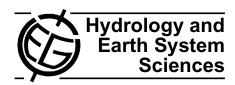
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Combining semi-distributed process-based and data-driven models in flow simulation: a case study of the Meuse river basin

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Abstract. One of the challenges in river flow simulation modelling is increasing the accuracy of forecasts. This paper explores the complementary use of data-driven models, e.g. artificial neural networks (ANN) to improve the flow simulation accuracy of a semi-distributed process-based model. The IHMS-HBV model of the Meuse river basin is used in this research. Two schemes are tested. The first one explores the replacement of sub-basin models by data-driven models. The second scheme is based on the replacement of the Muskingum-Cunge routing model, which integrates the multiple sub-basin models, by an ANN. The results show that: (1) after a step-wise spatial replacement of sub-basin conceptual models by ANNs it is possible to increase the accuracy of the overall basin model; (2) there are time periods when low and high flow conditions are better represented by ANNs; and (3) the improvement in terms of RMSE obtained by using ANN for routing is greater than that when using sub-basin replacements. It can be concluded that the presented two schemes can improve the performance of processbased models in the context of flow forecasting.

1 Introduction

It is a common practice to use semi-distributed conceptual models in operational forecasting for meso-scale catchments. These models are based on the principle of mass conserva-



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tion and simplified forms of energy conservation. Inaccurate precipitation data and the need for its averaging for the subbasin models may seriously influence the accuracy of modelling. Due to the limited representation of the full rainfall-runoff process, the complexity of the model integration and the identification of the lumped parameters, the proponents of fully distributed detailed models argue that there are many situations when the accuracy of conceptual models is not sufficient. However, the simplicity of these models and the high processing speed is an advantage for real time operational systems and often makes such models the first choice.

Precipitation forecasts are normally available for low resolution grids which are close to the size of the modelled subbasins. It has been shown that there are situations when such models are more accurate than the fully spatially distributed physically based and energy based models (Seibert, 1997; Linde et al., 2007).

An alternative approach to flow forecasting is using data-driven models (DDM). The most common DDMs used in hydrological forecasting are artificial neural networks (ANN) (ASCE, 2000; Brath et al., 2002; Toth and Brath, 2007), but other types of models, for example M5 model trees (Solomatine and Dulal, 2003) or support vector machines (Dibike et al., 2001) are used as well. Traditionally, modellers build a general model that covers all the processes of the natural phenomenon studied (overall model). Hydrological forecasting data-driven models are not exceptions in this sense: they tend to be developed on the basis of using a comprehensive overall model that covers all the processes in a basin (ASCE, 2000; Dibike and Abbott, 1999; Abrahart and See, 2002; Dawson et al., 2005). However, such models do not encapsulate much

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of the knowledge that experts may have about the system, and in some cases suffer from low extrapolation capacity (generalization capability). In many applications of data-driven models, the hydrological knowledge is "supplied" to the model via a proper analysis of the input/output structure and the choice of the adequate input variables (Solomatine and Dulal, 2003; Bowden et al., 2005). These models are less sensitive to precipitation and temperature information in hydrological systems where high autocorrelation is found in stream flows. Therefore, in operational systems where missing data is an issue, such models can replace local sub-basin models.

An important component on the semi-distributed hydrological model is the routing scheme, which integrates the sub-basin model discharges. The Muskingum-Cunge has for many years been successfully applied in flood modelling and prediction (NERC, 1975; Ponce et al., 1996). In this study, a river routing model based on the Muskingum-Cunge method is replaced by an ANN model that integrates the results of the different sub-basin models.

The approaches presented in this paper follow the general framework of integrating hydrological concepts and data-driven models using modular models that is being developed in our recent publications (Corzo and Solomatine, 2007a,b; Fenicia et al., 2007; Solomatine and Price, 2004) and has been also explored by Toth (2009); Abrahart and See (2002).

Finding adequate combinations of the mentioned model types (conceptual models and DDMs) is a relatively new area of research and has been studied only in recent years. Anctil and Tapé (2004) presented a successful combination of conceptual models where the information from the time series of soil moisture is fed into a neural network model. Their study concentrated on using the daily time series for flow forecasting purposes. However in the same study, the problems of using potential evapotranspiration and antecedent precipitation index as input to the ANN models are reported. The work presented by Nilsson et al. (2006) shows that not only information about soil moisture but also about snow accumulation may bring improvement to the ANN modelling process. Their results were based on monthly data with the purpose of having more accurate forecasts for power production, dam safety and water supply. Although in both papers integration of models is employed, none of them use all the information from the conceptual model. Basin sizes considered in these studies were not more than 1400 km².

Chen and Adams (2006) used ANN to link the sub-basin models. The basin area was around 8500 km², with a division into three sub-basins based mainly on the river network system. The calibration process included two stages: first, the whole catchment was considered (no sub-basin discharge information was available), and, second, the output discharges from the basins to the outlet were used as well. This approach is similar to the one presented in the present paper, but we considered a more complex basin, compared the model with the ANN routing integrator with a full basin hybrid model in-

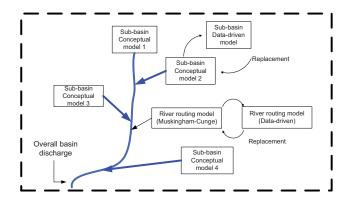


Fig. 1. Replacement of sub-basin models by ANN models.

volving ANN submodels, and performed additional analysis of the variations of the models seasonal performance (Fig. 1).

The objectives of this paper are: (i) to analyse the performance of DDMs in their role as sub-basin replacements for overall flow simulations; (ii) to explore the use of an ANN routing model for the integration of sub-basin models; (iii) draw conclusions about the applicability of the hybrid process-based and data-driven models in operational flow forecasting.

2 HBV-M model for Meuse river basin

The conceptual hydrological model HBV was developed in the early 1970s (Bergström and Forsman, 1973) and its versions have been applied to many catchments around the world (Lindström et al., 1997). HBV describes the most important runoff generating processes with simple and robust procedures. In the snow routine, snow accumulation and melt are determined using a degree temperature-index method. The soil routine divides the forcing by rainfall and meltwater, into runoff generation and soil storage for later evaporation. The runoff generation routine consists of one upper non-linear reservoir representing fast and intermediate runoff components, and one lower linear reservoir representing base flow. Runoff routing processes are simulated using a simplified Muskingum approach and/or a triangular equilateral transfer function (Ponce et al., 1996).

HBV is a semi-distributed model and the river basin can be subdivided into sub-basins (HBV-S). This model simulates the rainfall-runoff processes for each sub-basin separately with a daily or hourly time step. Each sub-basin is divided into homogenous elevations which are then divided into vegetation zones. Further details about the HBV model can be found in Lindström et al. (1997) and Fogelberg et al. (2004).

The HBV-S sub-basin models are linked by a Muskingum-Cunge equation. This routing equation is conventionally applied to river reaches where the distance between the outlets of the basins is significant. The Eq. (1) was used in this study.

$$Q_{n+1} = C_0 I_{n+1} + C_1 I_n + C_2 Q_n \tag{1}$$

$$C_0 = \left(\frac{K_x - 0.5\Delta t}{K - K_x + 0.5\Delta t}\right) \tag{2}$$

$$C_1 = \left(\frac{K_x + 0.5\Delta t}{K - K_x + 0.5\Delta t}\right) \tag{3}$$

$$C_2 = \left(\frac{K - K_x - 0.5\Delta t}{K - K_x + 0.5\Delta t}\right) \tag{4}$$

where, K is a storage factor with units of time, and Δt is the time interval considered in the simulation. The value of x represents the position on the river channel in meters. I_n and I_{n+1} are the inputs to the channel at the beginning and the end of the period Δt , respectively.

Diermansen (2001) presented an analysis of spatial heterogeneity in the runoff response of large and small river basins, and an increase of error is observed with an increase of the number of spatial details in the model. An alternative to fully-distributed models is the class of intermediate models, the so-called semi-distributed conceptual models, as the most appropriate modelling approach for meso-scale operational forecasting. In this research the IHMS-HBV model (Lindström et al., 1997) belonging to this class is used (http://www.smhi.se). In this paper it will be called simply HBV, and will refer to the initial hydrological model formulation used as a hydrological prototype module in the flood early warning system for the rivers Rhine and Meuse.

Ashagrie et al. (2006) presented a long term analysis for the effects of climate change and land use change on the Meuse river basin using the HBV model. This analysis showed that the agreement between the observed and measured discharge is generally good, in particular flood volumes and the highest peak are simulated well. However, there are some problems with the medium flow (shape and peak values), and a systematic deviation for certain observed periods (i.e. 1930–1960) was also observed. de Wit et al. (2007b) explored the impact of climate change on low-flows. They found high accuracy for the monthly average discharge and for the highest (January) and lowest discharge (August), but there was an overestimation and underestimation observed in spring and autumn, respectively. To improve the model performance, various calibration techniques have been tried, e.g. Booij (2005) presented the manual calibration and validation of the HBV based on expert tuning of model parameters. The problems mentioned above still remain unresolved and under investigation by a number of authors.



Fig. 2. The Meuse River basin and the sub-basins divisions upstream of Borgharen. The arrows represent the regions for which HBV-S model were replaced by ANNs (Scheme 2).

2.1 Characterisation of the Meuse River basin

The Meuse River originates in France, flows through Belgium and The Netherlands, and finally drains into the North Sea (Fig. 2). The river basin has an area of about 33 000 km² and covers parts of France, Luxembourg, Belgium, Germany and The Netherlands. The length of the river from its source in France to the North Sea at the Hollands Diep (an estuary of the Rhine and Meuse rivers) is about 900 km. Major tributaries of the Meuse are the Chiers, Semois, Lesse, Sambre, Ourthe, Amblève, Vesdre and Roer. The hydrological model of the Meuse basin upstream of Borgharen is subdivided into 15 sub-basins, covering an area of 21 000 km² (Fig. 2). For more detailed information about catchment geological and hydrological properties see Berger (1992) and de Wit et al. (2007a).

In general terms the land use in the basin is made up of 34% arable land, 20% pasture, 35% forest and 9% built up areas. Tu et al. (2004) found the coverage of forest and agricultural land relatively stable over the last ten years, but the forest type and management practices have changed significantly. In addition to this it seems that intensification and upscaling of agricultural practices and urbanization are the most important land changes in the last century.

As far as the hydrologic properties are concerned the Meuse can roughly be split into three parts (Berger, 1992):

1. The upper reaches (Meuse Lorraine), from the Lorraine sud to the mouth of the Chiers. Here the catchment is lengthy and narrow, the gradient is small and the major

bed is wide. Because of that the discharge up to the mouth of the Chiers has a comparatively calm course.

- 2. The central reaches of the Meuse (Meuse Ardennaise), leading from the Chiers to the Dutch border near Eijsden. In that section the main tributaries are Viroin, Semois, Lesse, Sambre and Ourthe. Here the Meuse transects rocky stone, resulting in a narrow river and a great slope. The poor permeability of the catchment and the steep slope of the Meuse and most of the tributaries contribute to a fast discharge of the precipitation. The contribution of the area to flood waves is great, the contribution to low flows is small.
- 3. The lower reaches of the Meuse, corresponding to the Dutch section of the river. The lower reaches themselves may again be split into the stretches from Eijsden to Maasbracht and from Maasbracht to the mouth. In the former part the slope is still relatively high. For the greater part the river has no weirs here. In the section the Meuse has no dikes. For those reasons the stretch above Maasbracht is occasionally reckoned as part of the Meuse Ardennaise, which in that case flows from Sedan to Maasbracht. It may be remarked that the stretch that forms the border with Belgium is called the Grensmaas (Border Meuse) in the Netherlands, and Gemeenschappelijke Maas (Common Meuse) in Flanders.

2.2 Data validation

The validation of the data sets presented in this paper are based on the results obtained from different researches (Booij, 2002; van Deursen, 2004; Leander and Buishand, 2007; Ashagrie et al., 2006; de Wit et al., 2007b). The model used for this study (IHMS-HBV-96) was calibrated and validated by van Deursen (2004) for the basin upstream of Borgharen over the period 1969–1984 and 1985–1998, respectively. The overall model error obtained in the validation was $\pm 5\%$. Ashagrie et al. (2006) concluded that the average correlation of the HBV predictions and measured data is around 0.9, and the Nash-Sutcliffe efficiency is 0.93.

Hereafter HBV-M (HBV-Meuse) refers to the instantiation of the HBV rainfall-runoff model for the whole of the Meuse basin. The calibration and validation data sets used in HBV modelling were constructed in such a way that the observed and simulated discharges in both data sets in terms of flow volumes, and the number of flood peaks and the overall shape of the hydrographs are similar. However, initially no specific low-flow indices are used neither for calibration nor validation. Therefore in this study the results of the hydrological simulation of the Meuse discharges done by de Wit et al. (2007b) are used. In their study, the model was specifically validated against low-flow indices derived for the period 1968–1998.

The HBV-M model simulates the rainfall-runoff processes for each sub-basin separately. The sub-basins are interconnected within the model schematization and HBV-M simulates the discharge at the outfall. The schematisation and parameter optimization is derived from the approach proposed by van Deursen (2004).

The Meuse basin model has been calibrated and validated using daily temperature (T) and precipitation (P) for 17 locations interpolated from measurement stations, the calculated potential evapotranspiration (E_{pot}) per subbasin, and the discharge (Q) at Borgharen. The interpolation of the different locations was performed using kriging (Stein, 1999).

HBV-M has been run on a daily basis using daily temperature, precipitation, potential evapotranspiration and discharge data for the period 1968–1984 (calibration) and 1985–1998 (validation) by Booij (2002, 2005) and fine-tuned (with more detailed data) by van Deursen (2004).

Complementary information on data validation can be found in the research done by de Wit et al. (2007a). Their work presents the complete and detailed description of the hydrological data used for the model development.

3 Methodology

In this study two hybrid modelling schemes were tested. In the first one, some of the HBV-S (sub-basin) models were replaced by data-driven model representations. The second scheme is based on the replacement of the Muskingum-Cunge flow routing model (1) by an ANN model integrating the outputs of the sub-basin models.

3.1 HBV-M model setup

The model results in this study have been evaluated against the observed discharge records using (a) the volume errors (mm/yr), (b) the coefficient of efficiency (CoE) for the gauging stations along the Meuse and the outlets of sub-basins and the root mean squared error (RMSE, Eq. 5); (c) the normalised RMSE (NRMSE, Eq. 6) (for comparing the sub-basin models with considerably different flows).

RMSE=
$$\sqrt{\frac{\sum_{i=1}^{n} (Q_{s}^{i} - Q_{o}^{i})^{2}}{n}}$$
 (5)

NRMSE=
$$\sqrt{\frac{\sum_{i=1}^{n} (Q_{s}^{i} - Q_{o}^{i})^{2}}{\sum_{i=1}^{n} (Q_{o}^{i} - \overline{Q_{o}})^{2}}}$$
 (6)

$$CoE = 1 - \frac{\sqrt{SSE}}{\sqrt{\sum_{t=1}^{n} (Q_{obs,t} - \bar{Q}_{obs,t})^2}}$$
(7)

where Q_s is simulated discharge (m³/s); Q_o is observed discharge (m³/s); n is the number of observations, and is average observed discharge (m³/s) over the whole period (all summations are run from time i=1 to n).

3.2 Scheme 1: sub-basin model replacement

3.2.1 HBV-S sub-basin models

The objective of the further analysis is to determine the average error contributions of the different sub-basin models (referred to as HBV-S) to the total error of HBV-M, and hence to identify the candidate sub-basin models that would need improvement or replacement. In this modelling exercise the river basin behaviour during different seasons and flow regimes will be also taken into account.

3.2.2 Sub-basin error contribution

The relative error contribution from a particular HBV-S (subbasin) model is calculated as follows. First, the HBV-M model is run and its RMSE at the outlet is calculated. Then, according to a given replacement scenario a number of input measured discharges are fed into the HBV-M. These measured discharges were available only for some basins, and are the ones used for the different HBV-S model replacements scenarios. The HBV-M model is run once for each scenario. The resulting RMSE for each scenario is compared to the RMSE of the standard HBV-M. This gives the possibility of identifying the overall error variation due to the sub-basin model simulation. Such an error contribution is calculated for the different flow conditions (e.g., dry and wet seasons).

The replacement of the sub-basin models is performed in sequence: it starts with the Lorraine Sud in the direction downstream towards Borgharen, then one more sub-basin model is replaced, then yet another one, until all selected sub-models are replaced (ending at Borgharen). It is important to stress that the independent replacements of sub-basins will not allow for seeing the accumulative error reduction, which is necessary to have an overall idea of the total error of the sub-basin replacement. Two important assumption are made to be able to visualize the error contribution. First, is that the compensation of errors when adding the basin is minimal in comparison to the error of the basin contribution. The second assumption is based on the additive linear error propagation along the river basin.

3.2.3 Data-driven sub-basin models

After the error contribution of the HBV-S models are identified, data-driven models (DDM) can be built for each of the sub-basins under consideration. Various data-driven techniques are compared to select the representative and accurate DDM. Their performances were compared to that of the existing HBV-M model. Apart from that, an attempt was made to recalibrate a number of local HBV models; however, the

Table 1. Data available for the Meuse tributaries (catchment area until Borgharen).

Sub-basin	Location of measurement	% Area ^a	Available
222 34011	tributary/river	, = = 1100	data
Subbas 1	St. Mihiel – Meuse	12.1	1969-2005
Subbas 2	Carignan – Chiers	10.5	1966-2005
Subbas 3	Stenay – Meuse	6.5	1982-2005
Subbas 4	Chooz – Meuse	10.7	1969-2005
Subbas 5	Membre – Semois	5.9	1968-2005
Subbas 6	Treignes – Viroin	2.5	1974-2005
Subbas 7	Maas Chooz Namur	5.4	_
Subbas 8	Gendron – Lesse	6.2	1968-2005
Subbas 9	Sambre	13.1	_
Subbas 10	Tarbeux – Ourthe	7.6	1988-2005
Subbas 11	Martinrive - Ambleve	5	1974-2005
Subbas 12	Chaudfontaine - Versdre	3.3	1992-2005
Subbas 13	Moha – Mehaigne	1.7	1969-2000
Subbas 14	Maas Namur Borgharen	7.4	_
Subbas 15	Jeker	2.2	_

^a Catchment area until Borgharen.

overall performance obtained was lower than that after the calibration of HBV-M as a whole, and these experiments are not presented here. A detailed reference of the algorithms used can be found in Haykin (1999) and Witten and Frank (2000).

In the case study, before identifying the relative error contribution of various sub-basin models, several types of the DDMs were compared for 8 of 15 sub-basins. This made it possible to judge if DDMs are useful as HBV-S replacements.

Each data-driven rainfall-runoff model for the sub-basins uses precipitation and measured discharge as inputs, and the response discharge of the basin is generated for the moment T time steps ahead. The general DDM forecast formulation can be represented as follows:

$$Q_{t+T} = f(R_t, R_{t-1}, R_{t-2}...R_{t-L}, Q_t....Q_{t-M})$$
 (8)

where the optimal lags L for precipitation and M for discharge are obtained through model optimization (these can be different for various forecast horizons T, in our case AMI and correlation results are used); f is the data-driven regression model, and T is the forecast horizon (e.g. 1 day). In this research several data-driven models are tested; including linear regression model (LR, Kachroo and Liang, 1992), artificial neural networks (ANN, Dawson et al., 2005 and M5 model trees (MT, Solomatine and Dulal, 2003).

Neural network are all trained using the same random seed, and trained with the Levenberg-Marquardt optimization algorithm (Levenberg, 1944; Marquardt, 1963). The learning rate was set to 0.1, one hidden layer with sigmoid function, and one linear transfer function in the output layer are common properties of the models. The ANN models

have been optimized using a cross-validation set for determining the number of hidden nodes.

Building M5 model trees (piece-wise linear regression models) followed the procedure presented by Witten and Frank (2000). The size of the trees is controlled by fixing of the minimum number of instances in linear regression models at leaves (e.g. four).

3.3 Scheme 2: integration of sub-basin models

Routing is a common way to integrate sub-basin models of a meso-scale catchment. However, river routing models include hydrodynamic conditions that require a large number of physical measurements. The accuracy is determined by the availability and the quality of these measurements and of the models. Since the cost of the measurements is high, often simplified routing equations are used. In HBV the sub-basin models use simple transfer functions that represent the routing process. The main idea of the Scheme 2 is the replacement of the traditional runoff routing equations by a more accurate non-linear function (data-driven model, Fig. 3). In this paper we have chosen for the multi-layer perceptron ANN (ANN-MLP) due to its widely known robustness and accuracy. The output discharges from the fifteen HBV-S sub-basin models are lagged and used as input to this model. The lags are determined using the correlation and average mutual information analysis involving different subbasin flows and the final outflow at Borgharen. The general ANN-MLP model to determine the flow downstream can be formulated as function of the different lags of the sub-basins.

$$\begin{split} \mathcal{Q}_{t+T}^{\text{Borgharen}} &= f\left(\mathcal{Q}_{t-l_{1}^{1}}^{1},\,\mathcal{Q}_{t-l_{2}^{1}}^{1},\,...,\,\mathcal{Q}_{t-l_{M}^{1}}^{1},\,\mathcal{Q}_{t-l_{1}^{2}}^{2},\,...,\,\\ &\mathcal{Q}_{t-l_{M}^{2}}^{2},\,...,\,\mathcal{Q}_{t-l_{M}^{N}}^{N}\right) \end{split} \tag{9}$$

where the lower-index T represents forecast horizon, N is the total number of sub-basins, and l_i^k the lag i at each sub-basin k. M is the total number of lags taken per sub-basin k. All basins in the model are lagged with respect to the current flow at Borgharen.

4 Application of Scheme 1: data-driven models for sub-basin representation

4.1 Inputs selection and data preparation for DDMs

Each data set is split into a training set (70%; some data is used for cross-validation as well) and a verification (30%) set. This procedure is performed in a way that ensures that the training data contains the maximum and minimum values of each variable to reduce the possible extrapolation problems. Additionally, the statistical similarity of each set was verified by comparing its probability density function. The first step in developing data-driven models for the Meuse sub-basins was to identify the most appropriate inputs for

predicting future discharges. Two approaches were used to select the appropriate input variables and their lags: correlation analysis and the average mutual information (AMI), as it was done, for example, by Solomatine and Dulal (2003). A lag is defined as the number of time steps by which a time series is shifted relative to itself (when autocorrelated), or relative to the corresponding time values of another time series (when cross-correlated). The correlation coefficient and AMI were calculated for 10 lag values. The variables compared were discharge, precipitation and evapotranspiration. Since the correlation analysis reflects only linear relationships and the phenomena are highly non-linear, the analysis based on AMI was employed as well. The AMI between two measurements x_i and y_j drawn from sets X and Y is defined by:

$$I_{XY} = \sum_{\substack{x_i \\ y_j}} P_{(X_i, Y_j)} log_2 \left[\frac{P_{XY}(x_i, y_j)}{P_X(x_i) P_Y(y_j)} \right]$$
 (10)

$$P_{(X_i,Y_j)} = \int \int_{XY} f(x,y) dx dy \tag{11}$$

where $P_{(X_i,Y_j)}$ is the joint probability density for measurements X and Y resulting in values x and y, which are the individual probability density functions for the measurements of X and Y. If the measurements of a value from X resulting in x_i is completely independent of the measurement of a value from Y resulting in y_j then the average mutual information I_{XY} is zero. The probabilities were calculated with different bin sizes and the results were similar. Figure 4a shows the AMI for the Ourthe (a) and Lorraine Sud (b), which represent the sub-basins with faster and slower precipitation-discharge response, respectively. The maximum AMI of precipitation-discharge time lag for the Ourthe corresponds to a three-day lag (P_{t-3}) , and for the Lorraine Sud sub-basin up to a four-day lag (P_{t-4})).

Based on a similar analysis to the one presented in the Fig. 4, the following model structure was adopted for eight basins:

$$Q_t = f(P_t, P_{t-1}, P_{t-2}, P_{t-3}, Q_{t-1})$$
(12)

The models were built for: Semois, Viroin, Lesse, Ourthe, Ambleve, Mehaigne, Chiers, Lorraine Sud; see location Fig. 2. The data used to build each sub-basin model (except Vesdre) covered the period from 1989 to 1995 for the training set and the period from 1996 to 1998 for testing. Due to the availability of data, for Versdre the data set used for training and testing covers the period from 1992 to 1996 and from 1997 to 1998, respectively. Stenay and Chooz (Sub-basin 3 and 4), have input from other three and one sub-basin flow (confluence sub-basins), and therefore not represented stricktly as catchment nor contemplated in this analysis. These two sub-basins are defined for the overall integrated HBV simulation and not for local model representation.

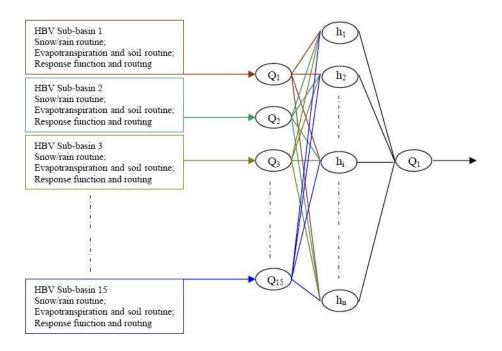


Fig. 3. Diagram of the ANN as replacement for the routing model (Chen and Adams, 2006).

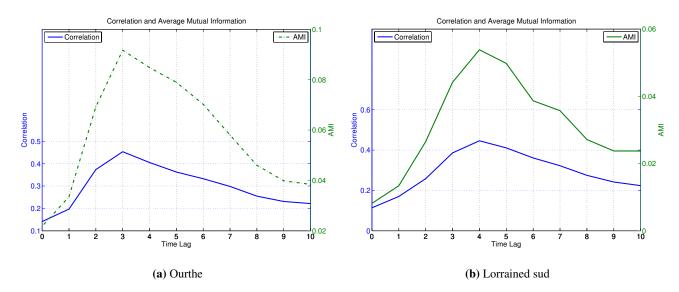


Fig. 4. Average mutual information for between lagged precipitation and discharge for sub-basins Ourthe (a) and Lorraine Sud (b).

4.2 Data-driven sub-basin models

The performance of the HBV-S models was compared with that of several data-driven models (LR, M5P, ANN, Fig. 5); NRMSE was used as the error measure.

Both ANN and M5P data-driven models outperform the HBV-S models. Only for the Lesse, Ourthe, Ambleve, and Vesdre HBV-S model error is relatively low, but even then it is not comparable with that of the data-driven models. According to Berger (1992), Ourthe sub-basin together with

Vesdre and Ambleve are the most important tributaries for flood forecasting, relating area percentage and response time. HBV-M results for Semois, Viroin, and Mehaigne show high NRMSE. The error graphs show that the M5P and ANN models outperform the HBV model for all the considered sub-basins.

It should be stressed that DDM and conceptual models are different in nature and are based on different assumptions. As mentioned by Toth and Brath (2007), DDM (referred as system-theoretic models) can incorporate information about

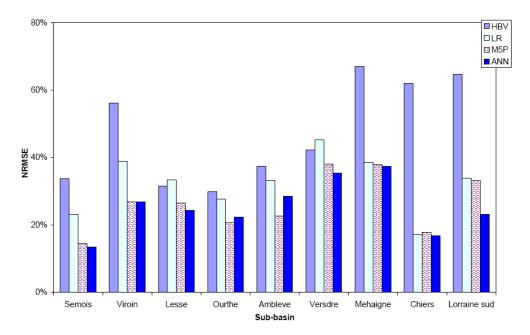


Fig. 5. Comparison of model performance for each sub-basin, expressed in NRMSE of streamflow (Calculated for verification period).

discharge coming from real-time measurements preceding the forecast instant, and the conceptual model assumes that only forcing (typically precipitation and temperature) input is sufficient to drive the evolution of the system. The conceptual model aims to represent the processes of the modelled phenomena (albeit roughly), and the DDM is based on the analysis of historical data.

Since the conceptual model only uses the forcing information (precipitation, temperature, etc.), to obtain forecast with extended lead times in the conceptual model weather forecast information can be effectively fed into conceptual models to make forecast for longer lead times.

To obtain more accurate real-time forecasts it is often possible to use the up-to-date observed system outputs in order to minimize the acknowledged errors due to the model in-adequacies (Kachroo, 1992; Moore, 1983; Schreider et al., 1997). Comparison of various updating schemes, using both types of models can be found, for example, in Toth and Brath (2007); Brath et al. (2002). Updating schemes were not considered in this study but it is planned to do so.

The ANN-MLP model outperforms HBV in more cases than M5P does, and therefore is selected for the replacement experiments. The results show that DDMs can serve as accurate replacement models for sub-basins. However, when more and more sub-basin models are replaced, there will be less and less hydrological knowledge (encapsulated in process models) left. Therefore analysis of the overall performance of the model under different replacements has been undertaken and presented below. Since there is a large number of possible scenarios of replacing various numbers of models, it is necessary to analyze the river basin behaviour

and the relative quality of the individual HBV-S sub-basin models with respect to the overall basin measurements given by the discharge at Borgharen.

4.3 Analysis of HBV-S simulation errors

The changes in the overall model performance (RMSE) on the verification data set as a result of various replacements with measured discharge data are shown in Fig. 6 and Table 2.

The replacement order can be followed by reading Fig. 6 from top to bottom. From the total RMSE of 83.84, Chiers has the largest relative error contribution of 4.53% (10.5% of the total area), followed by Lorraine Sud (2) and Lesse sub-basins with an error contribution of 3.86% (12.10% of the total area) and 2.81%, respectively. Chiers is the second largest sub-basin of the Meuse and it is known that it commonly influences floods generated by its slow response, Lorraine Sud is also a slow responding basin. Vesdre, Ambleve, Viroin and Ourthe basins closer to the outlet are the most accurate in the HBV-M model and are the ones directly responsible for floods.

Hydrological data is available for 52% of the basin area; however, only 20% of the total errors seem to be attributed to this area. The rest of the error contribution can be associated with the other variables in the system, the modelling capacity of the HBV, as well as the different uncertainties in modelling of the basin. It would also be interesting to identify the error contribution of the Sambre, the largest sub-basin, but this was not carried out due to data unavailability. In Fig. 6, the RMSE contributions obtained by each sub-basin replacement are associated with the measured discharge values.

Table 2. RMSE error contribution to the HBV overall simulation.

Sub-basin	Relative error reduction HBV-M (RMSE, m ³ /s)	Area (km²)	Area (% of total basin)	Observed – Simulated (% Volume Difference)
Mehaigne	0.87	346	1.65	1.04
Ambleve	1.44	1050	5.00	1.72
Ourthe	1.89	1597	7.60	2.26
Lesse	2.36	1311	6.24	2.81
Viroin	1.08	526	2.50	1.29
Semois	1.35	1235	5.88	1.61
Chiers	3.79	2207	10.51	4.53
Lorraine Sud	3.23	2540	12.10	3.86
Others	67.82	10 188	48.51	80.89
Total HBV error	83.84	21 000	100	100

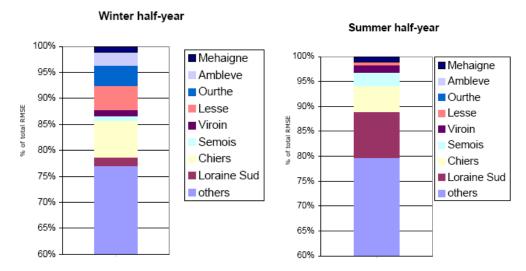


Fig. 6. Percentage of sub-basin models errors for dry and wet seasons.

Since it is well known that seasonality influences this river basin, the error contributions of the HBV-S models in summer (May–October) and winter (November–April) seasons are calculated in terms of the percentage of error with respect to the total HBV-M error; see Fig. 6. The results in Fig. 6 show that there is a homogeneous error contribution from Chiers in both seasons. The model for Lorraine Sud basin has a higher error contribution for summer and a small overall contribution in the winter. Clearly the calibration of the model is well suited for summer conditions where the slow response of the catchment is important for the average discharge in these periods. This is congruent with the size (2540 km²), which represents approximately 10% of the considered area.

In terms of flood forecasting at Borgharen the most sensitive basins for the HBV-M model distribution are Ourthe, Vesdre and Ambleve. The analysis shows that the Ourthe and Ambleve stream flows do not influence the model in the summer period, but together make a significant contribution to the error generated in the winter season. The contributions

of the Mehaigne and Viroin sub-basins do not depend on the season: they have a small and similar error percentage for both seasons.

4.4 Replacements of sub-basin models by ANNs

There are numerous replacement scenarios and these should be identified based not only on the previous error analysis, but also taking into account the river basin behaviour during the different seasons and the different flow regimes. The total number of possible replacement scenarios (combinations of the sub-basin models with the data availability) is too high and it is not feasible to analyze them all. The experiments to replace a sub-basin model were carried out using only 8 scenarios as shown in Table 3.

The scenarios reflect mainly the fact that sub-basins with slow and fast flow responses contribute to different components of the resulting streamflow (mainly low and high flows, respectively). Characterisation of the eight scenarios (R1-R8) is as follows:

Table 3. Replacement scenarios and the effect of their implementation.

Short Name	Replacement	PAR ^a (%)	ADC ^b (%)	RMSE Reduction (ANN-S)	RMSE Reduction ^c MD	ANN-S (%)
R1	Chiers	11	10	3.84	4.53	0.85
R2	Chiers, Semois, Viroin	19	22	6.17	7.42	0.83
R3	Ourthe and Ambleve	13	15	2.25	3.98	0.57
R4	Ourthe, Ambleve, Lesse	19	21	4.21	6.79	0.62
R5	Ourthe Ambleve, Semois	18	25	3.73	5.58	0.67
R6	Semois, Chiers, Lesse	24	28	7.52	8.39	0.9
R7	Ourthe, Ambleve, Semois, Lesse, Chiers	35	41	8.62	12.92	0.67
R8	Lorraine Sud, Chiers, Semois	28	28	9.47	9.99	0.95

^a Percentage of area replaced of the total basin (PAR).

^c Measured data (MD).

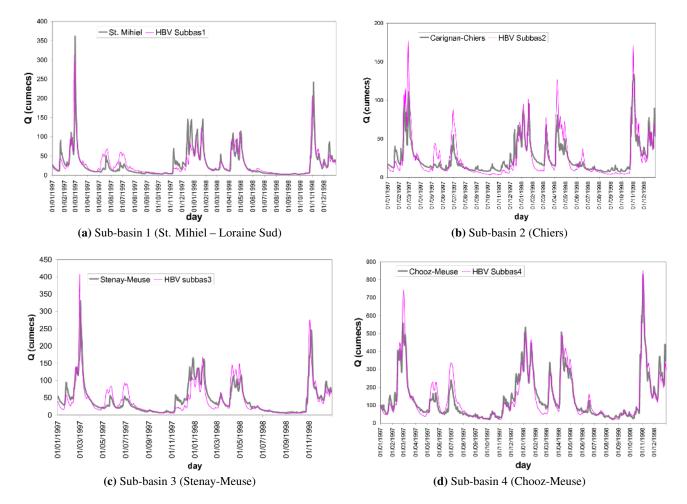


Fig. 7. Hydrographs of sub-basin models giving important contributions to the overall model.

^b Average discharge contribution in relation to the total average discharge (ADC). The total average discharge is calculated using the average annual discharge from 1970 to 2000 (280.1 m³/s).

- R1: the sub-basin (Chiers) with the largest error contribution, and a slow runoff response.
- R2: three sub-basins which include the Meuse tributaries upstream of Chooz. These are the highest elevation areas with relatively low slope and slow response during flood situations.
- R3: the two fast responding sub-basins that have high contributions during floods (Berger, 1992).
- R4: the same sub-basins as in R3, but together with the slow response Lesse sub-basin whose model has a high error in summer and a low error in winter.
- R5: the same sub-basins as in R3, but together with the slow responding Semois whose model has a high error in summer and low error in winter.
- R6: combination of slow and fast responding subbasins.
- R7: combinations of slow and fast responding subbasins, but with a larger area covering 35% of the basin.
- R8: slow responding sub-basins with a large total area.

Table 3 presents the HBV-M model performance changes as a consequence of the different ANN-S replacement strategies. The following statements describe the interpretation of some of the results:

The effectiveness of the models replacements can be evaluated by analysing the changes in the overall HBV-M RMSE. The last column presents the percentages of the maximum reduction possible in case of implementing a particular replacement scenario.

Comparing sub-basins with similar area and similar discharge we can see where the replacement of models was more successful. For example R1 and R3 have similar percentage of area (11 and 13, respectively), also similar average discharge contribution (10 and 15, respectively). However, the R1 (ANN-S) model gives a RMSE reduction (85%), which is higher than that for the scenarios R3, corresponding to larger areas and higher average discharge. This is an indicator that low flows play a significant role in the overall process, and also reflects the weakness of the HBV-S models currently used in simulating low flows.

A similar situation can be observed when R7 replaced a bigger area (35%) than R8 (28%), however, the efficiency for the latter replacement is significantly higher (95%). In terms of discharge, R8 has a smaller average discharge and therefore less contribution. For the scenarios R6 and R8 results show a similar error reduction after the replacement. They have approximately the same average discharge percentage contribution to the basin and a similar area, however, their seasonal error contribution is different (Fig. 6).

The influence of changing Ourthe and Ambleve for Lorraine Sud shows that most of the errors arise in the low flow

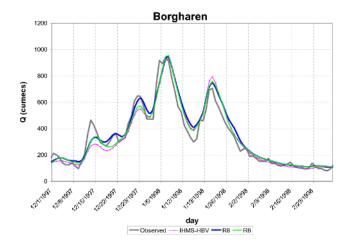


Fig. 8. Hydrograph replacements (R8) and (R6).

modelling. The Lorraine Sud is the most distant basin with relatively mild slope, and therefore its contribution to flash flood (fast flow and runoff) is minimal. This is consistent with the results of de Wit et al. (2007b), who showed that the peak discharges of Vesdre and Ourthe basins are larger than those of Chooz. The results point to a partial explanation based on the differences in precipitation depths of the region and on the difference in hydro-geological conditions. On the other hand, the basins Ourthe and Ambleve (central part) are closer to the outlet and their individual performances are more sensitive for short time lags and fast phenomena.

The results of simulations for the verification period (last three years) are evaluated by calculating the RMSE and Coefficient of efficiency (Fig. 9). A typical section of the hydrograph is extracted in Fig. 8. The shape of the hydrograph with ANN-S replacement is mainly driven by the overall hydrological model. It is possible to see that after the replacement R8 the flows under 600 m³/s are closer to the observed discharge. For flows above 600 m³/s the HBV-M is hardly affected due to the low influence of the replaced basins during the peak flow events (Fig. 8). This shows that the replacement affects mainly the low flow simulation periods.

If one analyses only the reduction in the overall RMSE, then the replacement scenario R8 would result in the model that can be recommended to use instead of the HBV-M.

5 Application of Scheme 2: integrating sub-basin models by ANN

To build a neural network model for routing, preprocessing and input variable identification is required. For this the AMI and cross-correlation analysis were carried out to identify the relation (time lag) between the local sub-basins discharge calculated by the HBV model and the measured discharge at Borgharen. For most of the sub-basins the maximum value of

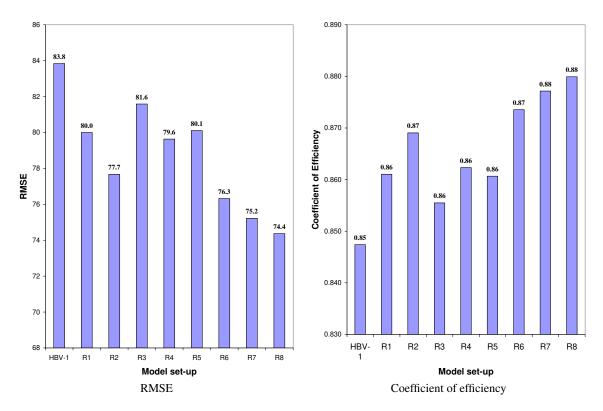


Fig. 9. Error reduction with different combinations of replacement (evaluated at Borgharen).

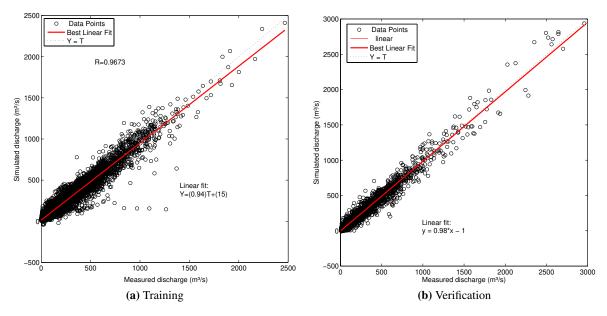


Fig. 10. Scatter plots of target (measured) and ANN model for training and verification period.

AMI related to the observed discharge at Borgharen is a time lag of 1 day. Exceptions are sub-basins 9 (Sambre), 10 (Ourthe), 13 (Mehaigne), and 15 (Jeker) since the corresponding AMI is at maximum for lags less than 1 day. Therefore in Eq. 8, only 1 day lags is considered for all basins. Fifteen

inputs and the discharge at Borgharen are the input and outputs, respectively. These results are in agreement with recent research (de Wit et al., 2007a), where it was found that the travel time between the measuring stations of the Sambre and Mehaigne, Ourthe and Jeker to Borgharen is less than half

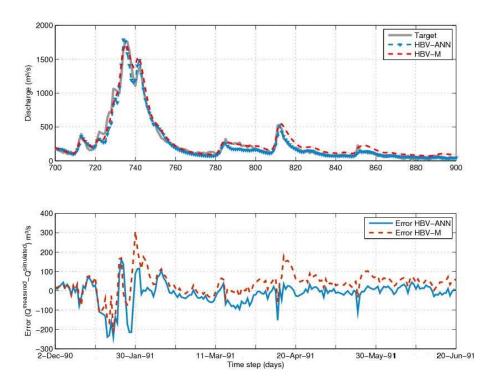


Fig. 11. Hydrograph of the original HBV-M and HBV-ANN integrated models.

a day. More precise time lags can be obtained with hourly data. The average travel time of the flow between the Semois measuring station (sub-basin 5) and Borgharen is one day (Berger, 1992).

The results of the model can be visualized by scatter plots. High correlations are found between the observed and simulated discharge both for training and verification sets (Fig. 10).

Figure 11 shows the observed and simulated discharges at Borgharen from 2 December 1990 (record 700) to 20 June 1991 (record 900). On average the integrated HBV-ANN model outperforms the original HBV-M model. The recession curve of the hydrograph is clearly closer to the measured curve and what was viewed as the systematic error in the recession curve of the HBV-M model is now corrected. An interesting phenomenon can be observed close to the measured peak: the measurement value goes up and down before it reaches its maximum value. This peak change in the hydrograph is reproduced by the ANN routing model with a relatively small underestimation.

For a 3 years error analysis the HBV-ANN gives RMSE of 58.66 m³/s. An extended error analysis of nine years verification period shows that the RMSE for the HBV-M and HBV-ANN are 86 m³/s and 55 m³/s respectively which is a 36% improvement (Table 4). The coefficient of efficiency is also improved from 0.918 for the HBV-M to 0.967 for HBV-ANN model. For both winter and summer seasons it is clear that the use of ANN for integrating the sub-basin models improves the accuracy.

5.1 Integrating Schemes 1 and 2

The ANN-MLP routing model integrates the results of the sub-basin models and generates the value of discharge at the outlet (Borgharen). By doing so, the ANN routing is already correcting the regional behaviour of each sub-basin model, so the ANN-MLP routing acts as an error corrector. Therefore, the use of another sub-basin model (e.g. R8 scenario in Table 3), with different error performance, as input of the ANN-routing model does not add new knowledge into the model, but only increases the error. The replacement R8 into the ANN-MLP (scheme) had almost the same performance as the original HBV without any replacement (RMSE 82.91, see Fig. 12).

6 Discussion

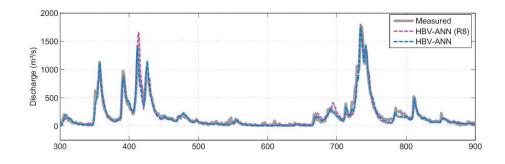
In this section the results for each scheme are discussed and compared.

6.1 Scheme 1

The results show that replacing some of the conceptual subbasin models with data-driven models clearly improves the overall model performance. Doing so the low flow errors related to some of the sub-basins can be reduced without any deterioration in the high flow performance. The operational forecasting system using process-based models requires variables like precipitation and temperature for each simulation

	Hydrological year (Nov-Oct)		Winter (Nov-Apr)		Summer (Apr–Oct)	
Model	HBV-1	HBV-ANN	HBV-1	HBV-ANN	HBV-1	HBV-ANN
RMSE (m^3/s)	85.65	54.51	100.02	64.26	71.66	45.56
NRMSE	0.29	0.18	0.27	0.18	0.48	0.31

Table 4. Comparison between the HBV-M model and the integrated HBV-ANN model.



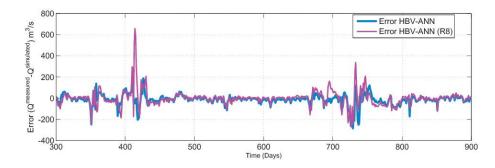


Fig. 12. Hydrograph comparison for the HBV-ANN with and without R8 replacement.

forecast, however, whereas the ANN models only previous measured discharge is needed. Therefore, this approach may bring operational advantages on the locations where weather forecast information may not be available.

The choice of the best combination of HBV and ANN components depends on various factors and is, in fact, a multi-criteria problem. One may also think of rules (taking into account for example the season, data availability, location) that decision maker would use to select the final model.

The use of Scheme 1 may well be suited for simulation, but comparative tests with data-assimilation and data-driven approaches of the whole basin may be needed to determine whether the use of data-assimilation in operational system is more accurate or suitable than a simple ANN model of a basin. This analysis will be conducted in further studies.

Note that the extended forecast made by DDMs can be produced in different ways. Simply using previously simulated discharges in an autoregressive conceptualization might be the most straightforward approach. Another approach was explored by Toth and Brath (2007); Corzo and Solomatine (2007a), where separate ANNs were created for each lead time value.

Three important implications have to be mentioned here. Firstly, the use of previously simulated discharges iteratively decreases the quality of the forecast. Secondly, if we assume that the measured information is a perfect forecast, the HBV average performance will not decrease for higher forecast horizons. Thirdly, the DDM is not representing the basin behaviour and instead is acting more as an autoregressive model with a small component given by the precipitation.

The data-driven model, which tends to generate high weight values for input from previous discharges in its structure, underestimate the use of other variables that are poorly correlated with the output. In this sense data-driven models (DDM) can simulate the flow quite accurately (only on average, however, and not in the beginning of a high precipitation event) even without the use of the variables that really drive the phenomena (precipitation and temperature).

6.2 Scheme 2

Applying the Scheme 2 with the integrating ANN model leads to a more accurate calculation of the overall river discharge, if compared to both Scheme 1 and to the simplified

routing scheme employed in the HBV-M model. Our results in this experiment are in agreement with the work by Chen and Adams (2006) where an ANN model was used to integrate the three basin models (Xinanjiang model, Tank model, and Soil Moisture Accounting model).

Scheme 2 does not only consider the integration of streamflow process, but can be also seen as a data assimilation approach (error corrector). Note that the ANN-MLP model does not target the accurate representation of the physical system dynamics; instead, the target is aimed to reproduce the measured value (discharge).

The use of physical conceptual and data-driven models in operation should consider the dynamics of the basin. The dynamics of the Meuse basin has hardly changed during the last decade (Tu et al., 2004), so the combination of models seems to be reliable under relatively long periods of time (e.g. 3 to 5 years as the validation period of the models presented).

It should be noted that the experiments presented in this paper are based on daily data and are aimed at improving the HBV-M hydrological model. In subsequent studies it is planned to explore the usefulness of the approaches above under a more detailed and complex framework (daily forecast with hourly data and precipitation forecast information). The challenge in extending these concepts to hourly-based models relates not only to the non-linearity and dynamics, but also to the influence of human interventions at weirs, sluices, canals, power plants, etc. These aspects are not included in the HBV-M model and are part of the motivation to use data-driven techniques, and, possibly, rule-based techniques allowing for multiple regimes of model operation.

7 Conclusions

This paper explored two schemes of introducing data-driven model components into a semi-distributed process based rainfall-runoff model. The first scheme explored the replacement of HBV sub-basin models by ANN-MLP models using several scenarios. The results show that such approach improves the discharge simulation both in terms of reducing the RMSE and increasing the model efficiency. The improvement was mainly observed for the summer periods for low flows.

The second scheme used the replacement of the routing model (combining the individual sub-basin models) by an ANN, and lead to higher gains in terms of the overall error than the first scheme. Nevertheless, it is important to stress that this latter scheme does not only reproduce the flow, but also the noise in the system. The use of an ANN for routing replacement is not only a simulation tool but also captures the variation in the time series. Therefore, its results can not be interpreted as the accurate representation of the river routing but more as a tool to combine the model's and which acts as an error corrector as well.

In general it can be concluded that the both combination schemes have a clear potential in improving the accuracy of the considered class of hydrological models.

Performance of operational systems is typically affected by the limited and/or inaccurate data. A possible way to alleviate this, is to use autoregressive models which are not sensitive to the precipitation, temperature and evapotranspiration. Yet another issue is the estimation of the models uncertainty associated with the inaccuracies in data and model structures. It is planned to explore all these issues and possibilities in further studies.

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