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Circuit Modelling of Broadband Antenna Using Vector Fitting and Foster Form Approaches for IoT Applications

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Abstract: Computation of the broadband antenna impedance behavior requires the wideband lumped equivalent circuit. This work aims to provide a comprehensive study of broadband antenna equivalent circuit models over broad frequency ranges for Internet of Things (IoT) applications using multiple approaches. The first approach is a Foster approximation, which is based on the antenna-simulated scattering parameters and impedance data. The second concerns a vector-fitting fitting approximation, which is based on the antenna-simulated impedance/admittance data. The studied antenna is modeled based on the radiating element's geometry and the multifractal slots, in addition to the DGS (Defected Ground Plane) effects. Applying these techniques, wideband lumped equivalent circuits of the antenna have been computed which are in good agreement with measurement data. These models could be useful for the enhancement of the performance of a broadband antenna and its systematic design as well as offering the advantage of saving computation time for full-wave simulations and facilitating the solution of problems that have both an electromagnetic part as well as a circuit part. For further analysis, the Gaussian pulse has been generated to drive a time-domain analysis of the current and power response waveforms antenna behavior under load.

Keywords: broadband antenna; equivalent circuit model; foster forms; time-domain analysis; vector fitting; Internet of Things (IoT)



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1. Introduction

Rapid development in wireless communications has resulted in a rising need for small antennas that can function across many frequency bands to meet the requirements of various applications. Therefore, it is preferred to have a single integrated antenna structure that can operate across a wide range of frequencies while keeping the system's footprint as small as possible. For this reason, antenna designs that combine the capabilities of several antennas into a single emitter structure have surged in popularity in recent years. On the other hand, multiband antennas reduce electromagnetic interference and pulse distortion effects. Moreover, their desirable characteristics, such as integration ease, lightweight, compact size, and low manufacturing cost, make them the preferred choice over their counterparts and excellent choices for modern wireless communication systems.

To further understanding of the antenna performance, it is recommended to obtain its equivalent circuit model. Such an electrical model can be very useful for circuit simulations, as might be desired in the analysis of an integrated antenna. Accordingly, the development of the electrical circuit model is important for its time-domain analysis, to understand

the antenna resonance and structure, to derive mathematical equations, and to design a systematic antenna exploring the equivalent circuit [1–13]. Moreover, it helps predict the effects of integrating the antenna [11]. However, developing equivalent circuits for complicated antenna configurations that have numerous resonances is a difficult task [13].

To design antenna structures, rigorous numerical methods are employed to resolve electromagnetic equations in integral or differential forms, such as CST, HFSS and FEKO, are employed. The concern is that these methods offer better accuracy, but they have some limitations [4,6,9]. They cannot cover all kinds of losses. Moreover, they generally require a long and cumbersome computation with complicated settings and cost consumption. Moreover, the equivalent circuit model, either in the form of a transmission line model or in the form of a lumped circuit model of antennas is widely used to enhance the antenna design features by considering antennas as load impedances.

The lumped equivalent circuit parameters can be computed either from the curve fitting method, using the rational approximation of frequency responses of the antenna, based on the cavity model of the antenna, or from graphical methods. A previous study reported in [4] that an RFID antenna was modelled as a parallel RLC circuit. The geometric dimensions of the antenna and the dielectric properties were used to determine the RLC parameters. In [13], we see that the rational approximation of the frequency domain response of a dual-band Planer Inverted-F Antenna (PIFA) and its lumped equivalent circuit formulation may be used to improve their performance. The UHF small double E-shaped meander line printed monopole antenna circuit model was produced by the authors of reference [14] using inductance and capacitance circuits. All of the circuits were linked in parallel. Using the work provided in [15], it is possible to demonstrate that the equivalent circuit model of a small multi-band antenna may be built using a series of parallel RLC circuits. Thus, the input impedance curve is used as a starting point for the initial values of the RLC parameters. Furthermore, in [16], researchers provide a novel method for determining the wideband lumped equivalent circuit of rectangular and Eshaped microstrip antennas. By using a nonlinear curve-fitting optimization strategy, the starting values for the equivalent circuit parameters are derived. With [17,18], a method is provided for generating wideband electrical models of frequency-domain responses approximating rational functions, which may be used in SPICE. They have shown that lowrank approximations of one-port or two-port systems may be effectively generated using the fitting method or reduced-order models. An alternative approach to the circuit modeling problem of the broadband antenna using frequency domain data from simulations or measurements was introduced in [19]. Using this method, an equivalent circuit may be created for use with broadband antennas, which is an intriguing prospect. An approach is also provided for establishing the antenna's input impedance model in the frequency domain, which involves the generation of a rational function approximation with actual coefficients. Several circuit models have been made to perform equivalent-circuit models of different UWB antenna shapes [20–24]. Some available and helpful equivalent circuit model synthesizing techniques were discussed and reported in [17,25-40] for readers' further and deep knowledge.

The aim of this work is to review the most important circuit synthesis approaches to derive lumped equivalent circuits for a broadband antenna based on frequency domain S-parameters/Admittance/impedance data. The lumped equivalent circuit of the designed antenna is derived from the rational approximation of its frequency domain response using Foster approximation, the vector-fitting approach (VF), and based on antenna geometry and substrate characteristics. Subsequently, the derived equivalent circuits are simulated in Advanced Design System (ADS) software. The accuracy of the models has been validated by comparing its transient response with the antenna measurement result. Afterward, the model's transient response is driven, and a time-domain analysis is performed to study the voltage, current, and power response waveforms of the antenna equivalent circuit. The generated models can then be connected to linear or nonlinear devices or localized elements to analyze the electromagnetic problems in the circuits associated with the antenna. The

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model can be used for any SPICE-based simulator tools; hence, it can be used in the co-design of the transmitter and receiver in circuit simulators.

The following is the outline for this paper: Foster approximation and rational function approximation using a vector-fitting method are two examples of the methods that are examined here. The equivalent circuit models of broadband antennas are calculated using the aforementioned methods, and their simulation results are shown in Section 2. In Section 3, we conduct a thorough time-domain analysis in ADS software of the antenna equivalent circuit with a pulse produced from the seventh Gaussian derivative. Section 4 provides some last thoughts on the matter.

2. Broadband Antenna Equivalent Circuit Methodologies

The antenna in Figure 1a was adopted to obtain further in-depth information on how the previously discussed approaches can be applied.

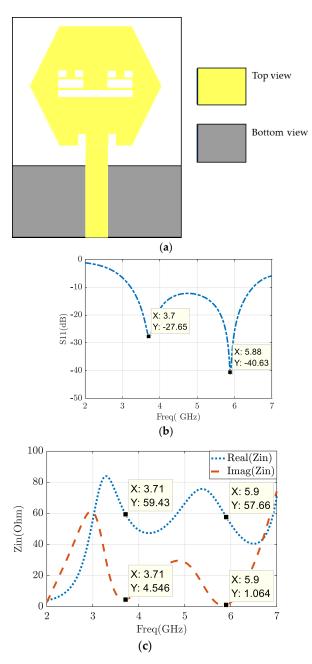


Figure 1. (a) Case study antenna; (b) the simulated antenna S11 (dB) versus frequency; (c) antenna-simulated impedance (Ohms).

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2.1. Stage I: Equivalent Circuit Model via Foster Canonical Form

Based on First Foster approximation, the input impedance Zin of an antenna is represented by the following Equation (1):

$$Z_{in}(\omega) \cong j\omega L_0 + \frac{1}{j\omega C_0} + \sum_{n=1}^{N_{max}} \frac{R_n}{1 + jQ_n \left(\frac{\omega}{\omega_n} - \frac{\omega_n}{\omega}\right)}$$
(1)

where N_{max} is the number of modes required to accurately describe the frequency behavior of the antenna input impedance, $Q_n = \omega_n R_n C_n$ and $\omega_n = (L_n C_n)^{-0.5}$. is the operating angular frequency, and ω_n is the resonant angular frequency of the nth resonant mode. C_0 is the quasi-static input capacitance, and L_0 is an inductance that accounts for higher-order modes as well as for feed effects, while C_n , L_n , R_n , and Q_n are the capacitance, inductance, resistance, and quality factor, respectively, describing the antenna's resonant processes [4,10].

The behavior of higher-order modes and antenna feed effects are modeled by C_0 and L_0 [38]. The quasi-static inductance L_0 is generally infinitesimal when the order of the resonant modes is low. In particular, each mode is assumed to be characterized by a natural resonance ω_n , a quality factor Q_n , and a damping resistance R_n .

The capacitance C_0 using Equation (2) [3,6].

$$C_0 = \lim_{\omega \to 0^+} \frac{Im\{Y_{in}^{EM}(\omega)\}}{\omega} = \lim_{\omega \to 0^+} \frac{\partial Im\{Y_{in}^{EM}(\omega)\}}{\partial \omega} \approx \frac{Im\{Y_{in}^{EM}(\Delta\omega)\}}{\Delta\omega}$$
(2)

EM: CST MWS electromagnetic simulations. where

$$\Delta\omega = 2\pi\Delta f \, Y_{in}^{EM} = 1/Z_{in}^{EM}$$

Furthermore, the resonant frequencies of the RLC dipoles can be calculated as a first approximation by determining the values $\omega_n(0)$ for which the real part of Z_{in}^{EM} has local maxima. Thus, the initial estimates of R_n and Q_n are computed using Equations (3) and (4) [3,6]:

$$R_n^{(0)} = Re\left\{ Z_{in}^{EM} \left(\omega_n^{(0)} \right) \right\} \tag{3}$$

$$Q_n^{(0)} = \frac{\omega_n^{(0)}}{2R_n^{(0)}} \frac{\partial Im\left\{Z_{in}^{EM}\left(\omega_n^{(0)}\right)\right\}}{\partial \omega} \cong \omega_n^{(0)} \frac{Im\left\{Z_{in}^{EM}\left(\omega_n^{(0)} - \Delta\omega\right)\right\} - Im\left\{Z_{in}^{EM}\left(\omega_n^{(0)} + \Delta\omega\right)\right\}}{4R_n^{(0)}\Delta\omega} \tag{4}$$

Therefore, the values of $L_n^{(0)}$ and $C_n^{(0)}$ result from their mutual relations, namely given by Equation (5):

$$L_n^{(0)} = \left(\frac{R_n^{(0)}}{Q_n^{(0)}}\right) C_n^{(0)} = \frac{R_n^{(0)}}{\omega_n^{(0)} Q_n^{(0)}} \tag{5}$$

Therefore, it is easy to show that the quasi-static inductance can be estimated as follows (Equation (6)):

$$L_0 = \frac{1}{\left(\omega_0^{(0)}\right)^2 C_0} \tag{6}$$

where $\omega_0^{(0)}$ is the lower frequency for which $\operatorname{Im}\left\{Z_{in}^{EM}\left(\omega_0^{(0)}\right)\right\}=0.$

Figure 1b displays the results of CST simulations of the reflection coefficient (S11), while Figure 1c represents the real and imaginary sections of the input impedance curves of the examined antenna. An antenna's equivalent circuit model may be derived from these curves, revealing its features at resonance. For example, in Figure 1b, each dip in the S11 curve might be interpreted as a different resonance frequency. The real and imaginary sections of the input impedance curve are about 50 and 0 Ohms, respectively, at these

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positions. That is to say, the factors considered are in agreement with resonant frequencies. Two such balance modes are found in the studied frequency range. As it turns out, a third-order circuit is presented as the basis for a lumped element model. Using resistors (R_i) , inductors (L_i) , and capacitors (C_i) , the suggested circuit model is a series of parallel RLC circuits. The actual component of the input impedance curve is used as a starting point for R_i (Equation (7)). The Formulas (8)–(11) are used to determine the starting values of the L_i and C_i components.

$$R_i = Real(Z_{in}(f_{ri})) \tag{7}$$

$$Q_i = \frac{f_{ri}}{BW_i} = 2\pi R_i C_i f_{ri} \tag{8}$$

$$BW_i = f_{hi} - f_{li} \tag{9}$$

$$C_i = \frac{Q_i}{2\pi f_{ri} R_i} \tag{10}$$

$$L_i = \frac{R_i^2 C_i}{Q_i^2} \tag{11}$$

In this expression, f_{ri} denotes the ith resonance frequency, Q_i denotes the ith quality factor, f_{hi} denotes the upper frequencies of the ith operating band, and f_{li} denotes the lower frequencies of the ith operating band. When a monopole antenna is operating at its lower frequency, its capacitance, C_0 , and inductance, L_0 , should be selected such that the antenna resonates at its initial resonant frequency. The final values of the lumped circuit components are determined by tuning the circuit elements to obtain the desired response. In Figure 2 is shown the equivalent circuit that was calculated using the S11 data.

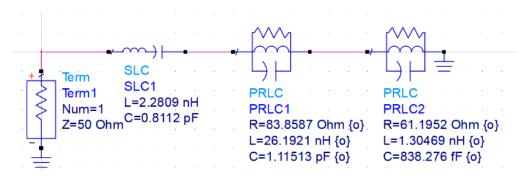


Figure 2. Antenna equivalent circuit based on impedance data.

To check the validity of the established model, the ADS software was used. The circuit model frequency responses are compared with CST simulations. The results are depicted in Figure 3a,b. Based on these results, it is seen that both graphs agree well with each other with a slight shifting.

2.2. Stage II: Equivalent Circuit Model via Vector-Fitting Approach

2.2.1. Vector-Fitting Approximation Principle

An antenna's total performance can be defined using a rational transfer function, allowing it to be coupled with other components in a communication system instead of being built as an isolated component. The first step is to approximate the simulated or measured frequency domain response data rationally. The acquired scattering and admittance parameters versus antenna frequency are estimated using the vector-fitting (VF) approach to rational functions. Vector fitting was first utilized in high-power transformers or electrical power distribution systems, but it was later adapted to higher frequencies, particularly microwaves. Furthermore, it is a robust algorithm able to convert frequency response data to rational functions via a collection of stable poles, ensuring the stability of

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the approximated rational function, and then enforcing the model's passivity. The rational approximation of a transfer function H(s) can be expressed as Equation (12):

$$H(s) = \sum_{n=1}^{N} \frac{r_n}{s - p_n} + d + es + hs^2 + \dots$$
 (12)

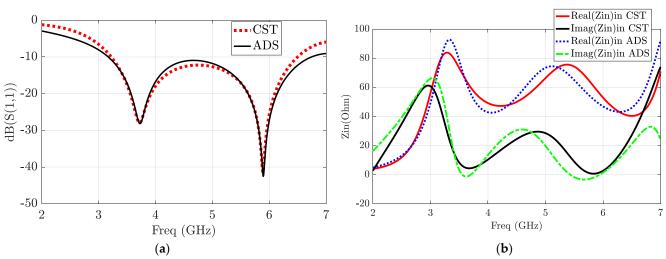


Figure 3. (a) Comparison of the SPICE equivalent circuit based on impedance and CST S11 results; (b) comparison of the resulting impedance from CST and equivalent circuit.

If the nonlinearity of Equation (12) is neglected; it can be approximated by the following Equation (13):

$$H(s) \approx \sum_{n=1}^{N} \frac{r_n}{s - p_n} + d + es \tag{13}$$

where $s = j\omega$ represents the frequency in the Laplace domain, r_k and p_k denote the kth residue and kth pole, which are either real quantities or complex conjugate pairs and are extracted by the fitting procedure. N presents the order of approximation and the number of poles. while d and e are real terms where d is a constant term, and e is a proportional term.

The vector-fitting method occasionally produces negative residues, resulting in negative element values. In reality, these negative aspects are unusable for design reasons and should be avoided at all costs. Even though these negative elements are not immediately visible, they can be used in modeling and simulation because they allow for accurate, comparable circuits. Furthermore, the negative aspects of the frequency analysis can be easily replicated. So far, extensive research has suggested a different structure, such as a cell with a positive value and a negative resistance. To eliminate nonphysical circuit components, even if the circuit's guaranteed stability and passivity are enforced, a different circuit representation of the complex poles was proposed in [17].

These new representations have demonstrated that a complex pole pair can be synthesized using RLC lumped elements and a single controlled source [18].

2.2.2. Antenna Modeling Using Vector Fitting

The antenna simulated admittance and impedance versus frequency are exported to Matlab using CST. The data-fitting process is carried out to the 8th order of approximation. It should be noted that the lower orders of approximation produce inaccurate results, and the higher orders of approximation bring a huge circuit.

Figure 4 depicts the approximated fitting rational function using vector fitting (FRVF) and the simulated Y and Z data using CST (data), respectively. It is found that the magnitude of approximated data and original simulated data are in good agreement. It is worth highlighting the vector-fitting algorithm used with passivity enforcement using the technique described in [35]. The previous results are used to generate two equivalent

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circuit models. Based on the given expressions in [17], the 8th order approximation of the simulated input impedance (Z data) produces four complex pole pairs, which means four parallel R-L-C-G cells connected in series, as reported in Figure 5. In contrast, the same order of the input admittance (Y data) approximation gives two real poles, one with a positive residue, the second with negative residue, and three complex poles pairs. The computed poles correspond to one series RL branch, a positive-valued series cell (RC) combined in parallel with a negative resistance, and three R-L-C-G cells, as illustrated in Figure 6. Figure 7 compares the plots of the obtained S-parameters from CST to those simulated by a SPICE equivalent circuit based on Z data and a SPICE equivalent circuit based on Y data. Figure 7 shows that the extracted models allow a satisfactory approximation of the studied antenna. Overall, these results indicate that the model generated using vector-fitting approximation, based on Z and Y data, reproduces perfect matching results in terms of S11 and input impedance/admittance.

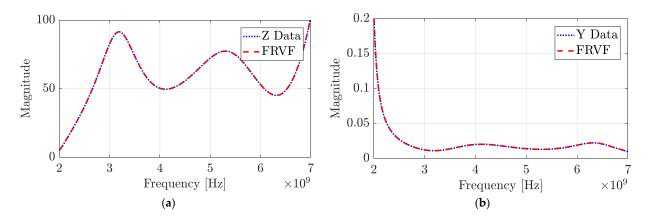


Figure 4. Comparison of the fitted rational vector function (FRVF) and simulated data (data): (a) impedance; (b) admittance.

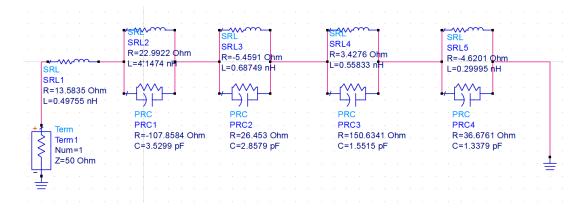


Figure 5. ADS model of the lumped equivalent circuit based on Z data.

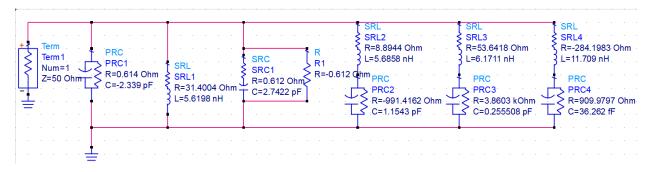


Figure 6. ADS model of the lumped equivalent circuit based on Y data.

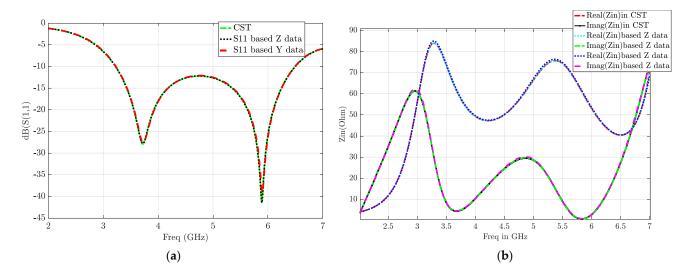


Figure 7. (a) S11 results from CST and SPICE equivalent circuit models comparison; (b) Zin results from CST and SPICE equivalent models comparison.

2.3. Equivalent Circuit Based on Antenna Geometry and Substrate Characteristics

The antenna geometry is a combination of a hexagonal patch and Cantor fractal slots of the second iteration. It is observed in Figure 8 that the hexagonal patch can be described as a corner truncated conventional rectangular patch. The equivalent circuit of the conventional patch is formed of resistance (R_p) , inductance (L_p) , and capacitance (C_p) , as described in Figure 8. Those lumped elements are calculated using the following Equations (14)–(17) [15].

$$Cp = \frac{\varepsilon_{eff}\varepsilon_0 L_p W_p}{2h} \cos^{-2} \left(\frac{\pi Y_0}{L_p}\right)$$
 (14)

$$Rp = \frac{Q_r}{2\pi f_0 C_n} \tag{15}$$

$$Q_r = \frac{c\sqrt{\varepsilon_{eff}}}{hf_0} \tag{16}$$

$$Rp = \frac{Q_r}{2\pi f_0 C_p} \tag{17}$$

where f_0 is the design frequency, ε_{eff} is the effective permittivity of the substrate, L_p and W_p are the patch length and width, respectively, the Y_0 feed point position along the patch length, in the case of the studied antenna, is feeding using an inset feed line, h is the substrate thickness, and c is the light velocity in free space.

The truncated corner effects are described by the capacitance given as Equation (18):

$$C = \frac{\varepsilon_0 \times \varepsilon_{eff} \times S}{h} \tag{18}$$

S is the surface of the truncated corners defined as Equation (19):

$$S = 2 \times Lt \times Wt \tag{19}$$

So, the hexagonal patch admittance can be written as Equation (20):

$$Yp = \frac{1}{Rp} + \frac{1}{j\omega Lp} + j\omega(Cp + C)$$
 (20)

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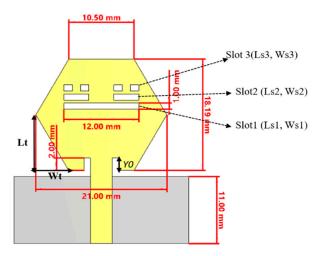


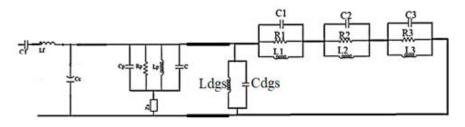
Figure 8. Studied antenna-radiating element.

The multifractal Cantor slots and the rectangular partial ground plane are described using a well-known and useful technique. In this technique, the slot is presented through a simple L-C resonator. Equation (21) describes the multifractal slots' admittance.

$$Ys = j\omega \left(\sum_{i=1}^{N} Ci - \frac{1}{\omega^2} \sum_{i=1}^{N} \frac{1}{Li} \right)$$
 (21)

In the antenna circuit model described in Figure 9, Lf and Cf represent the feed inductance and the antenna static capacitance, respectively. The impedance of the hexagonal patch is modelled by Zp. The Cantor multifractal slots are represented by L-C resonator cells marked Z_s , whereas Cc represents the mutual coupling among the radiating patch and the ground plane. The partial ground plane is modelled by L-C resonator as Zdgs. For further understanding, the antenna wideband impedance discontinuities (as described in Figure 1) are introduced in the equivalent circuit and represented by parallel RLC resonators. Using iterative techniques and curve fitting, the tuned values of circuit-lumped elements and the overall antenna equivalent model is shown in Figure 9b. The comparison of S11 response between CST simulation and the equivalent circuit simulation is shown in Figure 10. Based on these results, it can be observed that the computed equivalent circuit model almost perfectly matches the CST results.

To show the accuracy of the generated circuit models, the RMS error for between the antenna results and the results using the computed circuits are plotted in Figure 11. As clearly seen, the generated circuits using a vector-fitting approach allow a satisfactory approximation of the antenna behavior, and the RMS error on the magnitude is 1×10^{-6} within the operating bandwidth, whilst the circuits synthesized using the Foster approximation based on the antenna impedance data and based on antenna geometry show good accuracy. Consequently, the equivalent circuit model of the suggested design using the vector-fitting approach will be considered in the next study.



(a)

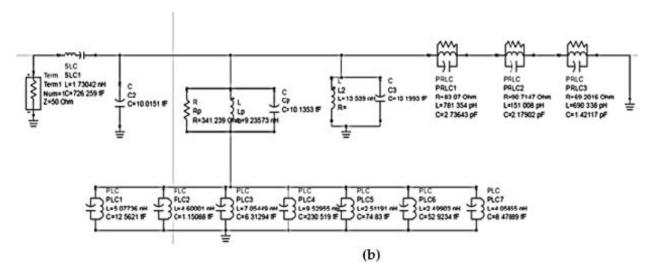


Figure 9. (a) Studied antenna simplified equivalent circuit model; (b) studied antenna equivalent circuit model computed under ADS.

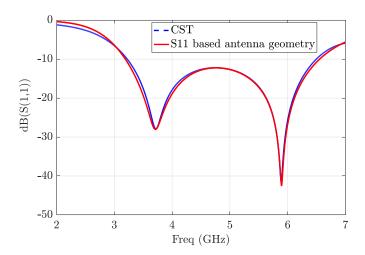


Figure 10. Comparative study of CST and computed equivalent circuit model results.

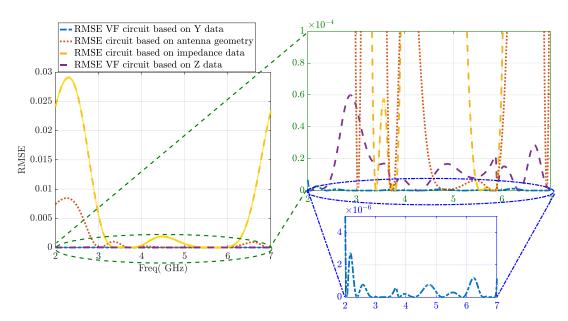


Figure 11. Comparative study of the RMSE of CST and computed equivalent circuit model results.

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2.4. Prototype, Measurement and Comparison

The prototype of the studied antenna and experimental setup using a Ceyear 3656D VNA are shown in Figure 12.

The comparison of the f S11 response between CST MWS simulation, the equivalent circuits simulations, and the d measurement result are shown in Figure 13. All the results are found in good correlation with each other. One can mention that the simulated results are in close contact with the practical results at the upper resonance frequency of 5.9 GHz, whereas there is a slight difference in S11 values at the lower resonance frequency.



Figure 12. (a) Studied antenna prototype; (b) the experimental setup.

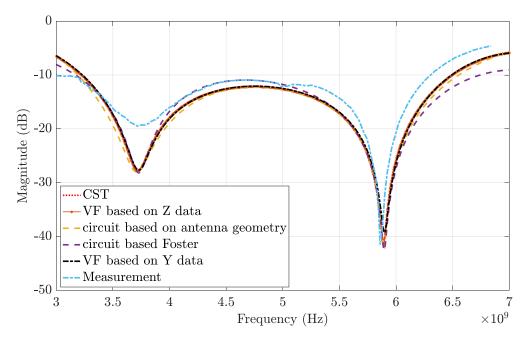


Figure 13. Comparative study of S11 response between CST simulation, equivalent circuits simulations, and measurement data.

3. Time-Domain Analysis Based on Equivalent Circuit

The pulse generation and shaping procedures are the most crucial tasks in wideband systems design. The pulse waveform determines the signals spectrum characteristic [36,37]. However, several techniques and approaches are discussed in the literature to generate a wideband pulse [36,39]. Different types of pulses can be used for wideband systems, antennas, and circuits. Interestingly, the Gaussian pulse and its derivatives are considered the main choices. The major purpose of this section is to establish the generation technique of the used pulse and the time-domain analysis.

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3.1. Pulse Generation Technique

The antenna used is of the ultra-wideband (UWB) kind, and it is true that a high performance in the frequency domain does not guarantee that the antenna will behave well in the time domain. Since this is the case, the seventh Gaussian derivative pulse (Figure 14a) is employed as the antenna excitation signal in CST to provide a desirable time-domain characteristic. Figure 14b shows the power spectral density (PSD) of a Gaussian pulse.

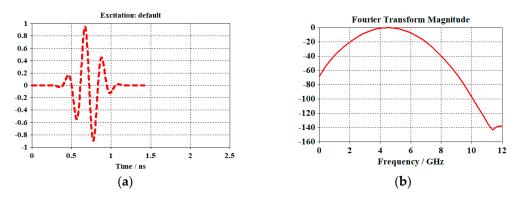


Figure 14. (a) The antenna input signal in CST; (b). antenna input signal spectrum.

The transistor properties, Schottky diode, and step recovery diode (SRD) are the primary areas of interest for the utilized pulse generator. These pulse generators are not the best option for simple and inexpensive designs because of their size.

The seventh Gaussian derivative pulse generation circuit shown in Figure 15, includes four parts: drive pulse production, SRD [40] pulse sharpening, second derivative pulse forming, and fifth-order derivative RLC. The driver circuit inverts the trigger signal to a driver pulse with high amplitude and sharp edges at its output terminal. Accordingly, the SRD pulse-shaping circuit based on SRD and Schottky diode generate a Gaussian pulse from the driver pulse by combining the negative reflected pulse toward the delay line with the other positive pulse in the terminal load. Then, a second Gaussian derivative pulse circuit forming is employed beside a backward decoupling circuit. This circuit is used to reduce the backward coupling effect and the resulting pulse's ringing level. Figure 16 describes the considered circuit.

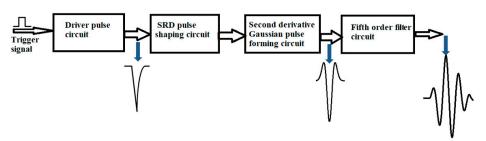


Figure 15. Block diagram of the seventh Gaussian derivative pulse generator.

A fifth-order derivative RLC illustrated in Figure 17 is employed to obtain the seventh Gaussian derivative pulse. Figure 18 shows the attained pulse.

3.2. Antenna Equivalent Circuit Output Results

To make comparisons, the waveform responses of the antenna connected to different loads are demonstrated. It is interesting to note that the pulse carries useful data. Hence, the output pulse is required to match the input pulse with minimum distortions.

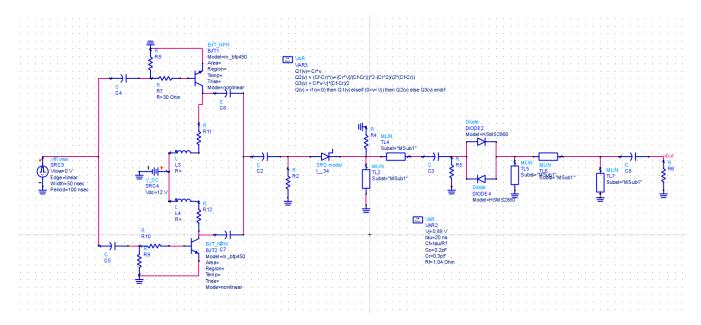


Figure 16. Second derivative Gaussian pulse circuit.

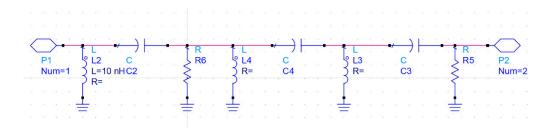


Figure 17. Fifth-order derivative circuit.

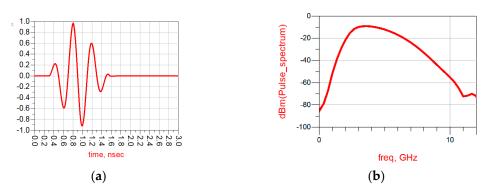


Figure 18. (a) Generated pulse, (b) its spectrum in ADS.

The input pulse is compared with the antenna output pulses. The output pulse waveforms are obtained by placing various loads in the terminal of the antenna equivalent circuit. From Figure 19a, it is found that the load of the free space (377 Ohms) has little effect on waveform distortion. The antenna presents good pulse-preserving capability and ensures the correspondence of the input and output waveforms signals after scaling and time shifting. While Figure 19b,c demonstrate that loads of 50 Ohms and 75 Ohms reveal more waveform distortions then more data loss.

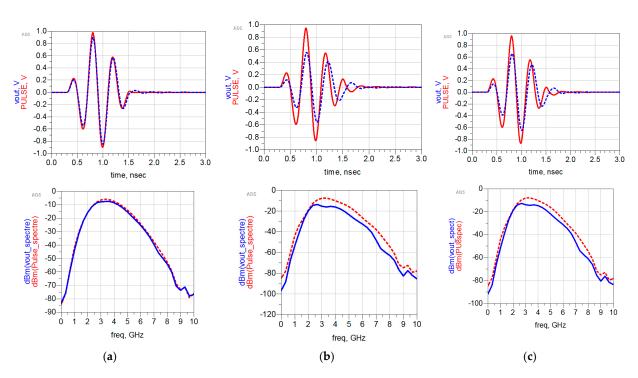


Figure 19. (a) The output voltage of the antenna equivalent circuit connected to 377 Ohm load; (b) the output voltage of the antenna equivalent circuit connected to a 50 Ohm load; (c) the output voltage of the antenna equivalent circuit connected to a 75 Ohm load.

To comprehend and appraise the antenna features objectively, each load's current and power are simulated and plotted versus time and frequency as depicted in Figure 20. Based on these results, it can be clearly seen that the current and power have the same waveforms without any distortions for the tree load, whereas the magnitude depends on the load value.

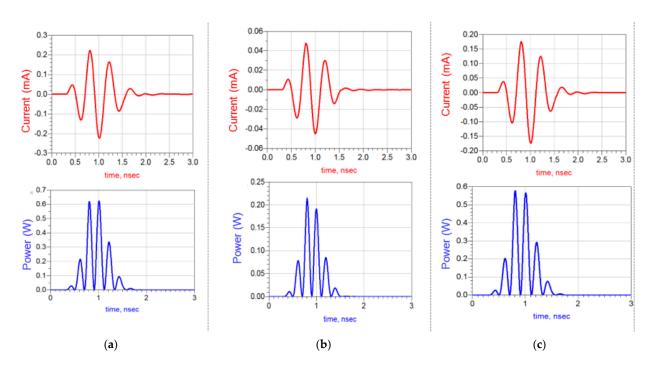


Figure 20. (a) The antenna equivalent circuit's current and power waveforms connected to a 50 Ohm load; (b) current and power of the antenna equivalent circuit connected to a 377 Ohm load; (c) current and power of the antenna equivalent circuit connected to 75 Ohm load.

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The output voltage pulse waveform for the different loads is distorted compared with the input pulse due to the antenna band rejection features. It can be clearly seen that the input and output pulses have similar waveforms with distortions. Then, an accurate time-domain feature can be attained using the free space load as a terminal of the antenna equivalent circuit; accordingly, there is less data loss.

4. Conclusions

This work aimed to propose and analyze several techniques and approaches for the formulating of lumped equivalent circuit model of a broadband fractal antenna. A Foster approximation approach was used to extract an equivalent circuit presented by parallel RLC cells connected in series. This method was based on scattering parameters of impedance/admittance data. The objective of the extracted equivalent circuits' models is to give more details about the impedance behavior in the studied band. Moreover, the vector-fitting approach applied rational function approximation of the antenna simulated impedance data. The equivalent circuit model was extracted from the fitted data. So far, an equivalent model was computed based on the antenna geometry in addition to the multifractal slots and the DGS effects. The obtained results proved that the simulated scattering parameters, impedance/admittance data of the antenna and those of the established equivalent circuits are matched perfectly. The seventh Gaussian derivative pulse was generated using two techniques for further comprehension of the antenna behavior. Then, the antenna equivalent circuit was excited, and a time-domain analysis was performed to check the validity of the antenna pulse response. Overall, these studies highlight that the investigated antenna equivalent circuit models are widely effective in understanding the antenna performance and predicting the effect of integrating antenna with the system. Then, the obtained models can be connected to linear/nonlinear devices or lumped elements in order to analyze electromagnetic circuit problems.

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