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CH₄ sources estimated from atmospheric observations of CH₄ and its ¹³C/¹²C isotopic ratios: 1. Inverse modeling of source processes

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[1] A time-dependent inverse modeling approach that estimates the global magnitude of atmospheric methane sources from the observed spatiotemporal distribution of atmospheric CH₄, ¹³C/¹²C isotopic ratios, and a priori estimates of the source strengths is presented. Relative to the a priori source estimates, the inverse model calls for increased CH₄ flux from sources with strong spatial footprints in the tropics and Southern Hemisphere and decreases in sources in the Northern Hemisphere. The CH₄ and ¹³C/¹²C isotopic ratio observations suggest an unusually high CH₄ flux from swamps (~200 ± 44 Tg CH₄/yr) and biomass burning (88 ± 18 Tg CH₄/yr) with relatively low estimates of emissions from bogs (~20 ± 14 Tg CH₄/yr), and landfills (35 ± 14 Tg CH₄/yr). The model results support the hypothesis that the 1998 CH₄ growth rate anomaly was caused in part by a large increase in CH₄ production from wetlands, and indicate that wetland sources were about 40 Tg CH₄/yr higher in 1998 than 1999.

INDEX TERMS: 0315

Atmospheric Composition and Structure: Biosphere/atmosphere interactions; 0322 Atmospheric Composition and Structure: Constituent sources and sinks; 0368 Atmospheric Composition and Structure: Troposphere—constituent transport and chemistry; 1040 Geochemistry: Isotopic composition/chemistry; KEYWORDS: inverse model, isotopic signature, methane

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1. Introduction

[2] High-quality, quantitative estimates of the CH₄ budget are crucial to predicting climate change, managing Earth's carbon reservoirs, and understanding atmospheric chemistry. CH₄ is the second most important greenhouse gas after CO₂ and is responsible for approximately 20% of the direct radiative forcing from all long-lived greenhouse gases [Intergovernmental Panel on Climate Change (IPCC), 2001]. CH₄ is the second most important sink for OH radical, which is the primary determinant of the oxidizing capacity of Earth's atmosphere. In addition, CH₄ plays an important role in tropospheric O₃ pollution [Fiore *et al.*, 2002], and about half of all stratospheric water

vapor comes from the oxidation of CH₄ [Jones and Pyle, 1984].

[3] Over the last 150 years, the mixing ratio of CH₄ in the atmosphere has more than doubled [Etheridge *et al.*, 1998], primarily as the result of the addition of anthropogenic methane sources such as ruminant animal husbandry and rice agriculture, production of natural gas, coal mining, biomass burning, and landfills. CH₄ is also produced naturally by anaerobic bacteria in wetlands, dry tundra, and termites. The oceans evolve CH₄ from anaerobic bacteria in surface waters, fossil methane in marine sediments, and destabilization of methane hydrates, although these sources are thought to be relatively small due to oxidation of CH₄ in the water column. Oxidation of CH₄ by OH radical in the troposphere is the principle CH₄ sink, accounting for approximately 90% of all CH₄ destruction. In addition, CH₄ is oxidized by methanotrophic bacteria in aerobic soils and by reaction with OH, Cl, and O (1D) in the stratosphere.

[4] Despite the importance of CH₄ to Earth's radiative balance and atmospheric chemistry, there are still large

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t1.1 **Table 1.** Methane Budget and the Mean $\delta^{13}\text{C}_4$ Isotopic Signatures of the Sources and Sinks^a

t1.2	Sources	A Priori Estimates, Tg CH ₄ /yr	Range of Estimates Reported by IPCC [2001], Tg CH ₄ /yr	Mean Isotopic Signature
t1.3	Total wetlands		92–237	–58‰ ⁱ
t1.4	Swamps	91 ^a		
t1.5	Bogs and tundra	54 ^a		
t1.6	Rice agriculture	60 ^b	25–100	–63‰ ⁱ
t1.7	Ruminant animals	93 ^b	80–115	–60‰ ⁱ
t1.8	Termites	20 ^c	20–20	–70‰ ⁱ
t1.9	Biomass burning	52 ^d	23–55	–25‰ ⁱ
t1.10	Energy		75–109	
t1.11	Coal	38 ^b		–37‰ ⁱ
t1.12	Natural gas and other industrial	57 ^b		–44‰ ⁱ
t1.13	Landfills	50 ^e	35–73	–55‰ ⁱ
t1.14	Ocean	10 ^f	10–15	–60‰ ⁱ
t1.15	Hydrates	5 ^f	5–10	–60‰ ⁱ
t1.16	Total source	530	500–600	~–53‰ⁱ
t1.17	Sinks	A Priori Estimates, Tg CH ₄ /yr	Range of Estimates Reported by IPCC [2001], Tg CH ₄ /yr	Isotopic Fractionation
t1.18	Tropospheric OH	507 ^g	450–510	5.4‰ ^j
t1.19	Stratospheric loss	40 ^h	40–46	12‰ ^k
t1.20	Soils	30 ^h	10–30	22‰ ^l
t1.21	Total	577		~ 6.7‰

t1.22 ^aIPCC range of estimates covers the high and low estimates from a suite of budgets compiled using different approaches listed in the IPCC [2001] report. These estimates are typical of the range of estimates that can be found in the literature for CH₄ sources.

t1.23 ^bLelieveld *et al.* [1998].

t1.24 ^cEDGAR emissions database [Olivier *et al.*, 1996].

t1.25 ^dSanderson [1996].

t1.26 ^eLevine *et al.* [2000].

t1.27 ^fBingemer and Crutzen [1987].

t1.28 ^gCicerone and Oremland [1988].

t1.29 ^hOn the basis of Spivakovsky *et al.* [2000] OH fields and model CH₄ mixing ratios, tuned to IPCC [2001] total CH₄ loss.

t1.30 ⁱIPCC [2001].

t1.31 ^jWhiticar [1993].

t1.32 ^kCantrell *et al.* [1990].

t1.33 ^lBrenninkmeijer *et al.* [1995], reflecting the total observed isotopic fractionation due to OH, O¹D, and Cl in the stratosphere.

t1.34 ^mTyler *et al.* [1994].

66 uncertainties in estimates of the CH₄ fluxes as shown by the
67 wide range of IPCC [2001] estimates in Table 1, and the
68 causes for the observed variability in the recent CH₄ growth
69 rate are not well understood [Dlugokencky *et al.*, 2003,
70 2001, 1998]. The growth rate of atmospheric CH₄ for the
71 1990s has an overall decreasing trend and includes anom-
72 alous increases in the growth rate in 1991 and 1998 and a
73 large decrease in the growth rate during 1992. Much
74 progress has been made toward qualitatively attributing
75 these features to source and sink processes by correlating
76 them to changes in climate, fossil fuel consumption, and
77 other phenomena [i.e., Dlugokencky *et al.*, 1996; Bekki
78 *et al.*, 1994; Dlugokencky *et al.*, 1998]. The 1998 growth rate
79 anomaly occurred during an unusually warm year, marked
80 by precipitation anomalies associated with the transition
81 from a strong El Niño condition to a La Niña [Bell *et al.*,
82 1999; Curtis *et al.*, 2001]. Comparisons between the CH₄
83 growth rate anomaly and a process-based model of wetlands
84 which included temperature and precipitation anomalies
85 illustrated that increased biospheric production could
86 account for this event [Dlugokencky *et al.*, 2001].

Conversely, Langenfelds *et al.* [2002] and Van der Werf *et al.* [2004] attributed much of the 1997–1998 CH₄ anomaly to extensive fires.

[5] Process-level estimates of CH₄ fluxes have significant uncertainties due to the aggregation or extrapolation of local measurements, often representing only a limited time period, of sources with large spatial and temporal variability to regional or global scales. Model simulations of the CH₄ atmospheric mixing ratio resulting from these bottom-up source estimates typically overestimate the interhemispheric gradient of CH₄ relative to the observations [i.e., Fung *et al.*, 1991; Hein *et al.*, 1997; Houweling *et al.*, 1999] (also Figure 1, this study) implying that the sources may be overestimated in the Northern Hemisphere (NH) and/or underestimated in the Southern Hemisphere (SH).

[6] Inverse modeling is a “top-down” approach to optimize trace gas flux estimates using observations of atmospheric mixing ratios, a model of atmospheric transport, the spatial distributions of the sources, and, in most cases, a prior estimate of the source magnitudes to calculate an optimal combination of fluxes to match the observational

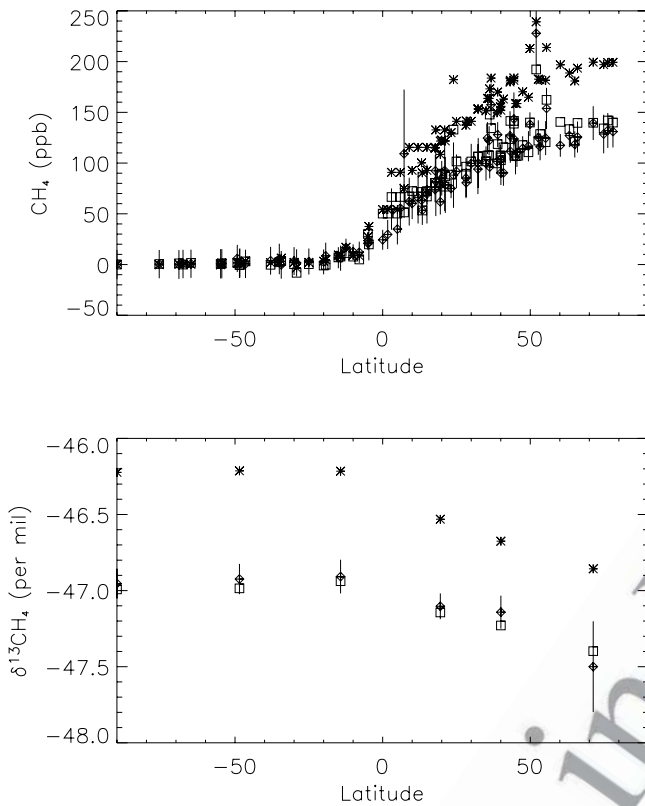


Figure 1. Latitudinal gradient of (top) CH_4 and (bottom) $\delta^{13}\text{C}_{\text{CH}_4}$ of the observations (diamonds), forward simulation based on the a priori estimates (asterisks), and forward simulation based on the a posteriori source estimates (squares). Error bars on the observations reflect the standard deviation of the individual observations from the annual mean.

108 data and our current understanding of the source processes.
 109 This technique has been applied to several atmospheric
 110 trace gases including CO_2 [e.g., Enting and Mansbridge,
 111 1989; Tans et al., 1990; Fan et al., 1998; Gurney et
 112 al., 2002], CH_4 [e.g., Hein et al., 1997; Houweling et al.,
 113 1999], and CO [e.g., Kasibhatla et al., 2002; Bergamaschi
 114 et al., 2000b].

115 [7] One of the difficulties associated with using atmo-
 116 spheric observations of CH_4 to gain insight into the sources
 117 and sinks of CH_4 is that atmospheric observations primarily
 118 provide information regarding the spatial distribution of the
 119 total CH_4 flux, and some of the CH_4 source processes have
 120 a great deal of spatial overlap. Two approaches have been
 121 used to address this issue in CH_4 inverse studies. In one
 122 approach, an inverse model was used to determine the
 123 spatial distribution of CH_4 flux required to match the
 124 atmospheric observations without differentiating the flux
 125 by source process [Houweling et al., 1999]. While this
 126 technique was able to reduce the uncertainty of the total
 127 CH_4 flux, especially in the NH, it provided limited insight
 128 into the physical processes responsible for the differences
 129 between the inverse model and process-based estimates. In
 130 an alternate approach, inverse models have been used to

estimate the magnitude of the total global fluxes for separate
 source process based on the spatial distribution of the
 sources [e.g., Hein et al., 1997; Bergamaschi et al.,
 2000a, 2001] or from separate source processes across large
 spatial regions [Chen, 2004]. These inverse estimates tend
 to find decreases in source estimates relative to the prior
 estimates for source processes with larger footprints in the
 NH and increases in sources with large footprints in the
 SH, consistent with the forward modeling results suggesting that
 a priori sources lead to an overestimate of the interhemis-
 pheric gradient. While Hein et al. [1997] were able to
 reduce the uncertainties associated with the source estimates
 using the station observations; they also found that a variety
 of different source scenarios could also match the observa-
 tional data, in line with the earlier work of Fung et al.
 [1991].

[8] Including observations of isotopic ratios in CH_4
 inversions may add a unique constraint to the problem by
 taking advantage of differences between the isotopic dis-
 crimination associated with different source processes. In
 addition to providing a new constraint to the underdeter-
 mined CH_4 inverse problem, observations of isotopic ratios
 may improve partitioning of the flux estimates between
 source processes with similar spatial patterns but differing
 isotopic signatures. The source processes can be separated
 into four broad categories based on their isotopic signatures:
 bacterial sources, including wetlands, rice paddies, ruminant
 animals, and termites, biomass burning, fossil sources, and
 landfills (Table 1).

[9] Previous inverse model studies have made limited use
 of observations of stable isotopes of CH_4 . Bergamaschi et
 al. [2000a] used the NOAA/CMDL observations of CH_4 to
 estimate the magnitude of the CH_4 source, then used
 observations from two SH stations and one NH station of
 the $^{13}\text{C}/^{12}\text{C}$ isotopic ratio in atmospheric CH_4 and the
 inverse CH_4 source estimates to optimize the isotopic
 signature of each source process. Hein et al. [1997] used
 observation of ^{13}C from three stations to further constrain
 their inverse study and optimize the isotopic signatures of
 the sources. However, since in the latter study only stations
 in the NH were used, interhemispheric gradient information
 was not included. Using a two-box model with annual,
 hemispheric averages of $^{13}\text{C}/^{12}\text{C}$ and CH_4 , Miller et al.
 [2002] conducted a simple inversion for two general CH_4
 source categories, bacterial CH_4 production and biomass
 burning, holding fossil fuel sources fixed. These studies
 found that measurements of $^{13}\text{C}/^{12}\text{C}$ isotopic ratios com-
 bined with measurements of CH_4 could provide constraints
 to the methane budget.

[10] Here we present the first time-dependent
 inverse estimates of CH_4 constrained by both the
 GLOBALVIEW- CH_4 data product and observations of the
 $^{13}\text{C}/^{12}\text{C}$ isotopic ratios from six NOAA/CMDL stations
 from 1998–1999. The variations between the two inverse
 model years are shown and discussed in the context of the
 1998 methane growth rate anomaly, and the inverse esti-
 mates are compared with recent process-based estimates and
 discussed in the context of observed physical phenomena
 likely to affect the source processes. In addition, the
 sensitivity of the inverse estimates is tested in response to

191 several potential sources of error. In a companion paper
 192 [Mikaloff Fletcher *et al.*, 2004], a complimentary technique
 193 will be used to interpret the relative source process con-
 194 tributions to regional CH₄ inverse estimates with observa-
 195 tions of ¹³C/¹²C isotopic ratios in CH₄.

196 2. Methods

197 [11] This study employs a time dependent assimilation
 198 and source retrieval technique [Bruhwiler *et al.*, 2000]. It is
 199 a conceptually straightforward mass balance approach that
 200 has minimal dependence on prior estimates. The behavior of
 201 a trace gas over time in the presence of sources, sinks, and
 202 transport processes can be described by the mass continuity
 203 equation,

$$\frac{dy}{dt} = \mathbf{T} \bullet y + S, \quad (1)$$

205 where \mathbf{T} is an operator that describes the atmospheric
 206 transport processes, y is the atmospheric abundance of the
 207 trace gas, and S is the net effect of sources and sinks.

208 [12] The effect of the sources over a given time step
 209 from a defined source region on the atmospheric abun-
 210 dance of a trace gas at an observing station in the absence
 211 of transport error over a given time period can be described
 212 by

$$y_j^{\text{obs}} - y_j = \sum_{i=1, \text{nsrc}} \mathbf{H}_{ij} x_i. \quad (2)$$

214 In this equation, y_j^{obs} is the observed mixing ratio at station j ,
 215 x_i is the source strength for the i th source region, and nsrc is
 216 the total number of source regions. The theoretical mixing
 217 ratio in the absence of sources, y , is calculated by applying
 218 the transport model to the three dimensional trace gas
 219 distribution from the previous time step without including
 220 source processes. \mathbf{H}_i is the basis function matrix which
 221 describes the signal observed at the station after one time
 222 step in response to an arbitrary, steady source from the i th
 223 source region, calculated by emitting 1 Tg CH₄/yr from the
 224 source region and allowing the transport model to act on
 225 these emissions. After the emissions have been transported
 226 for one inversion time step, in this case 1 month, the
 227 resulting mixing ratio distribution is sampled at the station
 228 locations. Thus, in the absence of error, the difference
 229 between the observed mixing ratio of a trace gas and the
 230 modeled mixing ratio in the absence of sources is described
 231 as a linear combination of the sources. This calculation was
 232 done monthly over the period of the inversion, 1998–2000.
 233 One important limitation to our inversion is that the basis
 234 functions only reflect 1 month of model transport. Errors in
 235 the flux estimates for a given month step are propagated to
 236 the next time step because they influence the modeled
 237 spatial distribution of the trace gas, y_j , in equation (2).
 238 Therefore an underestimate in the flux from a region in a
 239 given month may lead to an underestimate in the flux from
 240 that region or a neighboring region in a later month, since
 241 no mechanism is included for flux estimates from previous
 242 months to be adjusted based on observations for the current

month. This is likely to result in increased temporal noise in
 the inverse estimates.

[13] In addition to the station observation constraints used
 in the Bruhwiler *et al.* [2000], constraints from process-
 based estimates of the sources, or a priori estimates, have
 been included. A Singular Value Decomposition (SVD) is
 applied to determine the optimal source magnitudes
 required to match the observations and the prior estimates.
 When including a priori estimates, the relative weighting of
 the atmospheric observations and the a priori estimates
 based on their estimated uncertainty, σ , plays a critical role
 in the inverse flux estimates. In the limit of high model-data
 mismatch error relative to the prior uncertainty, the a
 posteriori inverse estimates may primarily reflect the a priori
 estimates. In this inversion, the uncertainty associated with
 the prior estimates was set equal to the difference between
 the high and low estimates for each source process
 published in the IPCC [2001] (Table 1), except in the case
 of termites, where the uncertainty was assumed to be 20 Tg
 CH₄/yr. The uncertainty associated with the observational
 data is much less straightforward, because it is not primarily
 associated with the measurements themselves; rather, it due
 to limitations in the model’s ability to describe the station
 observations. In this study, an average uncertainty was
 estimated for both continental and coastal or marine sites
 based on the mean standard deviation of the residuals from
 the smooth curve in the observations. Sites sampling marine
 air were assigned a model-data mismatch uncertainty of
 10 ppb and those sampling continental air were assigned an
 uncertainty of 21 ppb. This choice of sigma values results in
 a primarily data-driven inversion with the a priori
 constraints only ruling out truly nonphysical results such
 as uptake due to processes known to act exclusively as
 sources.

[14] In this experiment, following Hein *et al.* [1997], each
 source process is estimated separately with the spatial
 distribution of the source processes represented by the
 NASA Goddard Institute for Space Studies (GISS) flux
 maps described by Fung *et al.* [1991]. As in the work of
 Fung *et al.*, the five major wetland types [Matthews and
 Fung, 1987] are grouped into two broad categories: bogs,
 which occur mainly between 50°N and 70°N, and swamps,
 which primarily occur in the tropics. The isotopic signature
 of each source is prescribed in order to use the isotopic
 ratios measured at each observing station as additional
 constraints on the methane flux estimates. It is important to
 note that source process inversions are subject to significant
 error due to the inherent assumption that the a priori spatial
 distribution of each source process is correct and has little or
 no interannual variability. In addition, the large spatial
 extent of the source processes may lead to errors. Since the
 internal spatial distribution of the sources for a model region
 cannot be adjusted by the inversion and the sampling
 network is sparse, inaccuracies and unrepresented varia-
 bility in the spatial pattern for the region have been shown
 to introduce biases, also called “aggregation error”
 [Kaminski *et al.*, 1999]. Conversely, if very small model
 regions are used in an inverse model, the current observing
 network is unlikely to be able to provide sufficient
 constraints for many of the model regions, resulting in

303 inverse estimates that are strongly determined by a priori
304 estimates.

305 [15] Equation (2) can be rewritten in terms of ^{13}C as

$$R_j^{\text{obs}} y_j^{\text{obs}} - R_j y_j = \sum_{i=1, \text{nsrc}} \mathbf{H}_{i,j} R_i x_i, \quad (3)$$

307 where R_j^{obs} and R_j represent the $^{13}\text{C}/^{12}\text{C}$ ratios of
308 the observations and the model simulation, calculated in
309 the absence of sources during the time step, and R_i is the
310 isotopic ratio of $^{13}\text{C}/^{12}\text{C}$ in CH_4 observed for each source
311 process. In order to isolate very small changes in the
312 isotopic ratio due to the isotope effects of source and sink
313 processes, stable isotope ratios are conventionally expressed
314 as $\delta^{13}\text{C}$, the fractional deviation of the isotopic ratio of the
315 sample, R_{sample} , from a standard, $R_{\text{reference}}$.

$$\delta^{13}\text{C} = \left(\frac{R_{\text{sample}}}{R_{\text{reference}}} - 1 \right) \times 1000. \quad (4)$$

317 By using a linear combination of equation (2) and
318 equation (3) and applying the definitions of $\delta^{13}\text{C}$
319 (equation (4)), we can write an equation for the CH_4
320 sources in terms of both $\delta^{13}\text{CH}_4$ and CH_4 (Appendix A).

$$\delta_j^{\text{obs}} y_j^{\text{obs}} - \delta_j y_j = \sum_{i=1, \text{nr}} \mathbf{H}_{i,j} x_i \delta_i^{\text{src}}, \quad (5)$$

322 where δ_i^{src} is the isotopic signature of the i th source process.
323 The uncertainty estimate, equation (5), which plays an
324 important role in estimating the a posteriori error estimates
325 and the relative weighting of each linear equation in the
326 system of linear equations, is expressed in terms of the
327 uncertainty associated with δ , σ_j^{δ} , and the uncertainty
328 associated with y , σ_j^y .

$$\sigma = \sqrt{(\sigma_j^y y_j)^2 + (\delta_j \sigma_j^{\delta})^2}. \quad (6)$$

330 Thus, if equation (5) were used, the uncertainty for the
331 isotopic signature constraints would be strongly dependent
332 on the arbitrary reference value selected in equation (4),
333 $R_{\text{reference}}$. Therefore we set the reference ratio equal to the
334 calculated isotopic ratio expected in the absence of sources,
335 which is different for each station, such that the calculated
336 $\delta \equiv 0$ and equation (5) reduces to

$$\delta_j^{*\text{obs}} y_j^{\text{obs}} = \sum_{i=1, \text{nr}} \mathbf{H}_{i,j} x_i \delta_i^{*\text{src}}, \quad (7)$$

338 where $\delta^{*\text{obs}}$ and $\delta_i^{*\text{src}}$ represent the delta values defined in
339 terms of the calculated isotopic ratio for each station.
340 Equation (7) is added to the inversion as an additional
341 constraint on the CH_4 flux estimates.

342 [16] The isotopic ratios used in this equation are shown in
343 Table 1. The biomass burning source has a spatial pattern in
344 the isotopic signature of the sources. The two primary plant
345 photosynthetic pathways, C-3 and C-4, have differing
346 isotopic signatures in plant biomass leading to differing

isotopic signatures in emissions from combustion of C-3 347
and C-4 plants [Chanton *et al.*, 2000]. To account for this, a 348
spatial map of the relative fraction of C-4 plants [Still *et al.*, 349
2003] and mean isotopic signatures from C-3 and C-4 plants 350
[Chanton *et al.*, 2000] are applied to create a spatially 351
varying isotopic signature from biomass burning. The 352
resulting global mean isotopic signature from biomass 353
burning is -25% . 354

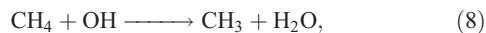
[17] The initial conditions were set as close to the real 355
atmosphere as possible. First, a “test” inverse model was 356
initialized to the observed hemispheric mean values of 357
atmospheric CH_4 and $\delta^{13}\text{CH}_4$ [Miller *et al.*, 2002] and run 358
from 1998 to 2000. The three-dimensional CH_4 and $\delta^{13}\text{CH}_4$ 359
fields from the final time step of this “test” inversion are 360
then used to initialize the inverse model. The first 3 months 361
of the final inverse results were excluded for further model 362
spin-up time. Three months is the time required for the 363
modeled CH_4 mixing ratios to be further corrected by the 364
station observations such that the differences between 365
modeled and observed CH_4 no longer reflect inaccuracies 366
in the initial conditions. 367

[18] Recent work has shown that it takes much longer to 368
establish large-scale spatial gradients in the isotopic ratios 369
than total CH_4 [Tans, 1997; Lassey *et al.*, 2000]. This 370
implies there may be a slowly adjusting drift in the 371
calculated atmospheric isotopic ratios due to inaccuracies in 372
the initial conditions, which would lead to errors in the 373
source partitioning by the inverse model. However, these 374
errors are likely to be smaller than the errors associated with 375
paucity of available data [Tans, 1997]. 376

[19] The transport was represented by the coarse-grid 377
version of the global, three-dimensional tracer transport 378
model, Transport Model 3 version 3.3 (TM3) [Heimann 379
and Körner, 2003], with a spatial resolution of 7.8° latitude 380
by 10° longitude by nine vertical levels. TM3 solves the 381
continuity equation numerically for an arbitrary number of 382
trace gases in a three-dimensional Eulerian grid using ‘off- 383
line’ wind fields. The National Centers for Weather 384
Prediction/National Center for Atmospheric Research 385
(NCEP/NCAR) wind fields concurrent with the model year 386
were used. Recent model studies have suggested that a 387
significant part of the inter-annual variability in the CH_4 388
growth rate may be explained by variability in model 389
transport [Warwick *et al.*, 2002; Johnson *et al.*, 2002], 390
implying that using meteorology corresponding to the 391
current model year rather than repeating meteorology from 392
a single year may be critical in correctly inferring surface 393
fluxes from the observed CH_4 mixing ratios. Tracer 394
transport that is resolved in the model grid is calculated 395
using a “slopes scheme” [Russell and Lerner, 1981], where 396
the distribution of each tracer within each model grid-box is 397
represented by a three-dimensional linear slope of the 398
mixing ratio distribution. Vertical sub-grid scale transport is 399
calculated based on cumulus cloud convection [Tiedke, 400
1989] and vertical diffusion based on calculated air stability 401
[Louis, 1979]. The ability of TM2, an earlier version of the 402
model, and the fine grid version of TM3 to reproduce 403
important features of tracer transport such as the interhemi- 404
spheric gradient and seasonal cycle due to transport of a 405
trace gas has been tested with SF_6 , a chemically and 406

407 biologically neutral trace gas with a single, well-known
 408 anthropogenic source in the TransCom Model Intercompar-
 409 ison experiment [Denning *et al.*, 1999], and the role of the
 410 choice of model resolution on tracer transport in TM3 has
 411 been explored by Heimann and Körner [2003].

412 [20] The CH₄ sinks due to tropospheric OH, stratospheric
 413 loss, and oxidation by aerobic soils were prescribed and not
 414 optimized. CH₄ is oxidized by OH in the following reaction:



416 which has a temperature-dependent rate constant of $k =$
 417 $2.45 \times 10^{-12} \text{ cm}^{-3} \text{ s}^{-1} e^{-1775/T}$ [DeMore *et al.*, 1997]. The
 418 global distribution of OH was represented by the monthly
 419 OH fields of Spivakovsky *et al.* [2000], which were scaled to
 420 match the IPCC estimate of 507 Tg CH₄/yr. These OH
 421 fields have been tested for consistency with the budgets of
 422 CH₃CCl₃, a trace gas with well-known emissions that is
 423 destroyed primarily by OH oxidation, in addition to a suite
 424 of other important atmospheric trace gases [Spivakovsky *et al.*,
 425 2000]. Spivakovsky *et al.* [2000] estimated the total
 426 uncertainty to be no greater than $\pm 15\%$.

427 [21] The destruction of CH₄ by OH was assigned a
 428 Kinetic Isotope Effect (KIE) of 1.0054 based on the
 429 laboratory measurements of Cantrell *et al.* [1990]. A more
 430 recent measurement of this KIE of 1.0039 has been made by
 431 Saueressig *et al.* [2001]. This value is used to test the
 432 sensitivity of the inverse result to the KIE of CH₄
 433 destruction by tropospheric OH.

434 [22] In addition to the tropospheric OH sink, which is
 435 responsible for approximately 88% of total CH₄ loss, CH₄ is
 436 destroyed in the stratosphere by OH, Cl, and O¹D. Owing to
 437 the large Kinetic Isotope Effect (KIE) of CH₄ destruction by
 438 Cl, the stratospheric loss term has relatively strong influence
 439 on atmospheric $\delta^{13}\text{CH}_4$ in comparison to CH₄ [Gupta *et al.*,
 440 1996; McCarthy *et al.*, 2001]. A spatially uniform strato-
 441 spheric loss term with a global total equal to the IPCC
 442 [2001] estimate of 40 Tg CH₄/yr was applied to all model
 443 grid cells above the temperature inversion as defined by off-
 444 line temperature fields. Following Hein *et al.* [1997], total
 445 isotopic fractionation of CH₄ due to chemical destruction in
 446 the stratosphere by OH, Cl, and O¹D was assigned an
 447 isotopic discrimination of 12‰ based on observations of the
 448 correlation between $\delta^{13}\text{CH}_4$ and CH₄ in aircraft measure-
 449 ments [Brenninkmeijer *et al.*, 1995]. These measurements
 450 occurred near the tropopause at high southern latitudes, a
 451 region of strong transport from the stratosphere to the
 452 troposphere and are in good agreement with the observa-
 453 tions of Sugawara *et al.* [1997]. Tropospheric Cl was not
 454 represented in the model, but recent measurements have
 455 suggested that there may be a significant active Cl sink in
 456 the boundary layer [Platt and Hönninger, 2003]. Owing to
 457 the large Cl KIE, this is an important source of uncertainty
 458 in the interpretation of the $\delta^{13}\text{CH}_4$ observations.

459 [23] The spatial distribution of the soil sink was repre-
 460 sented by the NASA GISS field described by Fung *et al.*
 461 [1991], and the total flux was tuned to the IPCC [2001]
 462 emission estimate of 30 Tg CH₄/yr. An isotopic fractiona-
 463 tion of 22‰ was assigned to the soil sink based on the
 464 measurements of Tyler *et al.* [1994]. Like the stratospheric

sink, owing to its strong isotopic fractionation the soil sink
 has a much greater impact on the atmospheric $\delta^{13}\text{CH}_4$ than
 it does on total CH₄.

[24] The GLOBALVIEW-CH₄ data product based on
 measurements from several international laboratories was
 used to represent the spatiotemporal CH₄ distribution
 (GLOBALVIEW-CH₄ [National Oceanic and Atmospheric
 Administration (NOAA), 2001]). GLOBALVIEW-CH₄ is
 based on regular samples collected at 67 land stations and
 along two ocean ship tracks. The ship tracks sample 17
 positions in the Pacific Ocean and seven positions in the
 South China Sea. The sampling sites are preferentially
 located to sample remote marine boundary layer air in order
 to ensure that the samples consist of well-mixed air,
 representing background mixing ratios of the trace gases
 measured. Duplicate samples are collected in flasks,
 typically once per week, and analyzed for CH₄ by gas
 chromatography (GC) followed by flame ionization detec-
 tion (FID). The measurements are adjusted to a single scale,
 the NOAA Climate Monitoring Diagnostics Laboratory
 (NOAA CMDL) scale, in order to account for differences
 between individual laboratories' standard scales [NOAA,
 2001].

[25] In order to create a temporally consistent time series
 over all the contributing stations, these observations are fit
 to a smoothed curve and the smoothed curve is sampled at
 regular, 7.6 day intervals. In cases where the data record is
 incomplete, the existing observations are extended based on
 the site climatology and observations from remote marine
 boundary sites at similar latitudes. The data extension and
 integration process used in GLOBALVIEW is described in
 more detail by Masarie and Tans [1995].

[26] Weekly, duplicate flask samples from six NOAA
 CMDL Cooperative Air Sampling Network have been
 sampled for $\delta^{13}\text{CH}_4$ at the Institute for Arctic and Atmo-
 spheric Research (INSTAAR) by GC isotope-ratio-mass-
 spectrometry (IRMS) since 1998 [Miller *et al.*, 2002]. The
 stations sampled for $\delta^{13}\text{CH}_4$ are Barrow, Alaska
 (71°N), Niwot Ridge, Colorado (40°N), Mauna Loa, Hawaii
 (20°N), Cape Matatula, American Samoa (14°S), Cape
 Grim, Tasmania (40°S), and South Pole, Antarctica (90°S).
 These observations are fit to a smoothed curve, excluding
 outliers more than 3 standard deviations from an initial
 smoothed curve fit. The smoothed curve is sampled at
 7.6 day intervals to create a $\delta^{13}\text{CH}_4$ data set comparable to
 GLOBALVIEW-CH₄. It is worthy of note that trace gas
 observations at American Samoa are particularly difficult to
 interpret due to the complex tropical meteorology at this
 site, and this station may be especially sensitive to errors in
 model transport.

[27] Long-term observational records of $\delta^{13}\text{CH}_4$ are avail-
 able for a number of other observing stations [e.g., Lowe *et al.*,
 1994; Quay *et al.*, 1999; Bergamaschi *et al.*, 2000a].
 National Institute of Water and Atmospheric Research
 (NIWA) observations of $\delta^{13}\text{CH}_4$ at Baring Head, New
 Zealand, and Scott Base, Antarctica [Lowe *et al.*, 1994], are
 used to validate the inverse estimates in section 6, but only
 the $\delta^{13}\text{CH}_4$ observations from the NOAA/CMDL network
 are used to constrain the inversion. The CH₄ observations
 from different laboratories have been carefully compared,

t2.1 **Table 2.** Summary of the Inversion Scenarios Implemented to Compare Prior Estimates With Inverse Results and Test the Sensitivity of the Inverse Results to Various Potential Sources of Error

t2.2	Scenario	Description	Additional Details
t2.3	S0	a priori source estimates	forward simulation of prior source estimates shown in Table 1
t2.4	S1	a posteriori estimates, excluding observations of $\delta^{13}\text{CH}_4$	inverse source estimates using CH_4 observations and prior estimates only, with no $\delta^{13}\text{CH}_4$ constraints
t2.5	S2	a posteriori estimates, including observations of $\delta^{13}\text{CH}_4$	inverse source estimates with $\delta^{13}\text{CH}_4$ constraints in addition to observations of CH_4 and prior estimates
t2.6	S3	sensitivity to OH kinetic isotope effect	S2 with the <i>Saueressig et al.</i> [2001] measurement of the KIE for OH
t2.7	S4	sensitivity to OH fields-upper limit	S2 with OH increased by 15% to the upper end of the uncertainty estimate of <i>Spivakovsky et al.</i> [2000]
t2.8	S5	sensitivity to OH field-lower limit	S2 with OH decreased 15% to the lower end of the uncertainty estimate of <i>Spivakovsky et al.</i> [2000]
t2.9	S6	sensitivity to initial conditions	S2 initialized to the observed hemispheric mean CH_4 and $\delta^{13}\text{CH}_4$ for 1998 [<i>Miller et al.</i> , 2002]

525 adjusted to a common scale [NOAA, 2001], and are
 526 available as a single, self-consistent data set. Limited
 527 comparisons between NOAA/CMDL observations and data
 528 from NIWA, *Quay et al.* [1999], and *Francey et al.* [1999]
 529 suggest there may be offsets between laboratories of about
 530 0.1‰ [Miller et al., 2002], about 15% of the interhemi-
 531 spheric gradient. Therefore, careful measurement intercom-
 532 parisons and linking of scales are essential before these data
 533 can be incorporated in the inversion to avoid introducing
 534 large biases.

535 [28] Inverse estimates were calculated for a variety of
 536 different “inverse scenarios,” summarized in Table 2, to
 537 isolate the impact of including the $\delta^{13}\text{CH}_4$ observations and
 538 test the sensitivity of the inverse estimates to uncertainties in
 539 the model.

540 [29] The first scenario, S0, is simply the a priori source
 541 estimates. These source estimates have been chosen to
 542 reflect a best process-based estimate only; therefore they
 543 do not balance the CH_4 budget. S1 is the inverse estimate
 544 including only the observations of CH_4 , but excluding
 545 observations of $\delta^{13}\text{CH}_4$, and S2 is the inverse model
 546 incorporating the observations of $\delta^{13}\text{CH}_4$. Throughout this
 547 paper, if the scenario being discussed is not explicitly
 548 specified, we refer to S2. Scenarios 3 to 7 test the sensitivity
 549 of the inverse model to uncertainties in OH chemistry,
 550 model transport year, and initial conditions. The base

scenario, S2, uses a KIE of 5.4‰ for the oxidation of
 CH_4 by OH. S3 applies the more recent measurement of
 OH KIE [Saueressig et al., 2001]. The error associated with
 the OH fields used to represent the chemical sink in this
 study has been estimated as $\pm 15\%$ [Spivakovsky et al.,
 2000]. To explore the sensitivity to this error, the OH fields
 have been increased uniformly by 15% in S4 and decreased
 by 15% in S5. Recall that the total OH sink based on the
 within-model CH_4 mixing ratio using the Spivakovsky OH
 fields of 470 Tg CH_4/yr has been adjusted to match the
 IPCC estimate of 507 Tg CH_4/yr , which is within the error
 limits of the Spivakovsky OH fields. The 15% variation for
 these scenarios was applied to the uncorrected value of
 470 Tg CH_4/yr in keeping with the original context of the
 error estimate. As a result, these scenarios are expected to be
 asymmetric around the base scenario. Finally, in S6, the
 model is initialized to the observed hemispheric mean
 atmospheric CH_4 and $\delta^{13}\text{CH}_4$ to evaluate the sensitivity of
 the inverse estimates to small errors in the initial conditions
 after the relatively short model spin-up time [Tans, 1997].

3. Inverse Estimates

[30] Comparing the a priori estimates with the a posteriori
 estimates (Table 3) constrained by the CH_4 observations
 alone (S1), the largest single change is the dramatic increase

t3.1 **Table 3.** Annual Mean Source Estimates for the A Priori Fluxes (S0) and the 1998–1999 Mean a Posteriori Estimates for the Inverse Scenarios Described in Table 2^a

t3.2	Sources	S0	S1	S2	S3	S4	S5	S6
t3.3	Swamps	90	204 ± 46	206 ± 44	196 ± 44	228 ± 44	134 ± 44	200 ± 44
t3.4	Bogs	50	8 ± 15	21 ± 14	22 ± 14	20 ± 14	25 ± 14	23 ± 14
t3.5	Tundra	5	3 ± 4	4 ± 4	5 ± 4	4 ± 4	4 ± 4	4 ± 4
t3.6	Rice agriculture	60	69 ± 18	54 ± 17	50 ± 17	56 ± 16	47 ± 17	59 ± 17
t3.7	Ruminant Animals	93	94 ± 19	91 ± 18	88 ± 18	91 ± 18	89 ± 18	91 ± 18
t3.8	Termites	20	36 ± 19	29 ± 18	22 ± 18	30 ± 18	24 ± 18	33 ± 18
t3.9	Biomass Burning	52	65 ± 20	88 ± 18	102 ± 18	94 ± 18	68 ± 18	80 ± 18
t3.10	Coal	38	30 ± 12	30 ± 11	34 ± 11	31 ± 12	28 ± 11	29 ± 11
t3.11	Natural gas	57	57 ± 18	52 ± 18	56 ± 18	53 ± 18	46 ± 18	53 ± 18
t3.12	Landfills	50	42 ± 14	35 ± 14	35 ± 14	36 ± 14	33 ± 14	37 ± 14
t3.13	Total source	515	609	610	610	644	498	609

t3.14 ^aNote that the relatively small ocean sources and all of the CH_4 sinks have been prescribed.

575 in CH₄ from swamps relative to the a priori estimates. This
576 difference is driven by the fact that forward simulations of
577 the a priori estimates lead to an underestimate of SH CH₄
578 mixing ratios compared to the observations, as shown in
579 Figure 1. Since swamps have a strong spatial footprint in
580 the SH and the a priori estimates for wetlands are highly
581 uncertain, the inverse model calls for an increase in
582 swamps to match the interhemispheric gradient. Adding
583 the observations of $\delta^{13}\text{C}$ (S2) does not significantly
584 change this conclusion. Since the isotopic signature of
585 wetlands is strongly depleted in ¹³C compared to the
586 atmosphere, this source is expected to be well constrained
587 by the observations of atmospheric $\delta^{13}\text{C}$. Therefore
588 the observations of CH₄ and $\delta^{13}\text{C}$ both strongly support
589 an increased source from swamps. From a strictly
590 atmospheric perspective, these features of the CH₄ obser-
591 vations might also be matched by a large increase in the
592 ocean source, which was prescribed in this study, rather
593 than an increase in swamp emissions. However, shipboard
594 measurements of seawater and atmospheric CH₄ do not
595 support such a dramatic increase in the oceanic CH₄ flux
596 estimates [e.g., *Bange et al.*, 1998; *Bates et al.*, 1996;
597 *Bange et al.*, 1994].

598 [31] Two recent process-model studies have also called
599 for increased wetland spatial coverage or CH₄ flux from
600 wetlands. Using a GCM in conjunction with a vegetation
601 model and algorithms for determining wetland area based
602 on topography and soil moisture, *Kaplan* [2001] estimated
603 11.0×10^6 km² of wetlands globally, about twice the spatial
604 coverage estimated by earlier wetland inventory approaches
605 [i.e., *Aselmann and Crutzen*, 1989; *Matthews and Fung*,
606 1987]. This was largely attributed to temporary wetlands
607 that are inundated for only part of the year and are therefore
608 not likely to be accounted for in wetland inventories. These
609 seasonal wetlands accounted for 61% of the total wetland
610 area estimate in this study, and over half of the seasonal
611 wetlands occur in the tropics. Although this study does
612 show a large increase in the spatial extent of wetlands
613 compared to previous work, *Kaplan* concluded a CH₄
614 wetland source of 140 Tg CH₄/yr, only about 30 Tg CH₄/yr
615 more than the inventory-based estimate of *Matthews and*
616 *Fung* [1987] using a CH₄ flux estimation technique based
617 on heterotrophic respiration. In addition to the *Kaplan* study,
618 *Walter* [1998] used a process model to calculate flux from
619 wetlands as a function of temperature and hydrological
620 conditions, finding an unusually large source of 263 Tg
621 CH₄/yr, even higher than that found in this top-down
622 approach.

623 [32] The previous CH₄ inversions of *Hein et al.* [1997]
624 and *Bergamaschi et al.* [2001] also found a large source
625 from swamps. *Chen* [2004] found a lower total wetland
626 source of 140–150 Tg CH₄/yr but very high emissions from
627 rice cultivation of 110–120 Tg CH₄/yr. He suggested that
628 the high inverse estimate rice paddies may be partially due
629 to wetlands since wetlands and rice paddies have similar
630 spatial patterns and seasonal cycles. These studies are based
631 on different time periods than this one, so these estimates
632 are not entirely comparable; however, they are consistent
633 with the hypothesis that CH₄ emissions from swamps may
634 be underestimated.

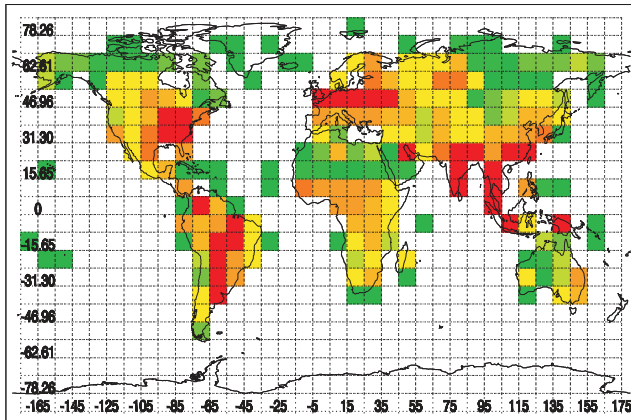
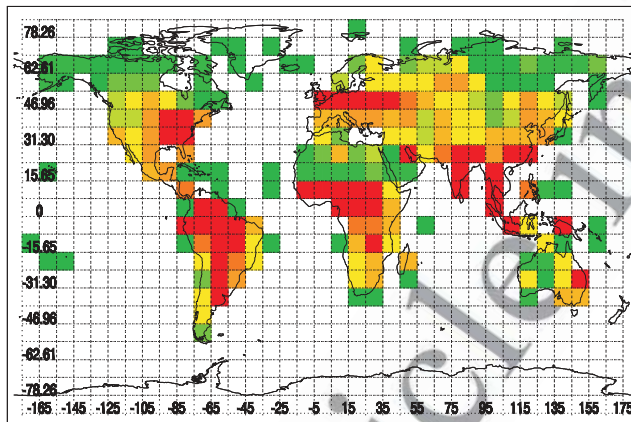
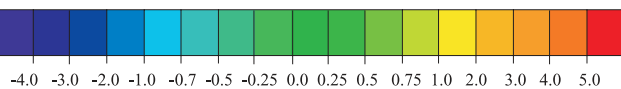
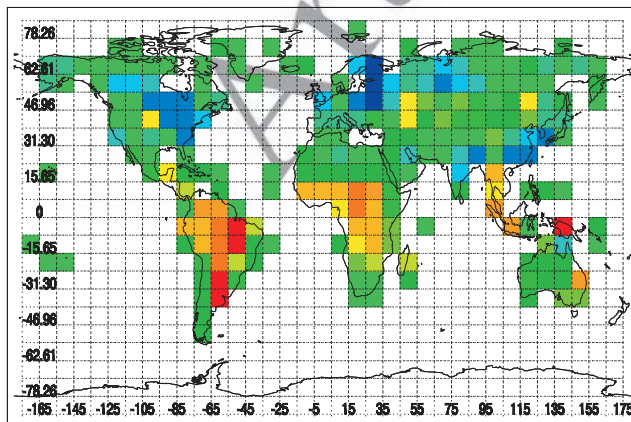
[33] The inverse flux estimates from bogs are reduced 635
relative to the a priori sources based on the CH₄ observa- 636
tions alone (S1), which is not surprising since this source 637
has a large spatial pattern in the NH, and the priors tend to 638
overestimate sources in the NH slightly in the forward 639
model. However, in S2, constrained by the observations 640
of $\delta^{13}\text{C}$, this source is not as greatly reduced. Like 641
swamps, the distinctive isotopic signature of the source 642
from bogs is expected to provide a strong constraint for 643
this source process. A very low estimate of CH₄ from bogs 644
from the 1998–1999 period would have been surprising 645
since 1998 was an unusually warm year with positive 646
precipitation anomalies over many high northern latitude 647
land regions during the growing season [*Bell et al.*, 1999; 648
Curtis et al., 2001], and the anomalously high growth rate 649
in 1998 has been partially attributed to increased emissions 650
from northern wetlands resulting from these conditions 651
[*Dlugokencky et al.*, 2001]. 652

[34] Both S1 and S2 estimated a somewhat high source 653
estimate for termites, although this difference is not large 654
compared to the error estimates on the a posteriori sources. 655
Since termites are a small, spatially diffuse source with a 656
similar isotopic signature to wetlands, rice paddies, and 657
ruminant animals, the station observations may not be 658
sufficient to discriminate between this source and the other 659
bacterial sources. 660

[35] As shown in Table 1, the a priori estimate for 661
biomass burning used in this study is on the high end of 662
the range of biomass burning estimates. This high estimate 663
of biomass burning is consistent with the observations of 664
CH₄, since differences between S1 and the a priori estimate 665
are small compared to the uncertainty. The observations of 666
 $\delta^{13}\text{C}$ call for an even greater biomass burning source. 667
This source is expected to be better constrained by the 668
observations of $\delta^{13}\text{C}$ than any other source process. Like 669
bacterial sources, biomass burning has a very distinctive 670
isotopic signature; however, unlike these sources the isotopic 671
signature of biomass burning is not shared by any other 672
source process. The inverse studies of *Hein et al.* [1997], 673
and *Bergamaschi et al.* [2001] indicated a much lower 674
biomass burning source than this study, and the estimates of 675
Chen [2004] were somewhat lower. This may be due in part 676
to the limited use of $\delta^{13}\text{C}$ observations to constrain the 677
total CH₄ budget in these studies, the differing observational 678
time period, or differences in inverse methodologies. *Miller* 679
et al. [2002] and *Quay et al.* [1999] also found relatively 680
high biomass burning sources using global mass balance 681
calculations of CH₄ and $\delta^{13}\text{C}$. In addition, recent studies 682
have indicated that the biomass burning source may have 683
been elevated during the period of this inversion 684
[*Langenfelds et al.*, 2002; *Van der Werf et al.*, 2004]. 685

[36] The landfill source estimate is reduced slightly com- 686
pared to the a priori estimates by the observations of 687
atmospheric CH₄ and reduced further by the inclusion of 688
the $\delta^{13}\text{C}$ observations. The isotopic signature of the 689
landfill source is very close to that of the background 690
atmosphere, so it is not constrained very well by the 691
atmospheric isotopic data. 692

[37] Differences between a priori and a posteriori esti- 693
mates of CH₄ emissions from tundra, rice agriculture, 694

Total *A Priori* FluxTotal *A Posteriori* FluxDifference Between *A Posteriori* and *A Priori*Methane Flux (Tg CH₄/grid box)

695 ruminant animals, coal, and natural gas are small compared
696 to the inverse error estimates for both S1 and S2. In order to
697 visualize the differences between the total a priori and a
698 posteriori fluxes spatially, the emissions estimates from the
699 source processes were used to create a total flux map by
700 multiplying the assumed a priori spatial pattern for each
701 source process by the corresponding inverse source esti-
702 mate. Recall that we have not estimated the flux from
703 each grid box individually. In Figure 2, the total flux
704 maps for the a priori CH₄ flux, the a posteriori CH₄ flux
705 (S2), and the differences between the a priori and a
706 posteriori estimates are compared. While the small ocean
707 source has been prescribed, there are some emissions
708 occurring in ocean regions due to the presence of
709 islands.

[38] Overall, the a posteriori estimates have been reduced
710 relative to the a priori sources in the NH and increased in the
711 SH, which is consistent with the changes expected from the
712 interhemispheric gradient of the forward simulation in
713 Figure 1. In North America and western Europe, the total
714 a posteriori flux is smaller than the a priori flux, largely due
715 to decreases in estimated emissions from landfills and coal
716 in industrial regions and the small decrease in bogs at high
717 northern latitudes. In eastern Eurasia, there is a slight
718 decrease in some high-latitude regions due to the decrease
719 in the a posteriori bog source relative to the a priori sources
720 and an increase in midlatitudes resulting from the large
721 increase in swamps.
722

[39] The spatial pattern of the difference between the a
723 priori and a posteriori fluxes is especially interesting in
724 Southeast Asia. In much of Asia, there is a decrease in
725 the total a posteriori flux estimates relative to the a priori
726 source estimates due to decreases in the emissions from
727 rice agriculture and coal mining. However, nearby grid
728 boxes in southern China and Indonesia show a great
729 increase in CH₄ emissions over the a priori sources
730 caused by the dramatic increase in the swamp source
731 strength. This may be a bias in the model associated with
732 the large spatial extent of the source-process regions. It is
733 possible that the spatial pattern of swamps overestimates
734 relative importance of the wetland contribution from these
735 islands. However, due to the aggregation of the CH₄
736 fluxes to an entire source process in the inverse model,
737 the flux from this small region must be increased pro-
738 portionally to all other swamps, possibly leading to an
739 overestimate of the flux from these islands. In order to
740 accommodate this overestimate, the inverse model might
741 underestimate the source from the continental rice
742 paddies. This possibility illustrates one of the major
743 problems associated with this type of inverse model.
744 Since the isotopic signatures of rice paddies and swamps
745 are similar, including the observations of $\delta^{13}\text{C}_{\text{CH}_4}$ is not
746 likely to improve this problem.
747

Figure 2. Global distribution of CH₄ flux in Tg CH₄ grid cell⁻¹ yr⁻¹ averaged over the 1998–1999 inversion time period for (top) a priori estimates, (middle) a posteriori estimates (S2), and (bottom) the difference between the a posteriori estimates and the a priori estimates.

t4.1 **Table 4.** Hemispheric and Global Total CH₄ Fluxes of the A Priori Estimates, Inverse Estimates Constrained by the Isotopes (S2), and the Work of *Houweling et al.* [1997]

t4.2	Region	A Priori Estimates (S0)	A Posteriori Estimates (S2)	<i>Houweling et al.</i> [1999]
t4.3	NH	398	401	340
t4.4	SH	127	209	165
t4.5	NH:SH ratio	3.1	1.9	2.0
t4.6	Global total	525	610	505

748 [40] The largest increases in CH₄ flux over the a priori
749 estimates occur in South America and Africa, and are
750 primarily driven by the large increase in swamps and
751 biomass burning and secondarily affected by the larger a
752 posteriori estimates of termites and natural gas. This change
753 is in approximate agreement with the inverse CH₄ flux maps
754 of *Houweling et al.* [1999].

755 [41] The hemispheric distribution of the sources in the a
756 priori estimates, the a posteriori estimates, and the inverse
757 study of *Houweling et al.* [1999] are compared in Table 4.
758 As illustrated in more detail above, the NH:SH ratio is
759 strongly reduced by including the atmospheric observations.
760 The a posteriori NH:SH ratio used in this study is
761 remarkably similar to the values estimated by *Houweling*
762 *et al.* [1999], despite significant differences in the model
763 representation of the OH sink, inverse technique, and time
764 period of the inverse model. The *Houweling* study
765 [*Houweling et al.*, 1999] used a chemistry transport model
766 (CTM) tuned to match the CH₃CCl₃ observations to
767 represent the OH chemistry and a time-independent inverse
768 technique in which the inverse model was solved for each
769 model grid box rather than aggregating the model to larger
770 inverse regions. The similarities between the NH:SH ratio
771 of these very different inverse models suggests this feature
772 is robust with respect to OH loss and inverse technique and
773 strongly driven by the atmospheric data. The large
774 differences between the global total CH₄ flux estimated
775 by *Houweling et al.* and this study are due partly to the fact

that they were modeling an earlier time period (1993–1995) 776
and partly to the smaller estimate of the OH sink (450 Tg 777
CH₄/yr) by *Houweling et al.* 778

4. Interannual Variability 779

[42] The time period covered by these estimates coincides 780
with the anomalously large 1998 CH₄ growth rate followed 781
by a decrease in the CH₄ growth rate in 1999, so these 782
inverse results may be able to add to the discussion of the 783
causes of these anomalies. Unfortunately, the observations 784
of δ¹³CH₄ at the NOAA CMDL flask sites did not begin 785
until 1998 and the model requires 3 months of spin-up time, 786
so only 9 months of inverse results for 1998 are available. 787
Table 5 shows the mean source estimates for the last 788
9 months of 1998 and the full year of 1999. The a priori 789
sources do not vary interannually but do vary seasonally. 790
Differences between the a priori estimates listed for 1998 791
and 1999 represent the seasonal bias associated with only 792
including the last 9 months of 1998 in the average, where 793
the full year is included for 1999. The total a posteriori 794
source estimate is much larger for 1998 than 1999, due in 795
part to the seasonal bias associated with the time period 796
sampled and in part to the anomalous 1998 growth rate. In 797
the a priori sources, the April–December mean is 25 Tg 798
CH₄/year higher than the annual average. In addition, the 799
1998 growth rate increase corresponds to an increase of 800
~24 Tg CH₄/yr in the imbalance between CH₄ sources and 801
sinks compared to the earlier 1995–1997 time period 802
[*Dlugokencky et al.*, 2001]. Between 1998 and 1999, the 803
global observed growth rate decreased from 12.7 ppb to 804
2.6 ppb, indicating a corresponding decrease in the source/ 805
sink imbalance. 806

[43] Currently, there are two competing hypotheses 807
regarding the 1998 growth rate anomaly. On the basis of 808
careful analysis of the methane growth rate and a process 809
model experiment, *Dlugokencky et al.* [2001] suggested that 810
the 1998 growth rate increase was due to increased flux 811
from wetlands as a result of the temperature and precipita- 812
tion anomalies. Conversely, a recent multispecies analysis 813
study suggested that a great deal of the 1998 CH₄ growth 814

t5.1 **Table 5.** Mean A Priori and A Posteriori Flux Estimates of CH₄ Flux for April–December 1998 and All of 1999^a

t5.2	Sources	A Priori Estimates April–Dec. Mean, Tg CH ₄ /yr	A Posteriori (S2) 1998 April–Dec. Mean, Tg CH ₄ /yr	A Priori Estimates Annual Mean, Tg CH ₄ /yr	A Posteriori (S2) 1999 Annual Mean, Tg CH ₄ /yr
t5.3	Swamps	92	221 ± 44	90	208 ± 44
t5.4	Bogs	61	30 ± 13	50	12 ± 143
t5.5	Tundra	7	12 ± 4	5	0 ± 4
t5.6	Rice agriculture	71	53 ± 17	60	56 ± 17
t5.7	Ruminant animals	93	97 ± 18	93	87 ± 18
t5.8	Termites	20	48 ± 18	20	16 ± 18
t5.9	Biomass Burning	51	91 ± 18	52	88 ± 20
t5.10	Coal	38	15 ± 11	38	40 ± 11
t5.11	Natural gas	57	49 ± 18	57	62 ± 18
t5.12	Landfills	50	34 ± 14	50	31 ± 14
t5.13	Total source	540	646	515	601

t5.14 ^aNote that the a priori source estimates do not include interannual variability. The differing a priori sources from 1998 to 1999 reflect the seasonality of the sources since the two time-averaged values include different months.

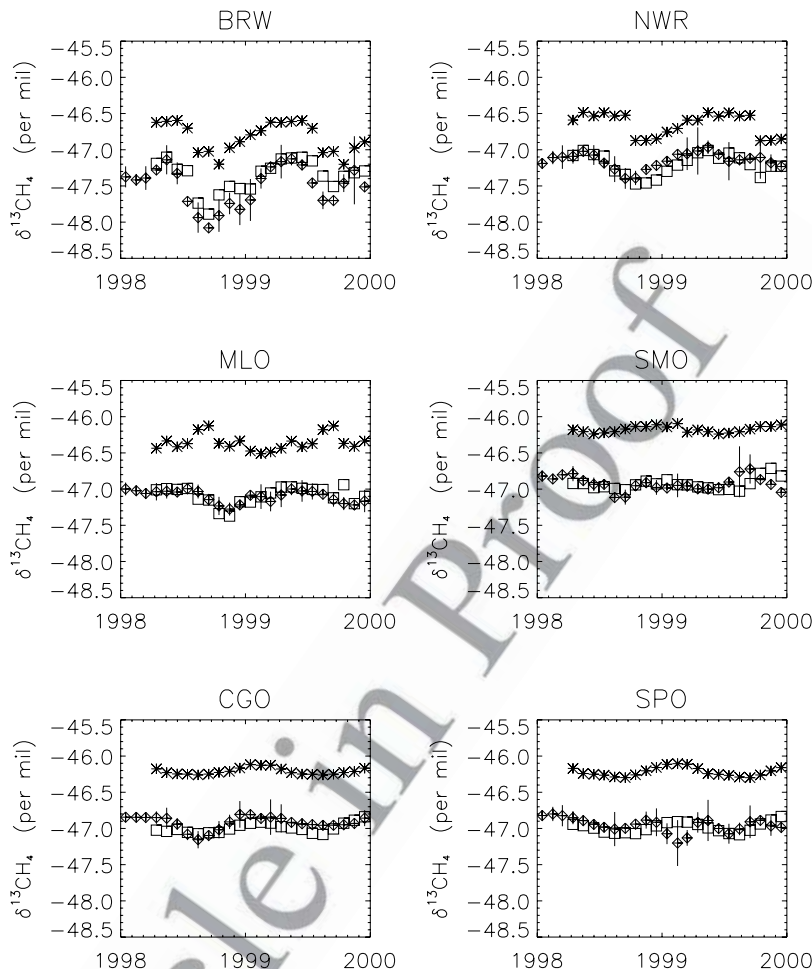


Figure 3. Comparison between the monthly mean $\delta^{13}\text{CH}_4$ measurement record at six observing stations (diamonds), model simulation based on a priori sources (asterisks), and the model simulation based on the a posteriori sources (squares). The observing stations shown are Barrow, Alaska (BRW), Niwot Ridge, Colorado (NWR), Mauna Loa, Hawaii (MLO), Tutuila, American Samoa (SMO), Cape Grim, Tasmania (CGO), and South Pole, Antarctica (SPO). Error bars on the measurements represent the standard deviation of the individual observations from the smoothed curve.

815 rate anomaly was caused by biomass burning rather than
 816 wetlands based on correlations between atmospheric
 817 observations of CO_2 and its $\delta^{13}\text{C}$, H_2 , CH_4 , and CO
 818 [Langenfelds *et al.*, 2002]. In addition, Van der Werf *et al.*
 819 [2004] also attributed much of the CH_4 anomaly to biomass
 820 burning based on satellite observations of fires combined
 821 with atmospheric models, CO observations, and observed
 822 emission ratios.

823 [44] The results of this inversion support the conclusions
 824 of Dlugokencky *et al.* [2001] that a large portion of the 1998
 825 growth rate anomaly was due to an unusually large wetland
 826 source. The large change between 1998 and 1999 occur in
 827 the wetland sources including swamps, bogs, and tundra,
 828 although the interannual variations in swamps and bogs are
 829 not far larger than the error estimates and should be
 830 interpreted with caution. In addition, the large change in the
 831 termite source, which is not consistent with process-level
 832 understanding of the interannual variability of termite
 833 emissions, is most likely due to variability in the wetland
 834 source. Since the termite source has a similar isotopic

signature to wetlands and a somewhat similar spatial 835
 footprint to swamps, it is possible that the inverse model 836
 is not effectively partitioning these two sources and part of 837
 this variability is actually due to wetlands. The magnitude 838
 of the 1998–1999 wetland variations is also in reasonable 839
 agreement with the process model simulations of 840
 Dlugokencky *et al.* regarding the anomaly. Using a global 841
 process-based model that includes soil temperature and 842
 moisture, they calculated an emission anomaly of 843
 11.6 Tg CH_4/yr for wetlands north of 30°N and 13 Tg for 844
 tropical wetlands. 845

[45] There is very little variation in the biomass burning 846
 estimate between these two model years. However, it is 847
 likely that fires played an important role in the increasing 848
 growth rate at the end of 1997 and perhaps the beginning of 849
 1998, consistent with the Langenfelds study [Langenfelds *et al.*, 2002]. There was an anomalous wildfire source from 851
 peat fires in Asia at the end of 1997, resulting in a large 852
 perturbation to the carbon cycle [Page *et al.*, 2002], but this 853
 event is not observed in these results, since 1997 and the 854

855 early months of 1998 were not included in these estimates.
 856 In addition, owing to the large uncertainty estimates
 857 associated with this work, these results do not preclude a
 858 moderate biomass burning anomaly in addition to large
 859 wetland fluxes during 1998. For example, if OH was lower
 860 in 1998 than 1999 [e.g., *Novelli et al.*, 2003], the ratio of
 861 bacterial sources to biomass burning sources might also be
 862 overestimated in 1998 and/or underestimated in 1999, since
 863 OH enriches atmospheric CH_4 in ^{13}C .

864 [46] The reason that the inversion attributed the bulk of
 865 the 1998–1999 variability to bacterial sources rather than
 866 biomass burning can be found in the observational record of
 867 $\delta^{13}\text{CH}_4$ (Figure 3). If this anomaly were primarily due to
 868 biomass burning, one would expect to see a peak in the
 869 observations of $\delta^{13}\text{CH}_4$ to reflect the relatively heavy
 870 isotopic signature of this source. Instead, more negative
 871 $\delta^{13}\text{CH}_4$ isotopic signatures were observed at Barrow,
 872 Alaska, Mauna Loa, Hawaii, and Cape Grim, Tasmania,
 873 in late 1998. Therefore the observations used to constrain
 874 this model call for greater fluxes from sources with lighter
 875 isotopic signatures than the background atmosphere in
 876 1998, resulting in high estimates of bacterial sources.

877 [47] Two hypothetical model scenarios were used to
 878 examine how well the observations of CH_4 and $\delta^{13}\text{CH}_4$
 879 might be able to constrain a biomass burning anomaly. The
 880 1998 anomaly reflects to a source/sink imbalance of 24 Tg
 881 CH_4 [*Dlugokencky et al.*, 2001]. In one biomass burning
 882 scenario, the entire anomaly is attributed to biomass burning
 883 by increasing the a posteriori biomass burning by 24 Tg
 884 CH_4 in 1998 and reducing the a posteriori wetland source
 885 by an equal amount. The second scenario reflects the effect
 886 of attributing one third of the total anomaly to biomass
 887 burning and the remainder to wetlands, following the results
 888 of an earlier analysis of $\delta^{13}\text{CH}_4$ [*Miller et al.*, 2002].

889 [48] These scenarios were constructed by combining the a
 890 posteriori CH_4 and $\delta^{13}\text{CH}_4$ mixing ratios with CH_4 and
 891 $^{13}\text{CH}_4$ mixing ratios calculated by forward model simula-
 892 tions of a 1998 biomass burning perturbation, $[\text{CH}_4]_{\text{BB pert}}$
 893 and a 1998 wetland perturbation, $[\text{CH}_4]_{\text{Wetl. pert}}$ in which
 894 both perturbations include OH loss. The resulting concen-
 895 trations of CH_4 and $^{13}\text{CH}_4$ can be written as

$$[\text{CH}_4]_{\text{Scenario}} = [\text{CH}_4]_{\text{a posteriori}} + [\text{CH}_4]_{\text{BB pert}} - [\text{CH}_4]_{\text{Wetl. pert}} \quad (9)$$

$$[^{13}\text{CH}_4]_{\text{Scenario}} = [^{13}\text{CH}_4]_{\text{a posteriori}} + [^{13}\text{CH}_4]_{\text{BB pert}} - [^{13}\text{CH}_4]_{\text{Wetl. pert}} \quad (10)$$

899 Then the $\delta^{13}\text{CH}_4$ for the new scenario is calculated
 900 following equation (4).

901 [49] A 24 Tg CH_4 increase in the biomass burning source
 902 and a corresponding decrease in the wetland source during
 903 1998 would result in a significant change in the $^{13}\text{C}/^{12}\text{C}$
 904 isotopic ratio of atmospheric CH_4 at most observing sta-
 905 tions, but very little change in the CH_4 mixing ratio, as
 906 shown for MLO in Figure 4. At the end of 1998, the
 907 atmospheric $\delta^{13}\text{CH}_4$ for this scenario is between 0.16 and
 908 0.23 per mil higher than the a posteriori isotopic signature

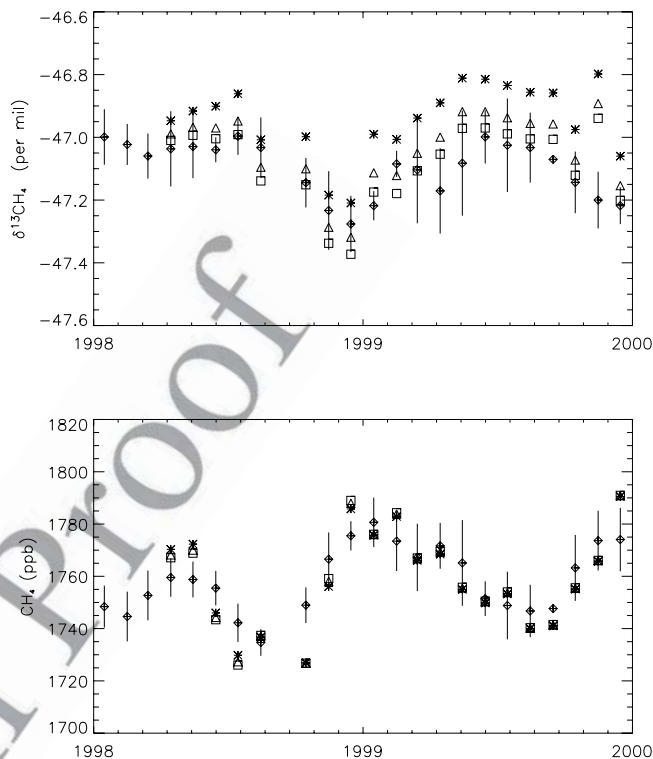


Figure 4. Comparison between the monthly mean (top) $\delta^{13}\text{CH}_4$ and (bottom) CH_4 measurement record at MLO (diamonds), model simulation based on a posteriori sources (squares), and two scenarios which explore the effect of a 1998 biomass burning anomaly on atmospheric $\delta^{13}\text{CH}_4$ and CH_4 . In once scenario, the entire 1998 anomaly was attributed to biomass burning by reducing the a posteriori wetland source by 24 Tg CH_4 during 1998 and increasing the a posteriori biomass burning source by the same amount (asterisks). Then, the possibility of an anomaly due to a combination of increased biomass burning and wetland emissions was examined by reducing the a posteriori wetland source by 8 Tg CH_4 during 1998 and increasing the a posteriori biomass burning source by the same amount (triangles). Error bars on the measurements represent the standard deviation of the individual observations from the smoothed curve.

909 for the three NH stations and between 0.02 and 0.16 per mil
 910 higher for the SH stations. At MLO, NWR, and SMO, the
 911 difference between the a posteriori $\delta^{13}\text{CH}_4$ and the new
 912 scenario during 1999 is close to the magnitude of the
 913 seasonal cycle. Conversely, the second scenario, in which
 914 only one third of the total anomaly is shifted to biomass
 915 burning, is still reasonably consistent with the observations
 916 (Figure 4). This simulation combined with the error estimate
 917 associated with the a posteriori biomass burning flux
 918 indicates that the observations used to constrain the inverse
 919 model are consistent with moderate contribution of biomass
 920 burning to the 1998 growth rate anomaly.

921 [50] The simulated CH_4 concentrations are very similar
 922 for the a posteriori case and both biomass burning
 923 scenarios (Figure 4, bottom), as would be expected based

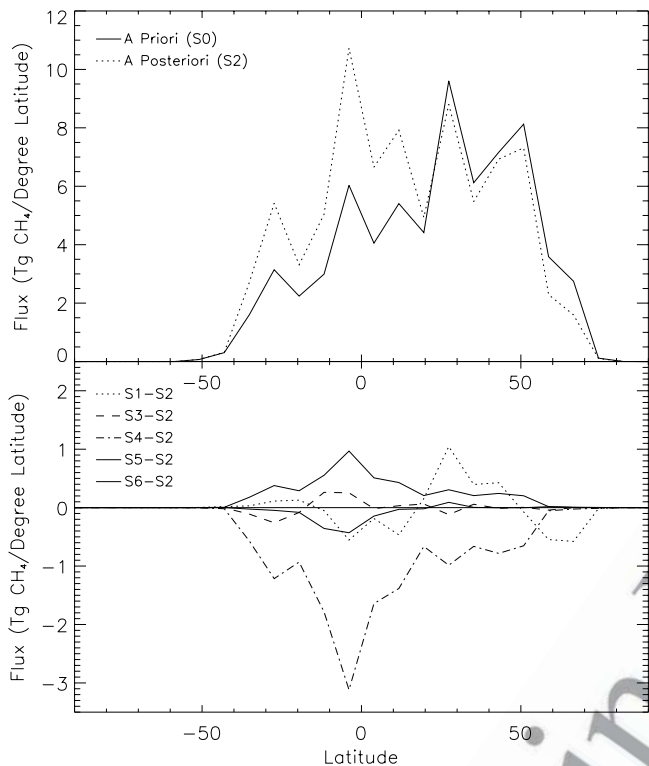


Figure 5. (top) Latitudinal gradient of the a priori and a posteriori CH_4 flux estimates and (bottom) the difference between the a posteriori flux estimates for the inverse scenarios described in Table 2 and the standard inverse scenario, S2.

924 on the work of *Fung et al.* [1991]. This suggests that a
 925 24 Tg CH_4 perturbation from biomass burning perturbation
 926 would be very difficult to distinguish from a similar
 927 perturbation due to wetlands based on the observations of
 928 CH_4 alone. Observations of $\delta^{13}\text{CH}_4$ provide far more insight
 929 into the source processes controlling changes of this
 930 magnitude.

931 [51] The changes in landfills, natural gas, coal, ruminant
 932 animals, and termites between 1998 and 1999 probably
 933 primarily reflect model noise as a function of time. These
 934 sources do not have significant seasonal variations, so
 935 seasonal bias issues do not apply to these sources. In
 936 addition, large variability on annual timescales is unlikely
 937 for these sources. For example, while the ruminant animal
 938 source is likely to change significantly with changes in feed
 939 quality, age demographics of the animals, and other factors,
 940 these kinds of changes on a global scale are not likely to
 941 occur over a 2-year time period.

942 5. Sensitivity of the Results

943 [52] In order to determine whether the major conclusions
 944 of this study are robust with respect to several sources of
 945 uncertainty, inverse estimates have been calculated after
 946 varying a number of model features in scenarios 3–7,
 947 summarized in Table 2. The results of these sensitivity tests

are compared to the base scenario, S2, in Table 3 and 948
 Figure 5 (bottom). 949

[53] Overall, the major conclusions of the inverse study 950
 are reasonably robust with respect to changes in these model 951
 parameters. Changing the KIE of CH_4 oxidation by OH (S3) 952
 had very little effect on the inverse results. The differences 953
 between S2 and S3 never exceeded the error bars of the 954
 inverse estimates. The largest percent difference between 955
 these two model runs is the biomass burning source, which 956
 changes by 14%. Since the smaller OH KIE results in less 957
 enrichment in atmospheric ^{13}C from the chemical sink, the 958
 inverse model calls for more biomass burning, since 959
 the biomass burning source is very enriched compared to 960
 the atmosphere. Since bacterial sources deplete the atmo- 961
 sphere in ^{13}C , most of the bacterial sources are reduced 962
 slightly between S2 and S3. Because OH concentrations are 963
 much higher low latitudes, the largest perturbations to the 964
 emissions under this scenario occur in the tropics (Figure 5), 965
 and emissions from bogs and tundra, which occur predom- 966
 inantly at high latitudes, increased slightly in S3 rather than 967
 decreasing. 968

[54] S4 and S5 test the upper and lower limits of the OH 969
 fields, as determined by *Spivakovsky et al.* [2000]. Recall 970
 that the lower limit test (S4) is expected to diverge more 971
 from S2 than the upper limit test (S5) because the base 972
 scenario is closer to the high end of the range. In both the 973
 upper and lower limit, the global total CH_4 source strength 974
 changes significantly, since the total magnitude of the sink 975
 is changed relative to the base scenario while the amount of 976
 CH_4 in the atmosphere remains unchanged, with the greatest 977
 changes occurring for sources with large emissions in the 978
 tropics (Figure 6). The upper limit OH estimate results in 979
 very little divergence from the base scenario for most 980
 sources, but does result in increased emissions from 981
 biomass burning and swamps. Applying the lower limit 982
 OH sink to the inversion (S5) results in large changes in the 983
 inverse flux estimates in the tropics (Figure 5). The largest 984
 decrease occurs in swamps; however, even with this 985
 decrease, the inverse model still calls for a large increase 986
 in this source compared to the a priori source estimates. A 987
 corresponding large change occurs in biomass burning, 988
 showing that the relatively high estimates of biomass 989
 burning found in this study are not robust in the lower limit 990
 of OH production. Changes to the other source strength 991
 estimates are small relative to the error estimates. The strong 992
 perturbations to the CH_4 emissions from swamps and 993
 biomass burning relative to the other source processes are 994
 probably due to the fact that destruction by OH is the 995
 greatest in the tropics, and these two source processes occur 996
 largely in the tropics, while their isotopic signatures have 997
 opposite effects on the atmosphere. Therefore, decreasing 998
 both sources corrects for the OH perturbation while 999
 matching the $\delta^{13}\text{CH}_4$ observations. Finally, the changes in 1000
 the source estimates from a large change in initial conditions 1001
 are small. 1002

[55] Overall, the most of the conclusions from the 1003
 previous section are robust with respect to these changes 1004
 in the model parameters tested here, but the a posteriori 1005
 flux estimates are sensitive to large changes in OH. Since 1006
 the OH sink is the largest single component of the CH_4 1007

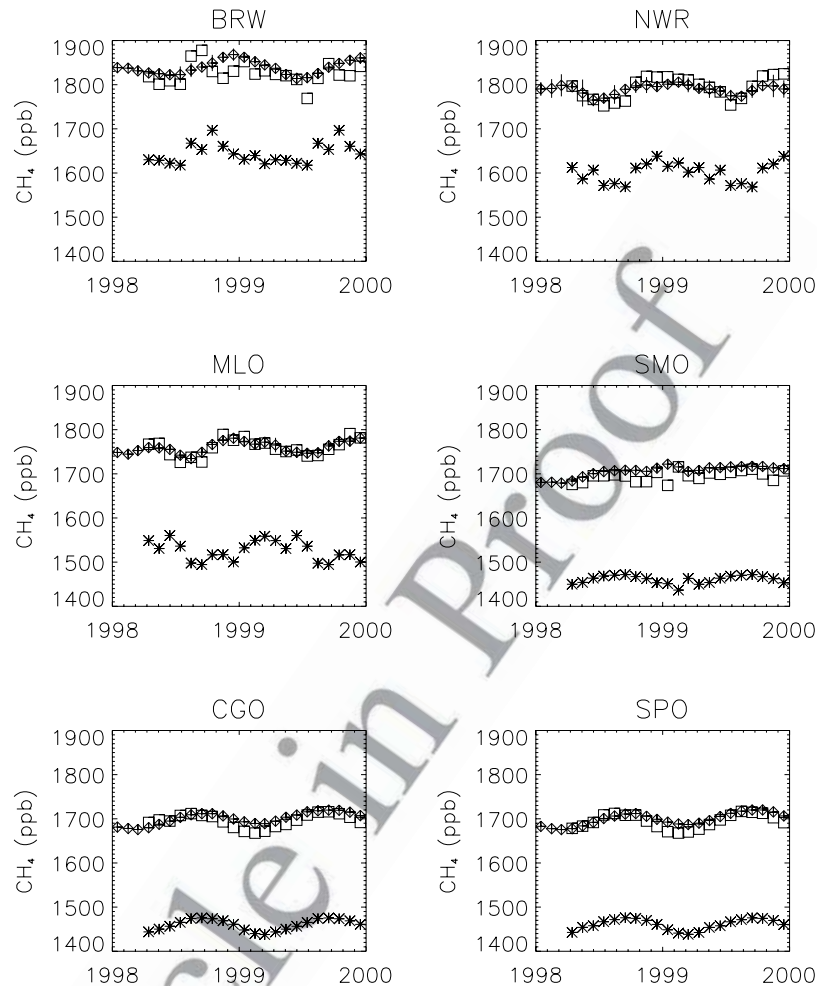


Figure 6. Comparison between the monthly mean CH₄ measurement record at six observing stations (diamonds), model simulation based on a priori sources (asterisks), and the model simulation based on the a posteriori sources (squares). Error bars on the measurements represent the standard deviation of the individual observations from the smoothed curve.

1008 budget, and changing the fractionation of this sink by
 1009 1.5% did not significantly change the inverse estimates,
 1010 the results shown here are not expected to be strongly
 1011 sensitive to small changes in the isotopic signatures of
 1012 the sources.

1013 6. A Posteriori Atmospheric CH₄ Mixing Ratios 1014 and $\delta^{13}\text{CH}_4$

1015 [56] One advantage of inverse source estimates is that they
 1016 are constrained by the observations of the trace gas in the
 1017 atmosphere. Therefore forward simulations using the inverse
 1018 estimates should reproduce the broad features of the obser-
 1019 vations such as the interhemispheric gradient and seasonal
 1020 cycle at observing stations well. Figures 1, 3, and 6 compare
 1021 the modeled CH₄ and $\delta^{13}\text{CH}_4$ based on the a posteriori
 1022 sources to those based on a priori sources to the observa-
 1023 tional record at the stations used to constrain the inversion.
 1024 Figure 7 compares the a posteriori $\delta^{13}\text{CH}_4$ with the obser-

1025 vational record from two NIWA stations that were not used
 1026 to constrain the inversion, Baring Head, New Zealand, and
 1027 Scott Base, Antarctica [Lowe *et al.*, 1994], as an
 1028 independent validation of the inverse model.

1029 [57] The inverse sources match the observed latitudinal
 1030 gradients of both CH₄ and $\delta^{13}\text{CH}_4$ well, especially in
 1031 comparison to the a priori estimates (Figure 1). There are
 1032 two stations that have very high observed values compared
 1033 to other stations at similar latitudes, which are not well
 1034 matched by the inverse estimates. These stations, located on
 1035 the Black Sea in Romania (BSC) and Cape Rama, India
 1036 (CRI), are likely to be influenced by the large continental
 1037 sources nearby. The observations at stations sampling
 1038 continental air were given a higher uncertainty than obser-
 1039 vations at stations sampling marine air, implying that
 1040 stations sampling continental air do not constrain the
 1041 inverse model as strongly as those sampling marine air.
 1042 The reason for weighting these stations more weakly in the
 1043 inversion is that these data are influenced more strongly by

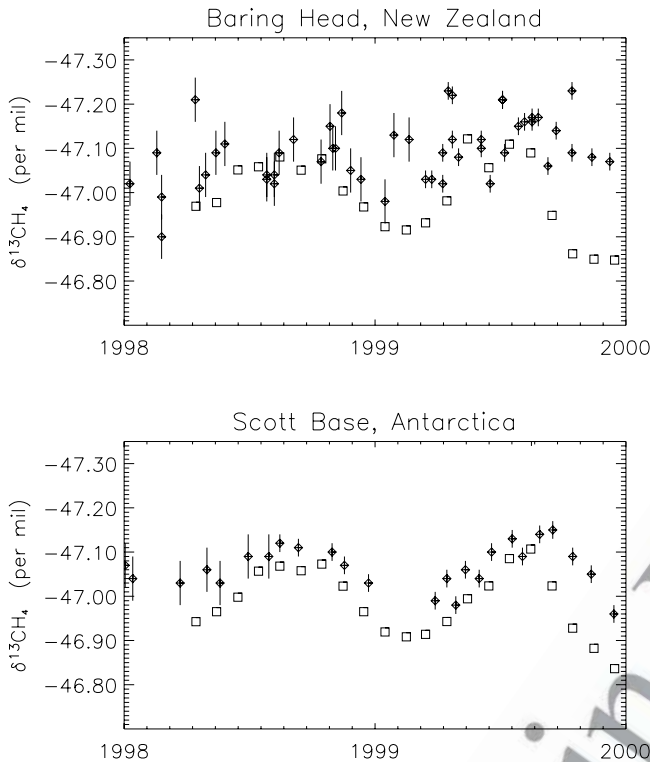


Figure 7. Comparison between the $\delta^{13}\text{CH}_4$ measurement (diamonds) and the model simulation based on the a posteriori sources (squares) for two NIWA observing stations: Baring Head, New Zealand, and Scott Base, Antarctica [Lowe *et al.*, 1994].

1044 local sources, small-scale transport effects, and other factors
 1045 that cannot be represented effectively in a coarse resolution
 1046 model. The a posteriori CH_4 does not reproduce observa-
 1047 tions at BSC and CRI well because they are weighted more
 1048 weakly, and a linear combination of large source regions
 1049 that matched these stations well would not be consistent
 1050 with the other station observations.

1051 [58] The monthly mean observations and model results
 1052 are compared at the six NOAA CMDL stations where
 1053 both observations of CH_4 and observations of $\delta^{13}\text{CH}_4$ are
 1054 made (Figures 3 and 5). Overall, the a posteriori esti-
 1055 mates match the broad features of the CH_4 and $\delta^{13}\text{CH}_4$
 1056 observations at these stations, as well as at the two NIWA
 1057 stations that were not used to constrain the inverse model
 1058 (Figure 7).

1059 [59] In all cases, the a posteriori CH_4 source estimates
 1060 result in a far better match to the station observations
 1061 than the a priori estimates. The a posteriori correct the a
 1062 priori underestimate of the overall magnitude of the CH_4
 1063 mixing ratio as well as the poor match to the a priori
 1064 seasonal cycle at BRW and MLO. There is a small a
 1065 posteriori overestimate of CH_4 at NWR at the end of
 1066 1998. The use of large spatial regions and coarse model
 1067 resolution can sometimes preclude an exact match to the
 1068 station observations based on linear combinations of these
 1069 large regions, and this may have caused this discrepancy.

The a posteriori calculation of atmospheric $\delta^{13}\text{CH}_4$ 1070
 generally matches the mean observed $\delta^{13}\text{CH}_4$ and the 1071
 observed $\delta^{13}\text{CH}_4$ seasonal cycle, as accurately as the CH_4 1072
 match. 1073

7. Conclusions 1074

[60] We have presented source estimates that are 1075
 optimally consistent with the observations of atmospheric 1076
 CH_4 and $\delta^{13}\text{CH}_4$ and process-level understanding of the 1077
 sources and sinks. There are many important departures 1078
 from previous source estimates. The CH_4 source from 1079
 wetlands was unusually large, which agrees with two recent 1080
 process-level models suggesting a greater importance of 1081
 wetland ecosystems than previously thought [Kaplan, 2001; 1082
 Walter, 1998]. The interannual distribution of this source 1083
 supports the hypothesis of Dlugokencky *et al.* [2001] that the 1084
 1998 growth rate anomaly was primarily caused by increased 1085
 wetland emissions. Biomass burning source estimates were 1086
 very high, in agreement with an earlier study incorporating 1087
 observations of $\delta^{13}\text{CH}_4$ [Miller *et al.*, 2002]. 1088

[61] These results show that through inverse modeling, 1089
 the atmospheric CH_4 and $\delta^{13}\text{CH}_4$ observations have the 1090
 capacity to add unique insight into the CH_4 problem, but 1091
 significant limitations to this technique persist. While the 1092
 inverse results are robust with respect to changes in the 1093
 initial conditions and the OH KIE, the CH_4 flux estimates 1094
 for biomass burning and swamps are sensitive to changes in 1095
 the assumed OH sink. The inverse estimates may also be 1096
 sensitive to inaccuracies in model transport and the assumed 1097
 isotopic signature of the sources. The aggregation of the 1098
 sources into spatially diffuse source process regions intro- 1099
 duces both a source of error and a limitation to the 1100
 understanding that may be provided by the inverse esti- 1101
 mates. The error is introduced by the assumption that the 1102
 CH_4 flux can be represented by a linear combination of a 1103
 small number of source regions and that the assumed spatial 1104
 pattern of the CH_4 emissions within these regions are 1105
 perfect. In reality, the spatial distributions of many of the 1106
 source processes are likely to vary with regional tempera- 1107
 ture anomalies and other physical processes. In addition, 1108
 grouping the sources in this way removes the potential to 1109
 use the CH_4 and $\delta^{13}\text{CH}_4$ observations to diagnose changes 1110
 in CH_4 flux on regional scales. 1111

Appendix A: Derivation of Equation (5) 1112

[62] First, equation (3) is divided by an arbitrary reference 1113
 ratio of $^{13}\text{C}/^{12}\text{C}$.

$$\frac{R_j^{\text{obs}}}{R_{\text{reference}}} y_j^{\text{obs}} - \frac{R_j}{R_{\text{reference}}} y_j = \sum_{i=1, \text{nsrc}} \mathbf{H}_{i,j} \frac{R_i}{R_{\text{reference}}} x_i. \quad (\text{A1})$$

Then, equation (2) is subtracted from equation (A1). 1115

$$\begin{aligned} & \left(\frac{R_j^{\text{obs}}}{R_{\text{reference}}} y_j^{\text{obs}} - y_j^{\text{obs}} \right) - \left(\frac{R_j}{R_{\text{reference}}} y_j - y_j \right) \\ &= \sum_{i=1, \text{nsrc}} \mathbf{H}_{i,j} \frac{R_i}{R_{\text{reference}}} x_i - \sum_{i=1, \text{nsrc}} \mathbf{H}_{i,j} x_i. \end{aligned} \quad (\text{A2})$$

1117 Equation (A2) is multiplied by 1000 and rearranged.

$$\begin{aligned} & \left(\frac{R_j^{\text{obs}}}{R_{\text{reference}}} - 1 \right) \times 1000 \times y_j^{\text{obs}} - \left(\frac{R_j}{R_{\text{reference}}} - 1 \right) \times 1000 \times y_j \\ &= \sum_{i=1, \text{nsrc}} \mathbf{H}_{ij} x_i \times \left(\frac{R_i}{R_{\text{reference}}} - 1 \right) \times 1000. \end{aligned} \quad (\text{A3})$$

1120 Finally, equation (4), the definition of δ units, can be
1121 substituted into equation (A3) to reach equation (5).

$$\delta_j^{\text{obs}} y_j^{\text{obs}} - \delta_j y_j = \sum_{i=1, \text{nsrc}} \mathbf{H}_{ij} x_i \delta_i.$$

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