CFN: A Complex-valued Fuzzy Network for Sarcasm Detection in Conversations

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Abstract-Sarcasm detection in conversation (SDC), a theoretically and practically challenging artificial intelligence (AI) task, aims to discover elusively ironic, contemptuous and metaphoric information implied in daily conversations. Most of the recent approaches in sarcasm detection have neglected the intrinsic vagueness and uncertainty of human language in emotional expression and understanding. To address this gap, we propose a complex-valued fuzzy network (CFN) by leveraging the mathematical formalisms of quantum theory (QT) and fuzzy logic. In particular, the target utterance to be recognized is considered as a quantum superposition of a set of separate words. The contextual interaction between adjacent utterances is described as the interaction between a quantum system and its surrounding environment, constructing the quantum composite system, where the weight of interaction is determined by a fuzzy membership function. In order to model both the vagueness and uncertainty, the aforementioned superposition and composite systems are mathematically encapsulated in a density matrix. Finally, a quantum fuzzy measurement is performed on the density matrix of each utterance to yield the probabilistic outcomes of sarcasm recognition. Extensive experiments are conducted on the MUStARD and the 2020 sarcasm detection Reddit track datasets, and the results show that our model outperforms a wide range of strong baselines.

Index Terms-Sarcasm detection, emotion recognition, fuzzy logic, quantum theory, artificial intelligence.

I. Introduction

ARCASM can be traced back to ancient Greece, and was first recorded in English in 1579 [1]. It is a kind

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of rhetorical strategy that is intended to express criticism or mock emotions by means of hyperbole, figuration, etc [2], [3]. Through the theory discussion for a long time, it is finally defined as "a mode of satirical wit depending for its effect on bitter, caustic, and often ironic language that is usually directed against an individual" [4]. The recent advancement of Internet and social network services has led to a huge and increasing usage of ironic language, which plays an important role in daily discourse. We here give two real-life examples: (1) a waiter sees one client struggling to open a door and asks the client, "Do you want help?", if the client replies by saying, "No, I'm really enjoying the challenge". Then the waiter knows he's being sarcastic. (2) When a husband comes home after a long day at work, he expresses his sarcastic attitude, "I love working 40 hours a week, well done!".

Thus, identifying the sarcasm emotion of user-generated texts has a large potential for a wide range of domains, e.g., to 20 help manufacturers predict the attitudes of consumers toward their products and to help political associations understand general public opinions. For example, Donald Trump takes an irony tone at Joe Biden in his tweets such as "He is actually somewhat better than a rabid dog", due to his stance against Biden who appeared to be his new rival in the next presidency election. As another example, the third-party sellers on Amazon want to find public or consumer opinions and emotions about their products and services. Hence, there has been an increasing interest from both academia and industry in detecting sarcasm 30 in texts [5], [6].

An effective sarcasm detector is also beneficial to applications like sentiment analysis [7], humor analysis [8], brand management [9], business intelligence and more broadly across our daily lives [10]. Sarcasm detection refers to the use of 35 natural language processing (NLP), statistics and machine/deep learning methods to recognize sarcasm or irony orientations for various granularities of texts at the sentence, document or conversation levels. It is often formalized as the binary classification problem [11]. Previous sarcasm detection methods 40 in the literature have mainly focused on analyzing narrative texts, e.g., product reviews, tweets, etc., without involving interaction among the writers or speakers.

Currently, there are a series of emerging conversational sarcasm detection models that target at detecting the sarcastic attitude of multiple speakers in an conversation. Compared with the traditional sarcasm detection, SDC is more challenging for two reasons: (1) in the conversation, the attitude of each speaker is heavily influenced by other speakers, thus they are inseparable and cannot be treated independently; (2) the

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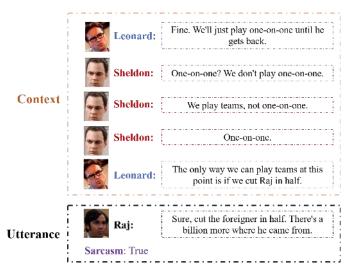


Fig. 1: Sample sarcastic utterance in a conversation along with its context.

interaction among people carries a wealth of information, such as their social relationships, stances, etc. However, such models, including the state of the art [12] are focused on investigating the role of conversation context or learning the contextual dependencies. They have not yet taken into consideration the inherent vagueness and uncertainty of human language

- in sarcasm expression, which needs to be studied from a more general cognitive science perspective. For illustration, Figure 1 provides a sarcastic example from the MUStARD dataset [2].
- In cognitive science, emotions are considered as the uncertain and vague part of human perception [13]. The uncertainty mainly refers to the spontaneity of emotional activities, where emotions are generated automatically without any rational reasoning process, and the change in emotional states does not
- ⁶⁵ involve any rational logical reasons. Even we have collected all prior knowledge, we might not determine emotional states. The vagueness refers that there is not a sharp line between different emotions, e.g., sad and depressed. Since emotion is a positive or negative personal experience, it cannot be as clear
 ⁷⁰ and determinate as rational logic.

As a specific form of emotional expression, sarcasm naturally inherits these characteristics. To model the fuzziness, a large body of fuzzy logic based models has been proposed [14], [15], [16], [17], [18]. A detailed literature review is given

- ⁷⁵ in Sec. II-B. They usually extract the syntactic and semantic features in a sentence by designing machine/deep learning architectures and obtain the predictions through using various fuzzy membership functions or constructing applicable *if-then* rules. Most of them neglect another key factor determining the
- sarcasm polarity, namely the uncertainty of human language. In recent years, quantum theory (QT), as a mathematical formalism to model the uncertain particle behaviors in quantum physics, has been adopted for describing elusive human cognitive and emotional activities in various AI tasks [19], [11].
- For instance, the quantum language model (QLM) [20] and neural network-based QLM [21] represented user's information needs and documents as density matrices (DMs) in a common quantum probabilistic space. The quantum sentiment repre-

sentation (QSR) model [22], [23] learned both the sentiment and semantic information with an improved version of QLM. However, such QT-based models are limited in that they restrict the models to finite vector spaces over real numbers. The potential for complex-valued formulations has not been fully developed. To address this problem, Wang and Li [24] defined a complex semantic Hilbert space to capture the "quantumness" in the cognitive aspect of human language. Nonetheless, their model randomized the complex phase instead of digging into its concrete meaning, and did not take into account the contextual interaction information, which is crucial for understanding human language.

In this paper, we argue that there are some fundamental connections between QT and fuzzy logic, since the fuzzy logic interpretation of quantum mechanics has been demonstrated under some circumstances [25]. Hence, unifying the quantum theory formalism and fuzzy logic would give us a more powerful theoretical framework to capture the subtle sentiments and semantics behind multiparty conversations. We thus propose a complex-valued fuzzy network, termed CFN, to jointly capture the uncertainty and vagueness of human language in sarcastic expression¹. To model the uncertainty, each utterance is treated as a quantum superposition of a set of basis words, which is represented by a complex-valued vector, where each component adopts an amplitude-phase form $z = re^{i\theta}$. The contextual interaction between adjacent utterances is described as the interaction between a quantum system and its surrounding environment, constructing a composite system. To model the fuzziness, the weight of interaction is determined by the fuzzy membership function. Then, the speaker's sarcastic attitude is viewed as a quantum mixed system composed of composite systems, which is mathematically encapsulated in a density matrix. Finally, considering the fact that all the information contained in one system (which, in this paper, refers to each utterance) is represented by the probability distribution of quantum measurement results, sarcastic features are extracted via the concept of quantum measurement, which is a natural choice. A fuzzy quantum measurement is performed on the density matrix of each target utterance to extract the probabilistic features, while these features are passed to a fully connected softmax layer to yield predictions over the sarcasm labels.

We have designed and carried out extensive experiments on two benchmark conversational sarcasm datasets, i.e., MUStARD and the 2020 sarcasm detection Reddit track, to demonstrate the effectiveness of the proposed CFN framework in comparison with a wide range of baselines, including a machine learning approach (i.e., support vector machine, SVM) and seven state-of-the-art sarcasm detection approaches (i.e., convolutional neural network (CNN), bidirectional gated recurrent unit (BiGRU), multi-head attention-based bidirectional longshort memory (MHA-BiLSTM) network, bidirectional encoder representations from transformers (BERT), RCNN-RoBERTa, contextual sarcasm detection network (C-Net) and a multi-task learning (MTL) framework). The results show that the CFN

¹We have made our source code publicly available at https://github.com/whatc0de/CFN-maste

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significantly outperforms a wide range of comparative models. The rest of this paper is organized as follows. Section II outlines the related work. Section III introduces the preliminaries of quantum theory and fuzzy logic. In Section IV, we describe the proposed complex-valued fuzzy network framework in detail. In Section V, we report the empirical experiments and analyze the results. Section VI concludes the paper and points out future research directions.

II. Related Work

A. Sarcasm Analysis

Sarcasm is a very subtle form of metaphorical language, where the literal meaning of the sentence is contrary to its true interpretation. In NLP, sarcasm detection is typically treated as a text classification task. Generally speaking, there exist three categories of approaches in the current literature: rule-based, machine learning-based and deep learning-based approaches.

Rule-based approaches. The rule-based approaches infer the overall sarcasm polarity of a piece of text based on refined sarcasm rules, which do not require a large data corpus and training algorithms. The early research in this direction assumed interjections as stereotypic of sarcastic text. Bharti et al. [26]

proposed two lexicon based approaches, one of which is a 165 parsing-based lexicon generation algorithm (PBLGA) and the other is based on the occurrence of the interjection word. Hernandez et al. [27] used the semantic relatedness between words as the sarcastic features. Bouazizi el al. [28] defined

four sets of features that cover different types of sarcasm, and used these features to classify sarcastic tweets. Clews and Kuzma [29] applied a string matching strategy against positive sentiment and used interjection lexicons to judge sarcasm. As the rule-based approaches largely depend on rules and

patterns, their classification accuracy is generally lower than 175 machine/deep learning approaches. Satoshi Hiai [30] extracted sarcastic sentences in product reviews using classification rules and classified the sentences into eight classes by focusing on evaluation expressions. Kamal et al. [31] proposed a selfdeprecating sarcasm detection approach using an amalgamation

of rule-based techniques.

The rule-based approaches do not consider the contextual interaction. Since they rely heavily on sarcasm rules or lexicons, their classification performance is generally inferior to machine/deep learning-based approaches.

Machine learning-based approaches. These methods mainly make use of machine learning methods, such as random forest, support vector machines, and neural networks. They often involve building classifiers from labeled data, essentially a supervised classification task. For instance, Lunando et al. [32] employed the negativity information and the number of interjection words in the translated SentiWordNet as features, and fed them into various machine learning classifiers. Habernal et al. [33] evaluated two machine learning classifiers with

various combinations of features, e.g., N-gram, POS, etc., on 195 both the Czech and English sarcasm datasets. Mukherjee and Bala [34] tested a range of feature sets using the Naive Bayes and fuzzy clustering algorithms for sarcasm detection of online text. Sharma [35] used features of user's account and tweets, and devised three machine learning algorithms for the task of potential rumour origin detection. Kumar and Garg [36] compared the performance of several machine learning algorithms, including support vector machines, decision trees, and random forest, etc.

There have been a few sarcasm detection approaches that 205 explored contextual features to acquire shared knowledge between the speakers. Rajadesingan et al. [37] used the user's past tweets to construct a behavioral modeling framework tuned for detecting sarcasm. Joshi et al. [38] proposed a sequence labeling approach and showed that the history utterances help 210 improve the performance of sarcasm detection.

There are a range of machine learning-based rumor propagation and recognition approaches that also develop similar strategy to investigate rumor. Belen and Pearce [39] checked general initial conditions of ignorants, spreaders and stiflers, and analyzed how the initial conditions bear on what proportion of ignorants by using rumor model. They also described an impulsive control model of a rumor process to classify the spreaders [40]. Belen et al. [41] proposed a solution to the problem of a repeated rumor based on the classical Maki-220 Thompson rumor model, and thus they improved the Maki-Thompson model and derived a new solution for each dynamics of spreading of a rumor [42]. Similarly, Wilhelm Weber and Gürbüz [43] chose the numerical approach to study the dynamics of a rumor propagation model, and conduct detailed 225 analysis. They then proved the effectiveness of the rumor propagation model [44]. Further, they proposed a numerical technique based on nonlinear ordinary differential equation, to solve a rumor propagation model [45].

Machine learning-based approaches usually achieve higher 230 classification results than rule-based approaches. However, they separate the feature extraction from the decision-making process. Their performance largely depends on the feature engineering, which is often cumbersome to design.

Deep learning based approaches. As deep learning based 235 architectures cast off the fetters of feature engineering, they usually achieve a better performance. A growing number of researchers apply deep learning technologies to sarcasm recognition as well.

As one of the first studies, Poria et al. [46] employed 240 a pre-trained CNN for extracting sentiment, emotion and personality features. Zhang et al. [47] used a bi-directional gated recurrent neural network (RNN) to capture contextual features for sarcasm detection. Similarly, Potamias et al. [6] designed a deep framework, which consisted of the pre-245 trained transformer-based architecture for irony and sarcasm detection. Chaturvedi et al. [48] designed a deep CNN to extract features from texts and images, and predicted the degree of a particular emotion using a fuzzy logic classifier. Vashishtha and Susan [49] proposed an unsupervised system that was 250 based on nine fuzzy rules to classify the posts into three sentiment classes. Chatterjee et al. [50] took the context of the utterance into consideration, and proposed a deep learning based approach. Liu et al. [51] proposed a deep neural network, called A2Text-Net, to mimic the face-to-face speech, which 255 integrated auxiliary clues such as punctuations, part of speech (POS), emoji, etc., to improve the performance of sarcasm

detection.

Recently, contextual information has been exploited for sarcasm detection. Jaiswal [52] investigated various pre-trained language representation models and utilized the contextual information along with the utterance for SDC. Ghosh et al. [53] used LSTM and attention-based LSTM to investigate the role of conversation context in detecting sarcasm in social media

discussions. For a similar purpose, Castro et al. [2] created a new dataset, MUStARD, for multimodal sarcasm research with high-quality annotations, including both mutlimodal and conversational context features. In a further work [54], they argued that knowledge in sarcasm detection could also be beneficial to sentiment analysis, and designed a multi-task learning framework using a deep neural network to improve the performance of both tasks. Similarly, Chauhan et al. [5] leveraged the multi-modal sentiment and emotion information for solving the problem of multi-modal sarcasm detection in a multi-task framework. However, they neglected the contextual

interaction between adjacent utterances.

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To sum up, the afore-discussed three types of studies have made a good progress in sarcasm detection, and motivated our work. They are mainly focused on studying refined sarcastic rules, extracting effective features and building deep learning architectures for sarcasm recognition. However, to the best of our knowledge, they have not yet systematically taken into account the vagueness and uncertainty of human language in

sarcastic expression, which we aim to tackle in this paper.

285 B. Fuzzy Logic based Models

To model the fuzziness in artificial intelligence problems, a large body of fuzzy logic based models has been proposed [15], [55]. For example, Alireza Goli's team has proposed a range of fuzzy models to solve cell formation problem (CFP) [14], relief vehicles problem [16], transportation route planning [55], etc [56]. Kropat and Weber [57] depicted the eco-finance networks for modeling gene-expression patterns with respect to errors and uncertainty. Erik Kropat [58] introduced timediscrete target-environment regulatory systems (TE-systems) under ellipsoidal uncertainty, and presented a mixed integer

regression problem for the relaxation by means of continuous optimization. They [59] also discussed a lot of regression models for gene-environment networks under ellipsoidal uncertainty. In order to model the relations between the targets

and environmental entities of the regulatory network, they proposed a fuzzy target-environment network and analyzed the vagueness of the regulatory system [60], [61]. Then, they extended the concept of fuzzy target-environment networks to fuzzy-regression models with fuzzy data sets for understanding
 of interconnected complex systems. [62].

To the best of our knowledge, our work is the first that brings together quantum theory and fuzzy logic for SDC. The major innovations of the work presented in this paper can be summarized as follows.

- A novel application of fuzzy logic to SDC is proposed.
 - Inspired by quantum probability theory, we introduce complex numbers into the utterance representation.
 - A complex-valued fuzzy network is designed, which leverages quantum probability theory and fuzzy logic

to capture both the vagueness and uncertainty in sarcastic 315 expression.

• We verify the effectiveness of our model by applying it to the task of SDC. Empirical experimental results show that our model outperforms strong baselines.

III. Preliminaries of Quantum Theory and Fuzzy Logic

A. Quantum Theory Preliminaries

In QT, the quantum probability space is naturally encapsulated in an infinite complex Hilbert space, denoted as \mathbb{H} . The essential difference between quantum and classical probability lies in the complex nature of quantum states.

With the Dirac's notation, a pure quantum state can be represented by a ray in a Hilbert space over the complex numbers. A quantum state vector in a complex vector space, \vec{u} , can be expressed as a ket $|u\rangle$, and its transpose can be expressed as a bra $\langle u|$. In Hilbert space, a quantum system can be in multiple mutually exclusive basis states simultaneously, with a probability distribution until it is measured, called quantum superposition, namely, $|u\rangle = \sum_{i=1}^{n} z_i |w_i\rangle$, where the $|w_i\rangle$ are orthogonal unit vectors and the z_i are complex components. After measurement it then collapses to one of the basis states that form the superposition. Quantum superposition describes the uncertainty of a single particle. For example, if there are two basis states $|0\rangle$ and $|1\rangle$, then a superposition state would be $|u\rangle = z_{\alpha}|0\rangle + z_{\beta}|1\rangle$, where z_{α} and z_{β} are complex coefficients, satisfying $z_{\alpha}^2 + z_{\beta}^2 = 1$.

A quantum event is defined to be a subspace of Hilbert space, represented by any orthogonal projector Π . Assume $|u\rangle$ is a unit vector, i.e., $\|\vec{u}\|_2 = 1$. The projector Π is written as $|u\rangle\langle u|$. A quantum mixed state corresponds to a probabilistic mixture of pure states, which is represented by the density 345 matrix, $\rho = \sum_{\lambda} \mu_{\lambda} |u\rangle \langle u|$. Density matrix ρ is symmetric (i.e., $\rho = \rho^T$), positive semi-definite (i.e., $\rho \ge 0$), and of trace 1. The quantum probability measure M is associated with the density matrix. The Gleason's Theorem has proven the existence of a mapping function $M(|u\rangle\langle u|) = tr(\rho|u\rangle\langle u|)$ for 350 any $|u\rangle$. In QT, quantum measurement describes the interaction (compositing) between a quantum system and the measurement device, where the composition system can be represented by the tensor product of two systems, e.g., $M \otimes |u\rangle$.

Measurement. Measurement is a process of testing or 355 manipulating the physical property of a system. In classical mechanics, the measurement process and measurement device are independent of the measured objects, which will not affect the measured objects. However, measurement in quantum world has an impact on the measured object, such as changing the 360 state of the system to be measured. Quantum measurement is described by a set of measurement operators acting on the state space of the system being measured $\{M_m\}$, where m represents the possible measurement outcomes. Suppose the quantum system is in a state of $\rho | u \rangle$ before the measurement, then the 365 probability to obtain the outcome m after the measurement is $p(m) = \langle u | M_m^{\dagger} M_m | u \rangle$. Moreover, the state of quantum system has changed to: $\frac{M_m |u\rangle}{\sqrt{\langle u|M_m^{\dagger}M_m|u\rangle}}$

By introducing the complex number, QT could define complex probability amplitude to construct classical probability 370

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(i.e., the square of the probability amplitude equals to the probability, providing a many-to-one relationship between probability amplitude and probability), and thus describe the uncertain events. QT provides a principled and effective mechanism to capture the intrinsic uncertainty.

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B. Basic Notations and Concepts in Fuzzy Logic

The conventional Boolean logic has been applied to a wide variety of AI applications, by only permitting two truth values, i.e., true and false. It has many deficiencies since two truth values are incapable of describing complex reasoning mode of human. As an extension, fuzzy logic was invented to deal with vagueness and imprecise information by defining many values between 0 and 1, in the form of fuzzy sets [3], [63].

Fuzzy logic commonly provides a three-step process, i.e., fuzzification, logical operation and defuzzification, to map the linguistic variables onto output results. Fuzzification targets at converting the numerical input of a system x to the degree of membership in a fuzzy set A, by using membership function μ_A . The degree of membership could be any values within the interval [0,1], $\mu_A(x) \in [0,1]$. There are different types of membership functions, e.g., triangular, trapezoidal, Gaussian, sigmoid, polynomial functions, etc.

Fuzzy logic has defined three basic operators, AND, OR and NOT. Assume that there are four fuzzy sets, i.e., A, B,

C and D, where $C = A \cup B$, $D = A \cap B$. Then, $\mu_C(x) =$ 395 $max \{\mu_A(x), \mu_B(x)\}, \mu_D(x) = min \{\mu_A(x), \mu_B(x)\}, \text{ and }$ $\mu_{A^{c}}(X) = 1 - \mu_{A}(X)$. Defuzzification is the process of transforming the output value of a fuzzy inference system into a crisp output. There are some mostly-used algorithms, e.g., finding the center of gravity, calculating the average mean,

calculating the left maximum, etc.

Building on many-valued logic, fuzzy logic aims to simulate human intelligence for automatically handling vague information, performing judgment and reasoning.

C. The Relations between QT and Fuzzy Logic 405

QT has a close tie with fuzzy logic, since both of them provide a mean to deal with concepts like vagueness and uncertainty. In comparison to fuzzy logic that is based on membership values, QT is defined on complex subspace identified by projectors [25]. The interaction of a projector with a density matrix produces a value which can be directly interpreted as the degree of membership. Meanwhile, the fuzzy membership function could be used to depict the relative importance of each quantum state. A few studies proved

that some logic operations of projectors (e.g., junction) in QT directly corresponds to the operations in fuzzy logic under some conditions [64]. They also conducted detailed analysis of a fuzzy logic interpretation of quantum theory by demonstrating that the Schroedinger equation can be deduced from the assumptions of the fuzziness [65]. 420

In this work, we bring QT and fuzzy logic together for modeling the intrinsic vagueness and uncertainty of human language in emotional expression and understanding.

D. How to Apply Key Notations to Our Approach

Here, we summarize the key notations in QT and fuzzy 425 logic and explain how to apply them to our approach. (1) The quantum state $|u\rangle$ could be seen as the utterance u in conversations, while the i^{th} basis vector $|w_i\rangle$ is linked to the i^{th} basis word vector. Each utterance is thus seen as in a quantum superposition of a set of basis words, and represented 430 as $|u\rangle = \sum_{i=1}^{n} z_i |w_i\rangle$. The target utterance $|u_t\rangle$ and its λ^{th} context $|c_{\lambda}\rangle$ are calculated in the same way (c.f. Sec. IV-C). (2) The composition system in OT is linked to the contextual interaction between the target utterance $|u_t\rangle$ and its context $|c_\lambda\rangle$, which could be calculated as the tensor product of them, e.g., 435 $|\Psi_t^{c_\lambda}\rangle = |u_t\rangle \otimes |c_1\rangle \otimes |c_2\rangle, ..., \otimes |c_\lambda\rangle.$ (3) The final representation of the target utterance is considered as a quantum mixed state that is in a statistical mixture over multiple composition systems, which can be mathematically encapsulated in a density matrix, i.e., $\rho_t = \sum_{\lambda} \mu_{\lambda} |\Psi_t^{c_{\lambda}}\rangle \langle \Psi_t^{c_{\lambda}} |$, where μ_{λ} is the fuzzy 440 membership function representing the relative importance of the λ^{th} composition system (c.f. Sec. IV-D). (4) Since we have obtained the representation of the target utterance ρ_t , a sequence of quantum fuzzy measurements $\{M_m\}$ on the representation ρ_t , for obtaining refined sarcastic features by 445 calculating $tr(M_m\rho_t)$ (c.f. Sec. IV-E). Hence, we will benefit from the unified and principled mathematics of QT.

IV. Complex-valued Fuzzy Network

In order to capture both the vagueness and uncertainty in human language, with conversational sarcasm detection as a 450 particular exemplar in this paper, we propose an end-to-end neural network based on QT and fuzzy logic, called complexvalued fuzzy network.

A. Problem Formulation and Overall Framework

Problem Formulation. Suppose the dataset has L 455 samples, the γ^{th} sample X_{γ} could be represented as $\{X_{\gamma} = (C_{\lambda}, U_t), Y_t\}$, where C_{λ} , U_t , Y_t represent the λ^{th} conversational context, the target utterance and its label respectively, where $C_{\lambda} \in \mathbb{H}^{l_{\lambda} \times d_{\lambda}}, U_{t} \in \mathbb{H}^{l_{t} \times d_{t}}$. Here, l_{λ} and l_t denote the sequence length of contextual and target 460 utterances, d_{λ} and d_t mean the dimensions of the contextual and textual features. $\lambda \in [1, 2, ..., k], \gamma \in [1, 2, ..., L]$.

Now, given a conversation (including the context C_{λ} and target utterance U_t), how to determine the sarcasm polarity (Y_t) . We formulate the problem as follows:

$$\zeta = \prod_{\lambda} p\left(Y_t | C_{\lambda}, U_t, \Theta\right) \tag{1}$$

where Θ represents the parameter set.

Overall Framework. The architecture of the CFN framework is shown in Fig. 2. (1) In the embedding layer, the target utterance u_t and its λ^{th} contextual utterance c_{λ} are embedded as complex-valued embeddings that are expressed in polar form, denoted as $|u_t\rangle$ and $|c_\lambda\rangle$. (2) In the fuzzy composition layer, the interactions between $|u_t\rangle$ and its contexts $\{|c_1\rangle, |c_2\rangle, \dots, |c_\lambda\rangle, \dots, |c_k\rangle\}$ are modeled as multiple quantum composite systems, which are given by the tensor product of individual utterance embedding, where the 475

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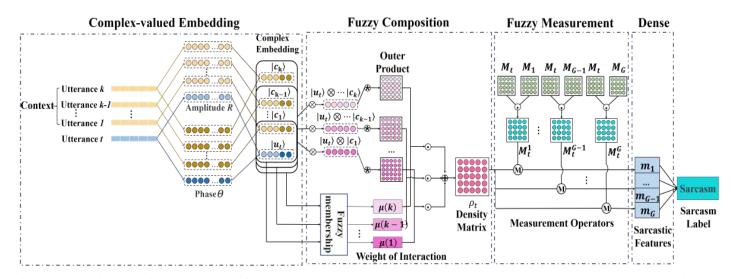


Fig. 2: The architecture of complex-valued fuzzy network. \otimes denotes the tensor product operation. \circledast denotes an outer production to a vector. \odot denotes point-wise multiplication. \oplus refers to a element-wise addition. \emptyset means a quantum fuzzy measurement.

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results are mathematically encapsulated in the density matrix ρ_t . (3) Sarcastic features are extracted via the concept of quantum measurement, which is a natural choice given the quantum state representation of sarcastic sentence. The fuzzy measurement layer is designed to perform a set of quantum fuzzy measurement operators to extract the sarcastic features $\vec{m_t}$. (4) The dense layer is employed to infer the final sarcasm polarity for the utterance.

B. Theoretical Advantages of Our CFN Framework

⁴⁸⁵ Before presenting the CFN framework, we provide the mathematical proofs here to show the advantages of our CFN framework in the form of three propositions.

Proposition 1 *Quantum probability is more general to capture the uncertainty in human language.*

Proof. Let $z(x) = re^{i\theta}$ be a quantum complex probability amplitude of event x. Using the definition of quantum probability, we get the classical probability of event x

$$p(x) = |z(x)|^2 = r^2$$

that is

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$$r = \sqrt{p\left(x\right)}$$

where $r \in \mathbb{R}$, $\theta \in (-\pi, \pi)$. Given p(x), the complex probability amplitude will satisfy

$$z(x) = \sqrt{p(x)} \times (\cos \theta + i \sin \theta) = re^{i\theta}$$

Hence, $\exists r_1, r_2 \in \mathbb{R}, r_1 \neq r_2$ and $\forall \theta_1, \theta_2 \in (-\pi, \pi), \theta_1 \neq \theta_2$, satisfies that $z_1(x) = r_1 e^{i\theta_1}, z_2(x) = r_2 e^{i\theta_2}$. We obtain

$$|z_1(x)|^2 = p(x) = |z_2(x)|^2$$
s.t $r_1^2 = r_2^2$
(2)

We conclude that $\exists z_1, z_2 \in \mathbb{H}$ and $z_1 \neq z_2$, then $z_1 \rightarrow p \land z_2 \rightarrow p$.

Remark 1. For example, the probability of a word w is 0.5, i.e., $p(x = w) = \frac{1}{2}$, then the corresponding probability amplitude may be $z(x = w) = \frac{\sqrt{2}}{2}e^{i\frac{\pi}{4}}$ or $z(x = w) = -\frac{\sqrt{2}}{2}e^{i\frac{2\pi}{5}}$,

etc. There is a many-to-one relationship between complex 495 probability amplitude and probability. The amplitude r links to the probability, while the phase θ may be associated with hidden sentiment or sarcasm orientations. An utterance thus could be represented in an amplitude-phase manner.

Proposition 2 *Quantum superposition embodies a non-linear* 500 *fusion of basis states.*

Proof. Let $z_1(w_1)$ and $z_2(w_2)$ be the complex probability amplitudes of two basis words w_1 , w_2 respectively, where $z_1(w_1), z_2(w_2) \in \mathbb{H}^{l_t \times d_t}$.

Let a compound term be $c \propto (w_1 \ w_2)$, we obtain

$$z_{3}(c) = \alpha z_{1}(w_{1}) + \beta z_{2}(w_{2})$$
(3)
s.t $\alpha^{2} + \beta^{2} = 1,$
 $\alpha, \beta \in \mathbb{H}$

where $z_3(c) \in \mathbb{H}^{l_t \times d_t}$. Based on Proposition 1, we have

$$p(w_1) = |z_1(w_1)|^2, \quad p(w_2) = |z_2(w_2)|^2$$

s.t $p(w_1), p(w_2) \in [0, 1]$

We can derive the probability of the compound term:

$$\begin{aligned} \varphi(c) &= |z_{3}(c)|^{2} = |\alpha z_{1}(w_{1}) + \beta z_{2}(w_{2})|^{2} \\ &= (\alpha z_{1}(w_{1}) + \beta z_{2}(w_{2})) \cdot (\alpha z_{1}(w_{1}) + \beta z_{2}(w_{2}))^{\dagger} \\ &= \alpha z_{1}(w_{1}) \cdot (\alpha z_{1}(w_{1}))^{\dagger} + \beta z_{2}(w_{2}) \cdot (\beta z_{2}(w_{2}))^{\dagger} \\ &+ \alpha z_{1}(w_{1}) \cdot (\beta z_{2}(w_{2}))^{\dagger} + \beta z_{2}(w_{2}) \cdot (\alpha z_{1}(w_{1}))^{\dagger} \\ &= \alpha z_{1}(w_{1}) \cdot (\alpha z_{1}(w_{1}))^{\dagger} + \beta z_{2}(w_{2}) \cdot (\beta z_{2}(w_{2}))^{\dagger} \\ &+ \alpha z_{1}(w_{1}) \cdot (\beta z_{2}(w_{2}))^{\dagger} + (\alpha z_{1}(w_{1}) \cdot (\beta z_{2}(w_{2}))^{\dagger})^{\dagger} \\ &= |\alpha z_{1}(w_{1})|^{2} + |\beta z_{2}(w_{2})|^{2} + 2Re\left(\alpha z_{1}(w_{1}) \cdot (\beta z_{2}(w_{2}))^{\dagger}\right)^{\dagger} \\ &= |\alpha z_{1}(w_{1})|^{2} + |\beta z_{2}(w_{2})|^{2} + 2|\alpha z_{1}(w_{1})\beta z_{2}(w_{2})|\cos\theta \\ &= \alpha^{2}p(w_{1}) + \beta^{2}p(w_{2}) + 2\alpha\beta\sqrt{p(w_{1})}p(w_{2})\cos\theta \end{aligned}$$

$$(4)$$

We use contradiction to prove the non-linearity. Assume that

$$p(x) = \alpha^{2} p(w_{1}) + \beta^{2} p(w_{2}) + 2\alpha \beta \sqrt{p(w_{1}) p(w_{2})} cosx$$
(5)

which is a linear function, satisfying

$$kp(x) = p(kx) \quad \forall x,$$

since this must hold for all x, it certainly must hold in the special case $x = \frac{\pi}{2}$. Let k = 2, then

$$2\alpha^{2} p(w_{1}) + 2\beta^{2} p(w_{2}) + 4\alpha\beta\sqrt{p(w_{1}) p(w_{2})} \cos\frac{\pi}{2} = \alpha^{2} p(w_{1}) + \beta^{2} p(w_{2}) + 2\alpha\beta\sqrt{p(w_{1}) p(w_{2})} \cos\frac{2\pi}{2}$$
(6)

which leads to the ridiculous conclusion that

$${}^{2}p(w_{1}) + \beta^{2}p(w_{2}) = -2\alpha\beta\sqrt{p(w_{1})p(w_{2})} \qquad (7)$$

Our assumption that Eq. 5 is linear is false.

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Remark 2. Hence, the probability of the compound term is the non-linear superposition of the probabilities of the basis words, with an interference term determined by the relative phase θ . This provides a higher level of abstraction.

Proposition 3 *Quantum composition system describes the correlations between parts and whole.*

Proof. Let u_i and u_j represent two adjacent utterances, we obtain

$$|u_i\rangle = \alpha_1 |w_1\rangle + \beta_1 |w_2\rangle$$

$$|u_j\rangle = \alpha_2 |w_1\rangle + \beta_2 |w_2\rangle$$

s.t $\alpha_1^2 + \beta_1^2 = 1,$ (8)
 $\alpha_2^2 + \beta_2^2 = 1,$
 $\alpha_1, \alpha_2, \beta_1, \beta_2 \in \mathbb{H}$

State space of a composite system \mathcal{H}_{u_i,u_j} consisting of two utterances u_i and u_j is written as a tensor product of the individual state spaces $|u_i\rangle$ and $|u_j\rangle$:

$$\begin{aligned}
\mathcal{H}_{u_{i},u_{j}} &= |u_{i}\rangle \otimes |u_{j}\rangle \\
&= (\alpha_{1}|w_{1}\rangle + \beta_{1}|w_{2}\rangle) \otimes (\alpha_{2}|w_{1}\rangle + \beta_{2}|w_{2}\rangle) \\
&= \alpha_{1}|w_{1}\rangle \otimes (\alpha_{2}|w_{1}\rangle + \beta_{2}|w_{2}\rangle) \\
&+ \beta_{1}|w_{2}\rangle \otimes (\alpha_{2}|w_{1}\rangle + \beta_{2}|w_{2}\rangle) \\
&= \alpha_{1}\alpha_{2}|w_{1}w_{1}\rangle + \alpha_{1}\beta_{2}|w_{1}w_{2}\rangle \\
&+ \beta_{1}\alpha_{2}|w_{2}w_{1}\rangle + \beta_{1}\beta_{2}|w_{2}w_{2}\rangle
\end{aligned}$$

$$\begin{aligned}
\text{Let } |w_{1}\rangle = (x_{1},x_{2})^{T}, |w_{2}\rangle = (y_{1},y_{2})^{T}, \text{ then}
\end{aligned}$$

$$\mathcal{H}_{u_i,u_j} = \alpha_1 \alpha_2 \begin{bmatrix} x_1^2 & x_1 x_2 \\ x_2 x_1 & x_2^2 \end{bmatrix} + \alpha_1 \beta_2 \begin{bmatrix} x_1 y_1 & x_1 y_2 \\ x_2 y_1 & x_2 y_2 \end{bmatrix} \\ + \beta_1 \alpha_2 \begin{bmatrix} y_1 x_1 & y_1 x_2 \\ y_2 x_1 & y_2 x_2 \end{bmatrix} + \beta_1 \beta_2 \begin{bmatrix} y_1^2 & y_1 y_2 \\ y_2 y_1 & y_2^2 \end{bmatrix}$$
(10)

⁵¹⁵ where \mathcal{H}_{u_i,u_i} is controlled by the basis words.

Remark 3. Eq. 10 proves that the composition system consisting of utterances embodies the correlations between words, which inspires us to model the contextuality by a "global to local" way. The details of the CFN framework will be given in the next subsections.

C. Complex-valued Utterance Embedding

In QT, quantum probability could be seen as the mathematical product of generalizing classical probability to the complex number field. Complex numbers are introduced to describe uncertain quantum state and behavior by defining the concept of quantum probability amplitude, where the modulus squared of the quantum probability amplitude represents a classical probability, providing a many-to-one relationship between probability amplitude and probability. Complex probability amplitude possesses outstanding ability to model the uncertainty.

Motivated by Wang and Li's work [66], we seek inspirations from quantum probability, and design a complex-valued utterance embedding layer. As word is the basic semantic unit of human language, we regard each word w_j in conversations as the basis state $|w_j\rangle$, and assume that $\{|w_1\rangle, |w_2\rangle, ..., |w_n\rangle\}$ builds the orthogonal basis of dialogic Hilbert space \mathbb{H}_d . The basis state $|w_j\rangle$ is mapped into dialogic Hilbert space \mathbb{H}_d using one hot encoding, which consists of zero in all cells with the exception of a single one in a cell used uniquely to identify

the word, i.e.,
$$|w_j\rangle = \left(0, 0, ..., 0, \frac{1}{j-1}, \frac{1}{j}, 0, ..., 0\right)$$

Then, an utterance could be seen as a collection of words. In QT, superposition is a fundamental concept, which has described the inherent uncertainty in the state of a microscopic particle (which, in this paper, refers to human sarcastic attitude). In order to capture the uncertainty in human language, we regard the target utterance u_t as a quantum superposition of a set of basis words $\{|w_1\rangle, |w_2\rangle, ..., |w_n\rangle\}$, which can be formulated as:

$$|u_t\rangle = \sum_{j=1}^{n} z_j |w_j\rangle$$

$$z_j = r_j e^{i\theta_j}$$
(11)

where *n* is the number of words in the utterance. z_j is a complex probability amplitude that is expressed in polar form, sufficing $\sum_{j} z_j^2 = 1$. *i* is the imaginary number satisfying the equation $i^2 = -1$. r_j represents the absolute value or modulus of the complex vector, termed amplitude. $\theta_j \in (-\pi, \pi)$ is the argument (phase) of z_j , referring to the angle of the ray with the positive real axis.

Let the amplitude **R** represent the length of the ray while the phase Θ denotes its direction. In this paper, we associate both of them with specific linguistic meanings. The amplitude is analogous to the semantic knowledge. As for the phase, since sarcasm is closely related to sentiment, it is linked to the sentiment orientation of the utterance. Now, the target utterance has been represented as a complex-valued vector, i.e., $|u_t\rangle = (r_1 e^{i\theta_1}, r_2 e^{i\theta_2}, ..., r_n e^{i\theta_n})^T$. The embedding of λ^{th} contextual utterance, i.e., $|c_\lambda\rangle$, can be calculated in the same way.

Eq. 11 is proposed to map each utterance into an embedding and learn its complex-valued vector representation. This complex-valued representation could capture the uncertainty in human language via the concept of quantum superposition and complex probability amplitude. This representation can be used to model the interaction between the target utterance and its contexts as a basic form (c.f. Eq. 13).

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Moreover, this representation uses both the amplitude and phase to determine the complex probability amplitude z_i , releasing strong ability to model the probability. It also allows for a non-linear fusion of amplitudes and phases in its mathematical form. Suppose the components $r_j^1 e^{i\theta_j^1}$ and $r_j^2 e^{i\theta_j^2}$ represent the j^{th} dimension of two utterances u_1 and u_2 respectively. The component $r_i^3 e^{i\theta_j^3}$ of the combination of u_1 and u_2 could be computed as:

$$r_{j}^{3}e^{i\theta_{j}^{3}} = r_{j}^{1}e^{i\theta_{j}^{1}} + r_{j}^{2}e^{i\theta_{j}^{2}}$$

$$= \sqrt{|r_{j}^{1}|^{2} + |r_{j}^{2}|^{2} + 2r_{j}^{1}r_{j}^{2}\cos\left(\theta_{j}^{1} - \theta_{j}^{2}\right)}$$

$$\times e^{i \arctan\left(\frac{r_{j}^{1}\sin\left(\theta_{j}^{1}\right) + r_{j}^{2}\sin\left(\theta_{j}^{2}\right)}{r_{j}^{1}\cos\left(\theta_{j}^{1}\right) + r_{j}^{2}\cos\left(\theta_{j}^{2}\right)}\right)}$$
(12)

Eq. 12 provides a non-linear fusion way to describe the compound term or phrase.

D. Learning Contextual Interaction with The Fuzzy Composition Laver 585

In QT, ideal quantum measurement describes the interaction (coupling) between a quantum system, the measurement device and their surrounding environments (e.g., other neighbor systems). However, we argue that the measurement device and

the environments may not participate equally in the interaction with the quantum system in realistic world, i.e., their degrees of involvement in the interaction are not equal. This interaction is analogous to the interaction among utterances in a conversation, while different context utterances, e.g., in the previous turns of a conversation, express different intensities of human interaction. 595

Inspired by this observation, we treat the target utterance u_t as a quantum system to be measured, its contextual utterances $C = \{c_1, c_2, ..., c_k\}$ as the surrounding environments. The measurement device is characterized as a set of measurement operators, which will be detailed in next subsection (c.f. 600 Sec. IV-E). Based on fuzzy logic, we thus design a fuzzy

composition layer to capture contextual interaction among

utterances. Suppose that a target utterance u_t is represented by its complex-valued embedding $|u_t\rangle$, and its contexts are represented by their embeddings $\{|c_\lambda\rangle\}_{\lambda=1}^k = \{|c_1\rangle, |c_2\rangle, ..., |c_k\rangle\}$ 605 respectively. The interaction between the target utterance u_t and its λ^{th} context c_{λ} constructs a composite system $|\Psi_t^{c_{\lambda}}\rangle$,

which is given by the tensor product of individual utterance embedding. In this work, the intensity of human interaction is 610 dependent on the distance of context utterances directly. We aim to learn both long and short range contextual interactions, by constructing multiple composite systems with a variable number of contexts. The λ^{th} composite system could be computed as:

$$\begin{aligned}
\Psi_t^{c_\lambda} &= |u_t\rangle \otimes \{|c_q\rangle\}_{q=1}^{\wedge} \\
&= |u_t\rangle \otimes |c_1\rangle \otimes |c_2\rangle \otimes, ..., \otimes |u_\lambda\rangle
\end{aligned} \tag{13}$$

where $\lambda \in [1,k]$. According to Eq. 13, we have built k composite systems for k context utterances, i.e., Ψ_k = $\{|\Psi_t^{c_1}\rangle, |\Psi_t^{c_2}\rangle, ..., |\Psi_t^{c_k}\rangle\}$. The role of Eq. 13 is to learn the interactions between the target utterance and its contexts, by introducing the operation of tensor product, where the result

is represented as the composite system. 620

Then, the final representation of the target utterance is in a statistical mixture over multiple composite systems Ψ_k , which can be mathematically encapsulated in a density matrix. Suppose the λ^{th} composite system $|\Psi_t^{c_\lambda}\rangle = \left(\Psi_{t,1}^{c_\lambda}, \Psi_{t,2}^{c_\lambda}, ..., \Psi_{t,d}^{c_\lambda}\right)$ the density matrix of utterance u_t can be represented as:

$$\rho_{t} = \sum_{\lambda=1}^{k} \mu_{\lambda} |\Psi_{t}^{c_{\lambda}}\rangle \langle \Psi_{t}^{c_{\lambda}}| \\
= \begin{bmatrix} \sum_{\lambda} \mu_{\lambda} \left(\Psi_{t,1}^{c_{\lambda}}\right)^{2} & \sum_{\lambda} \mu_{\lambda} \Psi_{t,1}^{c_{\lambda}} \Psi_{t,2}^{c_{\lambda}} & \dots & \sum_{\lambda} \mu_{\lambda} \Psi_{t,1}^{c_{\lambda}} \Psi_{t,d}^{c_{\lambda}} \\
& \sum_{\lambda} \mu_{\lambda} \Psi_{t,2}^{c_{\lambda}} \Psi_{t,1}^{c_{\lambda}} & \sum_{\lambda} \mu_{\lambda} \left(\Psi_{t,2}^{c_{\lambda}}\right)^{2} & \dots & \sum_{\lambda} \mu_{\lambda} \Psi_{t,2}^{c_{\lambda}} \Psi_{t,d}^{c_{\lambda}} \\
& \vdots & & \dots \\
& \sum_{\lambda} \mu_{\lambda} \Psi_{t,d}^{c_{\lambda}} \Psi_{t,1}^{c_{\lambda}} & \sum_{\lambda} \mu_{\lambda} \Psi_{t,d}^{c_{\lambda}} \Psi_{t,2}^{c_{\lambda}} & \dots & \sum_{\lambda} \mu_{\lambda} \left(\Psi_{t,d}^{c_{\lambda}}\right)^{2} \end{bmatrix}$$
(14)

where μ_{λ} is the fuzzy membership function representing the relative importance of the λ^{th} composite system. We argue that there is no firm boundary among the degrees of the participation in interaction, and thus adopt a Sigmoidal fuzzy membership function to model the fuzziness. μ_{λ} is decided by $\mu(\lambda : a, c) =$ $\frac{1}{1+e^{-a(\lambda-c)}},$ where λ is the index of context utterance, a and care trainable parameters learned during training.

Eq. 14 is used to obtain the matrix representation of the target utterance, and has shown each element of matrix. The density matrix ρ_t has encoded all the information and properties 635 of the target utterance u_t , e.g., the semantic dependencies, the probabilistic distribution information. The target utterance $|u_t\rangle$ and its contexts $\{|c_{\lambda}\rangle\}_{\lambda=1}^{k}$ are unified into a density matrix, for capturing both the uncertainty and vagueness simultaneously. The density matrix ρ_t is thus fed into the quantum fuzzy 640 measurement layer to extract more refined sarcastic features.

E. Quantum Fuzzy Measurement

In OT, measurement is a process of testing or manipulating the physical property of a quantum system, e.g., the movement locus of a particle. The outcome of quantum measurement is 645 associated with a set of numerical values. Before performing quantum measurement, there is uncertainty in the system in that it takes all possible measurement values simultaneously. After the measurement, the system collapses into one of these basis values, and the uncertainly on the system state is hence 650 removed.

Further, the information and property of a system (e.g., an utterance's sarcastic features) could be depicted by the probability distribution of the measurement outcomes, which are acquired by performing a finite set of quantum measurements on the 655 system [67]. As an extension of standard quantum measurement, quantum fuzzy measurement argues that the measurement device does not participate completely in interaction with the quantum system, meaning that the measurement device is not necessarily orthogonal to the quantum system, and could be set freely. Motivated by this, we perform a sequence of quantum fuzzy measurements with different measuring angles on the composite system, for obtaining rich sarcastic features for the target utterance $\vec{m}_t = (m_1, m_2, ..., m_G)$.

We define a set of fuzzy measurement operators $\{M_t^{\delta}\}_{\delta=1}^G$ 665 each of which is constructed by two sub-measurement M_t and $\{M_{\delta}\}_{\delta=1}^{G}$. M_t represents a trainable measurement operator

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(i.e., matrix) for the target utterance u_t , while $\{M_{\delta}\}_{\delta=1}^{G}$ represents another trainable measurement operator. The δ^{th} fuzzy measurement operator M_t^{δ} is a $d \times d$ matrix, satisfying the completeness condition that:

$$\sum_{\delta=1}^{G} \left(M_t^{\delta} \right)^{\dagger} M_t^{\delta} = 1$$
(15)

In QT, based on the density matrix of utterance u_t , the probabilistic expected value of quantum fuzzy measurement result, denoted as $\langle m^{\delta} \rangle$, is calculated as:

$$\langle m_{\delta} \rangle = \sum_{\lambda} \mu_{\lambda} \langle \Psi_{t}^{c_{\lambda}} | M_{t}^{\delta} | \Psi_{t}^{c_{\lambda}} \rangle$$

$$= \sum_{\lambda} \mu_{\lambda} tr(M_{t}^{\delta} | \Psi_{t}^{c_{\lambda}} \rangle \langle \Psi_{t}^{c_{\lambda}} |)$$

$$= \sum_{\lambda} tr(\mu_{\lambda} M_{t}^{\delta} | \Psi_{t}^{c_{\lambda}} \rangle \langle \Psi_{t}^{c_{\lambda}} |)$$

$$= tr\left(\sum_{\lambda} \mu_{\lambda} M_{t}^{\delta} | \Psi_{t}^{c_{\lambda}} \rangle \langle \Psi_{t}^{c_{\lambda}} |\right)$$

$$= tr(M_{t}^{\delta} \rho_{t})$$

$$(16)$$

Eq. 16 computes the expected value of the δ^{th} measurement result, and leads to the following calculation about the probability distribution over the measurement outcomes. We regard this probability distribution as the feature vector (i.e., \vec{m}_t) for the target utterance. The procedure is written as:

$$m_{\delta} = tr\left(M_{t}^{\delta}\left(M_{t}^{\delta}\right)^{\dagger}\rho_{t}\right)$$
$$= tr\left(\left(M_{t}^{\delta}\right)^{\dagger}M_{t}^{\delta}\sum_{\lambda}\mu_{\lambda}|\Psi_{t}^{c_{\lambda}}\rangle\langle\Psi_{t}^{c_{\lambda}}|\right)$$
$$= \sum_{\lambda}\mu_{\lambda}tr\left(\left(M_{t}^{\delta}\right)^{\dagger}M_{t}^{\delta}|\Psi_{t}^{c_{\lambda}}\rangle\langle\Psi_{t}^{c_{\lambda}}|\right)$$
$$= \sum_{\lambda}\langle\Psi_{t}^{c_{\lambda}}|\left(M_{t}^{\delta}\right)^{\dagger}M_{t}^{\delta}|\Psi_{t}^{c_{\lambda}}\rangle$$
(17)

where $M_t^{\delta} = M_t M_{\delta}, \ \delta \in [1, 2, ..., G]$. Eq. 17 is computed to obtain the probabilistic value of the δ^{th} fuzzy measurement outcome, which is treated as the δ^{th} eigenvector of $\vec{m_t}$. Finally, we have obtained a probabilistic feature vector $\vec{m_t} = (m_1, m_2, ..., m_{\delta}, ..., m_G)$.

685 F. Dense Layer

The probabilistic features $\vec{m_t}$ is passed to a fully connected layer whose output is used as the final utterance representation $\vec{x_t} = (x_1, x_2, ..., x_{\kappa})$. $\vec{x_t}$ is fed into the softmax function for sarcasm classification.

690 G. Classification

We put \vec{x}_t into a *softmax* function to yield the sarcasm label $Y \in \{y_{sar}, y_{non}\}$. That is,

$$\hat{y} = softmax \left(W_y \vec{x}_t + b_y \right) \tag{18}$$

where W_y and b_y are the weight and bias.

Model training. In our framework, cross entropy with L_2 regularization is used as the loss function, which is defined as: 695

$$J = -\frac{1}{N} \sum_{t} \sum_{\xi} y_t^{\xi} log \hat{y}_t^{\xi} + \tau_r \|\phi\|^2$$
(19)

where y_t denotes the ground truth, \hat{y}_t is the predicted sarcasm distribution. t is the index of utterance, ξ is the index of class, and L is the total number of utterances. τ_r is the coefficient for L_2 regularization. We use the back propagation method to compute the gradients and update all the parameters. In order 700 to avoid overfitting, we use dropout strategy.

V. Experiments

In this section, we validate the theoretical advantages of the QPM framework from an experimental viewpoint.

A. Experimental Settings

Our main research questions are:

(1) Is the complex-valued fuzzy representation effective for modeling human language?

(2) Does modeling of conversation context help in conversational sarcasm detection?

(3) Which component of CFN plays a key role on the performance?

To answer (1), we compare the performance of the CFN model with a number of baselines, and analyze the importance of the complex-valued fuzzy representation. To answer (2), we also perform all the experiments for the target utterances without context information, and make a detailed contrast. To answer (3), we conduct an ablation test by removing one component at a time and evaluate their impacts.

Datasets. Given that SDC is a new area, the benchmark datasets are relatively limited. In this work, we perform experiments on the MUStARD² [2] and the 2020 sarcasm detection Reddit track³ [68] datasets. MUStARD comprises 690 videos from several sources, e.g., Big Bang Theory, Friends, etc. The utterance in each dialogue is annotated with sarcastic or non-sarcastic label. Each utterance and its context consists of three modalities: video, audio, and text. Also, all the utterances are accompanied by their speaker identifiers. In this work, we focus on conversational sarcasm detection only from the textual information. Multimodal sarcasm detection is left as future work.

The 2020 sarcasm detection Reddit track (the Reddit track for short) is a subset of the Reddit Corpus, which consists of sarcastic responses and their contexts (quotes to which the posts are replies to). It contains 3,100 posts per class (sarcastic and not-sarcastic, for a total of 6200 posts) and more than 18,000 contextual utterances. Table I shows the detailed statistics for these two datasets.

Pre-processing. Apart from the standard preprocessing steps such as lowercasing the letters, removal of emojis, and correcting spelling mistakes, we remove the stop words using a standard English stopword list. Note that we do not filter out the punctuations, since they tend to carry subjective information.

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²https://github.com/soujanyaporia/MUStARD

³https://github.com/EducationalTestingService/sarcasm/releases

Dataset	No. of	f Utterance	No. of Contexts	
	Sarcastic	Non-sarcastic	THU. OF CONTEXES	
MUStARD	345	345	2261	
the Reddit track	3100	3100	18618	

TABLE I: Statistics of the	he datasets.
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Evaluation metrics. We adopt the **precision**, **recall**, *micro* **F1 score**, **accuracy**, **sensitivity** and **specificity** as the evaluation metrics to evaluate the classification performance. We run the experiments using five-fold cross-validation on all the comparative models.

Hyperparameters setting. In this work, the amplitudes are initialized with BERT semantic representation. The phases are set to the sentiment orientations of utterances using BERT. The fuzzy measurements are randomly initialized with an unit matrix. All weight matrices are given their initial values by sampling from a uniform distribution U(-0.1, 0.1), and all biases are set to zeros. The coefficient of L2 normalization in the objective function is set to 10^{-5} , and the dropout rate is

set to 0.5. We search for the best performance from a parameter pool, which contains a learning rate in {0.001,0.005,0.01}, the batch size in {32,64} and the number of fuzzy measurements in

 $\{100, 300, 500, 1000, 1500\}.$

B. Comparative Models

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In order for a comprehensive evaluation of the CFN framework, we include a range of baselines for comparison. They are listed as follows.

SVM+BERT [69] represents the textual utterances using BERT vectors and standard hyperparameter settings for sarcasm detection. We set the kernel function to "RBF". We also attempt to concatenate the contextual features.

CNN [70] contains two convolutional layers and a fully connected layer, which is trained on top of word embeddings for sarcasm classification in conversation.

BiGRU [71] leverages a bidirectional GRU network for learning utterance representations and then uses a classification layer to make prediction of sarcasm.

MHA-BiLSTM [36] extracts the most significant features and builds a multi-head attention-based bidirectional long-short memory network to detect sarcastic utterances.

Contextual LSTM [72] first uses the CNN to extract context-independent textual features and thus feeds them into the LSTM network to obtain context-sensitive feature representations and sarcasm labels for each utterance.

RCNN-RoBERTa [6] utilizes pre-trained RoBERTa vectors combined with a RCNN in order to capture contextual information for sarcasm classification.

C-Net [73] uses BERT and simple exponential smoothing to represent each utterance in conversation thread, and takes contextual information of a sentence in a sequential manner to classify it as sarcastic or non-sarcastic.

790 MTL framework [5] proposes two attention mechanisms, i.e., inter- and intra-segment inter-modal attentions, to learn the relationship between the different segments and the relationship within the same segment. Representations from both the attentions are concatenated for sentiment and sarcasm analysis. In this paper, we only use bimodal information (e.g., texts and ⁷⁹⁵ images).

C. Results and Analysis on MUStARD

The experimental results are summarized in Table II. Since the sample size of MUStARD is relatively small, we will pay more attention to F1 score and sensitivity here. We could 800 notice that those approaches including SVM+BERT, BiGRU, MHA-BiLSTM, Contextual LSTM, RCNN-RoBERTa, C-Net, MTL and CFN are all superior than CNN. Because all of them deal with the contextual information, which highlights the importance of modeling the contextual information in 805 SDC. Among all baseline approaches, SVM+BERT achieves a higher F1 score than three LSTM variants (i.e., BiGRU, MHA-BiLSTM and Contextual LSTM). The reason is that the pre-trained textual features provided by BERT have stronger discrimination ability. By integrating the contextual information 810 into the final features, SVM+BERT (+context) have obtained a slight improvement. Among three LSTM variants, BiGRU and Contextual LSTM get comparable F1 score, while MHA-BiLSTM performs worst. But MHA-BiLSTM has higher recall and sensitivity scores, which shows that MHA-BiLSTM could 815 classify more true samples. Contextual LSTM gets the highest specificity scores among all baselines, which implies that Contextual LSTM tends to identify negative (e.g., non-sarcastic) samples. This shows that: (1) preserving the sequential order of utterances is insufficient to effectively model the conversation 820 context; (2) the attention mechanism does not show obvious effects on improving performance on this dataset.

Through presenting improved modifications for training BERT models, RCNN-RoBERTa outperforms SVM+BERT in term of F1. But it achieves lower sensitivity and specificity 825 scores than SVM+BERT. The possible reason is that RCNN-RoBERTa is less sensitive to sarcastic utterances than SVM classifier. As a state-of-the-art conversational sarcasm detection baselines, C-Net leverages inter-speaker dependency of the speakers to model conversational context. It performs very well 830 in SDC. MTL framework achieves the best classification results among all baselines. Compared with C-Net, the sensitivity, f1 and accuracy results increase by 1.9%, 1.8% and 1.7%, respectively. The reason is that it designs a multi-task learning framework for multi-modal sarcasm, sentiment analysis. It 835 leverage the utility of sentiment and emotion of the speaker to predict sarcasm, based on textual and visual modalities. Finally, CFN outperforms the state-of-the-art method MTL by margins of 8.0%, 8.0% and 8.0%. CFN achieves best scores over almost all evaluation metrics, showing that our 840 model could not only distinguish sarcastic utterances from all testing samples, but also retrieve more sarcastic utterances from all sarcastic samples. CFN introduces complex-valued utterance embedding, where the amplitude is analogous to the semantic knowledge, while the phase is linked to the 845 subjective information. CFN brings the semantic and subjective information together by using this representation, which can improve the description of the sarcastic information. This explains its higher sensitivity when compared to previous

Dataset	Method	Evaluation metrics						
Dataset	wiethou	Precision	Recall	F1	Accuracy	Sensitivity	Specificity	
	SVM+BERT	0.651	0.646	0.647	0.646	0.646	0.643	
	SVM+BERT (+context)	0.655	0.651	0.650	0.651	0.651	0.650	
	CNN	0.579	0.569	0.571	0.589	0.569	0.533	
MUStARD	BiGRU	0.631	0.643	0.624	0.656	0.643	0.579	
	MHA-BiLSTM	0.673	0.652	0.614	0.668	0.652	0.644	
	Contextual LSTM	0.642	0.627	0.620	0.662	0.627	0.740	
	RCNN-RoBERTa	0.687	0.643	0.651	0.671	0.643	0.511	
	C-Net	0.679	0.683	0.681	0.683	0.683	0.678	
	MTL	0.694	0.694	0.693	0.695	0.694	0.690	
	CFN	0.753	0.755	0.754	0.754	0.755	0.701	
		(+8.0%)	(+8.0%)	(+8.0%)	(+8.0%)	(+8.0%)	(+1.4%)	
		•						

TABLE II: Performance of all baselines on MUStARD. The best performing system is indicated in bold. Numbers in parentheses indicate relative improvement over the MTL framework.

models. CFN obtains the second highest specificity score among all methods, showing that discovering non-sarcastic utterances is the weak point. We attribute the main improvements to both the complex valued embedding and the fuzzy composition mechanism, which ensures that CFN could preserve semantic
and sentiment information, capture the figurative language's vagueness and model the previous speaker's influence.

D. Results and Analysis on the Reddit track

Table III presets the performance comparison of CFN with the baselines on the Reddit track. Compared with MUStARD, the Reddit track involves longer utterances and only contains textual modality and sarcasm label.

From Table III, we can first notice the poor performance of BiGRU and Contextual LSTM. They get the worst and the second worst sensitivity and F1 scores. This phenomenon may be because the long range of contextual utterances makes it difficult for them to record useful information into the memory unit. Contextual LSTM gets a higher specificity scores over BiGRU, showing that Contextual LSTM tends to identify negative (e.g., non-sarcastic) samples. By introducing the attention mechanism to assign greater weights to important contexts, MHA-BiLSTM outperforms BiGRU and Contextual LSTM. Compared with MHA-BiLSTM, CNN gets comparable F1 score, cause that CNN may find relatively good local optima. But CNN achieves lower sensitivity result than MHA-

BiLSTM. The reason is that MHA-BiLSTM may focus on the sarcastic information by using the attention mechanism, which recognizes more sarcastic utterances and leads to a better sensitivity than CNN. Similarly, SVM+BERT overcomes the aforementioned baselines in terms of almost all evaluation

metrics. This shows the fact again that the pre-trained textual features provided by BERT have great discrimination ability. The reason is that BERT's word vector output encodes syntax trees in the word embeddings it outputs for a sentence, and encodes syntactic and semantic features in word vectors in complementary subspaces. Further, SVM+BERT (+context) performs better than SVM+BERT, by considering the contextual

features, which implies that the important role of contexts.

RCNN-RoBERTa achieves the best classification performance among all approaches, whose sensitivity, F1 and accuracy scores exceed 70%. Because RCNN-RoBERTa is

trained with dynamic masking, sentences without next sentence prediction loss, larger batches, and a larger byte-level BSE. It is based on a hybrid deep neural architecture that utilizes pretrained transformer models and feeds the hidden representations of the transformer into a recurrent convolutional neural network, 895 which can capture unbiased recurrent informative relationships within text. It is more suitable for applying to large size dataset. This can explain its main achievement on f1 and sensitivity results. C-Net is superior than SVM+BERT (+context) but it is weaker than RCNN-RoBERTa. This may indicate RoBERTa 900 performs better than BERT (base-uncased) on this track. Through combining both textual and visual modalities, MTL outperforms C-Net but it is still not suppress RCNN-RoBERTa. MTL does not perform well in uncovering non-sarcastic utterances. Because MTL is designed for multi-task learning 905 problems, which has considered mutual assistance between the two tasks. The generalization ability of MTL is insufficient to deal with various single task learning problems. RCNN-RoBERTa outperforms MTL by margins of 6.0%. From an overall perspective, it seems that the baselines that have used 910 the transformer-architecture perform better than those baselines that have used RNN-architecture. Transformer models are essentially attention based models. They regard the sentence as a whole unlike RNNs where the sentence is processed sequentially, i.e., one word per time step. Transformer models 915 can capture long term dependencies very naturally given the attention mechanism. These are the benefits of Transformers over RNNs, showing the effectiveness of pre-trained transformer model. The proposed CFN obtains comparable specificity, sensitivity, F1 and accuracy scores against RCNN-RoBERTa, 920 which achieves the second best classification performance. CFN brings the semantic and subjective information together by using this representation, which can improve the description of the sarcastic information. It encodes the contextual interactions between adjacent utterances into a density matrix. This 925 explains its higher sensitivity when compared to other models. Meanwhile, according to our preliminary analysis, the failure to adopt the attention attention is one possible reason why CFN obtains lower sensitivity and F1 results. But CFN involves fewer parameters and simpler structures than RCNN-RoBERTa. 930 We argue that CFN strikes a balance between effectiveness and efficiency.

Dataset	Method	Evaluation metrics						
Dataset	Methou	Precision	Recall	F1	Accuracy	Sensitivity	Specificity	
	SVM+BERT	0.640	0.642	0.638	0.640	0.642	0.647	
	SVM+BERT (+context)	0.649	0.647	0.643	0.651	0.647	0.659	
	CNN	0.631	0.623	0.629	0.623	0.623	0.611	
	BiGRU	0.600	0.599	0.600	0.600	0.599	0.561	
	MHA-BiLSTM	0.629	0.632	0.626	0.636	0.632	0.610	
Reddit track	Contextual LSTM	0.613	0.609	0.610	0.615	0.609	0.658	
	RCNN-RoBERTa	0.708	0.708	0.708	0.708	0.708	0.682	
	C-Net	0.663	0.664	0.663	0.663	0.664	0.657	
	MTL	0.667	0.668	0.667	0.668	0.668	0.625	
	CFN	0.680	0.680	0.680	0.680	0.680	0.664	
		(+1.5%)	(+1.5%)	(+1.5%)	(+1.5%)	(+1.5%)	(+6.2%)	

TABLE III: Performance of all baselines on the Reddit track. The best performing system is indicated in bold. Numbers in parentheses indicate relative improvement over the MTL framework.

E. Effect of Context Range

Dataset	Context range	Metrics		
Dataset	Context range	F1	Accuracy	
	Zero	0.640	0.641	
MUStARD	One	0.725	0.725	
	Two	0.699	0.699	
	All	0.754	0.754	
Reddit	Zero	0.596	0.596	
	One	0.641	0.641	
	Two	0.617	0.617	
	All	0.680	0.680	

Metrics Dataset Models F1 Accuracy CFN-Real 0.6440.645 CFN-Speaker Independent 0.640 0.641 **MUStARD** CFN-CNN 0.740 0.740 CFN 0.754 0.754 0.627 CFN-Real 0.626 CFN-Speaker Independent 0.596 0.596 Reddit CFN-CNN 0.675 0.675 CFN 0.680 0.680

TABLE V: Ablated CFN for both MUStARD and Reddit datasets.

In Table V, we observe that CFN-CNN and CFN get the best performance among these models. CFN-Real performs worse but still outperforms BiGRU and MHA-BiLSTM. This is because the fuzzy composition mechanism could incorporate rich interactive information into an unified density matrix. CFN-Speaker Independent under-performs CFN-Real, showing that the effectiveness of complex-valued representation and the key role of conversation contexts. Because complexvalued representation might encode non-linear semantic and sentiment compositionality. Finally, CFN-CNN, which replaces the quantum fuzzy measurement with the convolutional and pooling layers, obtains better results than CFN-Real and CFN-Speaker Independent, showing that the complex-valued embedding and fuzzy composition mechanism play the most important role in improving classification performance. CFN-CNN gets comparable results against CFN. However, CFN is theoretically more principled. Hence, these experimental results verify the effectiveness of CFN.

G. Sensitivity Study

In order to understand the relationships between inputs and outputs and study how the uncertainty in the output of the CFN model, we conduct the sensitivity analysis. In order to explore how much each input parameter is contributing to the output uncertainty, we choose one at a time (OAT) strategy, which is a common and effective sensitivity analysis method. We modify one input parameter and keep others at their original values. Then we repeat for each of the other parameters in the same way, to see the changes in the output.

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TABLE IV: Effect of context range.

We report results for CFN in Tables IV with different context scopes. Zero context means that we only use the complexvalued vector to represent the target utterance, ignoring the contextual interaction. One context utterance denotes that we use one history utterance before the target utterance to construct the density matrix. Two contexts mean that we use the previous

- ⁹⁴⁰ two history utterances to construct the density matrix. From Table IV, we could observe that CFN with zero context range expectedly performs worst on both MUStARD and the Reddit track. Because it does not consider any contextual information. This shows the important role of conversation contexts. Among
- three methods, CFN with one context range gets the best F1 scores of 72.5% and 64.1% on two datasets, which implies that modeling the previous one history utterance is of great help to improving performance. However, its performance is weaker than the performance of CFN with all context utterances. It
 shows that taking all conversation contexts into consideration may be the best way to reach optimal performance.

F. Ablation Study

In this subsection, we design a series of models to further demonstrate the effectiveness of our proposed CFN model: (1) *CFN-Real* that does not consider the complex embedding, i.e., replacing utterance embeddings with their real counterparts; (2) *CFN-Speaker Independent* model without modeling the contextual interaction, which only uses the complex vector to represent the target utterance; (3) *CFN-CNN*, which replaces the quantum fuzzy measurement with the convolutional and pooling

layers, to explore the significance of quantum measurement.

No.	Utterances		Sarcasm	
110.			CFN	
1	Good idea, sit with her. Hold her, comfort her. And if the moment feels right, see if you can cop a feel.	S	NS	
2	Just the latest copy of Applied Particle Physics quarterly.	S	NS	
3	but butshe did them herself, so that's like, original and so edgy!	S	NS	
4	I'm sorry, I am not going back to the Renaissance fair.	NS	S	
5	Nah, they're too afraid of a lawsuit and bad press.	NS	S	

TABLE VI: Few error cases for CFN.

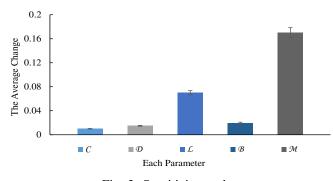


Fig. 3: Sensitivity study.

Due to the large amounts of parameters in deep neural networks, we mainly discuss five key parameters, which are the coefficient of L2 normalization (denoted as C), the dropout rate (denoted as D), the learning rate (denoted as L), batch size (denoted as B) and the number of measurement operators
(denoted as M). Fig.3 shows the average change in the output value of the CFN framework.

From Fig.3, we notice that the CFN framework is the most sensitive to the number of measurement operators. The average change in in the output value has reached about 17%. The second is learning rate \mathcal{L} , where the average change is 7%. Then, the coefficient of L2 normalization, batch size and the dropout rate may lead to a slight change. These results indicate that we may pay more attention to tuning the learning rate \mathcal{L} and the number of measurement operators

- M. There are two possible explanations: (1) the number of measurement operators determines the dimensionality of sarcastic feature space, which directly influences captured information. Intuitively, the more the number of measurement operators, the greater the performance of the CFN model; (2)
 the learning rate has been consider as the most important
- hyperparameter in neural network. A learning rate that is too large can cause the model to converge too quickly to a suboptimal solution, whereas a learning rate that is too small can cause the process to get stuck.

1015 H. Error Analysis

We have analyzed the prediction sarcasm labels and found that misclassification often happens in the situation where the speaker uses a few positive words to express his/her sarcastic attitude. In this case, the speaker is happy and comfortable literally, while s/he is angry and aggressive actually. We take an sarcastic utterance as an example, e.g., "Good idea, sit with her. Hold her, comfort her. And if the moment feels right, as a positive sentiment utterance, and thus feeds this wrong sentiment identification into the complex-valued embedding, then makes a wrong decision to regard it as a non-sarcastic utterance. Further, we also notice that a small amount of errors occur when an utterance expresses very negative sentiment. CFN may mix negative sentiment up with sarcasm polarity. This is due to the subtle difference between sentiment and sarcasm analysis. Discriminating irony attitude from negative sentiment is a tricky and complex problem, which is an open area of research. Table VI shows a few misclassification cases.

see if you can cop a feel.". CFN first mistakenly treats it

VI. Conclusions and Future Work

Sarcasm detection in conversation is an interesting and 1035 challenging AI task. In this paper, we introduce quantum theory and complex world into classical sarcasm detection. We propose a complex-valued fuzzy network to capture both the vagueness and uncertainty of human language in sarcastic expression. The main idea is to treat the utterance as a quantum superposition 1040 of a set of separate words, use the complex-valued vector to represent it. The contextual dependency among utterances is described as the interaction between a quantum system and its surrounding environment, which can be computed by the tensor product of individual utterance. Then, the speaker's sarcastic 1045 attitude is viewed as a quantum mixed system composed of composite systems, which is mathematically encapsulated in a density matrix. A fuzzy quantum measurement is performed on the density matrix of each target utterance to yield the probabilistic outcomes. The experimental results show that our 1050 proposed CFN model largely outperforms a number of strong sarcasm detection methods. To the best of our knowledge, this work is the first that brings together quantum theory and fuzzy logic for SDC.

Fuzzy logic provides us with a means to deal with vagueness 1055 and uncertainty, and quantum logic may give us more insights into the semantics behind the fuzzy norms algebraic product and algebraic sum. Since there are closely relationships between quantum theory and fuzzy logic, Future works will bridge them together and design a quantum fuzzy neural network 1060 for sarcasm detection. We also plan to provide a description of quantum mechanics in terms of a deterministic fuzziness using quantum fuzzy model. Moreover, since human language usually involves multimodal records, e.g., image, video, audio, etc., future works will also focus on incorporating multimodal 1065 information into the CFN model and designing a multimodal sarcasm detection model based on fuzzy logic and quantum theory. At the heart of this multimodal model is how to use fuzzy logic to represent visual and acoustic features.

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