



Centrosymmetric to noncentrosymmetric structural transformation in a superconducting high-entropy alloy due to carbon addition

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ABSTRACT The tetragonal σ phase is one of the most frequently occurring phases in transition metal alloys. However, the effect of carbon addition in σ type high-entropy alloys (HEAs) has not been studied to date. Here we report the observation of structural transformation by adding carbon in the superconducting $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}$ HEA (critical temperature $T_c = 4.87$ K). It is found that the $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEA adopts the centrosymmetric σ type structure for $0 \leq x \leq 2$, but transforms into the noncentrosymmetric β -Mn type structure for $16 \leq x \leq 20$. The transformed β -Mn type HEA also displays bulk superconductivity with a higher T_c of 5.34 K and an upper critical field approaching the Pauli paramagnetic limit. In addition, the structural transformation is attributed to the decrease in valence electron concentration as well as the increase in lattice distortion and mixing entropy due to carbon addition. Our results not only provide a rare example of centrosymmetric to noncentrosymmetric structural transformation in HEAs, but also consolidate that non-metallic carbon is an effective additive for tuning the structure and physical properties of HEAs.

Keywords: high-entropy alloys, structural transformation, carbon adding, superconductivity, noncentrosymmetric

INTRODUCTION

High-entropy alloys (HEAs) have been the subject of intensive studies over the past two decades as an emerging class of multicomponent alloys [1–7]. In contrary to traditional alloys based on one or two elements, HEAs are composed of at least five principled elements whose atomic concentrations vary from 5% to 35%. This large number of constituent elements results in increased mixing entropy, which overcomes the formation enthalpy for intermetallic compounds and leads to the formation of disordered solid solutions. So far, HEAs have been found in various crystal structures, including face-centered-cubic (fcc) [1,2], body-centered-cubic (bcc) [1,2], hexagonal-closed packed (hcp) [1,2], CsCl type [8], α -Mn type [9,10], σ type [11,12] and A15 type [13,14]. Besides their diverse crystal structures, HEAs also display a range of interesting mechanical and physical properties, such as the combination of ductility and high strength [15,16], enhanced corrosion and oxidation resistance

[17–20], exceptional thermal stability [21,22], and robust type-II superconductivity [23,24].

Recently, the interaction between HEAs and carbon has attracted increasing attention [25–32]. Given its small atomic radius, carbon prefers to occupy the interstitial position, causing an expansion of the lattice. On one hand, this leads to solid solution strengthening and hence an enhancement in micro-hardness of HEAs. On the other hand, the lattice expansion may induce a change in the electronic ground state, which allows for a tuning of their physical properties. So far, both these effects have been found in fcc [32] and bcc [31] HEAs. More remarkably, a transformation from the hcp structure to the fcc one is found to occur by adding carbon in the Mo-Re-Ru-Pd-Pt HEAs [32]. In addition, both the hcp and transformed fcc HEAs become superconducting and the key factors that control superconductivity are essentially the same despite their different structures. Given the structural diversity of HEAs, it is of significant interest to see whether a structural transformation can be induced by adding carbon in other structurally different HEAs.

The tetragonal σ phase is one of the most frequently occurring phases in transition metal alloys and of interest from both fundamental and application points of view [33]. As such, considerable efforts have been devoted to establishing the criteria for σ phase formation in HEAs [11,12,34,35]. However, no carbon added σ type HEA has been investigated to date. Here we report the effect of carbon addition on the structure and physical properties of the $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}$ HEA, which adopts a σ type structure and exhibits bulk superconductivity below 4.87 K. It is found that, upon carbon addition, the $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEA transforms into the noncentrosymmetric cubic β -Mn type structure for $16 \leq x \leq 20$, which also becomes superconducting with an almost x -independent T_c of 5.34 K and an upper critical field around 9.3 T. A comparison is made between the phase stability of σ type and β -Mn type HEAs, and its implication on the origin of structural transformation is discussed.

EXPERIMENTAL SECTION

Ingots of $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs with $0 \leq x \leq 25$ were prepared by the standard arc-melting method. Stoichiometric amounts of high-purity Ta (99.9%), Mo (99.9%), W (99.9%), Re

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(99.99%), Ru (99.9%) and C (99.5%) powders were mixed thoroughly and pressed into pellets in an argon filled glove-box. The pellets were then melted four times in an arc furnace, followed by rapid cooling on a water-chilled copper plate. The phase purity of the resulting samples was checked by powder X-ray diffraction (XRD) at room temperature using a Bruker D8 Advance X-ray diffractometer with Cu K α radiation. The structural refinements were performed using the Le Bail method with the JANA2006 programme [36]. The sample morphology, chemical composition and electron backscatter diffraction (EBSD) were investigated on a Zeiss Gemini 450 analytical field emission scanning electron microscope (SEM) equipped with an energy dispersive X-ray (EDX) spectrometer. The microstructure was examined on an FEI Tecnai G2 F20 S-TWIN transmission electron microscope (TEM). Electrical resistivity and specific heat measurements were carried out on a Quantum Design Physical Property Measurement System (PPMS-9 Dynacool). Magnetization measurements were performed on a Quantum Design Magnetic Property Measurement System (MPMS3).

RESULTS AND DISCUSSION

Fig. 1a shows the room-temperature XRD patterns for the series of Ta₁₀Mo₅W₃₀Re₃₅Ru₂₀C_x HEAs with x up to 25, and the data are shown with increasing carbon content x from bottom to top. One can see that the addition of carbon results in a drastic change in the crystal structure and there exist two separated single-phase regions at $0 \leq x \leq 2$ and $16 \leq x \leq 20$. In the former region, all the diffraction peaks correspond to the tetragonal σ

type structure with the $P4_2/mnm$ space group. The refined lattice parameters are $a = 9.6051(3)$ Å, $c = 4.9871(1)$ Å and $a = 9.6064(3)$ Å, $c = 4.9885(1)$ Å for $x = 0$ and 2, respectively. It thus seems that the σ phase can accommodate a small amount of carbon, leading to a lattice expansion. In the latter region, however, the number of diffraction peaks is strongly reduced and the pattern is consistent with the cubic β -Mn type structure (space group $P4_132$). Meanwhile, the cubic lattice constant increases monotonically from 6.8181(1) to 6.8308(1) Å, with increasing x from 16 to 20. Between these two regions ($5 \leq x \leq 12$), the σ and β -Mn type structures are found to coexist, and a small amount of α -Mn type phase is also identified for $x = 5$. At the highest carbon content of $x = 25$, fcc and hcp impurity phases start to appear (marked with different symbols) in addition to the main β -Mn type one. Hence the maximum content of carbon that can dissolve in the HEA is $x = 20$. This is reasonable since, in the β -Mn type structure, the carbon atoms occupy at most one sixth of the total crystallographic sites, which is equivalent of a maximum carbon-to-metal ratio of 20/100. Clearly, a structural transformation is induced by adding carbon in the Ta₁₀Mo₅W₃₀Re₃₅Ru₂₀ HEA.

The phase evolution in Ta₁₀Mo₅W₃₀Re₃₅Ru₂₀C_x is confirmed by structural refinements. Representative results for $x = 0, 5$ and 20 are shown in Fig. 1b–d, and the atomic coordinates used for the refinements are listed in Table 1. In the σ type structure, there are five different crystallographic sites of $2a$ (0, 0, 0), $4g$ (0.3986, 0.6014, 0), $8i_1$ (0.1312, 0.5365, 0), $8i_2$ (0.0661, 0.2607, 0), and $8j$ (0.3173, 0.3173, 0.2480), and the occupancy of transition metal atoms at each site is fixed according to their stoichiometry.

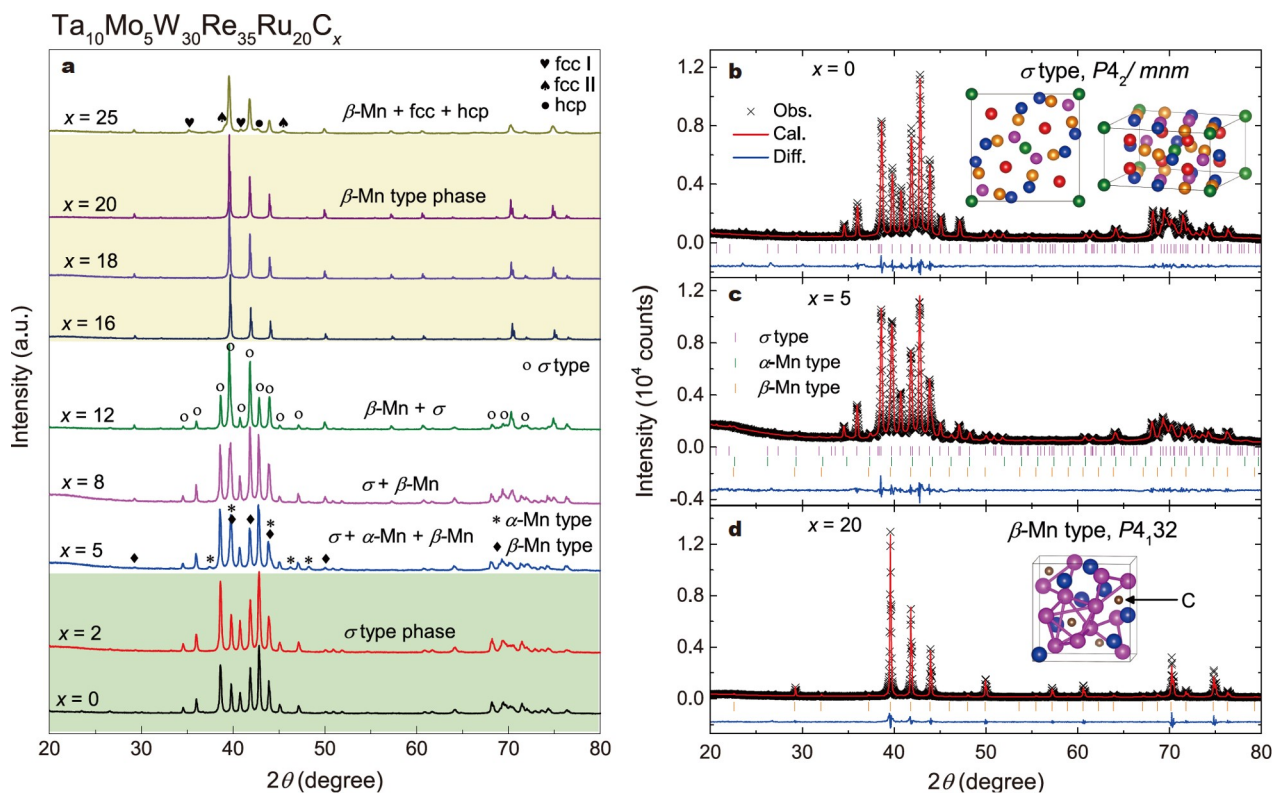


Figure 1 (a) Evolution of room-temperature XRD patterns with carbon content x for the Ta₁₀Mo₅W₃₀Re₃₅Ru₂₀C_x HEAs. The impurity phases for representative samples ($x = 5, 12$ and 25) are marked with different symbols, respectively. (b–d) The structural refinement profiles for the HEAs with $x = 0, 5$ and 20, respectively. In panel (b), the insets show the schematic structures of the σ type phase perpendicular and parallel to the c -axis. In panel (d), the inset shows the schematic structure of the β -Mn type phase and the interstitial C atom is marked by the arrow. In both panels, the different crystallographic sites are highlighted in different colors.

Table 1 Atomic coordinates used for the refinements in $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs ($x = 0, 5$ and 20). Here M represents the transition metal element.

σ type structure					β -Mn type structure					α -Mn type structure				
atom	site	x	y	z	atom	site	x	y	z	atom	site	x	y	z
M1	$2a$	0	0	0	M1	$8c$	0.0632	0.0632	0.0632	M1	$2a$	0	0	0
M2	$4g$	0.3986	0.6014	0	M2	$12d$	0.125	0.2028	0.4528	M2	$8c$	0.3179	0.3179	0.3179
M3	$8i_1$	0.1312	0.5365	0	C	$4a$	0.375	0.375	0.375	M3	$24g_1$	0.3571	0.3571	0.0346
M4	$8i_2$	0.0661	0.2607	0						M4	$24g_2$	0.0896	0.0896	0.2819
M5	$8j$	0.3173	0.3173	0.2480										

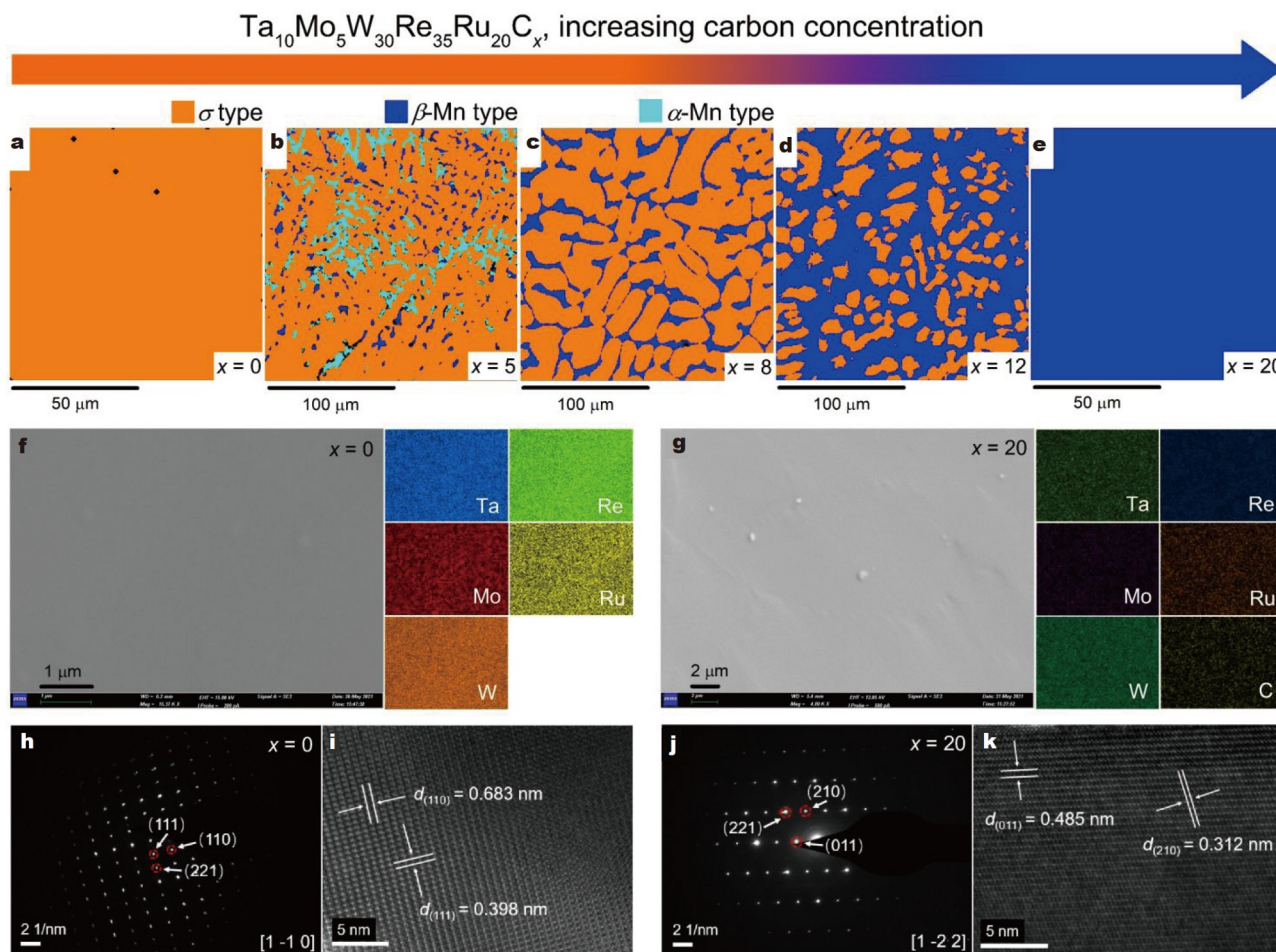


Figure 2 (a–e) EBSD phase maps for the $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs with $x = 0, 5, 8, 12$ and 20 , respectively. The arrow marks the direction of increasing carbon content. (f, g) SEM images together with EDX elemental mapping results for the HEAs with $x = 0$ and 20 , respectively. (h, i) SAED pattern and the corresponding HRTEM image, respectively, taken along the $[1 -1 0]$ zone axis of a single-crystalline grain for the σ type $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEA ($x = 0$). (j, k) The same set of data taken along the $[1 -2 2]$ zone axis of a single-crystalline grain for the β -Mn type $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_{20}$ HEA.

In the β -Mn type structure, however, there are only three different sites of $8c$ (0.0632, 0.0632, 0.0632), $12d$ (0.125, 0.2028, 0.4528) and $4a$ (0.375, 0.375, 0.375). The $8c$ and $12d$ sites are shared by all transition metal atoms, while the carbon atoms occupy the $4a$ one. As can be seen, the XRD pattern of $x = 0$ and 20 can be well fitted by a single σ ($R_{\text{wp}} = 6.38\%$, $R_p = 4.68\%$) and β -Mn type ($R_{\text{wp}} = 10.99\%$, $R_p = 7.88\%$) structure, respectively. As for $x = 5$, both σ and β -Mn type phases together with an α -Mn type ones are needed to achieve a good agreement between the calculated and observed XRD patterns ($R_{\text{wp}} = 4.87\%$, $R_p = 3.67\%$). It is worth noting that, in the β -Mn type structure, carbon is actually located at the interstitial position surrounded by six equivalent transition metal atoms, as expected from its

small atomic radius.

Fig. 2a–e show the phase maps from EBSD measurements for the $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs with $x = 0, 5, 8, 12$ and 20 , respectively. Here the σ phase is shown in orange, β -Mn type phase shown in blue and α -Mn type phase shown in cyan. It is obvious that the C-free HEA ($x = 0$) has nearly 100% σ phase, which is gradually suppressed as the carbon content increases. Indeed, the HEA with $x = 5$ contains 83.4% σ phase, 8.9% α -Mn type phase and 5.1% β -Mn type phase. At a slightly higher $x = 8$, the α -Mn type phase is no longer detectable and the volume fraction of β -Mn type phase is increased to 18.2%. On further increasing x , the β -Mn type phase becomes dominant (64.5%) at $x = 12$, and finally a single β -Mn type phase is observed at $x = 20$.

These results are in good agreement with those from the XRD measurements and corroborate the occurrence of structural transformation due to carbon addition.

The single-phase $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs with $x = 0$ and 20 are also characterized by SEM and TEM measurements. Typical SEM images together with EDX elemental mapping results are displayed in Fig. 2f, g. Both HEAs appear to be dense with a rather uniform distribution of the constituent elements. The measured Ta:Mo:W:Re:Ru = 9.5(1):4.3(1):30.2(1):35.3(1):20.7(1) for $x = 0$ and 9.6(1):4.6(1):29.8(1):35.2(1):20.8(1) for $x = 20$, in agreement with the nominal ratio. Since carbon has a light mass and is a mostly likely contaminant in the EDX analysis, its content cannot be determined accurately by the EDX measurements. Nevertheless, the actual carbon content should be close to nominal one given the negligible weight loss during the arc melting process. Fig. 2h–k show the selected-area electron diffraction (SAED) patterns and high-resolution TEM (HRTEM) images for these two HEAs. For $x = 0$, a well-defined SAED pattern is found along the $[1 -1 0]$ zone axis of a single-crystalline grain, and the spots near the center are indexable to (110), (111), and (221) reflections of the σ type structure. Accordingly, the HRTEM image of the same grain reveals two lattice spacings of 0.683 and 0.398 nm, which match well with the (110) and (111) planes, respectively. On the other hand, the spots near the center of the SAED pattern for $x = 20$, which is taken along the $[1 -2 2]$ zone axis of a single-crystalline grain, can be indexed to (011), (210), and (221) reflections of the β -Mn type structure. The corresponding HRTEM image gives two lattice spacings of 0.485 and 0.312 nm (Fig. 2k), which correspond well to the (011) and (210) planes. Therefore, both the pristine and transformed HEAs are homogeneous and possess a highly crystalline nature. Actually, we have also performed the

EDX elemental mapping measurements for the HEAs with $x = 5, 8$ and 12. The results, which are provided in the Supplementary information (Figs S1–S3), reveal a uniform distribution of the carbon. Nevertheless, this should be taken with caution considering possible carbon contamination on the sample surface. On the other hand, the segregation of Re and Ru is clearly visible for $x = 5$ and 8, indicating that the α -Mn and β -Mn type phases (darker regions) contain less Re and more Ru than the σ one (lighter regions).

In addition to structural transformation, superconductivity is also observed in the $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs. Since T_c is almost independent on x for both σ type and β -Mn type HEAs (see the insets of Fig. 3a, e), only those with $x = 0$ and 20 are characterized in detail and the results are displayed in Fig. 3a–h. In both cases, a resistivity drop, a large shielding fraction ($>100\%$) and a distinct specific heat (C_p) jump are detected, providing evidence for a bulk superconducting transition. From the midpoint of resistivity drop, T_c is determined to be 4.87 and 5.34 K for $x = 0$ and 20, respectively. In the normal state, the C_p data can be well fitted by the equation

$$C_p / T = \gamma + \delta T^2 + \eta T^4, \quad (1)$$

where γ and $\delta(\eta)$ are the electronic and phonon specific heat coefficients, respectively. Then the Debye temperature Θ_D is calculated through

$$\Theta_D = (12\pi^4 R / 5\delta)^{1/3}, \quad (2)$$

where $R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ is the molar gas constant. Thus, one obtains $\gamma = 3.32 \text{ mJ molatom}^{-1} \text{ K}^{-2}$, $\delta = 0.030 \text{ mJ molatom}^{-1} \text{ K}^{-4}$, $\Theta_D = 381 \text{ K}$, and $\gamma = 2.83 \text{ mJ molatom}^{-1} \text{ K}^{-2}$, $\delta = 0.045 \text{ mJ molatom}^{-1} \text{ K}^{-4}$, $\Theta_D = 342 \text{ K}$ for $x = 0$ and 20, respectively. Once Θ_D is known, the

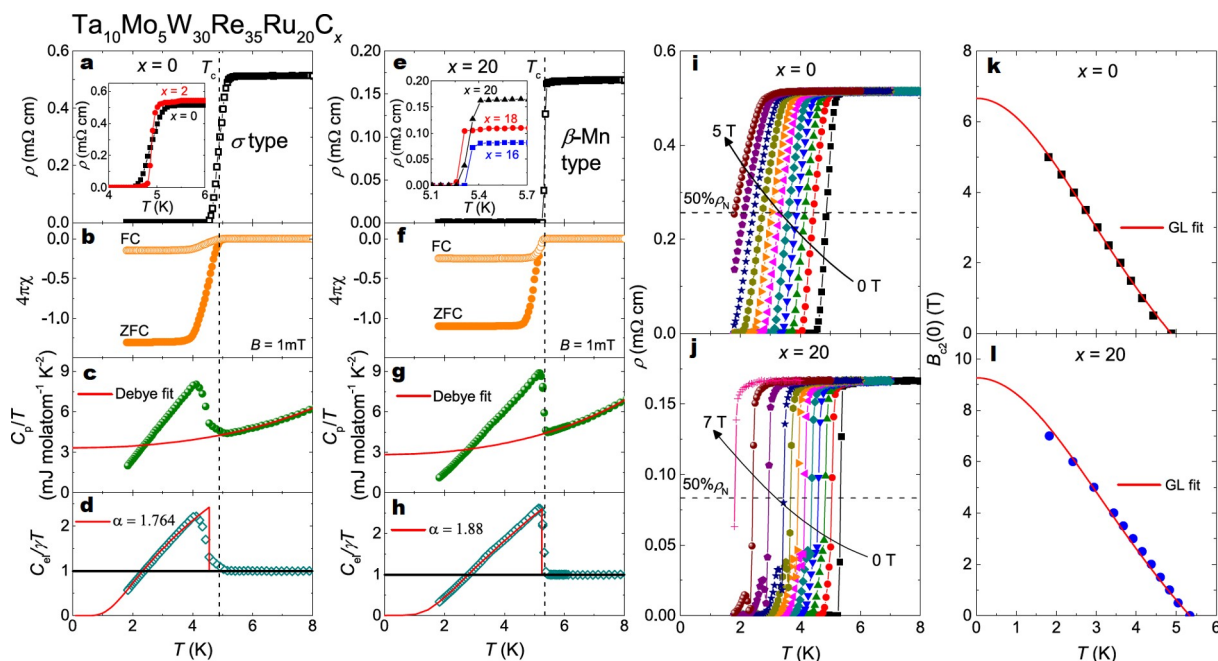


Figure 3 (a–d) Low temperature resistivity, susceptibility, specific heat, and normalized electronic specific heat data, respectively, for the σ type HEA with $x = 0$. In panel (a), the inset shows a comparison between the results for $x = 0$ and 2. In panels (c) and (d), the solid lines are fits to the data by the Debye model and α -model, respectively. (e–h) Same set of data for the β -Mn type HEA with $x = 20$. In panel (e), the inset shows a comparison between the results for $x = 16, 18$ and 20. In panels (g) and (h), the solid lines are fits to the data by the Debye model and α -model, respectively. (i, j) Temperature dependence of resistivity under various magnetic fields for the HEAs with $x = 0$ and 20, respectively. In both panels, the horizontal line denotes 50% drop of the normal-state resistivity. (k, l) Temperature dependence of the upper critical field for the two HEAs. In both panels, the solid line is a fit to the data by the GL model.

electron-phonon coupling strength λ_{ep} is estimated to be 0.59 for $x = 0$ and 0.62 for $x = 20$ on the basis of the inverted McMillan formula [37],

$$\lambda_{\text{ep}} = \frac{1.04 + \mu^* \ln(\Theta_{\text{D}}/1.45T_{\text{c}})}{(1 - 0.62\mu^*) \ln(\Theta_{\text{D}}/1.45T_{\text{c}}) - 1.04}, \quad (3)$$

where $\mu^* = 0.13$ is the Coulomb repulsion pseudopotential. By subtraction of the phonon contribution, the electronic specific heat C_{el} is isolated and plotted as $C_{\text{el}}/\gamma T$ versus T in Fig. 3d, h. The $C_{\text{el}}/\gamma T$ jumps of both HEAs can be well reproduced by the α -model, which was adapted from the single-band Bardeen-Cooper-Schrieffer (BCS) theory [38]. This model still assumes a fully isotropic superconducting gap but allows for the variation of coupling constant $\alpha = \Delta(0)/k_{\text{B}}T_{\text{c}}$, where $\Delta(0)$ is the gap size at 0 K. The resulting $\alpha = 1.764$ for $x = 0$, which is exactly the value predicted by the BCS theory [39]. As for $x = 20$, a slightly larger $\alpha = 1.88$ is obtained. These α values are consistent with magnitude of λ_{ep} , which together suggest that both σ type and β -Mn type HEAs have a weakly coupled, fully gapped superconducting state.

To determine the upper critical field $B_{\text{c}2}$, the temperature dependence of resistivity was measured under magnetic fields up to 7 T for the $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs ($x = 0$ and 20), the results of which are displayed in Fig. 3i, j. As expected, the resistive transition is suppressed to lower temperatures as the field increases. Notably, for the HEA with $x = 20$, a resistivity tail appears in the field interval between 2 and 6 T. This seems to be a common feature for several β -Mn type superconductors [40,41] and is attributed to the weak links between the superconducting grains originating from the poor conducting grain boundaries. At each field, T_{c} is determined by the midpoint of ρ drop, and the constructed $B_{\text{c}2}$ versus T phase diagrams are shown in Fig. 3k, l. The zero-temperature upper critical field $B_{\text{c}2}(0)$ is obtained by extrapolating the $B_{\text{c}2}(T)$ data based on the Ginzburg-Landau (GL) model

$$B_{\text{c}2}(T) = B_{\text{c}2}(0) \frac{1-t^2}{1+t^2}, \quad (4)$$

where $t = T/T_{\text{c}}$ is the reduced temperature. This gives $B_{\text{c}2}(0) = 6.7$ and 9.3 T for $x = 0$ and 20, respectively. In particular, the latter value is comparable to the Pauli paramagnetic limit $B_{\text{p}}(0) = 1.86T_{\text{c}} \approx 9.9$ T [42]. With $B_{\text{c}2}(0)$, the GL coherence length $\xi_{\text{GL}}(0)$ is calculated to be 7.0 and 6.0 nm for $x = 0$ and 20, respectively, through the equation

$$\xi_{\text{GL}}(0) = \sqrt{\frac{\Phi_0}{2\pi B_{\text{c}2}(0)}}, \quad (5)$$

where $\Phi_0 = 2.07 \times 10^{-15}$ Wb is the flux quantum. All these parameters are summarized in Table 2.

It is known that the stability of HEAs is related to a few parameters [18,43,44], including valence electron concentration (VEC), atomic size difference (δ) and mixing entropy (ΔS_{mix}). Fig. 4a shows the VEC dependence of T_{c} for the σ type and β -Mn type $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs, together with related HEA superconductors for comparison [11,32]. Here VEC is defined as

$$\text{VEC} = \sum_{i=1}^n c_i(\text{VEC})_i, \quad (6)$$

where c_i and $(\text{VEC})_i$ are the molar fraction and number of valence electrons for the i th element, respectively. The VEC values of $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEA superconductors are all located around 6.5, suggesting that they still obey the Matthias

rule [45]. Specifically, T_{c} of the σ type HEAs ($0 \leq x \leq 2$) increases with increasing VEC from 6.60 to 6.65, which matches well with the trend reported previously [11]. In comparison, the VEC of β -Mn type HEAs ($16 \leq x \leq 20$) lies in a lower range of 6.21 to 6.28, and it has nearly no influence on T_{c} . This overall behavior, which is reminiscent of that observed in carbon added ($\text{MoReRu}_{(1-2x)/3}(\text{PdPt})_x$ HEAs [32], suggests that the decrease in VEC is key in driving the structural transformation. In passing, it is pointed out that the β -Mn type $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ series are the first HEAs of this structure and have a considerably higher T_{c} than the fcc type ($\text{MoReRu}_{(1-2x)/3}(\text{PdPt})_x\text{C}_y$ ones.

We then compare the δ and ΔS_{mix} between the σ type and β -Mn type $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs. For the σ type HEAs, the parameters are calculated according to the equations,

$$\delta = \sqrt{\sum_{i=1}^n c_i \left(1 - r_i / \sum_{i=1}^n c_i r_i \right)^2} \quad (7)$$

and

$$\Delta S_{\text{mix}} = -R \sum_{i=1}^n c_i \ln c_i, \quad (8)$$

where r_i is the atomic radius for the i th element. Regarding the β -Mn type HEAs, given the interstitial position of carbon, the total mixing entropy is the sum of metal and carbon sublattices, which is expressed as [46,47]

$$\Delta S_{\text{mix}} = \Delta S_{\text{mix}}^{\text{metal}} + \Delta S_{\text{mix}}^{\text{carbon}}. \quad (9)$$

The calculation results are plotted as a function of VEC in Fig. 4b, c. As can be seen, the δ is 2.18% and 6.58% for the σ type HEAs with $x = 0$ and 2, respectively, both of which are below the threshold value of $\sim 6.6\%$ for the formation of single phase HEAs [18]. In contrast, the δ values of the β -Mn type HEAs are considerably larger and range from 16.43% to 17.98%, meaning that the lattice distortion is significantly enhanced upon carbon addition. On the other hand, ΔS_{mix} is the same of 1.43R for the σ type HEA with $x = 0$ and the β -Mn type HEA with $x = 20$. Nevertheless, ΔS_{mix} is increased to 1.93R and 1.76R for the β -Mn type HEA with $x = 16$ and 18, respectively. Taken together, it is reasonable to speculate that the lattice distortion and mixing

Table 2 Structural refinement results and physical parameters of $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs with $x = 0$ and 20

Parameter	$x = 0$	$x = 20$
Space group	$P4_2/mnm$	$P4_132$
a (Å)	9.6051(3)	6.8308(1)
c (Å)	4.9871(1)	—
V (Å ³)	460.11(2)	318.73(1)
R_{wp}	6.38%	10.99%
R_{p}	4.68%	7.88%
Goodness-of-fit (GOF)	1.69	1.88
T_{c} (K)	4.87	5.34
γ (mJ molatom ⁻¹ K ⁻²)	3.32	2.83
δ (mJ molatom ⁻¹ K ⁻⁴)	0.035	0.049
Θ_{D} (K)	381	342
λ_{ep}	0.59	0.63
$B_{\text{c}2}(0)$ (T)	6.7	9.3
$\xi_{\text{GL}}(0)$ (nm)	7.0	6.0

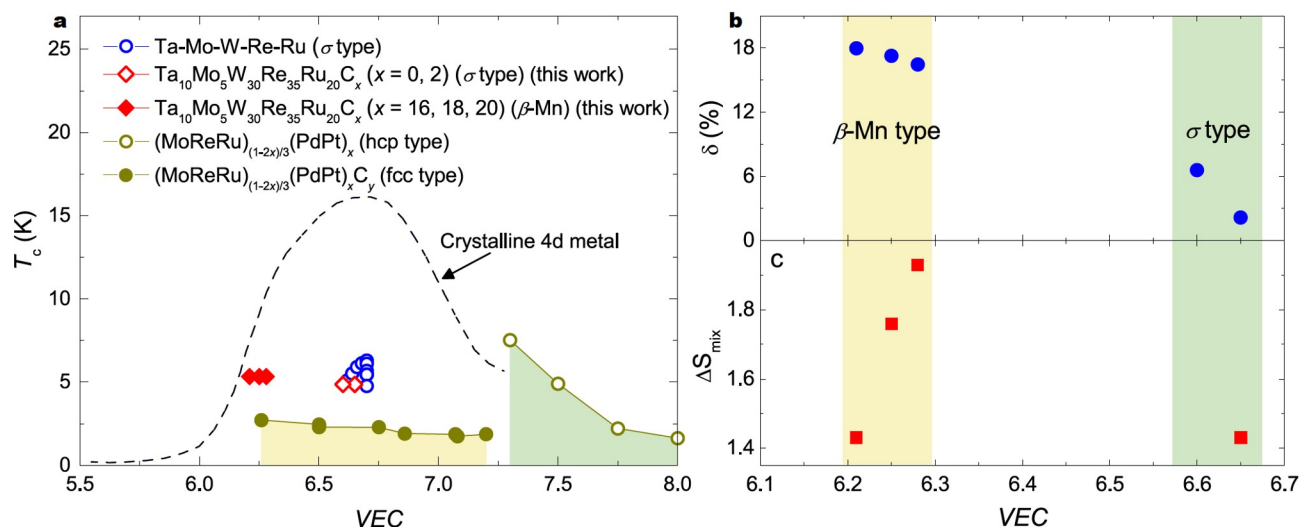


Figure 4 (a) VEC dependence of T_c for the σ type and β -Mn type $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs, together with related systems for comparison. The dashed line denotes the behavior for crystalline 4d metals [45]. (b, c) Comparison between the VEC dependence of δ and ΔS_{mix} , respectively, for the two types of HEAs.

entropy also play a nontrivial role in the structural transformation of $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$.

Finally, we briefly discuss the implications of our results on future research. First, our results suggest that the structural transformation by adding carbon in HEAs may be a general consequence due to the decrease in VEC as well as the increase in lattice distortion and mixing entropy, which certainly calls for theoretical understandings. Second, our study points to a connection between the σ type and β -Mn type structures. In this regard, it is of interest to see whether β -Mn type phase could be obtained by carbon addition in binary and ternary σ type phases. Third, the lack of inversion symmetry in the β -Mn type $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEAs may allow for a mixture of spin-singlet and spin-triplet pairing. Hence Muon spin rotation studies are worth pursuing to search for the signature of time-reversal symmetry breaking in the superconducting state.

CONCLUSIONS

In summary, we have studied the effect of carbon addition on the structure and physical properties of the $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}$ HEA. The results show that the $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ HEA adopts a centrosymmetric tetragonal σ type structure for $0 \leq x \leq 2$, which transforms into a noncentrosymmetric cubic β -Mn type structure for $16 \leq x \leq 20$. Both the σ type and β -Mn type HEAs exhibit bulk superconductivity with T_c values of 4.87 and 5.34 K. Especially, the upper critical field of the latter reaches 9.3 T, which is close to the Pauli paramagnetic limit. A comparison of phase stability between the σ type and β -Mn type HEAs suggests that the decrease in VEC and the increase in lattice distortion and mixing entropy are mainly responsible for the structural transformation. Our study not only provides a rare example of centrosymmetric to noncentrosymmetric structural transformation in HEAs, but also consolidates that carbon addition is an efficient way to tune the structure and physical properties of HEAs.

Received 27 April 2022; accepted 31 May 2022;
published online 12 August 2022

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Acknowledgements We thank the financial support by the foundation of Westlake University and the Service Center for Physical Sciences for technical assistance in SEM measurements. The work at Zhejiang University is supported by the National Natural Science Foundation of China (12050003).

Author contributions Xiao G initialized the project, synthesized the samples and did the physical property measurements with the assistance from Zhu Q, Yang W, Cui Y, Song S and Cao GH. Ren Z supervised the project and wrote the paper with input from Xiao G.

Conflict of interest The authors declare that they have no conflict of interest.

Supplementary information Supporting data are available in the online version of the paper.



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碳添加引起一种超导高熵合金的中心对称到非中心对称结构转变

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摘要 四方 σ 相是过渡金属合金中最常见的物相之一。然而， σ 型高熵合金中尚未有关于碳添加效应的报道。在本文中，我们发现在超导的 $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}$ 高熵合金($T_c = 4.87$ K)中添加碳会引起结构转变。结果表明在 $0 \leq x \leq 2$ 时 $\text{Ta}_{10}\text{Mo}_5\text{W}_{30}\text{Re}_{35}\text{Ru}_{20}\text{C}_x$ 高熵合金具有中心对称的 σ 型结构，但在 $16 \leq x \leq 20$ 时转变为非中心对称的 β -Mn型结构。转变后的 β -Mn型高熵合金仍表现出体超导电性且具有更高的 T_c (5.34 K)和接近泡利顺磁极限的上临界场。此外，该结构转变归因于碳添加引起价电子浓度的降低以及晶格畸变和混合熵的增加。我们的研究结果不仅提供了高熵合金中中心对称到非中心对称结构转变的罕见例子，而且夯实了非金属碳是调节高熵合金结构和物理性质的有效添加剂。