

## Chiral excitations of open-beauty systems

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We study the scattering of open-beauty mesons and Goldstone bosons as predicted by the chiral SU(3) Lagrangian. The impact of subleading-order chiral interactions to systems with  $J^P = 0^+$  and  $J^P = 1^+$  quantum numbers is worked out. We estimate the relevant low-energy coefficients from the open-charm sector, for which their values have been determined previously from sets of QCD lattice data. The leading-order heavy-quark symmetry-breaking effects are estimated by matching the  $B$ -meson ground-state chiral mass formula to the mass formula from the heavy-quark effective theory. We make refined predictions for the flavor antitriplet and sextet resonances that are generated dynamically by coupled-channel interactions.

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### I. INTRODUCTION

How to understand the spectrum of QCD is the long-lasting challenge in contemporary theoretical physics. While the strong interactions lead to a myriad of hadronic resonances, QCD, the fundamental theory, fails to describe these phenomena if tackled with a perturbative expansion in the gauge coupling constant. In order to unravel non-perturbative aspects of QCD, effective field theories are commonly employed. They are constructed to respect the asymptotic symmetries of QCD in its low-energy limit. Those symmetries include the chiral SU(3) symmetry (which holds exactly when the quarks  $u$ ,  $d$ , and  $s$  are massless) and the heavy-quark symmetry (which asymptotically holds as the quarks  $c$  or  $b$  tend to be infinitely massive). An open-charm or open-beauty system, which is composed of one heavy quark  $c$  or  $b$  and light quarks, possesses both of these two symmetries and therefore plays a crucial role in studies of QCD.

Chiral SU(3) symmetry drives the interactions between an open heavy-flavor meson and Goldstone bosons. Such interactions can be described by an effective chiral Lagrangian. The leading order  $s$ -wave interaction may be attractive or repulsive and resonant states can thus be dynamically generated (see, e.g., [1]). According to such an interaction, the nature of the open-charm meson  $D_{s0}^*(2317)$  can be successfully explained. While within a

quark model approach [2,3] such state poses a puzzle, coupled-channel scattering studies between Goldstone bosons and  $J^P = 0^-$   $D$ -meson ground states suggest that it is a bound state below the  $DK$  threshold [4–6]. It comes as a part of a flavor antitriplet, which is completed by a broad state with isospin-strangeness  $(I, S) = (1/2, 0)$  quantum numbers. The heavy-quark spin symmetry implies that a heavy-flavor hadron always comes with almost degenerate spin partners. This reflects the marginal importance of the spin orientation of its heavy-quark content. For instance, the  $D_{s1}(2460)$  can be understood as the spin 1 partner of the  $D_{s0}^*(2317)$ . In addition, the heavy-quark flavor symmetry suggests that open-beauty partners of the open-charm states should exist. We note, however, that so far no experimental evidence for the open-beauty partner of the  $D_{s0}^*(2317)$  has been found. How stable are these theoretical predictions? Answering this question requires systematic studies that take into account chiral symmetry and heavy-quark symmetry-breaking effects as based on effective Lagrangians suitably linked to QCD. In our work we use chiral perturbation theory (ChPT) and heavy-quark effective theory (HQET).

Chiral symmetry-breaking effects are encoded into low-energy constants (LEC) of the chiral Lagrangian [7–11]. In a recent study [12], the LEC relevant in the open-charm chiral Lagrangian have been well estimated from QCD lattice data on ensembles with a variety of unphysical quark masses. It was shown that the open-charm mesons  $D_{s0}^*(2317)$  and  $D_{s1}(2460)$  are stable against the next-to-leading order (NLO) chiral corrections [12,13]. Moreover, the same work [12] predicted the behavior of the  $(1/2, 0)$  antitriplet partner of the  $D_{s0}^*(2317)$  at unphysical quark masses, which has been recently confirmed by lattice simulations [14].

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Motivated by our success in the open-charm sector, we would like to derive more quantitative predictions for the open-beauty partner systems. In this article, we will study the chiral symmetry-breaking effects in the open-beauty systems, working out systematically heavy-quark spin and flavor symmetry-breaking effects. Such a projection requests a matching of ChPT to HQET.

We will first recall the part of the chiral Lagrangian responsible for the leading-order symmetry-breaking LEC. The heavy-quark mass dependence of those LEC is determined by matching the chiral formula of the  $B$ -meson masses to the HQET result. Based on such LEC, we will derive the pole positions of resonance states in the complex plane as generated by coupled-channel scattering from the chiral Lagrangian. Special attention will be paid to the antitriplet states. Predictions for the open-beauty partners of  $D_{s0}^*(2317)$  and  $D_{s1}(2460)$  will be made. A brief discussion on the flavor-exotic sextet states will follow [4,15]. In particular, we will comment on the disputed isospin and strangeness one  $X(5568)$  state [16–28].

## II. THE CHIRAL LAGRANGIAN WITH HEAVY-QUARK FLAVOR SYMMETRY

The pseudoscalar  $B$ -meson ground states form a flavor antitriplet  $B = (B^0, -B^+, B_s^+)$ . They are the heavy-quark flavor partners of the open-charm antitriplets  $D = (D^0, -D^+, D_s^+)$  states. In both flavor sectors the heavy-quark spin symmetry predicts almost degenerate  $J^P = 1^-$  partner states. According to the heavy-quark flavor symmetry, the chiral Lagrangian for these two types of mesons take the same form. Therefore it is useful to introduce generic heavy-meson fields  $H$  and  $H_{\mu\nu}$ , that refer either to a  $D$  or a  $B$ -meson antitriplet field. The kinetic terms of the heavy-flavored mesons constitute the leading-order chiral Lagrangian:

$$\begin{aligned} \mathcal{L}_{\text{kin}} = & (\hat{\partial}_\mu H)(\hat{\partial}^\mu \bar{H}) - \left(\bar{M} - \frac{3}{4}\Delta\right)^2 H\bar{H} \\ & - (\hat{\partial}_\mu H^{\mu\alpha})(\hat{\partial}^\nu \bar{H}_{\nu\alpha}) + \frac{1}{2}\left(\bar{M} + \frac{1}{4}\Delta\right)^2 H^{\mu\alpha}\bar{H}_{\mu\alpha}, \end{aligned} \quad (1)$$

where the LEC  $c_i = c_i(M_Q)$  and  $\tilde{c}_i = \tilde{c}_i(M_Q)$  depend on the heavy-quark mass  $M_Q$ . Throughout this work we will use a superscript  $(c)$  and  $(b)$  with e.g.,

$$c_i^{(c)} \equiv c_i(M_Q = M_c), \quad \tilde{c}_i^{(b)} \equiv \tilde{c}_i(M_Q = M_b), \quad (5)$$

for the open-charm and open-beauty systems, respectively. The chiral terms  $\Pi_H^{(2),i}$  are linear combinations of the light-quark masses:

where following [12,13] the tensor field representation is adopted for the vector mesons. The LEC  $\bar{M} - \frac{3}{4}\Delta$  and  $\bar{M} + \frac{1}{4}\Delta$  are the chiral-limit masses of the heavy pseudoscalar and vector mesons, respectively. They depend on the heavy-quark mass  $M_Q$ . The  $\bar{M} = \bar{M}(M_Q)$  scales as  $\bar{M} \sim M_Q$  in the heavy-quark mass limit. The hyperfine splitting  $\Delta = \Delta(M_Q)$  is caused by  $O(1/M_Q)$  heavy-quark spin symmetry-breaking effect [29,30].

The chiral covariant derivative  $\hat{\partial}_\mu$  in (1),

$$\begin{aligned} \hat{\partial}_\mu \bar{H} &= \partial_\mu \bar{H} + \Gamma_\mu \bar{H}, & \hat{\partial}_\mu H &= \partial_\mu H - H\Gamma_\mu, \\ \Gamma_\mu &= \frac{1}{2}e^{-i\frac{\Phi}{2f}}\partial_\mu e^{+i\frac{\Phi}{2f}} + \frac{1}{2}e^{+i\frac{\Phi}{2f}}\partial_\mu e^{-i\frac{\Phi}{2f}}, \end{aligned} \quad (2)$$

involves the flavor octet Goldstone-boson fields as encoded in the  $3 \times 3$  matrix  $\Phi$ . The parameter  $f$  is the chiral limit of the pion-decay constant for which we choose  $f = 92.4$  MeV. The leading-order, so called Tomozawa-Weinberg, interaction between the  $B$  mesons and the Goldstone bosons is implied by the kinetic terms (1) via its covariant derivative and the chiral connection  $\Gamma_\mu$ .

At the NLO the chiral Lagrangian has terms that are proportional to the masses of the  $u$ -,  $d$ -, and  $s$  quarks. Such terms break the chiral symmetry explicitly and define corrections to the heavy-flavor ground-state masses. We recall such terms in the chiral Lagrangian:

$$\begin{aligned} \mathcal{L}_\chi &= -(4c_0 - 2c_1)H\bar{H}\text{tr}\chi_+ - 2c_1H\chi_+\bar{H} \\ &+ (2\tilde{c}_0 - \tilde{c}_1)H^{\mu\nu}\bar{H}_{\mu\nu}\text{tr}\chi_+ + \tilde{c}_1H^{\mu\nu}\chi_+\bar{H}_{\mu\nu}, \\ \chi_\pm &= \frac{1}{2}(e^{+i\frac{\Phi}{2f}}\chi_0 e^{+i\frac{\Phi}{2f}} \pm e^{-i\frac{\Phi}{2f}}\chi_0 e^{-i\frac{\Phi}{2f}}), \end{aligned} \quad (3)$$

where the quark-mass dependence is embodied in the diagonal matrix  $\chi_0 = 2B_0 \text{diag}(m_u, m_d, m_s)$ , with the low-energy constant  $B_0$ . Throughout this work we assume perfect isospin symmetry with  $m_u = m_d = m$ . Those parameters contribute to the  $J^P = 0^-$  and  $J^P = 1^-$  meson masses at NLO:

$$M_H^2 = \begin{cases} \left(\bar{M} - \frac{3}{4}\Delta\right)^2 + (4c_0 - 2c_1)\Pi_H^{(2),0} + 2c_1\Pi_H^{(2),1} + \Pi_H^{\text{HO}} & \text{if } H \in [0^-] \\ \left(\bar{M} + \frac{1}{4}\Delta\right)^2 + (4\tilde{c}_0 - 2\tilde{c}_1)\Pi_H^{(2),0} + 2\tilde{c}_1\Pi_H^{(2),1} + \Pi_H^{\text{HO}} & \text{if } H \in [1^-] \end{cases}, \quad (4)$$

$$\begin{aligned} \Pi_H^{(2),0} &= 2B_0(2m + m_s), \\ \Pi_H^{(2),1} &= \begin{cases} 2B_0m & \text{if } H \in \{D, D^*, B, B^*\} \\ 2B_0m_s & \text{if } H \in \{D_s, D_s^*, B_s, B_s^*\}, \end{cases} \end{aligned} \quad (6)$$

that contribute to chiral order  $Q_\chi^2$ , with

$$Q_\chi \sim \sqrt{B_0 m_q}, \quad q = u, d, s. \quad (7)$$

The higher-order chiral corrections  $\Pi_H^{\text{HO}}$  start from  $O(Q_\chi^3)$  at the one-loop level.

The parameters  $c_i$  and  $\tilde{c}_i$  scale with the heavy-quark mass  $M_Q \sim \bar{M}$  in the heavy-quark mass limit [29,30]. It is useful to make this more explicit. We factor out their heavy-quark mass-independent part, denoted by  $C_i \sim \Lambda_\chi^{-1}$ . They are of dimension  $-1$  with  $\Lambda_\chi$  the chiral symmetry-breaking scale. Higher-order corrections account for the heavy-quark symmetry-breaking effects. At order  $1/\bar{M}$ , those effects enter. They consist of an overall shift to  $C_i$  and a hyperfine splitting between the  $c_i$  and  $\tilde{c}_i$  [31,32]. We introduce dimensionless parameters  $\zeta_i$  and  $\eta_i$  responsible for these two kinds of effects, and arrive at the following representation:

$$\begin{aligned} c_i(M_Q) &= \bar{M}(M_Q) \left( C_i + \frac{\zeta_i}{\bar{M}(M_Q)} - \frac{3}{4} \frac{\eta_i(M_Q)}{\bar{M}(M_Q)} \right), \\ \tilde{c}_i(M_Q) &= \bar{M}(M_Q) \left( C_i + \frac{\zeta_i}{\bar{M}(M_Q)} + \frac{1}{4} \frac{\eta_i(M_Q)}{\bar{M}(M_Q)} \right). \end{aligned} \quad (8)$$

The parameters  $\eta_i = \eta_i(M_Q)$  depend on  $M_Q$ . The remaining four parameters  $C_i, \zeta_i$  turn out to be independent of  $M_Q$ . This will be seen in the next section, in which an explicit matching with HQET is worked out.

The LEC in the charm sector  $c_i$  and  $\tilde{c}_i$  at  $M_Q = M_c$  were adjusted in four fit scenarios in [12]. In application of such values, the  $C_i$  can be determined modulo an unknown  $\zeta_i$  dependence:

$$C_i = \frac{1}{4\bar{M}^{(c)}} (c_i^{(c)} + 3\tilde{c}_i^{(c)} - 4\zeta_i), \quad (9)$$

where we apply our notation  $c_i^{(c)} \equiv c_i(M_c)$ . Similarly, the value of  $\eta_i$  at  $M_Q = M_c$  can be easily derived as

$$\eta_i^{(c)} = (\tilde{c}_i^{(c)} - c_i^{(c)}), \quad (10)$$

with again  $\eta_i^{(c)} \equiv \eta_i(M_c)$ .

In this work, the one-loop result is employed for the higher-order chiral correction terms  $\Pi_H^{\text{HO}}$ . At the one-loop level, they receive contributions from bubble and tadpole diagrams and their corresponding counterterms:

$$\Pi_H^{\text{HO}} = \Pi_H^{\text{bubble}} + \Pi_H^{\text{tadpole}} + \Pi_H^{\text{CT}}. \quad (11)$$

For explicit expressions, Refs. [12,13] are referred to. While more LEC are involved, they have been determined in the charm sector in Ref. [12]. Using the leading-order scaling behavior,  $\Pi_H^{\text{HO}} \sim \bar{M}(M_Q)$ , the LEC in the bottom sector can be well estimated.

### III. MATCHING THE CHIRAL LAGRANGIAN AND THE HQET

So far we have not yet fully specified the LEC  $c_{0,1}^{(b)}$  and  $\tilde{c}_{0,1}^{(b)}$  in (8). While at leading order in the  $1/M_Q$  expansion

their values may be inferred from  $c_{0,1}$  and  $\tilde{c}_{0,1}$  at  $M_Q = M_c$  this is no longer true at subleading order. Since such counterterms contribute at NLO in the chiral counting scheme it appears reasonable to consider the effect of order  $1/M_Q$ . Note that our approach considers chiral N<sup>2</sup>LO effects in the heavy pseudoscalar and vector-meson masses. We now set up a more detailed matching with HQET, in which the heavy-meson masses take the form [33]

$$M_H(M_Q) = \begin{cases} M_Q + \bar{\Lambda}_{(H)} + \frac{\mu_\pi^2}{2M_Q} - \frac{\mu_G^2}{2M_Q} & \text{if } H \in [0^-] \\ M_Q + \bar{\Lambda}_{(H)} + \frac{\mu_\pi^2}{2M_Q} + \frac{\mu_G^2}{6M_Q} & \text{if } H \in [1^-] \end{cases}. \quad (12)$$

The quantities  $\bar{\Lambda}$  and  $\mu_\pi^2, \mu_G^2$  come with an explicit index ( $H$ ), that resolves the specifics of the light-quark content. The  $\bar{\Lambda}$  is the contribution from light degrees of freedom, and therefore  $M_Q$  independent [34]. The  $\mu_\pi^2$  term accounts for the kinetic energy of the heavy quark in the meson's rest frame. Due to reparametrization invariance, it is  $M_Q$  independent as well [35]. Finally, the  $\mu_G^2$  is a chromomagnetic moment which leads to a hyperfine splitting between the  $0^-$  and  $1^-$   $B$  mesons. It depends on the heavy-quark mass. We assume that  $\mu_G^2$  can be factorized as a product of the high-energy and low-energy contributions,

$$\mu_G^2 = \hat{C}_{\text{cm}}(M_Q) \hat{\mu}_G^2, \quad (13)$$

where the factor  $\hat{\mu}_G$  accounts for low-energy contributions. The high-energy contributions are incorporated in the renormalization-group (RG) invariant Wilson coefficient  $\hat{C}_{\text{cm}}(M_Q)$  [36]. The RG evolution starts at a scale close to the heavy-quark mass  $\mu \sim M_Q$ , where the value of the Wilson coefficient is determined by matching the chromomagnetic moment from HQET to the multiloop calculations from the QCD Lagrangian. For our purposes it suffices to know the ratio  $\hat{C}_{\text{cm}}(M_b)/\hat{C}_{\text{cm}}(M_c)$ . This ratio has been derived at the one-loop and two-loop level in [37] and [38,39], respectively. The averaged result is

$$R \equiv \frac{\hat{C}_{\text{cm}}(M_b)}{\hat{C}_{\text{cm}}(M_c)} \simeq 0.80(4), \quad (14)$$

where the uncertainty is estimated by the difference of the one-loop and the two-loop results. In the latest calculation, a poor convergence pattern has been claimed at the three-loop level [40]. Therefore we refrain from using the three-loop result here.

The expansion moments  $\bar{\Lambda}$ ,  $\mu_\pi^2$ , and  $\hat{\mu}_G$  depend on physical scales significantly lighter than  $M_Q$ : the light-quark masses  $m_q$  and an intrinsic nonperturbative QCD scale  $\Lambda$ . While  $\Lambda$  was once commonly regarded as the Landau scale  $\Lambda_{\text{QCD}}$  in literature [37,41,42], we follow the

way of Refs. [31,43] and identify  $\Lambda \sim \Lambda_\chi$ . It has been demonstrated in [44] that only via such an assignment, ChPT and HQET can be matched convincingly at the loop level. Moreover, the size of  $\Lambda$  should be comparable to the mass difference  $\bar{M} - M_Q$  [31,37]. Using numerical values, this mass difference is  $\sim 0.8$  GeV for both charm and bottom systems, indeed consistent with estimates of  $\Lambda_\chi$ .

In the chiral limit, the  $\bar{\Lambda}$  scales as  $\sim \Lambda$  whereas the  $\mu_\pi^2$  and  $\hat{\mu}_G^2$  scale as  $\sim \Lambda^2$ . We can expand the components  $\bar{\Lambda}$ ,  $\mu_\pi^2$ , and  $\hat{\mu}_G^2$  in powers of the light-quark masses around their chiral limit. The corrections are suppressed by powers of  $\sqrt{B_0 m_q}/\Lambda_\chi$ . The small-scale expansion scheme entails the scaling behavior  $\Delta \sim \hat{\mu}_G^2/\bar{M} \sim Q_\chi$ , and therefore the expansion parameters in the chiral and heavy-quark expansions are comparable:

$$\frac{\sqrt{B_0 m_q}}{\Lambda_\chi} \sim \frac{\Lambda}{M_Q}. \quad (15)$$

By matching the mass formula (12) with the chiral result (4), we can recover the relations between the  $\bar{M}$ ,  $\Delta$ , and the heavy-quark moments [29,32]. It is emphasized that the chiral structure of (4) restricts the structure of the  $O(Q_\chi^2)$  corrections to the heavy-quark expansion moments. From the matching we obtain that  $C_i$  and  $\zeta_i$  are involved in the  $O(Q_\chi^2)$  corrections of  $\bar{\Lambda}$  and  $\mu_\pi^2$ , respectively. And they are indeed heavy-quark mass independent. In addition  $\eta_i$  contributes to the  $O(Q_\chi^2)$  corrections of  $\mu_G^2$ , and its scaling behavior is proportional to  $\hat{C}_{\text{cm}}$ . We summarize,

$$\frac{\bar{M}^{(b)} \Delta^{(b)}}{\bar{M}^{(c)} \Delta^{(c)}} = \frac{\eta_i^{(b)}}{\eta_i^{(c)}} = R. \quad (16)$$

Using (16) with  $R \simeq 0.80$  together with (10) we are left with three unknown parameters  $\bar{M}^{(b)}$  and  $\zeta_{0,1}$ . The  $M_Q$ -independent parameters  $C_i$  follow from (9).

The three unknown parameters  $\bar{M}^{(b)}$  and  $\zeta_{0,1}$  are determined by a fit with our chiral mass formula to the empirical values of the four  $B$ -meson ground-state masses. Here we admit a residual systematic uncertainty of 5 MeV in the heavy-meson masses. Such a value was used in our previous open-charm system studies [12]. It reflects the accuracy level at which we expect our one-loop chiral formula to hold. The results of  $\bar{M}^{(b)}$ ,  $\zeta_{0,1}$  are shown in Table I. In this table, we also show the parameters involved in the expansion (8) together with the associated LEC. In the fits, we used the results of [12], for the inputs of the LEC in the charm sector. In the charm sector, four sets of fitted results are determined according to the lattice data on  $D$ -meson ground-state masses and  $\pi D$   $s$ -wave scattering process. They are named Fits 1–4. We will recall some of the fitting details in the following discussion.

TABLE I. The low-energy parameters in (8), corresponding to Fits 1–4 in the charm sector [12]. The  $\chi^2/N$  is the chi-square per data point, with the number of data points  $N = 4$  and an *ad hoc* systematic error estimate of 5 MeV.

	Fit 1	Fit 2	Fit 3	Fit 4
$\bar{M}^{(b)}$ [GeV]	5.3743	4.8540	5.3303	5.3666
$\zeta_0$	0.0921	-1.5072	-0.0839	0.0523
$\zeta_1$	0.1689	0.1233	0.1585	0.1678
$C_0$ [GeV $^{-1}$ ]	0.0602	0.8777	0.1774	0.1145
$C_1$ [GeV $^{-1}$ ]	0.2376	0.3916	0.3382	0.3445
$\eta_0^{(b)}$	-0.0145	-0.0302	-0.0176	-0.0170
$\eta_1^{(b)}$	-0.0238	0.0318	-0.0276	-0.0238
$\Delta^{(b)}$ [GeV]	0.0562	0.0643	0.0563	0.0568
$c_0^{(b)}$	0.4262	2.7757	0.8750	0.6797
$\tilde{c}_0^{(b)}$	0.4117	2.7455	0.8574	0.6628
$c_1^{(b)}$	1.4637	2.0002	1.9820	2.0345
$\tilde{c}_1^{(b)}$	1.4399	2.0320	1.9544	2.0107
$\chi^2/N$	0.94	0.10	0.89	0.92

Consider first the scenarios of Fits 1, 3, and 4. The masses of the  $B$ -meson ground states can be reproduced within the systematic error of 5 MeV. All of the three fits give modest heavy-quark corrections to the leading-order expectations of  $c_{0,1}$  and  $\tilde{c}_{0,1}$ . At leading order,  $c_{0,1}$  and  $\tilde{c}_{0,1}$  are about 2.5 times larger at  $M_Q = M_b$  as compared to their values at  $M_Q = M_c$ . For convenience we recall the ranges  $c_0 \sim \tilde{c}_0 \sim (0.2-0.3)$  and  $c_1 \sim \tilde{c}_1 \sim (0.6-0.9)$  at  $M_Q = M_c$  from [12].

Scenarios 3 and 4 show quite similar values for the LEC. This is not the case for scenario 1. Here we recall a decisive distinction. Both Fit 1 and Fit 2 did not consider QCD lattice data on the  $\pi D$   $s$ -wave scattering process [45]. While Fit 1, nevertheless, appears reasonably consistent with the  $\pi D$  phase shift and inelasticity parameters as given in [45], this is not the case for Fit 2. The key feature of Fit 3 and also Fit 4 is their compatibility with the lattice data on the  $\eta D$  phase shift. Such data play a crucial role in the determination of the LEC. Based on this observation we would disfavor scenarios 1 and 2. In this context it is amusing to observe that Fit 2 should be rejected also based on an unnaturally large value of the  $\zeta_0$  parameter as shown in Table I. This is so despite the fact that it comes with the best chi-square value for the reproduction of the  $B$ -meson masses. The corresponding  $c_0 \sim \tilde{c}_0 \sim 2.7$  at  $M_Q = M_b$ , are nearly ten times larger than their charmed counterparts  $c_0 \sim \tilde{c}_0 \sim 0.3$ . This implied a serious violation of the leading-order scaling behavior. Such large LEC lead to unnaturally large higher-order corrections. Therefore, altogether we exclude Fit 2 from our further analysis.



#### IV. SCATTERINGS WITH COUPLED-CHANNEL DYNAMICS

The chiral Lagrangian predicts the formation of  $J^P = 0^+$  and  $J^P = 1^+$  resonance state as a consequence of coupled-channel final-state interactions of the Goldstone bosons with the ground-state heavy mesons with  $J^P = 0^-$  and  $J^P = 1^-$  quantum numbers. Such states are an unavoidable consequence of the flavor SU(3) chiral Lagrangian. We focus on the resonances generated by the  $s$ -wave scatterings with open-beauty quantum numbers. Here the leading-order coupled-channel interaction is predicted by the Tomozawa-Weinberg theorem in terms of the “known” parameter  $f$ . A resonance is dynamically generated from a scattering process when the reaction amplitude contains a pole in the complex  $s$  plane. The scattering amplitude with manifest  $s$ -channel unitarity is obtained from a self-consistent summation:

$$T_{ab}(s) = V_{ab}(s) + \sum_{c,d} V_{ac}(s) J_{cd}(s) T_{db}(s), \quad (17)$$

with given out- and in-going two-body states  $a$  and  $b$ . The  $T$  matrix exhibits poles in the complex  $s$  plane that we can determine by extending the definition of  $T(s)$  into the higher Riemann sheet of the  $s$  plane. The potential  $V_{ab}(s)$  is obtained with an on-shell condition [1], and set equivalent to the scattering amplitude as derived from the chiral Lagrangian at the matching point  $\sqrt{s} = \mu_M$ . It receives tree-level chiral symmetry-breaking contributions from the Lagrangian (3). Additional terms are implied by the LEC that imply the one-loop  $\Pi_H^{\text{HO}}$  structures decomposed in (11). The latter will also contribute to  $V_{ab}(s)$  as tree-level chiral symmetry-preserving corrections; see Ref [12]. Following [4], we set  $\mu_M = M_{B^*(S)}$  for  $S = 0, 2$  and  $\mu_M = M_{B_s^*(S)}$  for  $S = \pm 1$  scatterings with the total quantum numbers  $J^P = 0^+(1^+)$ . The diagonal analytic matrix  $J(s)$  function is universal as it leads to a scattering amplitude  $T(s)$  that is consistent with the coupled-channel unitarity condition and the microcausality condition. Such an approach can be justified if short-range forces largely dominate the system. Along the real axis from each threshold, there is a branch cut defining the doorway for the higher Riemann sheets. For an  $n$ -dimensional coupled-channel system there are  $2^n$  Riemann sheets, and we use the signature  $(\pm, \dots, \pm)$  as introduced in [13] to label a specific one.

We start with a discussion of the flavor antitriplet channels. Poles in the complex  $s$  plane are found from the parameter sets 1, 3, and 4. The complex pole masses are compared with the results from the Tomozawa-Weinberg interaction in Table II. To estimate the theoretical error, we allow a deviation of the matching points from their natural values for  $|\Delta\mu_M| = 0.1$  GeV. We first look at the states with isospin and strangeness  $(I, S) = (0, 1)$ . A pole below the  $BK$  threshold is found on the physical Riemann sheet

TABLE II. Complex pole masses (in GeV) of the flavor antitriplet states with  $J^P = 0^+$  and  $1^+$ . The relevant Riemann sheets are  $(-, +, +)$  and  $(+, +)$  for  $(I, S) = (1/2, 0)$  and  $(0, 1)$ .

	$(I, S) = (1/2, 0)$	$(I, S) = (0, 1)$
$J^P = 0^+$		
Fit 1	$5.5202_{-209}^{+282} - 0.0923_{-254}^{+463} i$	$5.6296_{-395}^{+431}$
Fit 3	$5.5137_{-225}^{+179} - 0.1073_{-387}^{+623} i$	$5.5689_{-544}^{+614}$
Fit 4	$5.5126_{-196}^{+154} - 0.1120_{-384}^{+595} i$	$5.5755_{-535}^{+610}$
TW	$5.5207_{-190}^{+260} - 0.0905_{-243}^{+456} i$	$5.6495_{-310}^{+353}$
$J^P = 1^+$		
Fit 1	$5.5652_{-208}^{+283} - 0.0915_{-252}^{+460} i$	$5.6763_{-391}^{+428}$
Fit 3	$5.5595_{-224}^{+179} - 0.1071_{-384}^{+624} i$	$5.6179_{-542}^{+610}$
Fit 4	$5.5586_{-198}^{+156} - 0.1115_{-382}^{+597} i$	$5.6242_{-533}^{+605}$
TW	$5.5658_{-190}^{+260} - 0.0903_{-242}^{+455} i$	$5.6959_{-311}^{+354}$

in the  $J^P = 0^+$  scattering amplitude always. It is the open-beauty partner of  $D_{s0}^*(2317)$ . The pole mass is 5.59(8) GeV. Comparing to the leading-order result at 5.65(3) GeV, the higher-order chiral corrections slightly reduce the pole mass. This result is somewhat lower than previous predictions with values above 5.7 GeV [10, 46–48]. In the axial-vector sector, the open-beauty partner of  $D_{s1}(2460)$  is found as a bound state at 5.64(8) GeV, which should be compared with previous predictions at above 5.75 GeV [10, 46–48]. Besides the bound states in the  $(I, S) = (0, 1)$  channels, broad resonances are found in the  $(I, S) = (1/2, 0)$  channels with poles in the unphysical Riemann sheet denoted by  $(-, +, +)$ . Their broad charmed partners were extensively discussed in previous theoretical studies [4, 7, 10, 15, 48, 49]. Our prediction of their pole masses are  $(5.52(3) - 0.12(5)i)$  GeV for the  $0^+$  state and  $(5.57(3) - 0.12(5)i)$  GeV for the  $1^+$  state. Both of them are in agreement with previous theoretical predictions [4, 10, 48, 50].

In the charmed and beauty sector, there are further poles belonging to a flavor sextet. In Table III, we listed the complex pole masses found in the sextet channels with  $(I, S) = (1/2, 0)$  and  $(1, 1)$  from Fits 1, 3, and 4. The other sextet channel, with  $(I, S) = (0, -1)$ , shows a pole in the vicinity of the scattering threshold within the range of our theoretical uncertainty always. The resonances with  $(I, S) = (1/2, 0)$  were also obtained in previous works [48, 50] with masses (5.84–5.85) GeV and (5.88–5.91) GeV, respectively, for  $J^P = 0^+$  and  $1^+$ . Our predicted values are significantly smaller than those. The  $J^P = 0^+$  member with  $(I, S) = (1, 1)$  is of particular interest. It has been speculated that the controversial  $X(5568)$  state has such quantum numbers (see e.g., [51, 52]). In [4], it was shown that the LO Tomozawa-Weinberg interaction implies the existence of an exotic state with  $J^P = 0^+$  and  $(I, S) = (1, 1)$  quantum numbers at  $\sqrt{s} \simeq (5.79(3) - 0.07(1)i)$  GeV. We demonstrate that this prediction is quite stable against higher-order

TABLE III. Complex pole masses (in GeV) of two flavor sextet states with  $J^P = 0^+$  and  $1^+$ . The relevant Riemann sheets are  $(-, +, +)$  and  $(-, +)$  for  $(I, S) = (1/2, 0)$  and  $(1, 1)$ .

	$(I, S) = (1/2, 0)$		$(I, S) = (1, 1)$	
$J^P = 0^+$				
Fit 1	$5.8104_{-099}^{+095}$	$-0.0148_{+010}^{-023} i$	$5.8045_{-205}^{+261}$	$-0.0730_{-064}^{+127} i$
Fit 3	$5.7274_{-144}^{+258}$	$-0.0595_{+158}^{-230} i$	$5.7945_{-154}^{+147}$	$-0.1871_{-219}^{+266} i$
Fit 4	$5.7422_{-171}^{+285}$	$-0.0517_{+186}^{-233} i$	$5.7868_{-134}^{+133}$	$-0.1938_{-190}^{+234} i$
TW	$5.7730_{-149}^{+148}$	$-0.0201_{+7}^{-22} i$	$5.7900_{-245}^{+319}$	$-0.0719_{-52}^{+107} i$
$J^P = 1^+$				
Fit 1	$5.8592_{-096}^{+091}$	$-0.0153_{+011}^{-025} i$	$5.8558_{-208}^{+264}$	$-0.0730_{-063}^{+127} i$
Fit 3	$5.7747_{-141}^{+254}$	$-0.0638_{+160}^{-237} i$	$5.8406_{-150}^{+146}$	$-0.1913_{-211}^{+256} i$
Fit 4	$5.7894_{-166}^{+279}$	$-0.0564_{+186}^{-241} i$	$5.8333_{-132}^{+133}$	$-0.1972_{-184}^{+227} i$
TW	$5.8192_{-150}^{+148}$	$-0.0198_{+7}^{-22} i$	$5.8362_{-246}^{+320}$	$-0.0708_{-51}^{+105} i$

corrections from our Fits 1, 3, and 4. The pole mass comes at  $(5.80(3) - 0.14(8)i)$  GeV as shown in Table III. We conclude that the  $X(5568)$  cannot be a chiral excitation, i.e., it is not explained convincingly by chiral coupled-channel dynamics. This supports previous such claims [53,54].

## V. SUMMARY

We studied open-beauty mesons with  $J^P = 0^+$  and  $1^+$  quantum numbers. Such states were predicted as a consequence of coupled-channel interactions based on the chiral SU(3) Lagrangian. Already the leading-order Tomozawa-Weinberg interaction implies attractive forces in the flavor

antitriplet and sextet channels between the Goldstone bosons and the heavy-meson ground states with  $J^P = 0^-$  and  $1^-$  quantum numbers.

In this article the role of the next-to-leading order chiral interactions in the  $s$ -wave open-beauty meson scattering processes was scrutinized. The LEC are derived mainly from corresponding LEC as obtained previously from global fits to the QCD lattice dataset in the charm sector [12]. Where possible additional direct data from the beauty sector were taken into account. The heavy-quark scaling behavior is constrained by the RG-invariant Wilson coefficient for the chromomagnetic moment. We employ the results of the Wilson coefficient calculated at the two-loop level.

We find that in the antitriplet but also in the exotic flavor sextet, the chiral correction terms lead to minor effects in the  $J^P = 0^+$  and  $1^+$  pole masses only. This confirms the semiquantitative predictions made almost two decades ago by one of the authors. Our refined values should be used in ongoing experimental searches and QCD lattice simulations. It is noted, however, that like in the open-charm sector, we expect the light-quark mass dependence in the flavor antitriplet and sextet states to be significant. This should be investigated further, in particular for the  $\pi B$   $s$ -wave phase shifts.

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