

## ORIGINAL ARTICLE

# Chain dimension of polyampholytes in solution and immobilized brush states

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The dimensions and intermolecular interactions of surface-grafted and unbound, free polyampholytes, poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate] (PMAPS) and poly(2-methacryloyloxyethyl phosphorylcholine) (PMPC), were estimated in an aqueous NaCl solution over a wide range of salt concentrations ( $C_s$ ). The free PMAPS and PMPC fractionated by a recycling preparative size-exclusion chromatography system were characterized in aqueous NaCl solutions for  $C_s$  over a range from 0 to 5.0 M by static light scattering and dynamic light scattering (DLS) measurements. The hydrodynamic radius ( $R_H$ ) and the concentration coefficient of the diffusion coefficient ( $k_D$ ) for PMPC were independent of  $C_s$ , whereas those for PMAPS were strongly dependent on  $C_s$ . Monodisperse silica nanoparticles immobilized with PMAPS (SiNP-PMAPS) and PMPC (SiNP-PMPC) by surface-initiated atom transfer radical polymerization were characterized in aqueous NaCl solutions for  $C_s$  over a range from 0 to 5.0 M by DLS and synchrotron radiation small-angle X-ray scattering (SAXS) measurements. The SAXS profiles from SiNP-PMAPS and SiNP-PMPC solutions were well described by the core-shell model, taking into account interacting self-avoiding chains and assuming a Schulz-distributed core with two fitting parameters.

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## INTRODUCTION

Zwitterionic polyelectrolytes that possess both positive and negative charges can be found in certain natural substances with a high molecular weight, such as poly(amino acid)s, proteins, DNA and cell membrane surfaces. These substances form self-assemblies and nanostructures in aqueous media.<sup>1</sup> Various types of polyelectrolyte brushes have been prepared to modify solid surfaces to achieve biocompatibility, switchable wettability and low friction under aqueous conditions.

For example, poly(3-(*N*-2-methacryloyl-oxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate) (PMAPS) and poly(2-methacryloyloxyethyl phosphorylcholine) (PMPC) are insoluble and soluble in deionized water at room temperature, respectively. PMAPS is soluble in a solution at a sufficiently higher temperature than the upper critical solubility temperature,<sup>2</sup> as well as in an aqueous salt solution because of the strong attractive intermolecular and intramolecular electrostatic interaction between ammonium cations and sulfonate anions. Huck and co-workers<sup>3</sup> prepared a PMAPS brush on gold surfaces by surface-initiated atom transfer radical polymerization, in which they showed that surface wettability changed from hydrophilic to hydrophobic because of the strong interchain and intrachain associations at the upper critical solubility temperature accompanying

a change in the thickness of the brushes in an aqueous medium. In addition, excellent lubrication in an aqueous medium was observed on the surface of a PMPC brush.<sup>4,5</sup> The PMPC brush has attracted a great deal of interest because of its excellent biocompatibility<sup>6,7</sup> and characteristics such as its antifouling behavior.<sup>8</sup> To understand the mechanism responsible for the excellent biocompatibility and lubrication behavior, it is very important to examine the swollen structure, the conformation of polyelectrolyte brushes in an aqueous solution and the dependence on ionic strength in comparison with the solution properties of unbound, free polyelectrolytes.

In general, high-density polymer brush chains immersed in a good solvent are extended in a perpendicular direction from a substrate because of the osmotic pressure generated by the excluded volume effect.<sup>9</sup> Tsujii *et al.* carried out force curve measurements on a swollen poly(methyl methacrylate) brush on a silicon wafer. They used a silica probe for atomic force microscopy and determined the equilibrium thickness of the brush. The thickness was three times as large as the scaled dry thickness.<sup>10</sup> However, it is very difficult to precisely determine the swollen thickness of polyelectrolyte brushes in an aqueous solution. In the case of atomic force microscopy, strong electrostatic attractive or repulsive interactions occur between the polyelectrolyte surface and the probe in an aqueous solution with low ionic strength.

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Previously, neutron reflectometry at the polyelectrolyte brushes/deuterium oxide interface was used to characterize the swollen structure of PMAPS<sup>11,12</sup> and PMPC<sup>13</sup> brushes. However, the neutron scattering length density profile provided only an ambiguous estimate of the internal structure of the brushes in an aqueous solution with a large molecular weight distribution (MWD) because the average height of the brush increases with polydispersity, whereas the average stretching in the brush decreases.<sup>14</sup>

In most studies, polyelectrolyte brushes are prepared either by adsorption of block copolymers consisting of a hydrophobic and a polyelectrolyte block on latex particles<sup>15</sup> or by surface-initiated polymerization of ionic monomers from hydrophobic polymer latex particles. Polzer *et al.*<sup>16</sup> prepared a PMAPS brush shell on a colloidal particle consisting of a polystyrene gel core, the structure of which was confirmed by cryogenic transmission electron microscopy and dynamic light scattering (DLS) in aqueous NaCl and KCl solutions. However, the interfacial width of the core and shell was unclear, especially in an aqueous salt solution because of the possibility that the polystyrene core might be strained by swollen PMAPS brush chains due to high osmotic pressure. Matsuda *et al.*<sup>17,18</sup> prepared surface-grafted PMPC on silica nanoparticles by surface-initiated atom transfer radical polymerization to measure DLS in aqueous NaCl solutions. Interestingly, they found that the hydrodynamic radius ( $R_H$ ) and the second virial coefficient ( $A_2$ ) of PMPC were independent of the concentration of NaCl (0–0.5 M), whereas both the  $R_H$  and the  $A_2$  of typical polyampholytes depended strongly on the ionic strength. Unfortunately, there is still a lack of studies at a salt concentration much higher than 1.0 M; such studies are of utmost importance to the full understanding of electrostatic excluded-volume and chain stiffness effects. To the best of our knowledge, previous experimental work on the polyelectrolyte brush state is limited to chain dimension in an aqueous solution. In this paper, we will focus on the dependence of the ionic strength of surface-grafted zwitterionic polyelectrolyte chains attached to the solid on the chain conformation.

In the case of free PMAPS, the dependence of  $R_H$  and intrinsic viscosity of poly(sulfobetaine)s on ionic strength have been well studied by DLS and viscometry measurements;<sup>2,19–23</sup> the unique phase behaviors have been known to depend on salt concentration,<sup>19,23,24</sup> additive salt ion species,<sup>25</sup> temperature,<sup>2</sup> molecular weight and solvent polarity.<sup>20,26</sup> The  $z$ -average, mean-square radius of gyration  $\langle S^2 \rangle_z$  and  $A_2$  of PMAPS in an aqueous NaCl solution at 1.0 M and in 2,2,2-trifluoroethanol (TFE) were estimated by Huglin and Radwan,<sup>22,27</sup> who also determined the intrinsic viscosity of PMAPS in a  $\theta$ -solvent. With increasing salt concentration in an aqueous solution above the  $\theta$ -concentration, greater chain dimensions of PMAPS were observed in an aqueous solution because the attractive electrostatic interaction among sulfobetaine groups was neutralized by the screening effect of salt ions.<sup>28</sup> Kato *et al.* estimated the  $\langle S^2 \rangle_z$  and  $\theta$ -concentration of PMAPS in an aqueous NaCl solution at 0.060 M with static light scattering (SLS) for polymers with a weight-average molecular weight ( $M_w$ ) in the range of  $5.4 \times 10^4$  to  $5.0 \times 10^6$ . However, the MWD of polymers was not clarified in their report. Polymers with a broad MWD are unfavorable for the estimation of chain dimensions.

In this study, we prepared a well-defined polyelectrolyte brush by surface-initiated atom transfer radical polymerization of MAPS and MPC monomers from SiNPs with a diameter of  $\sim 100$  nm. The chain dimensions and intermolecular interactions of surface-grafted and unbound PMAPS and PMPC were estimated in aqueous NaCl solutions at various salt concentrations ( $C_s$ ) from 0 to 5.0 M by SLS,

DLS and synchrotron small-angle X-ray scattering (SAXS). In particular, the effects of salt concentration on the chain conformation of surface-grafted PMAPS and PMPC chains on SiNPs will be discussed.

## EXPERIMENTAL PROCEDURES

### Materials

Copper (I) bromide (CuBr, Wako Pure Chemicals, Osaka, Japan, 99.9%) was purified by successive washing with acetic acid and ethanol and then dried under vacuum. 2-(Dimethylamino)ethyl methacrylate (Wako Pure Chemicals, 98%), 2,2'-dipyridyl (bpy, Wako Pure Chemicals, 99.5%), 1-ethyl-3-methylimidazolium chloride (EMImCl, Merck, KGaA, Darmstadt, Germany, 98%) and 1,3-propane sultone (Aldrich, St Louis, MO, USA, 99%) were used as received. TFE (Tokyo Chemical, 99.0%) was carefully degassed by a freeze-pump-thaw process before dilution of CuBr and bpy. MAPS,<sup>29</sup> MPC<sup>6</sup> and tris(2-(dimethylamino)ethyl) amine (Me<sub>6</sub>TREN)<sup>30</sup> were synthesized using previously reported procedures. Deionized water for sample preparation of light scattering and SAXS samples was purified with arium 611UV (Sartorius Stedim Biotech GmbH, Goettingen, Germany, resistivity=18.2 M $\Omega$  cm). Silica nanoparticles (SiNPs) with a radius of  $\sim 50$  nm dispersed in water (40 wt%) were kindly supplied by Nissan Chemical Industries, Tokyo, Japan. The free PMAPS and PMPC were prepared by free radical homopolymerization of corresponding monomer using 2,2'-azobis(isobutyronitrile) as an initiator in TFE at 60 °C for 24 h. Free polymer samples with a narrow MWD were fractionated by a recycling preparative size-exclusion chromatography system (Japan Analytical Industry, Tokyo, Japan, LC-9104) equipped with an RI detector (JAI RI-7s, Japan) using two columns (JAIGEL GS620-50L, GS320-50L) in an aqueous NaCl solution at  $C_s=0.2$  M as an eluent at a flow rate of 20 ml min<sup>-1</sup> at room temperature. The  $M_w$  and MWD of the fractionated samples were determined by size-exclusion chromatography measurement using an aqueous NaCl solution at  $C_s=0.2$  M as an eluent calibrated with a series of corresponding polymers as a standard.<sup>12</sup> The values of  $M_w$  and  $M_w/M_n$  of free PMAPS were determined to be  $2.47 \times 10^5$  g mol<sup>-1</sup> and 1.18, respectively. The values of  $M_w$  and  $M_w/M_n$  of free PMPC were determined to be  $2.34 \times 10^5$  g mol<sup>-1</sup> and 1.12, respectively.

### Immobilization of the surface initiator

The surface initiator (2-bromo-2-methyl)propionyloxyhexyltriethoxysilane (BHE)<sup>31</sup> was synthesized by hydrosilylation of 5-hexenyl 2-bromoisobutylate treated with triethoxysilane in the presence of the Karstedt catalyst.<sup>32</sup> Immobilization of BHE on a SiNP (SiNP-BHE) was accomplished using a previously reported procedure.<sup>17,31</sup> A commercially supplied SiNP suspension (10 ml) was collected in a 500-ml round-bottomed flask and was diluted with 100 ml of ethanol. A mixture of ammonia solution (28% NH<sub>3</sub> aqueous solution, 10 ml) and ethanol (180 ml) was added dropwise to the SiNP suspension over 3 h with stirring, and the system was stirred for 2 h at 40 °C. BHE (2 g, 4.8 mmol) diluted with ethanol (10 ml) was added dropwise to the suspension over 15 min, and the reaction mixture was continuously stirred for another 15 h at 40 °C. SiNP-BHE was then cleaned by consecutive centrifugation and redispersion in ethanol. Finally, the SiNP-BHE suspension in ethanol was solvent exchanged to TFE to obtain a 10 wt% suspension in TFE.

### Surface-initiated atom transfer radical polymerization of MAPS and MPC from SiNP

Thereafter, MAPS (0.327 mmol), EMImCl (0.65 g), TFE (3.4 g) and 10 wt% SiNP suspension in TFE (2.5 g) were loaded into a well-dried glass tube with a stopcock, degassed three times by the freeze-thaw process and flushed with argon.<sup>33</sup> A copper catalyst solution containing CuBr (0.0075 mmol) and bpy (0.015 mmol) diluted with degassed TFE was placed into another glass tube and injected into the mixture suspension. The resulting reaction mixture was again degassed by repeated freeze-thaw cycles to remove the oxygen and then subsequently sealed off under reduced pressure. The polymerization reaction was carried out in a stirring oil bath at 60 °C for 13 h. The reaction was stopped by opening the glass vessel to air at 0 °C. The reaction mixture was poured into methanol, filtered and dried. SiNP-PMAPS was purified by consecutive redis-

**Table 1** Characteristics of SiNP-PMAPS and SiNP-PMPC

Sample	$M_n \times 10^{-4a}$ ( $\text{g mol}^{-1}$ )	$M_w/M_n^a$	$R_c^b$ (nm)	$w^c$ (wt%)	Graft density (chains per $\text{nm}^2$ )	$N^d$
PMAPS	2.38	1.27	55	14.8	0.129	4910
PMPC	2.09	1.72	56	7.1	0.066	2590

Abbreviations: PMAPS, poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate]; PMPC, poly(2-methacryloyloxyethyl phosphorylcholine); SAXS, small-angle X-ray scattering; SEC, size-exclusion chromatography; SiNP, silica nanoparticle; TGA, thermogravimetric analysis.

<sup>a</sup>Determined by SEC measurement using an aqueous NaCl solution at 0.2 M as an eluent calibrated with a series of corresponding polymers as a standard.

<sup>b</sup>Determined by SAXS.

<sup>c</sup>The weight loss of polymer is measured by TGA.

<sup>d</sup>The average number of graft polymer chains per SiNP.

persion in TFE and reprecipitation in methanol to remove the unreacted MAPS and SiNP-BHE and was finally dried under reduced pressure at 60 °C for 12 h.

Thereafter, MPC (1.55 mmol), EMImCl (0.54 g) TFE (20 g) and a 10 wt% SiNP suspension in TFE (0.5 g) were loaded into a well-dried glass tube with a stopcock, degassed three times by the freeze-thaw process and flushed with argon. A copper catalyst solution containing CuBr (0.016 mmol) and bpy (0.032 mmol) diluted with degassed TFE was placed in another glass tube and injected into the mixture suspension. The resulting reaction mixture was again degassed by repeated freeze-thaw cycles to remove the oxygen and then subsequently sealed off under reduced pressure. The polymerization reaction was carried out in a stirring oil bath at 60 °C for 24 h. The reaction was stopped by opening the glass vessel to air at 0 °C. The reaction mixture was cleaned by three cycles of centrifugation and redispersion in methanol to remove the unreacted MPC. Finally, the SiNP-PMPC suspension in methanol was poured into tetrahydrofuran, filtered and dried under reduced pressure at 60 °C for 12 h.

To determine the  $M_n$  and  $M_w/M_n$  of the surface-grafted polymer on SiNPs, PMAPS and PMPC chains were cleaved from the surface as follows. SiNP-PMAPS and SiNP-PMPC were immersed in a solution mixture of 10 wt% hydrogen fluoride aqueous solution (5 ml) and an aqueous NaCl solution at  $C_s=0.2\text{ M}$  (10 ml) for 3 days in a plastic vessel and slowly neutralized using a sodium hydrogen carbonate aqueous solution. The resulting solutions were collected in a dialysis membrane tube (Spectra/Por 3, Standard regulated cellulose membrane,  $M_w=3.50 \times 10^3 \text{ g mol}^{-1}$ ) and dialyzed in water to remove inorganic salt ions for 3 days and were freeze dried from aqueous solution. The values of  $M_n$  and  $M_w/M_n$  of the obtained surface-grafted PMAPS and PMPC on an SiNP were determined by size-exclusion chromatography measurement using an aqueous NaCl solution at  $C_s=0.2\text{ M}$  as an eluent calibrated with a series of corresponding polymers as a standard. The characteristics of SiNP-PMAPS and SiNP-PMPC used in this study are listed in Table 1. The values of weight loss measured by thermogravimetric analysis (Perkin-Elmer Pyris TGA) of SiNP-PMAPS and SiNP-PMPC were determined to be 14.8 and 7.1 wt%, respectively.

## Measurements

Both SLS and DLS experiments of the free polymer and surface-grafted polymer on SiNPs in aqueous NaCl solutions at 25 °C were carried out at a scattering angle ( $\theta$ ) ranging from 30 to 150° using a goniometer system (ALV CGS-3-TAC/LSE-5004, Langen, Germany) using a HeNe laser (wavelength  $\lambda=632.8\text{ nm}$ ) with a power of 22 mW. The Rayleigh ratio at a scattering angle of  $\theta=90^\circ$  was based on that of pure toluene at a wavelength of 632.8 nm at 25 °C.<sup>34</sup> The autocorrelation function was obtained by pseudo-cross-correlation of the signals from two photomultipliers to suppress noise. The samples for SLS and DLS measurements had four different concentrations in aqueous NaCl solutions ( $C_s=0\text{--}5.0\text{ M}$ ) contained in 10-mm diameter quartz cells. The scattering vector ( $q$ ) was defined as  $4\pi n_s \sin(\theta/2)/\lambda$ , where  $n_s$  is the refractive index of the solvent.

The densities of aqueous NaCl solutions and polymer solutions were measured at 25 °C using a density meter (Kyoto Electronics Manufacturing DA-505, Kyoto, Japan). The density of an aqueous NaCl solution at 25 °C can be expressed by<sup>35</sup>

$$\rho_m = (41.873 m - 2.0737 m^{3/2} - 0.6235 m^2 - 0.0257 m^{5/2}) \times 10^{-3} + \rho_0, \quad (1)$$

where  $m$  and  $\rho_0$  are the molal concentration and density ( $0.99705\text{ g cm}^{-3}$ ) of pure water, respectively. The value of  $m$  is then converted to  $C_s$  (M) by

$$C_s(\text{M}) = \frac{m\rho_s}{10^3 + mM} \times 10^3, \quad (2)$$

where  $M$  is the molecular weight of NaCl. The values of the refractive index ( $n_s$ ) for aqueous NaCl solutions for  $C_s$  from 0 to 5.0 M were measured at 25 °C using a multi-wavelength refractometer (Kyoto Electronics Manufacturing RA-500NW-S,  $\lambda=633\text{ nm}$ ). The value was found to be expressed by

$$n_s = (-6.65 C_s^3 - 188 C_s^2 + 9.77 \times 10^3 C_s + 27) \times 10^{-6} + n_0, \quad (3)$$

where  $n_0$  is the refractive index (1.3313) of pure water. The viscosity of an aqueous NaCl solution at 25 °C can be expressed as follows:<sup>36</sup>

$$\eta_s = (1 + 0.0061 C_s^{0.5} + 0.0794 C_s + 0.01142 C_s^2 + 6.19 \times 10^{-4} C_s^{3.5}) \times \eta_0. \quad (4)$$

Here,  $\eta_0$  is the viscosity ( $8.902 \times 10^{-3}\text{ g cm}^{-1}\text{ s}^{-1}$ ) of pure water.

The specific refractive index increments ( $dn/dc$ ) of free polymers in aqueous NaCl solutions for  $C_s$  from 0 to 5.0 M were measured using a differential refractometer (Otsuka Electric DRM-1020, Osaka, Japan,  $\lambda=633\text{ nm}$ ). The values of  $dn/dc$  for free PMAPS ( $M_w=1.36 \times 10^5\text{ g mol}^{-1}$ ,  $M_w/M_n=3.07$ ) in aqueous NaCl solutions at  $C_s=0.050, 0.10, 0.50, 1.0, 3.0$  and  $5.0\text{ M}$  were determined to be 0.1347, 0.1343, 0.1300, 0.1251, 0.1124 and  $0.1023\text{ g}^{-1}\text{ cm}^3$ , respectively. The values of  $dn/dc$  for free PMPC ( $M_w=2.43 \times 10^5\text{ g mol}^{-1}$ ,  $M_w/M_n=8.90$ ) in aqueous NaCl solutions at  $C_s=0, 0.050, 0.50, 1.0, 3.0$  and  $5.0\text{ M}$  were likewise determined to be 0.1415, 0.1405, 0.1363, 0.1322, 0.1190 and  $0.1038\text{ g}^{-1}\text{ cm}^3$ , respectively. The value of  $dn/dc$  for free PMAPS in an aqueous NaCl solution at another unmeasured  $C_s$  was also determined to give the same  $M_w$  of free PMAPS in an aqueous NaCl solution at  $C_s=0.10\text{ M}$ .

Small-angle X-ray scattering experiments of surface-grafted polymer chains on SiNPs in aqueous NaCl solutions at room temperature were carried out at the BL03XU<sup>37</sup> beamline of SPring-8 at an incident X-ray wavelength  $\lambda$  of 0.1 nm with a sample-to-detector distance of 7994 mm. The scattered intensity was detected using an imaging plate with  $3000 \times 3000$  pixels over a scattering vector range from 0.02 to  $0.6\text{ nm}^{-1}$ . The scattering vector ( $q$ ) as defined by  $4\pi \sin(\theta)/\lambda$  was calibrated by the average of 6 peaks of dry collagen. The samples for SAXS measurements had four different concentrations ( $C_p=1.0\text{--}2.0\text{ mg cm}^{-3}$ ) of SiNP-PMAPS and SiNP-PMPC in aqueous NaCl solutions ( $C_s=0\text{--}5.0\text{ M}$ ) contained in 2-mm diameter quartz capillaries.

Polymer solutions for scattering experiments were carefully prepared by a gravimetric method. After the free polymer and surface-grafted polymer on SiNPs were sufficiently dried under reduced pressure for >24 h at 60 °C, the samples were dissolved in an aqueous NaCl solution at 40 °C for 12 h. The solutions of surface-grafted polymer on SiNPs were sonicated for 1 h to yield well-dispersed nanoparticle solutions. The resulting solutions were filtered with DISMIC filter units (polytetrafluoroethylene, PTFE, pore size of 0.45  $\mu\text{m}$ ) just before the measurements and poured directly into measurement cells in a clean bench. The weight fraction ( $W_p$ ) was then converted to  $C_p$  ( $\text{g cm}^{-3}$ ) by:

$$C_p(\text{g cm}^{-3}) = \frac{W_p}{\rho_s^{-1}(1 - W_p) + v_p W_p}, \quad (5)$$

where  $\rho_s$  and  $v_p$  are the densities of solvent and the partial specific volume of the polymer, respectively. The values of  $v_p$  for free PMAPS in aqueous NaCl

solutions at  $C_s=0.050, 0.10, 0.50, 1.0, 3.0$  and  $5.0\text{ M}$  were determined to be  $0.690, 0.688, 0.682, 0.678$  and  $0.702\text{ cm}^3\text{ g}^{-1}$ , respectively. The values of  $v_p$  for free PMPC in the aqueous NaCl solutions at  $C_s=0, 0.10, 0.50, 1.0, 3.0$  and  $5.0\text{ M}$  were determined to be  $0.729, 0.742, 0.759, 0.763, 0.762$  and  $0.764\text{ cm}^3\text{ g}^{-1}$ , respectively.

**Table 2 Results from SLS and DLS measurements of free PMAPS in aqueous NaCl solutions at  $C_s=0.050\text{--}5.0\text{ M}$**

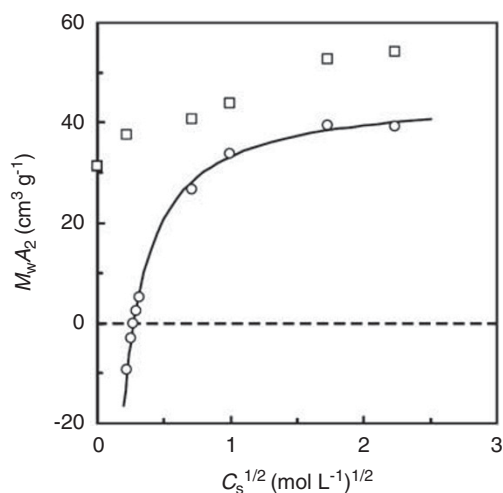
$C_s$ (M)	$A_2 \times 10^5$ ( $\text{g}^{-2}\text{ cm}^3\text{ mol}$ )	$D_0 \times 10^{-7}$ ( $\text{cm}^2\text{ s}^{-1}$ )	$R_H$ (nm)	$k_D$ ( $\text{g}^{-1}\text{ cm}^3$ )
0.050	-3.80	3.43	7.1	-15.8
0.065	-1.18			
0.074	0	3.36	7.2	-9.4
0.085	0.98			
0.10	2.12	3.29	7.4	-5.0
0.50	10.8	2.85	8.2	9.5
1.0	13.6	2.60	8.6	14.9
3.0	16.0	1.97	9.0	20.6
5.0	15.9	1.44	9.1	22.1

Abbreviations: DLS, dynamic light scattering; PMAPS, poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate]; SLS, static light scattering.

**Table 3 Results from SLS and DLS measurements of free PMPC in aqueous NaCl solutions at  $C_s=0\text{--}5.0\text{ M}$**

$C_s$ (M)	$A_2 \times 10^4$ ( $\text{g}^{-2}\text{ cm}^3\text{ mol}$ )	$D_0 \times 10^{-7}$ ( $\text{cm}^2\text{ s}^{-1}$ )	$R_H$ (nm)	$k_D$ ( $\text{g}^{-1}\text{ cm}^3$ )
0	1.34	2.12	11.6	28.9
0.050	1.60	2.11	11.6	29.6
0.50	1.74	2.03	11.6	30.9
1.0	1.87	1.99	11.3	25.9
3.0	2.25	1.52	11.7	32.9
5.0	2.32	1.14	11.5	30.5

Abbreviations: DLS, dynamic light scattering; PMAPS, poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate]; SLS, static light scattering.



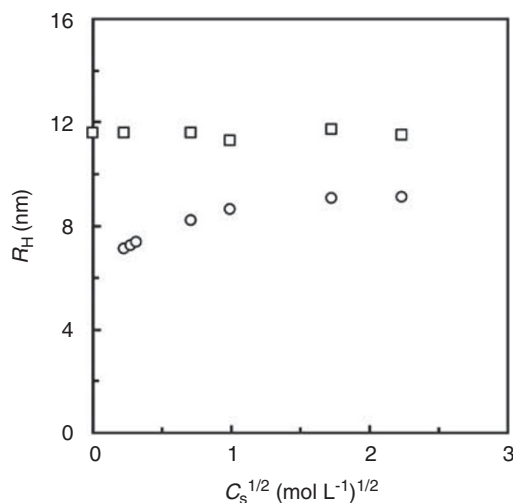
**Figure 1** Dependence of  $M_w A_2$  on  $C_s$  for free PMAPS ( $\circ$ ) and PMPC ( $\square$ ) in aqueous NaCl solutions. PMAPS, poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate]; PMPC, poly(2-methacryloyloxyethyl phosphorylcholine).

## RESULTS AND DISCUSSION

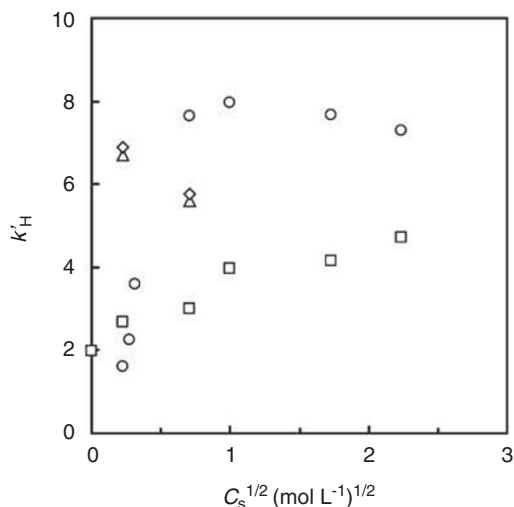
### Chain dimensional properties of free PMAPS and PMPC

The values of  $A_2$  of free PMAPS and PMPC in aqueous NaCl solutions at  $C_s=0\text{--}5.0\text{ M}$  are summarized in Tables 2 and 3. Details are described in the Supplementary Information. Figure 1 shows a  $C_s$  dependence of  $M_w A_2$  for free PMAPS ( $\circ$ ) and PMPC ( $\square$ ) in an aqueous NaCl solution at  $25\text{ }^\circ\text{C}$ . The  $M_w A_2$  for PMPC gradually increased with increasing  $C_s$ , whereas in the previous study,<sup>17</sup> the same parameter was almost constant over the entire  $C_s$  region from 0 to  $0.5\text{ M}$  ( $48.8\text{ cm}^3\text{ g}^{-1}$ ). It is possible that the small difference between our study and the previous one could be attributed to the MWD ( $M_w/M_n=1.50$ ) of PMPC. However, the  $M_w A_2$  for PMAPS increased sharply with increasing  $C_s$  in the  $C_s$  region below  $0.5\text{ M}$  and become almost constant in the higher  $C_s$  region  $\sim 3.0\text{ M}$ . As  $A_2$  reflects the volume exclusion of a polymer chain, Figure 1 suggests that the  $C_s$  dependence of the repulsive interaction between PMAPS chains in an aqueous NaCl solution is much stronger than that of PMPC. The value of  $M_w A_2$  for PMAPS was observed to be 0 in an aqueous NaCl solution at  $C_s=0.074\text{ M}$ . Therefore, we defined an aqueous NaCl solution at  $C_s=0.074\text{ M}$  as the  $\theta$ -concentration ( $C_{s,\theta}$ ) of PMAPS. Kato *et al.*<sup>28</sup> previously found using SLS that the  $C_{s,\theta}$  was  $0.060\text{ M}$  for PMAPS at  $30\text{ }^\circ\text{C}$  is an aqueous NaCl solution. It is possible that the small difference between  $C_{s,\theta}=0.074\text{ M}$  in our study and  $C_{s,\theta}=0.060\text{ M}$  in the previous study could be attributed to the MWD of PMAPS and the experimental temperature.

The values of the diffusion coefficient at an infinite dilution ( $D_0$ ), the hydrodynamic radius ( $R_H$ ) and the concentration coefficient of the diffusion coefficient ( $k_D$ ) of free PMAPS and PMPC in aqueous NaCl solutions at  $C_s=0\text{--}5.0\text{ M}$  are summarized in Tables 2 and 3. Details are described in the Supplementary Information. Figure 2 shows the  $C_s$  dependence of  $R_H$  for free PMAPS ( $\circ$ ) and PMPC ( $\square$ ) in aqueous NaCl solutions at  $25\text{ }^\circ\text{C}$ . The  $R_H$  of PMPC was almost constant regardless of  $C_s$ , whereas the  $R_H$  for PMAPS increased with increasing  $C_s$ . The  $R_H$  values of PMPC in aqueous NaCl solutions were larger than those of PMAPS at all  $C_s$ , despite that the weight average degree of polymerization ( $N_w=792$ ) of PMPC is less than that of PMAPS ( $N_w=884$ ). Considering that the  $R_H$  reflects the hydrodynamic dimen-



**Figure 2** Dependence of  $R_H$  on  $C_s$  for free PMAPS ( $\circ$ ) and PMPC ( $\square$ ) in aqueous NaCl solutions. PMAPS, poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate]; PMPC, poly(2-methacryloyloxyethyl phosphorylcholine).



**Figure 3** Dependence of  $K_H$  on  $C_s$  for free PMAPS (○) and PMPC (□) in aqueous NaCl solutions, together with that of free NaPSS<sup>41</sup> (△) and NaPAMPS<sup>42,43</sup> (◇) with the same molecular weight. PMAPS, poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate]; PMPC, poly(2-methacryloyloxyethyl phosphorylcholine).

sions of a polymer chain, the larger  $R_H$  of PMPC implies that the main chain stiffness of PMPC is higher than that of PMAPS in the solution.

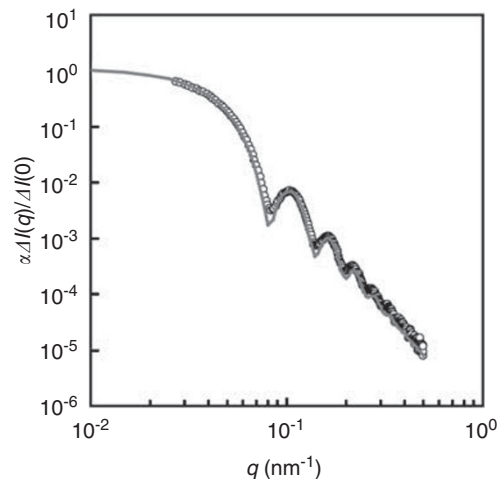
The value of  $k_D$  for flexible polymer chains is defined by the following equation:<sup>38</sup>

$$k_D = 2A_2M_w - v_p - k'_H \left( \frac{4\pi R_H^3}{3} \right) \left( \frac{N_A}{M_w} \right), \quad (6)$$

where  $k'_H$  is a universal constant for free chains irrespective of the kind of polymers and molecular weight. The value of  $k'_H$  for typical flexible polymers in a good solvent was reported over a range from 4 to 6.<sup>38</sup> The value of  $k'_H$  calculated from the literature data<sup>39,40</sup> for atactic poly(methyl methacrylate) in acetonitrile at 44.0 °C ( $\theta$ -solvent) is estimated to be approximately 1.3–1.8. The values of  $k'_H$  for free PMAPS and PMPC were calculated from equation (6) using the measured values of  $A_2$ ,  $M_w$ ,  $v_p$ ,  $k_D$  and  $R_H$ . Figure 3 shows the  $C_s$  dependence of  $k'_H$  for free PMAPS (○) and PMPC (□) in aqueous NaCl solutions at 25 °C, together with that of free poly(styrene sulfonate sodium salt) (NaPSS;  $M_w=2.56 \times 10^5$  g mol<sup>-1</sup>)<sup>41</sup> (△) and poly(2-acrylamido-2-methylpropanesulfonate sodium salt) (NaPAMPS;  $M_w=2.76 \times 10^5$  g mol<sup>-1</sup>)<sup>42,43</sup> (◇) with the same molecular weight. The values of  $k'_H$  for PMAPS and PMPC in aqueous NaCl solutions were revealed to be 1.5–8, which may be regarded as a  $\theta$ -state and a good solvent state, indicating the reduction in intramolecular and intermolecular interaction between polymer chains with increasing  $C_s$ . However,  $k'_H$  of the typical polyanions, such as NaPSS, NaPAMPS and sodium carboxymethyl cellulose,<sup>44</sup> apparently decreased with increasing  $C_s$  until eventually reaching a  $\theta$ -state and poor solvent state because the intramolecular and intermolecular repulsive interactions between polymer chains were screened by hydrated ions.

#### Characterization of SiNP-PMAPS and SiNP-PMPC

The scattering form factor ( $P(q)$ ), which is related to  $\Delta I(q)/\Delta I(0)$  ( $\Delta I(q)$  is the experimental excess scattering intensity) from the SAXS data for SiNP-BHE in TFE, may be compared with the solid sphere model with polydispersity. According to Arag3n and Pecora,<sup>45</sup> the scattering function ( $P_z(q\bar{R})$ ) for the assumed Schulz-distributed solid spheres with a radius of  $R$  is expressed by



**Figure 4** SAXS profiles of SiNP-BHE in TFE. The solid curves represent the theoretical values for the assumed Schulz-distributed spherical particles with a radius of  $R=55.0$  nm and an exponential parameter of  $z=180$ . SAXS, small-angle X-ray scattering; SiNP-BHE, immobilization of (2-bromo-2-methyl)propionyloxyhexyltriethoxysilane on a SiNP; TFE, 2,2,2-trifluoroethanol.

$$P_z(q\bar{R}) = \int_0^\infty \frac{\alpha^2(R) \left\{ \frac{3}{(qR)^3} [\sin(qR) - qR \cos(qR)] \right\}^2}{\alpha_z^2(\bar{R})} f_z(R) dR \quad (7)$$

and

$$f_z(R) = \frac{1}{z!} \left( \frac{z+1}{\bar{R}} \right)^{z+1} R^z \exp \left[ -\frac{(z+1)R}{\bar{R}} \right], \quad (8)$$

where  $\alpha(R)$ ,  $f_z(R)$ ,  $z$  and  $\bar{R}$  are the polarizability of the particle, the Schulz distribution function, the width of the distribution and the average radius of the sphere, respectively.  $\alpha(R)$  depends on the size through the bulk volume of the particle. Polydispersity ( $p$ ) for a Schulz distribution can be written as  $p^2=1/(z+1)$ . The experimental data for SiNP-BHE ( $C=1.38$  mg cm<sup>-3</sup>), which were used for preparation of SiNP-PMAPS, can be described assuming Schulz-distributed spherical particles with a radius of  $R=55.0$  nm and an exponential parameter of  $z=180$ , corresponding to a polydispersity of  $p=0.074$ , as shown in Figure 4. These values of SiNP-BHE used SiNP-PMPC were determined by the same method to be  $R=56.0$  nm,  $z=180$  and  $p=0.074$ .

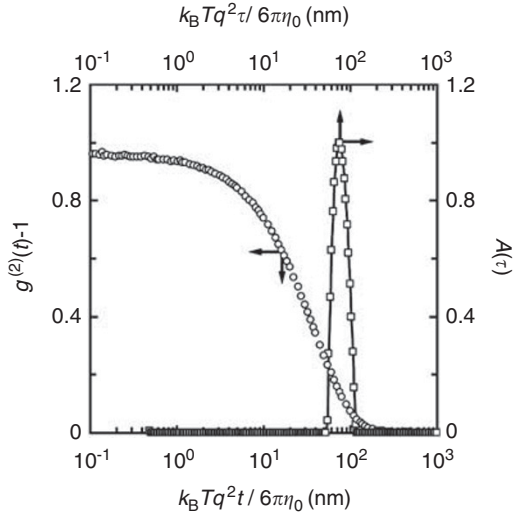
The graft density of a polymer brush on the SiNP surface is expressed by

$$\sigma = \frac{R\rho_{\text{silica}}N_A}{3M_n \left( \frac{1}{w} - 1 \right)}, \quad (9)$$

where  $\rho_{\text{silica}}$ ,  $w$  and  $N_A$  are the density of silica (1.6 g cm<sup>-3</sup>), the weight loss of a polymer and Avogadro's number, respectively. The graft densities of PMAPS and PMPC brushes on a SiNP surface were calculated using equation (9) to be 0.129 and 0.065 chains per nm<sup>2</sup>, respectively. The average numbers of graft PMAPS and PMPC chains per SiNP were estimated to be 4910 and 2590 chains, respectively, assuming the aforementioned graft density and the SiNP surface area. These values of SiNP-PMAPS and SiNP-PMPC are summarized in Table 1.

#### Dimensions of grafted chains of PMAPS and PMPC on SiNP

The typical autocorrelation function ( $g^2(t)-1$ ) and relaxation spectrum ( $A(\tau)$ ) measured by DLS for SiNP-PMAPS in an aqueous NaCl



**Figure 5** Typical autocorrelation function (○) obtained by DLS for SiNP-PMAPS and relaxation spectrum (□) calculated from the autocorrelation function. The concentration of SiNP-PMAPS in an aqueous NaCl solution at  $C_s=5.0\text{ M}$  and the scattering angle are  $C_p=0.47\text{ mg cm}^{-3}$  and  $\theta=90^\circ$ . DLS, dynamic light scattering; SiNP-PMAPS, silica nanoparticles immobilized with poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate].

**Table 4** Results from DLS and SAXS measurements of SiNP-PMAPS in aqueous NaCl solutions at  $C_s=0.050\text{--}5.0\text{ M}$

$C_s$ (M)	$D_0 \times 10^{-8}$ ( $\text{cm}^2\text{s}^{-1}$ )	$R_{H,brush}$ (nm)	$s$ (nm)	$v_{brush}$ ( $\text{g}^{-1}\text{cm}^3$ )	$\rho$
0.050	3.31	9.4	9.5	0.69	1.01
0.10	3.43	8.0	10	0.69	1.25
0.50	3.35	7.5	17	0.68	2.27
1.0	3.17	7.7	18	0.68	2.33
3.0	2.54	7.5	19	0.70	2.52
5.0	1.84	8.1	21	0.74	2.59

Abbreviations: DLS, dynamic light scattering; PMAPS, poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate]; SAXS, small-angle X-ray scattering; SiNP, silica nanoparticle.

**Table 5** Results from DLS and SAXS measurements of SiNP-PMPC in aqueous NaCl solutions at  $C_s=0\text{--}5.0\text{ M}$

$C_s$ (M)	$D_0 \times 10^{-8}$ ( $\text{cm}^2\text{s}^{-1}$ )	$R_{H,brush}$ (nm)	$s$ (nm)	$v_{brush}$ ( $\text{g}^{-1}\text{cm}^3$ )	$\rho$
0	3.45	7.5	9.5	0.73	1.26
0.050	3.40	7.8	9.5	0.74	1.21
0.50	3.29	7.6	9.5	0.76	1.25
1.0	3.11	8.0	9.5	0.76	1.19
3.0	2.51	7.5	9.5	0.76	1.26
5.0	1.83	7.7	9.5	0.86	1.23

Abbreviations: DLS, dynamic light scattering; PMAPS, poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate]; SAXS, small-angle X-ray scattering; SiNP, silica nanoparticle.

solution at  $C_s=5.0$  are shown in Figure 5. The concentration of SiNP-PMAPS and the scattering angle were  $C=0.47\text{ mg cm}^{-3}$  and  $\theta=90^\circ$ , respectively.  $A(\tau)$  at the relaxation time ( $\tau$ ) was calculated from the intensity of  $g^2(t)-1$  at time ( $t$ ) by a CONTIN analysis.<sup>46,47</sup>  $A(\tau)$  was observed as a single sharp peak.  $A(\tau)$  of all concentrations and

scattering angles for SiNP-PMAPS and SiNP-PMPC solutions showed a unimodal distribution and sharp peak, indicating the homogenous dispersion of SiNP-PMAPS and SiNP-PMPC in aqueous NaCl solutions at various  $C_s$  without any aggregations. By extrapolating to  $q=0$  and  $C=0$ , the values of  $D_0$  and  $R_H$  for SiNP-PMAPS in an aqueous NaCl solution at  $C_s=5.0\text{ M}$  were determined to be  $1.84 \times 10^{-8}\text{ cm}^2\text{s}^{-1}$  and  $71.2\text{ nm}$ , respectively. The values of  $D_0$  and  $R_H$  for SiNP-PMAPS and SiNP-PMPC in aqueous NaCl solutions at each  $C_s$  were also determined using the same method. The values of  $D_0$  and the hydrodynamic radius of a polymer layer ( $R_{H,brush}$ ) calculated from  $(R_H - R_c)/2$  are summarized in Tables 4 and 5.

Figure 6a shows the SAXS profiles for SiNP-PMAPS in aqueous NaCl solutions for  $C_s$  over a range from 0.050 to 5.0 M. The SAXS profiles showed smooth minima in the SiNP-PMAPS form factor, which was slightly shifted to a low- $q$  region, unlike the SiNP-BHE form factor. SiNP-PMAPS in an aqueous NaCl solution is expected to form a core-shell structure, as shown in the inset of Figure 6a. Here, we estimated the radius of gyration of the polymer layer of SiNP-PMAPS from the SAXS profile using a core-shell model analysis, taking the interacting excluded-volume chains into consideration. The scattering form factor for the core-shell model contains four terms as shown below:<sup>48</sup>

$$P(q) = \left\{ \begin{array}{l} N^2 \Delta Z_{e,core}^2 P_{core}(q) + N \Delta Z_{e,chain}^2 P'(q) \\ + 2N \Delta Z_{e,core} \Delta Z_{e,chain} S_{core-chain}(q) \\ + N[N - P'(0)] \Delta Z_{e,chain}^2 A_{chain}^2(q) \end{array} \right\} N^{-2} (\Delta Z_{e,core} + \Delta Z_{e,chain})^{-2}, \quad (10)$$

where  $N$  is the number of surface-grafted polymer chains on SiNP,  $\Delta Z_e$  the excess electron density,  $P_{core}(q)$  a scattering function for a rigid sphere assuming Schulz distribution calculated from equations (7) and (8),  $P'(q)$  the effective form factor of a chain in the corona chains expressed by the following equations (11) and (12),  $S_{core-chain}(q)$  the structure factor between the core and corona chains expressed by equations (13) and (14) and  $A_{chain}(q)$  the form-factor amplitude of the chain expressed by equation (14).

$$P'(q) = \frac{P_{PWC}(q)}{1 + v P_{PWC}(q)} \quad (11)$$

and

$$v = 1.4 \left[ \frac{Ns^2}{4(R_c + s)^2} \right]^{1.04}, \quad (12)$$

where  $P_{PWC}(q)$ ,  $v$  and  $s$  are the scattering functions for an infinitely thin perturbed wormlike chain,<sup>49</sup> parameter-related surface coverage of chains and radius of gyration of the polymer layer, respectively.

$$S_{core-chain}(q) = \frac{3}{(qR_c)^3} [\sin(qR_c) - qR_c \cos(qR_c)] A_{chain}(q) \quad (13)$$

and

$$A_{chain}(q) = \frac{\int Z_{chain}(r) r^2 \frac{\sin(qr)}{qr} dr}{\int Z_{chain}(r) r^2 dr}, \quad (14)$$

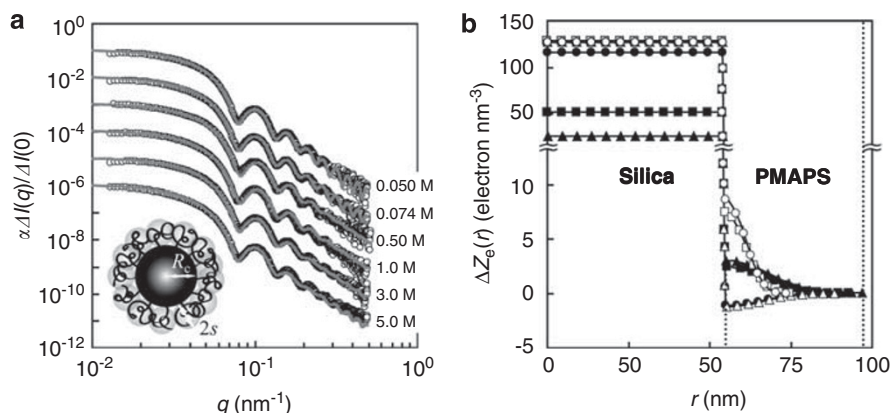
where  $R_c$  and  $Z_{chain}(r)$  are the core radius and the average radial electron density profile of the corona chains, respectively.

The excess electron density of the core ( $\Delta Z_{e,core}$ ) and chain ( $\Delta Z_{e,chain}$ ) are defined as

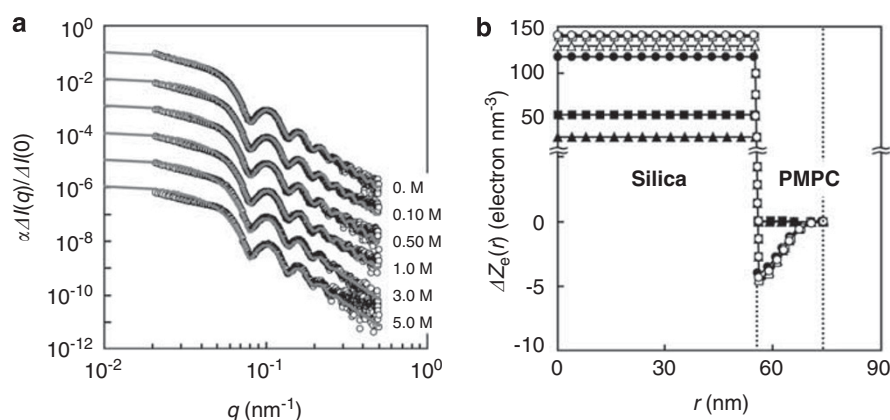
$$\Delta Z_{e,core} = N_A \rho_{silica} \frac{n_{e,silica}}{M_{silica}} - N_A \rho_{brush} \frac{n_{e,brush}}{M_{0,brush}} \quad (15)$$

and

$$\Delta Z_{e,chain} = N_A \rho_{brush} \frac{n_{e,brush}}{M_{0,brush}} - N_A \rho_s \frac{n_{e,s}}{M_s} \quad (16)$$



**Figure 6** (a) SAXS profiles of SiNP-PMAPS in aqueous NaCl solutions at  $C_s$  over a range from 0 to 5.0 M. The solid curves represent the values calculated from equations (7), (8) and (10)–(17) with the two model parameters. (b) Radial electron density profiles for SiNP-PMAPS in aqueous NaCl solutions at  $C_s=0.050$  (○), 0.074 (□), 0.50 (△), 1.0 (●), 3.0 (■) and 5.0 (▲) M estimated from the SAXS profile using a core-shell model analysis. SAXS, small-angle X-ray scattering; SiNP-PMAPS, silica nanoparticles immobilized with poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate].



**Figure 7** (a) SAXS profiles of SiNP-PMPC in the aqueous NaCl solutions at  $C_s$  over a range from 0 to 5.0 M. The solid curves represent the values calculated from equations (7), (8) and (10)–(17) with the two model parameters. (b) Radial electron density profiles for SiNP-PMPC in aqueous NaCl solutions at  $C_s=0$  (○), 0.050 (□), 0.50 (△), 1.0 (●), 3.0 (■) and 5.0 (▲) M estimated from SAXS profile using a core-shell model analysis. SAXS, small-angle X-ray scattering; SiNP-PMAPS, silica nanoparticles immobilized with poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate].

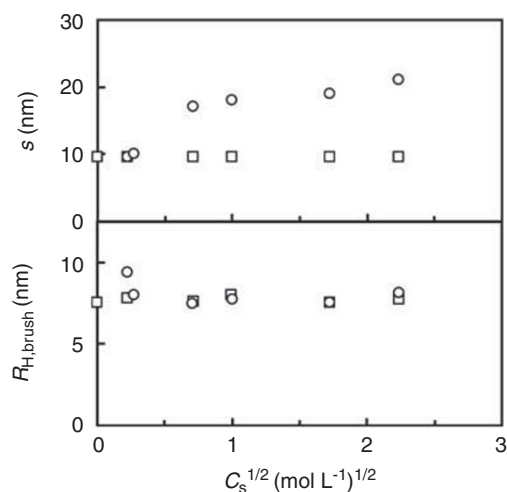
where  $n_{e,\text{core}}$  and  $M_{\text{silica}}$  are the number of electrons and the molecular weight of the silica, respectively, whereas  $n_{e,\text{brush}}$  and  $M_{0,\text{brush}}$  are the number of electrons and the molecular weight per repeating unit of the polymer brush, respectively. The density of the polymer brush in the solvent ( $\rho_{\text{brush}}$ ) is defined as  $(1 - \nu_{\text{brush}}\rho_s)C_{\text{brush}} + \rho_s$ , where the  $\nu_{\text{brush}}$  is the partial specific volume of the polymer brush, which was determined by fitting the experimental data of the SAXS profile with equations (7), (8) and (10)–(17) in the low- $q$  region. However, the accurate concentration of the polymer brush ( $C_{\text{brush}}$ ) has a distribution along with the distance from the nanoparticle surface to the outer solvent phase due to the swollen brush structure. Therefore, here we used the apparent concentration of the polymer brush in the solvent,  $C_{\text{brush,app}}$ , instead of  $C_{\text{brush}}$ , by calculation using the following expression:

$$C_{\text{brush,app}} = \frac{3M_{n,\text{brush}}N}{4\pi N_A [(2s + R_{\text{core}})^3 - R_{\text{core}}^3]} \quad (17)$$

The experimental SAXS profile for SiNP-PMAPS in an aqueous NaCl solution at  $C_s=0.050$  M was close to the theoretical profile obtained from equations (7), (8) and (10)–(17) for a core radius  $R_c=55.0$  nm, core polydispersity  $p=0.074$ , polymer layer radius  $s=9.5$  nm and

$\nu_{\text{brush}}=0.69 \text{ g}^{-1} \text{ cm}^3$  as shown in the Figure 6a. The values of  $s$  and  $\nu_{\text{brush}}$  for SiNP-PMAPS in aqueous NaCl solutions at various  $C_s$  values were also estimated using the same method, and these values are listed in Table 4. The solid lines in Figure 6a are values calculated from equations (7), (8) and (10)–(17) with the two model parameters. The value of  $\nu_{\text{brush}}$  was close to that of  $\nu_p$  of the free PMAPS in an aqueous NaCl solution at a given  $C_s$ . The experimental SAXS profiles for SiNP-PMAPS in aqueous NaCl solutions at all  $C_s$  values were close to the profiles calculated from equations (7), (8) and (10)–(17) with the two model parameters. Figure 6b shows the radial profiles for SiNP-PMAPS in aqueous NaCl solutions at various  $C_s$  values estimated from the SAXS profile based on the core-shell model incorporated with interaction among the surface-grafted perturbed wormlike chains, which are the so-called interacting self-avoiding chains.<sup>48</sup>

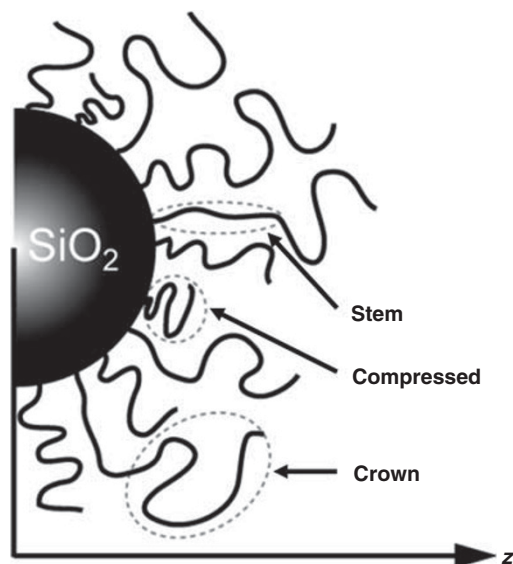
Figure 7a shows the SAXS profiles for SiNP-PMPC in aqueous NaCl solutions at  $C_s$  values over a range from 0 to 5.0 M. The characteristic parameters of the SiNP-PMPC in aqueous NaCl solutions at various  $C_s$  estimated by the procedure mentioned above are summarized in Table 5. The solid lines in Figure 7a are the theoretical curves calculated from equations (7), (8) and (10)–(17) with a core radius of  $R_c=56.0$  nm, core polydispersity of  $p=0.074$  and the model para-



**Figure 8** Dependence of  $s$  and  $R_{H,brush}$  on NaCl concentration for SiNP-PMAPS (○) and SiNP-PMPC (□) in aqueous NaCl solutions at  $C_s$  in the range 0–5.0 M. SiNP-PMAPS, silica nanoparticles immobilized with poly[3-(*N*-2-methacryloyloxyethyl-*N,N*-dimethyl) ammonatopropanesulfonate].

meters listed in Table 5. The scattering factor for SiNP-PMPC in aqueous NaCl solutions is described by the core-shell model, taking into account the interacting self-avoiding chains and assuming a Schulz-distributed core with two fitting parameters. The value of  $v_{brush}$  is close to that of  $v_p$  of free PMPC in aqueous NaCl solutions for a given  $C_s$ , except for  $C_s=5.0$  M. Figure 7b illustrates the radial profiles for SiNP-PMPC in aqueous NaCl solutions at various  $C_s$  values estimated from the SAXS profile and the core-shell model containing the interacting self-avoiding chains.

Figure 8 shows the  $C_s$ -dependence of  $R_{H,brush}$  and  $s$  for SiNP-PMAPS (○) and SiNP-PMPC (□) in aqueous NaCl solutions. The  $R_{H,brush}$  and  $s$  for SiNP-PMPC were constant over the entire  $C_s$  region from 0 to 5.0 M. The  $C_s$  dependence of  $R_{H,brush}$  for SiNP-PMPC is in good agreement with that reported by Matsuda *et al.*, who also did not observe a swelling of the PMPC brush upon addition of up to 0.5 M NaCl.<sup>17</sup> These results imply that  $C_s$  dependence of the repulsive interaction between polymer chains for SiNP-PMPC in an aqueous NaCl solution is similar to that of the free PMPC. However, the value of  $s$  for SiNP-PMAPS increased with increasing  $C_s$ , whereas  $R_{H,brush}$  for SiNP-PMAPS slightly decreased with increasing  $C_s$  in the  $C_s$  region below 0.5 M, and that parameter become almost constant in the  $C_s$  region above 0.5 M. Polzer *et al.*<sup>16</sup> reported that the  $R_H$  of PMAPS brush shell on a colloidal particle consisting of a divinylbenzene cross-linked polystyrene core (PS-*co*-DVB/PMAPS) was almost constant in the  $C_s$  region below 0.5 M, but increased with increasing  $C_s$  in the  $C_s$  region above 0.5 M.<sup>16</sup> The  $R_{H,brush}$  (7.7 nm) of the PMAPS brush for SiNP-PMAPS in an aqueous NaCl solution at  $C_s=1.0$  M was larger than that (4.0 nm) of the PMAPS brush shell in the previous report at the same  $C_s$ , despite that the  $M_w$  ( $3.02 \times 10^4$  g mol<sup>-1</sup>) of the surface-grafted PMAPS chains in our study was smaller than that ( $M_w=6.96 \times 10^4$  g mol<sup>-1</sup>) of the previous study. It is possible that the difference in the chain dimension of the PMAPS brush between SiNP-PMAPS ( $\sigma=0.129$  chains per nm<sup>2</sup>) and PS-*co*-DVB/PMAPS ( $\sigma=0.08$  chains per nm<sup>2</sup>) can be attributed to graft density. These results imply that the  $C_s$  dependence of the repulsive interaction between polymer chains for SiNP-PMAPS in an aqueous NaCl solution is similar to that of the PMAPS brush shell for PS-*co*-DVB/



**Figure 9** Schematic cross-sectional view of the internal structure of surface-grafted polymer chains with polydispersity on SiNPs. SiNP, silica nanoparticle.

PMAPS and the free PMAPS, except for the  $C_s$ -dependence of  $R_{H,brush}$  for SiNP-PMAPS.

The  $M_w$  dependence of the  $z$ -average, mean-square radius of gyration ( $\langle S^2 \rangle_z$ ) for the free PMAPS in a  $\theta$ -state in an aqueous NaCl solution at 0.074 M is given by<sup>12</sup>

$$\langle S^2 \rangle_z^{1/2} = 0.018 M_w^{0.5}. \quad (18)$$

The thickness of the polymer brush layer for SiNP-PMAPS was estimated to be 9.5 nm, which was much larger than the  $\langle S^2 \rangle_z^{1/2} = 3.1$  nm calculated from equation (18) for free PMAPS chains with the same  $C_s$  and  $M_w$ . The chain dimensions of the polymer brush for SiNP-PMAPS in an aqueous solution were actually larger than the free PMAPS. It is well known that polymer chains in concentrated polymer brushes are extended because of the excluded-volume effect of neighboring polymer chains.<sup>10</sup> Thus, significant change seems to have occurred in the chain conformation between the brush and the free polymer.

It is well known that  $\rho$ , defined as the ratio of the radius of gyration to the hydrodynamic radius, is a universal constant for free chains almost irrespective of the chemical structure and molecular weight of polymers. The values of  $\rho$  estimated from  $s$  measured by SAXS and  $R_{H,brush}$  measured by DLS of the polymer layer for SiNP-PMAPS and SiNP-PMPC in aqueous NaCl solutions at all  $C_s$  are summarized in Tables 4 and 5. The value of  $\rho$  for SiNP-PMPC in aqueous NaCl solutions at all  $C_s$  was approximately constant (1.19–1.26) and was similar to those of typical flexible polymers in  $\theta$ -solvent and good solvents (1.2–1.5).<sup>50</sup> The  $\rho$  for SiNP-PMAPS increased with increasing  $C_s$  in the  $C_s$  region below 0.5 M and became almost constant in the  $C_s$  region above 0.5 M. The values (2.27–2.59) of  $\rho$  for SiNP-PMAPS in the  $C_s$  region above 0.5 M were larger than those of reference data for PMAPS in an aqueous NaCl solution for  $C_s$  in the range 0.06–1.0 M at 30 °C (1.1–1.3)<sup>28</sup> and the Gaussian chain limit (1.48).<sup>50</sup> Thus, the chain conformation of PMAPS and PMPC brushes on the SiNP surface behaves like a semi-flexible and flexible polymer chain, respectively. It is possible that the difference in the chain conformation between PMAPS and PMPC brushes could be attributed to the broad



MWD and low graft density of PMPC because of the following reasons.

de Vos *et al.*<sup>14</sup> reported that the internal structure of the polymer brush by numerical self-consistent field theory is strongly influenced by polydispersity, as shown in Figure 9. Short chains are compressed close to the grafting interface, whereas long chains have a characteristic flower-like conformation. These long chains stretch strongly (forming a stem) when surrounded by shorter chains and decrease their stretching (forming a crown) when only surrounded by longer chains. These findings imply that chain conformation of the PMPC brush with a broad MWD on a SiNP surface behaves like a Gaussian coil. Therefore, our report may be the first experimental report on the crucial difference in the chain conformation between the brush on a SiNP and the free PMAPS with salt concentration dependence.

## CONCLUSIONS

We performed SLS, DLS and SAXS for PMAPS and PMPC in aqueous NaCl solutions and found that PMPC had a relatively stiff structure in an aqueous NaCl solution for a wide range of  $C_s$  (0–5.0 M), unlike PMAPS. This is because the  $R_H$  of PMPC in aqueous NaCl solutions was larger than that of the PMAPS, whereas the weight average degree of polymerization ( $N_w=792$ ) of PMPC was less than that of PMAPS ( $N_w=884$ ). The  $K_H$  values of both PMAPS and PMPC in aqueous NaCl solutions were higher than 1.5 in all  $C_s$  regions, indicating that the polymers were in the  $\theta$ -state or good solvent state. The scattering factors for SiNP-PMAPS and SiNP-PMPC in aqueous NaCl solutions at  $C_s=0$ –5.0 M were well described by the core-shell model, taking into account interacting self-avoiding chains and assuming a Schulz-distributed core with two fitting parameters. From the ratio of the radius of gyration measured by SAXS to the hydrodynamic radius measured by DLS for the polymer layer for SiNP-PMAPS and SiNP-PMPC in aqueous NaCl solutions at  $C_s=0$ –5.0 M, the chain conformations of PMAPS and PMPC brushes on a silica surface resembled semi-flexible and flexible polymer chains, respectively.

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