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# Challenges in Modeling Electrochemical Reaction Energetics with Polarizable Continuum Models

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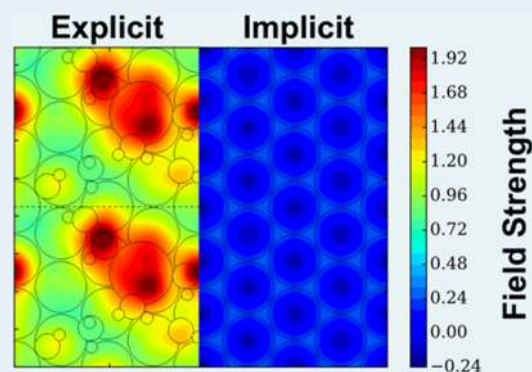
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## Supporting Information

**ABSTRACT:** A major challenge in the modeling of electrochemical phenomena is the accurate description of the interface between an electrolyte and a charged conductor. Polarizable continuum models (PCM) have been gaining popularity because they offer a computationally inexpensive method of modeling the electrolyte. In this Perspective, we discuss challenges from using one such model which treats the ions using a linearized Poisson–Boltzmann (LPB) distribution. From a physical perspective, this model places charge unphysically close to the surface and adsorbates, and it includes excessively steep ramping of the dielectric constant from the surface to the bulk solvent. Both of these issues can be somewhat mitigated by adjusting parameters built into the model, but in doing so, the resultant capacitance deviates from experimental values. Likewise, hybrid explicit-implicit approaches to the solvent may offer a more realistic description of hydrogen bonding and solvation to reaction intermediates, but the corresponding capacitances also deviate from experimental values. These deviations highlight the need for a careful adjustment of parameters in order to reproduce not only solvation energies but also other physical properties of solid–liquid interfaces. Continuum approaches alone also necessarily do not capture local variations in the electric field from cations at the interface, which can affect the energetics of intermediates with substantial dipoles or polarizability. Finally, since the double-layer charge can be varied continuously, LPB/PCM models provide a way to determine electrochemical barriers at constant potential. However, double-layer charging and the atomic motion associated with reaction events occur on significantly different timescales. We suggest that more detailed approaches, such as the modified Poisson–Boltzmann model and/or the addition of a Stern layer, may be able to mitigate some but not all of the challenges discussed.

**KEYWORDS:** density functional theory, catalysis, electrocatalysis, electrochemistry, solvation



## 1. INTRODUCTION

The interface between an electrode and the surrounding electrolyte plays a central role in electrochemistry, yet our understanding of its structure and function is still limited. Historically, theories have adopted a continuum description of the ions and treat the solvent as a dielectric medium.<sup>1–6</sup> Such models have offered insight into the ion distribution of the double layer and the charging behavior of the interface. In recent ab initio investigations of electrochemical reaction energetics, there are two main approaches toward the

electrolyte: a fully explicit, atomistic description, or an implicit description that builds upon classical continuum models.

In principle, a fully explicit description of the electrolyte would provide the most accurate description of the effects of solvation, interfacial fields, and applied bias.<sup>7–15</sup> However, an explicit description of the electrolyte is computationally demanding, and current approaches can often not appropri-

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ately sample the solvent's phase space at the desired thermodynamic conditions.<sup>8,12,16–20</sup> While it is possible in principle to adequately sample the solvent and ionic configuration space with a fully explicit approach,<sup>21,22</sup> such studies are extremely computationally demanding and not practical for the analysis of complex reaction mechanisms or for materials screening. Furthermore, achieving constant electrode potential during MD runs via the implementation of a potentiostat is technically challenging and requires the use of a continuum charge description to express noninteger fluctuations of the counter-charge density,<sup>23</sup> which poses several challenges as we discuss below. Explicitly modeled water can also suffer from band misalignment as reported in ref 24, because of poor description of the solvent LUMO and HOMO levels, and the resultant gap. This can in some cases result in unphysical charge transfer between the solvent and metal.

Implicit models, on the other hand, model the electrolyte using continuum approaches. Although such models have been developed for a long time, it is, to date, still unclear to what extent these methods accurately describe electrocatalytic processes at solid–liquid interfaces. Several types of implicit models have been proposed: a homogeneous background charge in the entire model system,<sup>25–27</sup> a Gaussian counter-charge distribution outside the surface,<sup>28,29</sup> and, more recently, a Poisson–Boltzmann description of the solvent and ion distribution.<sup>30–38</sup> The last approach is available in several widely used electronic structure codes<sup>30,32,34,39–41</sup> and has been successfully applied in a number of recent mechanistic studies of oxygen evolution, CO<sub>2</sub> reduction, and CO reduction.<sup>42–47</sup> By utilizing Green's function techniques to lift the requirement of periodicity in the direction normal to the surface, compensating charge can be modeled as an effective screening medium.<sup>48,49</sup> These techniques have been applied to surfaces to eliminate spurious multipole interactions associated with DFT slab calculations,<sup>50</sup> and as part of a scheme for grand-canonical *ab initio* molecular dynamics.<sup>23</sup> Several approaches combine quantum-level DFT with classical DFT for the electrolyte.<sup>45,51–53</sup> Finally, implicit continuum atomistic hybrids, dubbed microsolvation,<sup>15</sup> present the possibility of a computationally inexpensive solution by including a minimal amount of explicit solvent molecules within a continuum model framework. Such an approach avoids the elaborate calculations needed for explicit inclusion of solvent and ions, while retaining an *ab initio* consideration of the effect of solvent and ions at the interface.<sup>9,15,42–44,54,55</sup>

A particular challenge in *ab initio* computational electrocatalysis is the need for the inclusion of applied bias at the electrode. At the most basic level, an applied bias improves the feasibility of the overall process by shifting the energetics of each oxidative or reductive step in the process. This effect of the applied bias on the reaction thermodynamics is captured in the computational hydrogen electrode (CHE) model at effectively zero additional computational cost relative to surface science calculations, and represents a very simple and still widely used model applied to electrocatalysis.<sup>56</sup> While the CHE in principle can be<sup>12,17,57</sup> applied in conjunction with solvent and external electric fields, it cannot alone be used to probe charge transfer barriers and the associated kinetics.<sup>58</sup>

Because fully explicit solvent models operate under a constant number of electrons, changes in the dipole of the interface from either chemical or electrochemical steps along the reaction barrier lead to corresponding shifts in potential,

and extrapolation methods are needed to bridge the constant charge and constant potential limits.<sup>20,58</sup> Implicit solvent-electrolyte methods, which allow for a continuous variation of interfacial charge, offer the possibility of simulations at constant potential, since the Fermi level can be matched to the desired bias in an iterative manner. Due to the implicit solvent and electrolyte, it preserves the advantage of low-dimensional potential surfaces and avoids the need for statistical mechanics, and therefore requires a computational cost increase of only several-fold relative to bias-free modeling. For these reasons, the variants of this approach are likely to be widely used in the near future.

In the present Perspective, we examine the combined linearized Poisson–Boltzmann/polarizable continuum model (LPB/PCM)-DFT method and discuss a number of associated open challenges. We investigate the resultant charge distribution at the electrochemical interface and show how it affects the energetics of two elementary processes, CO<sub>2</sub> adsorption, and the Volmer reaction on Pt(111). In particular, we discuss several challenges associated with the determination of the electrochemical interfacial structure and reaction energetics:

1. Default parametrizations place the ionic countercharge unphysically close to the metal surface, and the dielectric constants are ramped too quickly to the bulk values.
2. LPB/PCM models alone cannot capture the local field variations from explicit cations.
3. Hybrid explicit/implicit descriptions of water lead to deviations in interfacial capacitance from experimental values and unphysical spilling of continuum counter-charge into Ångström-sized regions between explicit solvent molecules.
4. Constant potential reaction energetics are determined under the assumption that ion and solvent reorganization follow adiabatically the atomic motion associated with a reaction event. While this charging response gives rise to constant potential conditions, it also leads to variations in surface charge density and electric field along the reaction pathway.

## 2. THEORETICAL METHODS AND MODEL DETAILS

The results presented in this work are based on density functional theory (DFT) calculations performed with the Vienna *ab initio* Simulation Package<sup>59–61</sup> in conjunction with VASPsol,<sup>32,39</sup> but the conclusions presented herein are generally not specific to this implementation. Core electrons of each atom were modeled with projector augmented wave pseudopotentials,<sup>62</sup> while valence electrons were expanded as plane-waves up to a kinetic energy cutoff of 500 eV. When optimizing bulk platinum, the Brillouin zone was sampled with a 12 × 12 × 12  $\Gamma$ -centered Monkhorst–Pack<sup>63</sup> k-point grid, with valence electrons described by a plane-wave expansion up to 500 eV. Exchange and correlation interactions were accounted for using the RPBE functional for the CO<sub>2</sub> data<sup>64</sup> and the PBE functional for the Volmer data.<sup>65</sup> The accuracy of predicted solvation effects depends on the functional which was used to parametrize the implicit solvation model.<sup>39</sup> However, the transferability of the parameters to RPBE has been demonstrated.<sup>43</sup> RPBE was then chosen for the study of CO<sub>2</sub> adsorption for its improved accuracy in estimating chemisorption energies.<sup>64,66</sup> PBE was chosen for the Volmer study for its more accurate description of water geometries.<sup>67</sup>

We did not include any van der Waals corrections to avoid any possible solvation uncertainties due to the risk of non-transferability of the implicit solvation parameters.

Surface CO<sub>2</sub> calculations were performed on a 4 × 4 supercell, with four layers of surface atoms; the outer two layers were free to relax, while the middle two were constrained to the bulk lattice parameter of  $a = 3.989$  Å. These supercells were symmetric in the z-coordinate to prevent any net dipole interaction. We note that because the continuum solvation screens any net dipole (meaning the use of the dipole correction<sup>68</sup> is unnecessary), using a symmetric cell in the z-coordinate seems to have a negligible effect on the overall reaction energetics, as seen in SI Figure S1. Volmer calculations were performed in a 4 × 3 supercell, with three layers of surface atoms; the uppermost layer was free to relax, and the lower two layers were frozen to the bulk lattice parameter of  $a = 3.967$  Å. This slightly smaller lattice parameter is due to the different exchange-correlation functional used for the Volmer calculations. One explicit bilayer of solvent (8 water molecules) was included.

Geometries were considered optimized when the maximum force on any atom in the system was below 0.03 eV Å<sup>-1</sup>. For each electronic self-consistency cycle, the electronic energy was considered converged when it did not change by more than 10<sup>-4</sup> eV between iterations.

VASPsol treats solvent at the electrochemical interface implicitly (i.e., as a polarizable dielectric continuum described by the isotropic dielectric permittivity function  $\epsilon$ ). The ionic counter charge density  $\rho_{\text{ion}}$  is modeled by the linearized Poisson–Boltzmann (LPB) approach (given in atomic units):<sup>32,39</sup>

$$\rho_{\text{ion}}(\mathbf{x}) = -S(\tilde{\rho}_{\text{el}}(\mathbf{x})) \left( \frac{2c^0(qz)^2}{k_{\text{b}}T} \right) \phi(\mathbf{x}) = -\kappa^2(\tilde{\rho}_{\text{el}}(\mathbf{x}))\phi(\mathbf{x}) \quad (1)$$

where  $c^0$  is the ion concentration in the bulk solvent,  $q$  is the elementary charge,  $z$  the magnitude of the ionic charge,  $k_{\text{b}}$  the Boltzmann constant,  $T$  the temperature, and  $\phi(\mathbf{x})$  the electrostatic potential being the solution of the LPB equation:

$$[\nabla \cdot \{\epsilon(\tilde{\rho}_{\text{el}}(\mathbf{x}))\nabla\}]\phi(\mathbf{x}) = -4\pi(\rho_{\text{el}}(\mathbf{x}) + \rho_{\text{nuc}}(\mathbf{x}) + \rho_{\text{ion}}(\mathbf{x})) \quad (2)$$

$\tilde{\rho}_{\text{el}}(\mathbf{x})$  is the valence electron density plus a Gaussian pseudocore charge density, added at the nuclei to avoid solvent leakage inside of the atoms where the valence charge density can be small.  $\rho_{\text{el}}(\mathbf{x})$  is the valence electron density resulting from Kohn–Sham (KS) DFT, and  $\rho_{\text{nuc}}(\mathbf{x})$  is the nuclear charge density modeled as Gaussians.

To describe the interface between the electrode and electrolyte, both  $\kappa$  (cf. eq 1) and  $\epsilon$  are ramped up from inside the surface to the polarizable continuum by the shape function  $S$ :

$$\epsilon(\tilde{\rho}_{\text{el}}(\mathbf{x})) = 1 + (\epsilon_{\text{b}} - 1)(S(\tilde{\rho}_{\text{el}}(\mathbf{x}))) \quad (3)$$

with

$$S(\tilde{\rho}_{\text{el}}(\mathbf{x})) = \frac{1}{2} \operatorname{erfc} \left[ \frac{\log \left( \frac{\tilde{\rho}_{\text{el}}(\mathbf{x})}{\tilde{\rho}_{\text{el, cut}}} \right)}{\sigma\sqrt{2}} \right] \quad (4)$$

As in many implicit solvation models,<sup>30,33,38</sup> the solute's valence electron density is used to define the dielectric transition from solute ( $\epsilon = 1$ ) to bulk solvent ( $\epsilon = \epsilon_{\text{b}}$ ). Analogously, the ion exclusion function  $\kappa$ , which models ion–solute repulsions, is ramped up from 0 to  $\kappa_{\text{b}}$ , the inverse Debye length. The above functional form of  $S$  gives rise to two parameters determining the solvation and ion effect, an electron density cutoff  $\tilde{\rho}_{\text{el, cut}}$  and a smoothness parameter  $\sigma$ .

Nonelectrostatic contributions to solvation such as cavitation and repulsion are described by adding to the electrostatic KS energy expression the empirical term,<sup>69</sup>

$$A_{\text{cav}} = \tau \int |\nabla S| d^3\mathbf{x} \quad (5)$$

where the integral over the gradient of  $S$  is a representation of the surface area of the solvation cavity, and  $\tau$  can be considered as effective surface tension parameter which describes the nonelectrostatic interactions. Further details on the implementation of this model can be found in references 32 and 39.

To summarize, the ion distribution is determined by the five constants  $\epsilon_{\text{b}}$ ,  $\kappa_{\text{b}}$ ,  $\tilde{\rho}_{\text{el, cut}}$ ,  $\sigma$ , and  $\tau$ . Default parameters for VASPsol are 78.4, 0.0 Å<sup>-1</sup>, 2.5 × 10<sup>-3</sup> Å<sup>-3</sup>, 0.6, and 5.25 × 10<sup>-4</sup> eV Å<sup>-2</sup>, respectively, and were determined through fits to known experimental hydration energies of organic molecules.<sup>39</sup>

In contrast to the case of molecular solutes, where the parametrization against experimentally measured solvation energies has been shown to lead to reliable and transferable models,<sup>30,32–34,53,69–71</sup> this has not yet been proven for the case of extended surface slabs. The default parameters have been shown to give reasonable capacitances and potentials of zero charges (PZCs) on single-crystal transition-metal surfaces.<sup>32,35,39,43,72</sup> We note also that the PZC and surface work functions of metal slabs are linearly correlated,<sup>73</sup> so an accurate PZC prediction may be more reflective of the atomistic description of the metal work function than the description of the electrolyte. Furthermore, it is not clear that a correct description of pure metal surface properties in solution gives transferable estimates of solvation effects and reaction energies of arbitrary adsorbates. Recently, it was shown in implicit models for molecular solvation that ion-specific solute-ion repulsions can be correlated to differences in charge density cutoffs for these functions.<sup>70</sup> Therefore, assuming the availability of accurate experimental reference data, a careful parametrization of density cutoffs may enable modeling ion-specific capacitances on extended surfaces.

Due to the numerical instabilities illustrated in Supporting Information (SI) Figure S2,  $\tau$  is set to 0 for all calculations in this work, except where specified, as has been done in previous studies.<sup>71,74</sup> Table 1 shows the effects of varying  $\epsilon_{\text{b}}$ ,  $\tilde{\rho}_{\text{el, cut}}$ , and  $\tau$  on the overall capacitance ( $C$ ) and PZC, and the corresponding surface charge density vs potential curves used to determine  $C$  and PZC are shown in Figure S3 in the SI. Table 1 shows that the shift from the default value to 0 gives slight shifts in both capacitance and PZC. The effects of the variations in  $\epsilon_{\text{b}}$  and  $\tau$  are discussed further below, and a more complete factorial experiment showing the parameter dependence of PZC is shown in SI Figure S4.

Because of the adsorption of hydrogen and oxygen species, the experimental value for the PZC of Pt(111) has a large uncertainty, with reported values between 0.2 to 1.1 V vs SHE.<sup>75,76</sup> This scatter motivates the development of more reliable theoretical predictions of the PZC. A parity comparison between calculated and experimental reference

**Table 1. Tabulated Capacitances and Potentials of Zero Charge of Pt(111) for Varying Levels of Bulk Dielectric Constant  $\epsilon_b$ , Effective Surface Tension  $\tau$ , and Electron Density Cutoff  $\tilde{\rho}_{el,cut}$ <sup>a</sup>**

$\epsilon_b$	$\tilde{\rho}_{el,cut}/\text{\AA}^{-3}$	$\tau/\text{meV \AA}^{-2}$	$C/\mu\text{F cm}^{-2}$	PZC/V vs SHE
78.4	$2.5 \times 10^{-3}$	0.525	15.1	0.9
78.4	$2.5 \times 10^{-3}$	0.0	13.7	1.0
78.4	$1.0 \times 10^{-6}$	0.0	3.4	1.2
4.0	$2.5 \times 10^{-3}$	0.525	5.7	1.0
4.0	$2.5 \times 10^{-3}$	0.0	5.4	1.1
4.0	$1.0 \times 10^{-6}$	0.0	2.7	1.2

<sup>a</sup>In all cases,  $\sigma = 6.0$ , and  $\kappa_b = \frac{1}{3}\text{\AA}^{-1}$ . Row 1 shows the results for the default parameters.

values for various transition metals<sup>75,76</sup> is shown in SI Figure S5.

Reaction energies at constant electrode potential were calculated using an implementation similar to the method of ref 43. The electrode potential is given by eq 6.<sup>31</sup>

$$U_{\text{SHE}}(n) = \frac{-\epsilon_F(n) - \phi_{\text{SHE}}}{e} \quad (6)$$

Here  $\phi_{\text{SHE}}$  is the work function of the Standard Hydrogen Electrode, determined experimentally to be 4.4 eV,<sup>77</sup> and  $\epsilon_F$  is the Fermi energy of the slab relative to vacuum. A fixed-point iteration scheme was added to the KS DFT self-consistent field scheme, where the number of electrons  $n$  in the system was varied to reach the desired  $U_{\text{SHE}}$ . Using Newton's Method, we minimize  $\tilde{U}_{\text{SHE}}(n)$ ,

$$\min_n \tilde{U}_{\text{SHE}}(n) = \min_n |U_{\text{SHE}}(n) - U_{\text{des}}| \quad (7)$$

where  $U_{\text{SHE}}(n)$  is the electrode potential at  $n$  electrons, and  $U_{\text{des}}$  the desired potential.

In practice, Newton's Method generally takes only three SCF cycles to converge to the correct charge, since  $\epsilon_F$  depends approximately linearly on  $n$ . The optimization of  $n$  is followed by a geometry optimization step. This process repeated until

both the geometry is optimized to the aforementioned criteria and the potential is within 0.02 V of the desired potential.

The grand-canonical free energy of a reaction is obtained by accounting for the electronic and ionic reservoir energies being in exchange with the modeled system,<sup>43</sup>

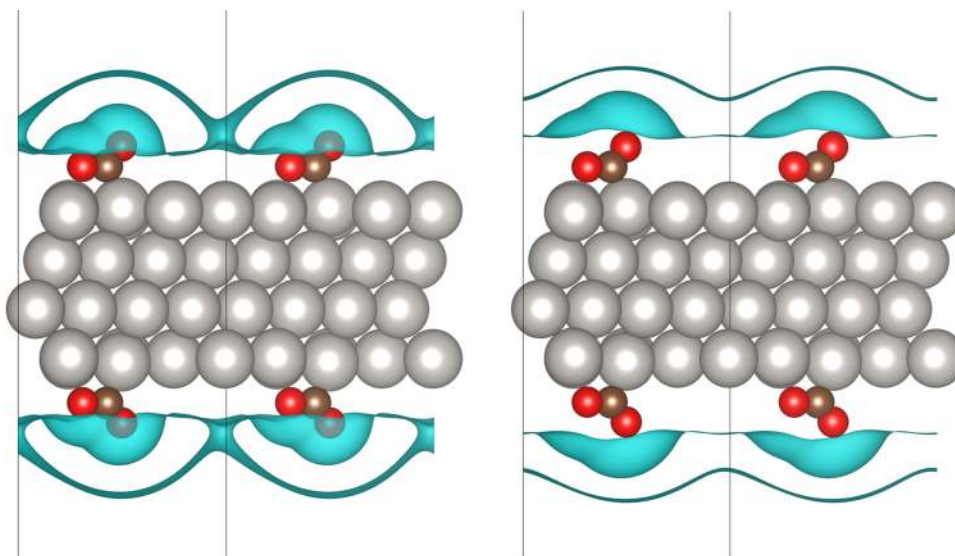
$$\Delta\Omega = \Delta G - \mu_{e^-}(N_{e^-}^{\text{FS}} - N_{e^-}^{\text{IS}}) \quad (8)$$

Here,  $\Delta G$  represents the change in Gibbs free energy required for an unsolvated  $\text{CO}_2$  molecule to adsorb to a charged, solvated surface, containing the typical vibrational and zero point energies. The free energy of the reference reservoir of electrons,  $\mu_{e^-}$ , is taken to be the Fermi energy corresponding to the desired potential and  $N_{e^-}^{\text{FS}}$  and  $N_{e^-}^{\text{IS}}$  denote the total number of electrons in the final and initial state, respectively.

We examined the convergence of the adsorption energy of  $\text{CO}_2$  on Pt(111) with respect to the separation between periodic slabs, as illustrated in SI Figure S6. We note that, due to the extent of the ion distribution, a separation between slabs of at least 50  $\text{\AA}$  is required to obtain adsorption energies within 0.1 eV of the infinite vacuum limit using default parameters. This issue seems to be related to long-range interactions between the repeated slabs, where we found the adsorption energy to follow a nearly perfect inverse cell volume dependence (cf. SI Figure S5). This decay length is proportional to the Debye length, meaning that for larger Debye lengths, even larger vacuum separations are necessary, as was found in ref 44. Despite the applicability of the linearized Poisson–Boltzmann equation to a very limited region near the PZC, such a model has been widely applied to study electrochemical reactions within potential ranges of  $\pm 0.5$  V, which we investigate in this work.

### 3. RESULTS AND DISCUSSION

Here we discuss several challenges identified with the use of LPB/PCM for understanding electrochemical reaction energetics. We first discuss those associated with physical description of the solvent and ion distribution, followed by those related to the determination of reaction energetics under constant potential.



**Figure 1.** Ionic countercharge density isosurfaces of  $2 \times 10^{-3} \text{ e\AA}^{-3}$  for  $\text{CO}_2$  adsorbed on Pt(111) in a  $2 \times 4$  supercell. Left: Default  $\tilde{\rho}_{el,cut} = 2.5 \times 10^{-3} \text{ e\AA}^{-3}$ . Right: Lowered  $\tilde{\rho}_{el,cut} = 1.0 \times 10^{-6} \text{ e\AA}^{-3}$ .

### 3.1. Description of the Solvent and the Ion Distribution.

**3.1.1. Ionic Countercharge Placement.** The LPB/PCM model as introduced above applies the same ramping function for ionic charge density and permittivity. Using default parameters and a Debye length of 3 Å, this leads to ions being placed unphysically close to the metal surface. The reason for this is a nonoptimal parametrization of the ionic shape function using the same cutoff parameter as for the dielectric ramping. In reality, ions are separated from the electrode by an effective hydration shell and physisorbed water, an effect that can be modeled by shifting the onset of the ion distribution further away from the surface.<sup>70</sup>

Figure 1 (left) illustrates a counter-charge density isosurface of  $2 \times 10^{-3} \text{ e}\text{\AA}^{-3}$  (corresponding to a value near the maximum density) on a  $\text{*CO}_2 \mid \text{Pt}(111)$  system using the default  $\tilde{\rho}_{\text{el,cut}}$ . Here the counter-charge is placed within 2 Å of the surface. Explicit solvent simulations suggest cations to be placed roughly 3–5 Å from the surface,<sup>6,78</sup> due to the size of the solvation shells of the ions. By adjusting  $\tilde{\rho}_{\text{el,cut}}$  from the default value of  $2.5 \times 10^{-3} \text{ \AA}^{-3}$  to the much lower value of  $1.0 \times 10^{-6} \text{ \AA}^{-3}$ , we can move the counter-charge density to a more physical location, as seen in Figure 1 (right), with almost enough room for an explicit water layer. The isosurface being multivalued in the z-coordinate arises from the rapid rise and subsequent decay of ion concentration moving away from the surface.

However, when the countercharge density is pushed away, the model's ability to predict the capacitance of Pt(111) is lost. As shown in Table 1 (and SI Figure S4), we observe a significant decrease (from  $13.7 \mu\text{F cm}^{-2}$  to  $3.4 \mu\text{F cm}^{-2}$ ) in the predicted capacitance relative to the capacitance reported in the model reference,<sup>32,39</sup> and significantly lower than experimentally determined.<sup>79</sup> The sensitivity of the capacitance to  $\tilde{\rho}_{\text{el,cut}}$  is in-line with the explorations on the Li | PCM interface reported in ref 80. We note that the most physical way to correct for this would be the introduction of an ion-free Stern layer, which can be achieved by ramping up the dielectric and ionic charge density functions at different density cutoffs.<sup>70</sup>

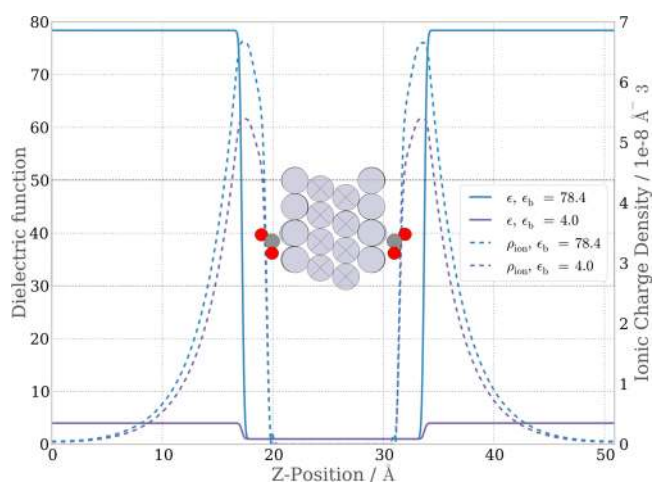
**3.1.2. Ramping of the Dielectric Function.** In most PCM models,<sup>30,33,38</sup> the dielectric function transition from the solute to the electrolyte is parametrized and fit (e.g., through least-squares) to reproduce neutral molecular solvation energies. However, its transferability to extended charged metal surfaces has not been investigated.

At the electrochemical interface, the metal–water interaction results in at least one ice-like bilayer of water on metal surfaces which extends 3–5 Å from the surface. This bilayer has been observed both experimentally in UHV<sup>81</sup> and theoretically on Pt(111).<sup>82–84</sup> When a potential is applied and a strong electric field is present, there is further ordering of the bilayer, which reduces the translational and rotational degrees of freedom of water.<sup>85,86</sup> Therefore, water near the electrochemical interface has a significantly lower dielectric constant relative to the bulk.<sup>87–89</sup> Such effects are not accounted for with an isotropic dielectric function that is optimized for molecular systems, even if they are charged.<sup>90</sup> Bonthuis and Netz evaluated the dielectric tensor at different interfaces by classical molecular dynamics simulations.<sup>91,92</sup> They found that constraining water close to interfaces results in a late transition of the perpendicular component of the dielectric permittivity to the bulk value at around 6–8 Å while the parallel component reaches its bulk limit within 2–4 Å. By constructing narrow channels, Fumagalli et al. measured the

out-of-plane dielectric constant of water to ramp from 2 at a thickness of 10 Å up to the bulk dielectric constant of 78.4 at channel widths of over 100 nm,<sup>93</sup> and find that this result holds regardless of the hydrophilicity of the surface.

These findings motivate the development of more advanced PCMs for interfaces that account for the two major dielectric tensor components in order to correctly describe ice-like water layers. In terms of an isotropic dielectric function as implemented in VASPsol and other commonly used PCMs, one can in principle effectively mitigate such effects by ramping up the dielectric function over a larger distance from metal to the bulk solvent or by simply adjusting the bulk permittivity to which the dielectric function ramps. Electric double layer field effects on electrochemical reaction kinetics are commonly dominated by the vertical component of the field on the surface<sup>12,94</sup> which suggests that a correct description of the parallel component of the dielectric tensor might be less significant. This procedure would, however, still require a careful parametrization of the perpendicular dielectric component. Comparison of calculated reaction rates from microkinetic modeling with experimental current densities may provide one way to parametrize the appropriate dielectric ramping function, since as we will discuss later, the dielectric ramping function has a strong effect on energetics.

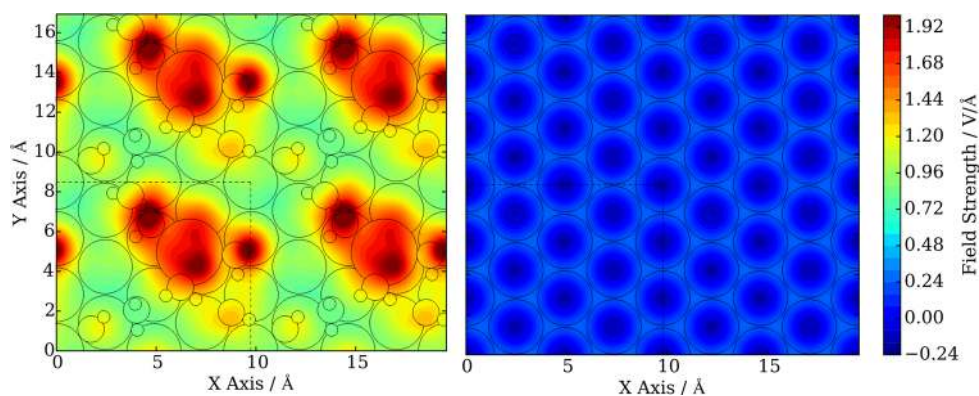
Figure 2 shows variation of the dielectric permittivity and  $xy$ -averaged ionic charge density for two values of  $\epsilon_b$ : 78.4



**Figure 2.** Increase of the  $xy$ -plane averaged dielectric function away from the surface for two values of  $\epsilon_b$ , and decay of the  $xy$ -plane averaged  $\rho_{\text{ion}}$  for the same two bulk dielectric permittivities at a fixed potential of 1.15 V vs SHE.

(corresponding to bulk water) and 4.0 (representing constrained water) at 1.15 V vs SHE. The figure shows that this ramping of  $\epsilon$  with the default parameters is too fast; we find that  $\epsilon$  reaches the bulk limit within 3–4 Å of the surface, which is well within the first water bilayer. This rate of ramping is faster than the experimental<sup>95</sup> and theoretical investigations.<sup>89,96</sup>

We also note that here, as illustrated by Figure 1, the ionic charge is unphysically close to the metal slab and a significant proportion lies in the region of vacuum permittivity. This charge placement gives rise to a relatively constant capacitance as a function of potential in these model systems. However, it arises from charge distributed unphysically close to the



**Figure 3.** Left: Field distribution on Pt(111) with explicit solvent molecules and a solvated sodium ion. Right: Field distribution on Pt(111) with implicit solvation, charged to have the same work function as in the left panel. Dotted lines mark the boundaries of the unit cell.

interface where the dielectric constant  $\sim 1$ , corresponding to that of vacuum.<sup>73,97,98</sup>

Since a decrease of the bulk permittivity would lead to an underestimation of the bulk solvent response to charged surfaces, a slow ramping of the dielectric function may be the more reliable approach. Unfortunately, however, using  $\sigma$  higher than the default parameter exhibits significant numerical instabilities. Further, while the ramping is indeed slower for larger  $\sigma$ , the onset of ramping is also moved closer to the slab, which in fact worsens the problem. These issues with  $\sigma$  are illustrated in SI Figure S7 and motivate the development of new dielectric function models particularly adjusted for solid–liquid interfaces.

We therefore focus our discussion on the impact of a decreased  $\epsilon_b$ . As shown in Table 1 and SI Figure S4, the associated capacitance is lowered from 13.7 to 5.4  $\mu\text{F cm}^{-2}$ . The decrease in capacitance from lowering the bulk dielectric constant synergizes with the decrease from pushing the countercharge density away from the surface; with both modifications made, the predicted capacitance drops to about 2.7  $\mu\text{F cm}^{-2}$ , which is about an order of magnitude lower than experimental capacitances. We also observe that the PZC of Pt(111) varies by about 0.3 V in changing these parameters. The sensitivity of the capacitance and PZC have also been reported in ref 80 for the Li | PCM interface, and is illustrated in SI Figures S3 and S4. We note that the capacitances reported here are not unphysical, despite this model applying Gouy–Chapman theory at large concentrations (a Debye length of 3.0 Å corresponds to a bulk ion concentration of roughly 1.0 M). The primary reason for this is, as illustrated by Figure 2, the dielectric ramping region acts as an effective Stern layer, where there is charge separation across a region of relatively low dielectric constant. This can also be observed in SI Figure S8, where increasing the Debye length (which affects the double-layer capacitance but not the Helmholtz capacitance), does not significantly change the overall capacitance until the Debye length is made quite large.

**3.1.3. Electric Field Distribution.** The continuum description of ionic charge, using the default parameters, provides a very different field distribution from an explicit picture. Continuum models are by construction not made for reproducing properties of single electrolyte configurations but for calculating thermodynamically averaged properties. Faradaic reactions at charged electrode surfaces, however, can be driven strong local fields that do not appear in the thermodynamically averaged ion distribution.<sup>12</sup> The impor-

tance of ion-induced field stabilization has been investigated for several important electrochemical reactions, including the oxygen reduction reaction (ORR)<sup>94</sup> and CO<sub>2</sub> reduction.<sup>12</sup> The effect of including explicit ions in addition to a continuum description of the solvation and ionic charge is being studied currently, and offers one potential solution to this problem.

Figure 3 compares the field at a distance of 3 Å from the surface associated with an explicit Na<sup>+</sup> ion solvated by explicit waters (left) vs the LPB/PCM description at the same work function of 4.5 eV (right). This distance is associated with that of the carbon atom in CO<sub>2</sub> adsorbed on the surface. In the case of explicit solvent, the local field variation was calculated by the following expression:<sup>12</sup>

$$E_{\text{field}} = -\frac{dV_{\text{diff}}}{dz} \quad (9)$$

with

$$V_{\text{diff}} = V_{\text{total}} - V_{\text{electrolyte}} - V_{\text{slab}} \quad (10)$$

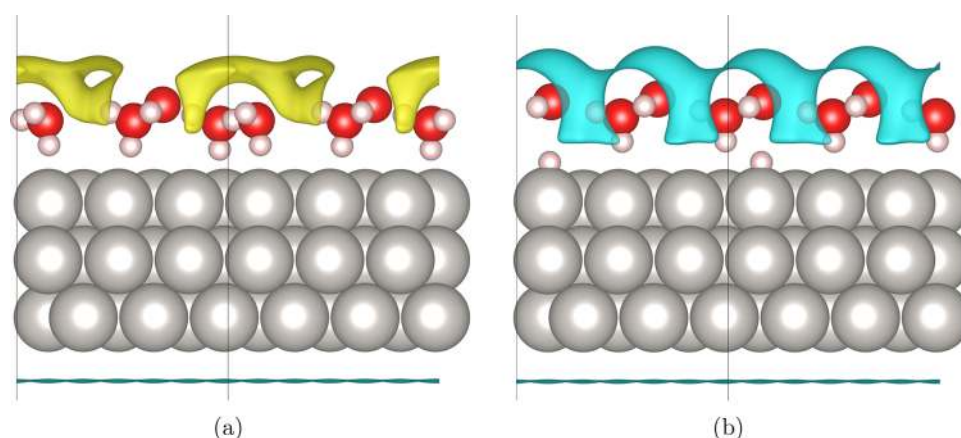
Here  $V_{\text{total}}$  is the ionic and Hartree potential of the total system (slab and explicit electrolyte),  $V_{\text{electrolyte}}$  is the ionic and Hartree potential of the electrolyte (with no slab), and  $V_{\text{slab}}$  is the ionic and Hartree potential of the slab (with no electrolyte).

In the case of implicit solvation, the field is calculated by eq 9, but with  $V_{\text{diff}}$  calculated instead as

$$V_{\text{diff}} = V_{\text{charged}} - V_{\text{uncharged}} \quad (11)$$

Here,  $V_{\text{charged}}$  refers to the potential of the charged surface, including the potential due to counterions, of the Pt(111) surface, and  $V_{\text{uncharged}}$  refers to the potential of the uncharged (but solvated) Pt(111) surface. Because the ions are placed very close to the surface, this field increases rapidly and then quickly decays to 0 about 1 Å from the surface. For sampling the field strength, we choose the  $z$  position to be between carbon and oxygen on adsorbed CO<sub>2</sub>.

As can be seen, there are stark differences in the field distributions in the two models. A LPB/PCM model obviously cannot capture the variation of the electric field in the  $xy$  plane associated with an explicit cation and the associated effects on the energetics of reaction intermediates. The LPB/PCM field is also significantly smaller, which arises from the placement of continuum charge extremely close to the surface (Figure 2) and the corresponding fast decay of the field along  $z$ . This could lead to an underestimation of local field effects on reaction kinetics.



**Figure 4.** Ionic countercharge density isosurface plot illustrating the charge intercalation into the explicit water layer for the (a) initial (charged) state, and (b) final (uncharged) state. Here the isosurface density value is  $1.4 \times 10^{-4} \text{ e}\text{\AA}^{-3}$ , with yellow representing positive electron density, and blue representing negative electron density. Both the initial and final state are charged to a potential of 0.0 V vs SHE.

**3.1.4. Effects of Explicit Water.** Recent simulations have made use of a hybrid approach which includes a few explicit waters at the metal | PCM interface. These approaches would allow for the explicit solvation of the ions that participate in charge transfer reactions,<sup>43,99</sup> and for a more physical description of charge and dielectric constant at the interface. Here we consider the Volmer reaction to be a proton–electron transfer to the surface, with the initial state being the proton in the inner Helmholtz plane, shown in Figure 4. SI Figure S9 shows the corresponding  $q$  vs  $U$  curves for the initial and final states. We use a static water structure, corresponding to the hexagonal structure observed by Ogasawara and co-workers.<sup>81</sup>

Overall, the introduction of the explicit solvent layer leads to significant deviations in capacitance from experimental values of  $\sim 20 \mu\text{F cm}^{-2}$ .<sup>100</sup> Because of the larger average ion–metal distances introduced by the explicit water (illustrated by the charge density isosurfaces of Figure 4), the capacitances are lowered. At the default  $\epsilon_0$  of 78, the capacitance is  $9.2 \mu\text{F cm}^{-2}$  in the charged (initial) state, and  $9.9 \mu\text{F cm}^{-2}$  in the uncharged (final) state; and at a bulk dielectric constant of 4 it is further decreased  $5.1 \mu\text{F cm}^{-2}$  in the initial state, and  $5.2 \mu\text{F cm}^{-2}$  in the final state. The work published in ref 101 also finds a decreased capacitance when an explicit solvent layer is added to the simulation. They find that the capacitance increases further, to  $27 \mu\text{F cm}^{-2}$  with an additional bilayer of explicit solvent. However, we find this actually decreases the capacitance, to about  $6.3 \mu\text{F cm}^{-2}$ , shown in SI Figure S10.

We note also that, under default model parameters, the continuum charge unphysically enters the spaces within the explicit hexagonal water structure, as illustrated in Figure 4. This mixture of implicit and explicit models within the Helmholtz plane may also yield unintended effects on reaction energetics of interest.

Overall, careful parametrization, and perhaps a modification to the model to prevent ion intercalation into the explicit region, would therefore be necessary in order to obtain a more physical model and to obtain agreement with experimental capacitances.

**3.2. Constant Potential Simulations.** A major challenge associated with ab initio simulations of electrochemical activation energies in fully explicit model systems is that the simulations operate at a constant number of electrons, while physical systems operate at constant potential. This issue can be mitigated in large cell calculations that mimic the physical

system<sup>102</sup> or in extrapolation schemes to the large cell limit based on simple capacitor models of the interface, illustrated in SI Figure S11.<sup>20,58</sup>

PB continuum models provide a way to keep the potential constant by varying the surface and electrolyte charge density. This allows to compensate for the continuous shifts in interface dipoles being associated with work function shifts during an electrochemical reaction process. In such calculations, intermediate images between the initial and final state are created, and a transition state search is performed using methods such as the dimer method<sup>103</sup> and the nudged elastic band (NEB).<sup>104,105</sup> The electronic and continuum ionic charge of the images are varied such that the entire reaction pathway is fixed at a given potential. This approach has been applied in a number of recent mechanistic studies.<sup>42,43,99,106,107</sup>

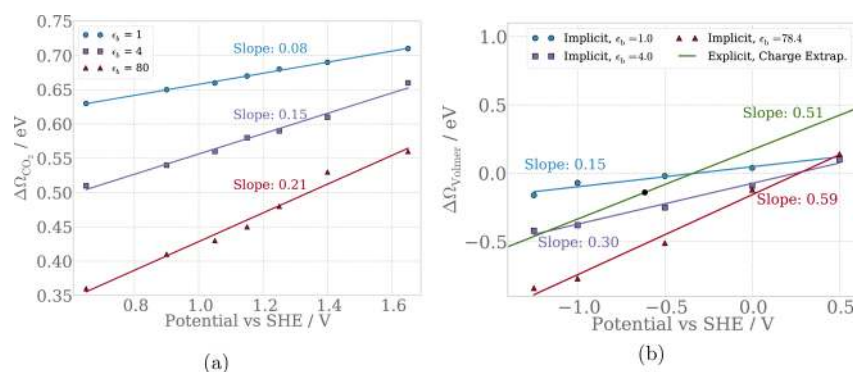
**3.2.1. Kinetics and Timescales.** A fundamental challenge with the physical picture of LPB/PCM schemes for electrochemical activation barriers at constant potential is the assumption that ions follow adiabatically the atomic motion associated with the electrochemical reactions. However, the atomic motion associated with reaction events occurs on much faster timescales than solvent reorganization and ionic diffusion. The physical movement of atoms during a proton transfer is on the order of femtoseconds, while ion rearrangement occurs on the order of pico- to nanoseconds.<sup>108</sup> Indeed, the classical theories of electron transfer such as outer-sphere Marcus theory predict that electron transfer proceeds diabatically, with no solvent reorganization.<sup>109,110</sup> This was more recently extended to proton transfer theory, where rate constants for a wide variety of PCET reactions were predicted with good agreement to experimental measurements.<sup>111</sup>

We estimate the timescales for ion rearrangement as follows. Table 2 shows the experimentally determined<sup>112</sup> ion mobilities

**Table 2.** Experimentally Determined<sup>112,117</sup> Ion Mobilities for Common Ions at 298 K

ion	mobility/ $10^{-8} \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$	$D/10^{-9} \text{ m}^2 \text{ s}^{-1}$	time/ps
$\text{Na}^+$	5.19	1.34	17
$\text{K}^+$	7.62	1.97	11
$\text{Cl}^-$	7.91	2.05	11
$\text{OH}^-$	20.64	5.34	4
$\text{H}^+$	36.23	9.37	2





**Figure 5.** Potential dependence of (a) CO<sub>2</sub> adsorption and (b) Volmer reaction on Pt(111) at varying bulk solvent dielectric constant  $\epsilon_b$ , compared to an explicitly calculated  $\Delta G$  via charge extrapolation.<sup>20,58</sup>

in aqueous media. To convert these mobilities into a diffusion constant, we use the Einstein relation<sup>113</sup>

$$D = \frac{\mu_q k_B T}{q} \quad (12)$$

where  $\mu_q$  is the electrical ion mobility,  $k_B$  the Boltzmann constant and  $q$  the charge of the ion. From  $D$ , one can arrive at a characteristic time for the ion to diffuse over a length scale with the following expression:<sup>114</sup>

$$t = \frac{L^2}{4D} \quad (13)$$

Here  $t$  is the characteristic diffusion time,  $L$  is a length scale.

Assuming the Debye length of 3 Å as a lower bound estimate of the length scale for the double layer response to charging the surface, we obtain an estimated time of 17 ps for Na<sup>+</sup> rearrangement using eq 13. The estimates for various other ions are shown in Table 2, and they all fall within the same order of magnitude. Previous work using Brownian dynamics simulations has also shown that it takes on the order of 1 ns for the electrochemical double layer to relax.<sup>115</sup> All these timescale estimates together suggest that the relaxation of the double layer is significantly slower than the femtosecond timescale of atomic motion during a reaction event. The timescales of reaction rates are also significantly longer than that for a given reaction event. On Pt in acidic solutions, the timescale of the hydrogen evolution, obtained from Arrhenius plots, is between 5 and 200 ps at low overpotentials (below 60 mV).<sup>116</sup> Reaction events are therefore exceedingly rare, and this element is captured through large cell calculations or through the extrapolation schemes discussed above.<sup>58</sup> Ionic motion should hence not be assumed to follow adiabatically the motion associated with reaction events.

**3.2.2. Energetics and Field Variations.** In addition to the fundamental challenge of timescales, we discuss two further technical challenges associated with PCMs of reaction activation energies. First, the energetics, like the interfacial capacitance and PZC, are sensitive to parametrization, and uncertainties in the parametrization translates to uncertainties in the energetics. As discussed above, a lowered  $\epsilon_b$  from the bulk value of 78 and an increased  $\tilde{\rho}_{el,cut}$  from the default value would give a more realistic description of the dielectric constant and the position of ions in the interface region, respectively. The effect of the dielectric constant ( $\epsilon_b = 78.4, 4.0,$  and  $1.0$ ) on the (a) CO<sub>2</sub> adsorption energy and (b) Volmer reaction energy as a function of potential are shown in

Figure 5. The Volmer reaction Gibbs free energy using a fully explicit approach, with extrapolation to the constant potential limit,<sup>20,58</sup> is also shown for comparison, and deviates from the implicit values, which can be attributed to the number of challenges discussed above.

Finally, while continuous charging of the interface allows for the calculation of reaction energetics at a constant potential, the corresponding surface charge density and electric field varies along the reaction path due to the charging response to the shift in interface dipole. Figure S9 (a) in the SI shows that the  $q$  at a fixed potential varies by about 0.4 electrons between IS and FS for CO<sub>2</sub> adsorption in a  $4 \times 4$  supercell, and by 0.6 electrons between the IS and FS the Volmer reaction in a  $4 \times 3$  supercell. In the limit where  $q$  is distributed uniformly, e.g. in a parallel plate capacitor, these shifts correspond to a shift in  $E_{field}$  of  $1.2 \text{ V \AA}^{-1}$  and  $1.3 \text{ V \AA}^{-1}$  for CO<sub>2</sub> adsorption and Volmer, respectively. These variations in field would impact the energetics of polar adsorbates, or explicit waters applied in hybrid explicit-implicit models, and likely contribute to the difference observed between the infinite cell limit (extrapolated) and LPB-PCM calculations observed in Figure 5b. It may be possible to correct for these effects; this is the focus of future work.

## 4. CONCLUSIONS AND OUTLOOK

Modern electronic structure theory consists of a hierarchy of approximate computational models that introduce trade offs between accuracy and computational feasibility, as exemplified by the five rungs on Perdew's Jacob's ladder classification.<sup>118</sup> The challenge of modeling the solid–liquid electrode–electrolyte interface in electrocatalysis invites the development of a similar range of models. The formally exact treatment, fully molecular, and grand-canonical in both electrons and electrolyte ions, is a challenge that lies beyond present-day computing resources if one is to obtain converged statistical sampling. There is therefore a computational necessity to also consider simpler models in order to model electrocatalysis today. One might roughly group such models into four groups: (1) Bias-free and electrolyte free modeling, as exemplified by early studies using the computational hydrogen electrode (CHE).<sup>56,119–123</sup> This approach captures the leading thermodynamic effects of applied bias, but neglects all bias and electrolyte induced changes in the electronic structure. (2) Bias-free, fully explicit solvation models, illustrated by many thermodynamic studies of electrochemical reactions using the CHE.<sup>12,17,102,124,125</sup> (3) Fully explicit solvent models, which rely on the CHE and extrapolation methods to obtain

potential-dependent reaction energetics. Because of constraints in computing time, rigorous statistical sampling is a challenge.<sup>16,20,57,58,126</sup> (4) Fully implicit electrolyte with applied bias, treated by linearized Poisson–Boltzmann/polarizable continuum models (LPB-PCM).<sup>30,32,34,37,40,42,43,71,74</sup> This mixed atomistic-continuum approach captures changes in electronic structure of surface species and interactions with the charged electrode to permit bias-dependent calculations, but neglects specific molecular solvent and electrolyte ion effects. We have carefully examined the challenges of the LPB-PCM in this Perspective.

LPB-PCMs provide a computationally inexpensive way to model the electrochemical interface, but come with a number of open challenges. Since ions are assumed to have no finite size, the ionic charge density is placed too close to the surface. Additionally, the dielectric constant increases to the bulk limit too quickly. These issues can be mitigated by modifying the charge density cutoff  $\tilde{\rho}_{\text{el,cut}}$  or the bulk dielectric constant, respectively. Both of these adjustments, while improving the solvent physics, render the LPB/PCM unable to reproduce experimental capacitances. LPB/PCM also necessarily smears out the ion density across the entire electrolyte and therefore gives essentially uniform fields, which may not capture the effect of localized field variations associated with explicit cations on reaction energetics. Further, the inclusion of a layer of explicit solvent, which can provide a more realistic solvation of the ions at the interface, can at the same time lead to unphysical placement of ionic countercharge and deviations of the interfacial capacitance from experimental values.

The determination of electrochemical reaction energetics using LPB/PCM also poses several challenges. LPB/PCM schemes allow for constant potential calculations through continuous variations in surface charge along with interface dipole shifts. The primary challenge with such an approach is the assumption that the double layer charging response follows adiabatically the atomic motion of reaction events, even though the former occurs at a significantly slower timescale. We also find reaction energetics to be sensitive to parametrization such that uncertainties in the parameters translate to uncertainties in energetics. Finally, while the charging of the interface gives rise to constant potential conditions, it also gives rise to variations in electric fields along the reaction pathway.

A modified Poisson–Boltzmann approach to modeling the electrochemical reaction energetics would mitigate some of the aforementioned issues, but not all. In particular, the countercharge placement and dielectric function behavior could be mitigated by the inclusion of a Stern layer, as has been implemented<sup>30,70</sup> for the FHI-aims code. However, this modification would not solve the localization of the field due to ions, and furthermore all continuum models will face challenges in the calculation of electrochemical barriers. The continuum model may still be useful in evaluating the charging response of systems of interest or find practical application in the problem of band misalignment of water<sup>24</sup> found in explicit solvent electrochemical barrier calculations. It is also quite possible that a hybrid approach, where solvent molecules are modeled by a continuum, but the work function is modified by explicitly solvated ions, could be used. This would mitigate the need to determine thermodynamically averaged water structures at the interface. This approach would also avoid the problems associated with the classical treatment of the countercharge and the intrinsic locality of the field, but retain

the ability of the continuum model to handle solvation energies.

## ■ ASSOCIATED CONTENT

### Supporting Information

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Figures and tables referenced in the text; tables of all data required to reproduce the figures in this work (PDF)

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### Notes

The authors declare no competing financial interest.

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