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Microscopic structure of three-dimensional charge order in kagome superconductor AV_3Sb_5 and its tunability

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Correlated electronic systems are naturally susceptible to develop collective, symmetry-breaking electronic phases as observed in Cu- and Fe-based high-temperature superconductors, and twisted Moiré superlattices. The family of kagome metals AV_3Sb_5 ($A = K, Rb, Cs$) is a recently discovered, rich platform to study many of these phenomena and their interplay. In these systems, three-dimensional charge order (3D-CO) is the primary instability that sets the stage in which other ordered phases emerge, including unidirectional stripe order, orbital flux order, and superconductivity. Therefore, determining the exact nature of the 3D-CO is key to capture the broader phenomenology in AV_3Sb_5 . Here, we use high-resolution angle-resolved photoemission spectroscopy to resolve the microscopic structure and symmetry of 3D-CO in AV_3Sb_5 . Our approach is based on identifying an unusual splitting of kagome bands induced by 3D-CO, which provides a sensitive way to refine the spatial charge patterns in neighboring kagome planes. Notably, we found a marked dependence of the 3D-CO structure on alkali metal and doping: the 3D-CO in CsV_3Sb_5 is composed of kagome layers with alternating Star-of-David and Tri-Hexagonal distortions, while KV_3Sb_5 , RbV_3Sb_5 , and Sn-doped CsV_3Sb_5 realize a staggered charge pattern breaking C_6 rotational symmetry. These results establish the microscopic structure of 3D-CO and its evolution with chemical composition for the first time, providing fresh insights on the origin of the cascade of exotic electronic phases in AV_3Sb_5 .

36 The family of AV_3Sb_5 is a newly discovered series of kagome-based compounds realizing
37 unconventional many-body phases and nontrivial electronic topology (Fig. 1c,d)^{1,2}. In close
38 analogy with other strongly correlated systems such as Cu- and Fe-based high-temperature
39 superconductors^{3,4}, as well as twisted Moiré superlattices⁵, a cascade of coupled symmetry-broken
40 electronic orders has been observed in AV_3Sb_5 . These include translational symmetry breaking in
41 the form of 2×2 charge order (CO) below $T_{CO} \approx 78\sim 102$ K^{2,6}, rotational symmetry breaking in the
42 form of unidirectional 1×4 stripe order below $T_{SO} \approx 50\sim 60$ K⁷⁻¹⁰, a time-reversal symmetry
43 breaking orbital flux phase below $T_f \approx 70$ K¹¹, and superconductivity below $T_c \approx 0.92\sim 2.5$ K^{2,12,13}.
44 Understanding the origin, nature, and interrelation between these electronic orders is a major
45 frontier of this emerging research field.

46 Notably, previous theoretical and experimental investigations point toward the unique role
47 of the electronic structure of the underlying kagome lattice in driving the rich physics of AV_3Sb_5 ¹⁴⁻
48 ²⁰. In the ideal limit, the kagome lattice exhibits multiple singularities in its electronic dispersion,
49 including Dirac fermions at the Brillouin zone corner K , van Hove singularity (vHS) at the zone
50 edge M , and flat bands across the whole Brillouin zone (Fig. 1a). Depending on the band filling
51 fraction n , these electronic states may engender various topological and correlated phases as
52 extensively investigated for more than a decade²¹⁻²⁶. Especially at the vHS filling fractions $n =$
53 $3/12$ and $5/12$ (Fig. 1a), the Fermi surface of the kagome lattice is perfectly nested by three
54 symmetry-equivalent reciprocal lattice vectors $Q_1 = (0.5, 0)$, Q_2 , and Q_3 (Fig. 1b). Combined with
55 the high density of states at vHS, the nesting creates a diverging electronic susceptibility and sets
56 the stage for pairing in multiple channels, and the subsequent emergence of charge/spin order and
57 superconductivity²⁴⁻²⁶. The electronic structure of the AV_3Sb_5 series follows this script, with
58 multiple kagome-derived vHS sharply aligned to the Fermi level (E_F)¹⁶⁻²⁰. Accordingly, as
59 displayed in Fig. 1e, density functional theory (DFT) calculation of phonon frequency reveals six
60 unstable modes exactly at the Q_1 , Q_2 , and Q_3 in-plane wave vectors – three at M ($k_z = 0$) and the
61 other three at L ($k_z = \pi$) – indicating that the pristine kagome structure is unstable toward the 2×2
62 charge distortion²⁷⁻²⁹. Combined with the experimental identification of the 2×2 CO^{2,6}, this
63 suggests that the toy-model vHS physics of the ideal kagome lattice is indeed realized within the
64 AV_3Sb_5 system.

65 Importantly, the contribution of L phonons with nonzero out-of-plane momentum ($k_z = \pi$)
66 indicates that the full description of CO in the AV_3Sb_5 series needs to go beyond the limit of two-

67 dimensional kagome lattice. The three-dimensional nature of CO was reported in early studies^{17,30},
68 supporting either twofold ($2\times 2\times 2$) or fourfold ($2\times 2\times 4$) c -axis modulations^{31,32}. As we illustrate in
69 Fig. 1f,g, M -point (L -point) phonons are associated to V-V bond distortions in-phase (out-of-phase)
70 across neighboring kagome planes (Fig. 1f)²⁸. Then, depending on the possible $3Q$ combinations
71 of M and L phonons, various microscopic 3D-CO structures can be realized in the AV_3Sb_5 series
72 (Fig. 1h-m): Star-of-David or SoD ($-M, -M, -M$); Tri-hexagonal or TrH (M, M, M); Alternating SoD
73 and TrH (L, L, L); Staggered SoD ($-M, -L, -L$); Staggered TrH (M, L, L); and Staggered Alternating
74 SoD and TrH (M, M, L).

75 We emphasize here that identifying the exact structure and symmetry of 3D-CO is of
76 paramount importance for understanding the sequence of electronic symmetry breaking transitions
77 observed in AV_3Sb_5 . This is because CO formation has the highest energy scale in AV_3Sb_5 series
78 ($T_{CO} \approx 78\sim 102$ K) and thus defines the background symmetry under which other electronic phases
79 emerge (stripe order, nematicity, flux phase, and superconductivity). As an example, if CO
80 crystallizes in the inverse MLL , MLL , or MML phases (Fig. 1k-m), C_6 -rotational symmetry is
81 spontaneously broken, which may provide a natural explanation for the unidirectional 1×4 stripe
82 order and electronic nematicity emerging below T_{CO} ⁷⁻¹⁰. However, the detailed microscopic
83 structure of 3D-CO and its composition dependence in AV_3Sb_5 series have not been conclusively
84 reported so far, with different approaches – X-ray diffraction^{31,32}, coherent phonon spectroscopy³³,
85 nuclear magnetic/quadrupole resonance³⁴, scanning tunneling microscopy²⁷, and DFT³⁵ – yielding
86 divergent results.

87 In the present study, we establish the microscopic structure of 3D-CO and its evolution in
88 the AV_3Sb_5 series by analyzing the detailed reconstruction of the electronic bands induced by 3D-
89 CO. Using high-resolution angle-resolved photoemission spectroscopy (ARPES), we observe an
90 unusual energy splitting of the kagome-derived vHS and Dirac bands, which is a direct
91 consequence of the unit cell reconstruction in the 3D-CO phase. Crucially, the precise morphology
92 of the band splitting is highly sensitive to the intra-unit-cell stacking between different 3D-CO
93 modulation patterns across adjacent kagome planes, which allows us to constrain the 3D-CO
94 structure and symmetry in the AV_3Sb_5 series. Using this approach, we determine that the band
95 splitting of CsV_3Sb_5 is most consistent with the Alternating SoD and TrH structure (LLL phase),
96 while those in KV_3Sb_5 , RbV_3Sb_5 , and Sn-doped CsV_3Sb_5 are markedly different from the CsV_3Sb_5
97 and can be assigned to the inverse MLL or MLL phases. These results expand our current

98 understanding of CO in the AV_3Sb_5 series, and reveal new essential details to explain the origin of
99 multiple collective phenomena realized in strongly correlated kagome systems.

100 We start with a brief description of the overall electronic structure of AV_3Sb_5 . As displayed
101 in Fig. 2a, the DFT band calculation for CsV_3Sb_5 reveals four bands near E_F : an electron-pocket
102 at the Brillouin zone center Γ (G -band), $d_{xy}/d_{x^2-y^2}$ orbital kagome bands with Dirac point at ≈ -0.27
103 eV and vHS near E_F ($K1$ -band), d_{xz}/d_{yz} orbital kagome bands with Dirac point at ≈ -1.3 eV and
104 vHS near E_F ($K2$ -band), and additional d_{xz}/d_{yz} orbital kagome bands with opposite parity from the
105 $K2$ -band ($K2'$ -band). All band dispersions have been closely reproduced in previous ARPES
106 studies^{19,20,36-38}. Meanwhile, we note that in the experimental geometry used in the present study,
107 only G -, $K1$ -, and $K2$ -bands are visible in the ARPES spectra (see Fig. 2c for example) due to the
108 destructive interference of photoelectrons from the $K2'$ -band³⁹. Additional characterization of the
109 electronic structures in AV_3Sb_5 , such as Fermi surfaces and wide-range energy-momentum
110 dispersions, can be found in the Extended Data Fig. 1.

111 As summarized in Fig. 2, we observed two distinct electronic reconstructions induced by
112 3D-CO in CsV_3Sb_5 . First, as shown in Fig. 2b-d, we detected clear shadow bands below T_{CO}
113 (dashed arrows in Fig. 2d), which are the replica of the original bands (solid arrows in Fig. 2c,d)
114 folded along the in-plane momentum direction. This is a direct consequence of the new periodicity
115 arising from the in-plane component of charge order, which folds the pristine Brillouin zone to the
116 smaller 2×2 CO Brillouin zone (see schematics in Fig. 2b). Such shadow bands and in-plane
117 folding effects have been typically observed in other charge order systems such as transition metal
118 dichalcogenides⁴⁰ and rare-earth trichalcogenides⁴¹. At the same time, as shown in Fig. 2e-k, a
119 detailed inspection below T_{CO} additionally reveals an unusual doubling or splitting of the kagome
120 bands along the energy axis. Such splitting, which is unreported, could be visualized only after
121 careful optimization of the spectral quality (see also Fig. 4f,g for corresponding energy and
122 momentum distribution curves). At the simplest level, one can understand the band doubling as a
123 consequence of the out-of-plane component of the 3D-CO, which folds the Brillouin zone along
124 the k_z -direction and superimposes the $k_z = \pi \sim \pi/2$ bands onto the $k_z = 0 \sim \pi/2$ bands (see schematics
125 in Fig. 2e). In the case of CsV_3Sb_5 , we find three sectors in the band structure where the doubling
126 becomes most prominent: near the vHS of the $K1$ -band (Fig. 2g,k), at the lower Dirac band of the
127 $K1$ -band (Fig. 2g,i), and at the $K2$ -band near E_F (Fig. 2k).

128 The key idea of our study comes from the recognition that the doubled-band dispersion in
129 the 3D-CO state is actually more than the simple superposition of $k_z = 0 \sim \pi/2$ and $k_z = \pi \sim \pi/2$ bands
130 of the pristine structure. In the 3D-CO state, the adjacent kagome layers in AV_3Sb_5 become distinct
131 upon realizing different CO patterns on each layer (Fig. 1j-m). The altered hopping pathways
132 between the two charge-ordered kagome planes further reconstruct the doubled-band dispersion.
133 This mechanism depends on the detailed charge distortions in adjacent kagome planes, with the
134 nature of the band splitting becoming strongly dependent on the 3D-CO structure. This provides a
135 unique and highly constrained way to resolve the microscopic structure of 3D-CO in AV_3Sb_5 series.

136 To illustrate this idea further, we simulated the reconstruction of CsV_3Sb_5 bands in all
137 possible 3D-CO structures using DFT. Fig. 3a-f represents the electronic structure of CsV_3Sb_5 at
138 $k_z = 0$ in the inverse MMM , MMM , LLL , inverse MLL , MLL , and MML phases, respectively. Note
139 that, for simplicity, we unfolded the band structure along the in-plane momentum-space, while
140 keeping the band folding along k_z . In accordance with the experimental results, the doubling of the
141 dispersions for the $K1$ - and $K2$ -kagome bands are closely reproduced in the 3D-CO states (see
142 yellow arrows in Fig. 3c for example). Most importantly, the details of band splitting are highly
143 dependent on the microscopic structure of 3D-CO. The most noticeable discriminant between
144 different 3D-CO structures is the behavior of the lower $K1$ -Dirac band. As marked with yellow
145 arrows in the insets of Fig. 3, the lower $K1$ -Dirac band barely splits in the inverse MMM , MMM ,
146 inverse MLL , and MLL structures (Fig. 3a,b,d,e), while an apparent doubling is observed in the
147 LLL structure (Fig. 3c). The latter closely reproduces the ARPES spectra in Fig. 2g,i. For the case
148 of the MML structure (Fig. 3f), both the lower $K1$ -Dirac band and $K1$ -vHS band split into at least
149 three bands if one takes an average over all possible C_2 -symmetric domains (see also the Extended
150 Data Fig. 2 for the domain-resolved calculations). Based on the above considerations, we conclude
151 that the observed band splitting supports the LLL structure or Alternating SoD and TrH phase (Fig.
152 1j) as the microscopic 3D-CO structure in CsV_3Sb_5 .

153 Intriguingly, the investigation of KV_3Sb_5 , RbV_3Sb_5 , and Sn-doped CsV_3Sb_5 revealed an
154 electronic reconstruction markedly different from the CsV_3Sb_5 case. Figure 4 displays ARPES
155 spectra of KV_3Sb_5 , RbV_3Sb_5 , and Sn-doped CsV_3Sb_5 measured at 6 K, in the CO state (See
156 Extended Data Fig. 3 for the transport characterization of superconductivity and CO in Sn-doped
157 CsV_3Sb_5). Similar to the case of CsV_3Sb_5 , the doubling or splitting of the $K1$ -vHS (Fig. 4a,b,c)
158 and $K2$ -bands (Fig. 4d,e) is clearly observed across the whole family. The corresponding energy

159 distribution curves of the $K1$ -vHS and momentum-distribution curves of the $K2$ -band (Fig. 4f,g)
160 also unambiguously demonstrate the presence of band doubling. These results indicate that the
161 3D-CO is a universal phenomenon in the AV_3Sb_5 series. However, we observe that the behavior
162 of the lower $K1$ Dirac band in KV_3Sb_5 , RbV_3Sb_5 , and Sn-doped CsV_3Sb_5 is very different from
163 that of the CsV_3Sb_5 case. As highlighted with yellow arrows in Fig. 4a-e, the lower Dirac
164 dispersion of the $K1$ band does not undergo a splitting in the 3D-CO state, in contrast to the
165 observations in CsV_3Sb_5 (Fig. 2g,i). Compared to the calculations in Fig. 3, this behavior rules out
166 the LLL and MML structures (Fig. 3c,f) but is consistent with the inverse MMM , MMM , inverse
167 MLL , and MLL structures (Fig. 3a,b,d,e). In case of the inverse MMM and MMM structures
168 however, the charge distortions do not distinguish the neighboring kagome planes (i.e. $2\times 2\times 1$
169 structure) and cannot induce the out-of-plane band doubling observed on the $K1$ -vHS and $K2$ -band.
170 We thus conclude that the 3D-CO in KV_3Sb_5 , RbV_3Sb_5 , and Sn-doped CsV_3Sb_5 manifests in the
171 inverse MLL or MLL phases (intrinsically breaking C_6 -rotational symmetry) at variance with the
172 LLL structure in pristine CsV_3Sb_5 . This implies that despite the charge ordering tendency of the
173 kagome lattice is universal in AV_3Sb_5 family, the microscopic details of 3D-CO are strongly
174 dependent on the chemical composition and doping, adding to the rich physics that can be realized
175 in the AV_3Sb_5 series.

176 Lastly, we discuss the insights obtained from our results in relation to the existing literature.
177 Previous DFT calculations have revealed that the net energy of AV_3Sb_5 only marginally depends
178 on the out-of-plane structure of 3D-CO, indicating that the charge order is only weakly correlated
179 along the c -axis³⁵. It is thus quite possible that the detailed microscopic structure of 3D-CO varies
180 sensitively depending on the interlayer spacing or strength of the inter-kagome-layer interactions,
181 which can be controlled by the alkali metal element¹ or Sn-doping to Sb1 sites⁴². Intriguingly,
182 several DFT studies have predicted the MLL structure or Staggered TrH phase to be the ground
183 state of AV_3Sb_5 ^{29,33}, consistent with our conclusions for KV_3Sb_5 , RbV_3Sb_5 , and Sn-doped CsV_3Sb_5 .
184 In the case of pristine CsV_3Sb_5 , it is still being debated whether the 3D-CO manifests in the $2\times 2\times 2$
185 form as in the K and Rb counterparts, or in a more complicated $2\times 2\times 4$ pattern^{31,32}. Nevertheless,
186 the X-ray structural refinements on CsV_3Sb_5 revealed the modulation pattern containing an
187 alternating TrH and SoD structure without staggering³¹, in close analogy with the LLL structure
188 obtained here. We note that in CsV_3Sb_5 , signatures of bulk rotational symmetry breaking and
189 surface stripe order emerge only below the characteristic temperature $T_{SO} \approx 60$ K and not in the

190 pure charge-ordered state between $T_{\text{CO}} \approx 94$ K and $T_{\text{SO}} \approx 60$ K^{7,10}. This suggests that the 3D-CO
191 itself does not break C_6 rotational symmetry, which is indeed the case for the *LLL* structure
192 revealed in the present study (Fig. 1j). The nematicity and surface stripe order observed in CsV_3Sb_5
193 thus represent additional emergent electronic symmetry breaking under the 3D-CO state. In
194 contrast, we conclude that the C_6 rotational symmetry to be already broken in the 3D-CO phase of
195 $(\text{K,Rb})\text{V}_3\text{Sb}_5$ with the *MLL* or inverse *MLL* structure (Fig. 1k,l). Indeed, the Fourier-transformed
196 scanning tunneling spectroscopy on KV_3Sb_5 revealed that the symmetry of system is reduced to
197 C_2 in the charge-ordered state even without stripe ordering⁹. However, the phenomena of 3D-CO
198 and rotational symmetry breaking are much less explored in $(\text{K,Rb})\text{V}_3\text{Sb}_5$ compared to the Cs case
199 – the present results thus invite future X-ray diffraction, nuclear magnetic resonances, and
200 transport investigations on the full series.

201 In conclusion, we establish the microscopic structure of 3D-CO and its tunability in the
202 family of topological kagome metals $AV_3(\text{Sb,Sn})_5$. Determining the exact structure of 3D-CO is a
203 topic of great relevance, as it sets the background symmetry of the system under which other many-
204 body effects emerge. Combining high-resolution ARPES and DFT supercell calculations, we
205 resolve the detailed electronic reconstruction of the kagome bands in the 3D-CO state. We reveal
206 that the 3D-CO in CsV_3Sb_5 consists of a stacking of kagome layers with alternating SoD and TrH
207 distortions (*LLL*), while KV_3Sb_5 , RbV_3Sb_5 , and Sn-doped CsV_3Sb_5 realize the staggered CO
208 structure breaking the C_6 rotational symmetry (*MLL* or inverse *MLL*). The remarkable tunability
209 of the 3D-CO state across otherwise similar compounds suggests that the $AV_3\text{Sb}_5$ series is a
210 candidate host for an extremely rich phase diagram of emergent electronic phases, enabling new
211 opportunities for fundamental studies at the nexus of strong correlation phenomena and topology.

212 **Methods**

213 **Sample synthesis and angle-resolved photoemission spectroscopy**

214 High-quality single crystals of pristine and Sn-doped AV_3Sb_5 were synthesized via flux
215 method as described in Ref.^{1,2,42}. ARPES experiments were performed at Beamline 7.0.2
216 (MAESTRO) of the Advanced Light Source, equipped with R4000 hemispherical electron
217 analyzer (Scienta Omicron). The samples were cleaved inside an ultrahigh vacuum chamber with
218 a base pressure better than $\approx 4 \times 10^{-11}$ torr. We keep the following experimental geometry
219 throughout the measurement: horizontal analyzer slit, linear horizontal light polarization, and Γ -
220 K-M direction of the sample aligned to the scattering plane. For each sample, photon energy was
221 scanned from 60 eV to 200 eV, covering more than three complete three-dimensional Brillouin
222 zone. For the high-resolution data in Fig. 2,4, we selected the photon energies for each sample that
223 best visualize the band splitting. The energy and momentum resolutions were better than 20 meV
224 and 0.01 \AA^{-1} .

225

226 **Density functional theory calculations**

227 DFT calculations were performed using the Vienna Ab initio Simulation Package^{43,44}, with
228 GGA-PBE exchange-correlation functional⁴⁵ and the pseudo potential formalism based on the
229 Projector Augmented Wave method⁴⁶. The phonon frequency spectrum was derived from the
230 Hessian matrix (which encodes the second derivatives of the atomic position coordinate) computed
231 with the density-functional-perturbation theory (DFPT) method, using a $4 \times 4 \times 2$ supercell unit⁴⁷.
232 We have further simulated various $2 \times 2 \times 2$ CO states from combinations of the unstable M and L
233 phonon modes. The CO structures were relaxed with a 350 eV energy cutoff for the plane-wave
234 basis and a $4 \times 4 \times 2$ grid sampling in the momentum space Brillouin zone. To elucidate the electronic
235 properties of these COs, we performed electronic band structure unfolding and projections based
236 on the Wannier models derived from DFT ground states, using Wannier 90 code.

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251

252 **Author contributions**

253 M.K., J.-H.P, and R.C. conceived the project; M.K. and J.Y. performed the ARPES experiments
254 and analyzed the resulting data with help from S.H.R., J.K., C.J., A.B., and E.L.; S.F. performed
255 the theoretical calculations with help from E.K., J.C.; B.R.O., Y.M.O., and S.D.W. synthesized
256 and characterized the crystals. M.K. and R.C. wrote the manuscript with input from all coauthors.

257

258 **Data availability**

259 The datasets presented within this study are available from the corresponding authors upon
260 reasonable request.

261

262 **Competing interests**

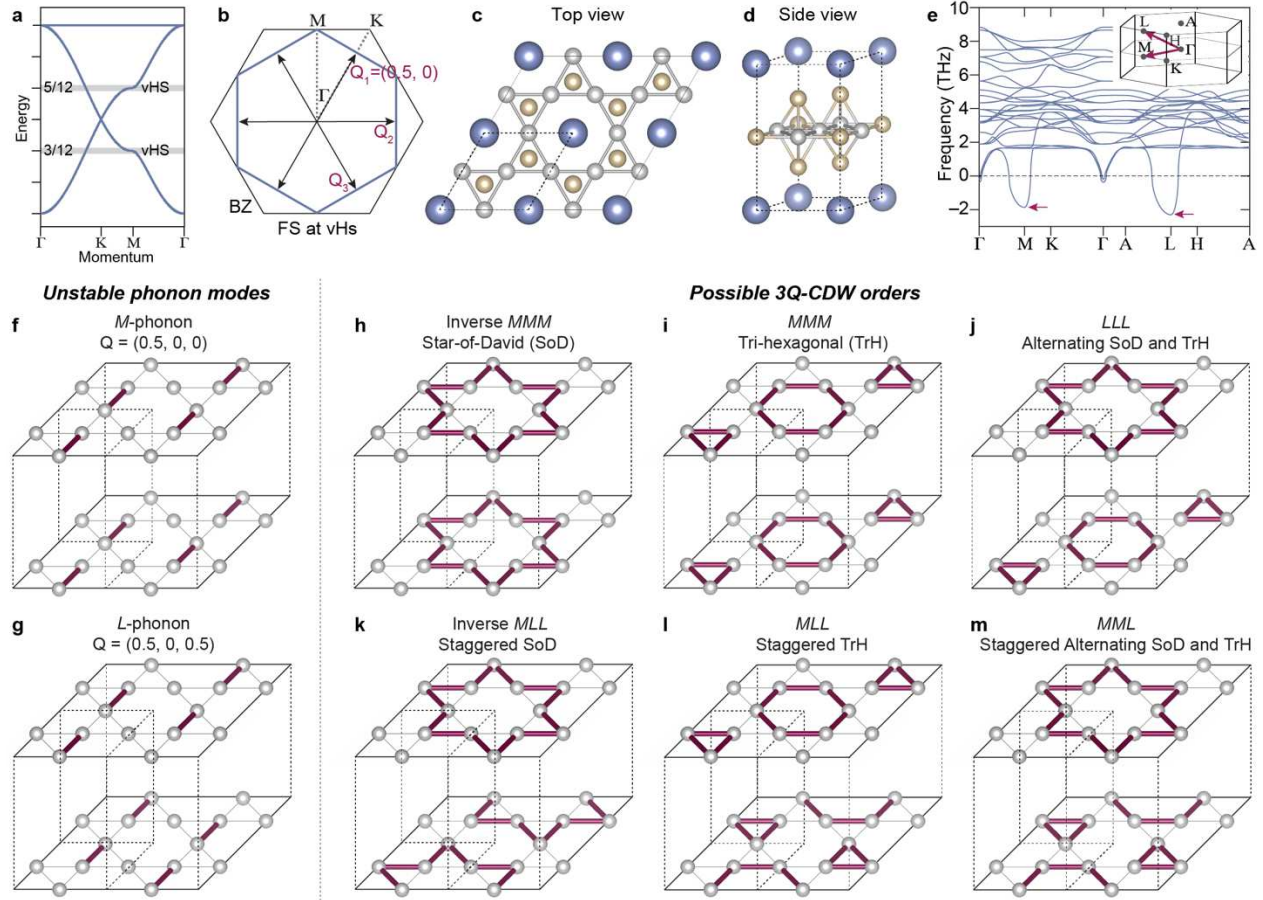
263 The authors declare no competing interests

264 **References**

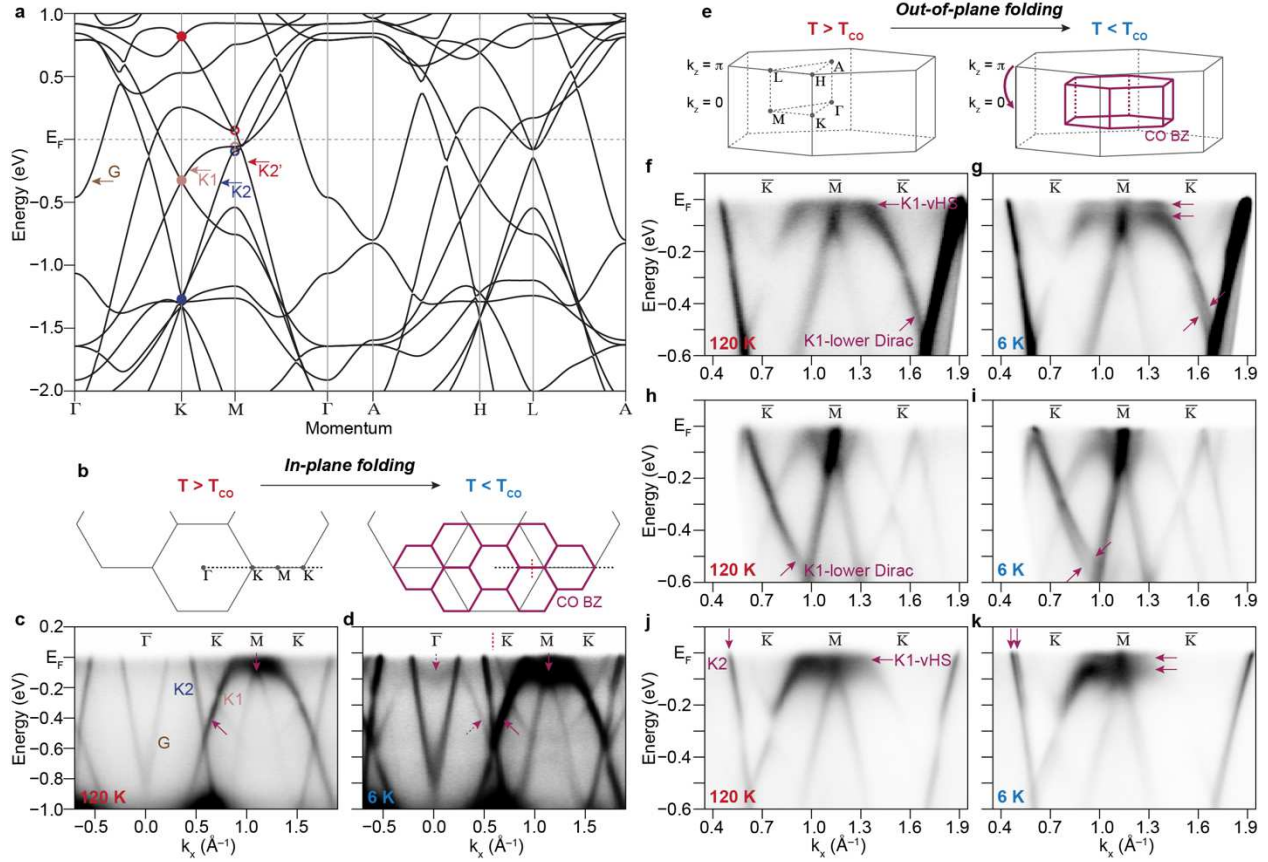
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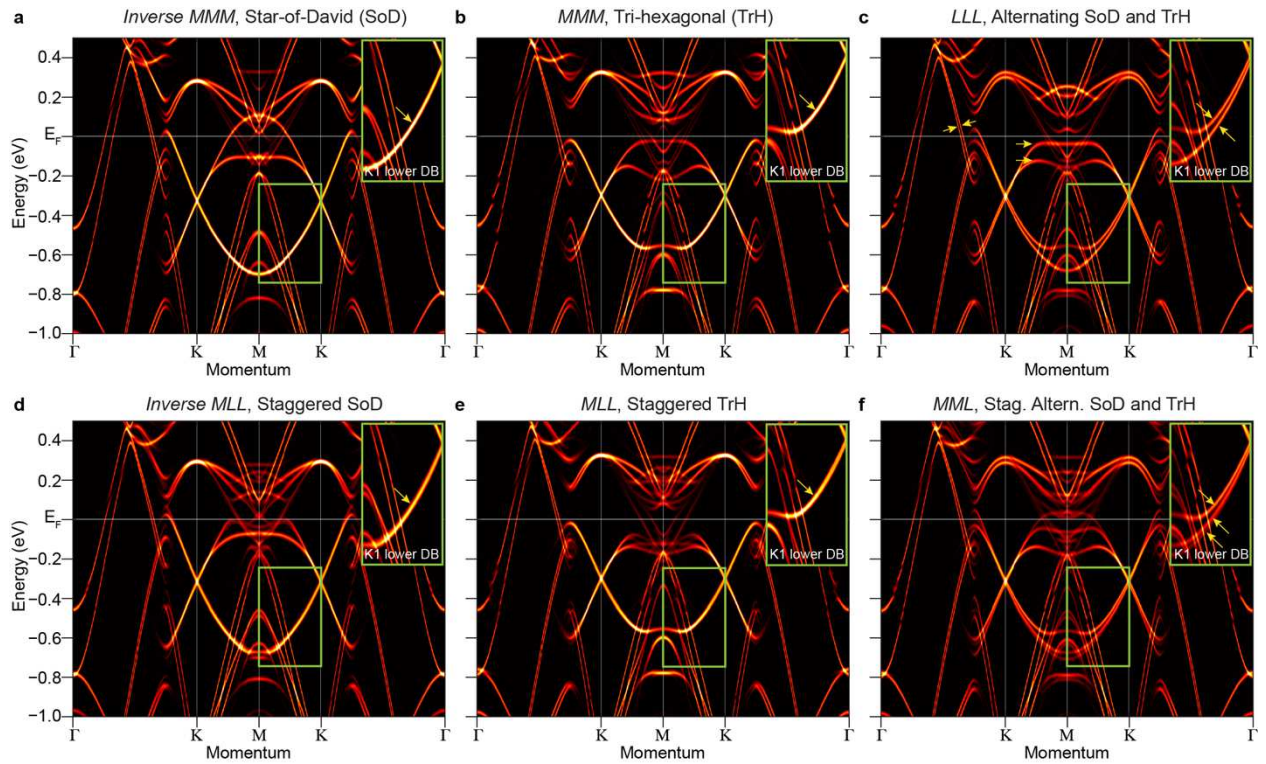
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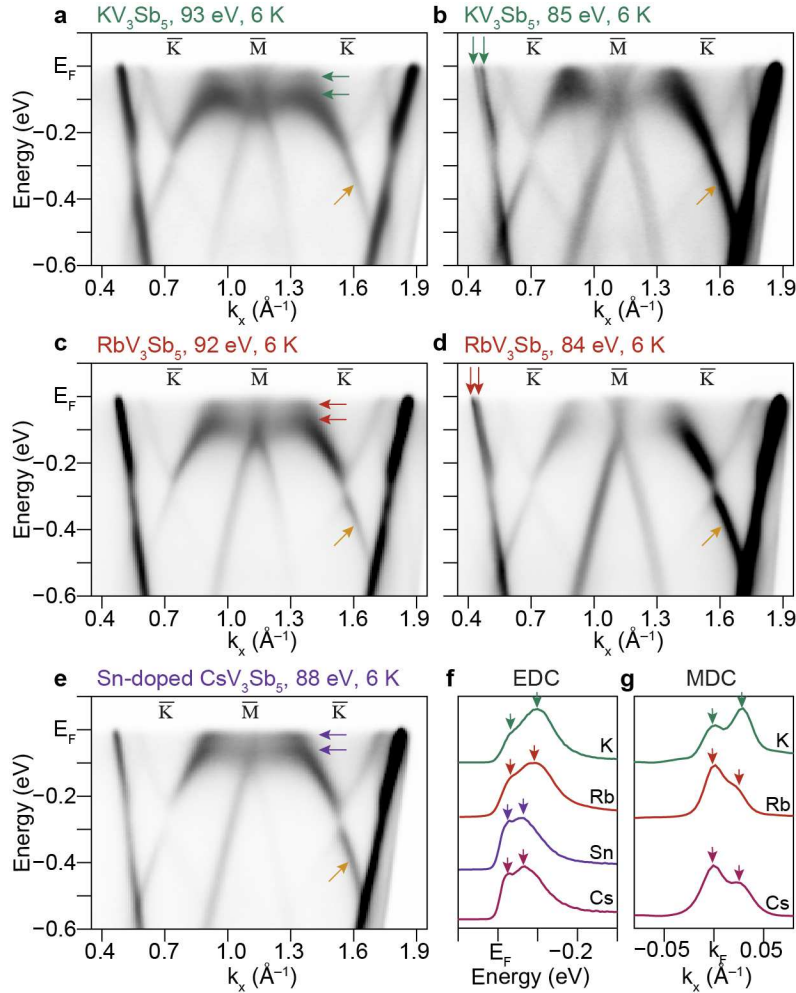
365 **Figure 1 | Possible microscopic structures of the three-dimensional charge order (3D-CO) in**
 366 **kagome metal AV_3Sb_5 .** **a**, Tight-binding electronic structure of an ideal kagome lattice. Grey-
 367 shaded lines mark the vHS filling fractions at 3/12 and 5/12. **b**, Perfectly nested hexagonal Fermi
 368 surface of the kagome lattice at the vHS filling fractions. Double-headed arrows indicate three
 369 symmetry-equivalent nesting vectors Q_1 , Q_2 , and Q_3 . **c,d**, Crystal structure of the AV_3Sb_5 with a
 370 V-kagome net. Dashed lines mark the unit cell in the undistorted phase. **e**, Calculated phonon
 371 dispersion of CsV_3Sb_5 showing instabilities of the pristine structure at M and L . Inset shows the
 372 Brillouin zone. **f,g**, Lattice distortions corresponding to the instabilities at M and L phonons,
 373 respectively. **h-m**, Possible structures of the 3D-CO in AV_3Sb_5 based on 3 Q -combinations of the
 374 M and L phonons.



375 **Figure 2 | Two distinct types of electronic reconstructions in CsV₃Sb₅ induced by 3D-CO.** **a,**
 376 DFT band structure of CsV₃Sb₅ showing four bands crossing the Fermi level: *G*, *K1*, *K2*, and *K2'*-
 377 bands. The Dirac points at *K* and vHS at *M* emerging from the *K1*, *K2*, and *K2'* kagome bands are
 378 marked with filled and open circles, respectively. **b-d,** Electronic reconstruction from the in-plane
 379 component of charge order. **b,** Schematics of the in-plane folding of the Brillouin zone. **c,d,**
 380 Experimental band dispersion of CsV₃Sb₅ measured at 120 K and 6 K (above and below T_{CO}),
 381 respectively. Solid arrows in c,d mark the original bands, while the dashed arrows in d indicate the
 382 replica bands. **e-k,** Electronic reconstruction from the out-of-plane component of 3D-CO. **e,**
 383 Schematics of the out-of-plane folding of the Brillouin zone. Panels f,h,j (g,i,k) represent the
 384 dispersions measured above (below) T_{CO}, at the first Brillouin zone with photon energy 86 eV, at
 385 the second Brillouin zone with photon energy 86 eV, and at the first Brillouin zone with photon
 386 energy 113 eV, respectively. Solid arrows in g,i,k indicate the doubling or splitting of the kagome
 387 bands in the 3D-CO state.

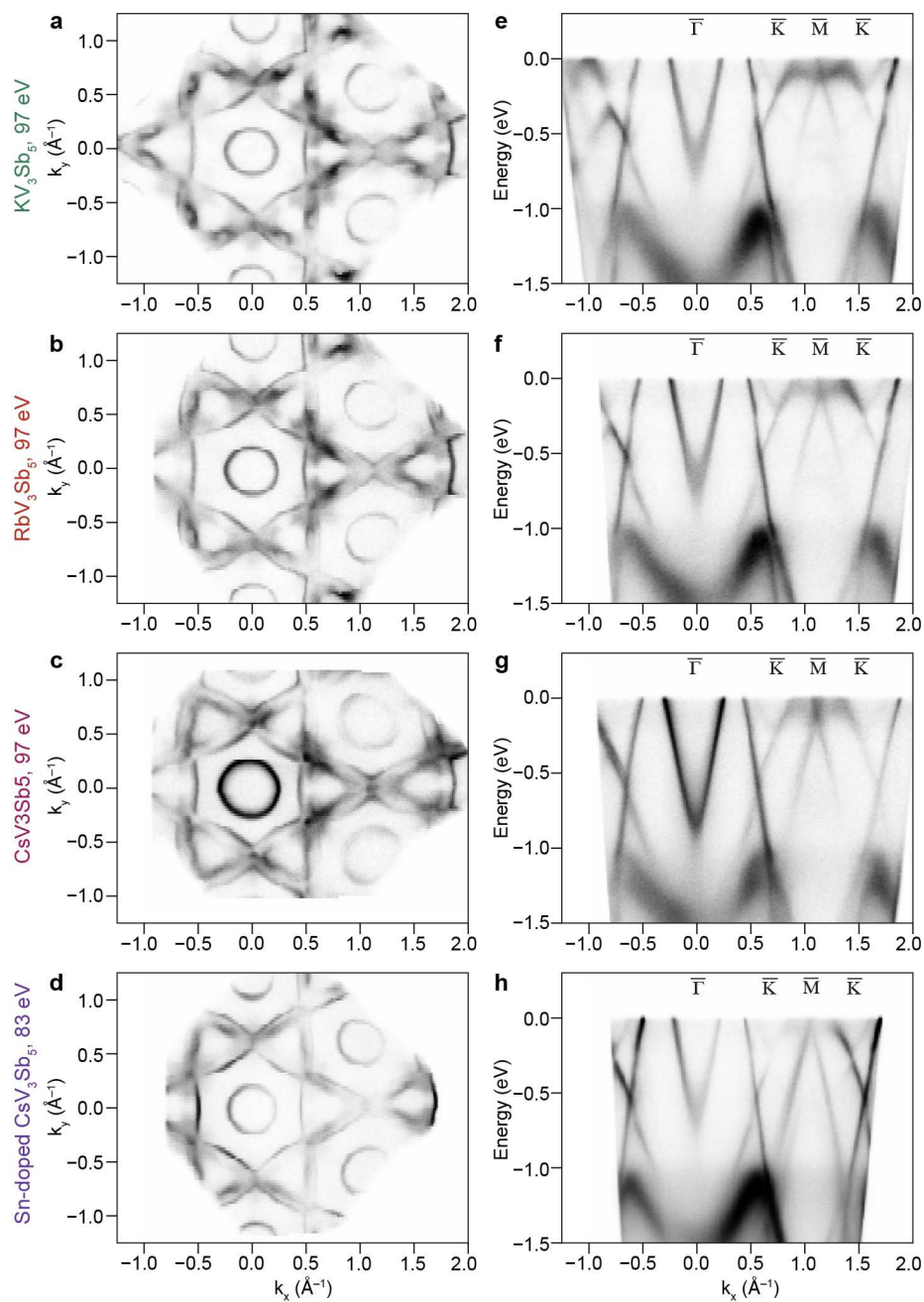


388 **Figure 3 | Theoretical calculation of electronic reconstruction in AV_3Sb_5 and its dependence**
 389 **on the microscopic structure of 3D-CO. a-f,** Calculated dispersion of CsV_3Sb_5 at $k_z = 0$ in the
 390 inverse *MMM*, *MMM*, *LLL*, inverse *MLL*, *MLL*, and *MML* phases, respectively. For simplicity, the
 391 dispersion is unfolded along the in-plane momentum direction. Yellow arrows in c highlight the
 392 splitting of *K1* and *K2* bands in the 3D-CO state. For the inverse *MLL*, *MLL* and *MML* phases (d-
 393 f) the calculation is averaged over three C_2 symmetric charge order domains to account for the
 394 macroscopic beam spot size. Corresponding domain-resolved dispersions are presented in the
 395 Extended Data Fig. 2. The insets zoom in the behavior of the lower *K1* Dirac band, whose splitting
 396 sensitively depends on the microscopic structure of 3D-CO (see yellow arrows).

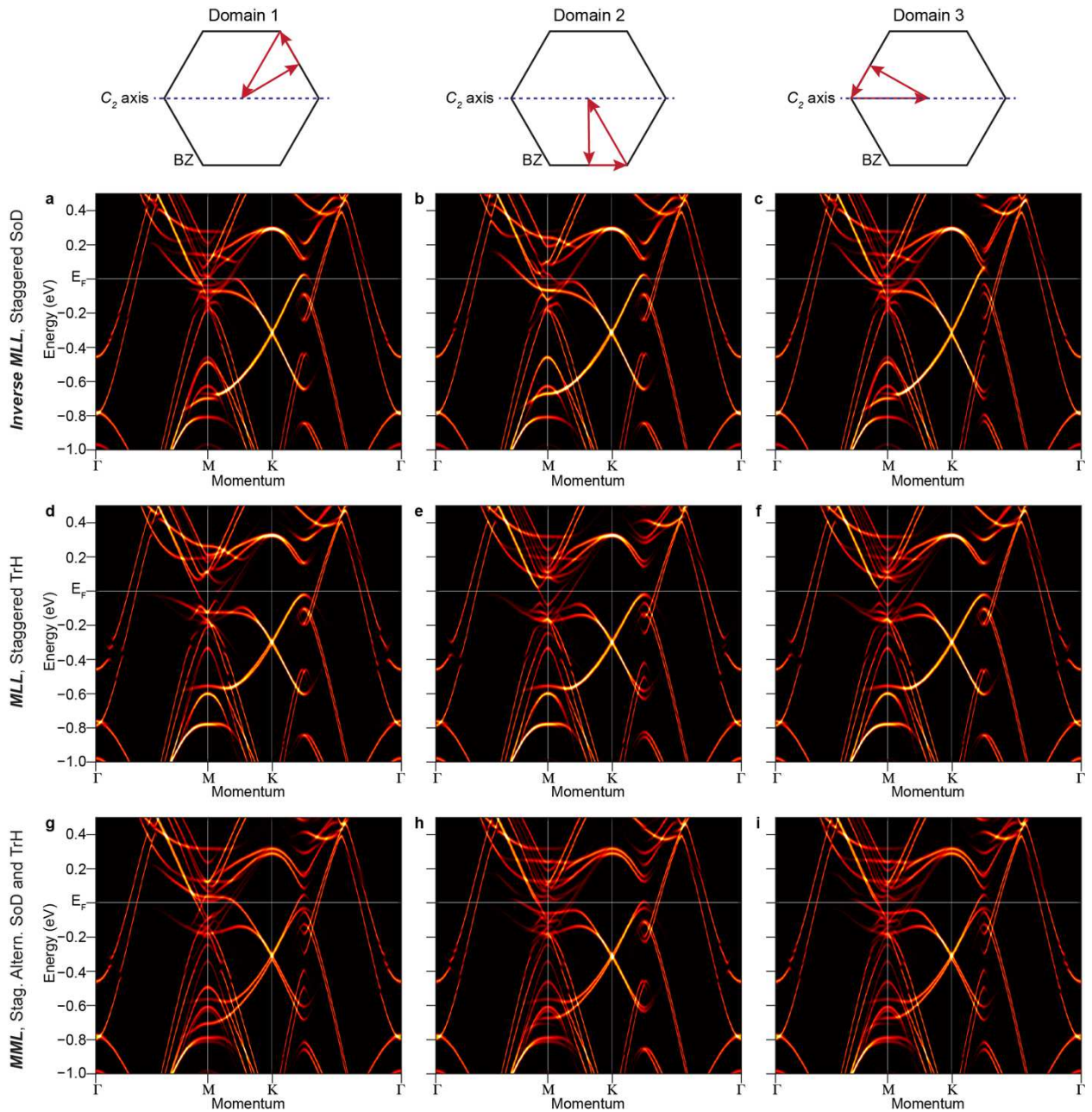


397 **Figure 4 | Electronic reconstructions in KV_3Sb_5 , RbV_3Sb_5 , and Sn-doped CsV_3Sb_5 in 3D-CO**
 398 **state. a-e**, ARPES spectra of KV_3Sb_5 (a,b) RbV_3Sb_5 (c,d), and Sn-doped CsV_3Sb_5 (e) measured at
 399 6 K. The spectra in a-e are collected with 93 eV, 85 eV, 92 eV, 84 eV, and 88 eV photons,
 400 respectively. Green, red, and purple arrows indicate the splitting of $K1$ -vHS and $K2$ -band.
 401 Corresponding energy-distribution-curves (EDCs) and momentum-distribution curves (MDCs)
 402 are shown in f,g (see below). Yellow arrows highlight the absence of splitting on the lower Dirac
 403 band of $K1$, which is markedly different from the case of CsV_3Sb_5 in Fig. 2g,i. **f**, EDCs measured
 404 near the Fermi momentum (k_F) of the $K1$ -band. Arrows highlight the splitting of $K1$ -band near
 405 vHS. **g**, MDCs of the $K2$ -band measured at the Fermi energy (E_F). Arrows highlight the splitting
 406 of the $K2$ -band.

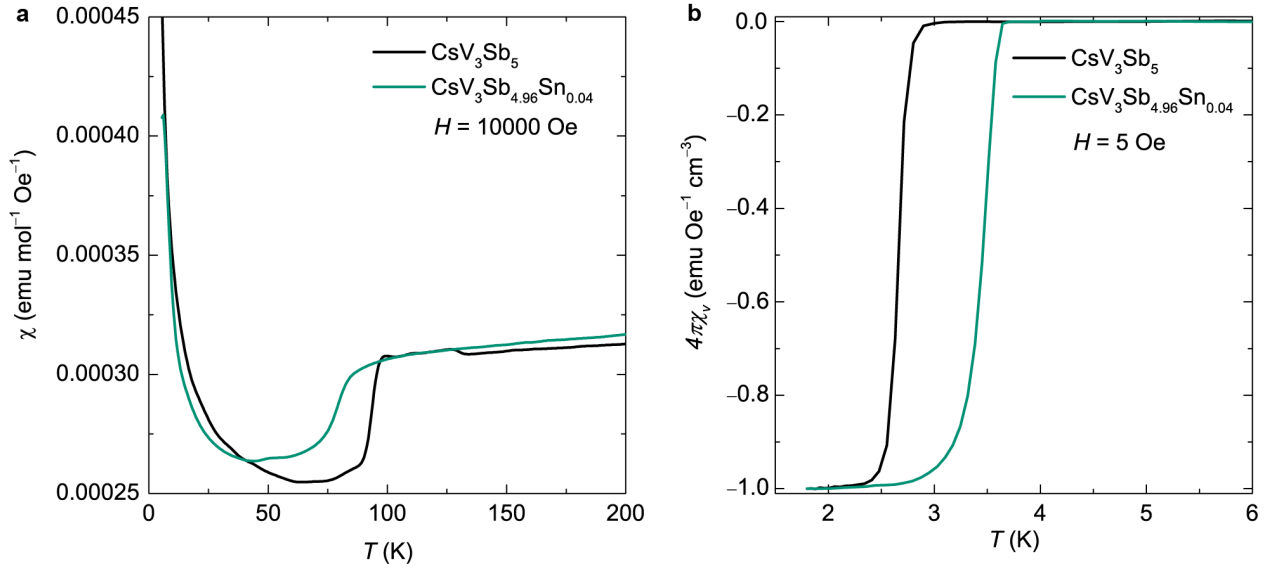
Extended Data Figures 1-3



407 **Extended Data Fig. 1 | Fermi surface and overall electronic structure of pristine and Sn-**
 408 **doped AV_3Sb_5 ($A = K, Rb, Cs$).** **a-d**, Fermi surfaces of KV₃Sb₅, RbV₃Sb₅, CsV₃Sb₅ and Sn-doped
 409 CsV₃Sb₅, respectively. **e-h**, Wide energy-momentum range ARPES spectra of KV₃Sb₅, RbV₃Sb₅,
 410 CsV₃Sb₅ and Sn-doped CsV₃Sb₅, respectively. All data are acquired at the base temperature 6 K,
 411 i.e. in the charge ordered state.



412 **Extended Data Fig. 2 | Domain-resolved electronic structures of CsV_3Sb_5 in C_2 symmetric**
 413 **3D-CO phases. a-c, Domain-resolved dispersion of CsV_3Sb_5 in the inverse MLL 3D-CO phase.**
 414 The location of three different k -paths with respect to the C_2 rotation axis is schematically
 415 displayed above each panel. **d-f, Same with a-c but in the MLL phase. g-i, Same with a-c but in**
 416 **the MML phase. Corresponding domain-averaged electronic structures of the inverse MLL , MLL ,**
 417 **and MML phases are shown in Fig. 3d-f.**



418 **Extended Data Fig. 3 | Characterization of the Sn-doped CsV₃Sb₅ single crystal.** **a**, Magnetic
 419 susceptibility of the pristine and Sn-doped CsV₃Sb₅ measured under a field of $H = 10000 \text{ Oe}$. Sn
 420 concentration (0.04 per unit cell) is determined by energy-dispersive X-ray spectroscopy. The
 421 sharp drop in the magnetic susceptibility characterizes the onset of the charge order. With Sn-
 422 doping, the T_{CO} decreases from 94 K to 79 K. **b**, Low-temperature magnetic susceptibility
 423 measured under a field of $H = 5 \text{ Oe}$. The perfect diamagnetic response ($4\pi\chi_v = -1$) characterizes
 424 the superconducting state. With Sn-doping, the superconducting transition temperature T_C
 425 increases from 2.7 K to 3.4 K (estimated from the midpoint of transition), indicating a competition
 426 between superconductivity and charge order in Sn-doped $AV_3\text{Sb}_5$ series.⁴²