

## WORKING PAPERS

4 | 2012

### COHESION WITHIN THE EURO AREA AND THE U. S.: A WAVELET-BASED VIEW

António Rua  
Artur Silva Lopes

February 2012

---

The analyses, opinions and findings of these papers  
represent the views of the authors, they are not necessarily  
those of the Banco de Portugal or the Eurosystem

---

Please address correspondence to  
António Rua  
Banco de Portugal, Economics and Research Department  
Av. Almirante Reis 71, 1150-012 Lisboa, Portugal;  
Tel.: 351 21 313 0841, email: [aru@bportugal.pt](mailto:aru@bportugal.pt)



*Banco de Portugal*  
EUROSYSTEM

**BANCO DE PORTUGAL**

Av. Almirante Reis, 71

1150-012 Lisboa

[www.bportugal.pt](http://www.bportugal.pt)

***Edition***

Economics and Research Department

***Pre-press and Distribution***

Administrative Services Department

Documentation, Editing and Museum Division

Editing and Publishing Unit

***Printing***

Administrative Services Department

Logistics Division

Lisbon, February 2012

***Number of copies***

80

ISBN 978-989-678-118-7

ISSN 0870-0117 (print)

ISSN 2182-0422 (online)

Legal Deposit no. 3664/83

# Cohesion within the euro area and the U. S.: a wavelet-based view

António Rua\*      Artur Silva Lopes†

## Abstract

The assessment of synchronization of macroeconomic fluctuations across countries or regions has been crucial, for example, for the debate on economic integration. In this paper, we propose a multivariate measure of synchronization to assess cohesion across countries or regions by resorting to wavelet analysis. This wavelet-based measure of cohesion allows one to assess how synchronization has evolved over time and across frequencies simultaneously. In particular, we investigate the cohesion among euro area countries and the cohesion within the U.S. both at the regional and state levels over the last decades. In addition, an analysis at the sectoral level is also conducted. The results obtained unveil a noteworthy heterogeneity and highlight the usefulness of a wavelet-based measure of cohesion.

*Keywords:* Cohesion; Wavelets; Time-frequency; Output growth.

*JEL classification:* C40, E32.

---

\*Banco de Portugal and ISEG–Technical University of Lisbon. Address: Economic Research Department, Banco de Portugal, Av. Almirante Reis no 71, 1150-012 Lisboa, Portugal. Email: antonio.rua@bportugal.pt

†CEMAPRE & ISEG–Technical University of Lisbon.

# 1 Introduction

The analysis of business cycle comovement has long been a topic of interest in economics. Several measures have been used in the literature to assess the synchronization of business cycles but the Pearson correlation coefficient remained the most popular because it summarizes the degree of comovement through time in a single value. However, due to its synthetic nature it can be rather limited describing the relationship between the variables. Alternatively, one can resort to spectral analysis, to obtain further insights about the relationship at the frequency level (see, for example, A'Hearn and Woitek (2001), Pakko (2004) and Breitung and Candelon (2006)). Croux *et al.* (2001) have suggested a spectral-based measure, the dynamic correlation, which is conceptually similar to the contemporaneous correlation but allows to measure comovement at the frequency level (empirical work drawing on this measure includes, for example, Tripier (2002), Rua and Nunes (2005) and Camacho *et al.* (2006)). However, while the Pearson correlation coefficient disregards completely the relationship at the frequency level, with the dynamic correlation proposed by Croux *et al.* (2001) all the information on time dependence of comovement is lost.

To overcome such caveats, Rua (2010) has proposed a measure of comovement by resorting to wavelet analysis. Wavelet analysis constitutes a very promising tool as it represents a refinement in terms of analysis, in the sense that both time and frequency domains are taken into account. Although wavelets have been more popular in fields such as signal and image processing, meteorology, and physics, such analysis can also provide fruitful insights about several economic phenomena (see, for example, the pioneer work of Ramsey and Zhang (1996, 1997) and Ramsey and Lampart (1998a,b)). Recent applications of wavelets in economics can be found, for instance, in Gallegati and Gallegati (2007), Gallegati *et al.* (2008), Yogo (2008), Crowley and Mayes (2008), Rua and Nunes (2009) and Rua (2011, 2012) (see Crowley (2007) for a survey). In particular, the wavelet-based

measure of comovement suggested by Rua (2010) allows one to assess simultaneously how variables are related at different frequencies and how such relationship has evolved over time. Therefore, it is possible to capture both time and frequency varying features within an unified framework.

In order to take on board more than two series when assessing comovement, Croux *et al.* (2001) have extended the dynamic correlation to the multivariate case and named this generalised measure as cohesion. Cohesion is based on the dynamic correlations between all possible pairs of series within a group of variables and has been used by Croux *et al.* (2001) to assess the comovement of output fluctuations between European countries and across the U.S. states and regions. As stressed by de Haan *et al.* (2008), this measure provides a useful summary statistic on the degree of comovement across countries or regions while avoiding the problem of choosing a base country or region. Cohesion has also been applied by Carlino and De Fina (2004) to study the comovement in employment across the U.S. states and sectors, by Crone (2005) to evaluate the business cycle cohesion within U.S. regions, and *inter alia*, by Eickmeier and Breitung (2006) for assessing output growth and inflation cohesion between European countries.

The assessment of comovement among different countries or regions now involves a huge literature. In fact, the degree of synchronization of macroeconomic fluctuations across countries or regions plays a key role on the discussion about the attractiveness of economic integration. In this respect, the debate about the European monetary union has dominated the literature over the past decade.<sup>1</sup> In particular, building on the work of Mundell (1961) on Optimum Currency Areas, it has been argued that the cost of joining a monetary union will be low if countries have highly synchronized business cycles. However, it has also been pointed out that economic integration itself can affect the synchronization of macroeconomic fluctuations.<sup>2</sup>

---

<sup>1</sup>See, for example, de Haan *et al.* (2008) for a literature survey regarding business cycle synchronization in the euro area.

<sup>2</sup>For instance, Frankel and Rose (1998) claim that the removal of trade barriers induces

Hence, besides the frequency level perspective of comovement, capturing its time-varying dimension is also a worthwhile purpose.

Following Croux *et al.* (2001), we extend the bivariate measure proposed in Rua (2010) to the more general case in order to obtain a measure of cohesion in the wavelet domain. The resulting measure allows one to assess how cohesion has evolved over time and across frequencies simultaneously. Therefore, it can provide a detailed and rich picture, with additional insights in the time dimension. Focusing on output growth, we investigate the cohesion between euro area countries and the cohesion within the U.S. at both the regional and state levels over the last decades.

We find that cohesion within the euro area has been higher at the long-run and business cycle frequencies and that it has increased since the mid-90s across all frequencies. For the U.S. we find that cohesion is higher at the typical business cycle frequency range but seems to have decreased since the beginning of the 90's, and we note that this finding holds at both the regional and state levels. Moreover, we also find that U.S. cohesion is higher at the regional level than at the state level, both across frequencies and over time. In addition, besides taking into account the spatial perspective when assessing cohesion, we also conduct an analysis at the sectoral level. Resorting to disaggregated data by eleven sectors for the euro area countries and U.S. regions and states, we find a noteworthy heterogeneity in the results at the sectoral level. This analysis allows us also to unveil the sectors underlying the previously mentioned overall results.

The paper is organised as follows. In section 2 the main building blocks are discussed and the wavelet-based measure of cohesion is presented. In section 3 a data description is provided, while in section 4 the empirical

---

a higher symmetry of output fluctuations, while Rose (2000) provides evidence that a common currency results in more trade. In contrast, Krugman (1993) argues that a higher level of trade can lead to a higher economic specialization and less synchronized business cycles. See, for example, Kalemli-Ozcan *et al.* (2001) for an overview of the effects of economic integration on output fluctuations symmetry.

application is carried out for both the euro area and the U.S.. Finally, section 5 concludes.

## 2 Measuring cohesion in the wavelet domain

While the well-known Fourier transform decomposes the time series into infinite length sines and cosines (see, for example, Priestley (1981)), discarding all time-localization information, the wavelet transform uses local base functions that can be stretched and translated with a flexible resolution in both frequency and time. In particular, the wavelet transform decomposes a time series in terms of some elementary functions, the daughter wavelets or simply wavelets  $\psi_{\tau,s}(t)$ . These wavelets result from a mother wavelet  $\psi(t)$ , that can be expressed as function of the time position  $\tau$  (translation parameter) and the scale  $s$  (dilation parameter), which is related with the frequency, that is,

$$\psi_{\tau,s}(t) = \frac{1}{\sqrt{s}}\psi\left(\frac{t-\tau}{s}\right). \quad (1)$$

To be a mother wavelet  $\psi(t)$  must fulfil several conditions (see, for example, Percival and Walden (2000) for further discussion). The continuous wavelet transform of a time series  $x(t)$  with respect to  $\psi(t)$  is given by the following convolution

$$W_x(\tau, s) = \int_{-\infty}^{+\infty} x(t)\psi_{\tau,s}^*(t)dt = \frac{1}{\sqrt{s}} \int_{-\infty}^{+\infty} x(t)\psi^*\left(\frac{t-\tau}{s}\right) dt, \quad (2)$$

where \* denotes the complex conjugate.

The most commonly used mother wavelet is the Morlet wavelet, which can be simply defined as

$$\psi(t) = \pi^{-\frac{1}{4}}e^{i\omega_0 t}e^{-\frac{t^2}{2}}. \quad (3)$$

One can observe that the Morlet wavelet is a complex sine wave within a Gaussian envelope whereas  $\omega_0$  is the wavenumber. In practice,  $\omega_0$  is set to 6 as it provides a good balance between time and frequency localization (see, for example, Adisson (2002) for further details on the Morlet wavelet).

Given two time series  $x_i(t)$  and  $x_j(t)$ , with wavelet transforms  $W_{x_i}(\tau, s)$  and  $W_{x_j}(\tau, s)$ , one can define the cross-wavelet spectrum as  $W_{x_i x_j}(\tau, s) = W_{x_i}(\tau, s)W_{x_j}^*(\tau, s)$ . As the mother wavelet is in general complex, the cross-wavelet spectrum is also complex valued and it can be decomposed into real and imaginary parts. The measure proposed in Rua (2010) is given by

$$\rho_{x_i x_j}(\tau, s) = \frac{\Re(W_{x_i x_j}(\tau, s))}{\sqrt{|W_{x_i}(\tau, s)|^2 |W_{x_j}(\tau, s)|^2}}, \quad (4)$$

where  $\Re$  denotes the real part of the cross-wavelet spectrum. This wavelet-based measure  $\rho_{x_i x_j}(\tau, s)$  allows one to evaluate the degree of comovement in the time-frequency space and assess over which periods of time and over which frequencies is the comovement higher. Basically, it plays a role as a contemporaneous correlation coefficient around each moment in time and for each frequency. Since it provides information about the comovement not only at the frequency level but also over time, it can be seen as a generalisation of the dynamic correlation measure suggested by Croux *et al.* (2001).

In a similar fashion to Croux *et al.* (2001), who extended the dynamic correlation measure to the multivariate case, providing a measure of cohesion in the frequency domain, we extend the bivariate measure proposed by Rua (2010) to the more general case in order to obtain a measure of cohesion in the wavelet domain. In particular, cohesion is defined as the weighted average of the wavelet-based measure  $\rho_{x_i x_j}(\tau, s)$  between all possible pairs of series:



$$coh(\tau, s) = \frac{\sum_{i \neq j} \varpi_{ij} \rho_{x_i x_j}(\tau, s)}{\sum_{i \neq j} \varpi_{ij}}, \quad (5)$$

where  $\varpi_{ij}$  is the weight attached to the pair of series  $(i, j)$ . As the  $\rho_{x_i x_j}(\tau, s)$  range between  $-1$  and  $1$ , the wavelet-based cohesion also varies between  $-1$  and  $1$ . This measure allows one to quantify the extent of cohesion among several series at different frequencies and investigate if such global relationship has changed over time. Hence, it enables a richer analysis than the one which is possible with the cohesion measure suggested in Croux *et al.* (2001), which focus only at the frequency level. This is of particular importance as there is by now evidence that comovement can vary across frequencies as well as over time. Moreover, the suggested wavelet-based cohesion allows to capture both features within an unified framework.

### 3 Data

Regarding the United States, we considered data at the regional and state levels provided by the Bureau of Economic Analysis (BEA) of the U.S. Department of Commerce.<sup>3</sup> Annual real GDP by region and state is available from 1977 up to 2008. However, as nominal data is available from 1963, in order to cover a longer time span we resorted to the U.S. GDP deflator prior to 1977. The disaggregation of regional and state output by sectors is also provided by the BEA for the same sample periods, and again we used

---

<sup>3</sup>The 8 BEA regions are: New England, Mideast, Great Lakes, Plains, Southeast, Southwest, Rocky Mountain, Far West. The 51 BEA states are: Alabama, Alaska, Arizona, Arkansas, California, Colorado, Connecticut, Delaware, District of Columbia, Florida, Georgia, Hawaii, Idaho, Illinois, Indiana, Iowa, Kansas, Kentucky, Louisiana, Maine, Maryland, Massachusetts, Michigan, Minnesota, Mississippi, Missouri, Montana, Nebraska, Nevada, New Hampshire, New Jersey, New Mexico, New York, North Carolina, North Dakota, Ohio, Oklahoma, Oregon, Pennsylvania, Rhode Island, South Carolina, South Dakota, Tennessee, Texas, Utah, Vermont, Virginia, Washington, West Virginia, Wisconsin, Wyoming. See <http://www.bea.gov/regional>.

the U.S. corresponding deflator, so as to obtain volume series since 1963 and up to 2008. In order to ease the comparison between the U.S. and the euro area, we considered eleven sectors, namely: (1) Agriculture, hunting, forestry, and fishing; (2) Mining; (3) Manufacturing; (4) Utilities; (5) Construction; (6) Wholesale and retail trade; (7) Transport and storage; (8) Information; (9) Finance, insurance, real estate and rental and leasing; (10) Services including professional and business services, educational services, health care, social assistance, arts, entertainment, recreation, accommodation and food services and other services; (11) Government.

Concerning the euro area, we considered all the member countries as of 1 January 2001, namely, Austria, Belgium, Finland, France, Germany, Greece, Ireland, Italy, Luxembourg, Netherlands, Portugal and Spain. Data regarding annual real GDP has been collected from the European Commission AMECO database.<sup>4</sup> Concerning sectoral data for the euro area countries, we used the EU KLEMS database provided by the Groningen Growth and Development Centre (GGDC, which is financially supported by the European Commission).<sup>5</sup> As this data ranges from 1970 up to 2007, we updated it with the year 2008 resorting to the AMECO database.

The weights used in (5) correspond to the share of output of the pair  $(i, j)$  in the year 2000.<sup>6</sup> As usual, all series are taken in logs and first differenced.

## 4 Cohesion within euro area and the U.S.

### 4.1 Spatial cohesion

In this section we proceed into the computation of the suggested measure to assess the cohesion among euro area countries and the cohesion within

---

<sup>4</sup>See [http://ec.europa.eu/economy\\_finance/db\\_indicators/ameco](http://ec.europa.eu/economy_finance/db_indicators/ameco) .

<sup>5</sup>See <http://www.euklems.net> .

<sup>6</sup>As both the euro area and the U.S. data are released with 2000 as the base year, this year was selected to compute the weights. Nevertheless, the results are not sensitive to the chosen year.

the U.S. at both the regional and state levels. As three dimensions are involved, the wavelet-based cohesion is presented through a contour plot. The horizontal axis refers to time while the vertical axis refers to frequency. To ease interpretation, the frequency is converted to time units (years). The gray scale is for the wavelet-based cohesion, where increasing darkness corresponds to an increasing value and mimics the height in a surface plot. Hence, through the inspection of the graph one can identify both frequency bands (in the vertical axis) and time intervals (in the horizontal axis) where cohesion is larger and whether it has changed over time.<sup>7</sup>

In Figure 1 we present the wavelet-based measure of cohesion among euro area countries in terms of GDP growth. Several findings seem to be particularly relevant. First, one can observe that cohesion is typically larger at low frequencies, *i.e.*, for long-run dynamics, than in the remaining frequencies. Moreover, at low frequencies cohesion has increased in the late 70's and early 80's and has kept high thereafter. Concerning the standard business cycle frequency range — that is, fluctuations between two and eight years —, although cohesion has been lower than at low frequencies, it has also increased since the mid-90s. At high frequencies, that is, for the very short-run fluctuations, cohesion has always been weak with the exception of the latter part of the sample. Hence, cohesion within the euro area has been larger for the long-term and business cycle dynamics and it has increased for several frequencies since the mid-90s.<sup>8</sup>

Regarding the U.S., we compute the cohesion at both the regional and state levels (see Figures 2 and 3, respectively). Likewise as in the euro area case, cohesion is positive within the U.S. at both the regional and state levels (see also Carlino and DeFina (2004)). Comparing Figures 2 and 3, one can observe that the U.S. cohesion at the regional level is higher than

---

<sup>7</sup>All computations are done using Matlab and the codes are available from the authors upon request.

<sup>8</sup>All these findings are broadly in line with the results of Rua (2010), who considers only the major euro area countries and assesses all possible country pairs individually.

at the state level, whatever the frequency and/or the time period. This is in line with the results of Croux *et al.* (2001), who argue that this is due to the fact that by aggregating the states the idiosyncratic sources of variations are diminished. In contrast with the euro area, the frequency range where cohesion is higher in the US is at the business cycle frequency range. A noteworthy and distinct finding is that, while in the euro area cohesion seems to have increased, reflecting most probably the deepening of the process of European economic integration, in the U.S. there seems to be evidence of a decrease in cohesion since the beginning of the 90's. This holds both at the regional and state levels.

To shed more light on this latter issue as well as on all the previous results, in the next section we conduct a cohesion analysis at the sectoral level.

## 4.2 Cohesion at the sectoral level

Up to now the focus has been on assessing the spatial cohesion within the euro area and the U.S.. To complement and provide further insights about the previous results, we also investigate cohesion at the sectoral level. This analysis allows us to identify whether the above findings are broadly based or if they are being driven by any particular sector.

The results at the sectoral level for the euro area are reported in Figure 4. Each plot presents the cohesion among the euro area countries for a given sector. In general, sectors like Agriculture, Mining, Government and to a lesser extent, Utilities, Construction, Transport and storage present relatively weak cohesion across frequencies and over time. Contrasting with these, sectors such as Manufacturing, Wholesale and retail trade, and Information denote a relatively high cohesion at low frequencies, one which has increased throughout time. These sectors seem to be responsible for the time-varying behaviour discussed earlier of cohesion within the euro area at low frequencies. It is also interesting to note that the sector where cohesion

has been increasing over the last decade and across all frequencies is the sector related to Finance, insurance and real estate. This clearly reflects the financial integration that has been taking place in the euro area.

We now turn to the U.S. results (see Figures 5 and 6). As pointed out in the previous section, cohesion at the regional level is higher than at the state level and this finding seems to hold for all the sectors across all the frequencies and over time. Since the results at the regional and state levels are qualitatively similar, henceforth we focus on the results obtained at the state level. The sectors that present lower cohesion are Agriculture, Mining, Finance, insurance and real estate and Government. In sectors like Construction, Transport and storage and, to a lesser extent, Utilities, cohesion seems to be higher at business cycle frequencies, whereas in the Information sector cohesion is more marked at low frequencies. On the other hand, in Manufacturing, Wholesale and retail trade, and Services including professional and business services and others, where cohesion has been high at the business cycle frequency range, have recorded a decrease in the last years. Hence, these appear to be the main sectors behind the recent deterioration of cohesion within the U.S..

## 5 Conclusions

The assessment of output synchronization across countries or regions has been of key importance in several strands of the literature as, for example, in the discussion of economic integration. Though comovement is traditionally measured in the time domain resorting to the well-known Pearson correlation coefficient, there has been an increasing focus on frequency domain analysis. However, while the former approach ignores the relationship at the frequency level, the latter disregards the fact that comovement can change over time. To overcome such shortcomings one can resort to wavelet analysis. In particular, in this paper we propose a wavelet-based measure of cohesion which allows one to assess how synchronization has evolved over

time and across frequencies simultaneously, within a set of countries or regions.

To illustrate its empirical application we focus on the output growth synchronization within the euro area and the U.S.. We study cohesion among the euro area countries and within the U.S., both at the regional and state levels over the last decades. The results obtained highlight the usefulness of a wavelet-based measure of cohesion so as to uncover both frequency and time-varying features. We find that cohesion within the euro area has been higher at the long-run frequencies and that it has increased since the mid-90s across all frequencies. In contrast, cohesion within the U.S. is higher at the typical business cycle frequency range but seems to have decreased since the beginning of the 90's. These findings for the U.S. hold both at the regional and state levels. Furthermore, we find that the U.S. cohesion at the regional level is higher than at the state level across all frequencies and over the whole sample period. Additionally, we find a noteworthy heterogeneity in the results at the sectoral level. The sectors that seem to lie behind the overall results are identified.

## References

- [1] Adisson, P. (2002) "The illustrated wavelet transform handbook", The Institute of Physics, London.
- [2] A'Hearn, B. and Woitek, U. (2001) "More international evidence on the historical properties of business cycles", *Journal of Monetary Economics*, 47, 321-346.
- [3] Breitung, J. and Candelon, B. (2006) "Testing for short- and long-run causality: A frequency-domain approach", *Journal of Econometrics*, 132, 363-378.

- [4] Camacho, M., Perez-Quiros, G. and Saiz, L. (2006) “Are European business cycles close enough to be just one?”, *Journal of Economic Dynamics and Control*, 30, 1687-1706.
- [5] Carlino, G. and DeFina, R. (2004) “How strong is co-movement in employment over the business cycle? Evidence from state/sector data”, *Journal of Urban Economics*, 55, 298–315.
- [6] Crone, T. (2005) “An alternative definition of economic regions in the United States based on similarities in state business cycles”, *Review of Economics and Statistics*, 87, 617–626.
- [7] Croux, C., Forni, M. and Reichlin, L. (2001) “A measure of comovement for economic variables: theory and empirics”, *Review of Economics and Statistics*, 83, 232-241.
- [8] Crowley, P. (2007) “A guide to wavelets for economists”, *Journal of Economic Surveys*, 21, 207-264.
- [9] Crowley, P. and Mayes, D. (2008) “How Fused is the Euro Area Core? An Evaluation of Growth Cycle Co-movement and Synchronization Using Wavelet Analysis”, *Journal of Business Cycle Measurement and Analysis*, vol. 4, no. 1, 63-95.
- [10] de Haan, J., Inklaar, R. and Jong-A-Pin, R. (2008) “Will business cycles in the euro area converge: a critical survey of empirical research”, *Journal of Economic Surveys*, vol. 22, no. 2, 234–273.
- [11] Eickmeier, S. and Breitung, J. (2006) “How synchronized are new EU member states with the euro area? Evidence from a structural factor model” *Journal of Comparative Economics*, 34, 538-563.
- [12] Frankel, J. and Rose, A. (1998) “The endogeneity of the optimum currency area criterion”, *Economic Journal*, 108, 1009-1025.

- [13] Gallegati, M. and Gallegati, M. (2007) “Wavelet Variance Analysis of Output in G-7 Countries”, *Studies in Nonlinear Dynamics and Econometrics*, vol. 11, no. 3, Article 6.
- [14] Gallegati, M., Palestrini, A., and Petrin, M. (2008) “Cyclical behavior of prices in the G7 countries through wavelet analysis”, *Advances in Complex Systems*, vol. 11, 1, 119-130.
- [15] Kalemli-Ozcan, S., Sorensen, B. and Yosha, O. (2001) “Economic integration, industrial specialization and the asymmetry of macroeconomic fluctuations”, *Journal of International Economics*, 55, 107-137.
- [16] Krugman, P. (1993) “Lesson of Massachusetts for EMU” in Giavazzi, F. and Torres, F. (eds), *The Transition to Economic and Monetary Union in Europe*, Cambridge University Press, 241-261.
- [17] Mundell, R. (1961) “A theory of Optimum Currency Areas”, *American Economic Review*, 51, 657-665.
- [18] Pakko, M. (2004) “A spectral analysis of the cross-country consumption correlation puzzle”, *Economics Letters*, 84, 341-347.
- [19] Percival, D. and Walden, A. (2000) *Wavelet Methods for Time Series Analysis*, Cambridge University Press.
- [20] Priestley, M. B. (1981) *Spectral Analysis and Time Series*, vol. I and II, Academic Press, London.
- [21] Ramsey, J. and Zhang, Z. (1996) “The application of wave form dictionaries to stock market index data”, In: Kratsov, Y., Kadtko, J. (Eds.), *Predictability of complex dynamical systems*, Springer.
- [22] Ramsey, J. and Zhang, Z. (1997) “The analysis of foreign exchange data using waveform dictionaries”, *Journal of Empirical Finance* 4, 341-372.



- [23] Ramsey, J. and Lampart, C. (1998a) "Decomposition of economic relationships by time scale using wavelets", *Macroeconomic Dynamics* 2 (1), 49-71.
- [24] Ramsey, J. and Lampart, C. (1998b) "The decomposition of economic relationships by time scale using wavelets: expenditure and income", *Studies in Nonlinear Dynamics and Econometrics* 3 (1), 23-42.
- [25] Rose, A. (2000) "One money, one market: estimating the effect of common currencies on trade", *Economic Policy*, 30, 9-45.
- [26] Rua, A. (2010) "Measuring comovement in the time-frequency space", *Journal of Macroeconomics*, 32, 685-691.
- [27] Rua, A. (2011) "A wavelet approach for factor-augmented forecasting", *Journal of Forecasting*, 30, 666-678.
- [28] Rua, A. (2012) "Money growth and inflation in the euro area: a time-frequency view", *Oxford Bulletin of Economics and Statistics*, doi: 10.1111/j.1468-0084.2011.00680.x.
- [29] Rua, A., and Nunes, L.C. (2005) "Coincident and leading indicators for the euro area: A frequency band approach", *International Journal of Forecasting*, 21, 503-523.
- [30] Rua, A., and Nunes, L.C. (2009) "International comovement of stock market returns: A wavelet analysis", *Journal of Empirical Finance* 16, 632-639.
- [31] Tripier, F. (2002) "The Dynamic Correlation Between Growth and Unemployment", *Economics Bulletin*, vol. 5, no. 4, 1-9.
- [32] Yogo, M. (2008) "Measuring business cycles: A wavelet analysis of economic time series", *Economics Letters*, 100, 208-212.

Figure 1 - Cohesion within euro area

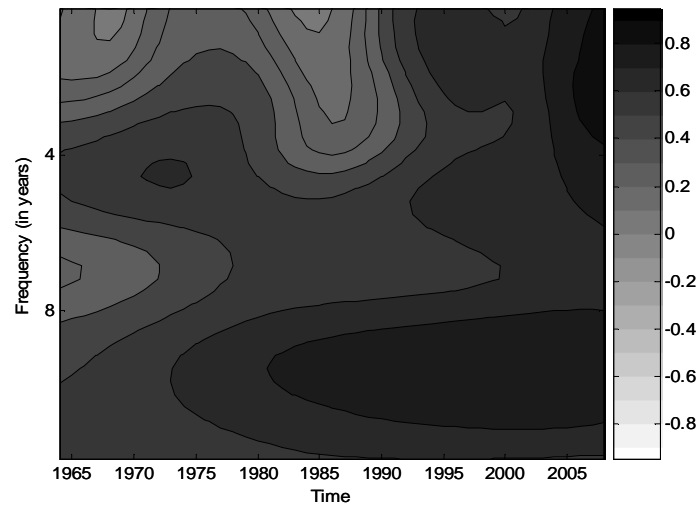


Figure 2 - Cohesion within US (at the regional level)

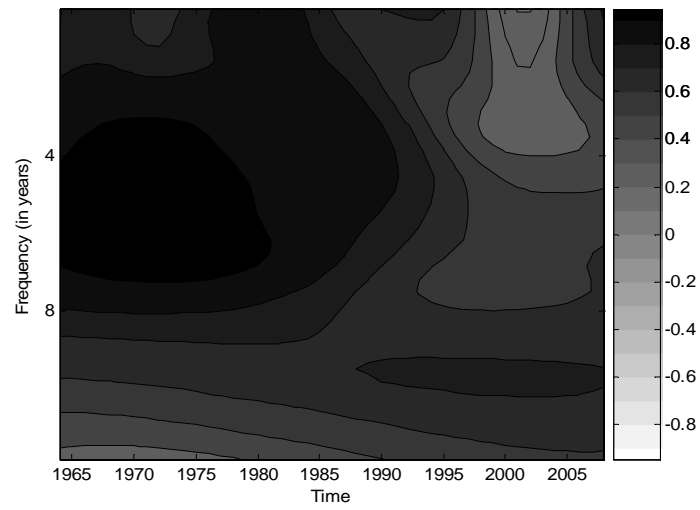


Figure 3 - Cohesion within US (at the state level)

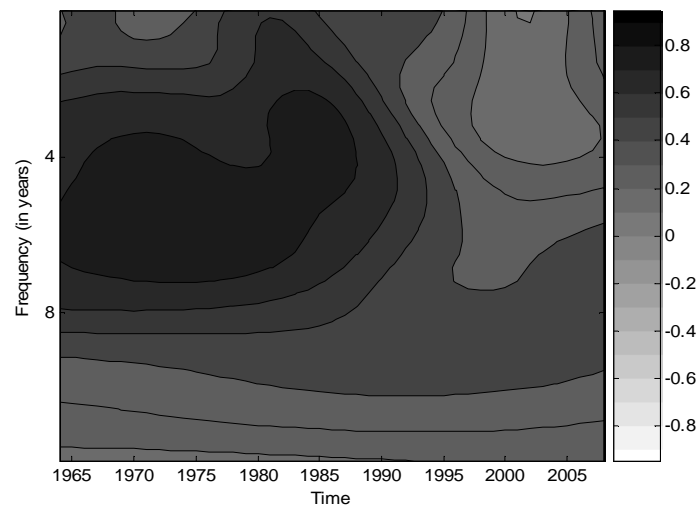


Figure 4 - Cohesion across euro area countries by sector

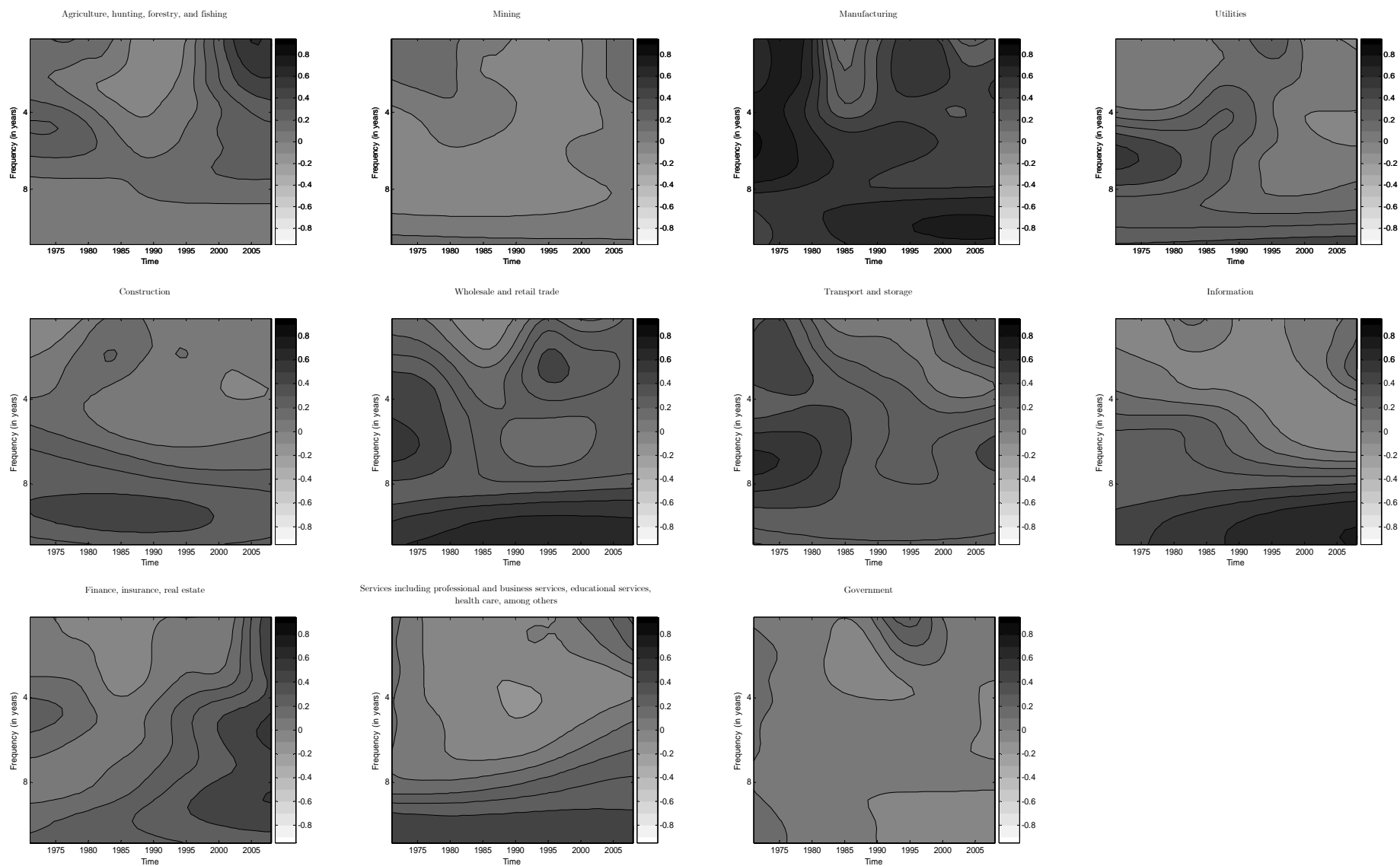


Figure 5 - Cohesion across US regions by sector

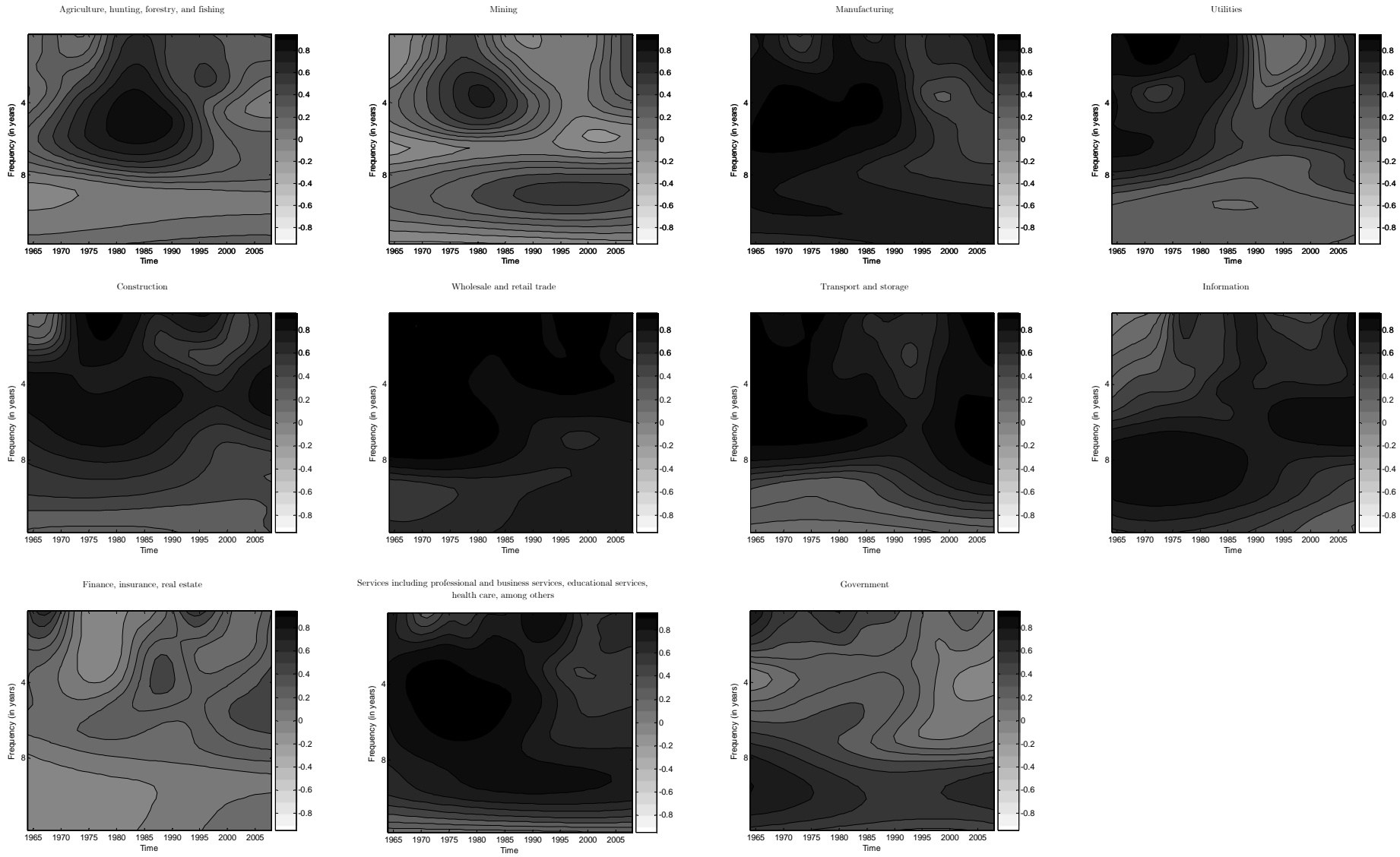
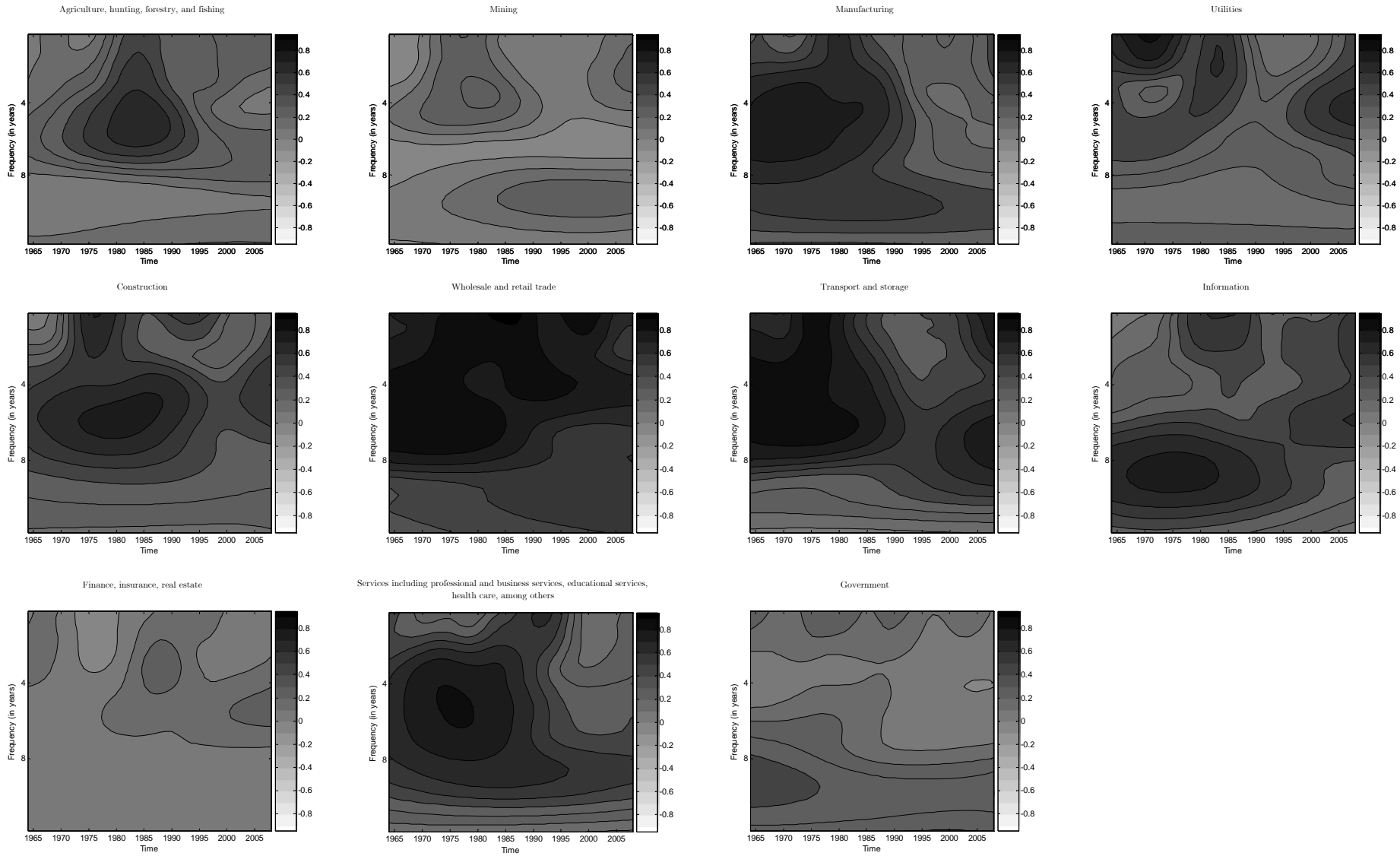


Figure 6 - Cohesion across US states by sector





## WORKING PAPERS

### 2010

- 1/10 MEASURING COMOVEMENT IN THE TIME-FREQUENCY SPACE  
— *António Rua*
- 2/10 EXPORTS, IMPORTS AND WAGES: EVIDENCE FROM MATCHED FIRM-WORKER-PRODUCT PANELS  
— *Pedro S. Martins, Luca David Opromolla*
- 3/10 NONSTATIONARY EXTREMES AND THE US BUSINESS CYCLE  
— *Miguel de Carvalho, K. Feridun Turkman, António Rua*
- 4/10 EXPECTATIONS-DRIVEN CYCLES IN THE HOUSING MARKET  
— *Luisa Lambertini, Caterina Mendicino, Maria Teresa Punzi*
- 5/10 COUNTERFACTUAL ANALYSIS OF BANK MERGERS  
— *Pedro P. Barros, Diana Bonfim, Moshe Kim, Nuno C. Martins*
- 6/10 THE EAGLE. A MODEL FOR POLICY ANALYSIS OF MACROECONOMIC INTERDEPENDENCE IN THE EURO AREA  
— *S. Gomes, P. Jacquinot, M. Pisani*
- 7/10 A WAVELET APPROACH FOR FACTOR-AUGMENTED FORECASTING  
— *António Rua*
- 8/10 EXTREMAL DEPENDENCE IN INTERNATIONAL OUTPUT GROWTH: TALES FROM THE TAILS  
— *Miguel de Carvalho, António Rua*
- 9/10 TRACKING THE US BUSINESS CYCLE WITH A SINGULAR SPECTRUM ANALYSIS  
— *Miguel de Carvalho, Paulo C. Rodrigues, António Rua*
- 10/10 A MULTIPLE CRITERIA FRAMEWORK TO EVALUATE BANK BRANCH POTENTIAL ATTRACTIVENESS  
— *Fernando A. F. Ferreira, Ronald W. Spahr, Sérgio P. Santos, Paulo M. M. Rodrigues*
- 11/10 THE EFFECTS OF ADDITIVE OUTLIERS AND MEASUREMENT ERRORS WHEN TESTING FOR STRUCTURAL BREAKS IN VARIANCE  
— *Paulo M. M. Rodrigues, Antonio Rubia*
- 12/10 CALENDAR EFFECTS IN DAILY ATM WITHDRAWALS  
— *Paulo Soares Esteves, Paulo M. M. Rodrigues*
- 13/10 MARGINAL DISTRIBUTIONS OF RANDOM VECTORS GENERATED BY AFFINE TRANSFORMATIONS OF INDEPENDENT TWO-PIECE NORMAL VARIABLES  
— *Maximiano Pinheiro*
- 14/10 MONETARY POLICY EFFECTS: EVIDENCE FROM THE PORTUGUESE FLOW OF FUNDS  
— *Isabel Marques Gameiro, João Sousa*
- 15/10 SHORT AND LONG INTEREST RATE TARGETS  
— *Bernardino Adão, Isabel Correia, Pedro Teles*
- 16/10 FISCAL STIMULUS IN A SMALL EURO AREA ECONOMY  
— *Vanda Almeida, Gabriela Castro, Ricardo Mourinho Félix, José Francisco Maria*
- 17/10 FISCAL INSTITUTIONS AND PUBLIC SPENDING VOLATILITY IN EUROPE  
— *Bruno Albuquerque*

- 18/10 GLOBAL POLICY AT THE ZERO LOWER BOUND IN A LARGE-SCALE DSGE MODEL  
— *S. Gomes, P. Jacquinot, R. Mestre, J. Sousa*
- 19/10 LABOR IMMOBILITY AND THE TRANSMISSION MECHANISM OF MONETARY POLICY IN A MONETARY UNION  
— *Bernardino Adão, Isabel Correia*
- 20/10 TAXATION AND GLOBALIZATION  
— *Isabel Correia*
- 21/10 TIME-VARYING FISCAL POLICY IN THE U.S.  
— *Manuel Coutinho Pereira, Artur Silva Lopes*
- 22/10 DETERMINANTS OF SOVEREIGN BOND YIELD SPREADS IN THE EURO AREA IN THE CONTEXT OF THE ECONOMIC AND FINANCIAL CRISIS  
— *Luciana Barbosa, Sónia Costa*
- 23/10 FISCAL STIMULUS AND EXIT STRATEGIES IN A SMALL EURO AREA ECONOMY  
— *Vanda Almeida, Gabriela Castro, Ricardo Mourinho Félix, José Francisco Maria*
- 24/10 FORECASTING INFLATION (AND THE BUSINESS CYCLE?) WITH MONETARY AGGREGATES  
— *João Valle e Azevedo, Ana Pereira*
- 25/10 THE SOURCES OF WAGE VARIATION: AN ANALYSIS USING MATCHED EMPLOYER-EMPLOYEE DATA  
— *Sónia Torres, Pedro Portugal, John T. Addison, Paulo Guimarães*
- 26/10 THE RESERVATION WAGE UNEMPLOYMENT DURATION NEXUS  
— *John T. Addison, José A. F. Machado, Pedro Portugal*
- 27/10 BORROWING PATTERNS, BANKRUPTCY AND VOLUNTARY LIQUIDATION  
— *José Mata, António Antunes, Pedro Portugal*
- 28/10 THE INSTABILITY OF JOINT VENTURES: LEARNING FROM OTHERS OR LEARNING TO WORK WITH OTHERS  
— *José Mata, Pedro Portugal*
- 29/10 THE HIDDEN SIDE OF TEMPORARY EMPLOYMENT: FIXED-TERM CONTRACTS AS A SCREENING DEVICE  
— *Pedro Portugal, José Varejão*
- 30/10 TESTING FOR PERSISTENCE CHANGE IN FRACTIONALLY INTEGRATED MODELS: AN APPLICATION TO WORLD INFLATION RATES  
— *Luis F. Martins, Paulo M. M. Rodrigues*
- 31/10 EMPLOYMENT AND WAGES OF IMMIGRANTS IN PORTUGAL  
— *Sónia Cabral, Cláudia Duarte*
- 32/10 EVALUATING THE STRENGTH OF IDENTIFICATION IN DSGE MODELS. AN A PRIORI APPROACH  
— *Nikolay Iskrev*
- 33/10 JOBLESSNESS  
— *José A. F. Machado, Pedro Portugal, Pedro S. Raposo*
- 2011**
- 1/11 WHAT HAPPENS AFTER DEFAULT? STYLIZED FACTS ON ACCESS TO CREDIT  
— *Diana Bonfim, Daniel A. Dias, Christine Richmond*
- 2/11 IS THE WORLD SPINNING FASTER? ASSESSING THE DYNAMICS OF EXPORT SPECIALIZATION  
— *João Amador*



- 3/11 UNCONVENTIONAL FISCAL POLICY AT THE ZERO BOUND  
— *Isabel Correia, Emmanuel Farhi, Juan Pablo Nicolini, Pedro Teles*
- 4/11 MANAGERS' MOBILITY, TRADE STATUS, AND WAGES  
— *Giordano Mion, Luca David Opromolla*
- 5/11 FISCAL CONSOLIDATION IN A SMALL EURO AREA ECONOMY  
— *Vanda Almeida, Gabriela Castro, Ricardo Mourinho Félix, José Francisco Maria*
- 6/11 CHOOSING BETWEEN TIME AND STATE DEPENDENCE: MICRO EVIDENCE ON FIRMS' PRICE-REVIEWING STRATEGIES  
— *Daniel A. Dias, Carlos Robalo Marques, Fernando Martins*
- 7/11 WHY ARE SOME PRICES STICKIER THAN OTHERS? FIRM-DATA EVIDENCE ON PRICE ADJUSTMENT LAGS  
— *Daniel A. Dias, Carlos Robalo Marques, Fernando Martins, J. M. C. Santos Silva*
- 8/11 LEANING AGAINST BOOM-BUST CYCLES IN CREDIT AND HOUSING PRICES  
— *Luisa Lambertini, Caterina Mendicino, Maria Teresa Punzi*
- 9/11 PRICE AND WAGE SETTING IN PORTUGAL LEARNING BY ASKING  
— *Fernando Martins*
- 10/11 ENERGY CONTENT IN MANUFACTURING EXPORTS: A CROSS-COUNTRY ANALYSIS  
— *João Amador*
- 11/11 ASSESSING MONETARY POLICY IN THE EURO AREA: A FACTOR-AUGMENTED VAR APPROACH  
— *Rita Soares*
- 12/11 DETERMINANTS OF THE EONIA SPREAD AND THE FINANCIAL CRISIS  
— *Carla Soares, Paulo M. M. Rodrigues*
- 13/11 STRUCTURAL REFORMS AND MACROECONOMIC PERFORMANCE IN THE EURO AREA COUNTRIES: A MODEL-BASED ASSESSMENT  
— *S. Gomes, P. Jacquinot, M. Mohr, M. Pisani*
- 14/11 RATIONAL VS. PROFESSIONAL FORECASTS  
— *João Valle e Azevedo, João Tovar Jalles*
- 15/11 ON THE AMPLIFICATION ROLE OF COLLATERAL CONSTRAINTS  
— *Caterina Mendicino*
- 16/11 MOMENT CONDITIONS MODEL AVERAGING WITH AN APPLICATION TO A FORWARD-LOOKING MONETARY POLICY REACTION FUNCTION  
— *Luis F. Martins*
- 17/11 BANKS' CORPORATE CONTROL AND RELATIONSHIP LENDING: EVIDENCE FROM RETAIL LOANS  
— *Paula Antão, Miguel A. Ferreira, Ana Lacerda*
- 18/11 MONEY IS AN EXPERIENCE GOOD: COMPETITION AND TRUST IN THE PRIVATE PROVISION OF MONEY  
— *Ramon Marimon, Juan Pablo Nicolini, Pedro Teles*
- 19/11 ASSET RETURNS UNDER MODEL UNCERTAINTY: EVIDENCE FROM THE EURO AREA, THE U.K. AND THE U.S.  
— *João Sousa, Ricardo M. Sousa*
- 20/11 INTERNATIONAL ORGANISATIONS' VS. PRIVATE ANALYSTS' FORECASTS: AN EVALUATION  
— *Ildeberta Abreu*
- 21/11 HOUSING MARKET DYNAMICS: ANY NEWS?  
— *Sandra Gomes, Caterina Mendicino*

- 22/11 MONEY GROWTH AND INFLATION IN THE EURO AREA: A TIME-FREQUENCY VIEW  
— *António Rua*
- 23/11 WHY EX(IM)PORTERS PAY MORE: EVIDENCE FROM MATCHED FIRM-WORKER PANELS  
— *Pedro S. Martins, Luca David Opromolla*
- 24/11 THE IMPACT OF PERSISTENT CYCLES ON ZERO FREQUENCY UNIT ROOT TESTS  
— *Tomás del Barrio Castro, Paulo M.M. Rodrigues, A.M. Robert Taylor*
- 25/11 THE TIP OF THE ICEBERG: A QUANTITATIVE FRAMEWORK FOR ESTIMATING TRADE COSTS  
— *Alfonso Irarrazabal, Andreas Moxnes, Luca David Opromolla*
- 26/11 A CLASS OF ROBUST TESTS IN AUGMENTED PREDICTIVE REGRESSIONS  
— *Paulo M.M. Rodrigues, Antonio Rubia*
- 27/11 THE PRICE ELASTICITY OF EXTERNAL DEMAND: HOW DOES PORTUGAL COMPARE WITH OTHER EURO AREA COUNTRIES?  
— *Sónia Cabral, Cristina Manteu*
- 28/11 MODELING AND FORECASTING INTERVAL TIME SERIES WITH THRESHOLD MODELS: AN APPLICATION TO S&P500 INDEX RETURNS  
— *Paulo M. M. Rodrigues, Nazarii Salish*
- 29/11 DIRECT VS BOTTOM-UP APPROACH WHEN FORECASTING GDP: RECONCILING LITERATURE RESULTS WITH INSTITUTIONAL PRACTICE  
— *Paulo Soares Esteves*
- 30/11 A MARKET-BASED APPROACH TO SECTOR RISK DETERMINANTS AND TRANSMISSION IN THE EURO AREA  
— *Martín Saldías*
- 31/11 EVALUATING RETAIL BANKING QUALITY SERVICE AND CONVENIENCE WITH MCDA TECHNIQUES: A CASE STUDY AT THE BANK BRANCH LEVEL  
— *Fernando A. F. Ferreira, Sérgio P. Santos, Paulo M. M. Rodrigues, Ronald W. Spahr*

## **2012**

- 1/12 PUBLIC-PRIVATE WAGE GAPS IN THE PERIOD PRIOR TO THE ADOPTION OF THE EURO: AN APPLICATION BASED ON LONGITUDINAL DATA  
— *Maria Manuel Campos, Mário Centeno*
- 2/12 ASSET PRICING WITH A BANK RISK FACTOR  
— *João Pedro Pereira, António Rua*
- 3/12 A WAVELET-BASED ASSESSMENT OF MARKET RISK: THE EMERGING MARKETS CASE  
— *António Rua, Luis C. Nunes*
- 4/12 COHESION WITHIN THE EURO AREA AND THE U. S.: A WAVELET-BASED VIEW  
— *António Rua, Artur Silva Lopes*