

Cavity QED with a Bose-Einstein condensate

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Collaborators

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(since 2007)

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Postdoc:

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PhD:

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Postdoc:

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Correlations at the Bose-Einstein phase transition

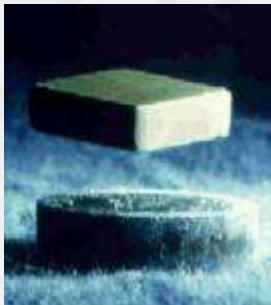
2nd Order Phase Transitions



uniaxial magnet



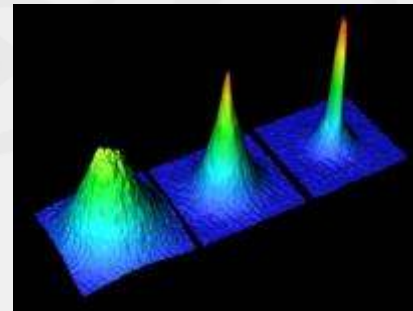
critical opalescence



superconductor

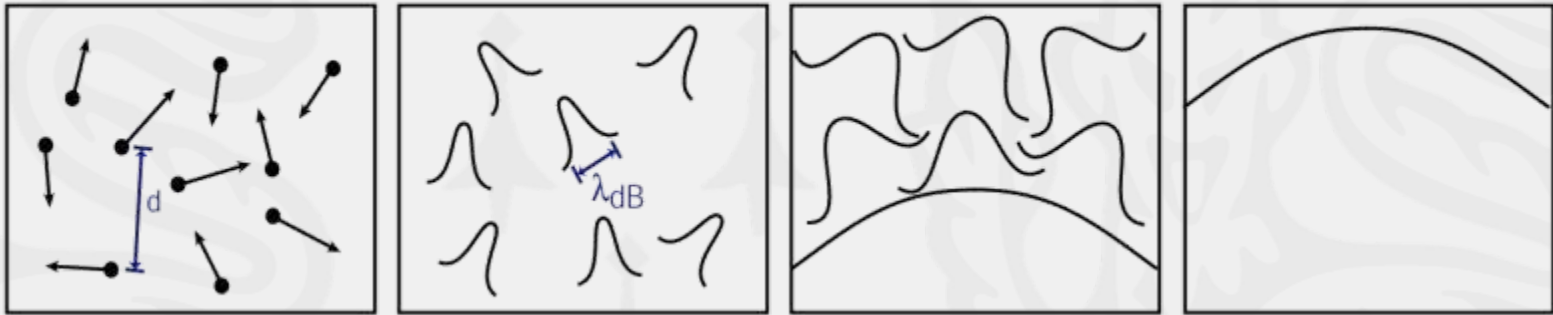


superfluid He



Bose-Einstein condensation

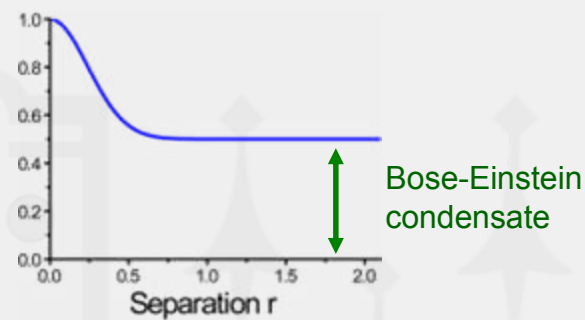
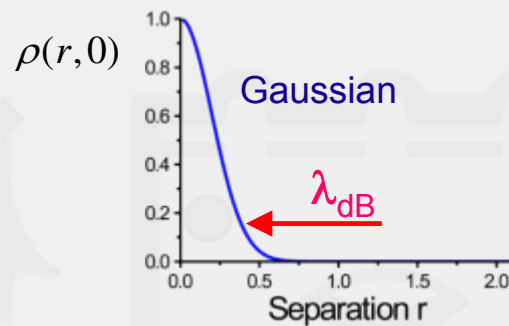
What is a Bose-Einstein condensate?



$$\rho(r_1, r_2) = \langle \hat{\Psi}^\dagger(r_1) \hat{\Psi}(r_2) \rangle$$

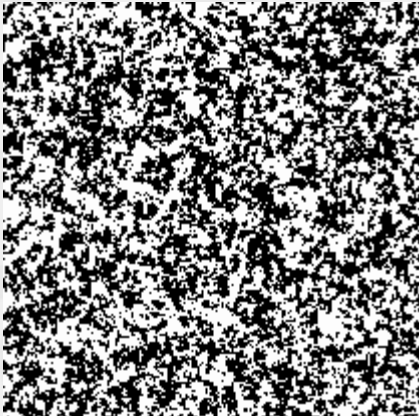
$$= \underbrace{\Psi^*(r_1) \Psi(r_2)}_{\text{condensate wavefunction}} + \underbrace{\langle \delta \hat{\Psi}^\dagger(r_1) \delta \hat{\Psi}(r_2) \rangle}_{\text{fluctuations}}$$

Penrose and
Onsager (1956)

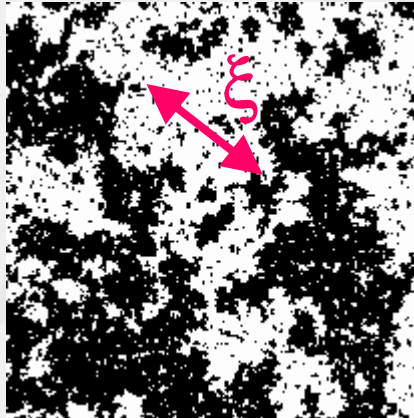


What drives a phase transition?

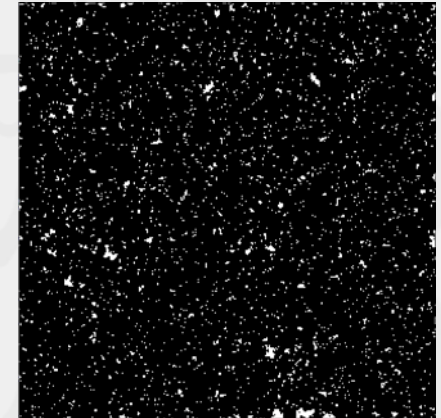
$T > T_c$



$T = T_c$

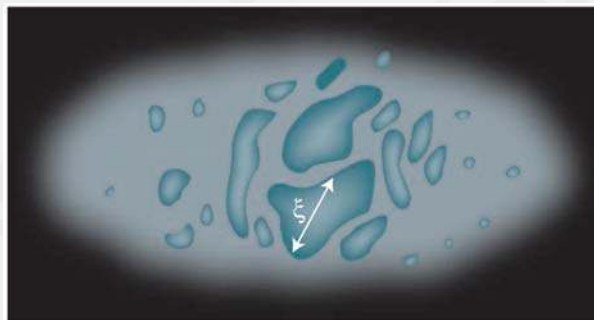


$T < T_c$



Correlation length ξ : typical range in which fluctuations are correlated

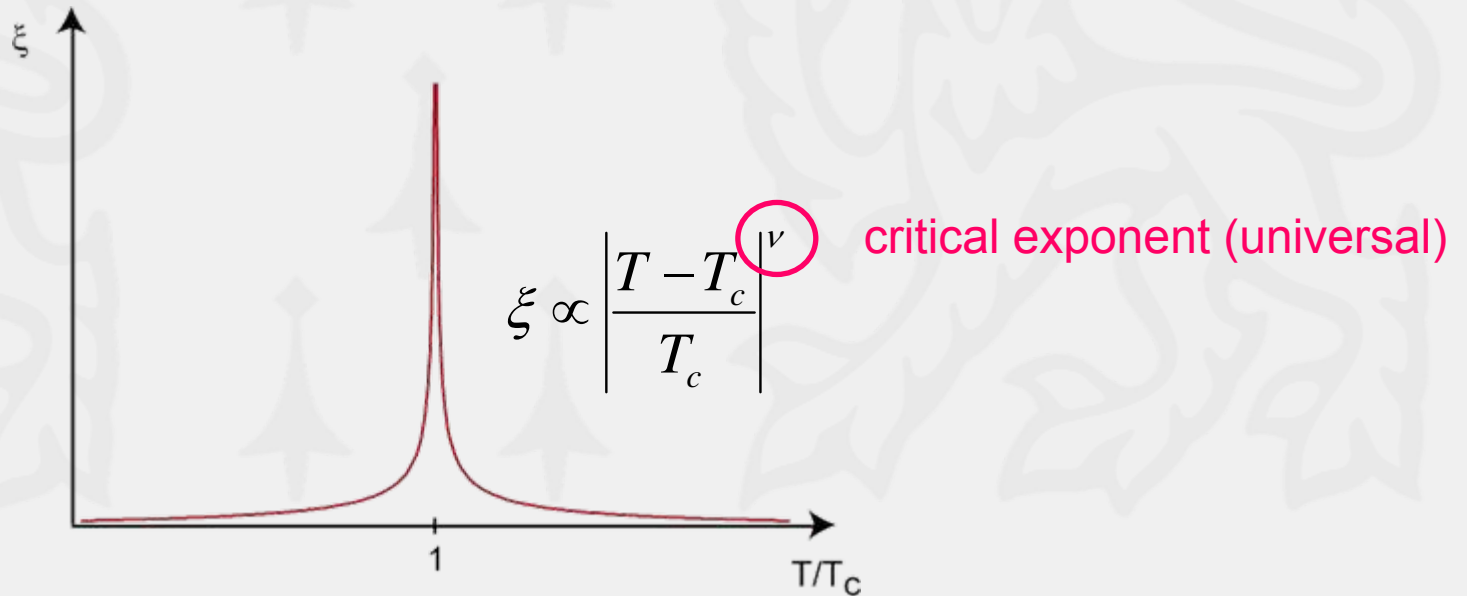
in BEC:



Ising model simulation from <http://www.ibiblio.org/e-notes/>

Critical correlations

Correlation length ξ is temperature dependent:



Decay of the correlation function close to T_c : $\rho(r, 0) \propto \frac{\exp(-r/\xi)}{r^{d-2+\eta}}$

i.e. algebraic decay at T_c

Critical exponents and universality

- Divergences at the phase transition $\left| \frac{T - T_c}{T_c} \right|^{-x}$

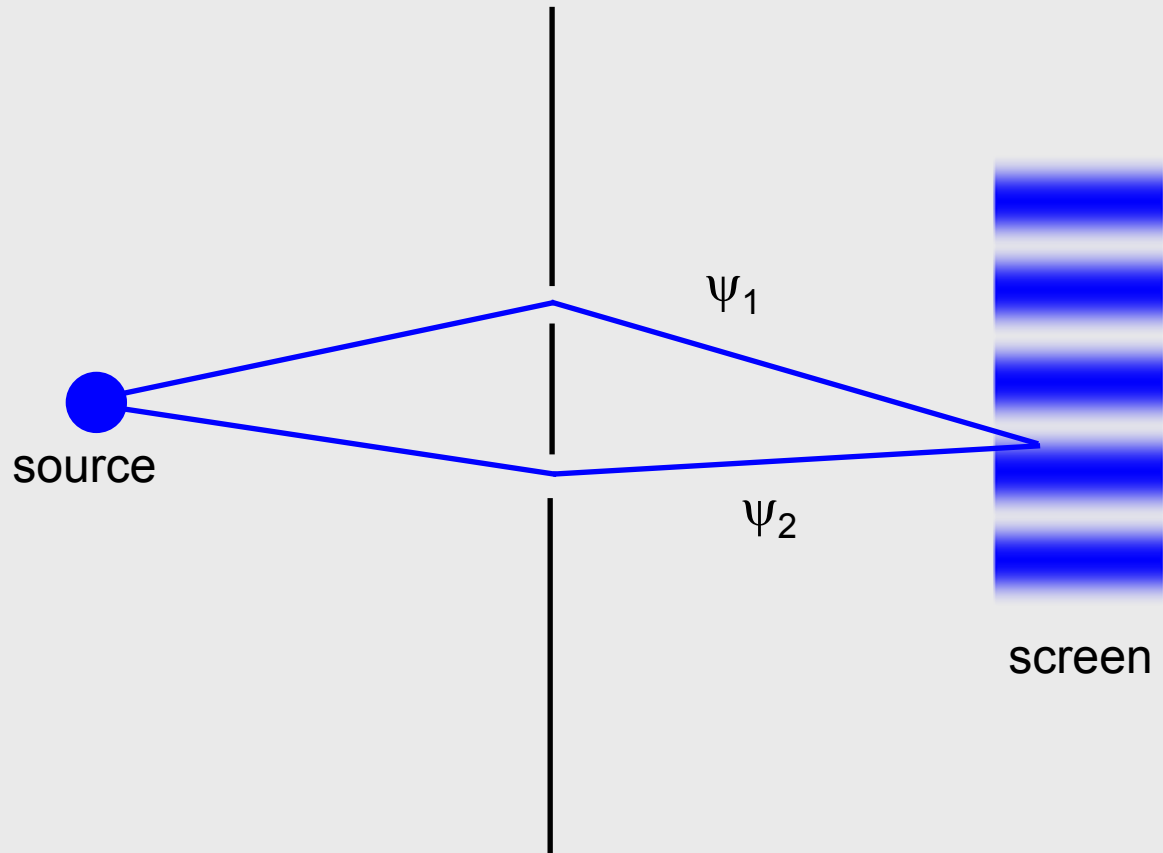
$x = \alpha$	β	γ	ν
specific heat	magnetization	susceptibility	correlation length

- Scaling relations e.g. $\nu d = 2 - \alpha$ (d: dimension)
- Systems in the same universality class have the same exponents.

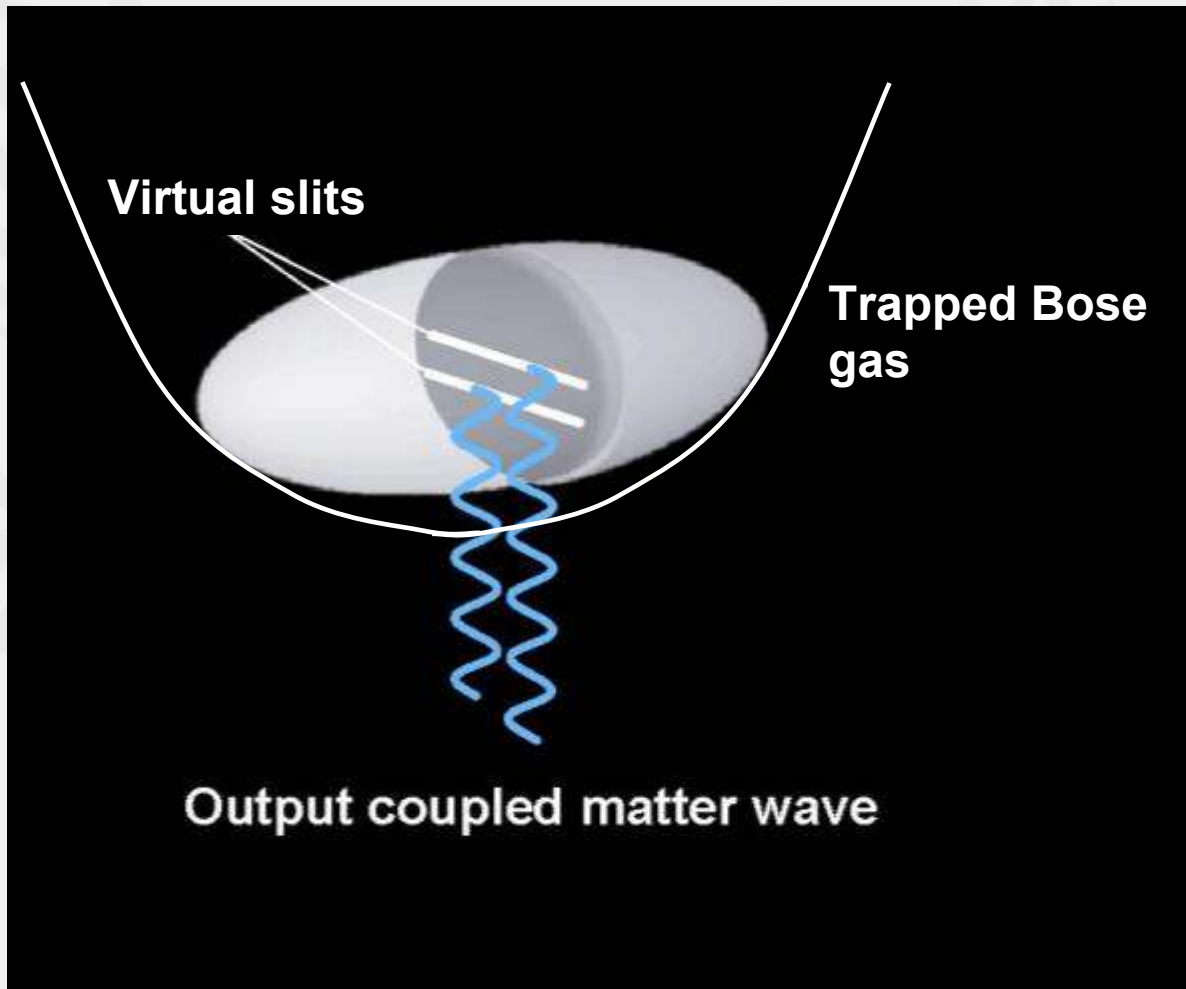
How to measure this?



Young's double slit experiment



Double slit experiment



Trapped Bose gas

Interfering
atomic beams

Single atom
detector
(optical cavity)

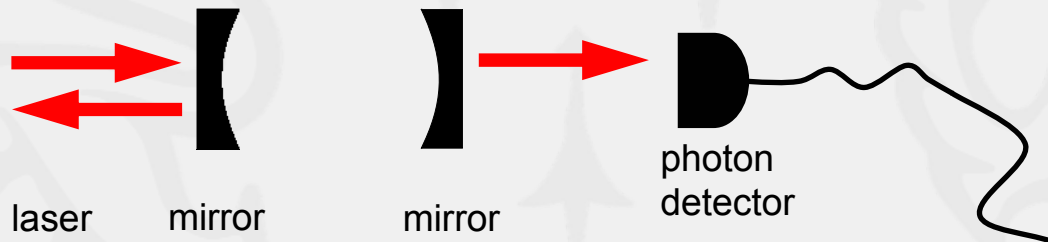
I. Bloch, T. Hänsch, T. Esslinger, Nature 403, 166 (2000).

T. Bourdel, T. Donner, S. Ritter, A. Öttl, M.K., T. Esslinger, Phys. Rev. A 73, 043602 (2006).

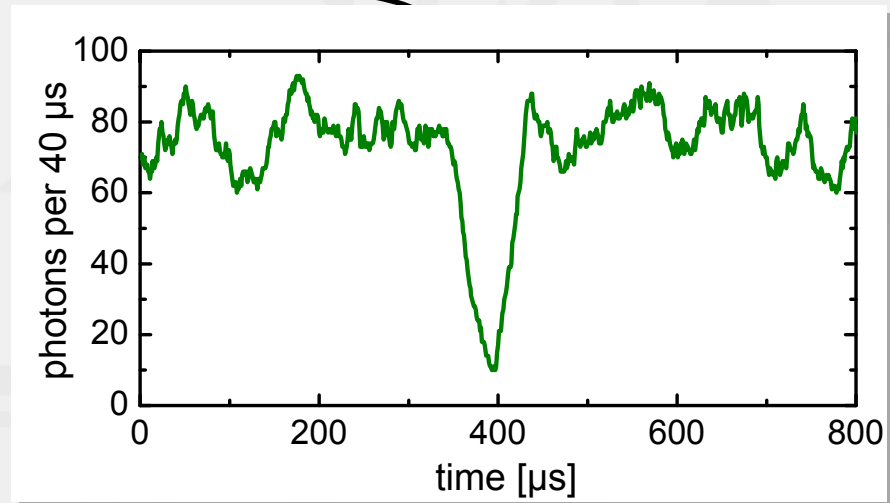


Single atom detection in cavity-QED

● single atom



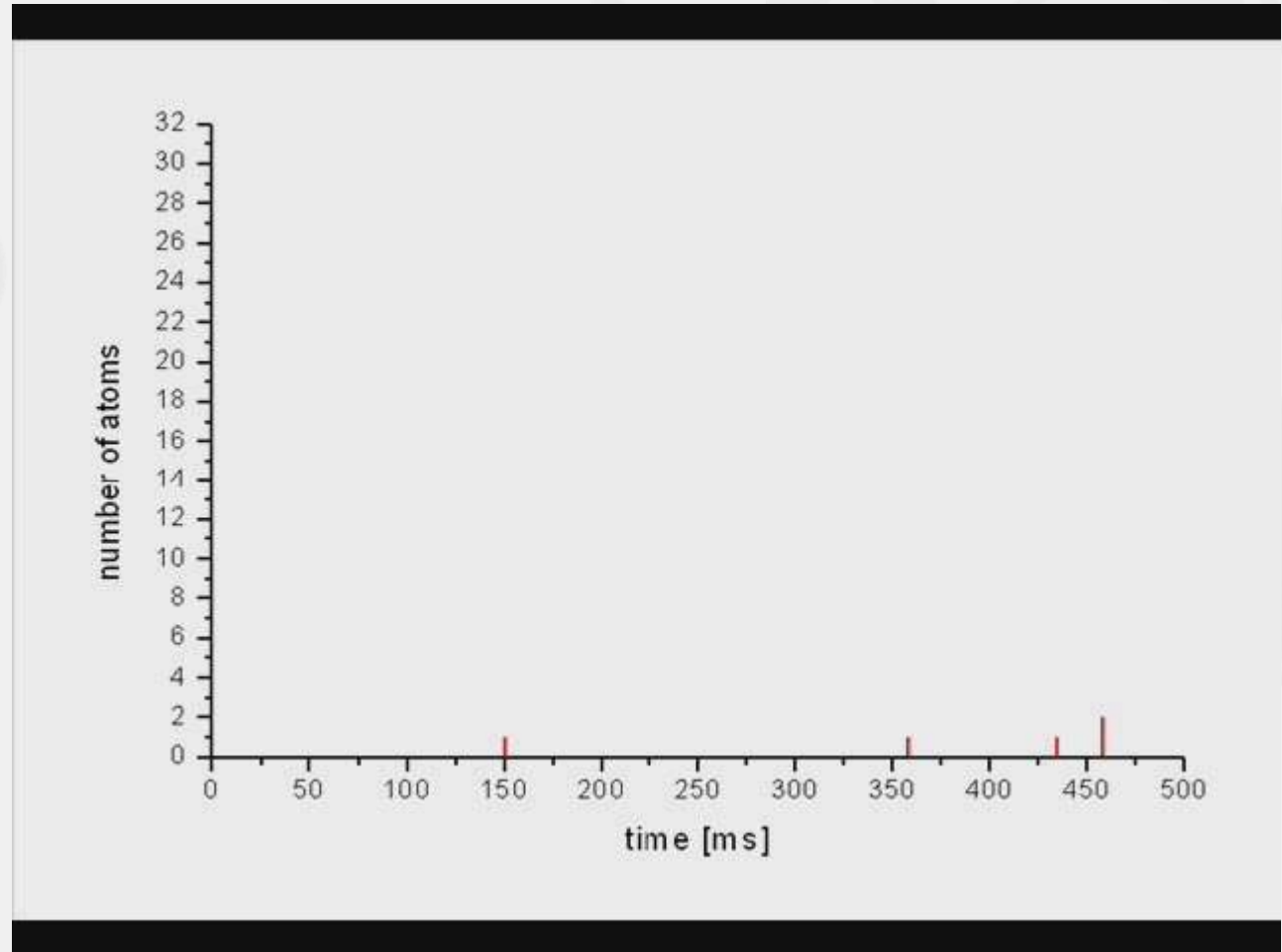
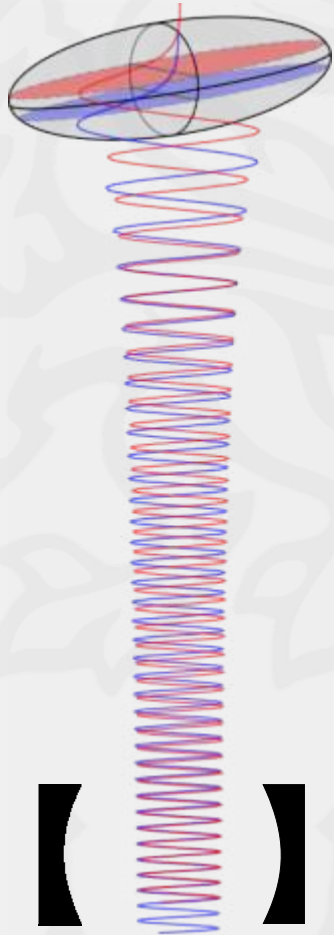
Cavity transmission:



First demonstration: H. Mabuchi et al., *Opt. Lett.* **21**, 1393 (1996)

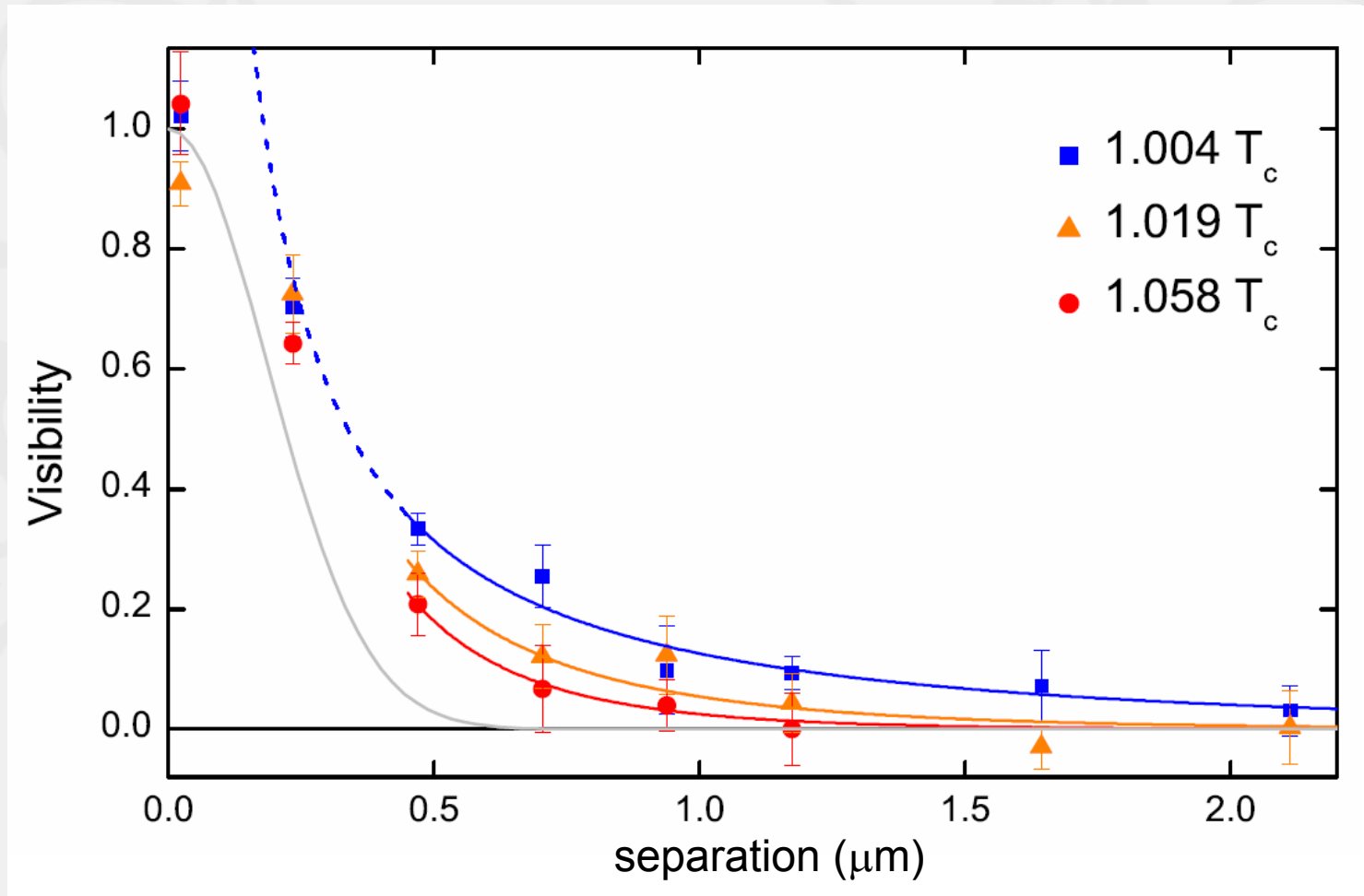


An interference pattern from single atoms

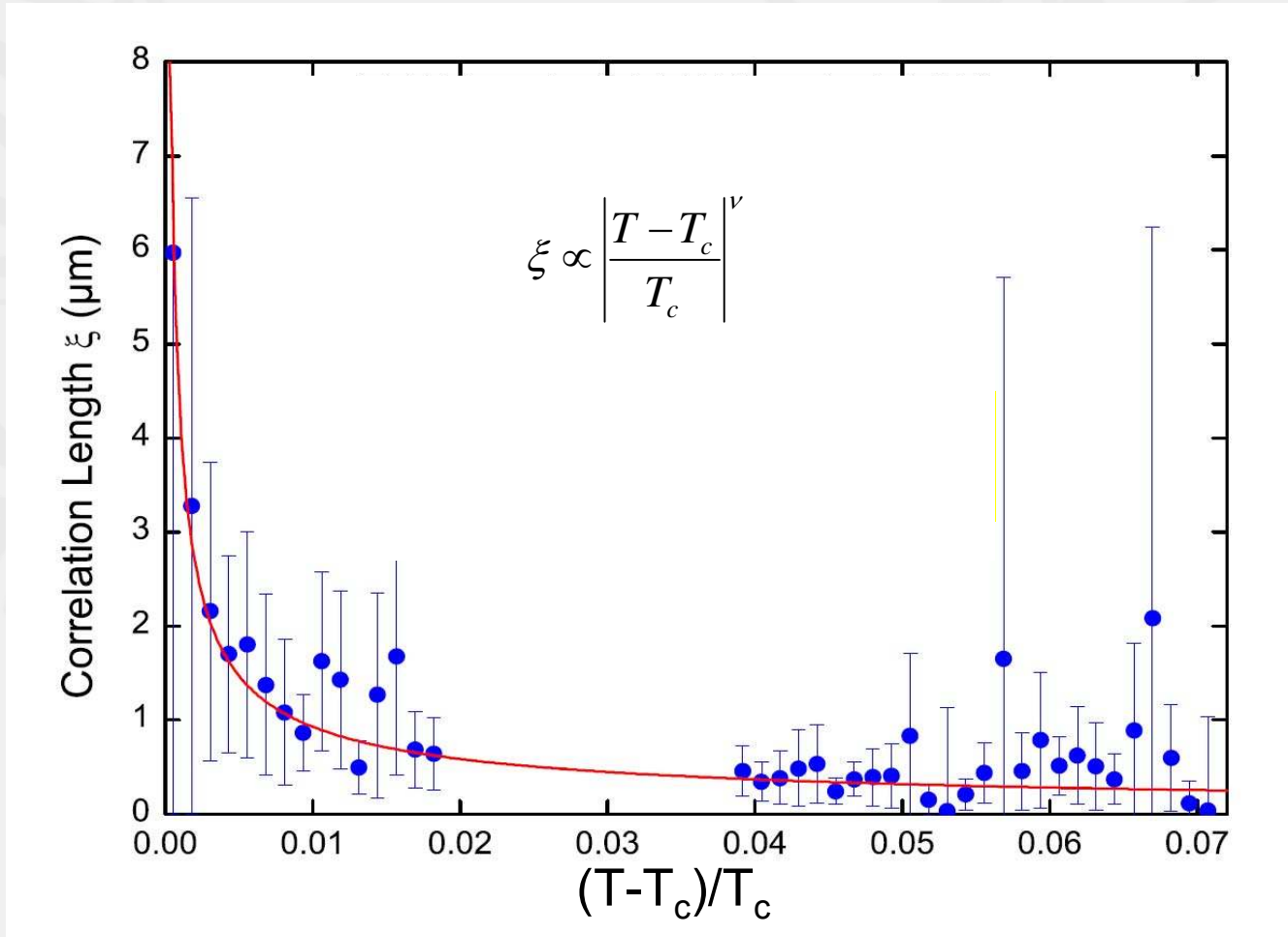


T. Bourdel, T. Donner, S. Ritter, A. Öttl, M.K., T. Esslinger, Phys. Rev. A 73, 043602 (2006).

Correlations near T_c



Divergence of ξ



T. Donner, S. Ritter, T. Bourdel, A. Öttl, M.K., T. Esslinger, Science 315, 1556 (2007).

The critical exponent ν

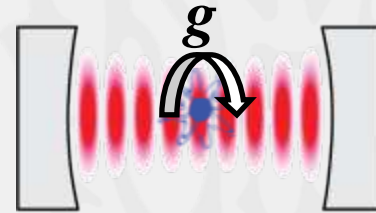
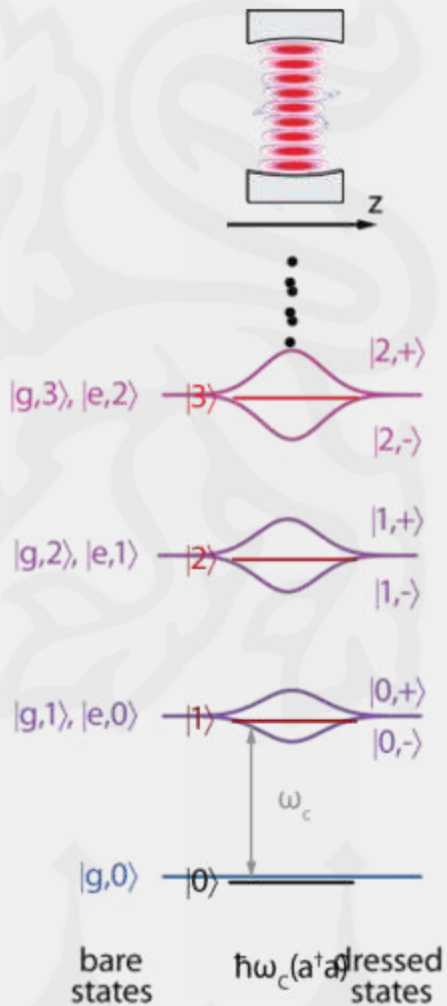
System	ν
Ideal Bose gas in a box:	1
Ideal Bose gas in a harmonic trap:	0.5
Landau's theory of phase transitions: (homogeneous & interacting)	0.5
RG theory of the XY universality class: (homogeneous & interacting) Camprostrini et al., PRB 63, 214503 (2001).	0.67155(3)
Determined in liquid Helium: Lipa et al., PRB 68, 174518 (2003).	0.6705(6)
Now measured in a harmonic trap: with a dilute Bose gas	0.67(13)

ten orders of
magnitude
different
in density !

Universality works 😊

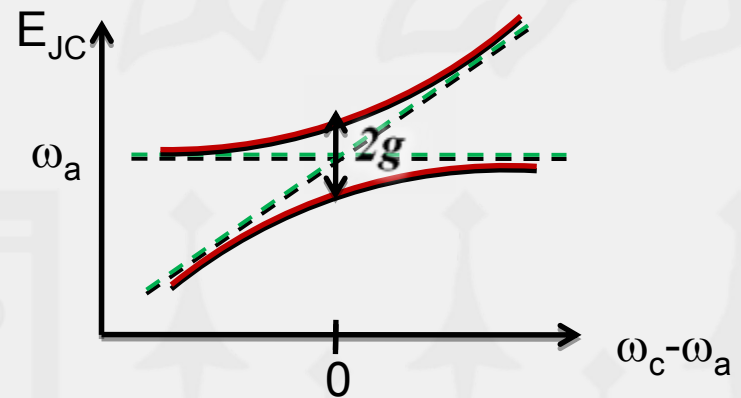
A new collective state of light and matter

Single atom cavity QED

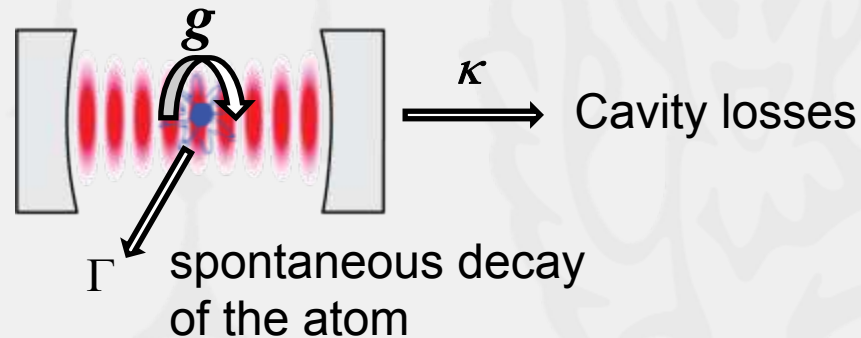


Jaynes-Cummings model

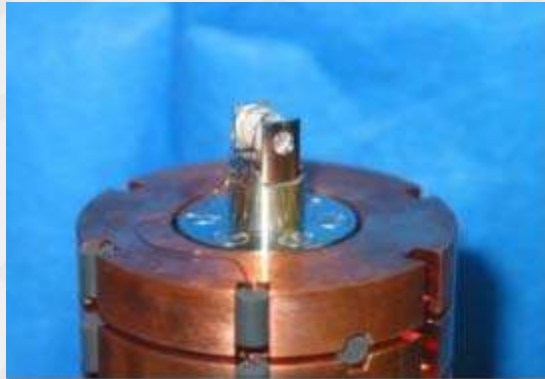
$$H_{JC} = \frac{1}{2} \hbar \omega_a \hat{\sigma}_z + \hbar \omega_c \hat{a}^\dagger \hat{a} + \hbar g(r) [\hat{\sigma}_+ \hat{a} + \hat{a}^\dagger \hat{\sigma}_-]$$



Dissipation and strong coupling



Strong coupling regime of cavity QED: $g \gg \kappa, \Gamma$



$$g = 2\pi \cdot 10.4 \text{ MHz}$$

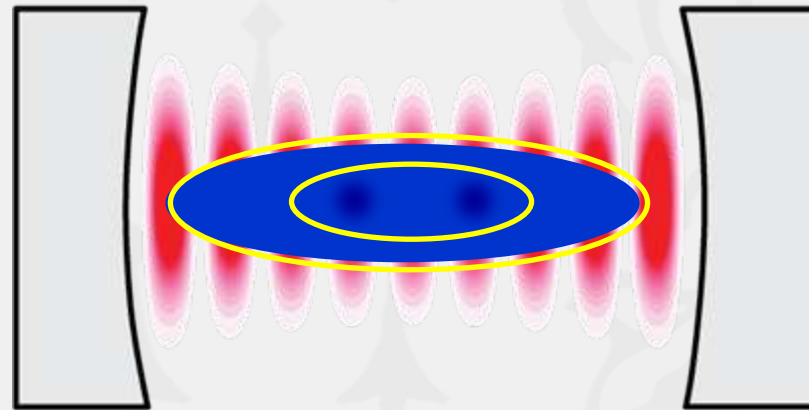
$$\Gamma = 2\pi \cdot 3.0 \text{ MHz}$$

$$\kappa = 2\pi \cdot 1.4 \text{ MHz}$$

related work: M. Chapman, S. Haroche, E. Hinds, H.J. Kimble, D. Meschede, J. Reichel, G. Rempe, D. Stamper-Kurn, H. Walther ...

From one to many

Cavity induced
interaction & entanglement



One excitation coherently shared by
 10^5 indistinguishable atoms.

Proposals by Cirac & Zoller, Moelmer, ...

Cavity QED with many identical atoms

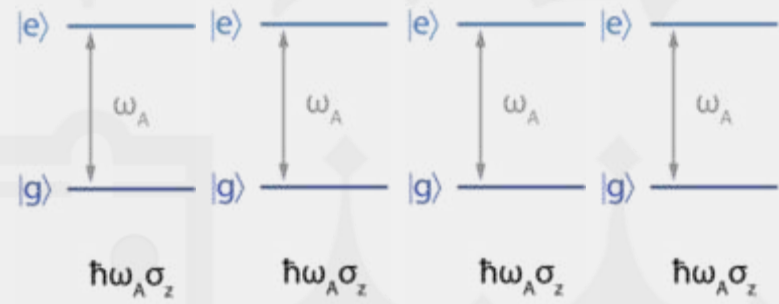
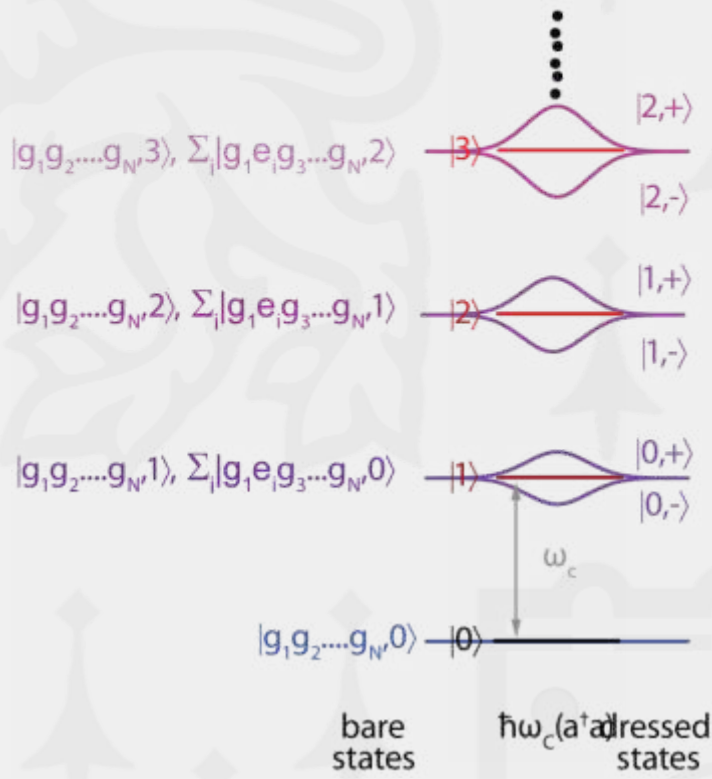


Tavis-Cummings model

$$H_{TC} = \hbar\omega_c \hat{a}^\dagger \hat{a} + \sum_{i=1}^N \frac{1}{2} \hbar\omega_a \hat{\sigma}_{i,z} + \hbar g(r_i) [\hat{\sigma}_{i,+} \hat{a} + \hat{a}^\dagger \hat{\sigma}_{i,-}]$$

Collective mode splitting
for N atoms (and weak excitation)

$$\pm \sqrt{N} g$$



Atomic ensembles in optical cavities

- **Cavity as a light-matter interface in QIP:**
Conversion of a single photon (“flying qubit”) into a collective atomic excitation (“memory qubit”) and back

$$\text{SNR} \sim g^2/\kappa\Gamma \rightarrow \text{enhancement of factor } N !$$

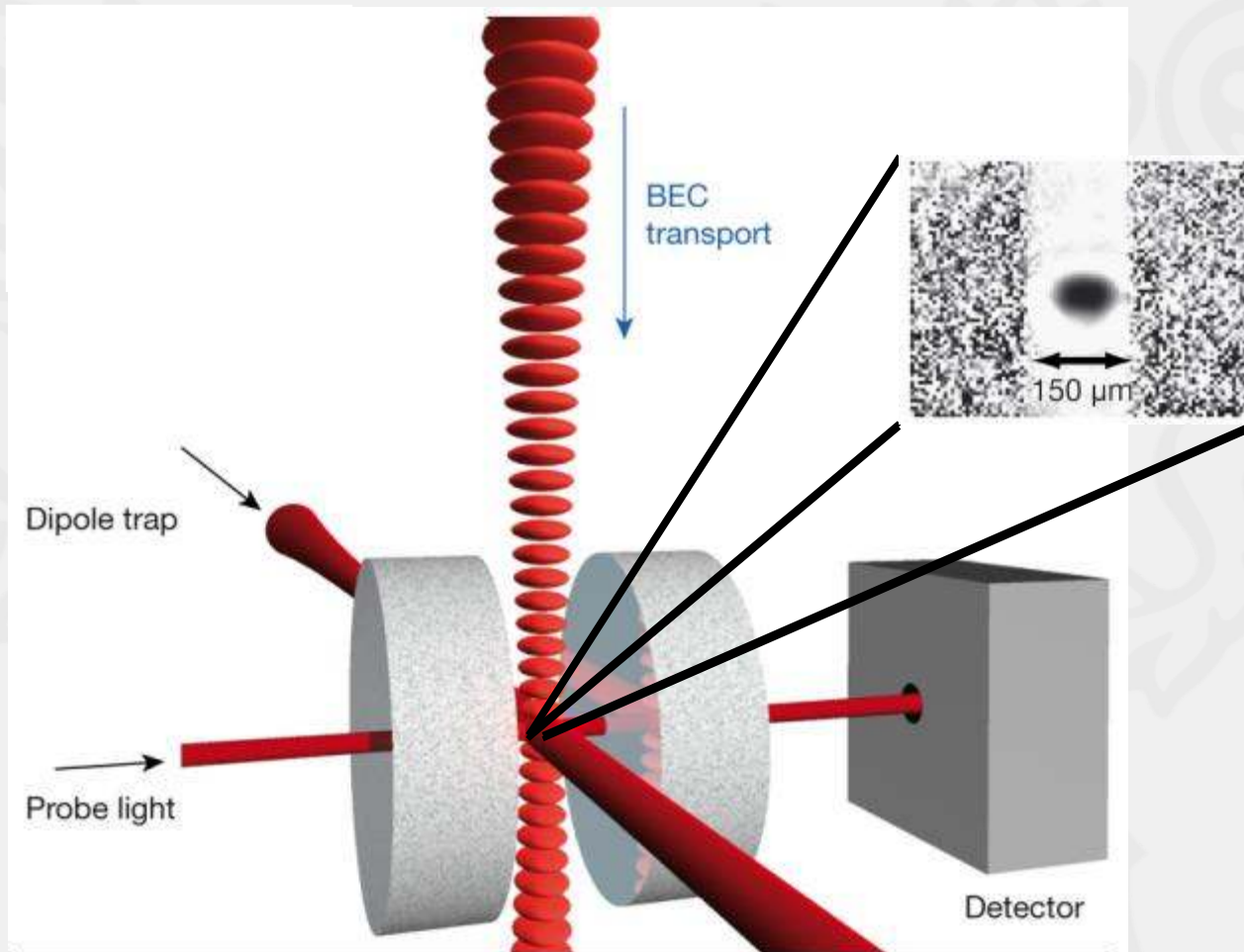
(exp. realized for a low-Q cavity: Vuletic et al., PRL (2007))

- **Nonlinear optics: huge Kerr non-linearities**
(with ultracold atoms: Stamper-Kurn, Chapman, ...)
- **Spin squeezing, measurement induced quantum manipulations, ...**
(e.g. Mabuchi et al., Science (2004), Zoller et al. PRL (2001), ...)

What can quantum degenerate gases offer?

- No motional decoherence
- Highest densities
- Indistinguishable atoms, all atoms couple exactly equal to the cavity mode
- Correlated quantum phases in optical lattices:
new probing techniques, new interactions
(Theory: H. Ritsch, P. Meystre, M. Lewenstein, I. Carusotto ...)

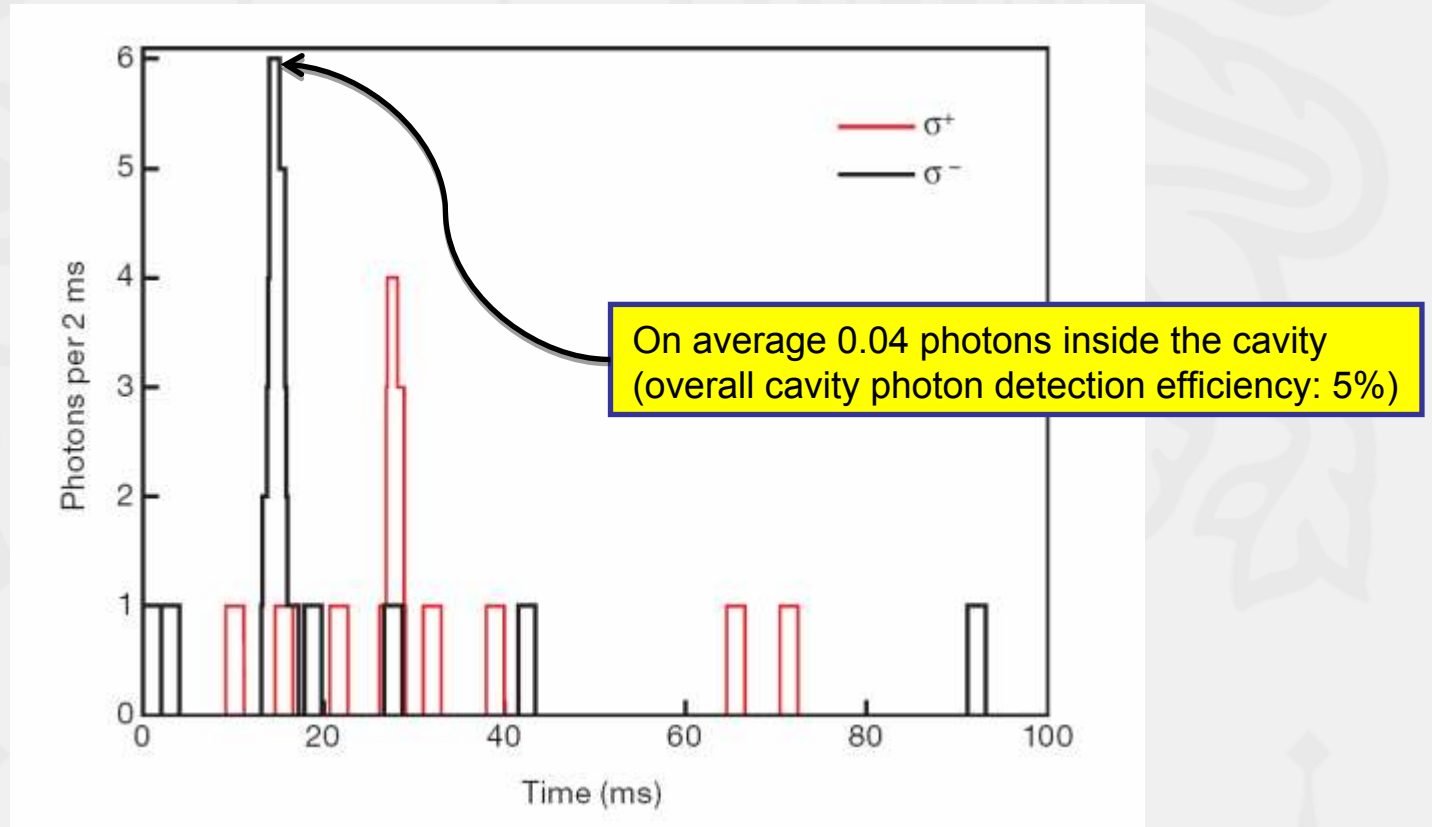
Delivery of the Bose-Einstein condensate



F. Brennecke, T. Donner, S. Ritter, T. Bourdel, M. K., T. Esslinger, Nature 450, 268 (2007)

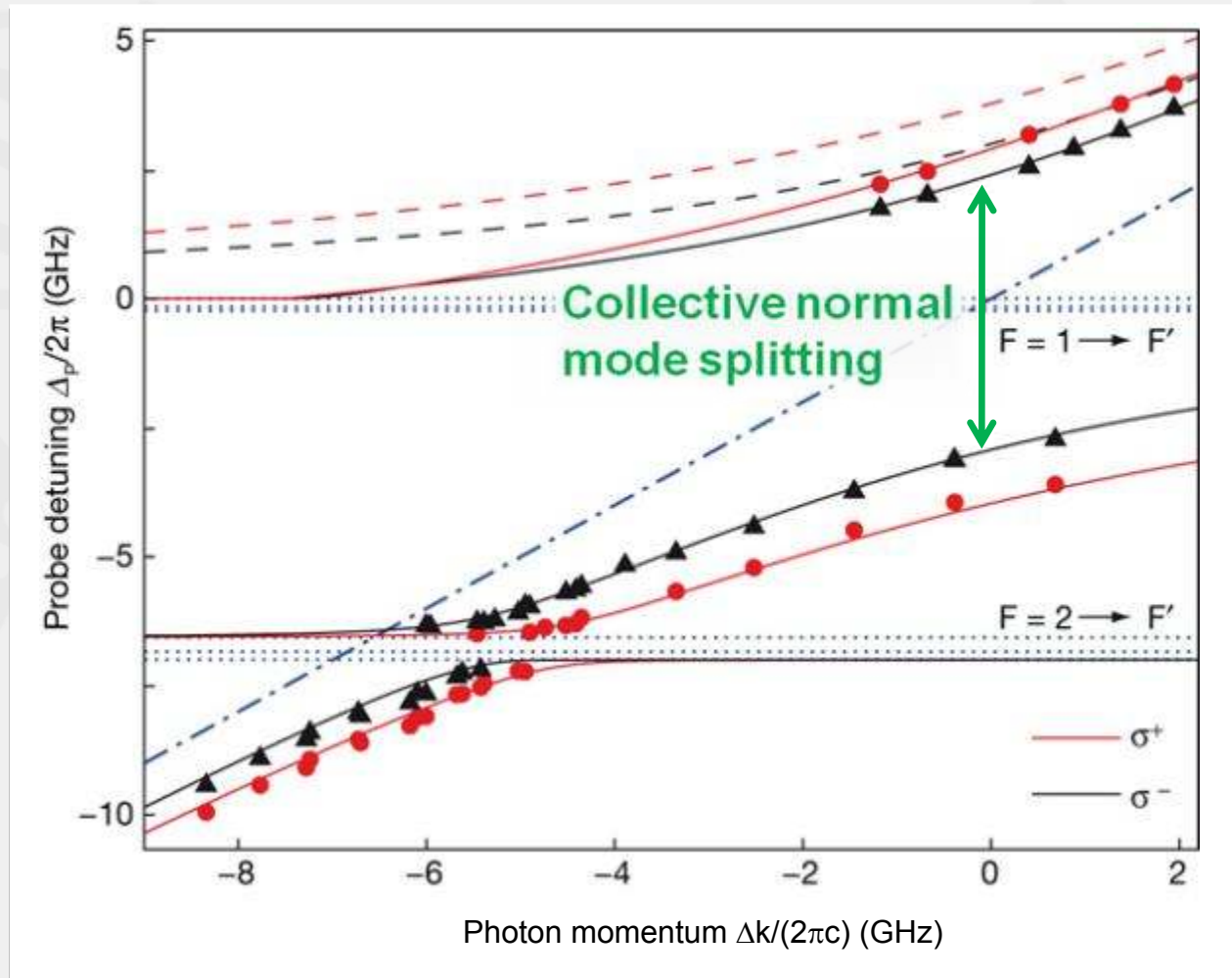


Sample measurement



Probe laser scan rate 25 MHz/ms

Cavity spectrum



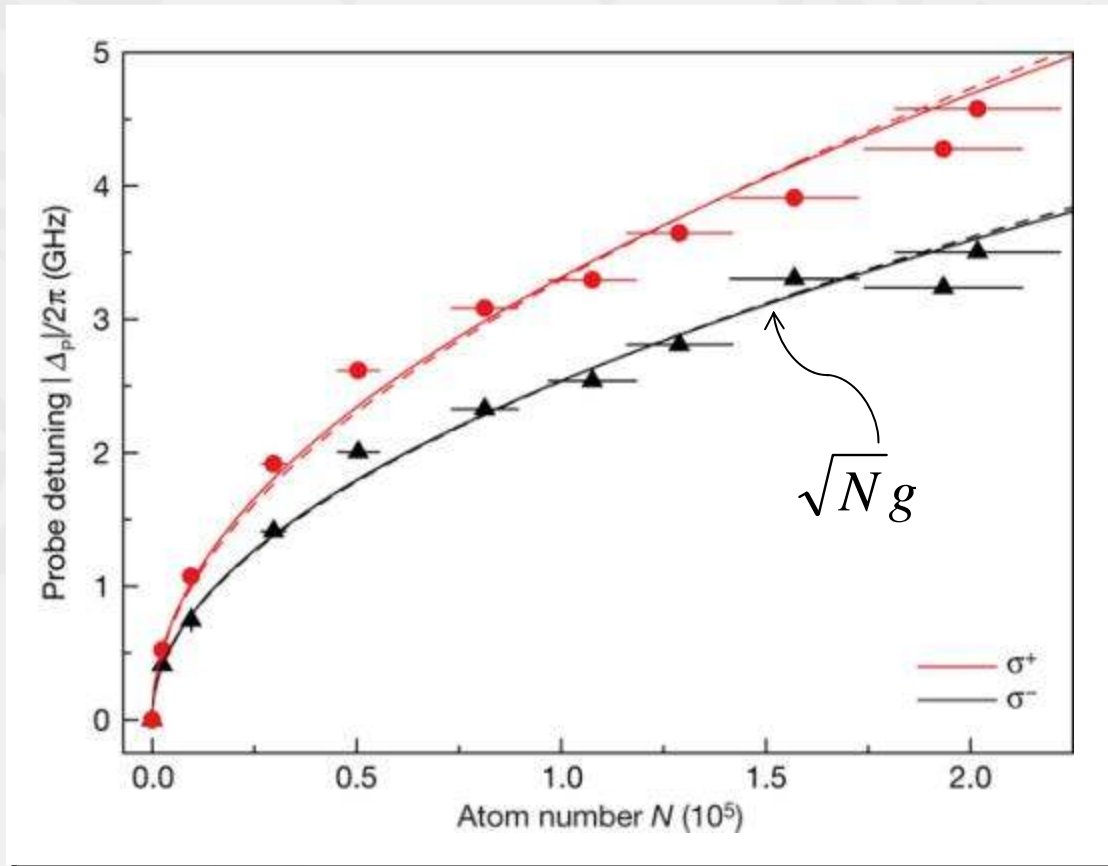
photon

“exciton”

“exciton”

F. Brennecke, T. Donner, S. Ritter, T. Bourdel, M. K., T. Esslinger, Nature 450, 268 (2007).
See also: Y. Colombe et al. Nature 450, 271 (2007).

Collective mode splitting



Summary

- Measurement of the critical exponent of a trapped weakly interacting Bose gas
- Eigenenergy spectrum of a Bose-Einstein condensate in an ultra-high finesse cavity