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Chemical differentiation, cold storage and remobilization of magma in the Earth’s crust

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The formation, storage and chemical differentiation of magma in the Earth’s crust is of
fundamental importance in igneous geology and volcanology. Recent data are challenging the
high melt fraction ‘magma chamber’ paradigm that has underpinned models of crustal magmatism
for over a century, suggesting instead that magma is normally stored in low melt fraction ’mush
reservoirs’1-9. A mush reservoir comprises a porous and permeable framework of closely packed
crystals with melt present in the pore space.1,10 However, many common features of crustal
magmatism have not yet been explained by either the ‘chamber’ or ‘mush’ reservoir concepts.1,11
Here we show that reactive melt flow is a critical, but hitherto neglected, process in crustal mush
reservoirs, occurring because buoyant melt percolates upwards through, and reacts with, the
crystals.10 Reactive melt flow in mush reservoirs produces the low crystallinity, chemically
differentiated (silicic) magmas which ascend to form shallower intrusions or erupt to the
surface.11-13 The magmas can host much older crystals, stored at low and even sub-solidus
temperatures, consistent with crystal chemistry data.6-9 Changes in local bulk composition caused
by reactive melt flow, rather than significant increases in temperature, produce the rapid increase
in melt fraction that remobilizes these cool- or cold-stored crystals. Reactive flow can also
produce bimodality in magma compositions sourced from mid- to lower-crustal reservoirs.14,15
Trace element profiles generated by reactive flow are similar to those observed in a well-studied
reservoir now exposed at the surface.16 We propose that magma storage and differentiation
primarily occurs by reactive melt flow in long-lived mush reservoirs, rather than by the commonly
invoked process of fractional crystallisation in magma chambers.14

Magma reservoirs occur at several depths within the crust and typically grow incrementally
through the intrusion of dykes or sills.1,11,13,16,17 High melt fractions must sometimes be present in
these reservoirs to produce eruptible, low-crystallinity magmas.1,7,8,9,13 However, geophysical data
suggest that reservoirs have low melt fraction even beneath active volcanoes2,5 and crystal
chemistry data indicate that long-term magma storage occurs at low or even sub-solidus
temperature.6-9 High melt fractions are therefore ephemeral, yet geochemical models typically
assume differentiation occurs by crystal fractionation from low-crystallinity magmas;11,14 moreover,
geochronological data demonstrate that crustal magma reservoirs can be long-lived, spanning
hundreds of thousands to millions of years.17-21 Existing models of crustal magma storage and
differentiation cannot reconcile these conflicting observations.

We use numerical modelling to investigate the storage and chemical differentiation of magma in
crustal reservoirs. The model describes repeated intrusion of mafic to intermediate sills into the
mid- to lower crust,12,13,16,21-23 the associated transport of heat via conduction and advection and, in a
key advance, mass transport via reactive flow of buoyant melt through the compacting crystal
framework.10 Transport of chemical components with the melt modifies the local bulk composition,
and melt fraction changes in response to the chemical reactions that maintain local thermodynamic
equilibrium. Phase behaviour is modelled using a two-component, eutectic phase diagram that,
although much simplified compared to natural systems, captures the critically important impact of
bulk composition on melting behaviour and the complex non-linear relationships between
composition, melt fraction and permeability (see Methods).10 Melting relationships obtained from
the phase diagram approximate common crustal igneous systems (Extended Data Fig. 1). The
concentration of an incompatible trace element is also modelled assuming a constant partition
coefficient.

Typical results are shown in Figure 1 (see also Supplementary Video 1). In this example, 100m
thick basalt (mafic) sills are intruded randomly over a depth range of 600m, initially at 18km depth
and then around a depth that is controlled by the density contrast between intruding magma and
host mush, reflecting the evolving reservoir composition and melt fraction (see Methods). We
emplace 7.8 km of basalt in total, at an average rate of 5 mm·yr\(^{-1}\) typical of crustal magmatic
systems,\(^{22-24}\) into solid crust with an initial geotherm of 20 K·km\(^{-1}\).\(^{21-23}\) Our example was chosen to
facilitate comparison with data from a well-studied deep crustal section.\(^{16,21}\) The key findings are
replicated over the depth range of 10-30 km typical of many crustal magma reservoirs and following
intrusion of intermediate as well as mafic magma, using model parameters over a wide range
reasonable for such systems (see Methods and Extended Data Table 1).

Initially, following each sill intrusion, the melt fraction rapidly falls to zero so there is no
persistent magma reservoir (Supplementary Video 1 and Extended Data Figure 2). This is the
‘incubation phase’ of the incipient magma reservoir, observed also in models that neglect reactive
flow.\(^{22,23}\) However, in our model, chemical differentiation occurs within each intrusion before it
solidifies, with more evolved melt (enriched in the incompatible trace element) accumulating at the
top of the intrusion, and more refractory and depleted crystals accumulating at the base. The rapid
increase in crystallinity traps the magma at the site of intrusion, but differentiation creates
compositional contrasts that cause the intrusion depth to progressively increase (Supplementary
Video 1 and Extended Data Figure 3a).

The incubation phase ends when the melt fraction is greater than zero between successive sill
intrusions, whereupon a magma reservoir has formed (Figure 1a; Supplementary Video 1). Melt is
now persistently present, but melt fraction remains low except for a brief period after each new
intrusion (Extended Data Figure 2b). The reservoir comprises a mush, rather than a high melt
fraction magma chamber. Reactive flow now significantly modifies the predicted reservoir behaviour
compared to previous models.\(^{22,23}\)

Buoyant melt migrates upwards through the mush, accumulating in the upper part of the
reservoir because it cannot travel beyond the solidus isotherm where the melt fraction and
permeability fall to zero (Supplementary Video 1). Melt composition evolves as it flows into, and
reacts with, progressively cooler mush. Reactive flow reduces, or removes, early-formed
compositional contrasts, so the locally varying melt fraction controls the depth of later sill intrusions,
which decreases as melt migrates upwards (see Methods). This is the ‘growing phase’ of the
reservoir.

The growing phase ends when melt accumulates below the solidus isotherm to form a high melt
fraction (typically >0.7) layer overlying a thick (several km), low melt fraction (typically <0.2) mush
(Figure 1b and Supplementary Video 1). The melt-rich layer contains chemically differentiated felsic
magma and can grow to several 100’s m in thickness. Although not captured by the model, buoyant
magma in the layer will be prone to leave the reservoir to produce shallower intrusions or volcanic
eruptions.\(^{25,26}\) Once magma leaves, a new layer grows by the same mechanism (see Methods).

This is the ‘active phase’ during which the reservoir can deliver evolved, low crystallinity magma
(Extended Data Figure 2b). We suggest that, although geophysical surveys are probing active
reservoirs, they image only the low melt fraction mush;\(^{2,5}\) the overlying high melt fraction layers are
not observed, because they are ephemeral and/or too thin to be resolved. Geophysical detection of
such a layer would suggest that magma mobilisation (and possible eruption) was imminent.\(^{7}\)

When intrusion of new sills ends, reactive flow continues wherever the temperature is above the
solidus but, overall, the reservoir cools. This is the ‘waning phase’ (Supplementary Video 1;
Extended Data Figure 3b) that persists until the mush has completely solidified (Extended Data
Figure 2b). If exhumed, the resulting body of rock is termed a deep crustal section of which there
are several natural examples.\(^{16,21}\)

During the active phase, the high melt fraction layer forms towards the top of the reservoir
where the temperature is low, rather than at the highest temperature (Figure 1b). This counter-
intuitive result is a consequence of reactive flow, whereby melt accumulation causes the local bulk
composition to evolve towards the eutectic. Melt composition in more chemically complex systems
will evolve towards other low-variance states such as cotectics, peritectics or multiple-saturation
points (see Methods), but the overall behaviour will be similar. A key finding here is that high melt fraction layers in crustal mush reservoirs can form in response to changes in bulk composition caused by reactive melt flow, rather than significant increases in temperature.

Magma in a high melt fraction layer contains c. 10% crystals (Figure 2a). These ‘antecrysts’ can long pre-date magma formation, because they derive from crystallisation of early sills at the top of the reservoir. Once formed, the antecrysts are stored at near- or sub-solidus temperature (i.e. ‘cool’ or ‘cold’; Figure 2b). The local temperature gradually increases in response to ongoing intrusion of sills deeper in the reservoir and, eventually, exceeds the solidus. Soon afterwards, buoyant, evolved melt, migrating upwards through the pore-space, accumulates around these older antecrysts, causing the local melt fraction to increase rapidly and by far more than would be possible by heating alone (Figure 2b).\textsuperscript{6,7,18,27} Cold mush is remobilized here not by a significant increase in temperature, but by buoyancy-driven reactive flow supplying evolved melt from deeper, more refractory parts of the reservoir, where temperature can be high but the melt fraction remain low (Figure 2c).

Remobilization is primarily caused by changes in local bulk composition, rather than temperature. In our example, melt accumulation forms a low crystallinity magma a few centuries after the local temperature exceeds the solidus, yet the magma contains antecrysts formed up to c. 1–1.4Ma earlier (Figure 2b). The range of antecrust ages reflects the timing of sill intrusions relative to the timing of melt accumulation. Crystal chemistry data show cool or cold storage and remobilization of older antecrysts hosted by younger felsic magma;\textsuperscript{6-9} our results suggest that this could result from reactive melt flow accumulating young, felsic melt within older mush. The antecrysts are not in equilibrium with the younger melt, creating disequilibrium crystal textures such as partial resorption. Flow of buoyant melt into the high melt fraction layer will drive convective overturn and homogenisation before, or during, evacuation of magma, yielding a range of antecryst ages that may span the entire reservoir history.\textsuperscript{28}

Magmas in the high melt fraction layers have evolved composition. Conversely, magmas in the sills shortly after intrusion have compositions close to the intruded basalt. Low crystallinity, mafic or felsic magmas can therefore leave the reservoir, but not magmas with intermediate composition. Many volcanic settings are characterised by bimodal volcanism (the ‘Daly Gap’), especially in oceanic settings (hotspots and island arc environments) and continental hotspots (Figure 3a).\textsuperscript{14,15,29} Our results suggest that compositional bimodality is another consequence of differentiation by reactive melt flow in mush reservoirs. However, not all systems show bimodality.\textsuperscript{10} Intermediate compositions could result from magma mixing\textsuperscript{15} or differentiation within multiple mush reservoirs comprising a vertically extensive magmatic system.\textsuperscript{1}

The modelled incompatible trace element concentration in the solidified reservoir shows a characteristic pattern. Towards the base, the spiky signature produced by differentiation in each sill during the incubation phase is preserved (Figure 3b). In the upper part, the profile is smoother and shows depletion relative to the initial concentration, reflecting extraction of melt. The top shows enrichment, reflecting accumulation of melt during the growing and active phases. Data from a deep crustal section show a similar pattern (Figure 3c).\textsuperscript{16} We suggest this pattern is another characteristic product of reactive melt flow in crustal mush reservoirs. Reactive melt flow at low melt fraction, rather than fractional crystallisation at high melt fraction, is the dominant mechanism controlling magma storage, accumulation and chemical differentiation in the continental crust (Fig. 4).

References


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Author Contribution Statement

MDJ wrote the code and produced the numerical results. JB prepared the phase equilibria model and calibrated this to experimental data. RSJS provided information on context and background for the study. All authors jointly designed the numerical experiments presented and drafted the manuscript text. MDJ prepared the figures.

Author Information

Reprints and permissions information is available at www.nature.com/reprints. The authors have no competing financial and/or non-financial interests to declare in relation to the work described. Correspondence and requests for materials should be addressed to m.d.jackson@imperial.ac.uk.

Main Figure Legends

**Figure 1 |** Snapshots showing temperature, melt fraction, bulk composition and incompatible trace element concentration as a function of depth during the growing and active phases of the reservoir after a, 0.97Ma following the onset of sill intrusions and b, 1.39Ma. Snapshots taken from Supplementary Video 1. At early times (not shown; see Extended Data Fig. 3a), during the incubation phase, individual sills cool rapidly. At later times a, during the growing phase, a persistent mush reservoir forms but the melt fraction is low. Buoyant melt migrates upwards and begins to accumulate at the top of the mush. During the active phase b, the accumulating melt forms a high melt fraction layer containing mobile magma. The composition of the melt in the layer...
is evolved and enriched in incompatible trace elements. Elsewhere in the mush, the melt fraction remains low. At late times (not shown; see Extended Data Fig. 3b) during the waning phase, sill intrusions cease and the mush cools and solidifies. To illustrate the key processes, intruding basalt and crust are assumed in this example to have the same initial incompatible trace element concentration. Shaded area in all plots denotes the vertical extent of basalt intrusions at that time. Equivalent results for sill intrusions at 10km depth are shown in Extended Data Fig. 5.

Figure 2 | Cold storage and rapid remobilization of magma. Plot a shows melt fraction as a function of depth at three different snapshots in time (1.346Ma and 4ka before and after). Reactive flow of buoyant melt produces a high melt fraction layer that migrates upwards. Plot b shows temperature and melt fraction as a function of time at a depth of 18.2km, close to the top of the reservoir. Similar results are obtained over the depth range 18-18.5km. Early sill intrusions rapidly cool and crystallize. The crystals are kept in ‘cold storage’ at sub-solidus temperature, but the temperature gradually increases in response to sill intrusions deeper in the reservoir. Soon (<0.3ka) after the temperature exceeds the solidus, the high melt fraction layer arrives at this depth (coloured arrow denotes the corresponding snapshot in plot a) and the reservoir is remobilised: the melt fraction increases rapidly to form a low crystallinity magma. The melt fraction increases much more rapidly and to a higher value than would be possible by melting alone. Plot c shows temperature and melt fraction as a function of time at a depth of 20km. Similar results are obtained over the depth range 18.5-21.5km. Melt fraction remains low because reactive flow has left a refractory residue at this depth. There is no remobilization, despite the increase in temperature. Data extracted from Supplementary Video 1. Equivalent results for intrusion at 10km depth are shown in Extended Data Fig. 6.

Figure 3 | Geochemical consequences of reactive melt flow in crustal magma reservoirs. Plot a shows SiO$_2$ content of low crystallinity (crystal fraction <30%) magmas. Solid curves show bulk magma composition (melt+crystals); dashed curves show melt composition alone. The peak at low SiO$_2$ corresponds to magma within the intruding sills; the peak at high SiO$_2$ corresponds to magma within high melt fraction layers near the top of the reservoir. Also shown for comparison are data from the Snake River Plain. The bimodality is clear, although the basalt has a lower SiO$_2$ content than modelled here. Results for different intruding sill compositions are shown in Extended Data Fig. 7. Plots b and c show modelled and observed neodymium concentration along a paleo-vertical transect through the Upper Mafic Complex in the Ivrea-Verbano zone. LBZ denotes Lower Basal Zone, IBZ denotes Intermediate Basal Zone, UBZ denotes Upper Basal Zone, MG denotes Main Gabbro and DIO denotes Diorite. Both modelled (b) and observed (c) data show a spiky profile at the base of the reservoir, depletion in the middle part of the reservoir, and enrichment at the top.

Figure 4 | Reactive flow of buoyant melt at low melt fraction is a critical mechanism controlling magma storage, accumulation and differentiation in mid- to lower-crustal reservoirs. The middle and lower parts of the reservoir comprise a thick (order km) mush layer, with low and relatively uniform melt fraction, formed by early sill intrusions during the incubation and growing phases. This layer is typically imaged in geophysical data. During the active phase, the upper part of the reservoir comprises transient layers containing either intermediate/mafic, or felsic magma, that can feed shallower intrusions or surface eruptions. The felsic magma layer is formed in response to changes in local bulk composition caused by upwards reactive flow of buoyant melt through the mush. The evolved melt accumulates around older antecrysts, which may have formed during the earliest sill intrusions and hence long pre-date magma formation. In the schematic shown here, the felsic magma hosts a mixture of old and young antecrysts. The old antecrysts were formed during early sill intrusions; the young antecrysts formed during late sill intrusion at similar depth.
Methods

Model Formulation

To understand processes within crustal mush reservoirs, a quantitative model is required that includes three key features. First, the model must include the addition of hot magma or heat, to initially solid crust, in order to create and grow the reservoir. Second, the model must operate primarily at low melt fraction, consistent with a wealth of evidence that crustal magma reservoirs are normally low melt fraction mushes rather than high melt fraction magma chambers. At low melt fraction, a magma reservoir comprises a mush of crystals forming a solid framework with melt distributed along grain boundaries. At higher melt fraction, the reservoir comprises a slurry of melt containing suspended crystals that can flow via fractures, faults or other pathways to be intruded at shallower depths or erupt at the surface. The latter process is not modelled explicitly in this study.

The intrusion of magma to form sills can occur in numerous tectonic settings, providing both a source of heat and a source of magma that can differentiate to produce evolved melt. Here, we follow earlier numerical approaches and model the repetitive intrusion of sills into the mid-to lower-crust (modelling magma reservoirs at depths over the range 10-30km), consistent with numerous contemporary magma reservoirs imaged in geophysical data, and magma reservoirs interpreted in deep crustal sections. It is assumed that the magma in the sills is delivered from some deeper reservoir in the crust or upper mantle. In most of the example cases shown, the intruding magma is mantle-derived basalt, recognizing that crustal magmatism is largely driven by basalt and consistent with numerous natural examples. However, in a later section we also show results for a case when the intruding sills contain more evolved (intermediate) magma.

Most models of repetitive sill intrusion do not include relative motion of melt and crystals and, therefore, there is no chemical differentiation: the bulk composition of the mush reservoir remains constant. Here, it is assumed that melt within the mush reservoir, produced by cooling and crystallisation of the intruded sills and also heating and melting of the surrounding crust, is present along grain boundaries and forms an interconnected network at low melt fraction. The melt is buoyant because it is less dense than the surrounding crystals, so a pressure gradient is present which causes upwards flow of melt relative to the crystalline matrix. The matrix can deform in response to melt flow. This coupled process of melt migration and matrix deformation is termed compaction. There is abundant evidence that compaction occurs in a wide variety of crustal igneous systems, and our assumptions are consistent with previous models of compaction.

Melt flow along grain boundaries in a mush reservoir allows efficient exchange of heat and mass between melt and solid phases, so that in most of the mush and over most of its lifetime, the phases remain in local thermal and chemical equilibrium. The local bulk composition of the mush therefore changes as the melt migrates upwards and the crystals compact downwards. To capture this, our model includes component transport and chemical reaction. The results shown here demonstrate that reactive flow of melt is a critically important process controlling the storage, accumulation and chemical evolution of magma within the mush reservoir.

Governing equations and method of solution

The governing equations and method of solution are modified from Solano et al. The enthalpy method is used to describe conservation of heat and a binary eutectic phase diagram is used to describe solid and melt compositions assuming local thermodynamic equilibrium.

In common with many previous studies, compaction is modelled using a modified version of the McKenzie formulation, assuming that deformation of the matrix occurs by melt-enhanced diffusion creep. This is reasonable in supra-solidus mush reservoirs deforming at low strain rates (<10^{-15} s^{-1}) and yields a Newtonian rheology for the mush. The matrix shear viscosity is assumed constant, but the matrix bulk viscosity has a power-law relationship with melt fraction. The melt is also...
assumed to have a Newtonian rheology, which is reasonable for crystal-free melts containing a few wt% water.\textsuperscript{57,58}

Surface tension and interphase pressure are neglected. The compaction formulation is currently being extended to include these potentially important effects, but a single, self-consistent model that includes phase change has not yet been presented.\textsuperscript{59-63} Differential stresses imposed by tectonic forces, and magma chamber over-pressuring and loading\textsuperscript{64} are also neglected, recognizing that at least some grain boundary flow is essential to separate melt and crystals in a mush reservoir and buoyancy is always available to drive this. Volatiles are assumed to remain in solution, so are not present as a separate phase. In shallow crustal reservoirs, an exsolved volatile phase likely plays an important role in controlling phase relations and melt flow, and driving magma mobilization.\textsuperscript{65,66}

As outlined in Solano et al.,\textsuperscript{10} the transport of heat, mass and components is modelled in 1-D, using a continuum formulation of the governing conservation equations. Typical sill intrusions and crustal mush reservoirs have high aspect ratio.\textsuperscript{2-5,16,21,38,42-44,67,68} Given this, and the predominately vertical flow of buoyant melt in the mush, a 1-D model is a reasonable starting point to determine the effects of reactive melt flow on magma storage and differentiation. However, a 1-D model does not admit the formation of high porosity, sub-vertical channels caused by reactive infiltration instability.\textsuperscript{54} Numerical modelling in 2-D has suggested that such channels are created during reactive melt flow in the mantle,\textsuperscript{54,69,70} but their formation and significance in crustal mush reservoirs is not yet clear. Future work should investigate whether additional and important controls on flow in crustal magma reservoirs are observed in 2- and 3-D models. Such models are likely to be computationally expensive.

The Boussinesq approximation is applied, so density differences between solid and liquid are neglected except for terms involving gravity.\textsuperscript{10,34,51} Melt fraction and porosity are synonymous in this model. However, in contrast to previous models of crustal magma reservoirs, changes in local bulk composition resulting from melt migration mean that the local melt fraction here cannot be simply related via temperature to the melt fraction in the initial bulk composition (Extended Data Fig. 1c). This is a very important aspect of our model and one that pertains in both simple chemical systems (as employed here) and complex natural systems.

The governing equations can be expressed in dimensionless form as\textsuperscript{10}

\[
\frac{\partial h'}{\partial t'} = \kappa \frac{\partial^2 T'}{\partial z'^2} + \text{Ste} \frac{\partial}{\partial z'}\left((1 - \varphi)w'_s\right) 
\]  
\[
\frac{\partial C}{\partial t'} = -\frac{\partial}{\partial z'}\left((1 - \varphi)w'_s C_s\right) - \frac{\partial}{\partial z'}\left(\varphi w'_m C_m\right) 
\]  
\[
\frac{\partial I}{\partial t'} = -\frac{\partial}{\partial z'}\left((1 - \varphi)w'_s I_s\right) - \frac{\partial}{\partial z'}\left(\varphi w'_m I_m\right) 
\]  
\[
\frac{\partial}{\partial z'}\left(\varphi^\beta \frac{\partial w'_s}{\partial z'}\right) = \frac{\mu' w'_s}{\varphi^\alpha} + (1 - \varphi) \Delta \rho' 
\]  
\[
\varphi w'_m = -(1 - \varphi) w'_s 
\]

where \(h\) is enthalpy per unit mass; \(T\) is temperature; \(t\) is time; \(z\) is the vertical coordinate; \(w\) is velocity; \(\varphi\) is melt fraction; \(C\) is composition, defined using the phase diagram described in the next section; \(I\) is trace element concentration; \(\Delta \rho\) is the density contrast between melt and crystals and \(\mu\) is melt shear viscosity, both discussed in the next section. Subscripts \(s\) and \(m\) denote solid and melt, respectively. Primes denote the dimensionless equivalents of the dimensional variables.

The characteristic time- and length scales used to non-dimensionalize the equations are given by\textsuperscript{10}
\[ \tau = \frac{1}{\Delta \rho_r g} \left( \frac{\mu_r \eta_0}{a^2 b} \right)^{1/2} \]  

(6)

\[ \delta = \left( \frac{\eta_0 a^2 b}{\mu_r} \right)^{1/2} \]  

(7)

where \( \Delta \rho \) is a reference density contrast and \( \mu_r \) a reference melt shear viscosity discussed in the next section, \( g \) is the acceleration due to gravity, and the matrix viscosity is related to the melt fraction by\(^{10,34,50}\)

\[ \frac{4}{3} \eta + \bar{\xi} = \eta_0 \rho^\beta \]  

(8)

where \( \eta \) is the shear viscosity, \( \bar{\xi} \) is the bulk viscosity, \( \eta_0 \) is a reference shear viscosity and \( \beta \) is an adjustable constant. The permeability of the mush \( k_\phi \) is given by\(^{10,34,48,51}\)

\[ k_\phi = a^2 b \rho^\alpha \]  

(9)

where \( a \) is the grain size, and \( b \) and \( \alpha \) are adjustable constants.

Temperature and enthalpy are scaled using\(^{10}\)

\[ T' = \frac{T - T_S}{T_L - T_S} \]  

(10)

\[ h' = \frac{h - h_S}{h_L - h_S} \]  

(11)

where the subscripts \( L \) and \( S \) denote liquidus and solidus respectively. The dimensionless scaling factor \( \kappa \) in equation (1) is given by\(^{10}\)

\[ \kappa = \frac{k_T \tau (T_L - T_S)}{\rho_r \delta^2 \left( c_p (T_L - T_S) + L_f \right)} \]  

(12)

and the Stefan Number by\(^{10}\)

\[ Ste = \frac{L_f}{c_p (T_L - T_S) + L_f} \]  

(13)

where \( k_T \) is the thermal diffusivity, \( c_p \) the sensible heat capacity, \( L_f \) the latent heat of fusion and \( \rho_r \) is a reference density discussed in the next section.

The initial condition is chemically homogenous crust with a constant linear geotherm \( T_{\text{geo}} \) and no melt present. Temperature, melt fraction and velocity are zero at the upper boundary (Earth surface); the lower boundary has constant \( T_{\text{geo}} \) and is set sufficiently deep that melt fraction and velocity remain zero. Equations (1)-(5) were solved numerically using finite difference methods and a code developed by the authors. Equation (1) was approximated using a forward-time-centered-space scheme; equations (2) and (3) using a modified Lax-Wendroff scheme; and equation (4) using a centered scheme. Node spacing and time-steps were chosen based on the results of convergence tests. Solutions reported here used 20-40 nodes per individual sill intrusion with time steps that were always less than the well-known CFL condition.\(^{34,71}\)
The numerical methods and code have been validated extensively against analytical solutions. The energy conservation equation (1) is a special case of the general parabolic diffusion-advection equation, while the mass conservation equations (2) and (3) are special cases of the general hyperbolic flux conservative equation. Analytical solutions are available for simplified forms of these general equations, and the numerical methods were tested against these. An analytical solution is available for a simplified set of the compaction equations and the code was also tested against this.

**Phase behaviour and composition-dependent material properties**

Phase change and compositions are described using a binary eutectic phase diagram that approximates the behaviour of natural systems. Several previous studies of crustal igneous systems have used a similar approach, which is preferable to more complex models involving, for example, the thermodynamic software MELTS for two reasons. First, reactive flow leads to local changes in bulk composition, so the local phase equilibria must be recalculated at each location and time; this is trivial using a simple phase diagram, but computationally intensive (albeit possible) using MELTS. Second, it allows fundamental aspects of compositional evolution to be identified without the additional complexity associated with modelling the phase behaviour of natural systems.

Melt fraction is related to composition through

\[ \phi = \frac{C - C_s}{C_m - C_s} \]  

(14)

where \( C \) is the local bulk composition. Assuming a linear release of enthalpy during melting, enthalpy is related to temperature through

\[ h = c_p T + L_f \phi \]  

(15)

Using equations (14) and (15), and the temperature-dependent liquid and solid compositions determined from the phase diagram, the melt fraction is determined locally.

The binary eutectic phase diagram is described by a quadratic function given by

\[ C_m = \begin{cases} 
-\frac{a_2 - \sqrt{a_2^2 - 4a_1(a_3 - T)}}{2a_1} & C < e \\
-\frac{b_2 + \sqrt{b_2^2 - 4b_1(b_3 - T)}}{2b_1} & C > e 
\end{cases} \]  

(16)

\[ C_s = \begin{cases} 
0 & C < e \\
1 & C > e 
\end{cases} \]  

(17)

Here, only compositions with \( C < e \) were used. Values of the constants \( a_1 - a_3 \) were selected so that the melting relations obtained for starting compositions chosen to represent crust and intruded basalt match typical experimental data for the equilibrium melting/crystallization of metagreywackes and basalt, respectively, over the pressure range 400 – 900MPa (Extended Data Figure 1a; Extended Data Table 1). The match is surprisingly good given the simple phase behaviour adopted.

It is important to recognize that the static melt fraction versus temperature relations shown in Extended Data Figure 1a are specific to the chosen starting bulk compositions. They are not valid if the bulk composition changes in response to reactive melt flow. The phase diagram provides a family of melting curves for all bulk compositions encountered in the reservoir; we show just two in Extended Data Fig. 1a. The effect of reactive melt flow in the reservoir is to decouple melt fraction and temperature (Extended Data Figure 1c). High melt fraction can be found at low temperature where
reactive melt flow has caused the bulk composition of the mush to evolve towards the eutectic and vice-versa. It is often assumed that high melt fraction necessitates high temperature. Reactive melt flow means that this is not the case in crustal mush reservoirs.

We choose to relate composition $C$ to a simple measure of differentiation, the SiO$_2$ content, by

$$S_{\text{SiO}_2} = a_5 + a_6 \tanh (a_7 + a_8 C) \quad (18)$$

Values of the constants $a_5$ - $a_8$ were selected to yield a variation in SiO$_2$ content with temperature that matches melt SiO$_2$ content from the same experimental melting/crystallization data (Extended Data Figure 1b; Extended Data Table 1). Again, the match is surprisingly good given the simple phase behavior adopted.

Rearrangement of equations (14), (16) and (17), followed by substitution into (15), yields a cubic polynomial in melt fraction, dependent on enthalpy $h$ and bulk composition $C$, which can be solved analytically

$$\phi = \frac{h}{L_f} - \frac{c_p}{L_f} \left( a_3 + \frac{C - C_s + C_s \phi}{\phi} + a_2 \right)^2 + a_2 \frac{1}{4a_1} \quad (19)$$

The model includes partitioning of a trace element between crystals and melt. The concentration in the melt is given by

$$I_m = \frac{I}{K + \phi (1-K)} \quad (20)$$

and in the solid by

$$I_s = K I_m \quad (21)$$

In the cases modelled here, the intruding magma and crust have the same initial concentration of an incompatible trace element. This is unlikely in nature, but allows the evolution of trace element concentration in response to reactive melt flow in the mush to be more clearly observed and understood. Trace element concentration does not affect the evolution of temperature or melt fraction, so the other key model results remain unchanged.

The density of the melt and matrix, and the viscosity of the melt, both vary as a function of composition. Solid and melt densities are given by

$$\rho_m = C \rho_{m\text{min}} + (1-C) \rho_{m\text{max}} \quad (22a)$$

$$\rho_s = C \rho_{s\text{min}} + (1-C) \rho_{s\text{max}} \quad (22b)$$

where the subscripts max and min denote, respectively, the most evolved and least evolved (most refractory) compositions in the system. The average density of the crystals+melt mixture (mush or magma) is given by

$$\rho = \phi \rho_m + (1-\phi) \rho_s \quad (23)$$

The dimensionless density is obtained by dividing by a reference density $\rho_0$ chosen as the initial density of the crust, and the dimensionless density contrast is obtained by dividing by a reference density
contrast \( \Delta \rho \) chosen to be the difference in density between the most refractory crystals \( \rho_{\text{max}} \) and most evolved melt \( \rho_{\text{min}} \).

The logarithm of melt shear viscosity \( \mu \) is linearly related to the dimensionless silica content of the melt \( s_{\text{SiO}_2} \):

\[
\mu = 10^\left( \frac{\mu_{\text{max}} - \mu_{\text{min}}}{S_{\text{SiO}_2} - s_{\text{SiO}_2}} \right)
\]

(24)

with

\[
s_{\text{SiO}_2} = \frac{S_{\text{SiO}_2} - s_{\text{SiO}_2}^{\text{min}}}{S_{\text{SiO}_2} - s_{\text{SiO}_2}^{\text{max}}}
\]

(25)

where \( S_{\text{SiO}_2} \) is the silica content of the melt (wt\%). The dimensionless melt shear viscosity is then obtained by dividing by a reference viscosity \( \mu_r \) chosen to be the maximum melt viscosity in the system (corresponding to the most evolved composition), to yield

\[
\mu' = 10^\left( \log(\mu_{\text{max}}/\mu_r) \left(1 - s_{\text{SiO}_2} \right) \right)
\]

(26)

In the illustrative models shown here, melt viscosity varies from a minimum of 1 Pa·s to a maximum of \( 10^5 \) Pa·s (Extended Data Table 1) for the most mafic and felsic compositions respectively, which is reasonable for melt containing a few wt\% water. A range of maximum melt viscosities is investigated in the sensitivity analysis described below.

**Modelling of sill intrusion**

The governing equations do not include terms representing addition of heat and mass in response to repetitive sill intrusion. Each sill intrusion is modelled numerically, using a simple approach in which new nodes, populated with the properties (enthalpy, melt fraction, major element composition and trace element concentration) of the magma in the sill, are added into the model at the target intrusion depth. \(^{22,32,34}\) The number of new nodes is chosen to yield the desired sill thickness. Pre-existing nodes below the location of sill intrusion are shifted downwards to accommodate the new nodes representing the sill; this approach represents, numerically, the case that intrusion of each new sill causes downwards displacement of deeper crust and approximates isostatic equilibrium. Intrusion of each sill is assumed to occur over a timescale that is small compared to the thermal and chemical evolution of the magma reservoir and within a single time-step in the model. We note that injection of magma may generate local over-pressure, fracturing and, during the growing and active phases of the magma reservoir, locally disrupt the mush. Future refinements will focus on methods to better couple thermal and mechanical models.

**Sill intrusion depth**

Previous numerical studies have modelled repetitive intrusion by over-accretion, in which each new sill is intruded immediately above the previous sill; under-accretion, in which each new sill is intruded immediately below the previous sill; and random intrusion of sills and dykes around a fixed depth. \(^{21,23,32,34}\) The approach used here to link sill intrusion depth to the state of the mush reservoir at the time of intrusion yields variations in intrusion depth that are not captured by these previous models.

Controls on the depth of sill intrusions include rigidity contrasts and rheology anisotropy, resulting from variations in lithology and (if present) melt fraction; rotation of deviatoric stress such that the minimum deviatoric stress becomes vertical; and density contrasts between the surrounding country rock and intruding magma. \(^{67,68}\) The initial intrusion depth is chosen here to match the depth of an observed magma reservoir. Understanding why a sill should be initially emplaced at a given depth is beyond the scope of the paper. Once the first sill is emplaced, the depth of subsequent intrusions is
controlled by the density contrast between the intruding magma and the surrounding reservoir. The next sill intrusion occurs at the deepest level of the mush that has a lower bulk density (crystals + melt) than the intruding magma. The top of the resulting reservoir tends to be close to the initial intrusion depth.

Density contrasts are controlled by the local composition and/or melt fraction of the mush reservoir. We use density contrasts here as a proxy for rigidity contrasts resulting from changes in rock composition or mush melt fraction. Density is calculated using equations (22) and (23); the chosen values of density for refractory crystals \( \rho_{\text{max}} \) and most evolved melt \( \rho_{\text{min}} \) (Extended Data Table 1) yield densities of c.3000 kg·m\(^{-3}\) and c.2600 kg·m\(^{-3}\) for solid basalt and evolved (felsic) rock compositions respectively, and densities of c.2800 kg·m\(^{-3}\) and c.2350 kg·m\(^{-3}\) for their corresponding molten counterparts. These values are consistent with measured data. The initial (reference) density of the solid crust is c.2850 kg·m\(^{-3}\), consistent with data for intermediate rocks.

During the incubation phase, melt fraction falls to zero between successive sill intrusions (Extended Data Figure 2), but variations in density arise in response to differentiation within each intruded sill as it cools. Differentiation yields a lower density, evolved top and a higher density, more refractory base (Extended Data Figure 3a and Supplementary Video 1). Similar compositional trends are observed in sills now exposed at the surface. The density-controlled intrusion depth of each new sill is, therefore, located below the deepest evolved top of a previous, now solidified, sill intrusion.

During the growing and active phases of the reservoir (Extended Data Figure 2b), melt is persistently present and the compositional and density variations formed during the incubation phase are reduced by reactive melt flow (Figure 1 and Supplementary Video 1). Variations in density are then primarily controlled by melt fraction, so the density-controlled intrusion depth of each new sill is located below the deepest high melt fraction layer.

Field observations from deep crustal sections suggest that intrusions progressively accumulate to form a mush zone. At early times, when the heat content of the reservoir is still low, intrusions cool without causing significant melting of the surrounding crust, leaving septa of crust interleaved with the intruded sills. We model this by intruding sills at random over a range of 300m above and below the intrusion depth determined by density contrast.

Random intrusion preserves septa of crustal rock between sill intrusions, whereas strictly density-controlled intrusion does not (see also Solano et al.). Varying the depth range of random intrusion affects the frequency and volume of preserved septa, but does not otherwise affect significantly the results obtained. Although septa between early intrusions are preserved, septa between later intrusions, when the heat content of the reservoir is higher, are partially assimilated into the melt phase, causing crustal contamination of the melt.

Validity of the model at high melt fraction
The reactive flow and compaction formulation is applied in the model regardless of local melt fraction. However, it is strictly valid only when the crystals form a solid framework that will expel melt if it undergoes mechanical disruption or viscous deformation. Estimates of the melt fraction at which this framework forms vary widely (over the range c. 0.4 - 0.7) and likely depend on local shear stresses and strain rates, and the crystal morphology and size distribution. Melt fractions higher than this are present in each sill immediately after intrusion and in the melt layers that form in response to reactive flow. However, we argue below that the formulation captures enough of the physics to yield informative results.

High melt fractions are present in the intruding sills over very short timescales (of order 100’s years) because the sills cool very rapidly, losing heat to the surrounding reservoir and/or crust (e.g. Extended Data Figure 2a). Over these short timescales following each intrusion, crystal-melt separation is assumed in the model to occur only by reactive flow and compaction, omitting other mechanisms of crystal-melt separation; moreover, it is assumed that there is no bulk flow of melt-crystals driven by convection. However, the modelled cooling timescale is correct, because the rate of heat loss from each sill is dominated by conduction and this is described by equation (1). Furthermore, in
each sill, the model captures enough crystal/melt separation to yield a more evolved top, relatively
enriched in incompatible trace elements, and a more refractory base, relatively depleted in
incompatible trace elements, consistent with observations (e.g. Figure 3). High melt fractions are also present in the layers that form in response to reactive melt flow (e.g. Figure 1). These layers are persistently present once formed and the model again assumes crystal-melt separation in each layer occurs only by reactive flow and compaction and that there is no bulk flow of melt+crystals driven by convection. However, the rate of delivery of new melt into the layer is controlled by reactive flow and compaction of the underlying mush where the formulation is valid. Moreover, the rate of upwards movement of the layer, which affects cold storage, is controlled by the rate of upwards movement of the solidus isotherm; this depends on conductive heat transfer in the overlying mush and solid rock, and is captured by the formulation. Thus we argue that the model captures the overall growth and upwards migration of the layers.

Within each high melt fraction layer, the formulation likely does not correctly capture the variation in melt fraction. However, the modelled temperature in each layer is constant at the solidus; melt fraction is also high and approximately constant, controlled primarily by the local bulk composition (e.g. Extended Data Video 1; Figure 1). Thus, the modelled temperature and melt fraction assuming reactive flow with no bulk flow of melt+crystals are similar to what would be observed for the opposite end-member model of vigorous convection in which crystals are suspended and mixed in the magma. We argue that vigorous convection may be more likely given the results of earlier studies of single sill intrusions.

**Magma mobilisation**

Accumulation of melt creates a high melt fraction layer which, as it migrates upwards, can remobilize old mush by causing a rapid increase in melt fraction. The short timescale of this process may not allow for local chemical equilibrium to be maintained, so older crystals can be preserved in the younger magma. Disequilibrium between melt and crystals may also give rise to resorption and zonation of crystals which is not described here.

The model does not attempt to capture migration out of the reservoir of the high melt fraction (low crystallinity) magmas in the layer. Felsic magma that accumulates at the top of the reservoir is buoyant relative to the surrounding mush reservoir, so there is a pressure gradient to drive ascent to higher crustal levels or eruption at the surface. The magma in each sill also evolves during cooling to become more buoyant relative to the more refractory mush, which may drive ascent of less evolved magmas. Preliminary work, not reported here, suggests that removal of felsic magma accumulating in a high melt fraction layer at the top of the reservoir does not affect the formation of subsequent layers, so long as ongoing sill intrusions continue to supply new magma to the reservoir. This preliminary work is not reported because the model does not yet include clearly defined criteria for magma removal and ascent. Moreover, we note that the presence of volatile species, such as H$_2$O, whose solubility is pressure-dependent, complicates phase relations and physical properties during magma ascent, and consequently is not considered here. Further work should determine the controls on mobilization and eruption of the low crystallinity magmas present in crustal mush reservoirs. What is clear from the results obtained here is that the compositions of low crystallinity magmas that can leave the reservoir, regardless of how or why that happens, are bimodal. In our model, the melt composition evolves to the eutectic; in more chemically complex systems, melt composition will evolve to other low-variance states, such as cotectics or peritectics (reaction boundaries). In all cases, the effect is to buffer chemically the composition of accumulated melts, as recently suggested on the basis of phase equilibrium experiments.

**Magmatic systems at shallower depth**

The results shown in Figure 1 (and also Supplementary Video 1 and Extended Data Figure 3) illustrate the key processes occurring within a crustal mush reservoir and were obtained using values
of the model parameters that are typical of crustal systems (Extended Data Table 1 and associated
references). The initial intrusion depth was chosen to allow model results to be compared against a
deep crustal section now exposed at the surface: the Upper Mafic Complex of the Ivrea-Verbano
zone, Italy.16,21,76 The complex is interpreted to represent c.8km of basalt intruded into the crust
over a few Ma (i.e. at intrusion rates of order a few mm·a⁻¹). The top of the complex is interpreted
to have been located at a depth of c.18 km at the time of formation.

The model results can explain a wide range of magmatic phenomena. However, we recognize that
many of the magmatic systems that provide compelling evidence for these phenomena cannot be
approximated by a model tuned specifically to match data from the Upper Mafic Complex. In
particular, systems providing evidence for cold storage and/or compositional bimodality are often
located at shallower levels in the crust.6-9 Moreover, major and trace element and isotopic data for
these systems suggest they may be supplied by magmas of more evolved composition than basalt.6-
9,88 In transcrustal magmatic systems¹ there are likely multiple zones of intrusion: primitive basalt
magmas may form intrusions deep in the crust that generate more evolved magmas; these magmas
ascend through the crust to form intrusion zones at shallower depths.

We test here whether similar results are obtained if the first sill is intruded at a depth of 10km,
rather than 18km. Numerous magmatic systems are observed in geophysical data at similar
depth.2,4,5,38 All model parameters are the same as used previously (Extended Data Table 1), except
that we assume the initial geotherm is appropriate for thermally mature crust where, for example, a
deeper magmatic zone has thermally primed the upper crust prior to the onset of shallower
magmatism. Previous studies have shown that this is necessary to allow upper crustal magmatic
systems to form without a prohibitively long incubation period or unreasonably high rate of magma
intrusion.23

The results obtained are qualitatively similar to those observed at 18km depth. There is an
incubation period, during which the melt fraction rapidly falls to zero, with compositional contrasts
formed by chemical differentiation within each sill intrusion prior to solidification causing the intrusion
depth to increase progressively (Supplementary Video 2; Extended Data Figure 4a). During the
growing phase, buoyant melt again migrates upwards through the mush and reactive melt flow
reduces, or removes, early formed compositional contrasts, so that the intrusion depth becomes
controlled by the locally varying melt fraction (Supplementary Video 2; Extended Data Figure 5a).

During the active phase, the reservoir can again produce evolved, low crystallinity magmas from
the high melt fraction layer that forms beneath the solidus isotherm, close to the top of the reservoir
(Supplementary Video 2; Extended Data Figure 5b). When intrusion of new sills ends, the reservoir
enters the waning phase (Supplementary Video 2; Extended Data Figure 4b) until the mush has
completely solidified.

Cold storage is again observed where upwards migrating, evolved melt rapidly accumulates around
older antecrysts derived from crystallisation of early sills (Extended Data Figure 6). In this shallower
example, melt accumulation forms a low crystallinity magma a few 100's years after the local
temperature exceeds the solidus, but the magma contains antecrysts formed c. 1.3Ma earlier
(Extended Data Figure 6). Compositional bimodality is again observed, as magmas in the high melt
fraction layers have evolved composition, but magmas in the sills shortly after intrusion have
compositions close to that of the intruded basalt (Extended Data Figure 7a). Thus, the key results are
consistently observed in models of shallower magmatic systems created and sustained by basaltic
magmatism.

Intrusion of more evolved magma

We now test whether similar results are obtained at 10km if the intruding sills contain magma of
intermediate (andesitic) rather than basaltic composition. All other model parameters are the same
as used in the previous 10km model (Extended Data Table 1). We do not model intrusion of rhyolite
magma because our density controlled intrusion depth model does not apply for rhyolite magma:
density controlled intrusion alone would suggest that rhyolite should mostly erupt. That evolved, low density magmas often intrude rather than erupt has been a challenge to density driven models of magma ascent and intrusion for many years.\textsuperscript{67,68}

Intrusion of intermediate composition (c. 61\% SiO\textsubscript{2}) magma yields qualitatively similar behavior to that observed in response to intrusion of basaltic magma. The incubation, growing, active and waning phases of reservoir life are all observed and, during the active phase, a high melt fraction layer containing evolved (felsic) magma overlies a thicker, low melt fraction mush (e.g. Extended Data Figure 8). Older antecrysts are again rapidly remobilized by the arriving melt layer although, in this case, storage is ‘cool’ rather than ‘cold’: the temperature remains above the solidus, but the melt fraction remains low until the melt layer arrives. Whether crystals are kept in cold (sub-solidus) or cool (supra-solidus) conditions may be difficult to determine from crystal chemistry data, requiring accurate estimates of reservoir and solidus temperatures;\textsuperscript{6-9} the key point is that the crystals are stored at low (non-eruptible) melt fraction, as opposed to ‘warm storage’ where the magma remains eruptible.\textsuperscript{18}

Compositional bimodality is again observed, but here the magma compositions are either evolved (felsic), reflecting melt accumulation in the upwards migrating layer, or intermediate, reflecting the composition of the intruding magma (Extended Data Figure 7b). In general, we suggest that crustal mush reservoirs deliver magmas with compositions that reflect either (i) low-variance states, such as eutectics, cotectics or peritectics (reaction boundaries)\textsuperscript{87} or (ii) the intruding magma that creates the reservoir.

**Intrusion depth model**

Numerical tests show that compositionally bimodal, low crystallinity magmas are obtained regardless of whether the intrusion depth is modelled using our sill intrusion depth model or simple under- or over-accretion. ‘Cold’ (or at least ‘cool’) storage of crystals, in a non-eruptible state, is also observed (e.g. Extended Data Figure 9a,b), except when intrusion depth is modelled using simple over-accretion. Over-accretion cannot yield cold or cool storage of antecrysts formed as part of the same magmatic event, as persistent sill intrusion at the top of the magma reservoir causes the melt layer to migrate upwards and form in the overlying crust (e.g. Extended Data Figure 9c,d). The crystals here are rapidly mobilized by the arrival of the melt layer, but the history of the crystals and their genetic relationship with the magmatic event may be much more complex. However, simple over-accretion requires the magma supplying each sill to pass through the mush reservoir regardless of local melt fraction, rheology or density, which is inconsistent with available evidence and models.\textsuperscript{67,68} We argue that our sill intrusion model better captures the effect of the local mush state on intrusion depth.

**Sensitivity analysis**

Extended Data Table 1 shows that crustal magma reservoirs are described by a broad range of material properties. Values of many of these are poorly constrained. A simple sensitivity analysis was used to confirm that the results obtained are typical.

Previous work has shown that solutions to equations (1) – (5) are largely dictated by the value of the dimensionless scaling factor $\kappa$.\textsuperscript{51,71} The effect of varying the other dimensionless parameter $\text{Ste}$ is much smaller. Other studies, confirmed by additional numerical experiments conducted here, have shown that, for a given depth of intrusion and initial geothermal gradient, the thermal impact of intruding sills is controlled by the intrusion rate, irrespective of the model used to choose the sill intrusion depth.\textsuperscript{22,23,32,33} The chosen intrusion rate of 5mm·yr\textsuperscript{-1} for the example results shown here corresponds to the time-averaged magma productivity in arc settings simplified to a 1D geometry.\textsuperscript{24} We now explore a range of intrusion rates around this value, consistent with estimates for different crustal magmatic systems and previous studies.\textsuperscript{21-24,32-34}

A simple Monte-Carlo analysis\textsuperscript{89} shows that 90\% of the calculated values of $\kappa$ for typical crustal parameters lie within the range 0.028 < $\kappa$ < 2160 (-1.55 < log $\kappa$ < 3.335; see Extended Data Figure 10a). Numerical solutions were obtained for ten values of log $\kappa$ sampled evenly over this range in log space,
for a range of values of the sill intrusion rate, three different intrusion depths and basalt that is
intruded to a maximum thickness of 20km (Extended Data Table 1). The results are summarized in
Extended Data Fig. 10b,c by plotting the incubation time (the time required to reach the end of the
incubation phase and produce a persistent mush reservoir; see Extended Data Figure 2b), the
activation time (the time required to produce an active reservoir with a low crystallinity felsic magma
layer; see Extended Data Figure 2b), the bulk composition of the mobile magmas (i.e. magmas with
melt fraction >0.7), and the ‘cold storage time’ of antecrysts at the top of the reservoir, as a function
of sill intrusion rate for the different intrusion depths. The ‘cold storage time’ is the time elapsed
between the last intrusion and the local melt fraction exceeding 0.7 at locations close to the top of
the reservoir (see Fig. 2 and Extended Data Figures 6, 8). The cold storage time reflects the likely range
of crystal ages in magmas that have achieved melt fractions exceeding 0.7.

The incubation time scales with the reciprocal of the intrusion rate squared $q^{-2}$ (Extended Data Fig.
10b). The same scaling has been obtained in previous, purely thermal, models of repetitive sill
intrusion using a variety of intrusion depth schemes, showing that the incubation time is relatively
insensitive to the details of sill intrusion. Varying the value of $\kappa$ over the range specified has a
negligible impact on the incubation time, regardless of intrusion rate or depth, reflecting the relatively
small range of uncertainty in thermal parameters such as thermal conductivity, specific heat capacity
and latent heat (Extended Data Table 1).

The impact of varying $\kappa$ on the accumulation time is more significant, especially at lower intrusion
rates when the accumulation time may be several million years longer than the incubation time
(Extended Data Fig. 10b). Longer incubation times are observed for large values of $\kappa$ that correspond
to larger values of the melt shear viscosity and smaller values of matrix grain size, and for small values
of $\kappa$ that correspond to large values of the matrix bulk viscosity (Extended Data Table 1). Nevertheless,
the accumulation time is finite so long as the incubation time is reached within the maximum intruded
thickness of basalt; in other words, the formation of a high melt fraction layer is inevitable, so long as
a persistent mush reservoir is present.

The composition of the high melt fraction (eruptible) magma in the reservoir is always bimodal,
irrespective of the value of $\kappa$, the intrusion rate or intrusion depth (Extended Data Fig. 10c). The
magma in the intruded sills has a composition close to that of the intruding basalt, while the magma
in the layer that accumulates at the top of the reservoir has an evolved (approximately eutectic)
composition, consistent with the results shown earlier for specific cases (Figure 3; Extended Data
Figure 7a).

The impact of varying $\kappa$ on the cold storage time is more significant, as is the effect of intrusion
rate (Extended Data Fig. 10c). Smaller cold storage times are observed for larger values of $\kappa$ that
correspond to larger values of the melt shear viscosity and smaller values of matrix grain size
(Extended Data Table 1). Smaller cold storage times are also observed for higher intrusion rates,
because evolution of the system as a whole occurs more rapidly. The cold storage time reflects the
relative timing of sill intrusion relative to remobilization. Nevertheless, the cold storage time is always
non-zero; in other words, some antecrysts are stored in a cold (or cool), non-eruptible state, prior to
remobilization by reactive flow.

Code availability.
The code (MUSHREACT) used to solve equations (1)-(5) and produce the results reported here is
available from the corresponding author on request. The code is platform dependent and is not
optimized or tested for broad distribution, but the methodology is described within the article and
preceding studies.10,34

Data Availability Statement
No original data are reported that were not created using the software code (MUSHREACT). Data
can be recreated using the code.


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Extended Data Figure and Table Captions

Extended Data Figure 1 | Phase behaviour and compositions of the modelled system. a, Static melt fraction versus temperature for the modelled basalt and crust, extracted from the binary phase diagram for the chosen initial bulk compositions. Also shown are experimental equilibrium melting/crystallization data for metagreywackes and basalt over the pressure range 400-900MPa.12,73,74 Triangles denote data from ref. 73; circles data from ref. 74; squares data from ref. 12. Static melt fraction denotes the melt fraction obtained if there is no relative motion of melt and crystals, so the bulk composition remains constant. b, SiO2 content versus temperature modelled
here. Also shown are experimental data corresponding to those shown in (a). c, Melt fraction versus
temperature obtained from the numerical model (data extracted from Supplementary Video 1 at
three snapshots in time (0.97Ma, 1.39Ma and 1.66Ma after the onset of sill intrusions) corresponding
to Figure 1 and Extended Data Figure 3b. Reactive flow in the mush decouples temperature and melt
fraction: high melt fraction can be found at low temperature where reactive melt flow has caused the
bulk composition of the mush to evolve and vice-versa.

Extended Data Figure 2 | Maximum melt fraction as a function of time. a, following a single sill
intrusion during the incubation period, and b, over the life of the reservoir. In a, the sill cools rapidly,
with the melt fraction falling below 0.7 (i.e. the crystallinity exceeding 30%) within 63a after intrusion,
and the sill solidifying within 225a. The sharp decrease in melt fraction prior to full solidification is
physical and represents the arrival of the solidification front during crystallisation at the eutectic. In
b, during the incubation phase, maximum melt fraction spikes after each sill intrusion, but decreases
rapidly and falls to zero between sill intrusions. The incubation phase ends when the melt fraction
remains greater than zero between sill intrusions. During the growing phase, the maximum melt
fraction at the top of the mush reservoir increases in response to reactive flow of buoyant melt. Spikes
in melt fraction correspond to ongoing sill intrusions deeper in the reservoir. Melt fraction at the top
of the mush increases until, during the active phase, evolved, low crystallinity (<30%) magma is
present which is likely to rapidly leave and ascend to shallower crustal levels. New sill intrusions cease
and, sometime later, the melt fraction at the top of the mush also starts to decrease. Overall, the
reservoir is cooling. This is the waning phase, at the end of which the reservoir has completely
solidified. Data in both plots extracted from Supplementary Video 1.

Extended Data Figure 3 | Snapshots showing temperature, melt fraction, bulk composition and
incompatible trace element concentration as a function of depth through a crustal section at 18km
during the incubation and waning phases of the reservoir after a, 0.82Ma following the onset of sill
intrusions and b, 1.66Ma. Snapshots are taken from Supplementary Video 1. At early times a, during
the incubation phase, individual sills cool rapidly. During the growing phase (not shown here; see
Figure 1a), a persistent magma reservoir forms but the melt fraction is low and relatively uniform.
However, buoyant melt migrates upwards and begins to accumulate at the top of the reservoir. During
the active phase (not shown here; see Figure 1b), a high melt fraction layer forms. At late times b,
during the waning phase, sill intrusions cease and the mush cools and solidifies. Shaded area in all
plots denotes the vertical extent of basalt intrusion at that time. Equivalent results for intrusion at
10km depth are shown in Extended Data Fig. 4.

Extended Data Figure 4 | Snapshots showing temperature, melt fraction, bulk composition and
incompatible trace element concentration as a function of depth through a crustal section at 10km
depth during the incubation and waning phases after a, 0.82Ma following the onset of sill intrusions
and b, 1.66Ma. Snapshots are taken from Supplementary Video 2. The results are qualitatively very
similar to those obtained at 18km depth (Extended Data Figure 3). During the incubation phase a,
individual sills cool rapidly. During the waning phase b, sill intrusions cease and the mush cools and
solidifies. Shaded area in all plots denotes the vertical extent of basalt intrusion at that time.

Extended Data Figure 5 | Snapshots showing temperature, melt fraction, bulk composition and
incompatible trace element concentration as a function of depth through a crustal section at 10km
depth during the growing and active phases after a, 0.99Ma following the onset of sill intrusions and
b, 1.39Ma. Snapshots are taken from Supplementary Video 2. The results are qualitatively very similar
to those obtained at 18km depth (Figure 1). During the growing phase a, a persistent mush reservoir
forms but the melt fraction is low. Buoyant melt migrates upwards and begins to accumulate at the
top of the reservoir. During the active phase b, the accumulating melt forms a high melt fraction layer
containing mobile magma. The composition of the melt in the layer is evolved and enriched in incompatible trace elements. Elsewhere in the mush, the melt fraction remains low. Shaded area in all plots denotes the vertical extent of basalt intrusions at that time.

Extended Data Figure 6 | Cold storage and rapid remobilization of magma in a reservoir at 10km depth. Results are qualitatively very similar to those obtained at 18km depth (Figure 2). Plot a shows melt fraction as a function of depth at the first snapshot after remobilization at 10km (1.441Ma). Shaded area denotes intruded basalt. Reactive flow of buoyant melt produces a high melt fraction layer that migrates upwards. Plot b shows temperature and melt fraction as a function of time at a depth of 10km. Similar results are obtained over the depth range 10-10.5km. Early sill intrusions rapidly cool and crystallize. The crystals are kept in ‘cold storage’ at sub-solidus temperature, but the temperature gradually increases in response to sill intrusions deeper in the reservoir. Soon (<0.3ka) after the temperature exceeds the solidus, the high melt fraction layer arrives at this depth and the reservoir is remobilized: the melt fraction increases rapidly to form a low crystallinity magma. The melt fraction increases much more rapidly and to a higher value than would be possible by melting alone. Plot c shows temperature and melt fraction as a function of time at a depth of 12km. Similar results are obtained over the depth range 10.5-15km. Melt fraction remains low because reactive flow has left a refractory residue at this depth. There is no remobilization, despite the increase in temperature. Data extracted from Supplementary Video 2.

Extended Data Figure 7 | Geochemical consequences of reactive melt flow in crustal magma reservoirs at 10km depth created by intrusion of (a) mafic sills and (b) intermediate sills. Both plots show SiO$_2$ content of low crystallinity (crystal fraction <30%) magmas. Solid curves show bulk magma composition (melt plus crystals); dashed curves show melt composition alone. The peak at low SiO$_2$ corresponds to magma within the intruding sills; the peak at high SiO$_2$ corresponds to magma within high melt fraction layers near the top of the reservoir. In plot (a), measured data from the Snake River Plain are shown for comparison; the bimodality is clear although the basalt has a lower SiO$_2$ content than modelled here. Bimodal compositions correspond to (1) the magma intruded into the reservoir, and (2) the most evolved composition obtained by differentiation.

Extended Data Figure 8 | Cool storage and rapid remobilization of magma in a reservoir created by intrusion of intermediate magma at 10km depth. Results are qualitatively similar to those obtained by intruding basalt magma. Plot a shows melt fraction as a function of depth at the first snapshot after remobilization at a depth of 11.4km (1.28Ma). Reactive flow of evolved, buoyant melt produces a high melt fraction layer that migrates upwards. Plot b shows temperature and melt fraction as a function of time at a depth of 11.4km. Early sill intrusions rapidly cool and crystallize. The crystals are kept in ‘cool storage’ at near-solidus temperature. At 1.28Ma, the high melt fraction layer arrives at this depth and the reservoir is remobilized: the melt fraction increases rapidly to form a low crystallinity magma. The melt fraction increases much more rapidly and to a higher value than would be possible by melting alone. Melt fraction deeper in the reservoir remains low because reactive flow has left a refractory residue at this depth.

Extended Data Figure 9 | Consequences of emplacement during (a, b) under-accretion and (c, d) over-accretion. During under-accretion, plot a shows melt fraction as a function of depth at the first snapshot after remobilization at a depth of 22km (1.02Ma). Reactive flow of evolved, buoyant melt produces a high melt fraction layer that migrates upwards. Plot b shows temperature and melt fraction as a function of time at a depth of 22km. Similar results are obtained over the depth range 22-22.5km. Under-accretion causes the sill intrusion depth to progressively increase from 18km; in this case, an intrusion at 22km occurs at 0.75Ma that rapidly cools and crystallises. The crystals are kept in ‘cool storage’ at close-to-solidus temperature. At 1.02Ma the high melt fraction layer arrives
at this depth and the reservoir is remobilized. During over-accretion, plot c shows melt fraction as a function of depth at a snapshot in time (1.53Ma). In this case, the high melt fraction layer has migrated into the overlying country rock. Plot d shows temperature and melt fraction as a function of time at a depth of 17.5km, close to the top of the active magma reservoir. Similar results are obtained over the depth range 17.5-18km. Crystals in the magma are sourced from the country rock and may be genetically unrelated to the melt. There is no cold storage of crystals brought into the reservoir by basaltic sill intrusions, as intrusion occurs deeper in the reservoir. In plots a and c, the shaded area denotes intruded basalt.

Extended Data Figure 10 | Sensitivity analysis. Plot (a) is a frequency plot showing values of the dimensionless scaling factor $\kappa$ calculated using equation (12). Values of the input values were varied uniformly over the range given in Extended Data Table 1 in a simple Monte-Carlo analysis. Plot (b) shows incubation and activation time; plot (c) shows cold storage time and eruptible magma composition. Error bars and shaded regions in (b) and (c) denote the effect of varying the dimensionless scaling factor $\kappa$ over the range $0.028 < \kappa < 2160$. Error bars on the incubation time are within the symbol size. Dashed lines denote fit to the incubation time of the form $q^{-2}$ where $q$ is the intrusion rate. Colours in (b) and (c) denote different initial emplacement depths of 10km, 18km and 30km. Models were run for a maximum 20km of intruded basalt.

Extended Data Table 1 | Parameters used in the numerical experiments. Values used to produce the results shown in all figures except Extended Data Figure 10. A steeper geotherm suitable for thermally mature crust was assumed for the results shown in Extended Data Figures 4-8 which have intrusion at 10km depth. The range of values for the sensitivity analysis was used to calculate the range of values of the dimensionless scaling factor $\kappa$ shown in Extended Data Figure 10a and produce the associated numerical modelling results shown in Extended Data Figure 10b,c. Data sources are indicated.
Spikes in melt fraction correspond to sill intrusions.

Persistent high melt fractions between sill intrusions correspond to the high melt fraction layer at top of mush reservoir.

Crystallinity of felsic magma during active phase is c. 10%.

Arrival of solidification front at eutectic composition.

Persistent high melt fractions between sill intrusions correspond to the high melt fraction layer at top of mush reservoir.

Crystallinity of felsic magma during active phase is c. 10%.
a

Location of most recent sill intrusion

No melt present except for a few ka after each sill intrusion

Spiky trace element signature reflecting segregation in each sill intrusion

Enrichment

Depletion

b

Temperature buffered at the solidus

Low and approximately uniform melt fraction

Spiky trace element signature preserved in deeper reservoir

Septa of preserved crust

Initial trace element concentration

Incompatible trace-element concentration (p.p.m.)
a

Location of most recent sill intrusion

No melt present except for a few ka after each sill intrusion

Spiky trace element signature reflecting segregation in each sill intrusion

Depletion

Spiky trace element signature preserved in deeper reservoir

Septa of preserved crust

b

Temperature buffered at the solidus

Low and approximately uniform melt fraction

Enrichment

Depletion

Spiky trace element signature reflecting segregation in each sill intrusion

Septa of preserved crust
Low melt fraction 'mush' Buoyant melt migrates upwards and reacts with compacting crystals

Solidus

Buoyant melt migrates upwards and reacts with compacting crystals

550 750 950 1150

Temperature (°C)

Melt fraction

SiO$_2$ (%)

350 550 750 950 1150

Temperature (°C)

Melt fraction

SiO$_2$ (%)

-18 -16 -14 -12 -10

Depth (km)

Incompatible trace-element concentration (p.p.m.)

Maximum temperature

High melt fraction layers of evolved magma

Low melt fraction 'mush'

Evolved bulk composition in response to upwards reactive melt flow

Spiky major/trace element signature in deeper reservoir

350 550 750 950 1150

Temperature (°C)

Melt fraction

SiO$_2$ (%)

Incompatible trace-element concentration (p.p.m.)
Buoyant melt migrates upwards

Remobilization by reactive melt flow from deeper reservoir

- Sill intrusion at this depth
- Temperature and melt fraction rapidly decrease after intrusion
- Cold (sub-solidus) crystal storage
- Temperature (oscillations show thermal response to sill intrusions deeper in reservoir)
- Melt fraction
- Solidus

Melt fraction

Temperature (°C)

Sill intrusion at this depth

Temperature (oscillations show thermal response to sill intrusions shallower in reservoir)

Melt fraction

Temperature (°C)
Figure a: Mafic sills and Felsic high melt fraction layer.

Figure b: Intermediate sills and Felsic high melt fraction layer.
Buoyant melt migrates upwards.

Cool (near-solidus) crystal storage.

Remobilization by reactive melt flow from deeper reservoir.

Sill intrusion at this depth.

Temperature (oscillations show thermal response to sill intrusions elsewhere in reservoir).

Remobilization by reactive melt flow from deeper reservoir.

Buoyant melt migrates upwards.
Solidus
Temperature
Cool crystal storage
Sill intrusion at this depth
Melt fraction

Temperature (°C)
Time (Myr)
0 0.5 1 1.5 2
0 0.2 0.4 0.6 0.8 1
Buoyant melt migrates upwards

Buoyant melt migrates upwards
Melt layer created by reactive melt flow from deeper reservoir
Remobilization by reactive melt flow from deeper reservoir

Melt fraction
Depth (km)
-22
-23
-24
0 0.2 0.4 0.6 0.8 1
Melt fraction
Temperature
0 0.2 0.4 0.6 0.8 1
0 0.2 0.4 0.6 0.8 1
0 0.2 0.4 0.6 0.8 1
0 0.2 0.4 0.6 0.8 1

Temperature (°C)
Melt fraction
Depth (km)
Melt fraction
Time (Myr)
0 0.5 1 1.5 2
0 0.2 0.4 0.6 0.8 1
0 0.2 0.4 0.6 0.8 1
0 0.2 0.4 0.6 0.8 1

Remobilization by reactive melt flow from deeper reservoir
Buoyant melt migrates upwards
Melt layer created by reactive melt flow from deeper reservoir
Intrusion rate (mm·yr⁻¹)

Time (Myr)

0 5 10 15 20

10km

18km

30km

SiO₂ content

Time (Myr)

0 5 10 15 20

10km

30km

18km

Melt layer

Basalt sills

Normalized frequency

Scaling factor κ (dimensionless)

0 0.01 0.1 1 10 100 1000 10000

0.01 0.02 0.03 0.04
Intrusion rate (mm·yr⁻¹)

Time (Myr)

10km

18km

30km

SiO₂ content

Time (Myr)

Scaling factor κ (dimensionless)

Normalized frequency

κ

0.01

0.02

0.03

0.04

0.05

0.1

1

10

100

1000

10000

a

b

c

Melt layer

Basalt sills
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<th>Symbol</th>
<th>Description and sources</th>
<th>Example case</th>
<th>Sensitivity analysis</th>
<th>Units</th>
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