# Characterization of the Propagation Properties of the Half-Mode Substrate Integrated Waveguide

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Abstract—The propagation properties of the half-mode substrate integrated waveguide (HMSIW) are studied theoretically and experimentally in this paper. Two equivalent models of the HMSIW are introduced. With the first model, equations are derived to approximate the field distribution inside and outside the HMSIW. Using the second model, an approximate closed-form expression is deduced for calculating the equivalent width of an HMSIW that takes into account the effect of the fringing fields. The obtained design formulas are validated by simulations and experiments. Furthermore, the attenuation characteristics of the HMSIW are studied using the multiline method in the frequency range of 20-60 GHz. A numerical investigation is carried out to distinguish between the contributions of the conductive, dielectric, and radiation losses. As a validation, the measured attenuation constant of a fabricated HMSIW prototype is presented and compared with that of a microstrip (MS) line and a substrate integrated waveguide (SIW). The SIW is designed with the same cutoff frequency and fabricated on the same substrate as the HMSIW. The experimental results show that the HMSIW can be less lossy than the MS line and the SIW at frequencies above 40 GHz.

Index Terms—Half-mode substrate integrated waveguide (HMSIW), propagation properties.

#### I. INTRODUCTION

RECTANGULAR waveguides are widely used in many microwave and millimeter-wave systems because of their high performance in terms of quality factor and power-handling capacity. However, the integration of these 3-D devices with planar circuits is difficult due to their high profile. As a solution to this problem, some integrated waveguides, such as the substrate integrated waveguide (SIW) [1], post-wall waveguide [2], and laminated waveguide [3] have been proposed. While main-

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taining the advantageous characteristics of conventional rectangular waveguides, these integrated waveguides present additional advantages of low profile and low cost, which confer them a prospect of wide application in integrated circuits. In fact, during the recent years, the propagation properties of the SIW have been studied extensively [4]-[7] and a number of high-performance planar components have been developed based on SIW structures [8]-[12]. However, for many practical applications, the SIW is still too wide. Aiming at a further reduction of the transverse size of the SIW, the concept and geometry of a folded substrate integrated waveguide (FSIW) was introduced in [13] and exploited to develop components such as filters [14]. Recently, approximate formulas were proposed for the FSIW design and for the calculation of its phase constant in [15]. Nevertheless, a close consideration of the structure of the FSIW indicates that its fabrication is rather complicated and costly since it consists of three metallic layers. Additionally, compared with the SIW, the total metallic surface area enclosing the fields (considering the top, middle, and bottom layers) is not reduced. As a result, the FSIW encounters ohmic losses at the same level as the SIW in the millimeter-wave band.

The concept of the half-mode substrate integrated waveguide (HMSIW) was proposed recently in [16] and its geometry is depicted in Fig. 1(a) and (b). It can be observed, on one hand, that both the waveguide width and the surface area of the metallic sheets are reduced by nearly half compared with the SIW, and on the other hand, that the fabrication complexity is maintained at the same level as for the SIW. Several components have been developed based on the HMSIW since its introduction [17]–[20]. However, as one of the most important aspects for a transmission line, the propagation properties of the HMSIW still have not been studied systematically.

The focus of this study includes the determination of the field distribution inside and outside the HMSIW, the calculation of the phase constant, and the characterization of the attenuation. In Section II, approximate equations for the field distribution and a set of explicit design formulas are derived according to two equivalent models of the HMSIW. Subsequently, in Section III, the conductive, dielectric, and radiation losses in the HMSIW are distinguished by utilizing a numerical analysis procedure. Finally, the attenuation of a fabricated HMSIW is measured and compared with that of both a SIW and a microstrip (MS) line in the frequency range of 20–60 GHz.

# II. MODAL ANALYSIS AND DESIGN EQUATION

For the investigation on the field modes and the propagation constant of the HMSIW, two prototypes are created in the configuration depicted in Fig. 1(a) and simulated using the simula-

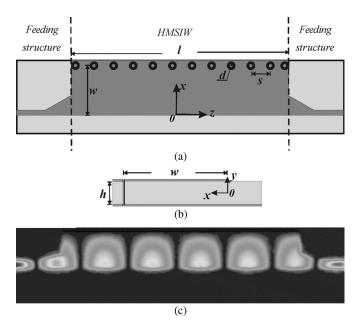


Fig. 1. (a) Top view of the configuration of an HMSIW fed by an MS line. The substrate is shown as light grey, and the dark grey areas are metallized. The metal posts (vias) are shown as circles. (b) Side view of the configuration of the HMSIW. (c) Instantaneous electric field distribution of the quasi- $TE_{0.5,0}$  mode in the H-plane at 10 GHz.

tion tools Ansoft High Frequency Structure Simulator (HFSS) and CST Microwave Studio. The first prototype is designed for operation in the X-band and has a width of  $w=10~\mathrm{mm}$  and a height of  $h=0.508~\mathrm{mm}$ . The second HMSIW prototype is designed for the frequency range of 20–60 GHz and has a width of  $w=2.5~\mathrm{mm}$  and a height of  $h=0.254~\mathrm{mm}$ . Both prototypes are built on a Duroid substrate with a permittivity of 2.2 and a loss tangent of 0.001. The vias in both prototypes share a common diameter  $d=0.5~\mathrm{mm}$ , as well as a spacing  $s=0.6~\mathrm{mm}$ .

Due to the large ratio of HMSIW width to height and the discrete arrangement of the metallic vias, only the quasi- $TE_{p=0.5,0}$  ( $p=1,2,\ldots$ ) modes can propagate in the HMSIW. The H-plane electric field distribution corresponding to the fundamental quasi- $TE_{0.5,0}$  mode is plotted in Fig. 1(c). It can be observed that the fundamental mode in the HMSIW is quite similar to half of the dominant quasi- $TE_{10}$  mode in the SIW. This explains the mode nomenclature with index 0.5 and the origin of the denomination for the *half-mode* SIW.

# A. First Equivalent Model: Field Distribution in the HMSIW

Simulating the HMSIW prototypes in CST yields the distribution of the normalized electric field component  $E_y$  in cross section, as illustrated in Fig. 2. The plot shows that the y-component of the electric field can be approximated as a quarter-cosinusoid in the HMSIW (0 < x/w < 1) and decays rapidly beyond the open side of the waveguide (x/w < 0).

A first equivalent model, as shown in Fig. 3, is proposed for the analytical determination of the fields inside and outside the HMSIW. This model is composed of a leaky-wave guide in a homogeneous medium with a permittivity of  $\varepsilon_{0,\rm eff}$ . The leaky-wave guide shares a common structure and dielectric material with the original HMSIW, whereas the homogeneous surrounding medium is used to equivalently represent the effects of

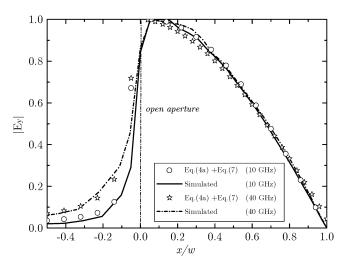


Fig. 2. Normalized electric field in cross section for two HMSIW prototypes operating in X- and Ka-band, respectively.

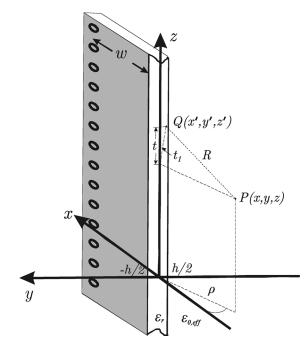


Fig. 3. First equivalent model of the HMSIW and the corresponding coordinates for the calculation of the field distribution.

the substrate, ground plane, and free space outside the HMSIW. The value of  $\varepsilon_{0,\mathrm{eff}}$  lies, therefore, in between the permittivity of free space  $\varepsilon_0$  and that of the substrate material  $\varepsilon_r$ . For an HMSIW made of thin substrate extending past the open aperture, the value of  $\varepsilon_{0,\mathrm{eff}}$  is close to  $\varepsilon_0$ . The fields in the leaky-wave guide and in the homogeneous medium correspond to those inside and outside the HMSIW, respectively.

According to the simulated electric field distribution inside the HMSIW (0 < x/w < 1), as given in Fig. 2, the function  $\psi$  in the electric vector potential  $\vec{F} = \vec{a}_z \psi$  is assumed in the following form for the quasi-TE<sub>p=0.5,0</sub> ( $p = 1, 2, \ldots$ ) modes

$$\psi_{p-0.5,q} = A_{p-0.5,q} \cos \left[ k_{x,(p-0.5,q)}(w-x) \right] \times \cos(k_{y,(p-0.5,q)}y) e^{-jk_{z,(p-0.5,q)}z}, \qquad 0 \le x \le w$$
(1)

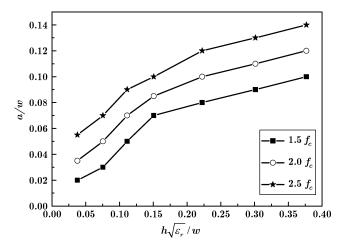


Fig. 4. Dependence of the normalized maximum electric field position a/w on the electric height  $h\sqrt{\varepsilon_T}$  normalized to the HMSIW width w. The curves correspond to results at different frequencies expressed in terms of cutoff frequency  $f_c$ .

in which  $A_{p-0.5,q}$  is a constant, and p and q represent the numbers of extrema of the transverse electric field components in the x- and y-direction, respectively. The parameters  $k_{x,(p-0.5,q)}$ ,  $k_{y,(p-0.5,q)}$ , and  $k_{z,(p-0.5,q)}$  are connected through the separation equation

$$k_{x,(p-0.5,q)}^2 + k_{y,(p-0.5,q)}^2 + k_{z,(p-0.5,q)}^2 = k_0^2 \varepsilon_r$$
 (2)

where  $k_0 = (2\pi f)/c$  is the free-space wavenumber with f being the operation frequency and c being the velocity of light in free space.

Considering that the HMSIW is mainly applied in single-mode operation, the following analysis is restricted to the fundamental quasi- $TE_{0.5,0}$  mode and the subscript (0.5,0) is omitted for simplicity. The corresponding function  $\psi$  is

$$\psi \equiv \psi_{0.5,0} = A\cos k_x (w - x)e^{-jk_z z}, \qquad 0 \le x \le w \quad (3)$$

with

$$k_x = \frac{\pi}{2(w-a)}$$

$$k_y = 0$$

$$k_z = \sqrt{k_0^2 \varepsilon_r - \frac{\pi^2}{4(w-a)^2}}$$

in which the parameter a is the x-coordinate of the position of the maximum electric field along the cross section of the HMSIW. The dependence of the value a/w on the frequency, on the substrate dielectric permittivity  $\varepsilon_r$ , and on the HMSIW width w and height h is demonstrated in Fig. 4. Data in this figure are obtained by simulating a number of HMSIW models of various  $\varepsilon_r \in (2.2,15), h \in (0.254 \text{ mm}, 2.54 \text{ mm}),$  and  $w \in (2.5 \text{ mm}, 10 \text{ mm})$  with the help of the software CST Microwave Studio. It is noted that for fixed HMSIW dimensions, the position of the maximum electric field moves inwards the waveguide with increasing frequency.

Substituting (3) in the general equation [21, equ. (3–89)], the field components inside the HMSIW can be calculated as follows:

$$E_{y,(0.5,0)} = Ak_x \sin k_x (w - x)e^{-jk_z z}$$
(4a)

$$H_{x,(0.5,0)} = \frac{-Ak_x k_z}{\omega \mu} \sin k_x (w - x) e^{-jk_z z}$$
 (4b)

$$H_{z,(0.5,0)} = \frac{A(\varepsilon_r k_0^2 - k_z^2)}{j\omega\mu} \cos k_x (w - x) e^{-jk_z z},$$

$$0 < x < w$$
(4c)

where  $\omega$  is the phase frequency with the value of  $\omega=2\pi f$  and  $\mu$  is the substrate permeability. The characteristic impedance of the dominant mode takes the form of the wave impedance and can be accordingly calculated as  $Z_c=E_y/H_x=(-\omega\mu)/k_z$ , as in the case of conventional rectangular waveguides [22].

The field in the homogeneous medium is mainly due to the radiation from the open aperture (x=0). In principle, the equivalent electric and magnetic currents on the aperture can be analytically computed according to the field components given in (4). However, since the ratio of a/w is close to 0, which leads to  $\cos k_x w \approx 0$ , the equivalent electric current density  $\vec{J}_y = 2\vec{a}_x \times \vec{a}_z H_{z,(0.5,0)}|_{x=0}$  can be neglected. Therefore, only the equivalent magnetic current density  $\vec{M}_z$  is considered in the following calculation of the field outside the HMSIW.

As depicted in Fig. 3, the points P and Q are the field observation point and source point, respectively. The equivalent magnetic current density  $\vec{M}_z$  is calculated as [23]

$$\vec{M}_z = -2\vec{a}_x \times \vec{a}_y E_{yI,(0.5,0)}|_{x=0}$$
  
=  $-\vec{a}_z 2Ak_x \sin(k_x w) e^{-jk_z z}$ . (5)

where the factor 2 arises from the mirror effect of the ground plane.

Multiplying (5) with the Green function in the surrounding medium and integrating the product over the open aperture, i.e.,  $y' \in (-h/2, h/2)$  and  $z' \in (-\infty, +\infty)$ , the electric vector potential can be obtained as

$$F_z \approx -\frac{Ahk_x}{2\pi}\sin(k_x w)e^{-jk_z z} \int_{-\Delta l}^{\Delta l} e^{-jk_z t} \frac{e^{-jk_{0,\text{eff}}R}}{R} dt \quad (6)$$

where  $\Delta l \to \infty$ , t=z'-z, and  $k_{0,\mathrm{eff}}=2\pi f \sqrt{\varepsilon_{0,\mathrm{eff}}}/c$ . In (6), R represents the distance between the source point Q and the field observation point P. The exact value of R is  $\sqrt{\rho^2+t_1^2}$ , as shown in Fig. 3, but for simplicity, the approximation  $R\approx \sqrt{\rho^2+t^2}$  is adopted in the integration of (6) due to the small thickness h of the substrate. Moreover, since the field intensity at point P mainly depends on those source points in the near region, the integral can be limited to a finite value of  $\Delta l$ . In this study, it is empirically found that the minimum value of  $\Delta l$  required for a satisfactory convergence of (6) is three to five times the wavelength in free space.

Based on (6), the field components can be calculated using  $E_{\varphi}=(\partial F_z/\partial \rho)$  and  $H_z=(j/\omega\mu)((\partial^2 F_z/\partial \rho^2)+(\partial F_z/\rho\partial \rho))$  in cylindrical coordinates [23].

The calculated electric field component  $E_y$  on the xoz-plane is plotted in Fig. 2. The normalized electric field inside the

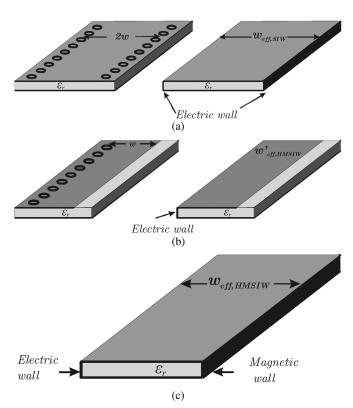


Fig. 5. (a) SIW with a width 2w and the corresponding equivalent model (a conventional rectangular waveguide). (b) HMSIW as evolution from the SIW cut along its longitudinal symmetry plane, and the correspondingly cut equivalent model. (c) Second equivalent model of the HMSIW, proposed for the calculation of the phase constant.

HMSIW (0 < x/w < 1) is given by dividing (4a) by the magnitude  $|Ak_x|$  and that outside the HMSIW (x/w < 0) is calculated through numerical integration of

$$\overline{E}_{\varphi} = \frac{E_{\varphi}}{|Ak_{x}|} \\
= \frac{h \sin(k_{x}w)}{2\pi} e^{-jk_{z}z} \\
\times \int_{-\Delta l}^{\Delta l} \frac{(1+jk_{0,\text{eff}}\sqrt{\rho^{2}+t^{2}})\rho e^{-jk_{0,\text{eff}}}\sqrt{\rho^{2}+t^{2}}-jk_{z}t}{(\rho^{2}+t^{2})^{3/2}} dt.$$
(7)

A good agreement between the calculation and simulation results is observed, which validates the field equations.

# B. Second Equivalent Model: Phase Constant

As depicted in Fig. 5(a), a SIW with a width 2w is equivalent, in terms of cutoff frequency, to a conventional rectangular waveguide with a width  $w_{\text{eff,SIW}}$  when the widths 2w and  $w_{\text{eff,SIW}}$ satisfy the fitted equation [7, eq. (9)]

$$w_{\text{eff,SIW}} = (2w) - 1.08 \frac{d^2}{s} + 0.1 \frac{d^2}{(2w)}$$
 (8)

where d and s are the vias' diameter and the spacing between adjacent vias, respectively. This equivalent rectangular waveguide has the same height h and is filled with the same dielectric material as the SIW.

Cutting the SIW and its equivalent rectangular waveguide in half along their longitudinal symmetry planes, an HMSIW with a width w and the corresponding equivalent waveguide with a width

$$w'_{\text{eff,HMSIW}} = w_{\text{eff,SIW}}/2$$
 (9)

are obtained as shown in Fig. 5(b). It is noted that the equivalent model in Fig. 5(b) is an open structure. Therefore, due to the fringing fields, it is still difficult to calculate the cutoff frequency and phase constant of the HMSIW by directly using the width  $w'_{\text{eff,HMSIW}}$ .

Considering, on one hand, that the electric field is mainly tangential to the open aperture where it approximately reaches its maximum (Fig. 2), and on the other hand, that the magnetic field is mainly perpendicular to the open aperture, a new equivalent waveguide is proposed with the open aperture replaced by a magnetic wall, as shown in Fig. 5(c). The width of this new equivalent model of the HMSIW is

$$w_{\text{eff,HMSIW}} = w'_{\text{eff,HMSIW}} + \Delta w$$
 (10)

where the additional width  $\Delta w$ , which still needs to be determined, accounts for the effect of the fringing fields and is a function of the width  $w'_{\mathrm{eff,HMSIW}}$  , of the waveguide height h , and of the substrate permittivity  $\varepsilon_r$ . Based on the present equivalent model, the cutoff frequency and phase constant of the quasi- $TE_{0,5,0}$  mode in the original HMSIW can be easily calculated as

$$f_{c,\text{TE}_{0.5,0}} = \frac{c}{4\sqrt{\varepsilon_r}w_{\text{eff,HMSIW}}}$$
 (11)

$$f_{c,\text{TE}_{0.5,0}} = \frac{c}{4\sqrt{\varepsilon_r} w_{\text{eff,HMSIW}}}$$

$$k_{z,\text{TE}_{0.5,0}} = \sqrt{k_0^2 \varepsilon_r - \left(\frac{\pi}{2w_{\text{eff,HMSIW}}}\right)^2}$$
(12)

with  $k_0$  defined as in (2).

To determine the additional width  $\Delta w$ , the following procedure is carried out. Firstly, two HMSIWs [such as in Fig. 1(a)] with an identical profile, but different lengths, are modeled and simulated in HFSS. The resulting scattering parameters are processed using the multiline method (ML) [24], [25] in order to obtain the cutoff frequency  $f_{c,{
m TE}_{0.5,0}}.$  Secondly, the obtained  $f_{c,\mathrm{TE}_{0.5.0}}$  is substituted into (11) to calculate the width  $w_{
m eff.HMSIW}$  of the equivalent waveguide. Thirdly, the equivalent width  $w'_{\text{eff},HMSIW}$  is calculated using (8) and (9), according to the metal posts configuration of the HMSIW. Finally, the additional width  $\Delta w$  can be computed by substituting the obtained equivalent widths  $w_{\text{eff},\text{HMSIW}}$  and  $w'_{\text{eff},\text{HMSIW}}$  into (10).

Varying the values of the HMSIW width w, of the HMSIW height h, and of the substrate permittivity  $\varepsilon_r$  and iterating the procedure above, different sets of curves can be obtained describing  $\Delta w$  versus  $w'_{\text{eff.HMSIW}}$ ,  $\Delta w$  versus h, or  $\Delta w$  versus  $\varepsilon_r$ . Fitting all curves with the nonlinear least squares method [26], the additional width  $\Delta w$  normalized to the HMSIW height h can be estimated as

$$\frac{\Delta w}{h} = \left(0.05 + \frac{0.30}{\varepsilon_r}\right)$$

$$\times \ln\left(0.79 \frac{w_{\text{eff,HMSIW}}^{\prime 2}}{h^3} + \frac{104w_{\text{eff,HMSIW}}^{\prime} - 261}{h^2} + \frac{38}{h} + 2.77\right).$$
(13)

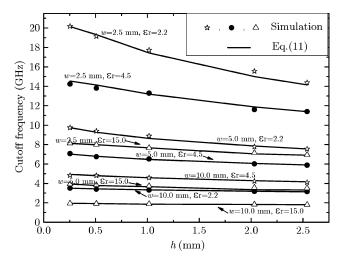


Fig. 6. Cutoff frequency versus the HMSIW height for variations of the HMSIW width and substrate permittivity. In all cases, the diameter d and the spacing s of the vias are 0.5 and 0.6 mm, respectively.

This expression is valid for  $\varepsilon_r \in (2.2, 15)$ ,  $h \in (0.254 \text{ mm}, 2.54 \text{ mm})$ , and  $w \in (2.5 \text{ mm}, 10 \text{ mm})$  covering a potential range of operation frequency from 2 to 60 GHz.

At this point, all necessary design formulas are available. For the practical synthesis of an HMSIW with a specified cutoff frequency, where the thickness h and the substrate permittivity  $\varepsilon_r$  of the printed circuit board are given, the equivalent width  $w_{\rm eff,HMSIW}$  is first determined using (11). Subsequently, the proper diameter d and the spacing s of the metallic posts are selected according to the operation frequency range [7]. Finally, substituting the known parameters h,  $\varepsilon_r$ ,  $w_{\rm eff,HMSIW}$ , d, and s into (8)–(10) and (13), the HMSIW physical width w (as the only unknown) can be obtained by solving those four equations simultaneously.

As shown in Fig. 6, the cutoff frequencies calculated through this procedure for various HMSIW widths, heights, and substrate permittivities have been compared to those obtained from simulations of the corresponding devices. For all the examined examples in Fig. 6, the diameter and spacing of the vias in the HMSIW are  $d=0.5~\mathrm{mm}$  and  $s=0.6~\mathrm{mm}$ , respectively. In the mentioned valid range of the design formulas, the calculation error is estimated below 2%.

Furthermore, for the two HMSIW prototypes mentioned at the beginning of this section, the phase constants have been calculated using (12) and compared with the simulation and measurement results, as plotted in Figs. 7 and 8. The agreement between all results in Figs. 6–8 validates the proposed design formulas (8)–(10) and (13).

Using the present equivalent model, the frequency range for the single mode operation can also be estimated based on the calculation of the cutoff frequencies for the fundamental quasi- $TE_{0.5,0}$  mode [as given in (11)] and the first higher order quasi- $TE_{1.5,0}$  mode. In the closed equivalent waveguide, the cutoff frequency of the quasi- $TE_{1.5,0}$  mode can be approximated as

$$f_{c,\text{TE}_{1.5,0}} = \frac{3c}{4\sqrt{\varepsilon_r}w_{\text{eff,HMSIW}}}$$
(14)

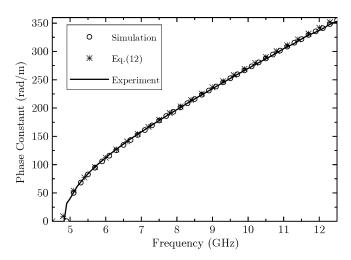


Fig. 7. Phase constant of the quasi- $\text{TE}_{0.5,0}$  mode in the HMSIW with a width w=10.0 mm, height h=0.508 mm, and substrate permittivity  $\varepsilon_r=2.2$ . The diameter d and the spacing s of the vias are 0.5 and 0.6 mm, respectively.

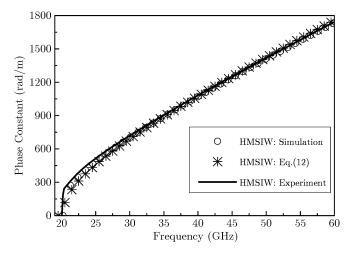


Fig. 8. Phase constant of the quasi-TE $_{0.5,0}$  mode in the HMSIW with a width w=2.5 mm, height h=0.254 mm, and substrate permittivity  $\varepsilon_{\tau}=2.2$ . The diameter d and the spacing s of the vias are 0.5 and 0.6 mm, respectively.

which is three times that of the fundamental mode. Therefore, if not considering any suppression of higher modes through feeding technologies, an HMSIW with a width w yields a single-mode operation frequency range approximately twice that of a SIW with a width 2w.

## III. ATTENUATION

In this section, the attenuation of the HMSIW is investigated numerically and experimentally. First, a comparison of the simulated results with the experimental data is provided as an assessment of the simulation accuracy. A procedure is then presented for numerically analyzing the loss mechanism of the HMSIW in the frequency range of 20–60 GHz. Finally, the measured losses of the HMSIW are compared to those of the SIW and the standard MS line in a representative case.

All HMSIW models used in the simulations and all the fabricated HMSIW devices are corresponding to the second prototype mentioned at the beginning of Section II and operate in the frequency range of 20–60 GHz. In those models and devices, the feeding MS lines and transitions are kept identical, but the

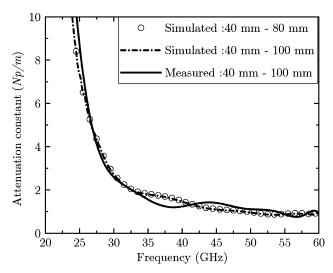


Fig. 9. Simulated and measured attenuation constant of the HMSIW with a width w=2.5 mm, height h=0.254 mm, and substrate permittivity  $\varepsilon_r=2.2$ . The diameter d and the spacing s of the vias are 0.5 and 0.6 mm, respectively. All curves are obtained by applying the ML method to lines of different lengths, as given in the legend.

middle HMSIW length [marked as l in Fig. 1(a)] is varied for the ML analysis.

#### A. Validation of the Simulation

Since the analysis of the loss mechanism in the HMSIW is based on simulations, the accuracy of the simulation tool has been firstly assessed. For this purpose, three HMSIW prototypes with lengths l=40 mm, l=80 mm, and l=100 mm were first analyzed using HFSS. The attenuation constant was then calculated by comparing the losses of the HMSIWs with lengths l=40 mm, and l=80 mm using the ML method. Similarly, the attenuation constant can also be computed by comparing the losses of the HMSIWs with lengths l=40 mm and l=100 mm. The attenuation constant obtained through both computations is presented in Fig. 9. It can be seen that the results of both cases are consistent, indicating that the simulations and calculations are convergent. A quantitative analysis shows that the difference between the two curves is within 0.04 Np/m.

On the experimental side, HMSIW prototypes with lengths  $l=40~\rm mm$  and  $l=100~\rm mm$  were fabricated and measured. The experimentally obtained attenuation constant is also plotted in Fig. 9. A fairly good agreement is achieved between the simulated and measured results over the entire band of interest. This further confirms the accuracy of the simulation method and provides justification for the following numerical analysis.

#### B. Numerical Investigation of the Losses in HMSIW

To characterize the loss mechanism in the HMSIW, the same two HMSIWs with  $l=40~\mathrm{mm}$  and  $l=100~\mathrm{mm}$  are simulated again, yet with altered properties of the materials, i.e., the conductivity of the metal and the loss tangent of the dielectric are varied. This procedure allows distinguishing between the conductive, dielectric, and radiation losses in the HMSIW and provides a qualitative characterization of their variation with frequency.

1) Radiation Losses: To determine the total power leakage from both the open aperture and the space between the vias, all

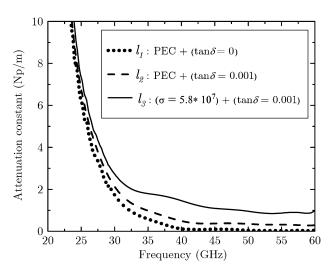


Fig. 10. Simulated attenuation constant of the quasi-TE<sub>0.5,0</sub> mode in the HMSIW with varied conductivity of the conductor and loss tangent of the dielectric substrate. The dimensions of the HMSIW are w=2.5 mm, h=0.254 mm, d=0.5 mm, and s=0.6 mm. The substrate permittivity is  $\varepsilon_r=2.2$ . The label PEC denotes perfect electric conductor  $(\sigma=\infty)$ .

the materials used in the HMSIW simulation models are first set to be lossless, i.e., the conductivity of the metal is set to  $\sigma=\infty$  and the loss tangent of the dielectric to  $\tan\delta=0$ . The obtained attenuation constant is shown as the curve  $l_1$  in Fig. 10. Since there are no conductive or dielectric losses in the model, the attenuation constant completely characterizes the power leakage from the HMSIW. It can be observed that those radiation losses become extremely high as the frequency is decreased toward the cutoff. The reason for this performance degradation can be intuitively understood when considering that at the cutoff frequency, the open side of the HMSIW can be viewed as a slot with constant field distribution.

However, as frequency exceeds 40 GHz, the attenuation constant exclusively resulting from the radiation losses drops to below 0.1 Np/m, indicating a small contribution to the total attenuation. This corroborates the observation in Fig. 8 that the nonradiative equivalent model, as given in Fig. 5(c) and (12), can approximate the HMSIW more accurately at higher frequencies than close to cutoff.

2) Dielectric Losses: Maintaining the metallic material to be lossless, realistic dielectric losses are introduced in the HMSIW simulation models as loss tangent set to  $\tan \delta = 0.001$ . The resulting simulated attenuation constant as a function of the frequency is plotted as  $l_2$  in Fig. 10. The increased attenuation compared to the lossless case is obviously caused by dielectric losses in the HMSIW, which, therefore, can be directly characterized as the difference between the curves  $l_1$  and  $l_2$ .

From Fig. 10, it can be found that the effect of the dielectric losses is masked by radiation losses at frequencies below 25 GHz. As frequency increases, the two curves  $l_1$  and  $l_2$  get visibly separated from each other and reveal the effect of dielectric losses. Above 35 GHz, the dielectric losses change only *slightly* with the frequency for the currently used substrate material of stable dispersion properties. More specifically, the difference between curves  $l_1$  and  $l_2$  remains at a level of 0.3  $\pm$  0.1 Np/m above 35 GHz.

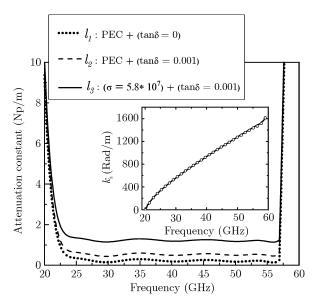


Fig. 11. Simulated attenuation constant of the quasi- $TE_{10}$  mode in the SIW with varied conductivity of the conductor and loss tangent of the dielectric substrate. The SIW width and height are 5.45 and 0.254 mm. The diameter and spacing of the vias are 0.5 and 0.6 mm, respectively. The substrate permittivity is  $\varepsilon_r = 2.2$ . The label PEC denotes perfect electric conductor ( $\sigma = \infty$ ). The inset shows the corresponding phase constant obtained from simulations (solid line) and measurements (discrete circles).

3) Conductive Losses: Finally, both the conductor and dielectric used in the simulated models of the HMSIW are set to be the realistic lossy materials, i.e., with the conductivity  $\sigma=5.8\times10^7~{\rm S\cdot m^{-1}}$  for the metal and the loss tangent  $\tan\delta=0.001$  for the dielectric substrate. The attenuation constant for this case is plotted as the curve  $l_3$  in Fig. 10, and reflects the combined effects of the conductive, dielectric, and radiation losses. The difference between the curves  $l_2$  and  $l_3$  arises from the added conductive losses in this prototype. Therefore, comparison of the curve  $l_3$  to  $l_2$  leads to the conclusion that conductive losses can be almost negligible at frequencies lower than 28 GHz when compared to radiation losses. However, with the further increase of frequency, the conductive losses become the dominant cause of attenuation in the HMSIW if a low-dispersion low-loss substrate material is used.

4) Comparison to Losses in the SIW: For comparison, two SIWs with lengths of  $l=40~\mathrm{mm}$  and  $l=100~\mathrm{mm}$  fed by a centered MS line have been designed using the same substrate as the second HMSIW prototype (20–60 GHz). The radius and spacing of the vias in the SIWs are the same as those in the HMSIW. The width of the SIWs is determined to be  $2w=5.45~\mathrm{mm}$  in order to obtain the same cutoff frequency as the HMSIW, as indicated in the inset of Fig. 11. Furthermore, the symmetry granted by the centered feeding line suppresses all the even modes, thereby providing the SIW with a single-mode operation frequency range approximately matching that of the HMSIW.

The losses in the SIW are analyzed numerically by applying the same procedure as for the HMSIW. The obtained attenuation constants corresponding to the fundamental quasi- $TE_{10}$  mode are shown in Fig. 11. The drastic increase in the attenuation at frequencies above 58 GHz results from the occurrence of the bandstop [7]. For the present SIW design, the findings are similar to those for the HMSIW and can be summarized

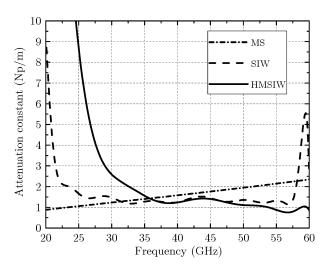


Fig. 12. Measured attenuation constants of the MS line, SIW, and HMSIW.

as follows. The dominant attenuation is caused by the conductive losses. The dielectric losses are quite low for the presently used low-loss dielectric substrate. The radiation losses are almost negligible when the waveguide operates far above cutoff. The increase of radiation losses near cutoff is less pronounced than in the HMSIW, as there is no fully open side in the SIW.

# C. Experimental Comparison of HMSIW With SIW and Microstrip

For a direct experimental comparison with the second HMSIW prototype, the SIWs studied above and two standard  $50-\Omega$  MS lines of lengths of 50.8 and 299.3 mm have also been fabricated. The MS lines were manufactured on the same substrate as the SIWs and HMSIWs. A *time gating technique* was used in the measurements in order to exclude the effects of the connectors. The measured attenuation constants are given in Fig. 12.

The attenuation of the MS line increases monotonically with the frequency and is lower than that of the SIW and HMSIW at frequencies below 35 GHz. This is explained by the large radiation losses occurring around the cutoff frequency of the SIW and HMSIW. As the frequency increases, both the conductive losses and radiation losses increase in the MS line. As a consequence, the attenuation of the MS line exceeds those of the SIW and HMSIW at frequencies above 35 GHz.

Comparing the losses of the SIW and HMSIW indicates that the attenuation of the HMSIW is higher than that of the SIW at frequencies close to the cutoff, but becomes lower as the frequency increases above 40 GHz. This can be explained by considering the results in Figs. 10 and 11.

- At frequencies below 40 GHz, the conductive and dielectric losses of the SIW are comparable to those of the HMSIW. However, with the same cutoff frequency, the radiation losses of the HMSIW are much higher than those of the SIW due to the power leakage from the open side of the HMSIW.
- 2) At frequencies above 40 GHz, the radiation losses of the HMSIW are reduced to a level comparable to those of the SIW, and so are the dielectric losses. The conductive losses become dominant for both lines in this frequency range. In the absence of fringing at the open side, the conductive

losses in the HMSIW would be equal to those in the SIW. However, as the frequency increases, more energy propagates along the waveguide in the fringing region, where the fields are not affected by the conductors. Consequently, a lower attenuation is achieved in the HMSIW.

Although the comparison of the attenuation above is based on the study of specific examples rather than general models, this work with no loss of generality presents a method to analyze the attenuation of a transmission line through the separation of the conductive, dielectric, and radiation losses from the total attenuation. The presented measurement results demonstrate a practically achievable level of attenuation in the HMSIW for the frequency range of 20–60 GHz.

Before concluding, a general remark on substrate selection in the perspective of this study is required. In a typical practical design procedure, an appropriate substrate is generally determined in advance according to certain specifications such as the operation frequency band. Subsequently, the type of transmission line is selected, by considering the losses, volume, fabrication cost, etc. Therefore, the use of an identical substrate has been assumed here as a preliminary condition for a fair comparison of the losses between the MS line, SIW, and HMSIW.

However, in a case where there are no *a priori* restrictions on the choice of substrate, other considerations need to be taken into account. In particular, increasing the height of the SIW can significantly reduce the conductive losses in comparison with the MS line [27]. This strategy is not viable for the HMSIW since the height is strictly constrained by the operation frequency band and cannot be enlarged arbitrarily. Additionally, a general drawback of the HMSIW and the SIW is the larger volume compared with the MS line. Therefore, due to their specific advantages and drawbacks, either the MS line, SIW, or HMSIW may be preferred in different applications.

# IV. CONCLUSION

The propagation properties of the HMSIW, i.e., the phase constant and attenuation constant, have been investigated using theoretical, numerical, and experimental methods. Two equivalent models have been proposed to analyze the field distribution and calculate the phase constant of the HMSIW. An approximate design equation has been derived using a statistical method and has been validated by numerical and experimental results. Additionally, the attenuation characteristics of the HMSIW have been studied through a numerical separation of the conductive, dielectric, and radiation losses. It is found that for identical materials and arrangement of the vias, the losses in the HMSIW can be at the same level or even lower compared to those of the SIW. Further, in the millimeter-wave range, both the HMSIW and SIW exhibit lower attenuation compared to a standard MS line made of the same materials. To make the comparison as reasonable as possible, the selected dimensions and materials in all investigated examples of transmission lines are quite common in the sense of practical applications.

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