,  $\sigma_m^2$ 's for  $m = 0, \dots, N_o - 1$ , is known, and it can be used to reconstruct the channel frequency response from  $\hat{h}_{n,m}^{(q,l)}$ , the NMSE of  $\hat{H}_{n,k}^{(q,l)}$  can be significantly reduced. In this case, if the  $\alpha_m$ 's are selected to minimize the NMSE of

$$\hat{H}_{n,k}^{(q,l)} = \sum_{m=0}^{N_o-1} \alpha_m \hat{h}_{n,m}^{(q,l)} W_N^{km}, \quad (39)$$

then it can be proven that the optimal  $\alpha_m$  is

$$\alpha_m = \frac{\frac{\sigma_m^2}{\sigma_m^2 + \sigma^2}}{\sum_{m'=0}^{N_o-1} \frac{\sigma_{m'}^4}{\sigma_{m'}^2 + \sigma^2}} \quad (40)$$

and the NMSE is

$$\text{NMSE}_o = \frac{\sigma^2 \sum_{m=0}^{N_o-1} \frac{\sigma_m^2}{\sigma_m^2 + \sigma^2}}{\sum_{m=0}^{N_o-1} \frac{\sigma_m^4}{\sigma_m^2 + \sigma^2}}. \quad (41)$$

As indicated in [32], channel's delay profile depends on the environment, and therefore, is usually unknown. However, for MIMO-OFDM systems, channels corresponding to different transmit or receive antennas should have approximately the same delay profile. Therefore,  $\sigma_m^2 = E \left| h_{n,m}^{(q,l)} \right|^2$  can be estimated by

$$\hat{\sigma}_m^2 = \frac{1}{QL} \sum_{q=1}^Q \sum_{l=1}^L \left| \hat{h}_{n,m}^{(q,l)} \right|^2.$$

With the estimated  $\sigma_m^2$ , enhanced channel frequency responses can be reconstructed by (39).

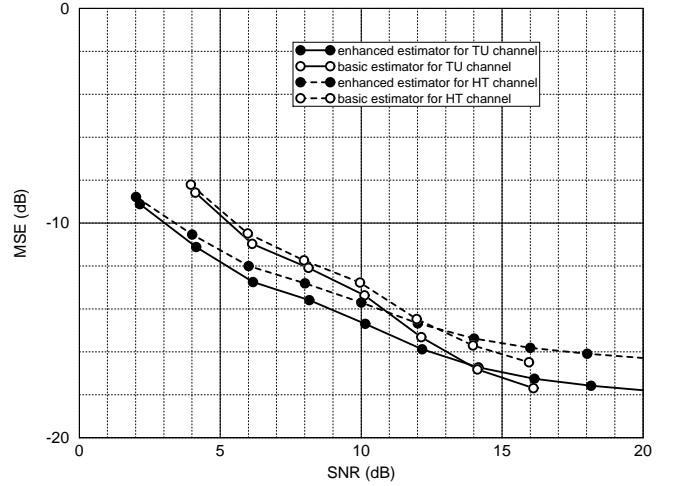


Fig. 9. MSE comparison of the basic and the enhanced channel estimation techniques for a  $4 \times 4$  MIMO-OFDM system.

Figure 9 compares the MSE of the basic and enhanced channel estimation for a  $4 \times 4$  MIMO-OFDM system. From the figure, the MSE of the enhanced channel estimator is about 1.5 dB better for the COST207 TU channels and 1 dB better for the COST207 HT channels than the basic estimator described in Section V-A and [31].

#### VI. SPACE-TIME CODING TECHNIQUES FOR MIMO-OFDM

OFDM is an effective and low-complexity strategy for dealing with frequency-selective channels. Roughly speaking, an OFDM transmitter divides the frequency band into  $N$  narrow subchannels and sends a different sequence of symbols across each subchannel. When the subchannel bandwidth is sufficiently narrow, the frequency response across each subchannel is approximately flat, avoiding the need for complicated time-domain equalization. In this way, OFDM transforms a frequency-selective channel into a collection of



$N$  separate flat-fading channels. In the same way, when an OFDM transmitter is used by each of  $Q$  transmit antennas, and an OFDM front-end is used by each of  $L$  receive antennas, a MIMO frequency-selective channel is transformed into a collection of  $N$  flat-fading MIMO channels, one for each tone, with each having dimension  $L \times Q$ .

Traditional space-time codes were designed to extract spatial diversity from a flat-fading MIMO channel, and are not generally effective at extracting the additional frequency (or multipath) diversity of a frequency-selective fading channel. Quantitatively, the maximum achievable diversity order is the product of the number of transmit antennas, the number of receiver antennas, and the number of resolvable propagation paths (i.e., the channel impulse response length) [11][12]. To achieve this full diversity requires that the information symbols be carefully spread over the tones as well as over the transmitting antennas. A *space-frequency* code – or more generally, a *space-time-frequency* code – is a strategy for mapping information symbols to antennas and tones as a means for extracting both spatial and frequency diversity.

Space-frequency codes based directly on space-time codes (with time reinterpreted as frequency) have been proposed [10], [19], [50], [51], [52], but they fail to exploit the frequency diversity of a frequency-selective fading MIMO channel [11]. Guidelines for the design of full-diversity space-frequency codes are given in [11]. A simple method for transforming any full-diversity space-time code into a full-diversity space-frequency code has recently been proposed, at the expense of a reduced rate [49]. An example of a space-frequency code that achieves full spatial and frequency diversity is given in [13]. The design of space-frequency and space-time-frequency codes is currently an active area of research [11] [12] [13] [14] [15] [16] [17] [18].

In the remainder of this section we highlight two approaches to space-time processing for MIMO-OFDM. The first is a combination of delay-diversity and OFDM known as multicarrier delay-diversity modulation, while the second is a closed-loop system with channel knowledge at the transmitter.

#### A. Multicarrier Delay Diversity Modulation (MDDM)

Delay diversity was the first transmit diversity approach for flat-fading MIMO channels [34], [35], [36], [37]. Multiple transmit antennas send delayed copies of same signal, and maximum-likelihood sequence estimation [36], [38] or decision-feedback equalization [39] is used at the receiver to estimate the transmitted sequence. The natural ability of OFDM to mitigate frequency-selective fading makes delay diversity an attractive option for MIMO-OFDM [20]. For frequency-selective fading channels, a cyclic delay-diversity approach with OFDM is proposed in [21], a combination known as *multicarrier delay-diversity modulation (MDDM)*. MDDM is further investigated with space-time block coding in [22]. With proper coding, MDDM can achieve full spatial diversity on flat fading channels [23]. Moreover, MDDM provides a very flexible space-time coding approach for any number of transmit antennas, allowing the number of transmit antennas to be changed without changing the codes that are employed, unlike STBC [23].

Fig. 10 shows the baseband MDDM transmitter with  $Q$  transmit antennas. A length- $N$  sequence  $(X_0, \dots, X_{N-1})$  modulates  $N$  subcarriers, where the multicarrier modulation is, again, an IDFT. A length- $G$  cyclic guard interval in the form of a cyclic prefix is added to the time domain sequence  $\{x_n\}$ . The  $Q$  transmit antennas are arranged in a length- $Q$  tapped-delay line configuration, where the delay interval is equal to symbol period  $T$  of the sequence  $\{x_n\}$ . The initial values of transmitting antennas are  $x_{N-G}, x_{N-G-1}, \dots, x_{N-G-Q+1}$  for the 0-th antenna to the  $(Q-1)$ -th antenna, respectively. The MDDM scheme requires a slight increase in the guard interval to account for the increased delay spread caused by the delays of the transmitter.

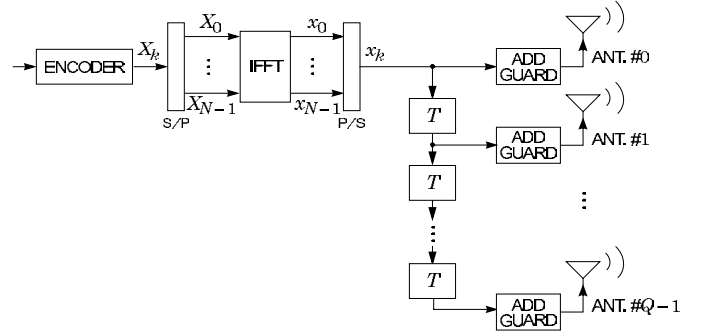


Fig. 10. A multicarrier delay-diversity modulation (MDDM) transmitter.

Consider MDDM with  $Q$  transmit antennas and transmitted sequences  $\mathbf{X}$  of length  $N$ ,  $N > Q$ . Note that  $\mathbf{X}$  is the encoded sequence in the frequency domain before the IDFT. If all distinct pairs of sequences  $(\mathbf{X}, \tilde{\mathbf{X}})$ ,  $\mathbf{X} \neq \tilde{\mathbf{X}}$  differ in at least  $Q$  coordinates, then MDDM achieves full spatial diversity on quasi-static flat Rayleigh fading channels [23]. For BPSK and QPSK symbols this give a simple design criteria: any binary code  $\mathcal{C}$  having minimum distance  $d_m \geq Q$  will achieve full spatial diversity for an MDDM system having  $Q$ -transmit antennas. With MDDM, interleaving of the coded bits is also necessary for maximizing the coding gain. Criteria for *optimum* interleaving have been derived in [23], where it is also shown that a simple block interleaver achieves near optimum performance.

#### B. Closed-Loop MIMO-OFDM

A *closed-loop* MIMO transmitter has knowledge of the channel, allowing it to perform an optimal form of precompensation at the transmitter known as *eigenbeamforming*. In particular, for a flat-fading channel, it is well-known that a capacity-achieving transmitter bases its space-time processing on a singular-value decomposition (SVD) of the  $L \times Q$  matrix of channel gains  $\mathbf{H} = \mathbf{U}\mathbf{S}\mathbf{V}^*$ , where  $(\cdot)^*$  denotes the Hermitian transpose, where  $\mathbf{U}$  and  $\mathbf{V}$  have orthogonal columns and where  $\mathbf{S}$  is a diagonal matrix whose diagonal entries are the nonnegative singular values that are ordered from largest to smallest. A capacity-approaching transmitter will then implement eigenbeamforming by applying the linear filter  $\mathbf{V}$  to symbol vectors before transmission. A receiver matched to the cascade of this prefilter and the channel will essentially



apply the filter  $\mathbf{U}^*$  to the received vector, which transforms the flat-fading channel into a bank of independent scalar channels. The problem has thus been reduced to one of communication across a bank of independent parallel scalar subchannels, where the subchannel gains are the nonnegative, nonincreasing singular values of the channel.

Because OFDM reduces a frequency-selective channel to a collection of flat-fading MIMO channels, a closed-loop MIMO-OFDM system can use eigenbeamforming on a tone-by-tone basis to transform a frequency-selecting MIMO channel into a collection of  $MN$  parallel subchannels [9], where  $M = \min\{Q, L\}$  is the minimum number of antennas at each end and  $N$  is the number of OFDM tones. A MIMO-OFDM system with eigenbeamforming is illustrated in Fig. 11-a for the special case of two transmit and two receive antennas. The prefilters  $\{\mathbf{V}_n\}$  and postfilters  $\{\mathbf{U}_n^*\}$  are related to the 2-by-2 matrix of channel gains for the  $n$ -th tone  $\mathbf{H}_n$  by the SVD  $\mathbf{H}_n = \mathbf{U}_n \mathbf{S}_n \mathbf{V}_n^*$ . The permuter  $\pi$  at the transmitter is a simple row-column interleaver of dimension  $N \times 2$ . The entire system of Fig. 11-a reduces to the bank of scalar channels shown in Fig. 11-b, where  $s_{i,j}$  denotes the  $i$ -th singular value for the  $j$ -th tone.

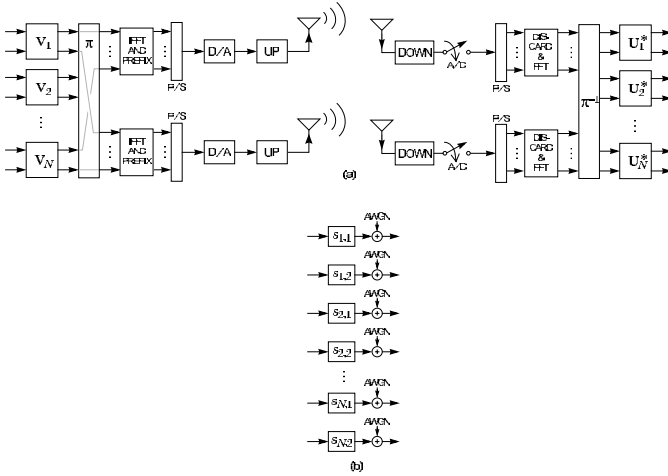


Fig. 11. A combination of eigenbeamforming and OFDM transforms a closed-loop frequency-selective fading channel (a) into a bank of scalar channels (b), each with independent noise.

Ideally, information bits (constellation size) and symbol energy would be allocated to the  $MN$  subchannels of Fig. 11-b so as to minimize the overall SNR requirement, subject to a target bit rate. (Alternatively, the bits and energy could be allocated so as to maximize the bit rate, subject to a target energy constraint.) Unfortunately, the complexity of an exhaustive search for the bit-allocation is prohibitive when the number of subchannels is large. In a practical MIMO-OFDM application, the number of subchannels  $MN$  can be very large, which motivates a search for low-complexity bit-allocation strategies with near-optimal performance.

A simple and effective way to reduce complexity is to

impose a *flat-frequency constraint*, where each tone is restricted to have the same bit budget [40]. We now illustrate that the penalty due to this constraint can be small. Let  $B$  denote the total bit budget for each OFDM signaling interval. Without the flat-frequency constraint, and without constraining the symbols to a discrete alphabet, the optimal rate  $r_{i,j}$  for the  $i$ -th spatial channel (singular value) and the  $j$ -th tone is found by waterpouring over both space and frequency, yielding

$$r_{i,j} = \{\log_2(\lambda s_{i,j}^2)\}^+,$$

where  $\{x\}^+ = \max\{0, x\}$ , and where  $\lambda$  ensures that the total bit budget is met,  $\sum_{i,j} r_{i,j} = B$ . On the other hand, if we enforce the flat-frequency constraint, the constrained optimal solution is

$$r_{i,j} = \{\log_2(\mu_j s_{i,j}^2)\}^+,$$

where  $\mu_j$  ensures that  $\sum_i r_{i,j} = B/N$  for each  $j = 1, \dots, N$ . Since  $\mu_j$  is calculated anew each tone, this amounts to water-pouring over space but not frequency. In either case, the average required SNR is given by:

$$E/N_0 = E\left[\sum_{i=1}^M \sum_{j=1}^N \frac{2^{r_{i,j}} - 1}{s_{i,j}^2}\right],$$

which serves as a figure of merit.

The penalty of the flat-frequency constraint is easily measured by comparing this SNR requirement with and without the constraint. For example, Fig. 12 illustrates the SNR penalty of the flat-frequency as a function of zero-outage capacity, also known as the delay-limited capacity, in b/s/Hz. These results were based on 10,000 independent frequency-selective channels generated according to the typical urban profile, with Rayleigh fading on each path. The SNR penalty for the case of a  $2 \times 2$  channel ( $M = 2$ ) is relatively large, more than 0.5 dB. However, for the cases of  $M = 4$  and  $M = 6$ , the flat-frequency strategy performs only marginally worse, suffering a 0.1 dB penalty for  $M = 4$  and a 0.05 dB penalty for  $M = 6$ . Clearly, the flat-frequency constraint incurs little penalty, especially when there are more than two antennas at each end.

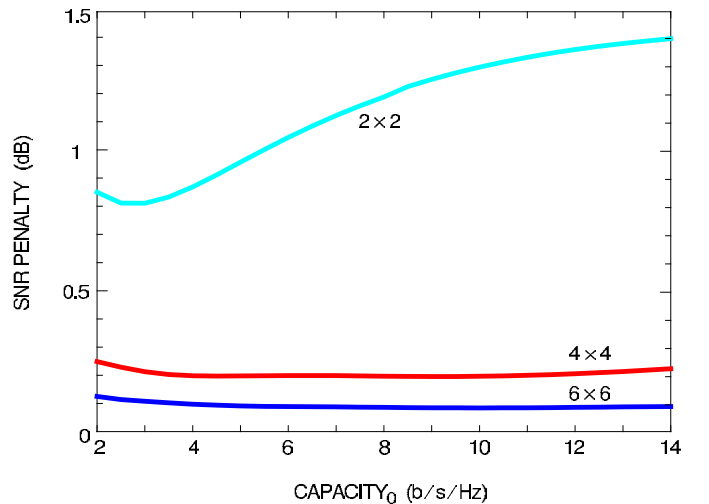


Fig. 12. The flat-frequency constraint incurs a small SNR penalty.



We can further reduce complexity by imposing a *fixed spatial allocation* on top of the flat-frequency constraint [41]. Instead of exhaustively searching all possible spatial allocations meeting a bit budget of  $B/N$ , this strategy fixes the allocation based on the anticipated statistics of MIMO Rayleigh fading channels. The penalty due to a fixed allocation is surprisingly small, thanks to a combination of the known Rayleigh fading statistics and the ordered nature of the singular values. Combining the flat-frequency constraint with a fixed spatial allocation per tone leads to a totally *nonadaptive* bit-allocation strategy. Remarkably, this fixed-frequency fixed-space strategy performs reasonably well when there are two antennas at each end, and it is even better when there are more antennas.

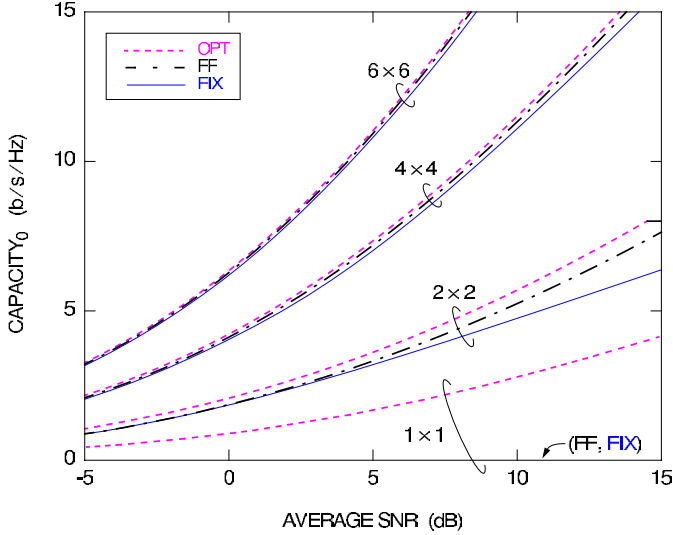


Fig. 13. The nonadaptive strategy, which uses a combination of the flat-frequency constraint and a fixed spatial allocation, approaches the fully adaptive waterpouring solution as the number of antennas grows.

Fig. 13 illustrates the performance of the nonadaptive strategy with the water-pouring solution, with and without the flat-frequency constraint. The channel conditions are identical to those used in Fig. 13. Although the nonadaptive strategy suffers a significant penalty when  $M = 2$ , it is nearly optimal for  $M = 4$  and  $M = 6$ . The conclusion is that a closed-loop MIMO system need not perform adaptive modulation in order to approach capacity. Instead, a combination of eigenbeamforming and fixed modulation is sufficient, at least on i.i.d. Rayleigh channels with more than two antennas at each end.

## VII. ERROR CORRECTION CODING FOR MIMO-OFDM

There are many possible error control strategies in MIMO OFDM systems, in this section we highlight some of the methods that have been proposed. At this writing this is a very active and rapidly evolving research area. As in any system there are important performance-complexity tradeoffs, however, we do not address those here. Furthermore, depending on the application, the desired bit error rate may result in the need for only minimal or no error correction, namely the modulation code might be sufficient to provide the needed

BER, for example  $10^{-3}$ . However, if either near capacity performance or a very low BER is required (e.g.  $10^{-6}$  to  $10^{-12}$ ) a powerful error control code is needed. From this perspective much of the recent work has focused on the use of iteratively decodable codes such as turbo codes and low density parity check codes. As turbo codes are special cases of low density parity check codes, we focus on those. Also we start our description with single-input, single-output channels as many practical error control strategies for MIMO systems will be designed for SISO channels and then mapped to MIMO channels.

### A. Low-Density Parity-Check Codes and SISO flat fading channels

LDPC codes are specified by a sparse parity-check matrix and can be categorized into regular and irregular LDPC codes. The regular LDPC codes have parity-check matrices whose columns have the same number of ones. In this paper, we focus on regular LDPC codes.

A parity-check matrix  $\mathbf{P}$  of a  $(c, t, r)$  LDPC code has  $c$  columns,  $t$  ones in each column and  $r$  ones in a row. A  $(c, t, r)$  LDPC code has a code rate of  $1 - t/r$ . Gallager [42] showed that there is at least one LDPC code whose minimum distance,  $d_{\min}$  grows linearly with block length  $c$  when  $t > 2$ . Therefore, we can expect a better coding gain with a longer code length, although the coding length is limited by practical considerations like decoding latency, decoder complexity etc. The rate of growth of  $d_{\min}$  is bounded by a nonzero number, which is determined by the selection of  $t$  and  $r$ .

The belief propagation algorithm has been widely adopted for decoding LDPC codes. MacKay [43] gives a good description of the iterative message passing decoder based on the belief propagation algorithm which can be implemented in either probability or log-probability domain. The decoder in this paper works in the log-probability domain. For the message-passing decoder, we need the LLR of each bit. A general form of the LLR computing formula is given by

$$\text{LLR}(b_j) = \log \left[ \frac{\sum_{i=1}^{2^{k-1}} P(\mathbf{R}|b_j = 1, \mathbf{m}_j = m_i)}{\sum_{i=1}^{2^{k-1}} P(\mathbf{R}|b_j = 0, \mathbf{m}_j = m_i)} \right] \quad (42)$$

where  $\mathbf{R}$  is a received signal vector,  $b_j$  is  $j$ -th bit of a transmitted message,  $\mathbf{m}_j$  is a message less the  $j$ -th bit,  $m_i$  is one of  $2^{k-1}$  possible symbols of  $\mathbf{m}_j$  and each symbol carries  $k$  bits.

On an AWGN channel with flat fading, (42) can be expressed as

$$\text{LLR}(b_j) = \log \left[ \frac{\sum_{i=1}^{2^{k-1}} \exp \left\{ -\frac{d(\mathbf{R}, \mathbf{c}_i^{b_j=1})^2}{2\sigma^2} \right\}}{\sum_{i=1}^{2^{k-1}} \exp \left\{ -\frac{d(\mathbf{R}, \mathbf{c}_i^{b_j=0})^2}{2\sigma^2} \right\}} \right] \quad (43)$$

where  $\mathbf{c}_i^{b_j=b}$  is a signal constellation for a message defined by  $m_i$  and  $b_j$  and  $d(\mathbf{R}, \mathbf{c}_i^{b_j=b})$  is the Euclidean distance between the received signal vector  $\mathbf{R}$  and  $\mathbf{c}_i^{b_j=b}$ .



To prevent possible underflow or overflow, the equation can be modified to a more applicable form as

$$\text{LLR}(b_j) = \frac{(d_{\min}^0(j))^2 - (d_{\min}^1(j))^2}{2\sigma^2} + \log \left[ 1 + \sum_{\substack{i=1, \\ i \neq l_1}}^{2^k-1} \exp \left\{ -\frac{d(\mathbf{R}, \mathbf{c}_i^{b_j=1})^2 - (d_{\min}^1(j))^2}{2\sigma^2} \right\} \right] - \log \left[ 1 + \sum_{\substack{i=1, \\ i \neq l_0}}^{2^k-1} \exp \left\{ -\frac{d(\mathbf{R}, \mathbf{c}_i^{b_j=0})^2 - (d_{\min}^0(j))^2}{2\sigma^2} \right\} \right] \quad (44)$$

where  $d_{\min}^b(j) = d(\mathbf{R}, \mathbf{c}_{l_b}^{b_j=b}) = \min_{1 \leq i \leq 2^k-1} d(\mathbf{R}, \mathbf{c}_i^{b_j=b})$  and  $b$  is in  $\{0, 1\}$ .

Fig. 14 shows the BER performance of LDPC codes having code length  $c = 1024$  and code rates of 0.5, 0.75, 0.875 and 1.0 (uncoded) with 16 and 64-QAM modulation on an AWGN channel.

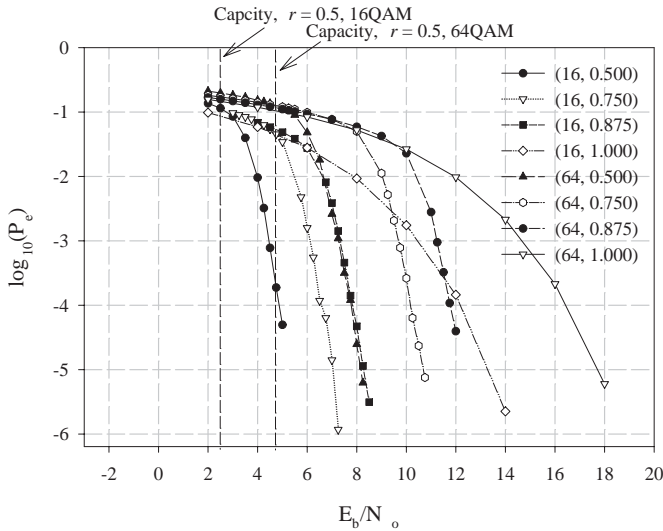


Fig. 14. BER performance of LDPC codes having code length  $c = 1024$  and code rates of 0.5, 0.75, 0.875 and 1.0 (uncoded) with 16 and 64-QAM on an AWGN channel.

Other recent work in this area shows several things regarding the possible *universality* of LDPC codes on fading channels. If the encoder side has partial or full channel knowledge the code rate can be adapted to account for the quality of the channel (provided the fading is slow enough). In [44] it is shown that a properly designed LDPC can be punctured to produce a (higher rate) code that is just as good as an optimally designed code for that higher rate. In principle this allows one to design and implement a single LDPC that is optimal across a range of rates.

If no information is available at the encoder and the fading is faster, other recent work by [45] indicates that a properly designed LDPC might also be universal. That is, regardless of the fading, they show that the maximum achievable rate

of an LDPC code is very close to the theoretical maximum achievable rate of any code. This indicates that a significantly better code than an LDPC probably does not exist.

Both of these topics are very active and we expect new results that will further strengthen the idea that LDPCs are good both theoretically and practically.

## B. SISO and MIMO channels with and without OFDM

When a SISO or MIMO channel uses OFDM there are many FEC options. For closed-loop SISO OFDM channels where the encoder has complete channel knowledge (see Section VI-B) a waterfilling approach can be used, where each subcarrier is coded separately at a rate  $R_i = \log_2(1 + \frac{|a_i|^2 E_i}{2\sigma^2})$ . This can be a costly approach if the number of subcarriers is large since each carrier uses a separate encode and decoder. In systems like IEEE 802.11a, where the encoder does not know the channel, a single (convolutional) code is used across all subcarriers and various decoding strategies can be employed to account for the fact that some subcarriers are better than others. Another case of interest is single carrier MIMO channel, there are a host of recent papers, see for example [46], [47], [48]

For full MIMO OFDM, in [53] LDPC system is compared with space-time trellis code (STTC), the LDPC-based STC can significantly improve the system performance by exploiting both the spatial diversity and the selective-fading diversity in wireless channels. Compared with the recently proposed turbo-code-based STC scheme [54], LDPC-based STC exhibits lower receiver complexity and more flexible scalability.

## VIII. ANTENNA AND BEAM SELECTION

The cost of the MIMO-OFDM system is largely driven by the number of transmit and receive chains, for example each receiver chain includes frequency conversion, IF filtering, and analog-to-digital conversion. The circuits performing these functions must be replicated  $L$  times if a MIMO receiver has  $L$  receive branches. However, it is possible to have the spatial diversity and interference suppression benefits of many more antennas than full receiver chains through the use of antenna or beam selection. In this section, we consider antenna and beam selection, give a summary of a low-complexity selection algorithm for OFDM, and show some results for measured channels that compare antenna to beam selection.

### A. Antenna Selection

Transmit antenna selection for MIMO has been previously considered for flat-fading MIMO links in the absence of interference [55], [56] and with interference [57], [58]. In the no-interference works, the selection criterion was based on average SNR criteria. Selection of 2 antennas from 3 antennas appeared to give a second-order diversity gain for zero-forcing spatial multiplexing receivers, and produced vector symbol error rates that matched that of the 2 by 2 maximum likelihood receiver without selection [55]. For space-time block coding, selection of 2 transmit antennas from 5 to 10 antennas, assuming 2 receive antennas, provided an SNR gain of 2 to 3 dB [56]. For the flat-fading channel with interference, Blum



and Winters [57] show about a 7 dB improvement for 8-select-2 diversity at both ends of the link, assuming one or two interference data streams and simulated iid MIMO channels.

The MIMO selection diversity gain comes with a price: the switch that performs the antenna selection requires a non-trivial design and has a non-negligible insertion loss [59]. For example the 8-select-2 switch in [59] has an insertion loss of 3.15 dB. In a transmitter, the insertion loss reduces the radiated power. In a receiver, the insertion loss degrades the SNR. The degradation can be made negligible by placing low-noise-amplifiers between the antenna elements and the switch. However, this addition can add significant expense to the receiver. On the other hand, the degradation in SNR may not be important if the receiver performance is limited by interference.

The gain from antenna selection for OFDM-MIMO may not be as large as it is for the flat-fading channel because the best selection of elements is likely to change with frequency. While subcarrier-dependent antenna selection is considered in [60], we do not consider this here, since our goal is for the solution to have a certain limited number of transmit and receive chains.

### B. Beam Selection

An alternative selection approach for OFDM-MIMO is to select beams instead of selecting antennas. Fig. 15 shows the architectures when  $4 \times 2$  (a) antenna selection and (b) beam selection are used at both ends of the link. Both architectures require the  $4 \times 2$  switch. Beam selection is motivated by the observation that multipath angles are often clustered [61], [62]. The cluster angles are not expected to be very frequency-dependent, so the best selection of beams should not change much with frequency. Therefore, if the beamwidth can be matched to the cluster width, there should be an SNR advantage in the absence of interference [63] and a signal-to-interference (SIR) advantage with interference. Moreover, analog beamforming circuits, such as the Butler matrix [64], are inexpensive compared to the switch at microwave frequencies because they can be implemented in stripline [65]. Therefore, the percentage increase in cost to have beam selection should be small. Like the switch, the beamformer has an insertion loss (2.26 dB for the 8-beam Butler matrix is in [65]) so its effects must be more than overcome to justify its use. Two-beam selection for array receivers over simulated clustered indoor channels have indicated that four 8-element linear arrays, placed end-to-end in a square configuration to provide 360 degrees azimuth coverage, yield an almost 6 dB SNR improvement compared to two fixed omnidirectional antennas when the two beams are processed by a joint decision-feedback equalizer [66]. When the same beam-selection configuration is simulated for Space-time block coded OFDM, an SNR improvement of approximately 5 dB is obtained without interference, and an SIR improvement of more than 16 dB is obtained with interference [67].

### C. A Selection Algorithm

In order to select receive beams with good SIR, but with a constraint on the number of full receiver chains, a two-metric,

iterative selection algorithm has been proposed [67]. This algorithm assumes a single-input-multiple-output channel and it applies to both antenna and beam selection. It is described below for the case of two receiver chains, however, it easily extends to an arbitrary number of receiver chains.

The first metric, RSSI, is measured for all beams by analog detectors, while the second metric, the peak-to-trough ratio (PTR) [68], is based on a sliding correlation of the received preamble with one stored OFDM preamble symbol and is computed in the digital signal processor (DSP) prior to full OFDM synchronization. We note that the second metric in [67] is bit-error-rate. The PTR, to be defined below, is judged to be a more practical and readily available second metric. The two beams having the highest RSSI are connected to the receiver chains by the RF switch. Then, the PTR values are checked for the two selected beams. If the PTR value for a beam is less than a threshold (which can be set based on the real system's requirement), we conclude that this beam has too much interference; then we check the beam with the next-highest RSSI until we find a PTR value that is higher than the threshold.

To get the PTR value, we use the following equation

$$R_x(m) = \frac{\left| \sum_{n=0}^{N1} \bar{r}_x(n+m) \bar{t}_x^*(n) \right|}{\left| \sum_{n=0}^{N1} \bar{r}_x(n+m) \bar{r}_x^*(n+m) \right|}, \quad (45)$$

$$m = 0, 1, 2, \dots, N2$$

where  $r_x$  is the received short training sequence which includes noise and interference, and  $t_x$  is the original one-period-long training sequence. N1 is the length of one period of the training sequence. N2 is the length of the whole short training sequence plus one period length.  $R_x(m)$  is the normalized cross-correlation function. If the received signal includes limited noise and interference,  $R_x(m)$  will have  $N2/N1-1$  peaks. Then each peak and some points on each side of it are removed. The remainder depends on the correlation of the training sequence with the noise and interference. The second metric is computed as

$$PTR = \frac{\langle (\text{magnitude of the peaks})^2 \rangle}{\langle (\text{magnitude of the remainder})^2 \rangle} \quad (46)$$

Where  $\langle \rangle$  indicates a time average.

Figs. 16 show the results of a wired hardware test of the PTR metric. The preamble, which is 64 symbols long, is generated at IF. The IF signal was added to the output of a noise generator using a power combiner and then sampled and downconverted. The PTR metric was computed in the DSP. Varying amounts of noise were added. The PTR was computed for 10 trials for each noise value. The sample values of the PTR metric for each noise power value are shown in Fig. 16. An example beam reject threshold is shown. The figure shows that the PTR is an effective indicator of SNR.

From simulation, we can also conclude that PTR metric is very robust to synchronization offsets: frequency offset, sampling frequency offset and frame time offset.



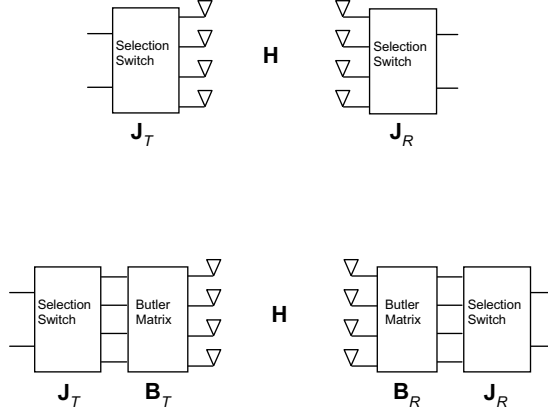


Fig. 15. Antenna selection and beam selection architectures.

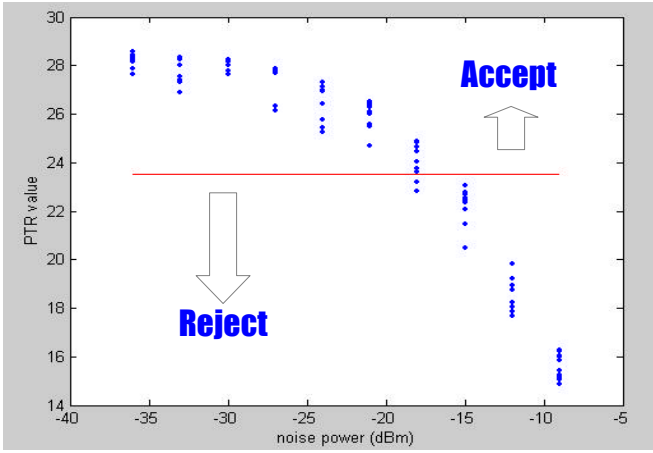


Fig. 16. PTR with different noise powers.

#### D. Comparison of Antenna and Beam Selection

The two architectures in Fig. 15 have been compared over indoor MIMO channels measured in the Residential Laboratory (ResLab) at the Georgia Institute of Technology [69]. Using a virtual array approach, 4 wideband  $4 \times 4$  MIMO realizations were captured. Each of these realizations was sampled at 51 frequencies, with 10 MHz separation between consecutive frequency samples. Interference was created by a second MIMO link in the ResLab. The performance for each link was quantified by the capacity of the interference-whitened channel, averaged over the 51 frequency samples. The throughput is the sum of these two average capacities. Fig. 17 shows the results for a topology where the angles of arrival (and departure) of the interference and desired signal are not close, and Fig 18 corresponds to a topology where both desired and interfering signals are emerging from a hallway, and are therefore likely to be close (spatially correlated) [69]. “T-beam, T-Antenna, and T-No Selection” correspond to two transmit beams selected from four, two transmit antennas are selected from four, and the first two transmit antennas are always used, respectively. This corresponds to a condition of

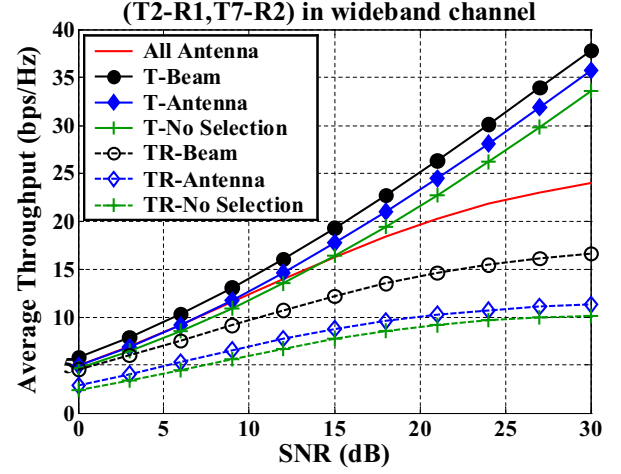


Fig. 17. Average throughput for two interfering MIMO links with various kinds of selection; uncorrelated interference.

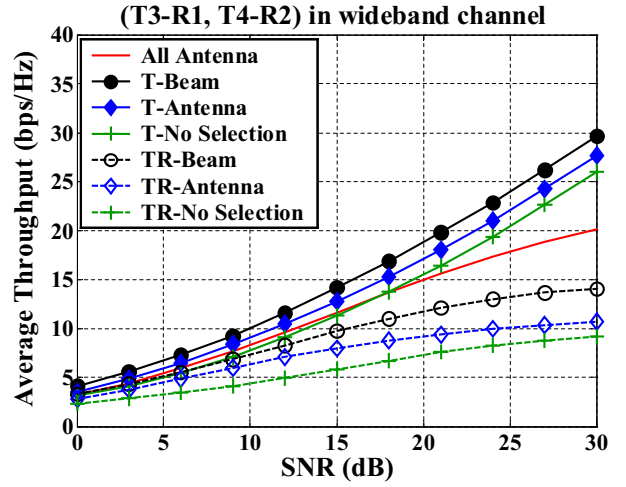


Fig. 18. Average throughput for two interfering MIMO links with various kinds of selection; correlated interference.

“stream control” where neither receiver is overloaded with too many streams [70]. T-beam and T-antenna selection occurs optimally for both interfering links. “TR-Beam, TR-Antenna, and TR-No Selection” correspond to the selection occurring at transmitters and receivers. We note that the receivers are overloaded with too many streams for the TR cases. The “All antennas” case has no selection and also corresponds to an overloaded condition. We observe that there is little difference between beam-, antenna-, and no-selection when the receivers are not overloaded for either correlated or uncorrelated interference. However, when the receivers are overloaded, beam selection outperforms antenna selection for uncorrelated interference by a SNR margin that is 10 dB and larger, depending on the throughput value. The margin is smaller for correlated interference.



## IX. MEDIUM ACCESS CONTROL

Although not the focus of this paper, MAC protocols are essential for effective broadband wireless access. MAC protocols for OFDM can be based on time division multiple access (TDMA), where all the OFDM sub-carriers are used at once. Such protocols are used in IEEE802.11a and IEEE802.16a for example. An alternative is to use OFDMA or clustered OFDM, where each connection uses a subset of the OFDM sub-carriers. Such an approach is used in some operating modes of IEEE802.16a. MAC protocols generally must support hundreds of end-user terminals that demand a mixture of services ranging from traditional voice and data, internet protocol (IP) connectivity, multimedia and real time applications such as voice over IP (VoIP). The support of these services requires a MAC protocol that handles both continuous and bursty traffic with quality of service (QoS) guarantees that depend on the application. The issues of transport efficiency are addressed at the interface between the MAC and PHY layers, and the actual throughput that is achieved is highly dependent on the choice of MAC protocol. For example, the MAC adjust PHY layer parameters such as the type of modulation and coding employed to meet QoS and link availability requirements. Additional information on typical MAC related issues are available in a variety of sources including the IEEE802.16a standard [2].

## X. SOFTWARE RADIO IMPLEMENTATION

The proliferation of high-performance DSP cores, FPGAs and ASICs - as well as the current trend towards System-on-a-Chip (SoC) integration - are bringing the software radio paradigm closer to practical realization. While advances in these key technology areas - and other areas such as wideband A/Ds, low-power circuit technology and wideband amplifiers - are critical in the evolution of software radio, technology today allows one to begin to discover and appreciate the great promise that software radio holds. Current trends in the wireless telecommunications industry are steering towards advanced applications requiring wider bandwidth, which will place increasing processing loads upon future SDR implementation architectures.

Faculty at Georgia Tech are collaborating to develop a high bandwidth, high data-rate wireless gateway using advanced technologies including software radio, smart antennas, MIMO-OFDM, advanced FECs, and higher layers that support quality of service. A key component in the research is the implementation of the techniques in a programmable testbed at the GT Software Radio Laboratory. In this paper, we focus on a description of the physical layer and on the implementation of MIMO-OFDM in the testbed.

In the first part of this section, we describe the design and performance of the software-radio testbed, which was developed using commercial components to implement programmable transceivers for wireless communications. The system provides a useful vantage point for empirical exploration of issues related to software radio implementation. We describe the major hardware components, the algorithm flow through the system, and the implementation performance for MIMO-OFDM.

### A. Software Radio Overview

Software radio, as discussed in this section, refers to a transceiver with radio receive and/or transmit functions defined in software. Given the current state of technology, software-defined radio functions are typically employed in the intermediate frequency (IF) and baseband subsystems. Often, software defined functions are supported with complementary technologies, including programmable devices, such as Field Programmable Gate Arrays (FPGAs), which can perform certain functions - e.g., down-conversion, FFTs and FEC decoding - more efficiently than software-defined functions in processing cores. In future Software Defined Radio (SDR), software defined functions and programmable features would be reconfigurable either through over-the-air commands or via adaptive circuitry allowing a mobile transceiver to seamlessly reconfigure itself based on the electromagnetic environment or other cues available to a transceiver [71].

The programmable functions and features of the testbed are not entirely mature, but do provide a reasonable degree of programming flexibility. As might be expected, the most flexible portions for defining radio functions in our system are those implemented in baseband digital signal processors (DSPs). Programming flexibility of the system diminishes as one moves from baseband operations (with DSP and FPGA processing) towards the RF end. In the IF section, the system can employ programmable digital down-converters, DSPs and leverage FPGAs to implement algorithms. The system is least flexible in the radio frequency (RF) front end of the system, where the RF equipment offers programmable control of tuning frequency and input and output signal attenuations. Following conventional wisdom, the programmable hardware is more easily reconfigured over a limited range of operation but does not offer the same flexibility that software defined functions afford. The advantage of software defined functions, however, is balanced by challenges presented by real-time implementation issues: the engineer is faced with the task of defining and then implementing algorithms for real-time operation with constraints imposed by buffering, data input/output (I/O) throughput, bus architectures and capacity, processing speeds, and memory size and access times.

### B. Testbed Architecture

The testbed configuration, shown in Fig. 19, consists of two software radio platforms, host PCs for programming and controlling software radio functions, PCs to support MAC and the MAC/IP interface, an Ethernet hub, and PCs hosting client and server applications.

The software radio platform architecture is depicted in Fig. 20. The design is based in part on the architecture proposed by Mitola [72]. The radio physical layers are implemented in a VME rack system populated with commercial off-the-shelf boards to provide functions associated with RF/baseband down- and up-conversion, analog to digital conversion, digital-to-analog converters, and IF and baseband processing.



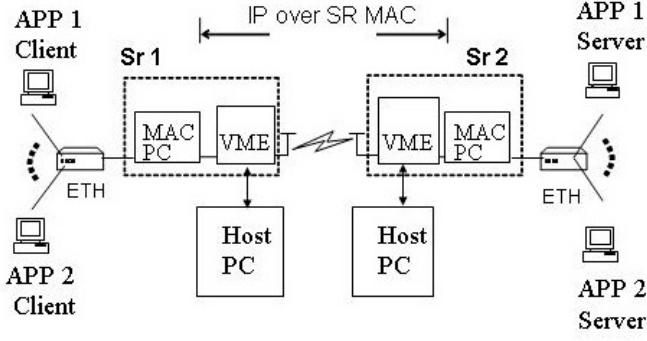


Fig. 19. Software radio testbed configuration.

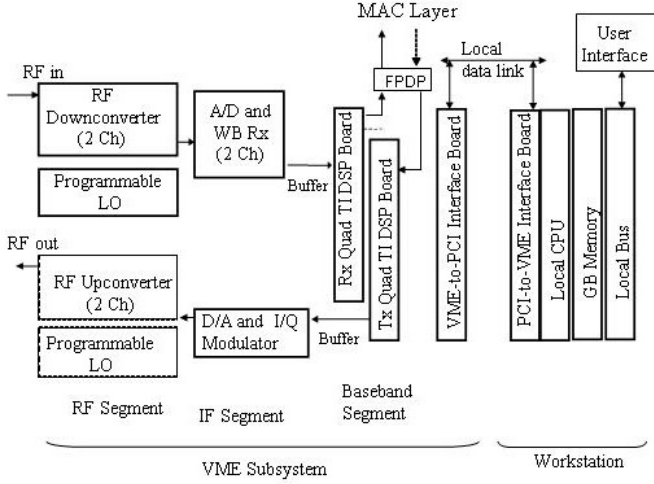


Fig. 20. Software radio platform configuration.

### C. MIMO OFDM IMPLEMENTATION

Software radio-based implementations of OFDM have been reported in literature see for example, [73] [74] [75] [76] [77] [78]). But, as yet, software radio implementations for MIMO OFDM do not appear to be prevalent. In our implementation, the software radios were configured to implement a 2x2 space-time coded MIMO OFDM system, shown in Fig. 21, based on Alamoutis approach [4]. A more complete description of the system is presented in [79]. The left side of the figure depicts the transmitter on a single Quad DSP board. The input to the board is derived from the MAC layer imbedded in a PC through an FPDP I/O link. The transmit functions include data parallelization, QAM mapping, IFFT transformation, space-time coding, and framing. Algorithms associated with these functions are implemented among processors A, B, C, and D, where the functions are distributed as presented in the figure.

The receive functions include time synchronization, frequency offset estimation and compensation, channel estimation and compensation, and symbol demodulation and QAM demapping. These functions are implemented in a separate quad DSP board, where the algorithms are distributed among processors A, B, C, and D according to the figure. The output of this board is passed through an FPDP I/O link to the receive MAC processor that resides in a PC.

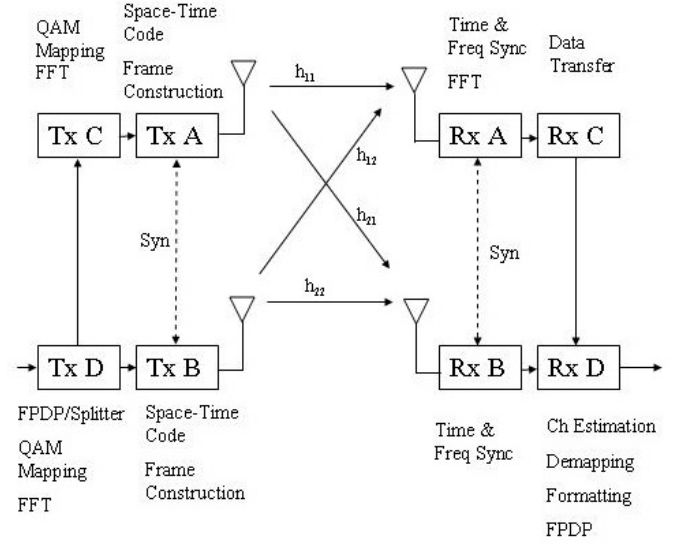


Fig. 21. The configuration of  $2 \times 2$  MIMO-OFDM space-time system.

Typically, receiver processing requires greater computational horsepower than transmit processing, due in large part to synchronization and FEC decoding (if present). The data flow associated with the MIMO-OFDM receive functions in the DSPs are illustrated in Figs. 22 and 23. Fig. 22 shows the processing functions/algorithms associated with Processor A. The same processing is employed in Processor B. Fig. 23 shows the processing associated with Processor D. Processor C serves as a buffer for delivering the output data from Processor A into Processor D.

The associated time budgets associated with the functions are listed in Table I, where the alphanumeric designation t# in the table corresponds to the processing function indicated in the figures above. The time budgets for each function are presented in terms of clock cycles, where each cycle corresponds roughly to 6 ns.

Following synchronization, the maximum achievable throughput of the system depends upon the maximum processing time required by any one processor in the pipeline to process an OFDM symbol. Based on the chart above, one of the processors requires roughly 5 KC for FFT computations, indicating that the system can support complex sample rates as high as 10 MHz.

### D. System Expansion

System scalability was a key design consideration in the development of the testbed system. The MIMO-OFDM system is now undergoing modification to incorporate new features to increase the system bandwidth and the spectral efficiency of the system, and to improve the interference performance and reliability of the system. Power-PC-based processing boards are being integrated into the system to replace the DSP-based processing boards. The new boards offer processing efficiency increases for many functions, particularly for algorithms that can be vectorized. Example gains that have been demonstrated in the system include FFT speeds that are nearly 4 times



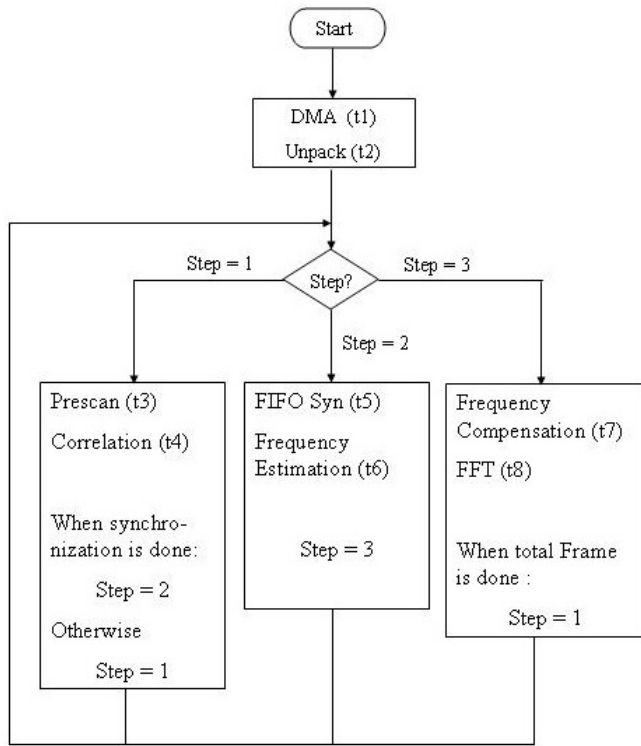


Fig. 22. The data flow chart of Rx.A.

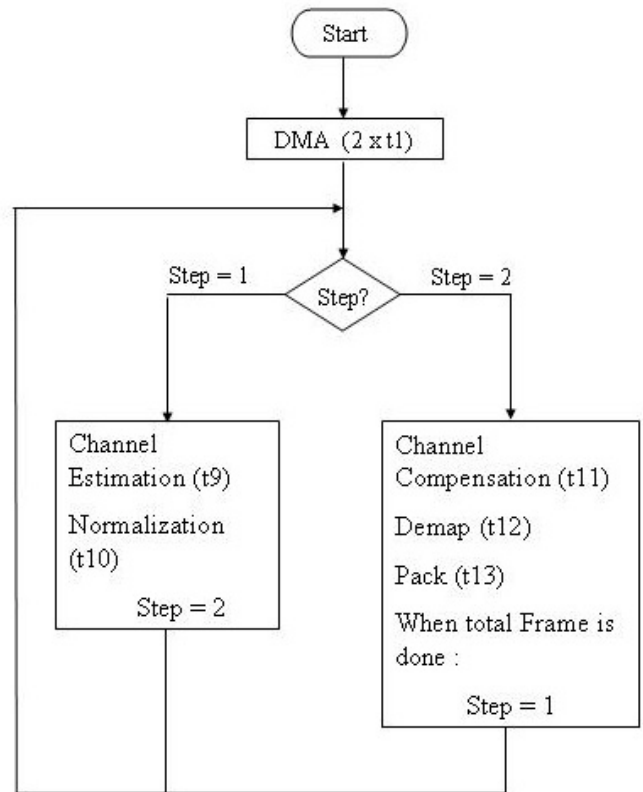


Fig. 23. The data flow chart of Rx.D.

faster than with the DSP boards. Spectral efficiency is to be increased through the utilization of BLAST-type algorithms in a 4x4 MIMO OFDM system. Interference suppression will be achieved with beamswitching antennas that monitor the SINR on each channel. FEC is also being integrated in FPGAs, where proprietary FEC cores for Reed Solomon coding are initially being deployed, but where more advanced FEC cores are planned for integration in the future.

#### E. Extensions to System-on-a-Chip

We have described the implementation and processing performance of a MIMO OFDM system in a software radio testbed. The specific architecture of the system, including the bus design, processor interconnectivity, board interconnectivity, the memory resources, access times and arbitration, and the processing resources associated with the system are largely inflexible and depend on specific vendor designs. Parallel work to the testbed integration work is also being conducted to evaluate alternative bus architectures, memory arbitration, and custom logic in heterogenous multi-processor environments [80] [81]. The purpose of these studies is to determine architectures to enhance the system performance for system-on-a-chip multi-processor implementations. This work is particularly relevant to the design of future SDR systems, which may eventually demand implementation architectures that are scalable (e.g., to accommodate increased transmission bandwidths), and flexible (e.g., to accommodate new functions and algorithms).

## XI. CONCLUDING REMARKS

This paper has discussed a number of physical layer issues relevant for the implementation of broadband MIMO-OFDM systems. We have discussed in detail the peculiar issues relating to MIMO-OFDM synchronization and channel estimation. We then discussed space-time coding strategies for closed loop MIMO-OFDM systems where knowledge of the channel is available at the transmitter. Error correction coding was discussed with an emphasis on high-rate low density parity check codes. Adaptive analog beam forming techniques were discussed that can provide the best possible MIMO channel environment. Finally, the paper discussed a software radio test bed at Georgia Tech for MIMO-OFDM.

## ACKNOWLEDGEMENTS

The authors wish to thank Apurva Mody for his contributions to Sections II, III, and IV, and Joon Hyun Sung for his contributions to Sections VI. Acknowledgement is also given to Dr. Weidong Xiang for his software radio implementation contributions to the research.

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TABLE II  
FUNCTION TIME BUDGETS

	Processing	Time Budget in Cycles $1\text{ Cycle} = 1/167\text{MHz}$ $= 5.988\text{ns}$
t1	DMA Transfer of 320 Complex Samples Complex Samples from IO FIFO to IDRAM	320C
t2	Unpacking 320 Complex Samples to IQ (in idram)	1KC
t3	Detect the approximate frame start sample using energy	2KC
t4	Use cross-correlation to find the frame start sample	3KC
t5	FIFO synchronization to OFDM symbols	640C
t6	Frequency estimation	3KC
t7	Frequency Compensation	3KC
t8	FFT (radix 4) and bit reversal	4KC + 800C
t9	Channel Estimation	9KC
t10	Normalization	3KC
t11	Channel Compensation	3KC
t12	64 QAM De-mapping	3KC
t13	Packing	3KC
Ta	Complex Conjugate Vector Production (256 Complex Numbers)	700C
Tb	Complex Vector Production (256 Complex Numbers)	700C
Tc	Vector Sum (256 Complex Numbers)	700C

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