

(∞, C) -ISOMETRIC OPERATORS

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Abstract. In this paper we study properties of (∞, C) -isometric operators. In particular, we prove that if T is an (∞, C) -isometry and Q is a quasinilpotent operator, then $T + Q$ is an (∞, C) -isometry under suitable conditions. Moreover, we show that the class of (∞, C) -isometric operators is norm closed. Finally, we investigate properties of products and tensor products of (∞, C) -isometric operators.

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