

# Charts of spatial noise distribution in planer resistors with finite contacts

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Thomson University of Technology  
Rabat, Morocco

Department of Electrical Engineering

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CHARTS OF SPATIAL NOISE  
DISTRIBUTION IN PLANAR RESISTORS  
WITH FINITE CONTACTS

by

A.H. de Kuijper and L.K.J. Vandamme

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E I N D H O V E N U N I V E R S I T Y O F T E C H N O L O G Y

Department of Electrical Engineering

Eindhoven

The Netherlands

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## CHARTS OF SPATIAL NOISE DISTRIBUTION IN PLANAR RESISTORS WITH FINITE CONTACTS

A.H. de Kuijper and L.K.J. Vandamme,  
Eindhoven University of Technology,  
Department of Electrical Engineering,  
Eindhoven, Netherlands.

### Abstract

Calculations and experimental results are presented of the voltage and the voltage fluctuations across a pair of sensor electrodes on a planar resistor. A constant current is passed through another pair of driver electrodes. Three types of geometry are considered all of which are invariant for rotations of 90 degrees. Areas of low and high contributions to the voltage fluctuations are calculated assuming homogeneous conductivity fluctuations. Sixty-six spatial noise distribution charts are presented. The noise parameter of conductance fluctuations in films can be calculated from experimental results under different measuring conditions and for different geometries. The calculation method rests on the sensitivity theorem in electrical network. Calculations are in agreement with experimental results.

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## Introduction

A general expression has been derived for the spectral noise density of the voltage fluctuations between two arbitrarily shaped sensor electrodes placed arbitrarily on a two-dimensional conductor for the case that a constant current is applied to another pair of arbitrarily shaped and positioned driver electrodes [1,2].

The current is assumed to be noise-free. The voltage fluctuations across the sensor electrodes are caused by homogeneous resistivity fluctuations. This report comprises calculations with regard to the noise and the noise distribution in two-dimensional conductors with a geometry as shown in Figs. 1a, 1b and 1c.

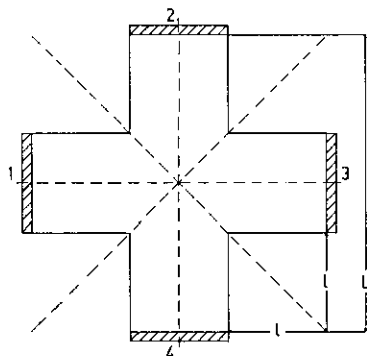


Fig. 1a

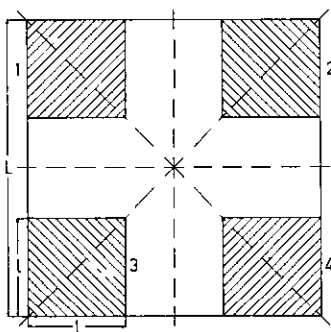


Fig. 1b

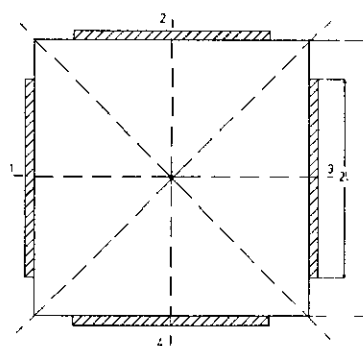


Fig. 1c

All figures: // : ideal contacts

Fig. 1a: Cross-shaped planar resistor with 4 contacts.

Fig. 1b: Square-shaped planar resistor with 4 corner contacts.

Fig. 1c: Square-shaped planar resistor with 4 side contacts.

The samples are invariant for rotations of 90 degrees. We calculated the noise power at the sensor electrodes and the spatial noise distribution for various  $2L/l$  ratios and various connections of the current source and sensor to the contacts. The noise consists of a thermal noise term and a conduction noise term. The thermal noise is proportional to the resistance between the sensor electrodes. When a constant current is passed through the sample, the conductivity fluctuations cause electric field fluctuations, which can be observed either on the sensor electrodes, the driver electrodes or across one driver and one sensor electrode. The conduction noise term is proportional

to the square of the current  $I$  passed through the sample. Here we consider noise due to conductivity fluctuations.

### 1. Calculation of the noise power density $S_v$ .

We assume the material to be homogeneous. The statistical properties of the conductivity fluctuations are also assumed to be homogeneous. The driver and sensor electrodes are assumed to be ideally conducting. The calculations have been developed from a purely macroscopic point of view without any reference to the origin and particular properties of the spectrum of the conductance fluctuations.

To obtain numerical results we carried out calculations on a network that simulated a two-dimensional conductor. This network consists of horizontal and vertical resistors, all having the same value, a current source and resistors to simulate the contacts. The current source was connected to a pair of driver electrodes  $D$ , and the voltage fluctuations were calculated on a pair of sensor electrodes  $Q$ . The first order sensitivity  $\delta V_Q / \delta R$  was calculated by using the adjoint network [3,4]. In our case the adjoint network was obtained only by changing sensor and driver electrodes. The sensitivity of the voltage changes across the sensors in the original network due to a small change in a resistor  $R$  at an arbitrary place in the network is then given by the first order sensitivity

$$\frac{\delta V_Q}{\delta R} = \frac{i \tilde{i}}{I} \quad (1)$$

where  $i$  is the current through that resistor in the original network,  $\tilde{i}$  is the current through the same resistor in the adjoint network and  $I$  is  $1A$ . We shall only consider the first-order sensitivities given by (1).  $\delta V_Q / \delta R$  is proportional to  $I$ , because  $i$  and  $\tilde{i}$  are proportional to  $I$ .

To calculate the total squared average voltage fluctuations  $\langle (\delta V_Q)^2 \rangle$ , we divide the network in equal squares, each having the same properties in the  $x$  and  $y$  directions. Fig. 2 gives some possibilities of connecting the resistors inside such squares.

The possibilities denoted by 2 and 3 inside the dotted line in fig. 2 have the drawbacks that they strongly increase the number of nodes and the number of resistors. Therefore, we chose the representation denoted by 1 and called it the "L-form" square of unit area. In ref. [1] it is demonstrated that the total average of the squared voltage fluctuations  $\langle (\delta V_Q)^2 \rangle$  is

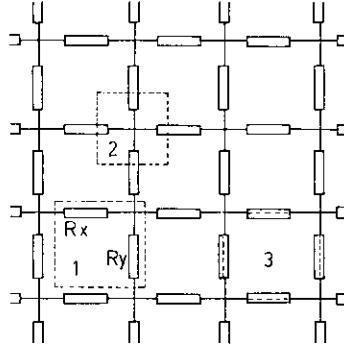


Fig. 2: The lumped network model of a planar resistor showing three possible representations of a unit area A by resistors.

$$\langle (\Delta V_Q)^2 \rangle = \frac{\langle (\Delta R)^2 \rangle}{I^2} \sum_{\text{all squares}} [i_x \tilde{i}_x + i_y \tilde{i}_y]^2 \quad (2)$$

where  $i_x, i_x$  and  $i_y, i_y$  are the currents and adjoints currents through  $R_x$  and  $R_y$  of an "L-form" area.  $\langle (\Delta R)^2 \rangle$  stands for the variance of the resistance fluctuations in  $R_x$  and  $R_y$ . The sum in (2) must be taken over all squares of the network. Since the network is purely resistive, the method applies to frequency as well as time domain calculations. The spectral noise power density  $S_Q$  is the variance of the filtered fluctuations at frequency  $f$  per Hz bandwidth.

$$S_Q = \frac{\langle (\Delta V_Q)^2 \rangle}{\Delta f} = \frac{\langle (\Delta R)^2 \rangle}{I^2 \Delta f} \sum_{\text{all squares}} [i_x \tilde{i}_x + i_y \tilde{i}_y]^2 \quad (3)$$

Now  $\langle (\Delta V_Q)^2 \rangle$  and  $\langle (\Delta R)^2 \rangle$  stands for the variance of the filtered fluctuations at frequency  $f$  in a bandwidth  $\Delta f$ . The simulation computer program we used provides a d.c. analysis and a first order sensitivity analysis of each network element with respect to a selected pair of nodes  $Q$ . We then denote the added and squared sensitivity  $L_s$  inside on "L-shape" as

$$L_s = (i_x \tilde{i}_x + i_y \tilde{i}_y) / I^2 \quad (4)$$

because, owing to the homogeneous statistical noise properties,  $\langle (\Delta R)^2 \rangle$  is the same for all squares in the conductor, and  $S_Q$  equals  $\langle (\Delta R)^2 \rangle (\sum L_s) / \Delta f$ .



## 2. Spatial noise distribution

As the simulation program provides the sensitivity  $\frac{\delta V_Q}{\delta R}$  of each resistor, it gives us the opportunity to study the noise distribution in the conductor. Therefore, we divided the value of  $L_s$  of each "L-form" area into four classes.

class 1:  $L_s < M/5$

class 2:  $L_s < M/2$

class 3:  $L_s > 2*M$

class 4:  $L_s > 5*M$

where  $M$  is the average value of  $L_s$ . In order to find the areas with a large or a small contribution to the noise at the sensors, we programmed the computer to plot the "L-form" areas if their representing  $L_s$  values fall in one of the classes 1 and 4. This gives a picture of the spatial noise distribution. Three examples of such pictures are given in fig. 3, fig. 4 and fig. 5. The total of the  $L_s$  values belonging to class 1 is smaller than that of class 2, and the total of the  $L_s$  values belonging to class 4 is smaller than that of class 3.

For instance, the horizontally hatched areas around the contacts  $D, Q$  in fig. 3 are together about 5 per cent of the total surface while their contribution to the total noise power  $S_Q$  is 82 per cent. The vertically hatched area, however, is about 65 per cent of the total surface and its contribution to  $S_Q$  is only 2 per cent.

When sensor and current electrodes coincide as in fig. 3, we see that, because  $S_Q \propto \Sigma (i_x^2 + i_y^2)^2$ , areas with a high current density give the largest contribution to the total noise power. As can be seen in fig. 3, such areas are around the current carrying electrodes.

Fig. 4 shows a three probe and fig. 5 a four-probe problem. Next to these figures are denoted the percentages of the total noise contributed by each class. Fig. 5 is a good example to demonstrate that neither  $i$  nor  $\tilde{i}$  is dominant for the total noise but the dot product  $(i_x \cdot \tilde{i}_x + i_y \cdot \tilde{i}_y)$  is. At the contacts  $D_1, D_2$  the adjoint current density is almost zero, and at  $Q_1, Q_2$  the current density is almost zero. In the centre of the cross,  $i$  and  $\tilde{i}$  are large, but  $i \cdot \tilde{i}$  is negligibly small due to the fact that  $i$  is almost perpendicular to  $\tilde{i}$ .

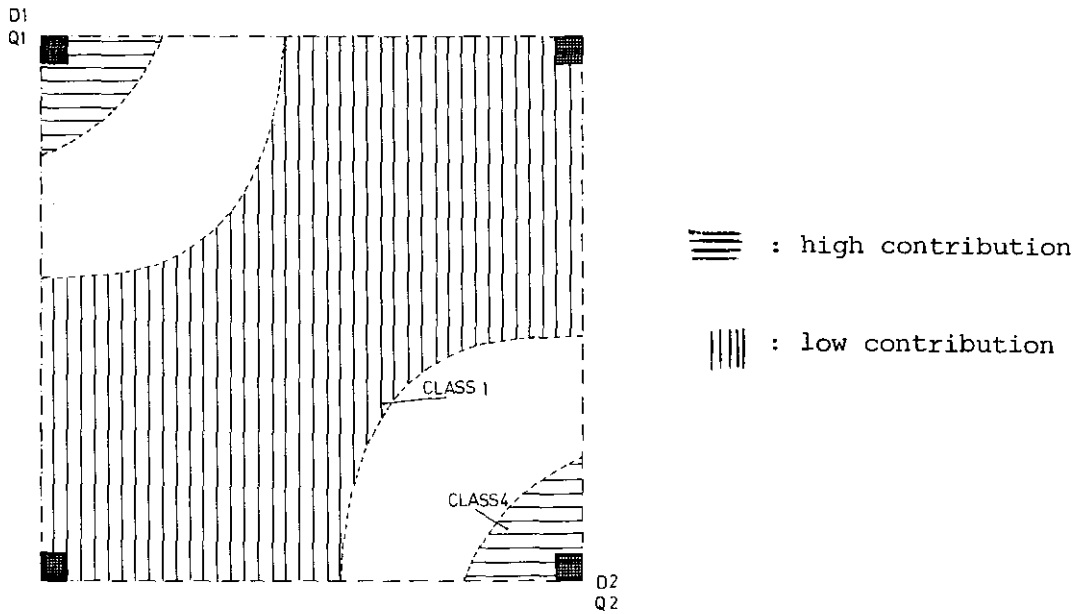


Fig. 3: Spatial noise distribution in a two-contact arrangement

	each $L_s$	total area contribution
class 1	< 0.2 M	2 %
class 2	< 0.5 M	5 %
class 3	> 2 M	90 %
class 4	> 5 M	82 %

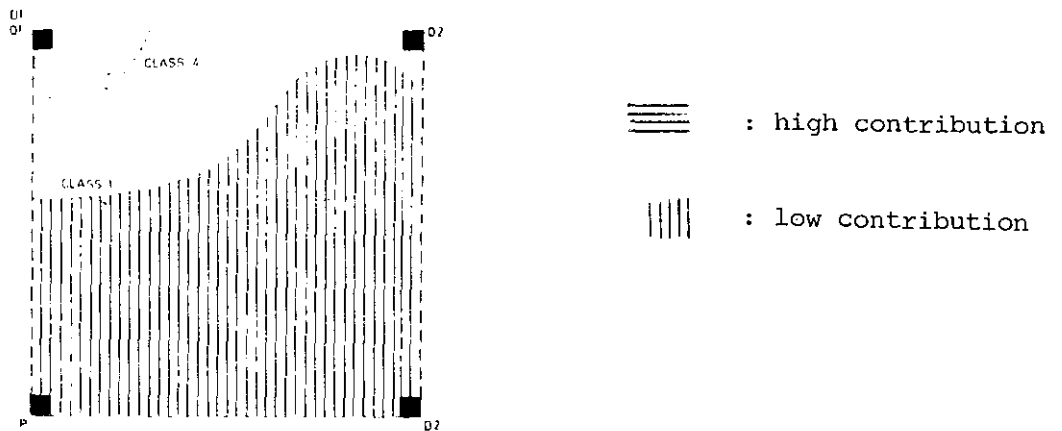


Fig. 4: Spatial noise distribution in a three-contact arrangement

	each $L_s$	total area contribution
class 1	< 0.2 M	2 %
class 2	< 0.5 M	3 %
class 3	> 2 M	92 %
class 4	> 5 M	87 %

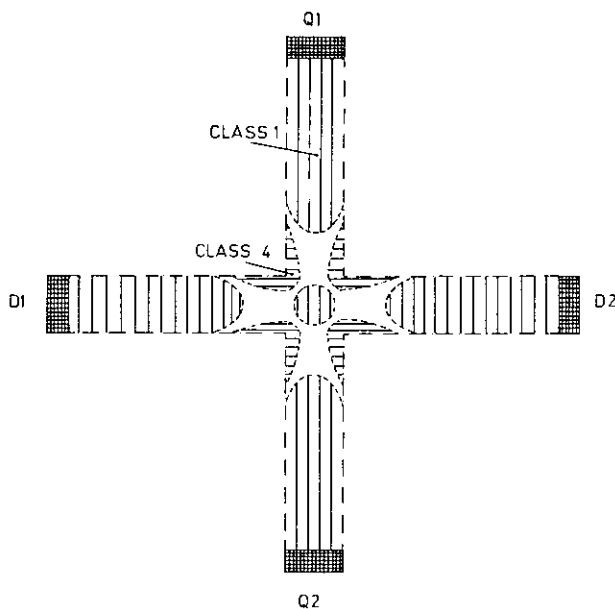


Fig. 5: Spatial noise distribution in a four-contact arrangement

	each $L_s$	total area contribution
class 1	$< 0.2 M$	0.3 %
class 2	$< 0.5 M$	4 %
class 3	$> 2 M$	96 %
class 4	$> 5 M$	84 %

A survey of the spatial noise distribution of 2, 3 and 4-point situations for various  $2l/L$  ratios of the geometries in Figs.1a and 1b is given in Appendix B.

### 3. Comparison between experimental results and calculations

We calculated the noise power in the situations given in fig. 1 and checked some of them with  $1/f$  noise on carbon sheet resistors. The geometry of the samples of fig. 1 was varied from  $2l/L = 0.1$  to  $2l/L = 0.9$ . For  $1/f$  conductivity fluctuations across a square with sheet resistance  $R_{\square} (\Omega)$  and a surface  $A$  corresponding to the area of the "L-form" (representing a square of unit area) and submitted to a homogeneous field, we use [6]

$$\left\langle \left( \frac{\Delta R}{R_{\square}} \right)^2 \right\rangle = C \frac{\Delta f}{f} = \frac{C_{us}}{A} \frac{\Delta f}{f} \quad (5)$$

where  $C$  and  $C_{us}$  are the relative  $1/f$  noise power density at 1 Hz for the whole conductor and for a unit square respectively,  $\Delta f$  is the bandwidth of the

filter at frequency  $f$ . Owing to a discretisation of 20 or 18 resistors for a length  $L$ ,  $A$  equals  $L^2/K$  in our computer simulation.  $K$  is the number of "L-shape" areas in a square with side  $L$ . For fig. 1a and fig. 1c  $K$  equals 340; for fig. 1b  $K$  equals 420.

Using (3), (4) and (6) we find

$$S_Q = \frac{R_{\square}^2 C_{us}}{I^2 f A} \sum_{\text{all squares}} (i_x \tilde{i}_x + i_y \tilde{i}_y)^2 = \left( \frac{I_e}{I} \right)^2 \frac{R_{\square}^2 C_{us} K}{f L^2} \Sigma L_s \quad (6)$$

and, in case sensor and driver electrodes coincide,

$$S_D = \frac{R_{\square}^2 C_{us}}{I^2 f A} \sum_{\text{all squares}} (i_x^2 + i_y^2)^2 = \left( \frac{I_e}{I} \right)^2 \frac{R_{\square}^2 C_{us} K}{f L^2} \Sigma L_s \quad (7)$$

The  $L_s$  are presented in table 1 (p.15 to 21. incl.).

We compared the calculated ratio  $S_Q/S_D$  with the experimental  $S_Q/S_D$  ratio found on carbon paper. The results of measured and calculated ratios as a function of the  $2l/L$  ratio for the various four-probe situations are plotted in figs. 6 to 9. The results show good agreement.

To compare the absolute values of  $S$  we have to standardize the  $L_s$  values which have been calculated for  $I = 1A$  to experimental current  $I_e$ . Various results are presented in table 1 in Appendix A. The difference in calculated and experimental results is mainly due to anisotropy and spreading in the carbon sheet resistivity. Calculations for anisotropic conductors are discussed in chapter 4 and in tables 2 and 3 of Appendix A.

The experimentally obtained results of  $S_Q$  on a sample geometry of fig. 1 can be analyzed in terms of  $C_{us}$ . Knowing  $l$ ,  $L$ , and  $I_e$  and measuring  $R_{\square}$  and  $S_Q$  at a certain frequency  $f$ , the value of  $C_{us}$  can be calculated using eq. (6) or (7) and the calculated sum of  $L_s$  presented in table 1 in Appendix A. There the  $\Sigma L_s$  are presented for two- three- and four-probe arrangements on samples with a geometry given by fig. 1.

It is our experience that a sample can be considered to be two-dimensional, if the thickness  $\delta$  of the film (such as the epitaxial layer or the diffused or implanted impurity layer) is below  $L/20$ . For non-granular samples,  $C_{us}$  equals  $\alpha/N_I$ , with  $N_I$  the surface concentration ( $m^{-2}$ ) of the free charge carriers in the sample, and  $\alpha$  a dimensionless constant of the order of  $10^{-3}$  [5].

For granular structures such as used in thick-film resistors  $C_{us}$  is dominated by the noise at the contacts between grains [6].

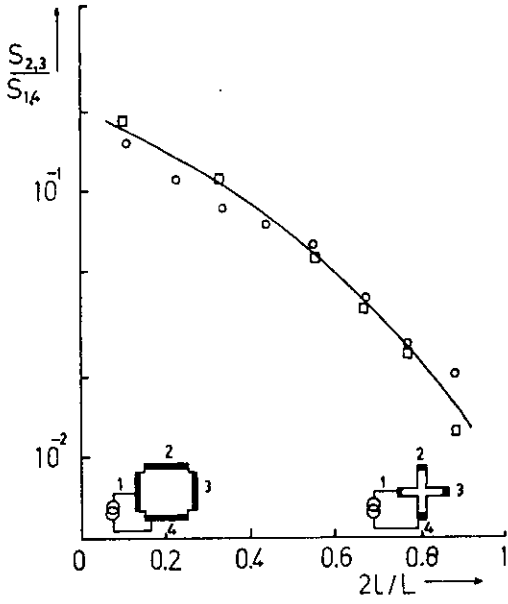


Fig. 6:  $S_Q/S_D$  ratios as a function of  $2l/L$  for a cross-shaped sample with  $\langle v_Q \rangle \neq 0$

□ : calculated  
○ : experimentally observed results

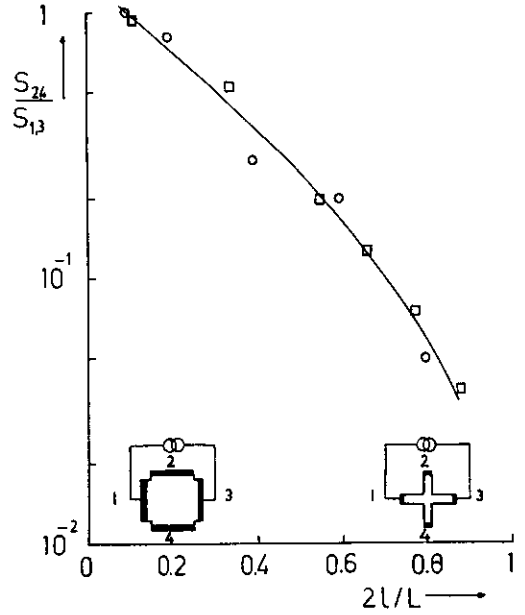


Fig. 7:  $S_Q/S_D$  ratios as a function of  $2l/L$  for a cross-shaped sample with  $\langle v_Q \rangle = 0$

□ : calculated results  
○ : experimentally observed results

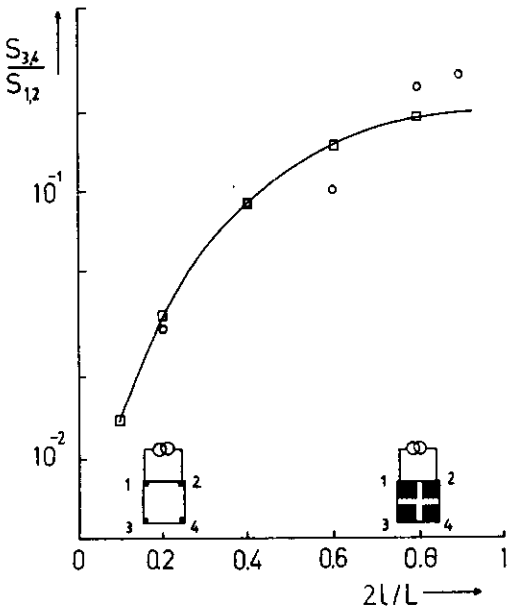


Fig. 8:  $S_Q/S_D$  ratios as a function of  $2l/L$  for square-shaped samples with four corner contacts and  $\langle v_Q \rangle \neq 0$

□ : calculated results  
○ : experimentally observed results

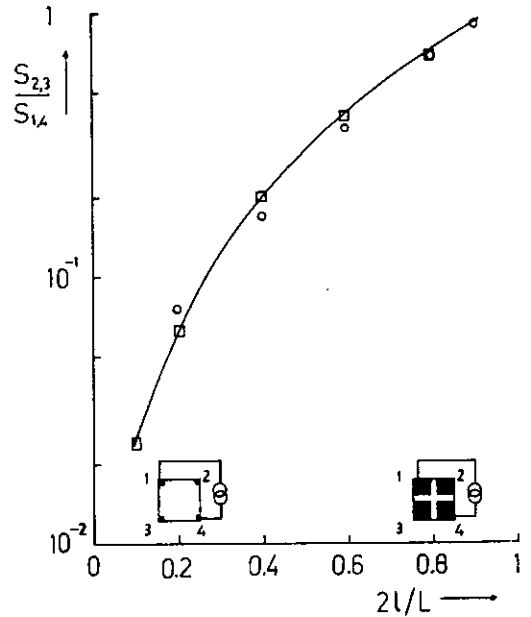


Fig. 9:  $S_Q/S_D$  ratios as a function of  $2l/L$  for square-shaped samples with four corner contacts and  $\langle v_Q \rangle = 0$

□ : calculated results  
○ : experimentally observed results

#### 4. Anisotropy

In some cases in table 1 in Appendix A there is a difference between calculated and observed  $S_Q$  values. Part of these differences is caused by an anisotropy of the carbon sheet resistor of about 25 per cent. Another part is due to some inhomogeneities in the sheet resistor characteristics such as  $R_{\square}$  and  $C_{us}$ . To investigate this anisotropy numerically, we replaced all vertical resistors of the network by resistors of  $1.25\Omega$  instead of  $1\Omega$ . The effect was losses of symmetry. The samples no longer are invariant for rotation of  $90^\circ$  degrees.

Table 2 of Appendix A shows calculated results for the geometry of fig. 1b with the current source connected to contacts (1, 2) and to contacts (1, 3). If there is no anisotropy, there is no difference between the columns  $D_{12}$  and  $D_{13}$  and the results are equal to the results presented in table 1. Table 2 shows difference when the anisotropy is 25 per cent. Further we compared situations with anisotropy with their corresponding situations without anisotropy.

Table 3 of Appendix A shows the results. As can be seen, differences of factor two are possible. So the anisotropy is a reasonable explanation of differences between observed and calculated results in table 1 of Appendix A. Note that the influence of anisotropy strongly depends on terminal shape and geometry.

#### 5. Discretisation error

If the discretisation is smaller, the number of resistors increases and the currents  $i$  and  $\tilde{\gamma}$  become smaller, while  $\Sigma L_s$  also becomes smaller. However, the ratio  $(\Sigma L_s)/A$  remains about constant if the discretisation is small enough.

In order to investigate the discretisation error we modelled fig. 1c twice.

1. The total length  $L$  simulated by 12 resistors.
2. The total length  $L$  simulated by 18 resistors.

We choose fig. 1c because this is the most sensitive geometry to discretisation errors. Since the noise is inversely proportional to the "L-form" area  $A$  and proportional to  $L_s$ , the value of  $L_s$  was standardized for the small network (larger  $A$  values) by the factor 0.466 which is the ratio of the small to the large  $A$  values.

Fig. 10 shows the results. The difference between the dotted and solid lines gives an idea of the discretisation error. When L is simulated by 20 resistors there is almost no difference in the results compared with 18 resistors. We concluded that with respect to practical problems the simulation of L by 20 resistors is acceptable.

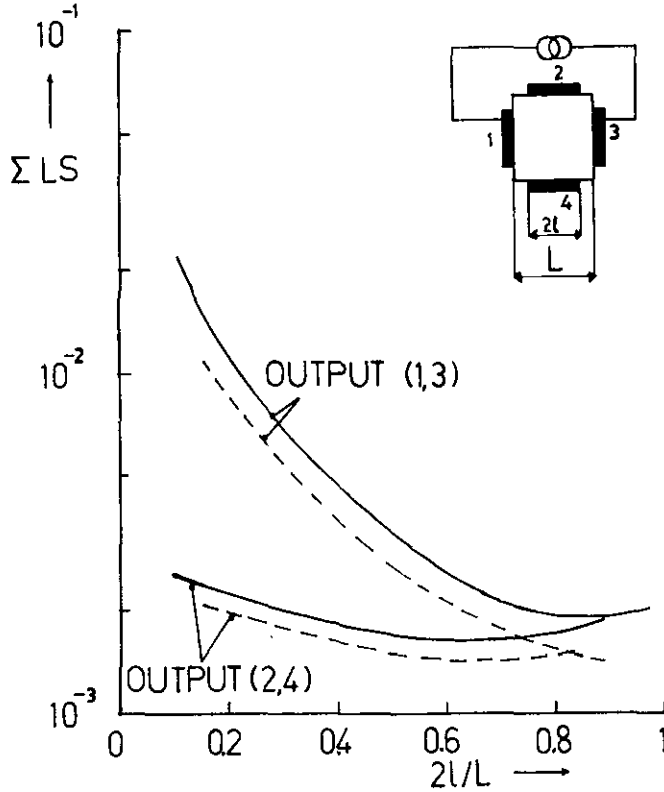


Fig. 10: The comparison  $\Sigma L_s/A$  for a discretisation with 18 resistors (solid lines) and by 12 resistors (dotted line). The results are given in arbitrary units. The results with 20 resistors are about the same as with 18 resistors.

## 6. Discussion

Contact noise is notorious in  $1/f$  noise investigations.

To avoid a contribution of the noise at the contacts, a sample geometry with four probes must be chosen. Among these four-probe situations, those with areas of low noise contributions around the contacts are in favour. Such a selection can be made by the aid of the spatial noise distribution charts. If the experimentally observed ratio  $S_Q/S_D$  is much smaller than the values presented in the figures 6 to 9 for corresponding geometries, the experimental results are affected by a contact noise. This is due to the fact that in two-probe arrangements the contact noise fully contributes.

In other investigations, this method of calculation will also apply, for

instance in the calculation of the change in noise with the change of the trim cut in a thick-film resistor by using eq. (2) or eq. (5). For a two-probe arrangement the sensor and driver electrodes coincide, and  $i_x = \tilde{i}_x$  and  $i_y = \tilde{i}_y$  in the planar conductor. The computer program easily produces the increase in resistance and noise values with increasing trim cut.

For more complex geometries (with many edges and holes) the discretisation error arises. Choosing more "L-forms" leads to long computer process time. Therefore, we are limited in choosing the geometry and discretisation.

However, for most practical geometries this method of calculation will apply.

#### Acknowledgements

We appreciate the work of Mr. J. Couwenberg who provided the drawings of the spatial noise distribution charts.



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Appendix A Numerical and experimental results

Let us first code the geometry terminal shape and  $2l/L$  ratio using the following key consisting of 5 sets of parameters.

- A, B or C denotes the geometry of fig. 1a, 1b or 1c respectively.
- 2, 3, 4 denotes a two, three or four probe situation.
- N or O denotes whether the drivers are connected to contacts next to each other or opposite to each other.
- n or o denotes whether the sensors are connected next to each other or opposite to each other.
- 1.1, 3.3, ..., 8.8  
denoted the  $2l/L$  ratio multiplied by 10.

So A 4 O o 6.6 denotes a cross shaped sample, considering a 4 terminal situation, with the driver contacts opposite to each other, the sensor contacts also opposite to each other and the  $2l/L$  ratio is 0.66.

After each situation code the following information is denoted in six columns

- $\sum L_s$  : This column denotes the sum of the added and squared sensitivities in all L-shapes according to the sum in the R.H.S. of eq. (3) or eq. (4).
- $V_Q$  : Denotes the d.c. voltage between the sensor electrodes when a current of 1A is passed through the driver electrodes and the sheet resistance is  $1\Omega$ . For four-probe arrangements, when the driver and sensor electrodes are next to each other and the contact length is small in comparison with the hole length of the boundary of the sheet, we can expect  $V_Q \approx \frac{\ln 2}{\pi} = 0.22$  following van der Pauw's result [7]. Using the following expression
$$R_{\square} = \frac{V_e}{I_e} \cdot \lambda(2l/L)$$
we can calculate the sheet resistivity. In the calculations  $R_{\square} = 1\Omega$  and  $I = 1A$ , so  $(2l/L)$  equals  $1/V_Q$  obtained from table 1. Measuring  $V_e$  and  $I_e$ , we can calculate the sheet resistance  $R_{\square}$  of any sample with the same geometry.

- percentages : This column denotes the contribution per cent of the classes 1 to 4 incl. in this sequence with respect to the total given in the first column.

When the percentages of all classes are low, it means that the noise is homogeneously distributed. The percentages for geometry C have not been calculated. Owing to the accuracy of the calculation all percentages are rounded off to integers.

- calculated  $S_Q$  : If there is a corresponding experimental result (same geometry in the next column, this column gives the calculated  $S_Q$  using eq. (6) and the following data:

$$\text{All situations: } \left\{ \begin{array}{l} f = 1 \text{ Hz} \\ I_{\text{cal}} = 1 \text{ Amp.} \\ R_{\square} = 4k5 \\ C_{\text{us}} = 5 \times 10^{-10} (\text{cm}^2). \end{array} \right.$$

$$\text{A4 and A3 situations: } \left\{ \begin{array}{l} I_e = 90 \mu\text{A} \\ L = 10.4 \text{ cm} \\ \text{Number of "L-form" areas } K = 340 \\ A = 0.32 \text{ cm}^2 \end{array} \right.$$

$$\text{A}_2 \text{ situations: } \left\{ \begin{array}{l} I_e = 55 \mu\text{A} \\ L = 13.6 \text{ cm} \\ \text{Number of "L-form" areas } K = 340 \\ A = 0.54 \text{ cm}^2 \end{array} \right.$$

$$\text{B situations: } \left\{ \begin{array}{l} I_e = 55 \mu\text{A} \\ L = 15 \text{ cm} \\ \text{Number of "L-form" areas } K = 340 \\ A = 0.54 \text{ cm}^2 \end{array} \right.$$

$$\text{C situations: } \left\{ \begin{array}{l} I_e = 90 \mu\text{A} \\ L = 12 \text{ cm} \\ \text{Number of "L-form" areas } K = 340 \\ A = 0.42 \text{ cm}^2 \end{array} \right.$$

- experimental  $S_Q$  : The experimentally observed results of  $S_Q$  measured under conditions as described in the foregoing column.
- spatial distribution This column gives the number of the page where a chart on page : chart of the spatial noise distribution of this situation is shown.

TABLE 1

Situation code	$\Sigma L_s$	$V_Q$ (V)	Percentages	Cal. $S_Q$	Exp. $S_Q$	Distr. Plot Page:
A4 Oo 1.1	$3.2 \times 10^{-3}$	0	1,3,90,90	$8.2 \times 10^{-13}$	$2.0 \times 10^{-12}$	25
A4 Oo 3.3	$2.6 \times 10^{-3}$	0	2,5,83,57	$6.8 \times 10^{-13}$	$1.8 \times 10^{-12}$	25
A4 Oo 5.5	$3.5 \times 10^{-3}$	0	2,5,70,52	$9.1 \times 10^{-13}$	$4.5 \times 10^{-12}$	26
A4 Oo 6.6	$5.0 \times 10^{-3}$	0	2,6,81,64	$1.3 \times 10^{-12}$	$3.5 \times 10^{-12}$	26
A4 Oo 7.7	$9.1 \times 10^{-3}$	0	2,5,84,78	$2.4 \times 10^{-12}$	$8.1 \times 10^{-12}$	27
A4 Oo 8.8	$2.2 \times 10^{-2}$	0	0,4,96,84	$5.7 \times 10^{-12}$	$4.0 \times 10^{-11}$	27
A4 Nn 1.1	$9.0 \times 10^{-4}$	0.12	2,3,94,87	$2.3 \times 10^{-13}$	$5.9 \times 10^{-13}$	28
A4 Nn 3.3	$7.2 \times 10^{-4}$	0.18	3,9,80,63	$1.9 \times 10^{-13}$	$5.2 \times 10^{-13}$	28
A4 Nn 5.5	$1.1 \times 10^{-3}$	0.21	2,7,60,43	$2.9 \times 10^{-13}$	$1.2 \times 10^{-12}$	29
A4 Nn 6.6	$1.6 \times 10^{-3}$	0.22	2,7,63,45	$4.2 \times 10^{-13}$	$1.2 \times 10^{-12}$	29
A4 Nn 7.7	$3.0 \times 10^{-3}$	0.22	1,5,81,49	$7.8 \times 10^{-13}$	$2.3 \times 10^{-12}$	30
A4 Nn 8.8	$7.5 \times 10^{-3}$	0.22	1,2,85,62	$1.9 \times 10^{-12}$	$1.2 \times 10^{-11}$	30
A3 Nn 1.1	$1.4 \times 10^{-3}$	0.15	2,4,92,86	$3.6 \times 10^{-13}$	$1.1 \times 10^{-12}$	31
A3 Nn 3.3	$2.3 \times 10^{-3}$	0.52	3,5,87,65	$6.0 \times 10^{-13}$	$1.1 \times 10^{-12}$	31
A3 Nn 5.5	$8.3 \times 10^{-3}$	0.65	3,4,92,82	$2.2 \times 10^{-12}$	$3.7 \times 10^{-12}$	32
A3 Nn 6.6	$2.0 \times 10^{-2}$	0.94	2,3,92,86	$5.2 \times 10^{-12}$	$7.0 \times 10^{-12}$	32
A3 Nn 7.7	$5.9 \times 10^{-2}$	1.47	1,2,96,89	$1.5 \times 10^{-11}$	$2.6 \times 10^{-11}$	33
A3 Nn 8.8	$3.0 \times 10^{-1}$	2.70	1,1,98,95	$7.8 \times 10^{-11}$	$1.6 \times 10^{-10}$	33
A3 No 1.1	$2.7 \times 10^{-3}$	0.26	2,4,92,86	$7.0 \times 10^{-13}$	$1.6 \times 10^{-12}$	34
A3 No 3.3	$3.3 \times 10^{-3}$	0.52	2,5,83,61	$8.6 \times 10^{-13}$	$1.5 \times 10^{-12}$	34
A3 No 5.5	$9.8 \times 10^{-3}$	0.87	2,5,87,72	$2.6 \times 10^{-12}$	$3.5 \times 10^{-12}$	35
A3 No 6.6	$2.2 \times 10^{-2}$	1.16	2,3,92,83	$5.6 \times 10^{-12}$	$7.5 \times 10^{-12}$	35
A3 No 7.7	$6.3 \times 10^{-2}$	1.68	1,2,93,89	$1.6 \times 10^{-11}$	$2.6 \times 10^{-11}$	36
A3 No 8.8	$3.1 \times 10^{-1}$	2.91	0,1,96,90	$8.1 \times 10^{-11}$	$1.8 \times 10^{-10}$	36

TABLE 1 (continued)

Situation code	$\Sigma L_s$	$V_Q$ (V)	Percentages	Cal. $S_Q$	Exp. $S_Q$	Distr. Plot Page:
A2 Nn 1.1	$5.1 \times 10^{-3}$	0.42	2,3,95,91	$2.9 \times 10^{-13}$	$6.0 \times 10^{-13}$	37
A2 Nn 3.3	$6.3 \times 10^{-3}$	0.86	2,4,83,70	$3.6 \times 10^{-13}$	$1.1 \times 10^{-12}$	37
A2 Nn 5.5	$1.9 \times 10^{-2}$	1.52	1,2,89,51	$1.1 \times 10^{-12}$	$2.9 \times 10^{-12}$	38
A2 Nn 6.6	$4.3 \times 10^{-2}$	2.10	1,2,92,36	$2.5 \times 10^{-12}$		38
A2 Nn 7.7	$1.3 \times 10^{-1}$	3.15	1,1,93,21	$7.4 \times 10^{-12}$	$4.5 \times 10^{-11}$	39
A2 Nn 8.8	$6.2 \times 10^{-1}$	5.60	0,1,97,10	$3.6 \times 10^{-11}$		39
A2 Oo 1.1	$3.3 \times 10^{-3}$	0.53	3,6,87,85	$1.8 \times 10^{-13}$	$4.2 \times 10^{-13}$	40
A2 Oo 3.3	$4.9 \times 10^{-3}$	1.04	1,4,74,44	$2.8 \times 10^{-13}$	$1.1 \times 10^{-12}$	40
A2 Oo 5.5	$1.7 \times 10^{-2}$	1.73	1,2,82,13	$9.7 \times 10^{-13}$	$2.4 \times 10^{-12}$	41
A2 Oo 6.6	$4.1 \times 10^{-2}$	2.32	1,1,87, 8	$2.3 \times 10^{-12}$		41
A2 Oo 7.7	$1.2 \times 10^{-1}$	3.37	0,1,92, 8	$6.8 \times 10^{-12}$	$4.2 \times 10^{-11}$	not presented
A2 Oo 8.8	$6.2 \times 10^{-1}$	5.81	0,0,96, 0	$3.5 \times 10^{-11}$		42
B4 Oo 1	$1.6 \times 10^{-3}$	0	1,2,85,16	$9.1 \times 10^{-14}$		43
B4 Oo 2	$1.6 \times 10^{-3}$	0	1,2,85, 0	$9.1 \times 10^{-14}$	$1.5 \times 10^{-13}$	43
B4 Oo 4	$1.6 \times 10^{-3}$	0	1,2,86, 0	$9.1 \times 10^{-14}$	$1.9 \times 10^{-13}$	44
B4 Oo 6	$1.4 \times 10^{-3}$	0	0,2,86, 0	$8.0 \times 10^{-14}$	$2.0 \times 10^{-13}$	44
B4 Oo 8	$7.8 \times 10^{-4}$	0	0,1,80, 0	$4.5 \times 10^{-14}$	$8.5 \times 10^{-14}$	45
B4 Nn 1	$8.6 \times 10^{-4}$	0.22	1,4, 0, 0	$4.9 \times 10^{-14}$		46
B4 Nn 2	$8.4 \times 10^{-4}$	0.22	1,4, 0, 0	$4.8 \times 10^{-14}$	$1.0 \times 10^{-13}$	46
B4 Nn 4	$7.3 \times 10^{-4}$	0.20	1,3, 0, 0	$4.2 \times 10^{-14}$	$9.0 \times 10^{-14}$	47
B4 Nn 6	$5.2 \times 10^{-4}$	0.16	1,5, 2, 0	$3.0 \times 10^{-14}$	$5.2 \times 10^{-14}$	47
B4 Nn 8	$2.7 \times 10^{-4}$	0.09	1,1,14, 0	$1.5 \times 10^{-14}$	$4.0 \times 10^{-14}$	48

TABLE 1 (continued)

Situation Code	$\Sigma L_s$	$V_Q$ (V)	Percentages	Cal. $S_Q$	Exp. $S_Q$	Distr. Plot page:
B3 Nn 1	$2.8 \times 10^{-2}$	1.16	2,3,91,85	$1.6 \times 10^{-12}$		49
B3 Nn 2	$1.1 \times 10^{-2}$	0.85	2,4,88,78	$6.3 \times 10^{-13}$	$2.2 \times 10^{-12}$	49
B3 Nn 4	$3.1 \times 10^{-3}$	0.48	2,5,79,57	$1.8 \times 10^{-13}$	$4.5 \times 10^{-13}$	50
B3 Nn 6	$1.2 \times 10^{-3}$	0.26	4,6,68,31	$6.8 \times 10^{-14}$	$1.1 \times 10^{-13}$	50
B3 Nn 8	$3.7 \times 10^{-4}$	0.11	6,7,33,15	$2.1 \times 10^{-14}$	$4.5 \times 10^{-14}$	51
B3 On 1	$2.9 \times 10^{-2}$	1.37	3,5,90,85	$1.7 \times 10^{-12}$		52
B3 On 2	$1.2 \times 10^{-2}$	1.06	3,6,84,76	$6.8 \times 10^{-13}$	$1.5 \times 10^{-12}$	52
B3 On 4	$4.1 \times 10^{-3}$	0.68	3,8,79,57	$2.3 \times 10^{-13}$	$7.5 \times 10^{-13}$	53
B3 On 6	$1.9 \times 10^{-3}$	0.42	1,8,75,49	$1.1 \times 10^{-13}$	$2.0 \times 10^{-13}$	53
B3 On 8	$7.6 \times 10^{-4}$	0.20	0,7,74,55	$4.3 \times 10^{-14}$	$9.5 \times 10^{-14}$	54
B2 Oo 1	$5.7 \times 10^{-2}$	2.74	3,5,89,81	$3.3 \times 10^{-12}$		55
B2 Oo 2	$2.2 \times 10^{-2}$	2.12	4,8,84,71	$1.3 \times 10^{-12}$	$2.0 \times 10^{-12}$	55
B2 Oo 4	$6.5 \times 10^{-3}$	1.37	3,9,74,47	$3.7 \times 10^{-13}$	$1.1 \times 10^{-12}$	56
B2 Oo 6	$2.8 \times 10^{-3}$	0.84	1,6,58,28	$1.6 \times 10^{-13}$	$3.8 \times 10^{-13}$	56
B2 Oo 7	$1.8 \times 10^{-3}$	0.61	1,3,42,23	$1.0 \times 10^{-13}$		not presented
B2 Oo 8	$1.1 \times 10^{-3}$	0.40	0,2,27,15	$6.3 \times 10^{-14}$	$1.3 \times 10^{-13}$	57
B2 Nn 1	$5.9 \times 10^{-2}$	2.52	2,5,85,73	$3.4 \times 10^{-12}$		58
B2 Nn 2	$2.4 \times 10^{-2}$	1.90	1,4,79,61	$1.4 \times 10^{-12}$	$3.2 \times 10^{-12}$	58
B2 Nn 4	$8.0 \times 10^{-3}$	1.16	2,5,80,41	$4.6 \times 10^{-13}$	$1.0 \times 10^{-12}$	59
B2 Nn 6	$3.6 \times 10^{-3}$	0.68	4,6,86,23	$2.1 \times 10^{-13}$	$5.0 \times 10^{-13}$	59
B2 Nn 8	$1.4 \times 10^{-3}$	0.31	3,4,94, 8	$8.0 \times 10^{-14}$	$1.6 \times 10^{-13}$	60

TABLE 1 (continued)

Situation code	$\Sigma I_s$	$V_Q$ (V)	Cal. $S_Q$	Exp. $S_Q$
C4 Oo 1.1	$2.5 \times 10^{-3}$	0 V	$5 \times 10^{-13}$	$3.4 \times 10^{-12}$
C4 Oo 2.2	$2.3 \times 10^{-3}$	0 V	$4.6 \times 10^{-13}$	$2.8 \times 10^{-12}$
C4 Oo 3.3	$2.2 \times 10^{-3}$	0 V	$4.4 \times 10^{-13}$	$3.5 \times 10^{-12}$
C4 Oo 6.6	$1.7 \times 10^{-3}$	0 V	$3.4 \times 10^{-13}$	$2.0 \times 10^{-12}$
C4 Oo 8.8	$1.9 \times 10^{-3}$	0 V	$3.8 \times 10^{-13}$	$2.2 \times 10^{-12}$
C4 Nn 1.1	$7.4 \times 10^{-4}$	0.22	$1.5 \times 10^{-13}$	$9.2 \times 10^{-13}$
C4 Nn 2.2	$6.6 \times 10^{-4}$	0.21	$1.3 \times 10^{-13}$	$8.0 \times 10^{-13}$
C4 Nn 3.3	$6.3 \times 10^{-4}$	0.20	$1.3 \times 10^{-13}$	$8.0 \times 10^{-13}$
C4 Nn 6.6	$4.9 \times 10^{-4}$	0.15	$9.8 \times 10^{-14}$	$5.5 \times 10^{-13}$
C4 Nn 8.8	$6.0 \times 10^{-4}$	0.10	$1.2 \times 10^{-13}$	$7.4 \times 10^{-13}$
C3 Nn 1.1	$1.1 \times 10^{-2}$	0.63	$2.2 \times 10^{-12}$	$2.9 \times 10^{-11}$
C3 Nn 2.2	$5.2 \times 10^{-3}$	0.50	$1.0 \times 10^{-12}$	$5.3 \times 10^{-12}$
C3 Nn 3.3	$3.0 \times 10^{-3}$	0.40	$6.0 \times 10^{-13}$	$2.8 \times 10^{-12}$
C3 Nn 6.6	$1.0 \times 10^{-3}$	0.22	$2.0 \times 10^{-13}$	$9.0 \times 10^{-13}$
C3 Nn 8.8	$9.0 \times 10^{-4}$	0.12	$1.8 \times 10^{-13}$	$1.0 \times 10^{-12}$
C3 No 1.1	$1.3 \times 10^{-2}$	0.85	$2.6 \times 10^{-12}$	$3.1 \times 10^{-11}$
C3 No 2.2	$6.2 \times 10^{-3}$	0.70	$1.2 \times 10^{-12}$	$5.7 \times 10^{-12}$
C3 No 3.3	$3.9 \times 10^{-3}$	0.60	$7.8 \times 10^{-13}$	$3.8 \times 10^{-12}$
C3 No 6.6	$1.7 \times 10^{-3}$	0.37	$3.4 \times 10^{-13}$	$1.4 \times 10^{-12}$
C3 No 8.8	$1.7 \times 10^{-3}$	0.21	$3.4 \times 10^{-13}$	$2.4 \times 10^{-12}$
C2 Oo 1.1	$2.2 \times 10^{-2}$	1.70	$4.4 \times 10^{-12}$	$1.9 \times 10^{-10}$
C2 Oo 2.2	$1.1 \times 10^{-2}$	1.41	$2.2 \times 10^{-12}$	$3.2 \times 10^{-11}$
C2 Oo 3.3	$6.5 \times 10^{-3}$	1.20	$1.3 \times 10^{-12}$	$2.6 \times 10^{-11}$
C2 Oo 6.6	$2.3 \times 10^{-3}$	0.73	$4.6 \times 10^{-13}$	$4.1 \times 10^{-12}$
C2 Oo 8.8	$2.0 \times 10^{-3}$	0.43	$4.0 \times 10^{-13}$	$3.8 \times 10^{-12}$
C2 Nn 1.1	$2.5 \times 10^{-2}$	1.50	$5.0 \times 10^{-12}$	$1.3 \times 10^{-10}$
C2 Nn 2.2	$1.2 \times 10^{-2}$	1.20	$2.4 \times 10^{-12}$	$2.6 \times 10^{-11}$
C2 Nn 3.3	$7.5 \times 10^{-3}$	1.00	$1.5 \times 10^{-12}$	$1.8 \times 10^{-11}$
C2 Nn 6.6	$3.3 \times 10^{-3}$	0.58	$6.6 \times 10^{-13}$	$4.0 \times 10^{-12}$
C2 Nn 8.8	$3.3 \times 10^{-3}$	0.33	$6.6 \times 10^{-13}$	$6.4 \times 10^{-12}$



TABLE 2

Situation	$D_{12}$		$D_{13}$	
	$\Sigma L_s$	$V_Q$	$\Sigma L_s$	$V_Q$
B4 Nn 1	$6.8 \times 10^{-4}$	0.18	$1.9 \times 10^{-3}$	0.34
B4 Nn 2	$6.6 \times 10^{-4}$	0.18	$1.8 \times 10^{-3}$	0.34
B3 Nn 1	$4.6 \times 10^{-2}$	1.28	$4.6 \times 10^{-2}$	1.28
B3 Nn 2	$1.2 \times 10^{-2}$	0.93	$1.2 \times 10^{-2}$	0.93
B3 On 1	$4.7 \times 10^{-2}$	1.45	$4.7 \times 10^{-2}$	1.62
B3 On 2	$1.3 \times 10^{-2}$	1.11	$1.3 \times 10^{-2}$	1.27
B2 Nn 1	$9.7 \times 10^{-2}$	2.73	$9.8 \times 10^{-2}$	2.90
B2 Nn 2	$2.7 \times 10^{-2}$	2.04	$3.0 \times 10^{-2}$	2.21

Table 2: Columns denoted by  $D_{12}$  give  $\Sigma L_s$  and the corresponding d.c. voltage  $V_Q$  when the current source is connected to (1, 2). Column denoted by  $D_{13}$  given  $\Sigma L_s$  and  $V_Q$  but now with the current source is connected to (1, 3). See the figure below. The sample of fig. 1b is simulated by a resistor network with all row resistors having a value of  $1.25\Omega$ . So table 2 shows the effect of loss of symmetry. Note that in the special case of B3 Nn there is no difference in the results because in that situation we are applying the reciprocity principle and the reciprocity principle holds for this simple linear passive network.

The arrow in the fig. indicates the "easy direction" of the resistivity. In the direction perpendicular to the arrow the sheet resistance and  $C_{us}$  is 25% higher than in the arrow direction.

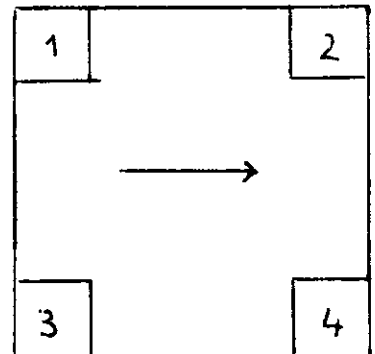


TABLE 3

Situation code	isotropic		anisotropic	
	$\Sigma L_s$	$V_Q$	$\Sigma L_s$	$V_Q$
B4 Oo 1	$1.6 \times 10^{-3}$	0	$2.4 \times 10^{-3}$	0.17
B4 Oo 2	$1.6 \times 10^{-3}$	0	$2.4 \times 10^{-3}$	0.16
B4 Nn 1	$8.6 \times 10^{-4}$	0.22	$6.8 \times 10^{-4}$	0.18
B4 Nn 2	$8.4 \times 10^{-4}$	0.22	$6.6 \times 10^{-4}$	0.18
B3 Nn 1	$2.8 \times 10^{-2}$	1.16	$4.6 \times 10^{-2}$	1.28
B3 Nn 2	$1.1 \times 10^{-2}$	0.85	$1.2 \times 10^{-2}$	0.93
B3 On 1	$2.9 \times 10^{-2}$	1.37	$4.7 \times 10^{-2}$	1.45
B3 On 2	$1.2 \times 10^{-2}$	1.06	$1.3 \times 10^{-2}$	1.11
B2 Oo 1	$5.7 \times 10^{-2}$	2.74	$8.8 \times 10^{-2}$	3.08
B2 Oo 2	$2.2 \times 10^{-2}$		$3.6 \times 10^{-2}$	2.38
B2 Nn 1	$5.9 \times 10^{-2}$	2.52	$9.7 \times 10^{-2}$	2.73
B2 Nn 2	$2.4 \times 10^{-2}$	1.90	$2.7 \times 10^{-2}$	2.04

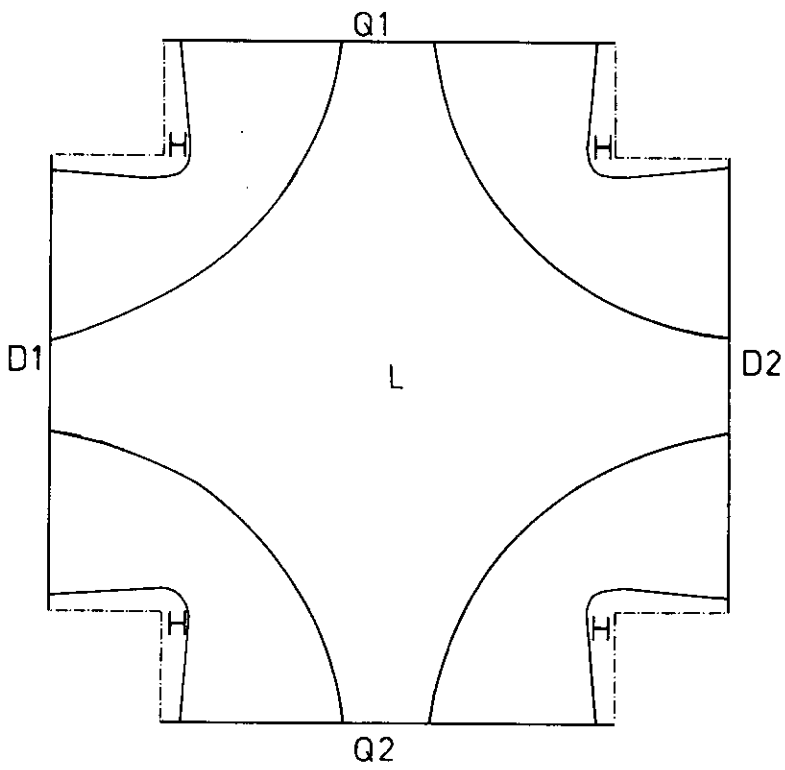
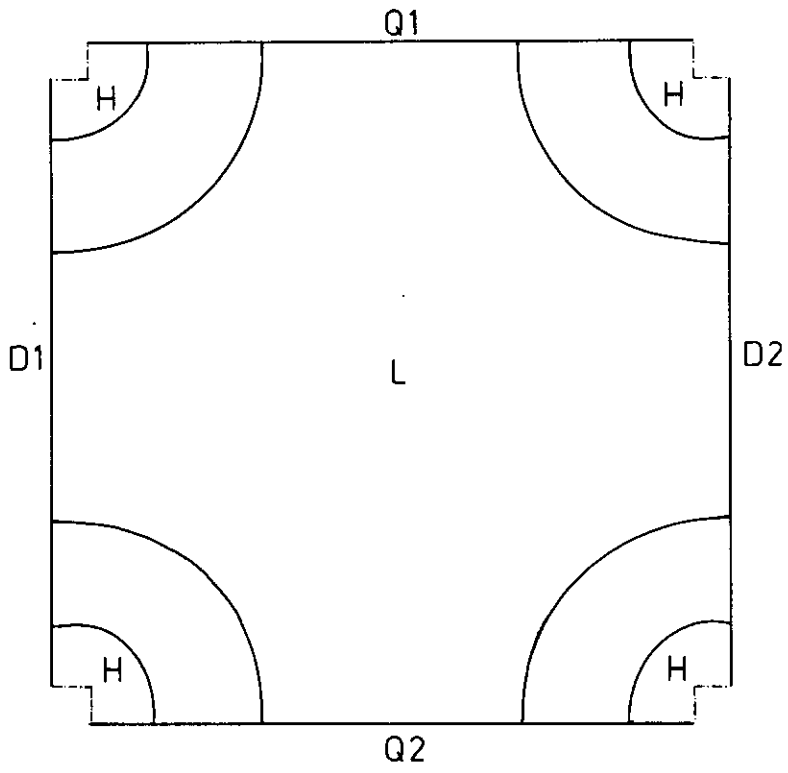
Table 3: Columns denoted "isotropic" give  $\Sigma L_s$  of output  $Q_1, Q_2$  (the  $\Sigma L_s$  column in table 1) and the corresponding d.c. voltage  $V_Q$  when the planar resistor of fig. 1b, is simulated by a network with all resistors having the same value. The columns denoted "anisotropic" give corresponding results when the vertical resistors are  $1.25 \Omega$  and the horizontal resistors are  $1 \Omega$ . The isotropic and anisotropic results deal with exactly the same situations, which means that not only the configuration is the same but also the terminals D and Q are connected to contacts with the same numbers.

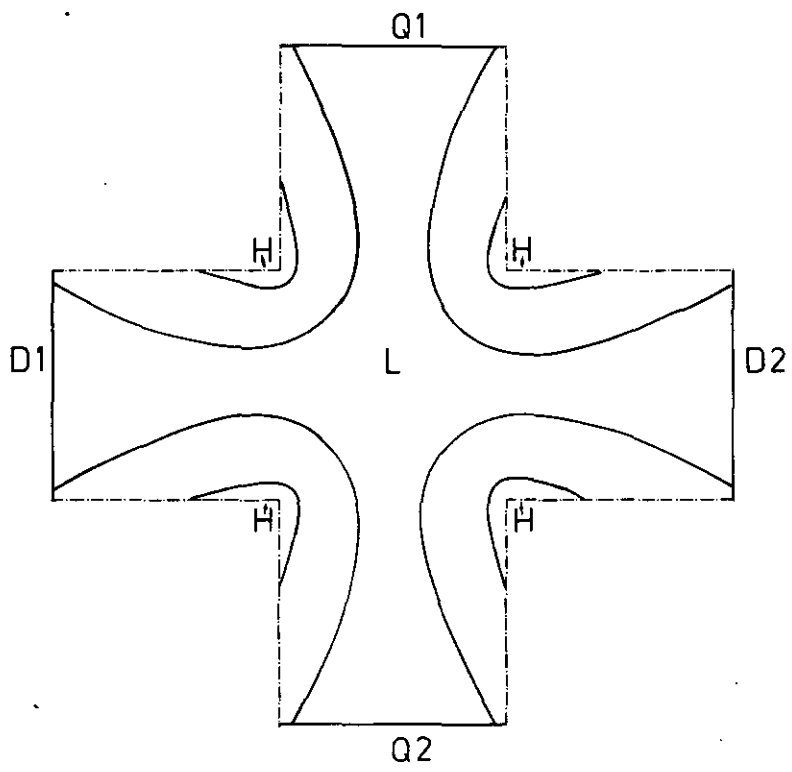
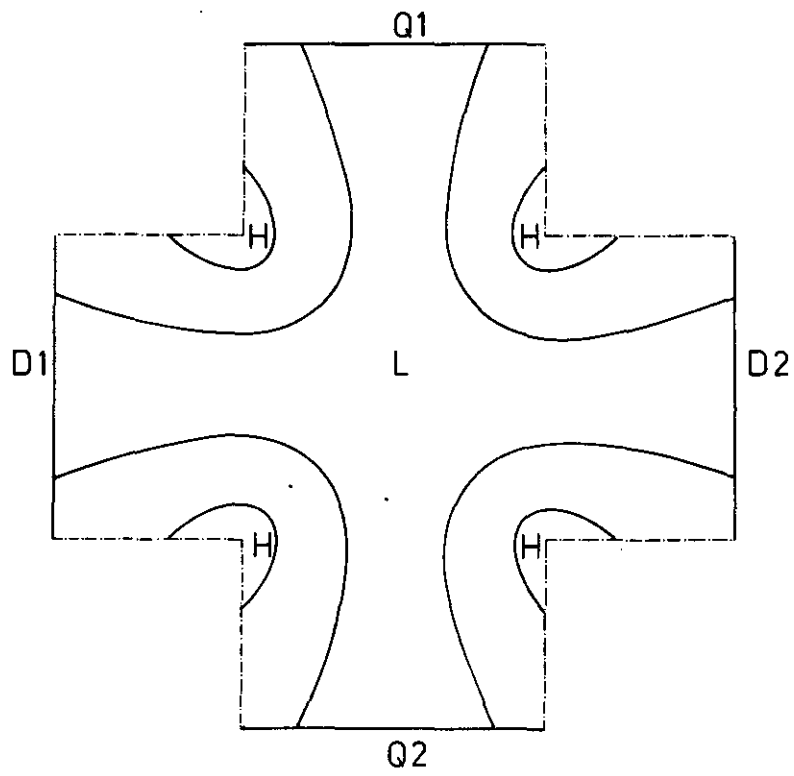
Appendix B Spatial noise distribution

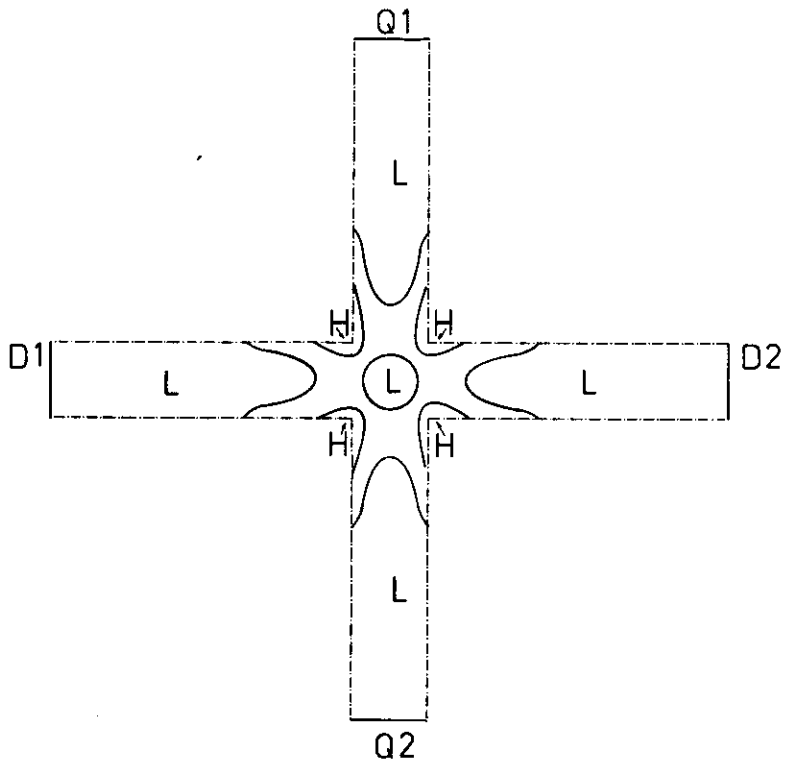
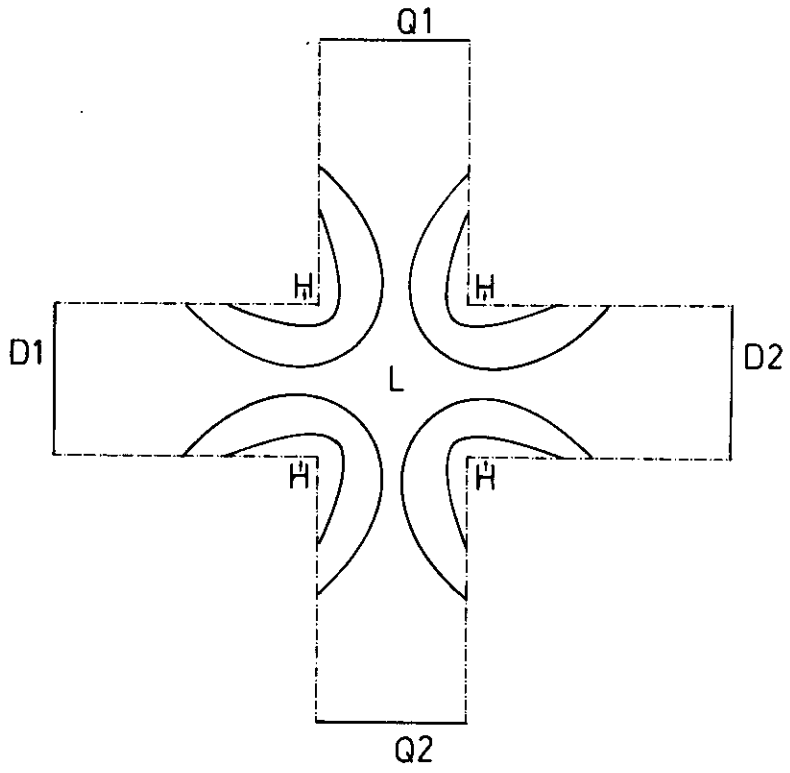
This appendix contains charts of all spatial noise distributions of the A and B situations given in Appendix A, table 1.

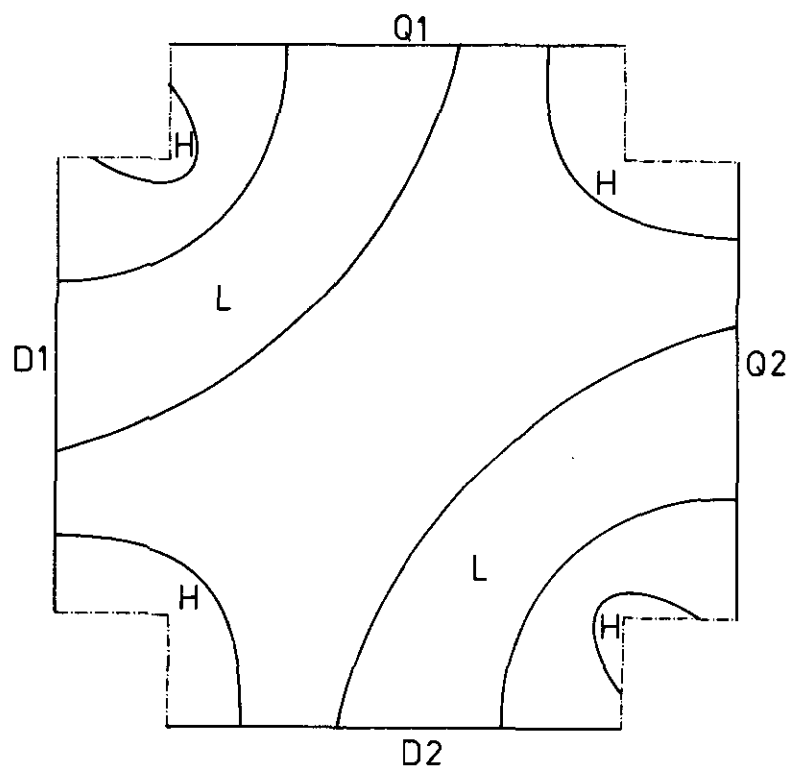
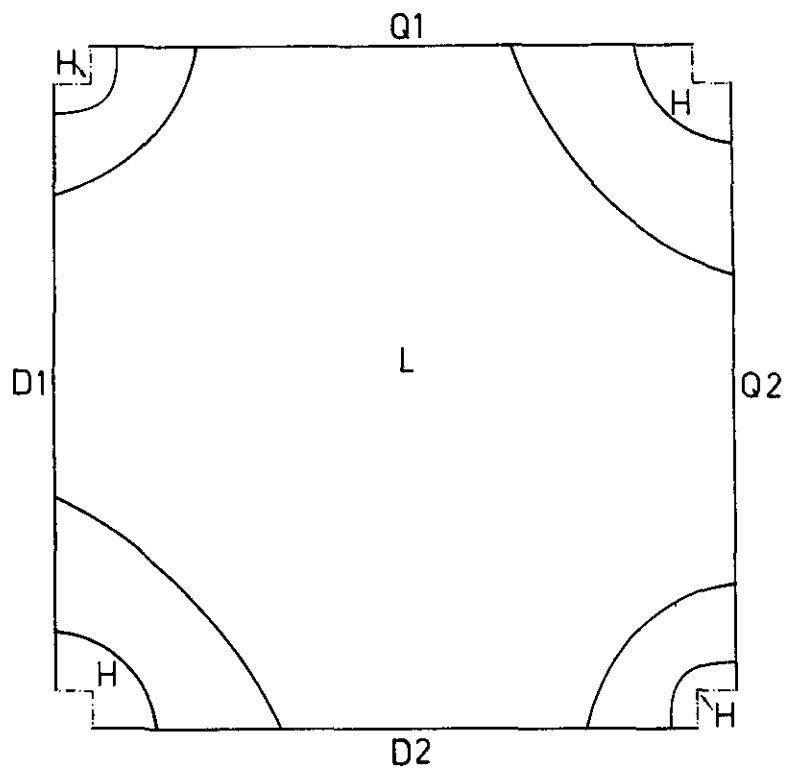
In the plots the conductor boundaries are represented by dotted lines. Areas with a low and high noise contribution are bordered by solid lines. When such an area is indicated by the letter "L" for low contribution, it means that all squares of unit "L-form" areas inside that area fall in class 1; when indicated by "H" for high contribution, the unit areas bordered by the solid line fall in class 4. For the exact information of each plot see Appendix A, table 1.

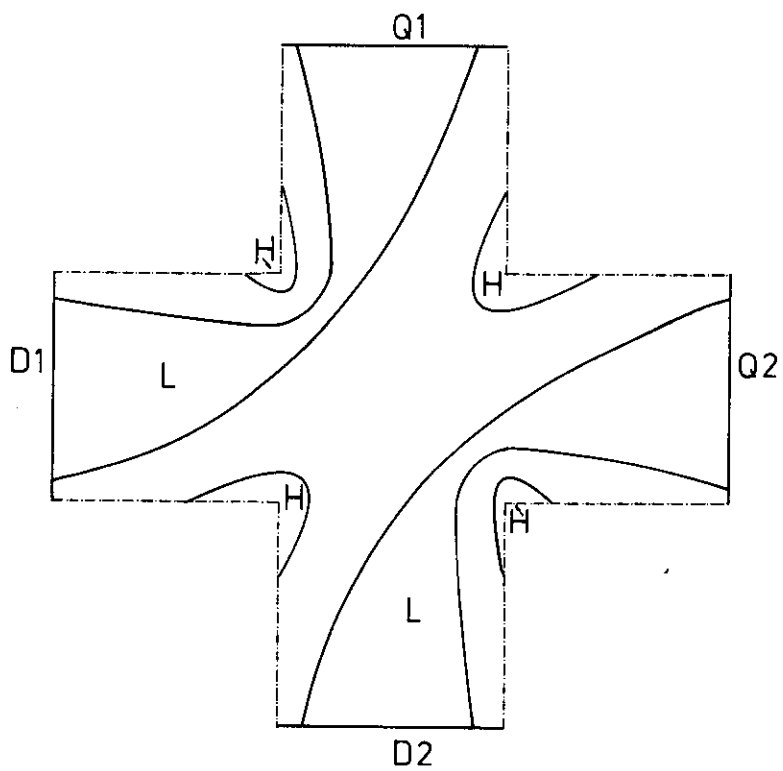
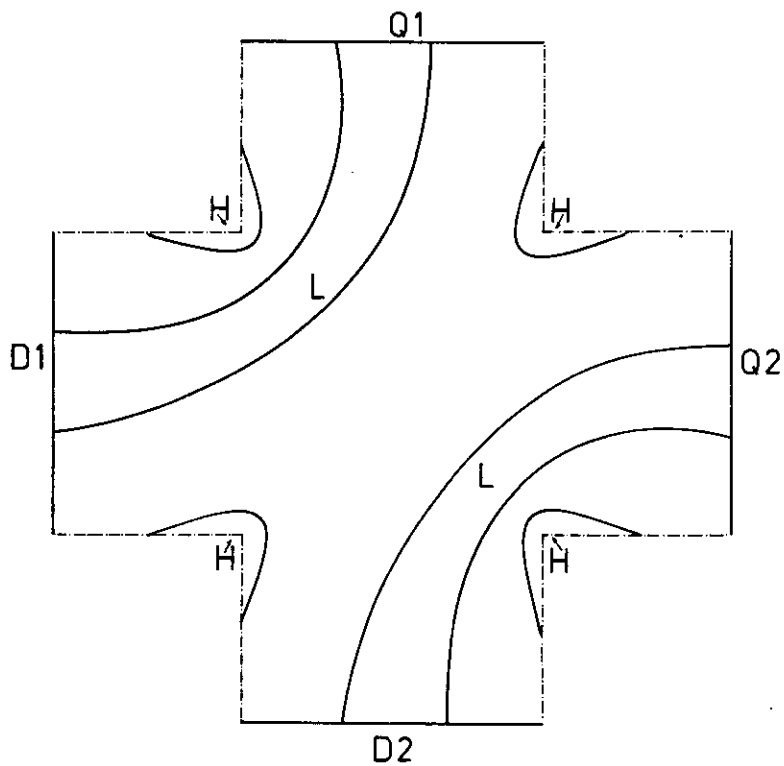
In all plots  $D_1$  and  $D_2$  are the driver electrodes,  $Q_1$  and  $Q_2$  the sensor electrodes.



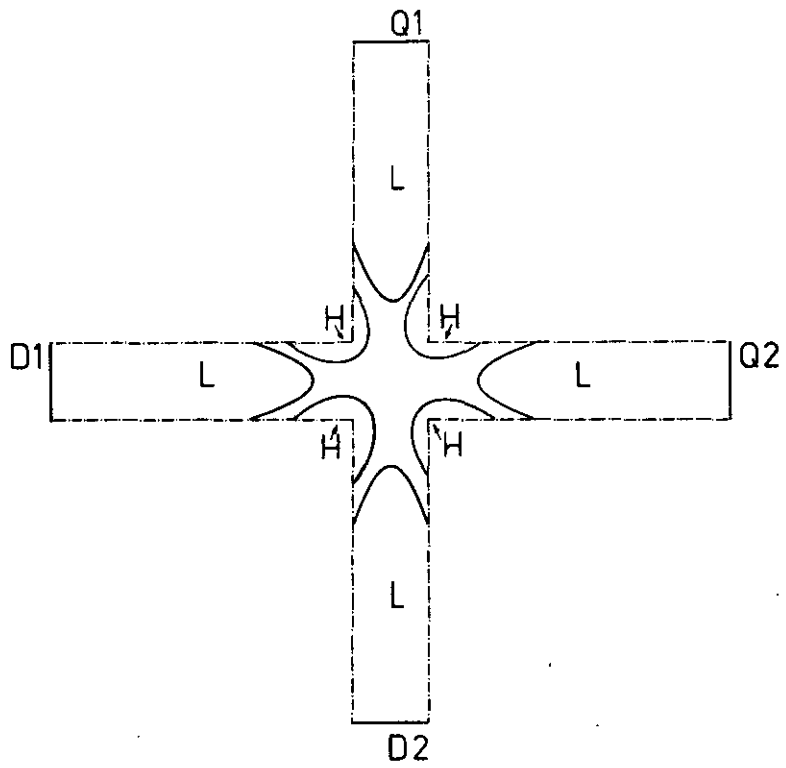
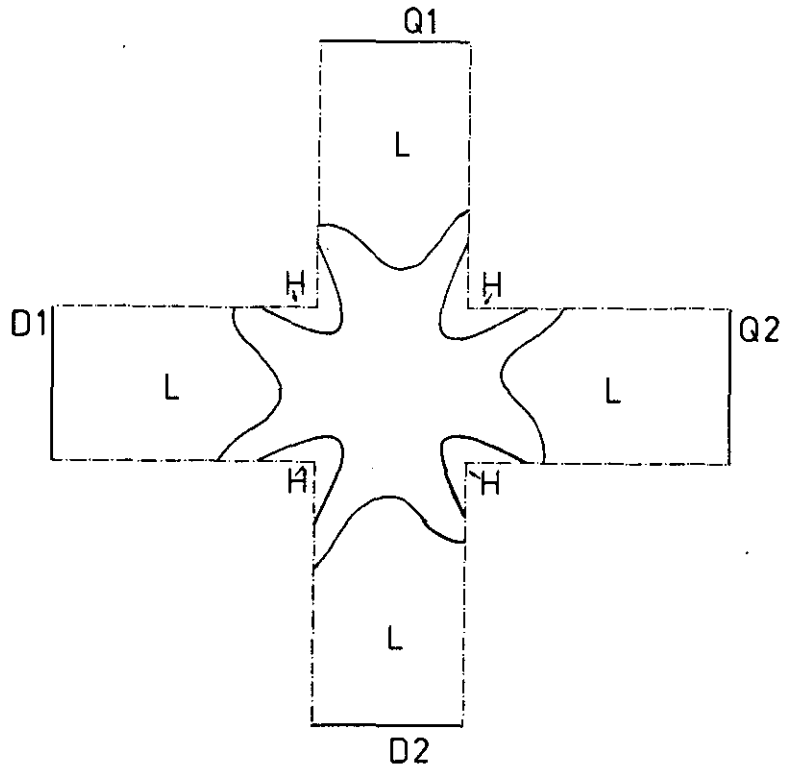


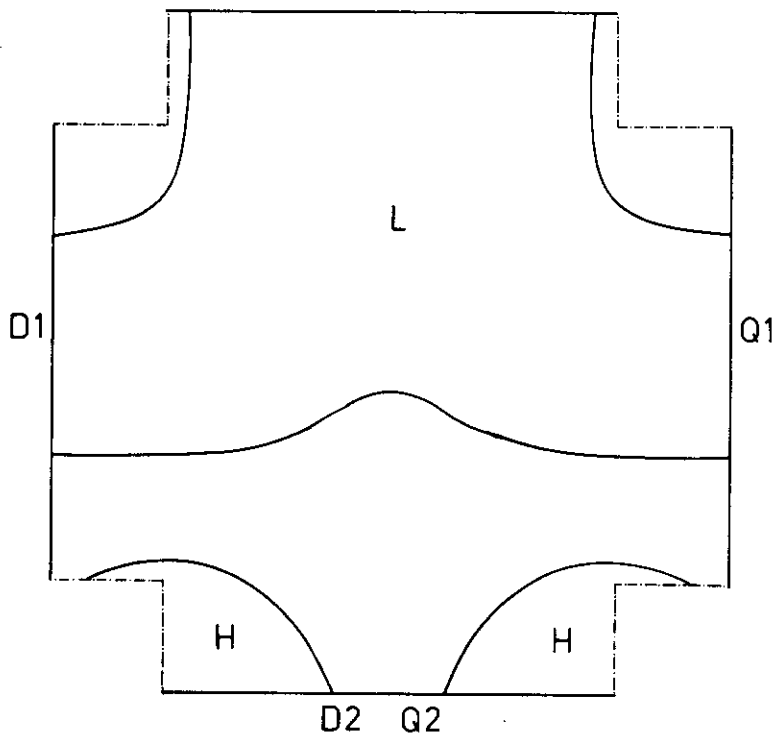
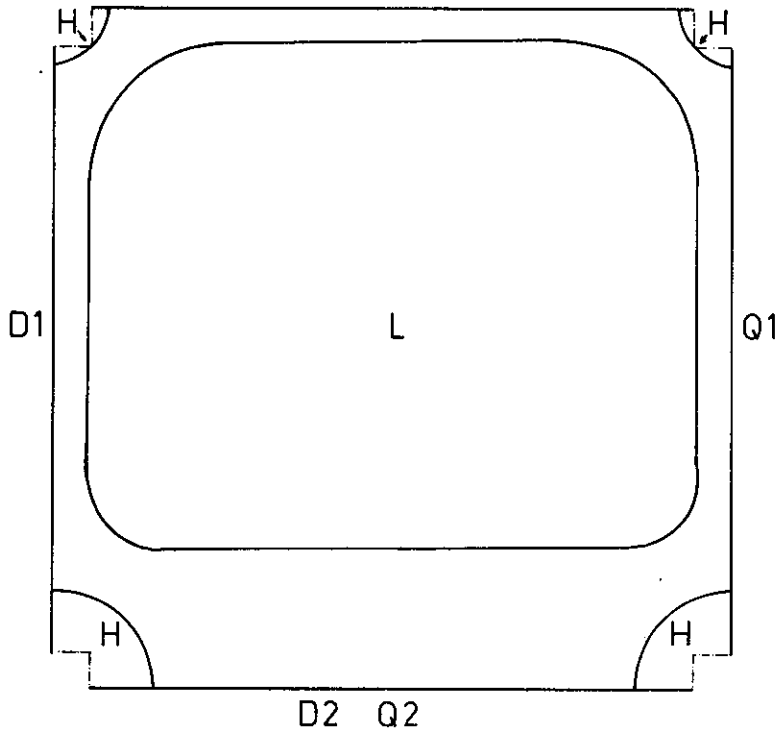


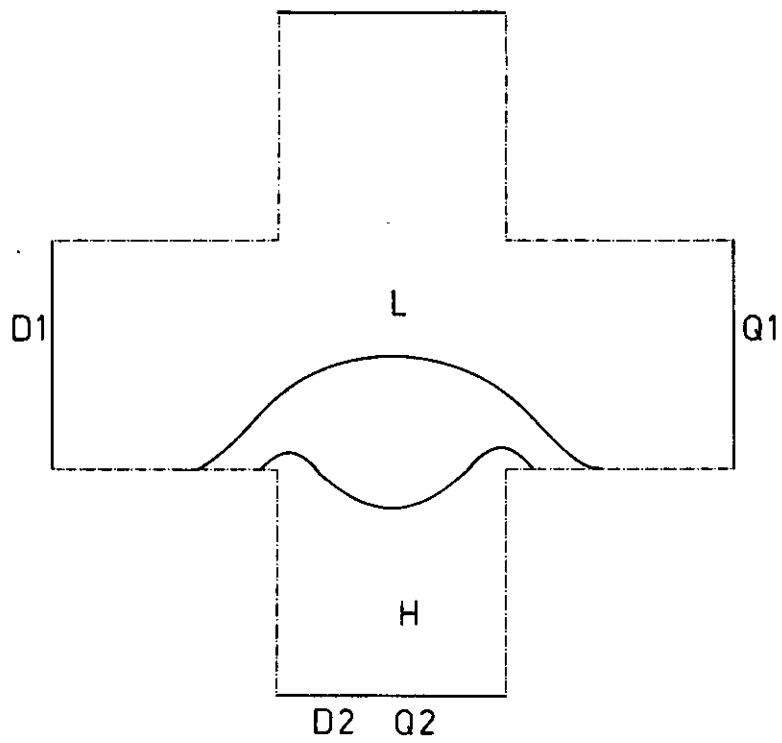
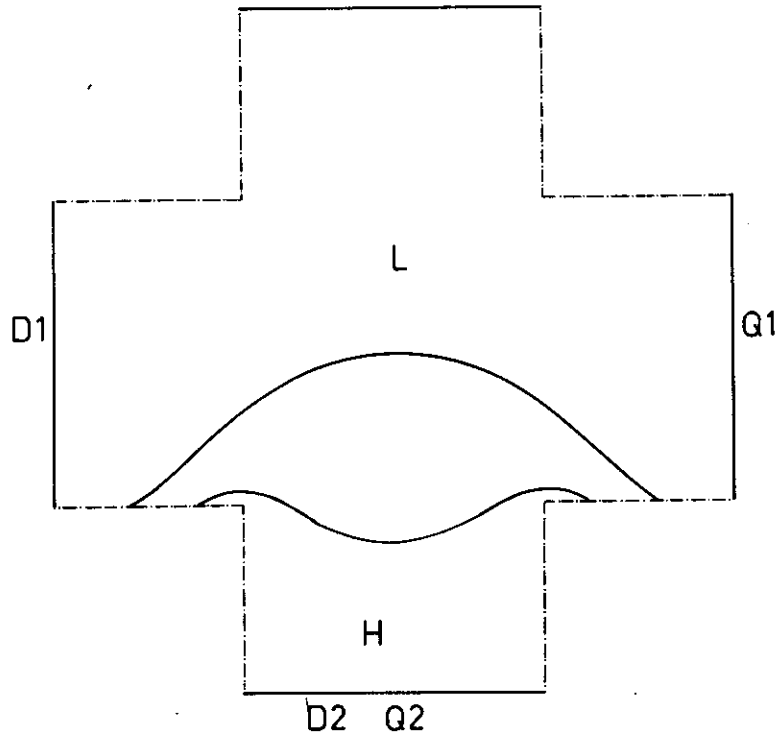


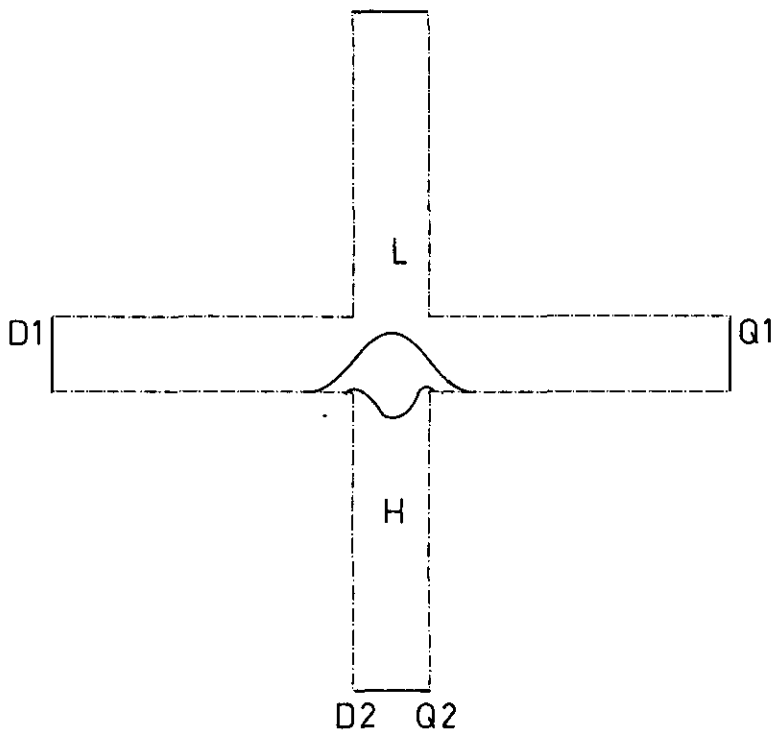
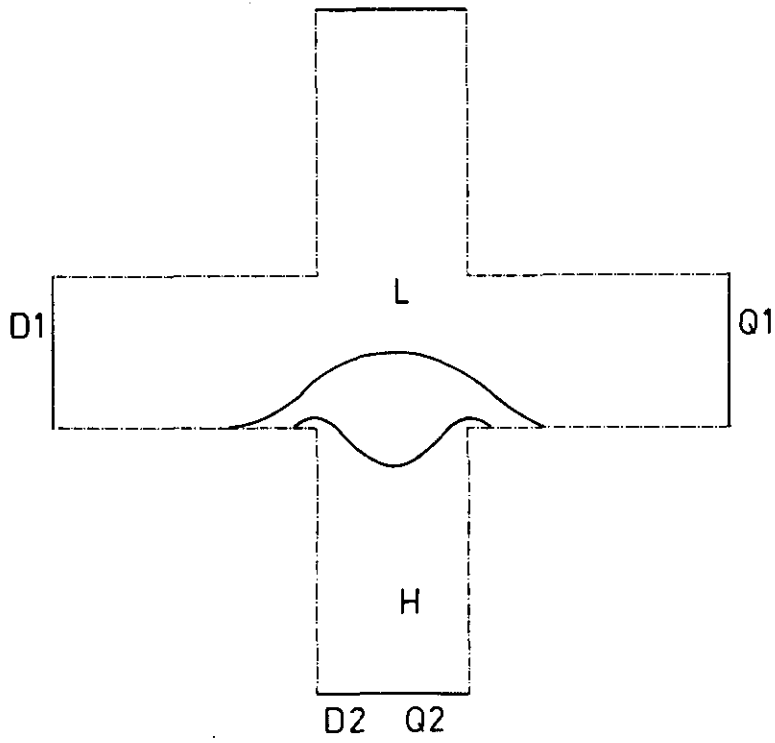


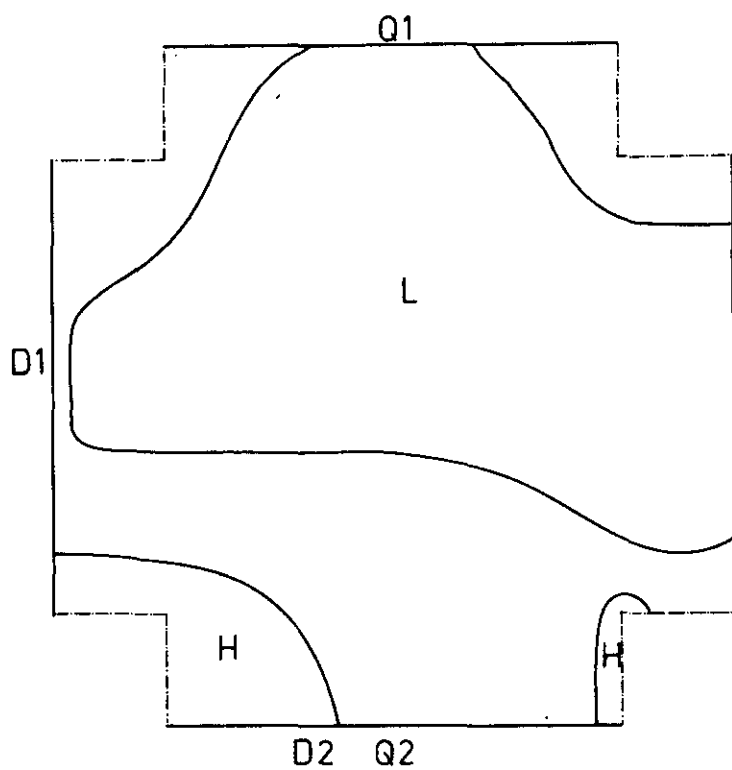
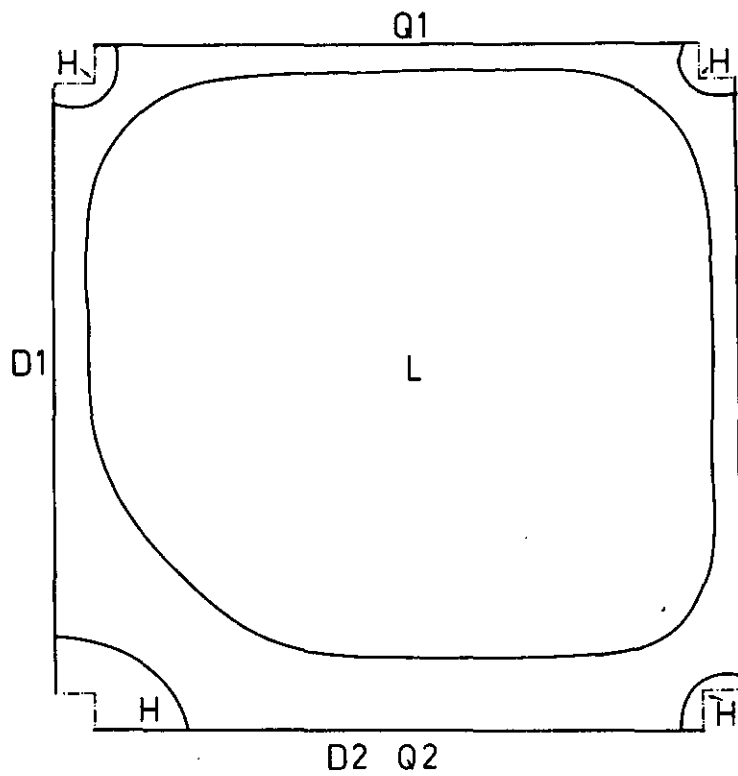


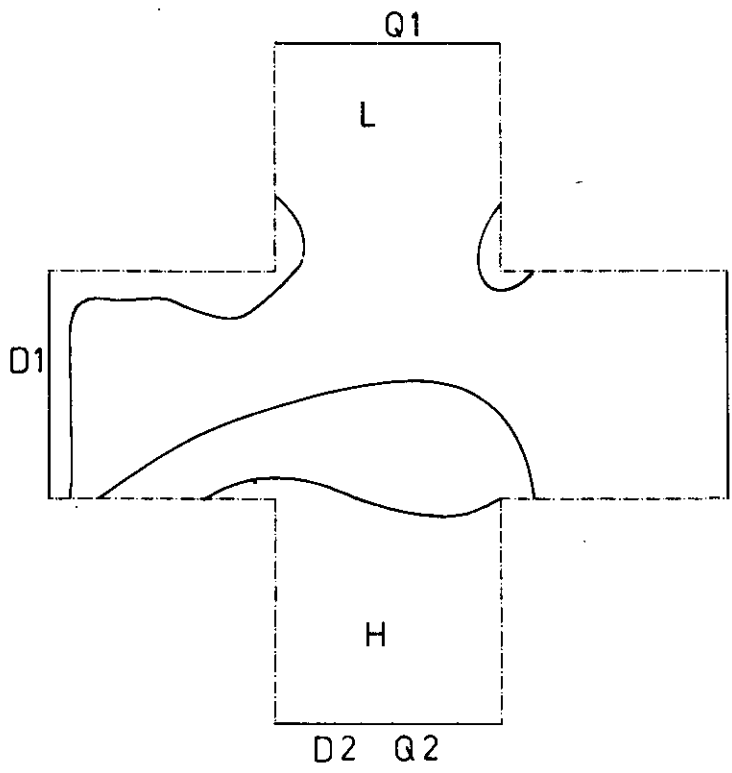
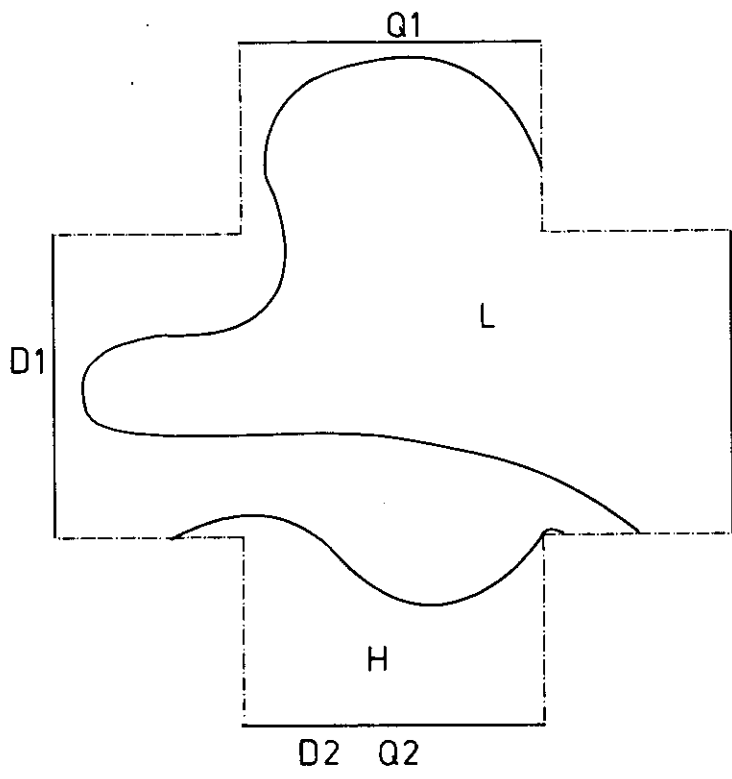


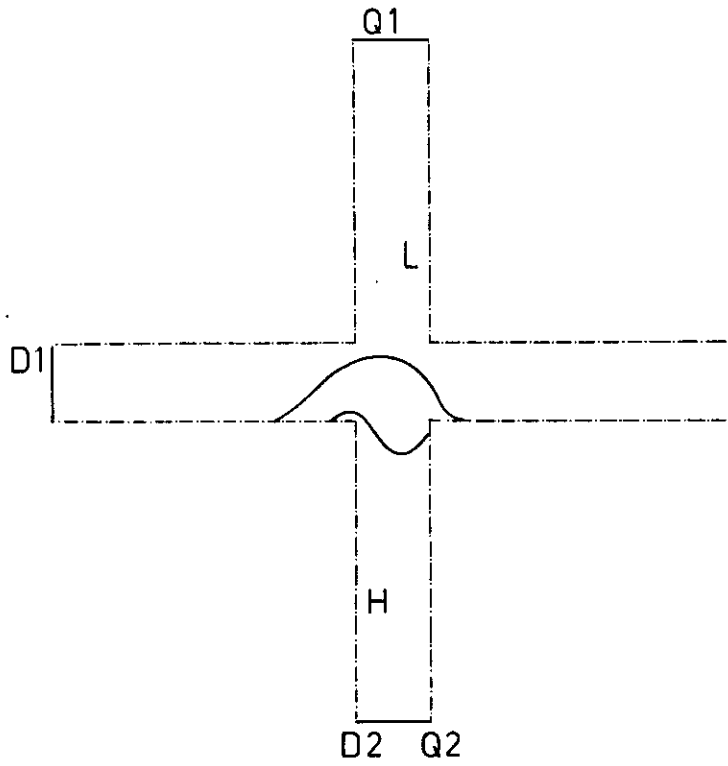
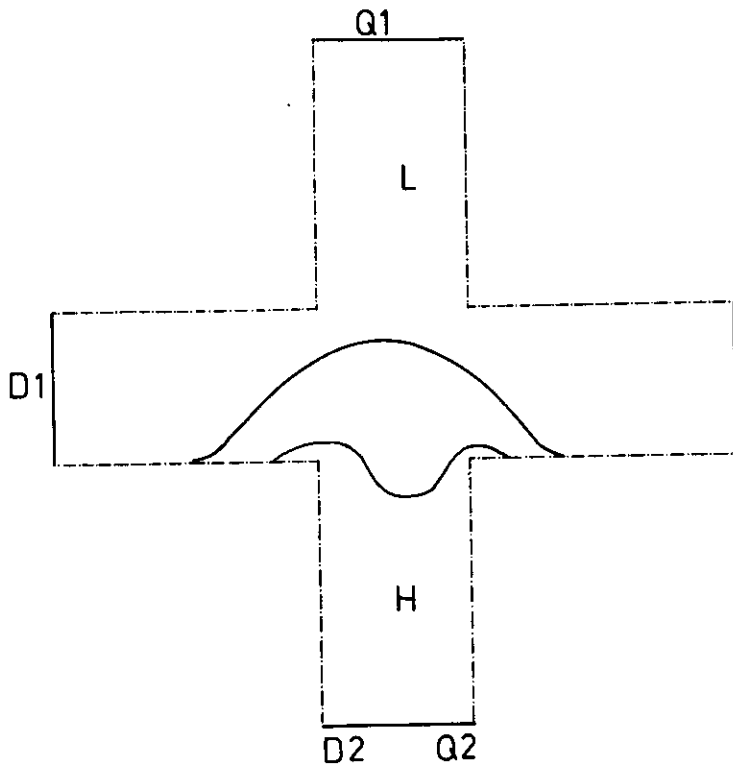


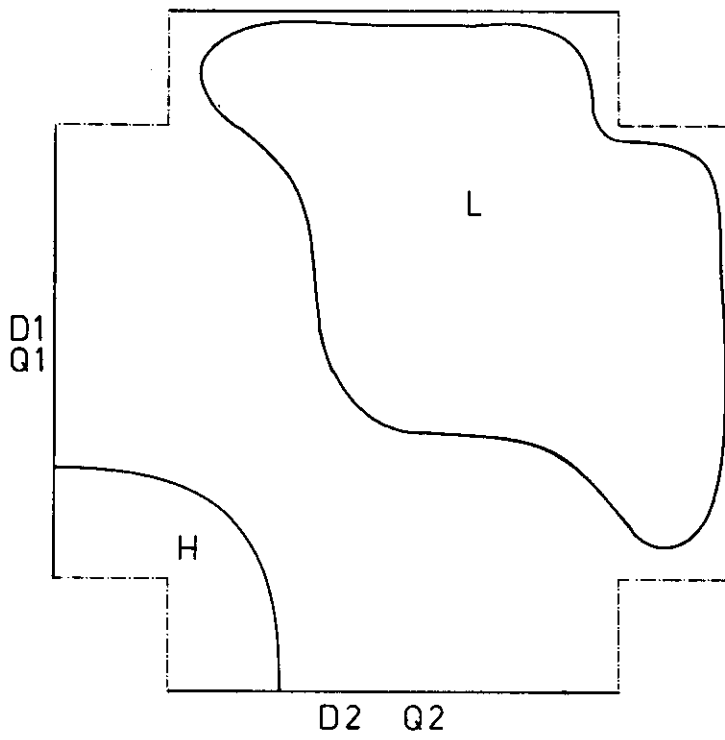
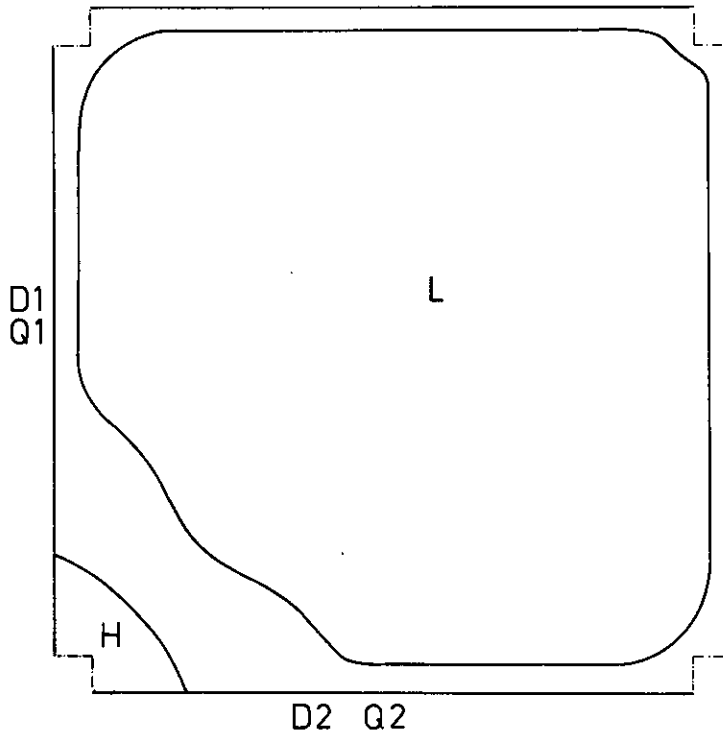




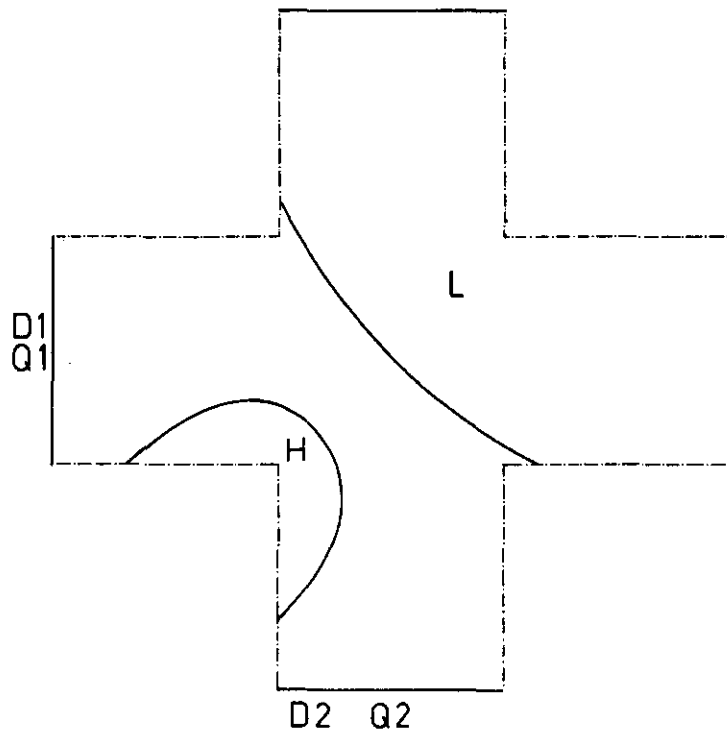
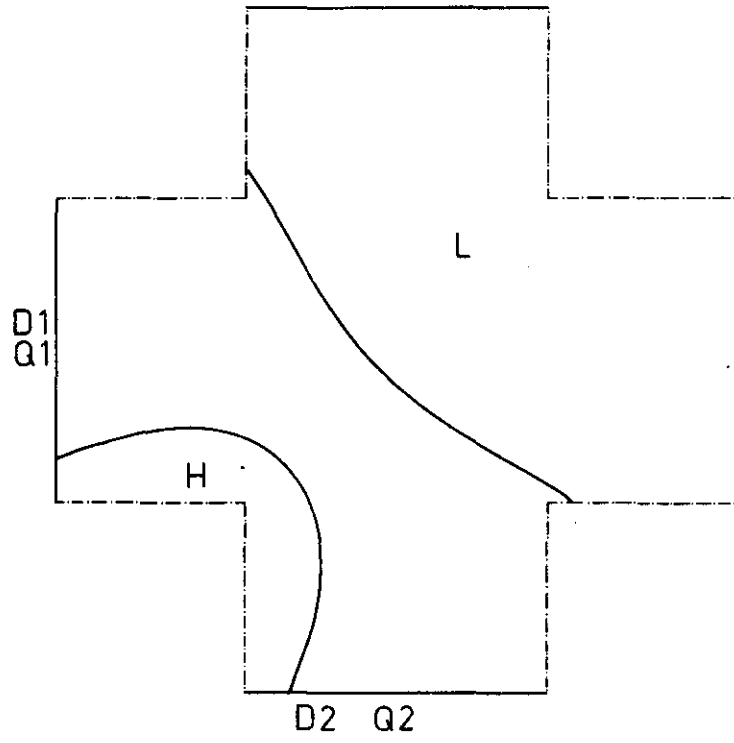


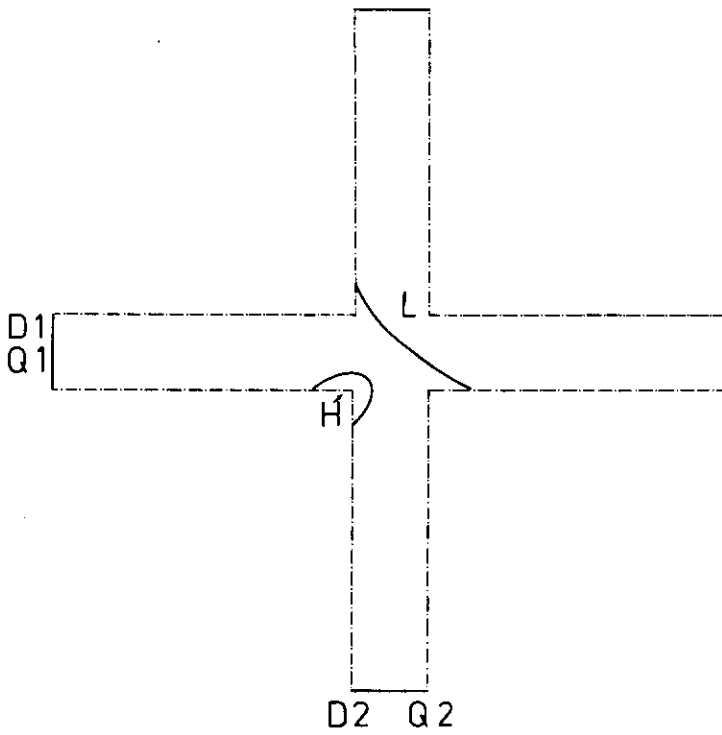
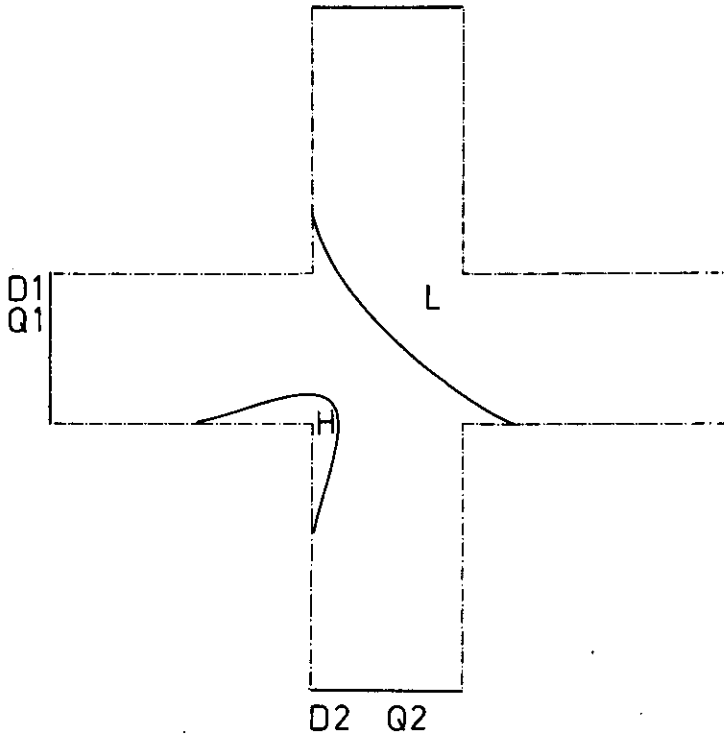


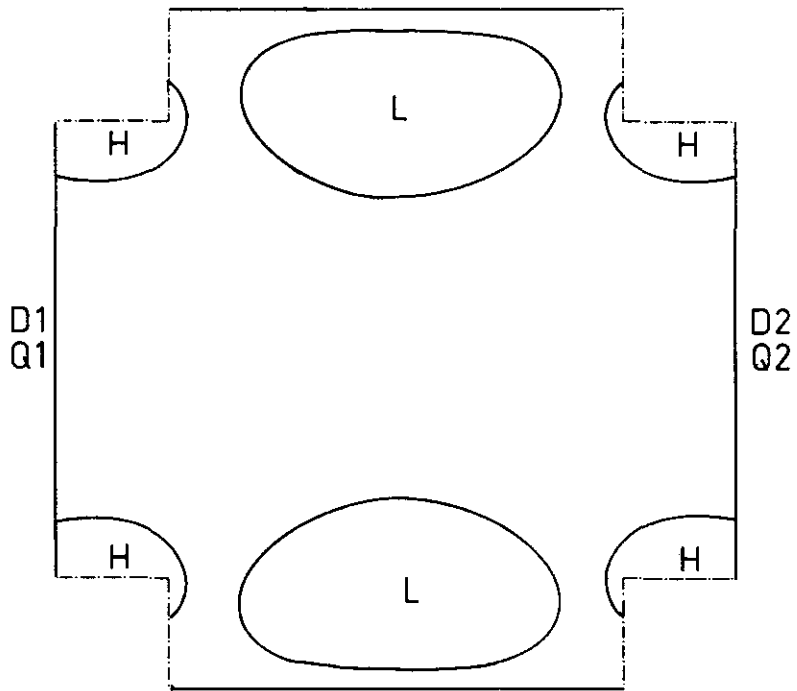
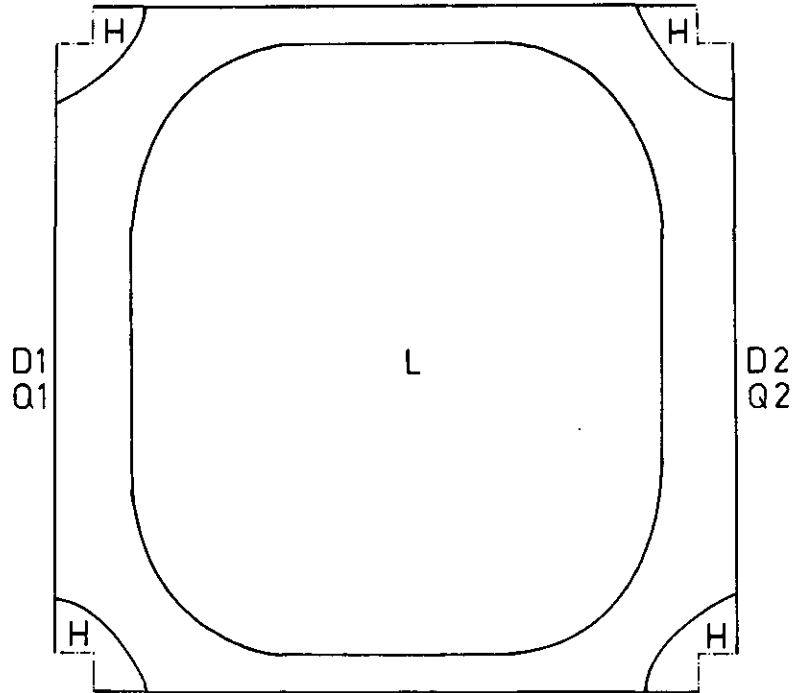


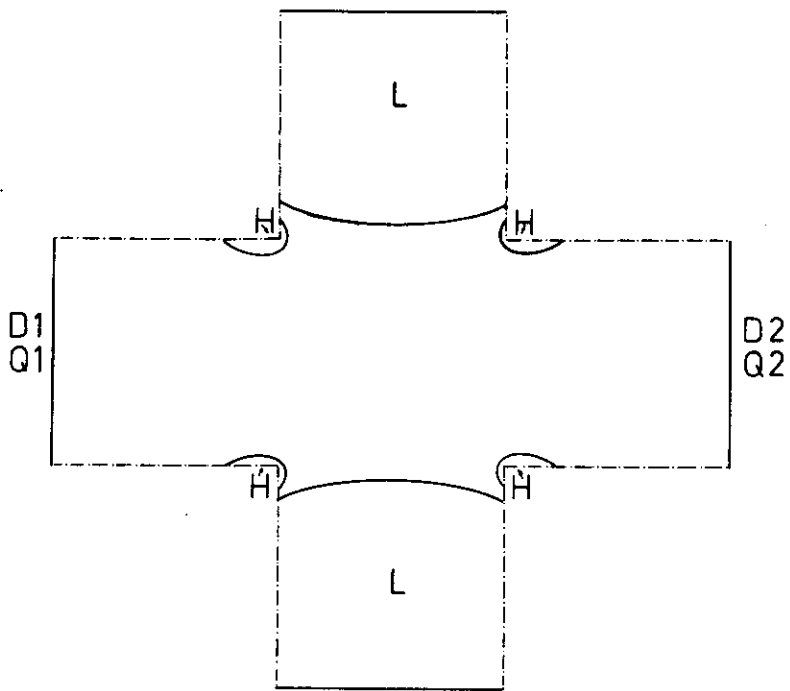
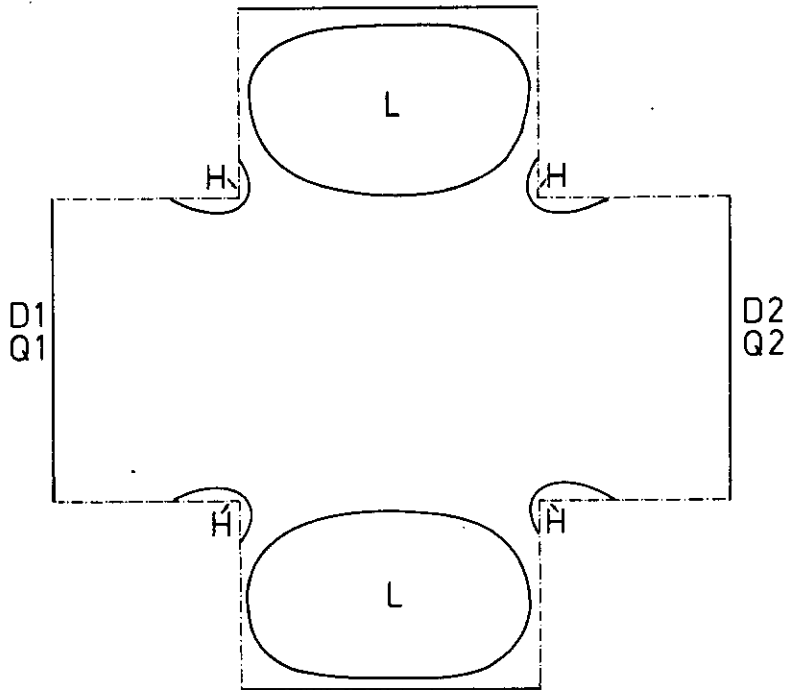


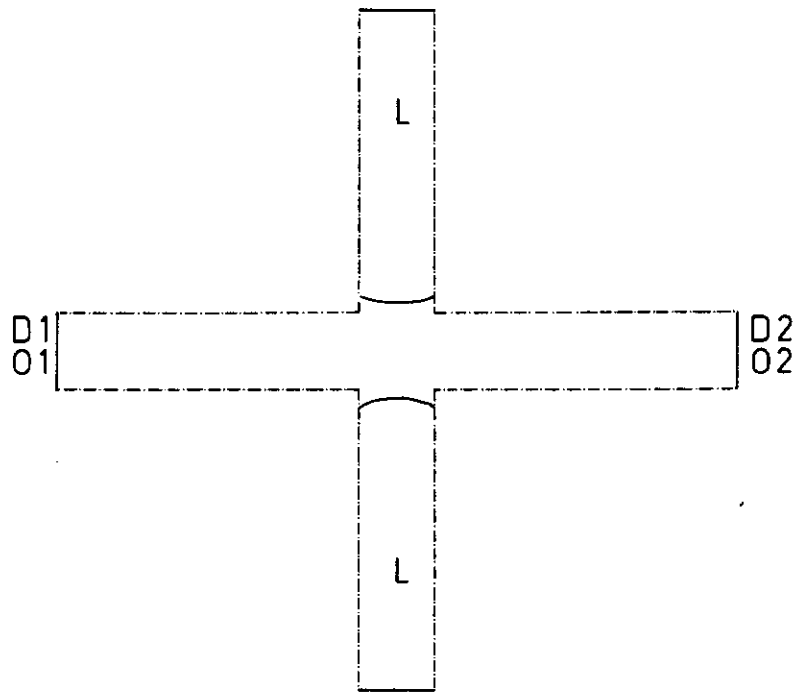
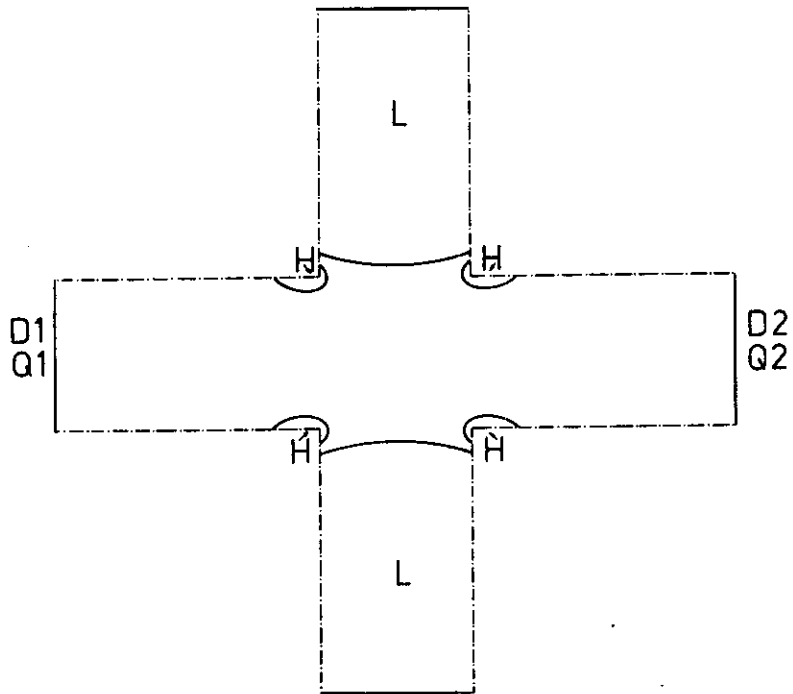


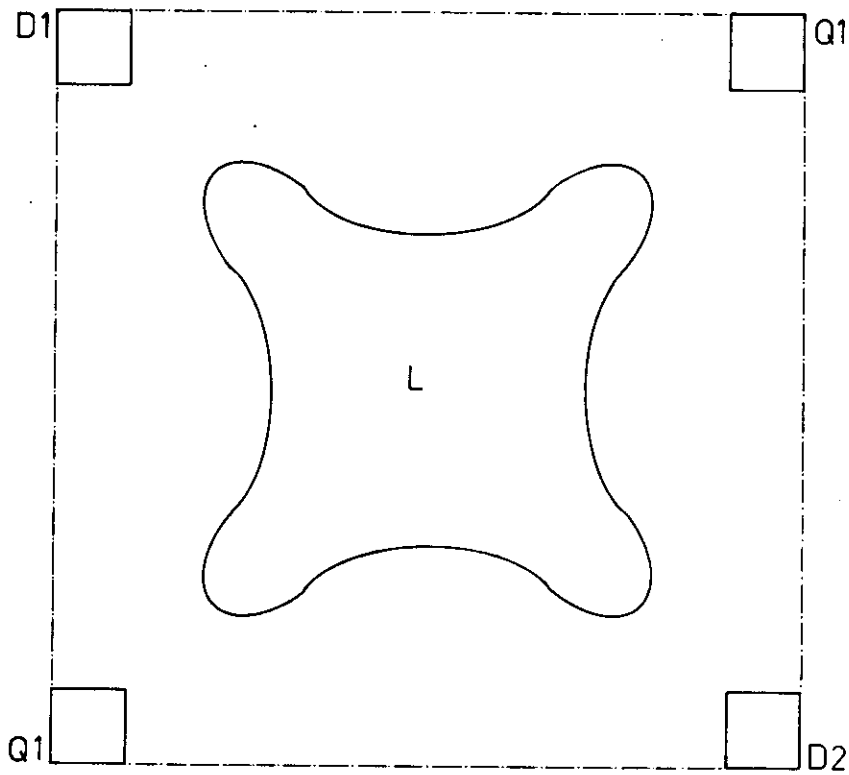
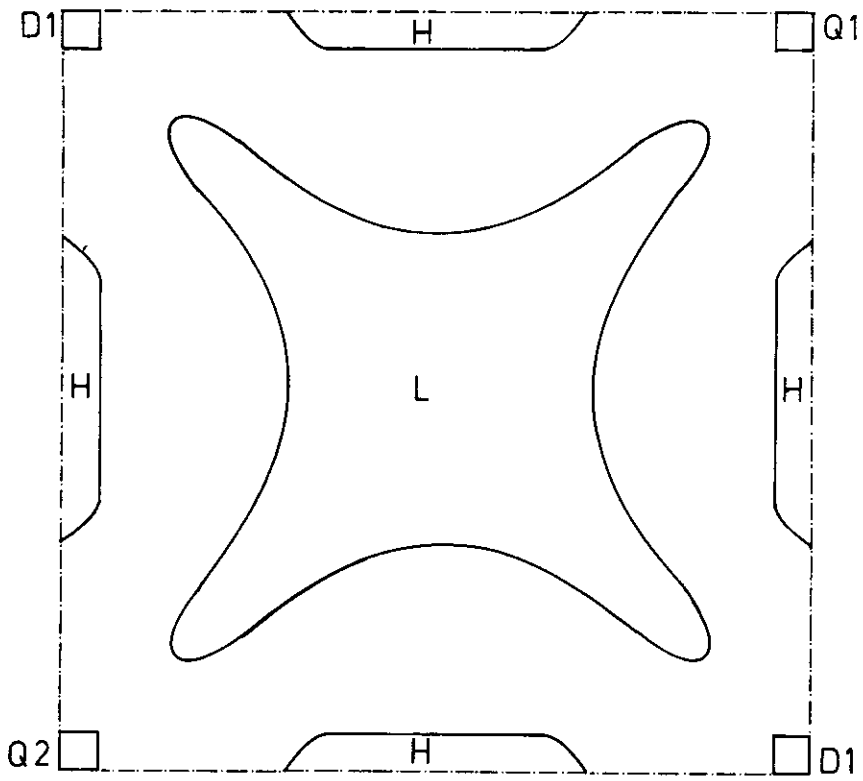


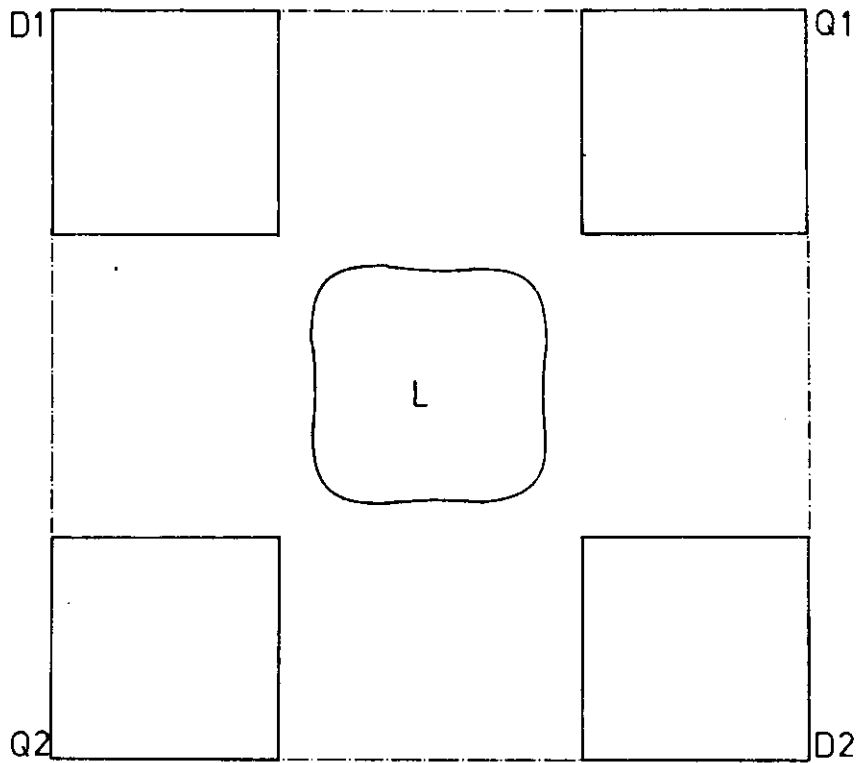
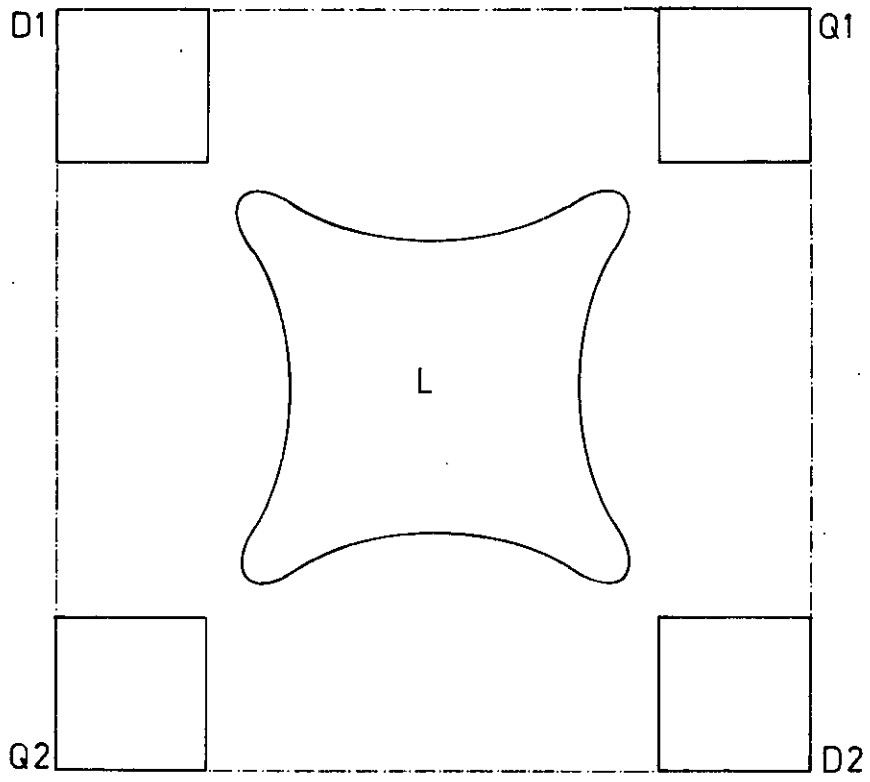


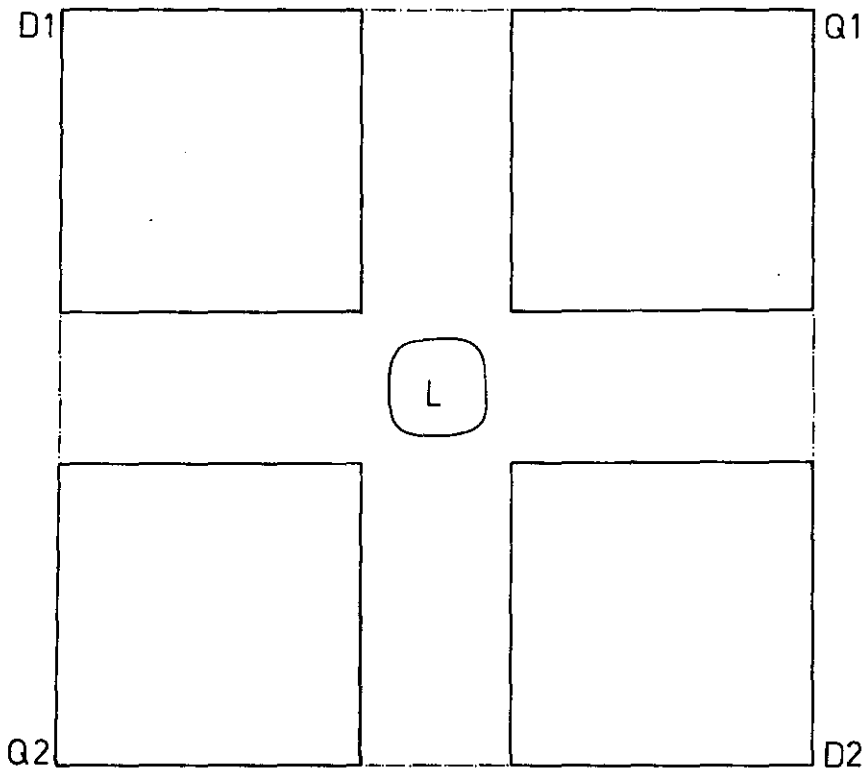




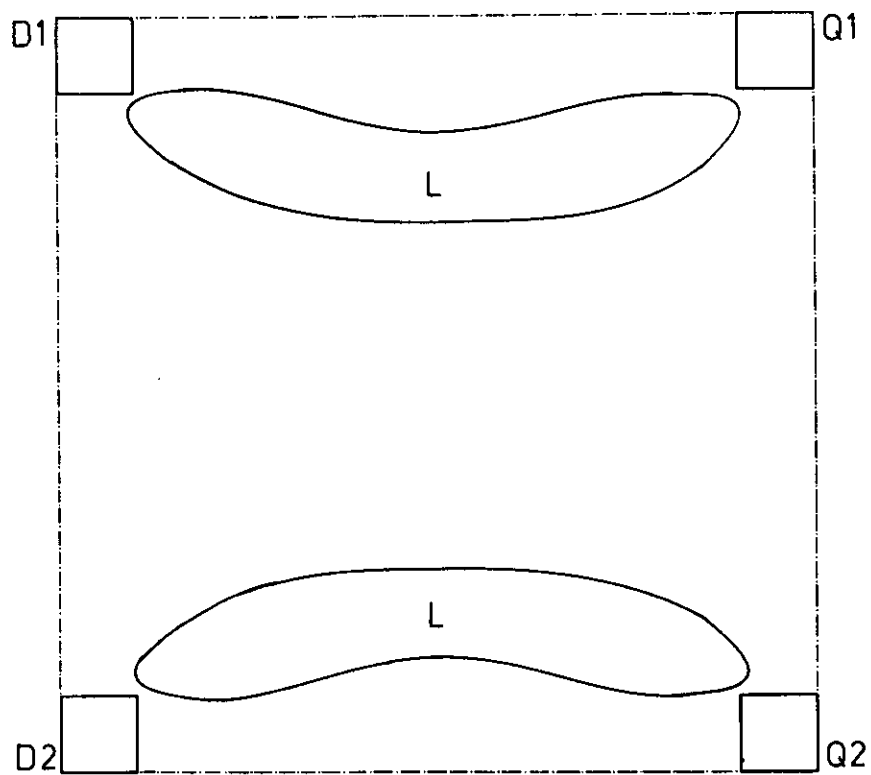
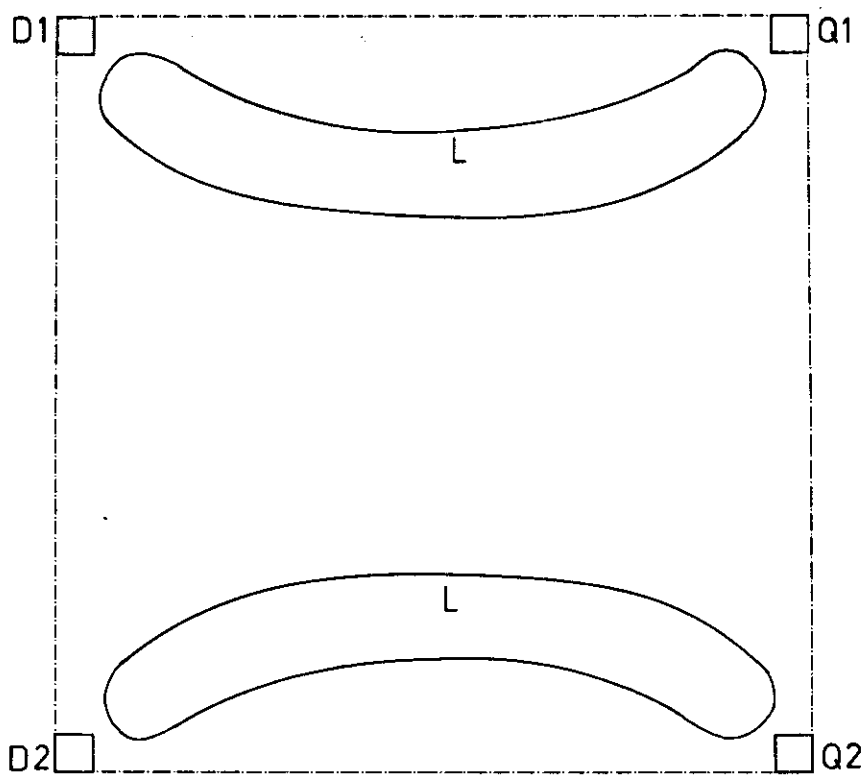


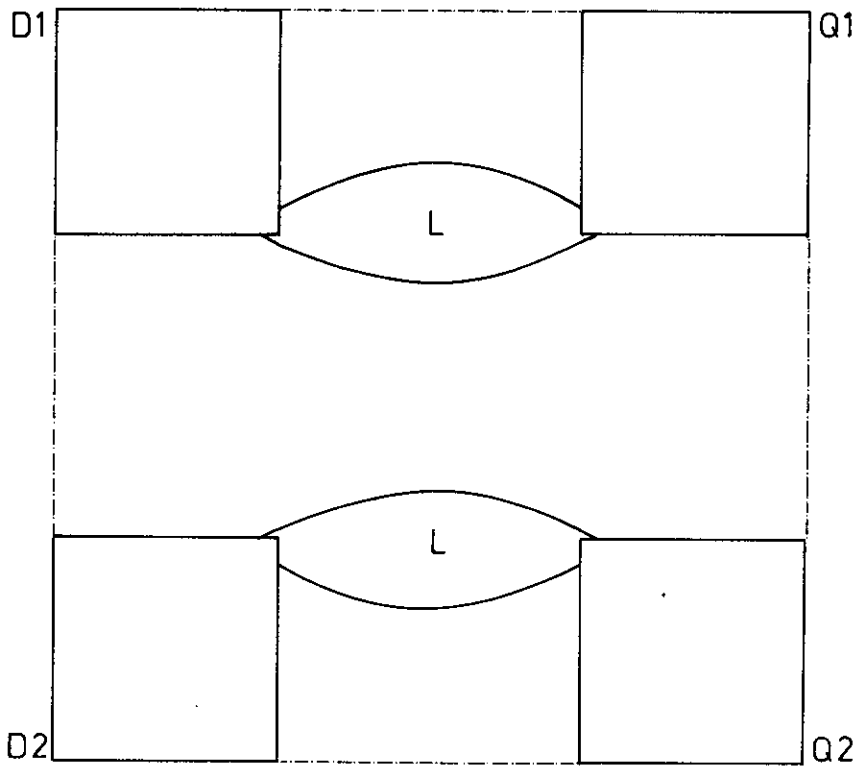
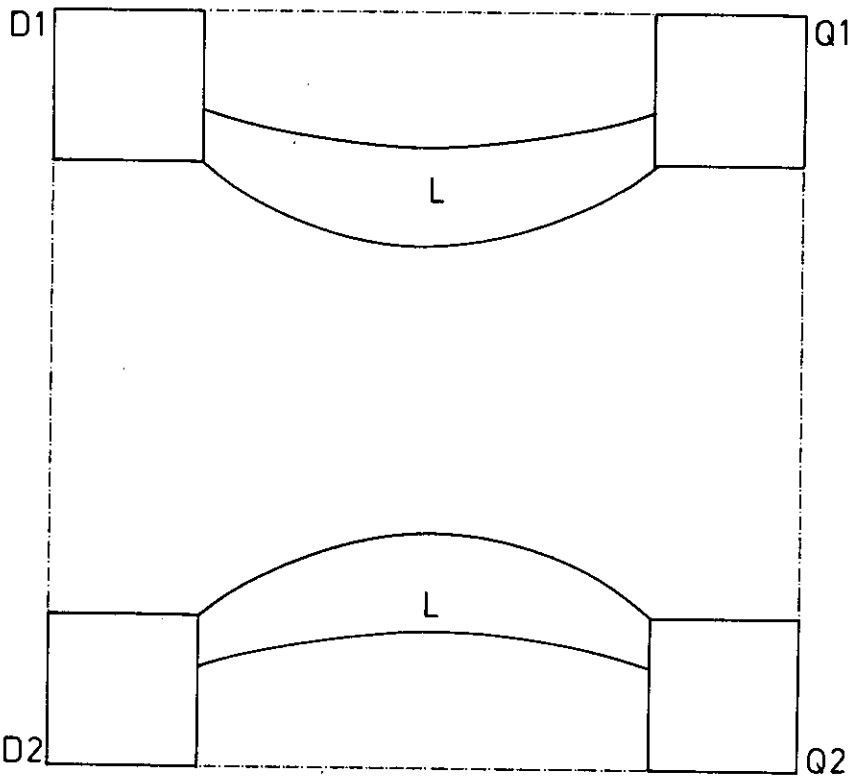


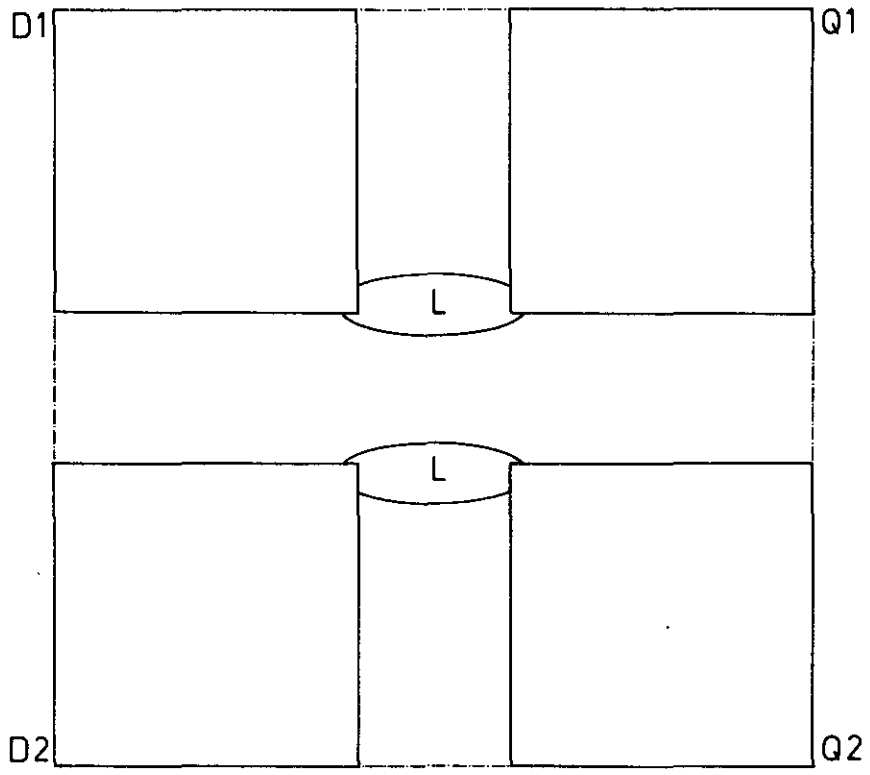


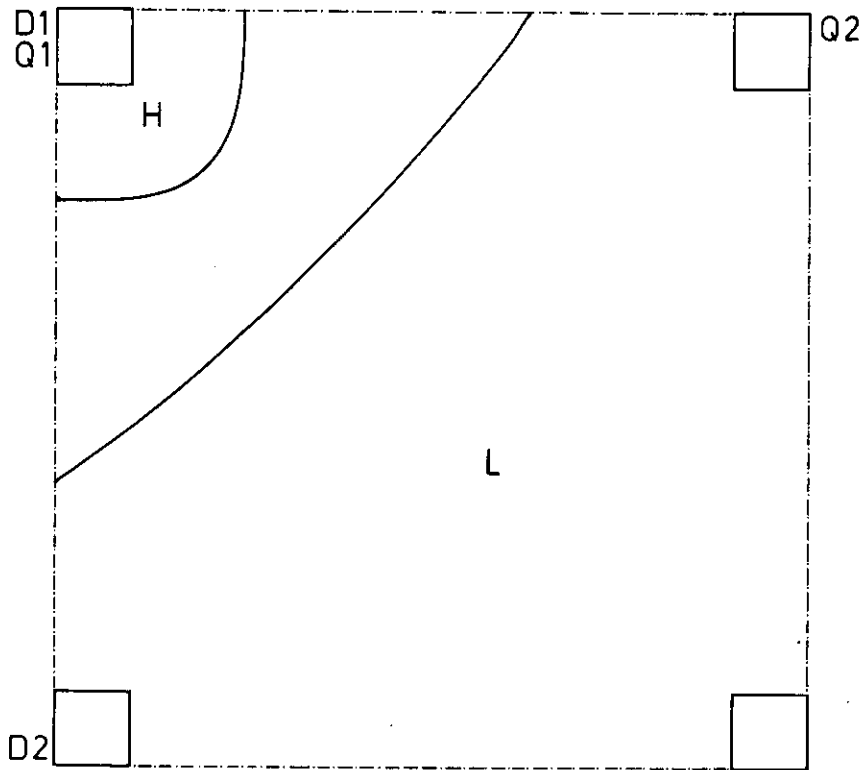
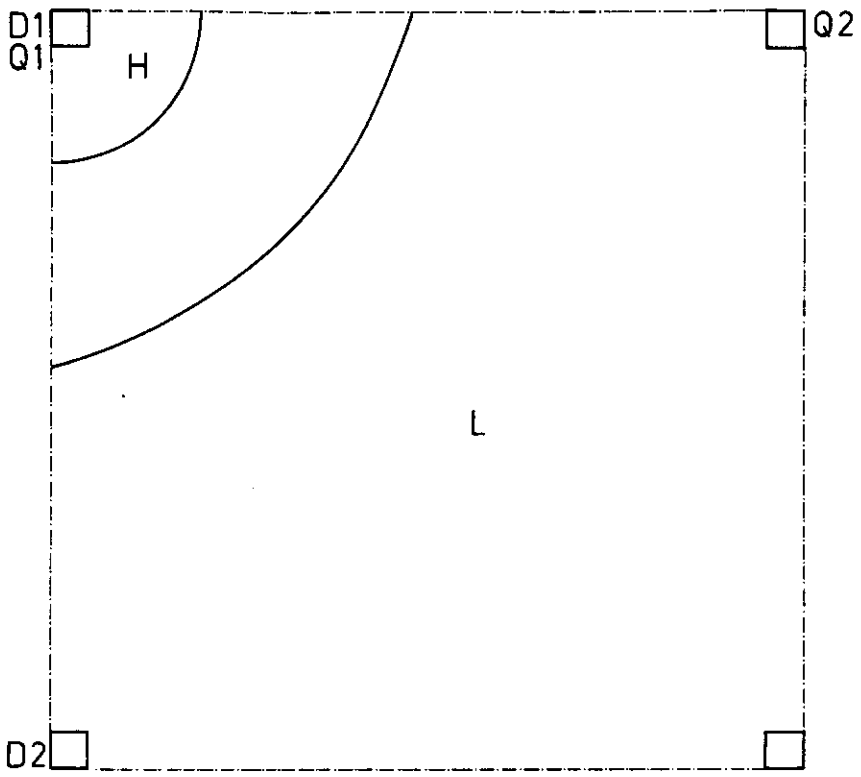


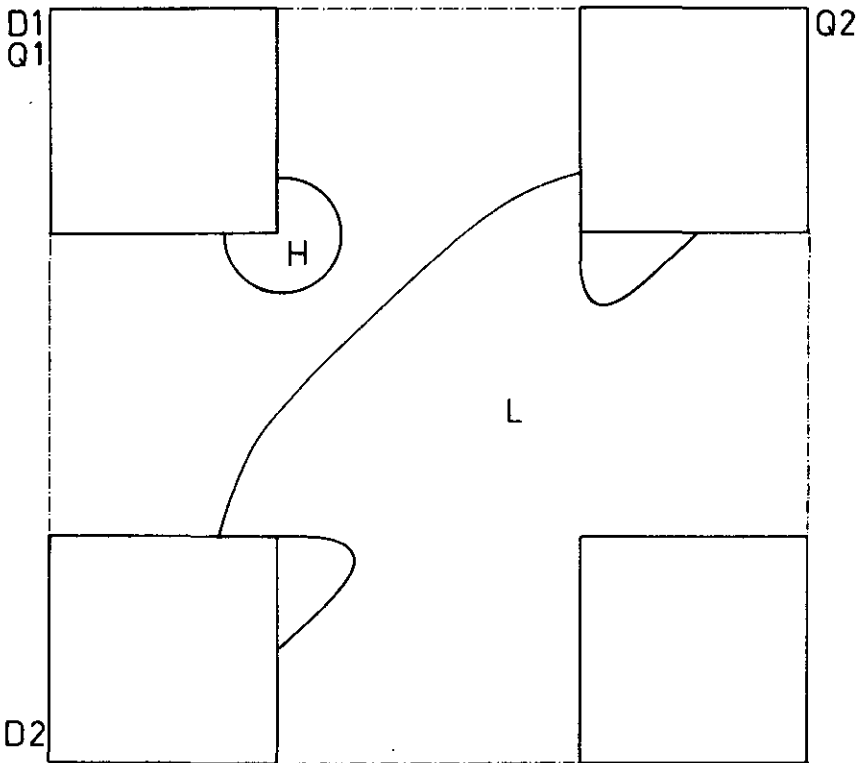
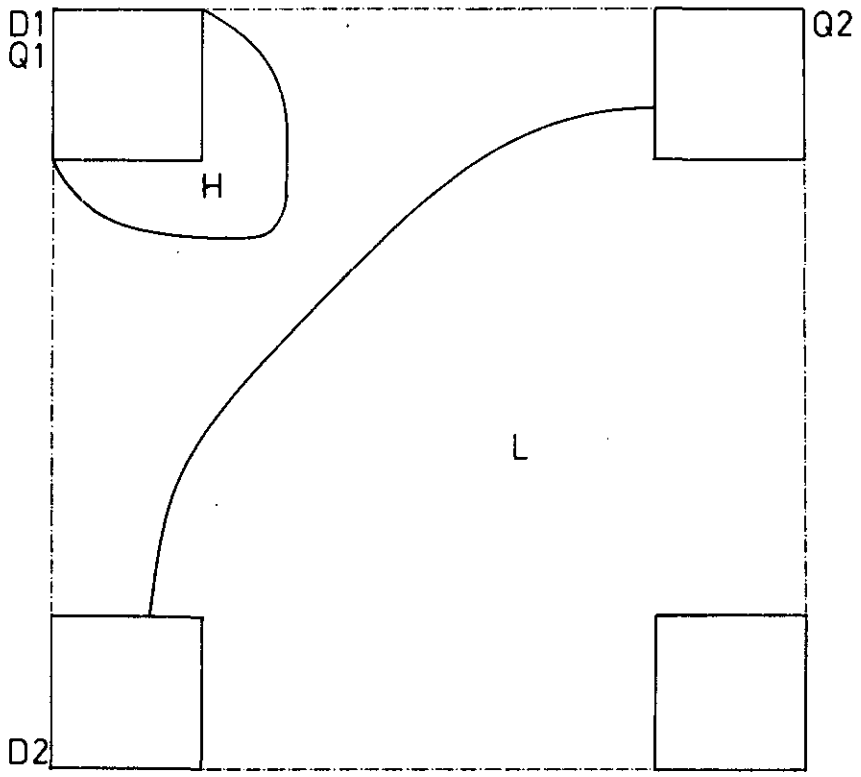


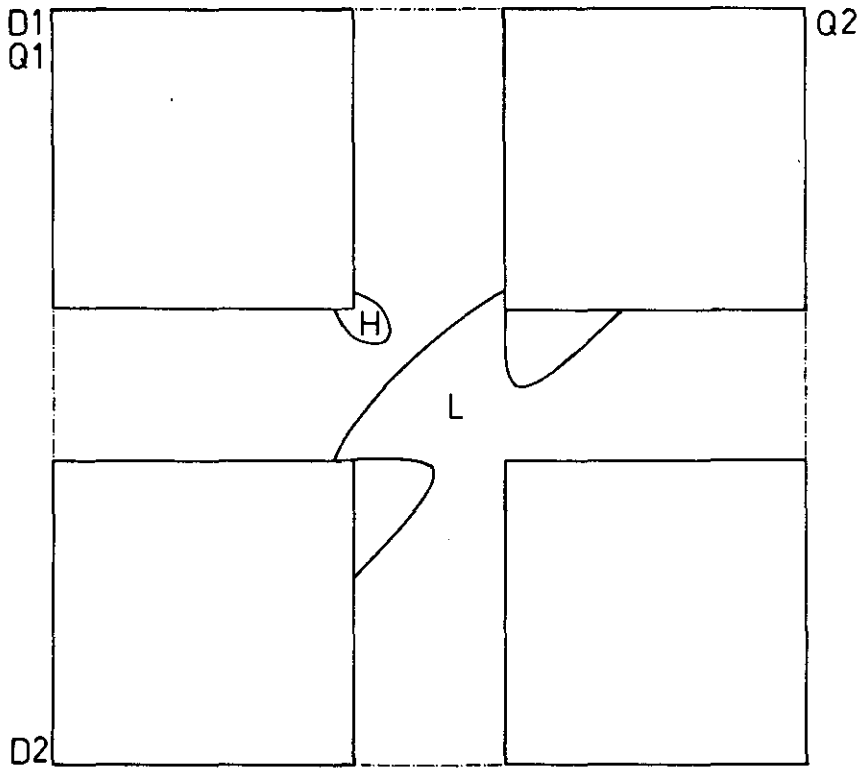


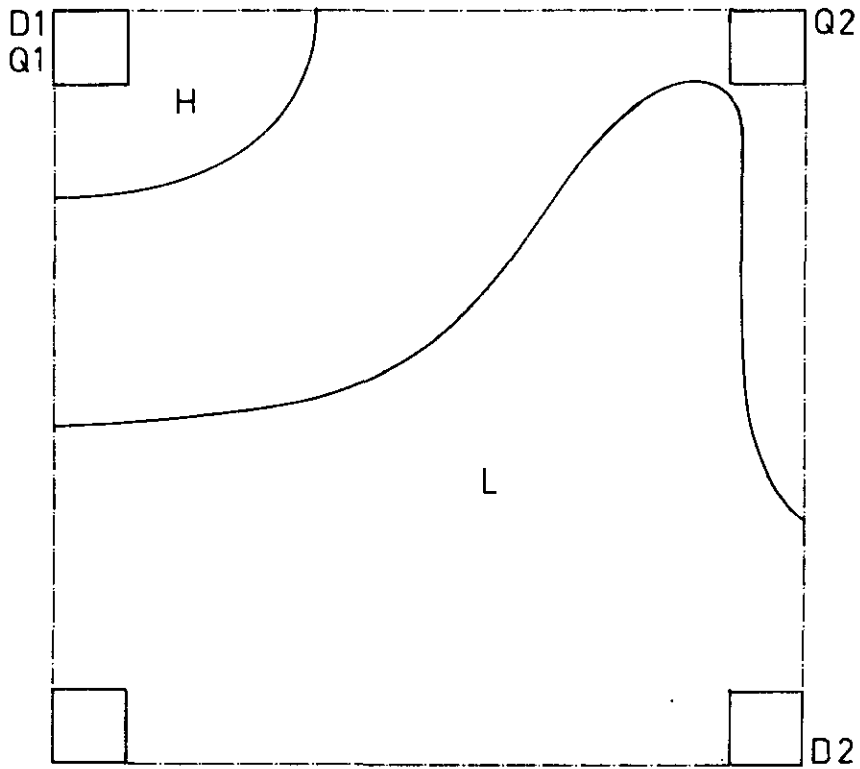
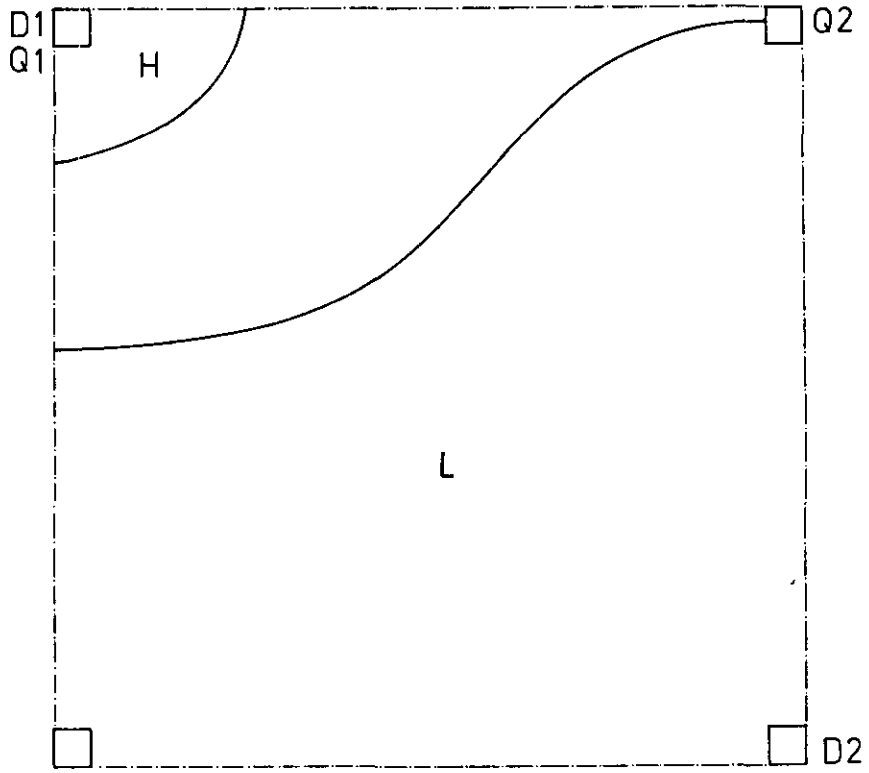


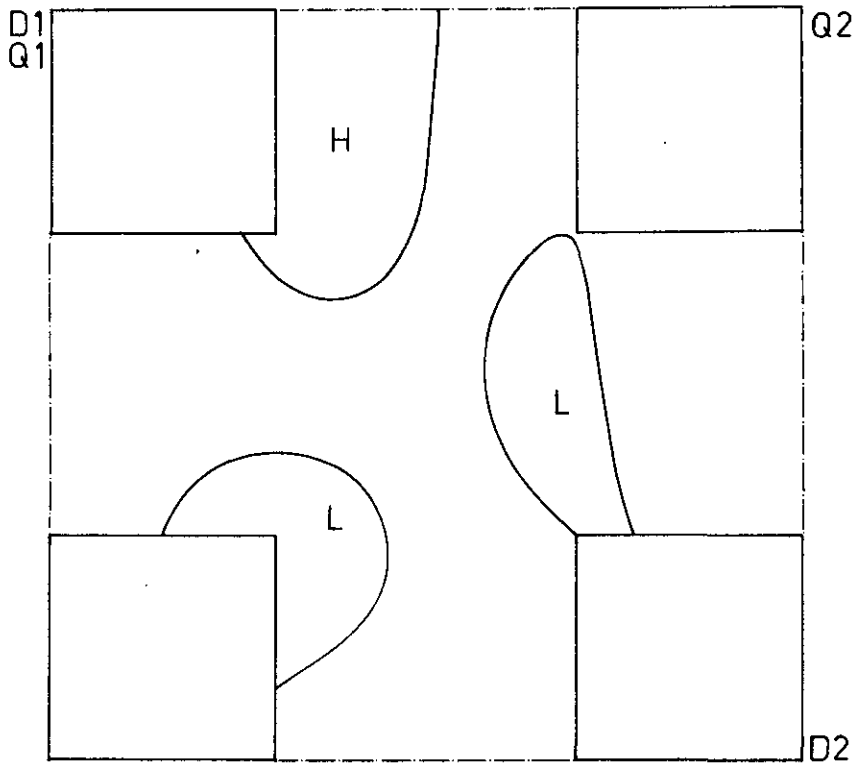
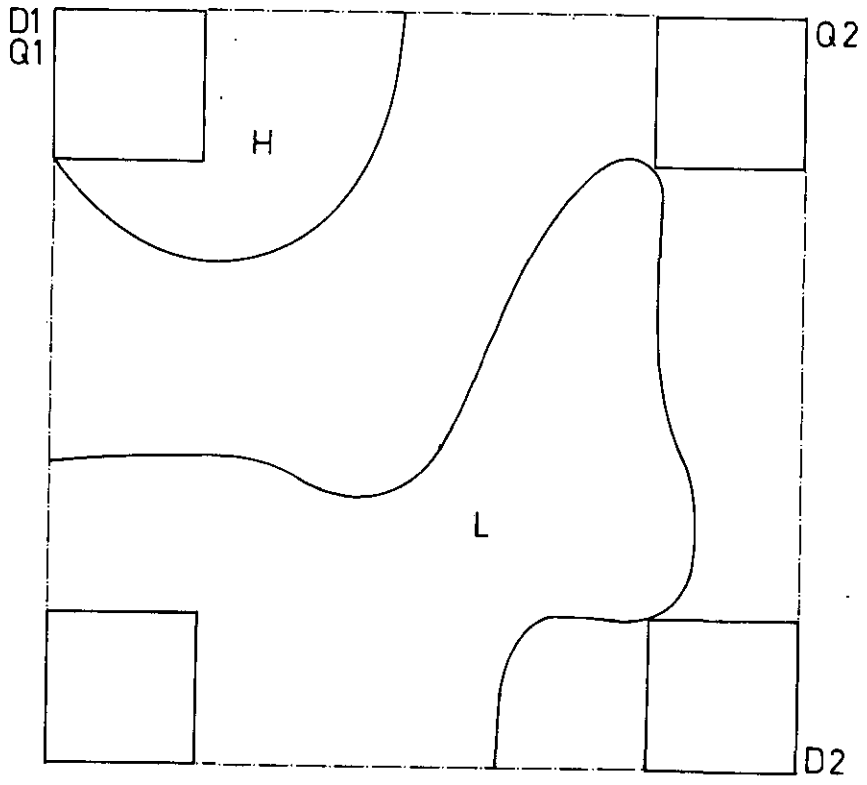




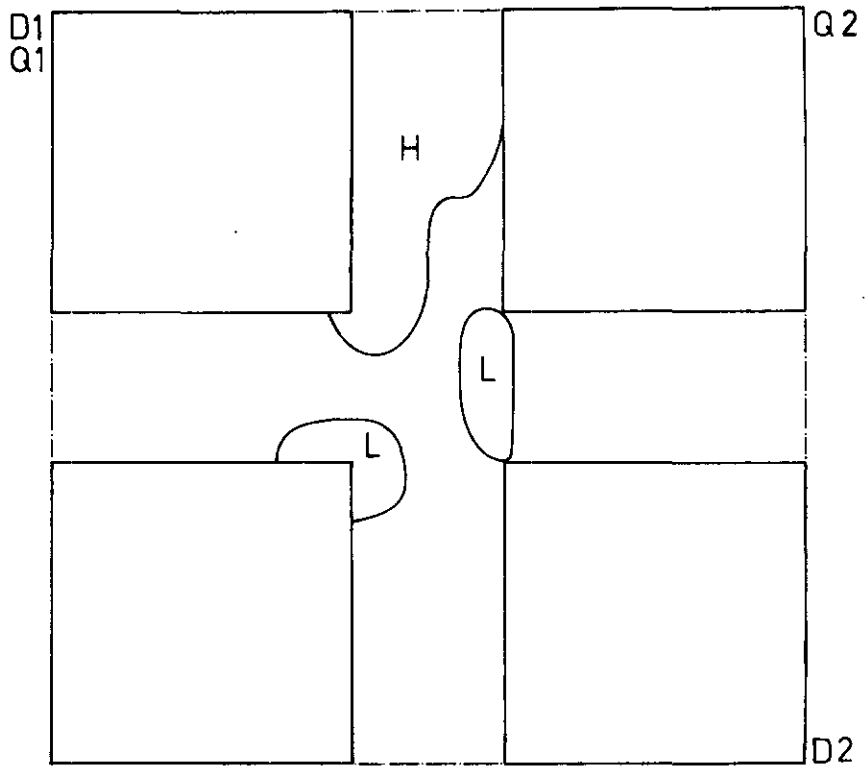


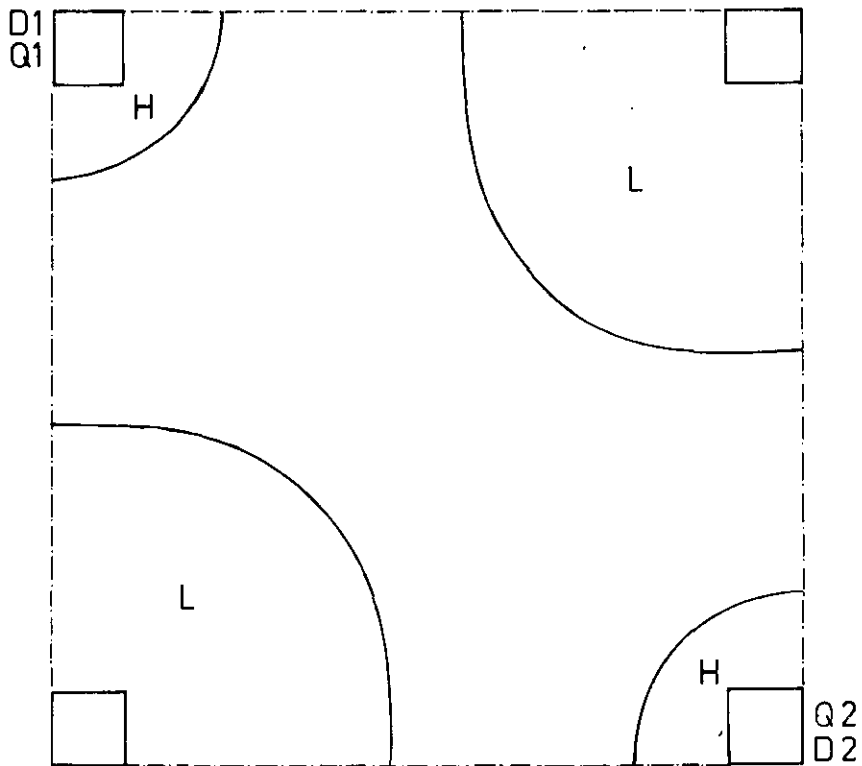
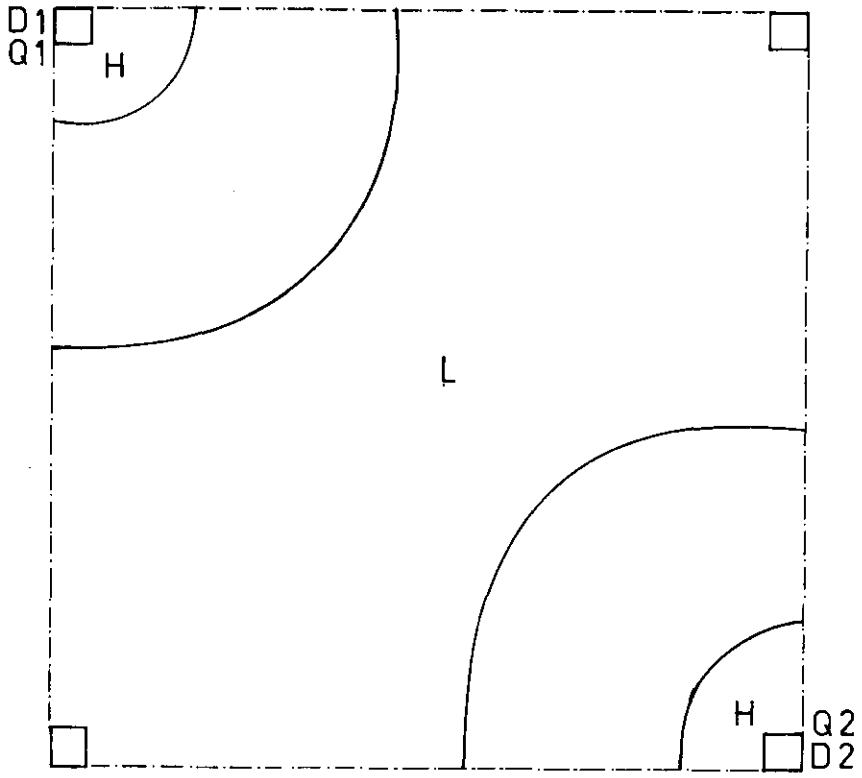


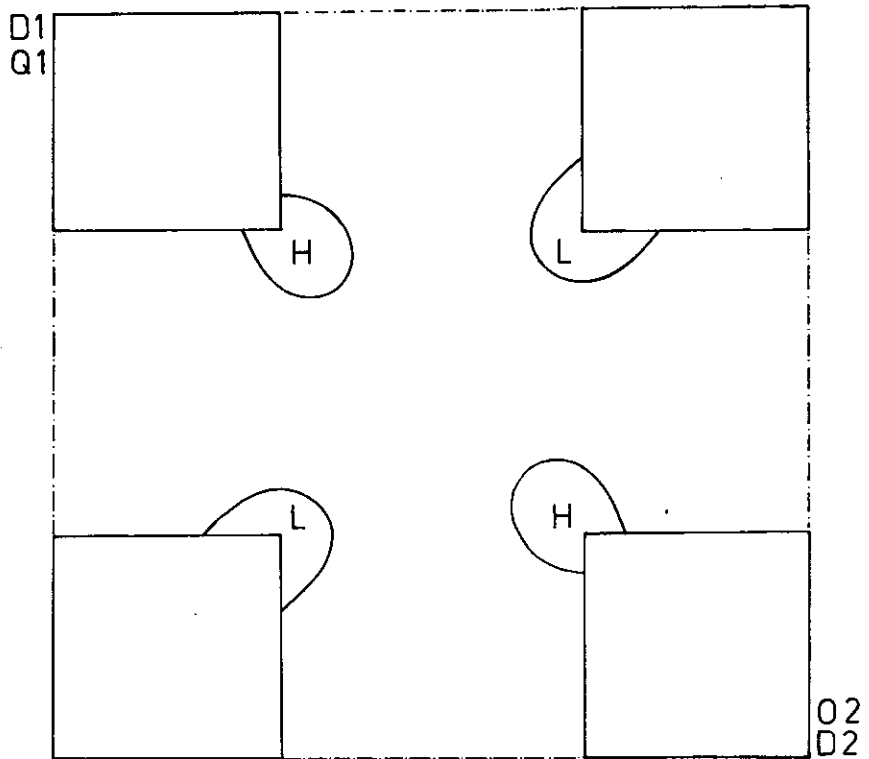
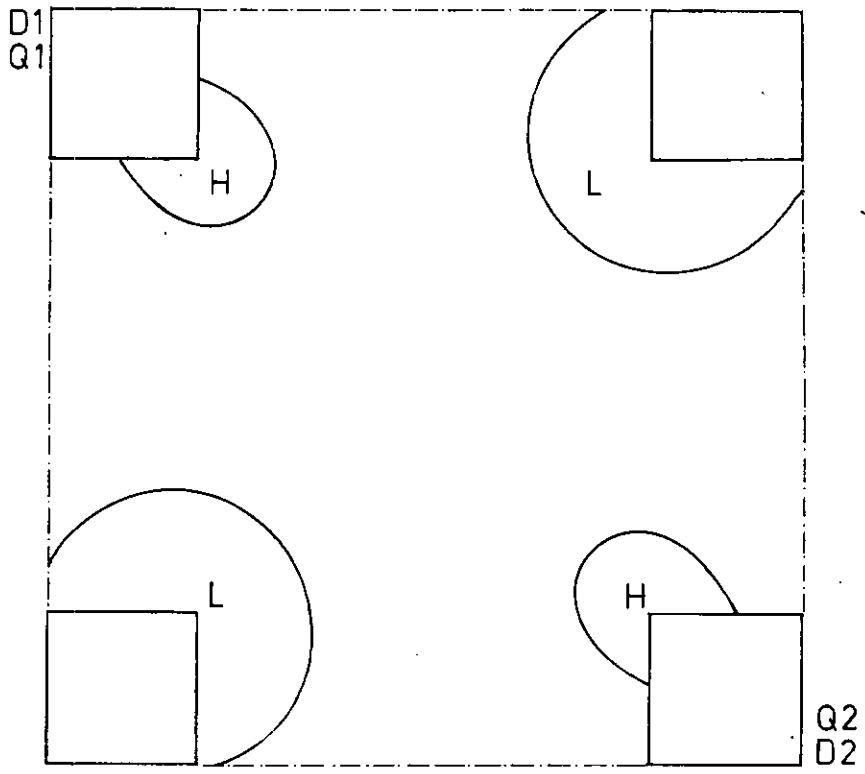


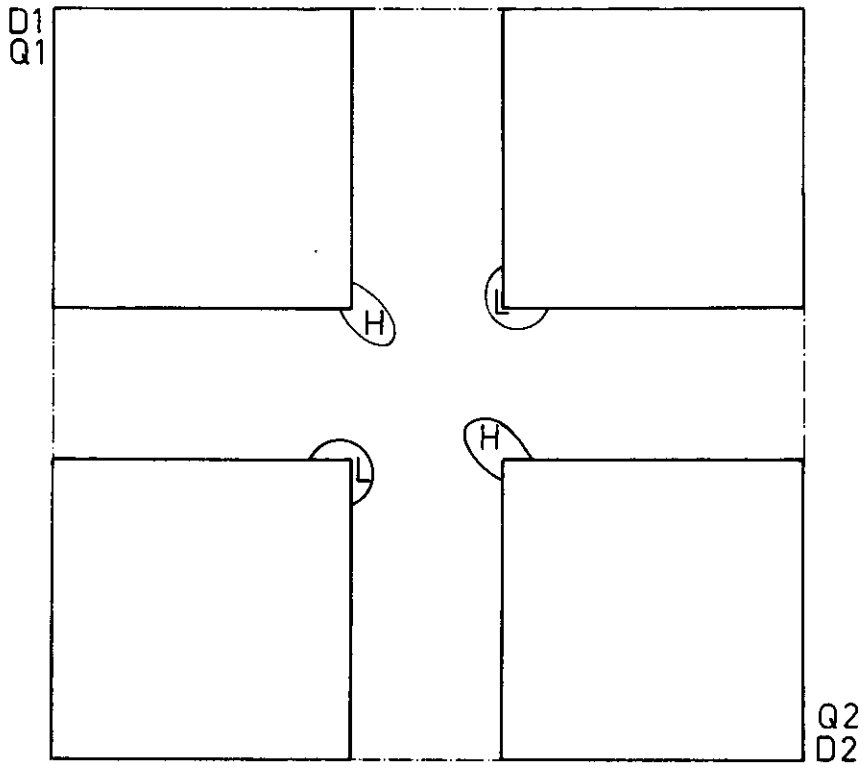


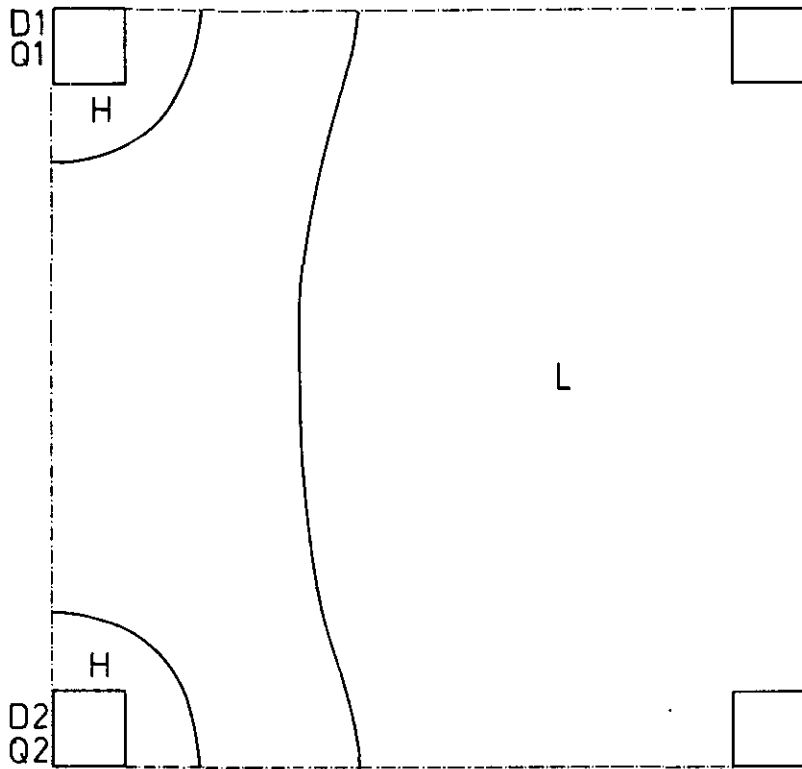
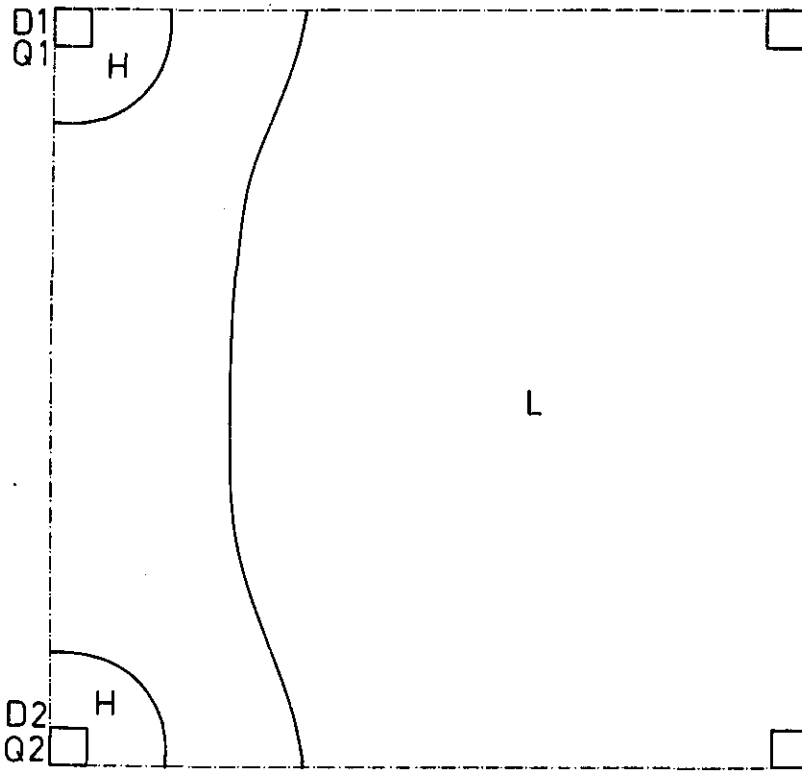


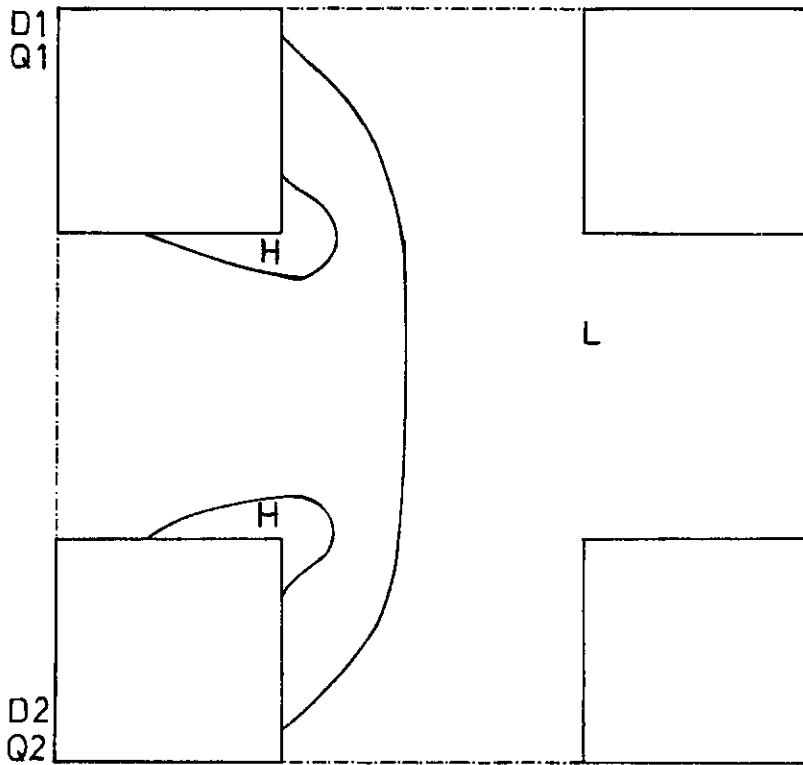
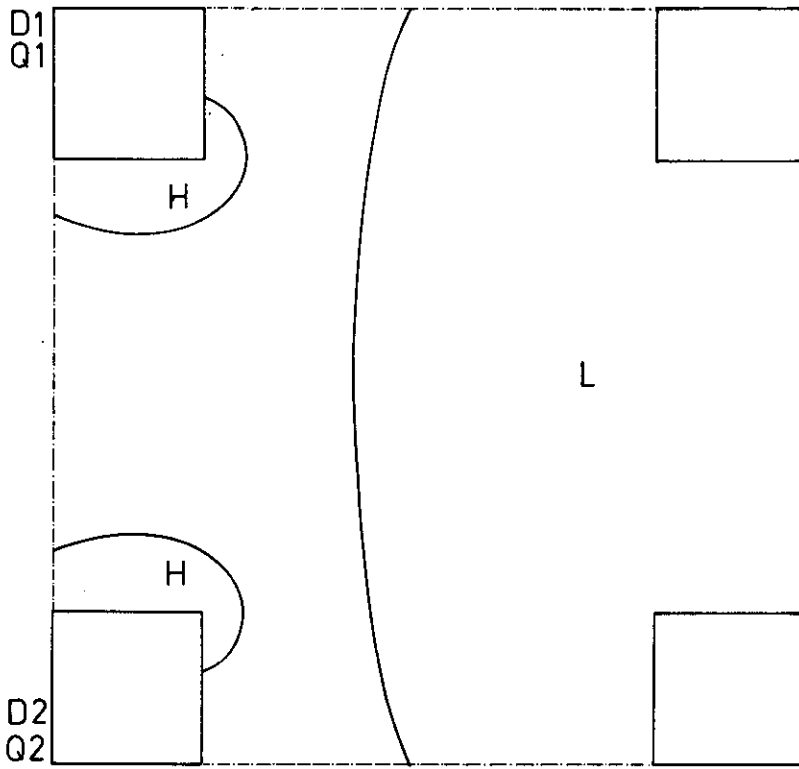


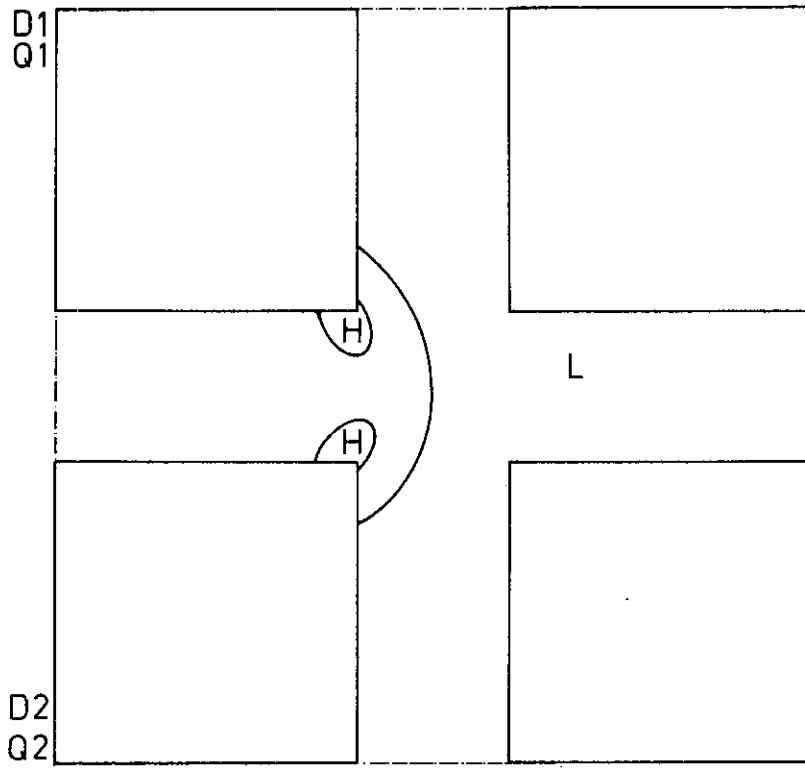












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