

## COEFFICIENT ESTIMATES OF NEW CLASSES OF $q$ -STARLIKE AND $q$ -CONVEX FUNCTIONS OF COMPLEX ORDER

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*Abstract.* We introduce new classes of  $q$ -starlike and  $q$ -convex functions of complex order involving the  $q$ -derivative operator defined in the open unit disc. Furthermore, we find estimates on the coefficients for second and third coefficients of these classes.

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