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Complexity of the dipolar exciton Mott transition in GaN/(AlGa)N nanostructuresF. Chiaruttini,¹ T. Guillet¹, C. Brimont¹, D. Scalbert¹, S. Cronenberger¹, B. Jouault¹, P. Lefebvre¹, B. Damilano² and M. Vladimirova^{1,*}¹Laboratoire Charles Coulomb, UMR 5221 CNRS-Université de Montpellier, 34095 Montpellier, France²CRHEA, Université Côte d'Azur, CNRS, Valbonne, France (Received 19 October 2020; revised 5 January 2021; accepted 7 January 2021; published 26 January 2021)

The Mott transition from a dipolar excitonic to an electron-hole plasma state is demonstrated in a wide GaN/(Al,Ga)N quantum well at $T = 7$ K by means of spatially resolved magnetophotoluminescence spectroscopy. Increasing optical excitation density, we drive the system from the excitonic state, characterized by a diamagnetic behavior and thus a quadratic energy dependence on the magnetic field, to the unbound electron-hole state, characterized by a linear shift of the emission energy with the magnetic field. The complexity of the system requires taking into account both the density dependence of the exciton binding energy and the exciton-exciton interaction and correlation energy that are of the same order of magnitude. We estimate the carrier density at Mott transition as $n_{\text{Mott}} \approx 2 \times 10^{11} \text{ cm}^{-2}$ and address the role played by excitonic correlations in this process. Our results strongly rely on the spatial resolution of the photoluminescence and the assessment of the carrier transport. We show that in contrast to GaAs/(Al,Ga)As systems, where transport of dipolar magnetoexcitons is strongly quenched by the magnetic field due to exciton mass enhancement, in GaN/(Al,Ga)N the band parameters are such that the transport is preserved up to 9 T.

DOI: [10.1103/PhysRevB.103.045308](https://doi.org/10.1103/PhysRevB.103.045308)**I. INTRODUCTION**

New states of matter and various phase transitions in bosonic systems have benefited from particular attention in recent years. Among different physical platforms, two-dimensional bilayer systems, where electron and hole are spatially separated and form an indirect exciton (IX), are particularly interesting. Due to this spatial separation between electron and hole, the lifetime of the IX is considerably increased (up to tens of microseconds) and it acquires a nonzero electric dipole moment [1–7]. These rich and tunable properties offer the opportunity to achieve experimentally high densities of cold IXs, and to explore various intriguing quantum phenomena including Bose-Einstein-like condensation (BEC), darkening, formation of dipolar liquids, superfluidity, and excitonic ferromagnetism [8–16]. A possible phase diagram that can be suggested theoretically for IXs hosted by GaN/(AlGa)N quantum wells (QWs) is represented in Fig. 1(a) [17]. The particularity of this phase diagram with respect to other bosonic systems is that in a large range of densities the onset of quantum degeneracy is accompanied by the set-in of multiparticle interactions and correlations due to the IX dipolar interactions. Therefore, dipolar IXs are expected to behave as a strongly interacting liquid (dipolar liquid) rather than as a weakly interacting BEC.

Figure 1(a) shows that the critical temperature that should be attained to scrutinize collective IX states is constrained by the maximum possible IX density. The difficulty faced in this context is the onset of avalanche ionization of excitons at high densities, as a result of screening and momentum

space filling [18]. This many-body effect is usually referred to as the Mott transition, in analogy with the phase transition from an electrically insulating to a conducting state of matter predicted by Sir Nevill Mott in a system of correlated electrons [19].

Mott transition of IXs has been addressed both experimentally and theoretically, but mainly in GaAs-based coupled QWs under electric bias [20–26]. However, so far, no consensus regarding the dynamics of this transition in two-dimensional systems has been reached, neither for traditional excitons nor for IXs. In particular, it is not clear whether the ionization of excitons occurs abruptly or gradually when the density is increased [21–23,26–30]. Moreover, an intriguing hysteretic behavior has been predicted when the temperature is slowly changed at an intermediate carrier density [29], while at low densities an entropic ionisation of excitons can be expected [31].

The objective of this paper is to address the Mott transition of IXs hosted by wide polar GaN/(AlGa)N QWs. GaN-hosted IXs have relatively high binding energies (20 meV), small Bohr radii (5 nm), and greater mass $M = 1.6 m_0$ as compared to GaAs-based structures (m_0 is the free electron mass) [33]. Hence the density/temperature phase diagram [Fig. 1(a)] is quite different from that of GaAs-based systems.

Because GaN QWs grown along the (0001) crystal axis naturally exhibit built-in electric fields of the order of megavolts per centimeter, IXs are naturally created in the absence of any external electric field [34–36]. This offers the opportunity not only for all-optical generation of IXs, but also for shaping at will the in-plane potential experienced by the IXs by simple deposition of metallic layers on the surface, without application of any external electric bias. We have recently demonstrated the electrostatic trapping and control of the cold

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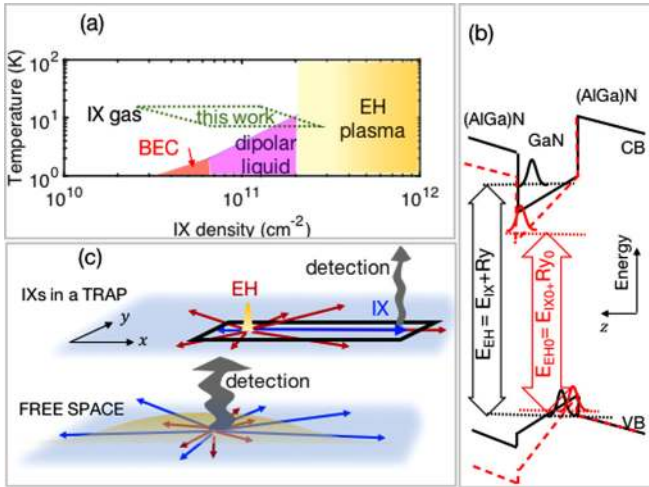


FIG. 1. (a) IX phase diagram. Four phases theoretically expected are shown by different colors. The green region delimited by dotted line represents the phase space area explored in this paper. The critical density corresponding to the transition toward plasma states is determined in this paper. (b) Sketch of the GaN/(Al,Ga)N QW bands in the absence (red dashed line) and in the presence of optical excitation (black solid line). Corresponding electron and hole wave functions and energy levels are shown with the same color code. The band-to-band transitions are indicated by arrows. (c) Artist view of the two ways to study IX emission: IX in a trap (upper sketch)—pointlike excitation followed by spatially separated PL analysis in the trap (used in Ref. [32]) and free space (lower sketch)—broad excitation followed by detection in the center of the excitation spot (used in this paper).

IX density in such structures [32]. IXs at a quasithermal equilibrium state could be studied in spatial regions situated tens of micrometers away from the laser excitation spot. We called such areas excitonic lakes. We have determined the lower limit for the carrier density for the set of excitation powers used and demonstrated that the carrier temperature remains power independent. However, despite careful analysis of the spectral shape of the photoluminescence (PL) from the lakes, we could not evidence the onset of the Mott transition.

The reasons for that are numerous. First, the PL line shape does not show any characteristic shape modification when the system undergoes Mott transition [37]. Second, excitonic correlations, when they are strong, strongly affect the exciton density estimated by comparing the PL energy shift to the one calculated by solving the coupled Schrödinger and Poisson equations (see Fig. 13) [11,12,38–40]. Such correlations can arise from the strong depletion of the exciton gas around a given exciton due to repulsive interactions between IXs. At high IX density, they are also expected to favor the transition from an excitonic gas to a dipolar liquid, rather than a Bose-Einstein-like state, see Fig. 1(a). Third, the IX binding energy at the lowest excitation densities and the typical blue shift of the electron-hole recombination energy at highest excitation densities are of the same order of magnitude, ≈ 20 meV. This makes it extremely challenging to unravel the effects of the binding energy reduction due to the screening of the built-in electric field and exciton-exciton interactions at nonzero density. The density-induced modifications of the

QW band diagram and the resulting transition energy shift E_{int} are schematically shown in Fig. 1(b). Finally, the contribution of the band-to-band emission (unbound electron-hole pairs) to the PL spectrum that could help us estimate the IX binding energy, at least at the lowest excitation densities [25,27,28], is useless in the trap geometry with pointlike excitation which we have employed in Ref. [32]. Indeed, when PL is recorded from the same spatial region where the excitation takes place, according to the Saha equation, a mass-action law describing the equilibrium concentration of a gas of coexisting excitons and free carriers, one can eventually extract both exciton and band-to-band emission [41]. This is not the case for a pointlike excitation of IXs. Because IXs are rapidly expelled from the excitation spot by strong dipole-dipole interaction, the equilibrium between IXs and band carriers is probably never achieved under the excitation spot [Fig. 1(c), upper sketch]. The detection of the thermalized IXs trapped in the lake tens of micrometers away from the excitation spot does not offer the opportunity to detect simultaneously thermalized IX and band-to-band emission.

In this paper, we choose a different strategy, based on two key ingredients: (i) broad ($\approx 300 \mu\text{m}$) and spatially homogeneous excitation, PL detection with spatial resolution, to selectively address the emission in the center of the excitation area [Fig. 1(c), lower sketch]. A similar approach has been used in Ref. [27]. The underlying idea is to detect the PL of IXs and free electron-hole pairs coexisting spatially and to monitor their relative energies and intensities as a function of power and temperature; and (ii) application of a magnetic field in Faraday geometry (parallel to the growth axis) to discriminate between the diamagnetic field dependence typical of excitons (quadratic energy shift [42]) from the Landau quantization expected for unbound charge carriers (linear increase of energy, usually referred to as cyclotron shift).

The analysis of the experimental results suggests that at the lowest studied sample temperature (7 K) and at the highest excitation power (carrier density $n_{\text{Mott}} \approx 2 \times 10^{11} \text{ cm}^{-2}$) the system undergoes the Mott transition: The zero-field PL energy spectrally merges with the electron-hole emission and the magnetic-field dependence changes from quadratic to linear. Such a high carrier density could not be reached at $T > 7$ K, presumably due to more efficient nonradiative recombination. The determination of the corresponding carrier density is quite complex because of the interplay between different density-dependent effects: the built-in electrostatic potential, reduction of the exciton binding energy (accompanied by the increase of the in-plane Bohr radius), and build-up of excitonic correlations. In this paper, we have tried to unravel their respective contributions. We have also observed that, in contrast to GaAs/(AlGa)As systems, where the transport of dipolar magnetoexcitons is strongly quenched by the magnetic field due to exciton mass enhancement [43,44], in GaN/(Al,Ga)N the band parameters are such that the transport is preserved up to 9 T.

The paper is organized as follows. In the next section, we present the sample and experimental setup. The third section presents the ensemble of the experimental results, namely, the PL study of IX transport as a function of the magnetic field, laser excitation power, and temperature. In Sec. IV, we interpret the results in terms of the situation of our experiments in

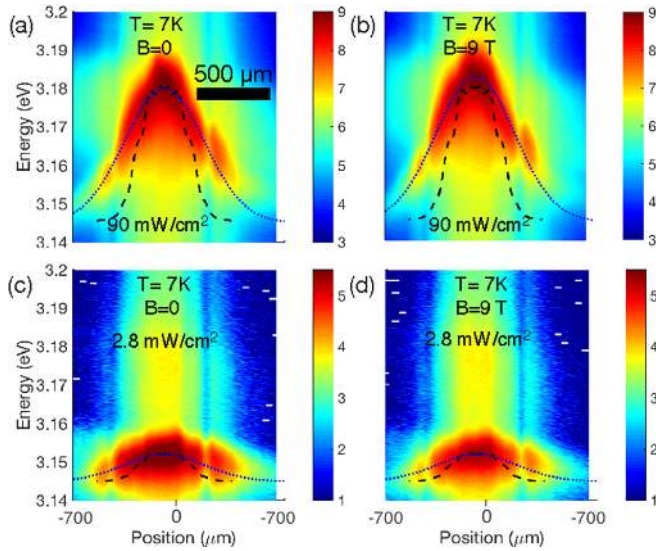


FIG. 2. PL intensities (color encoded in log scale) measured at $T = 7$ K and two different excitation power densities: $P = 90$ mW/cm² (a), (b); $P = 2.8$ mW/cm² (c), (d); and two magnetic field values: $B = 0$ (a), (c); $B = 9$ T (b), (d). The measured laser intensity profile (normalized to unity) is shown by dashed lines. Dotted lines are Gaussian-shaped guides for the eye showing the decrease of the IX emission energy when the distance from the excitation center increases.

the IX phase diagram. The last section summarizes the results and concludes the study.

II. SAMPLE AND EXPERIMENTAL SETUP

We investigate a 7.8-nm-wide GaN QW sandwiched between 50- (top) and 100-nm-wide (bottom) Al_{0.11}Ga_{0.89}N barriers, grown on a free-standing GaN substrate. The band diagram of such a structure is shown schematically in Fig. 1(b). In the absence of photoexcitation the built-in electric field due to spontaneous and piezoelectric polarization confines electrons and holes at the two opposite interfaces of the QW. In the studied structure, the field effect is so strong that the ground-state exciton energy [$E_{IX0} = 3.145$ eV in Fig. 1(b)] is pushed below the exciton energy in bulk GaN $E_{\text{GaN}} = 3.49$ eV [32–36,45]. The corresponding IX radiative lifetime is estimated as $\tau_0 \approx 10\mu\text{s}$, orders of magnitude longer than in traditional narrow QWs [46–49]. The sample is placed in a variable temperature magneto-optical cryostat and cooled down to temperatures in the range from $T = 7$ to 14 K. Magnetic fields B up to 9 T created by superconducting magnets are applied in the Faraday geometry (parallel to the QW growth axis).

We use a continuous wave laser excitation at $\lambda = 355$ nm, very close to the GaN band-gap energy but well below the emission energy of the Al_{0.11}Ga_{0.89}N barriers. The laser beam is loosely focused on the sample surface ($\approx 300\text{-}\mu\text{m}$ -diameter spot) to create a broad, homogeneously excited area (see dashed lines in Figs. 2 and 3). The PL spectra are acquired by a charge coupled device (CCD) camera over 1.5 mm with $\approx 250\text{-}\mu\text{m}$ spatial resolution (pixel size). Such broad excitation combined with the spatially resolved detection appeared

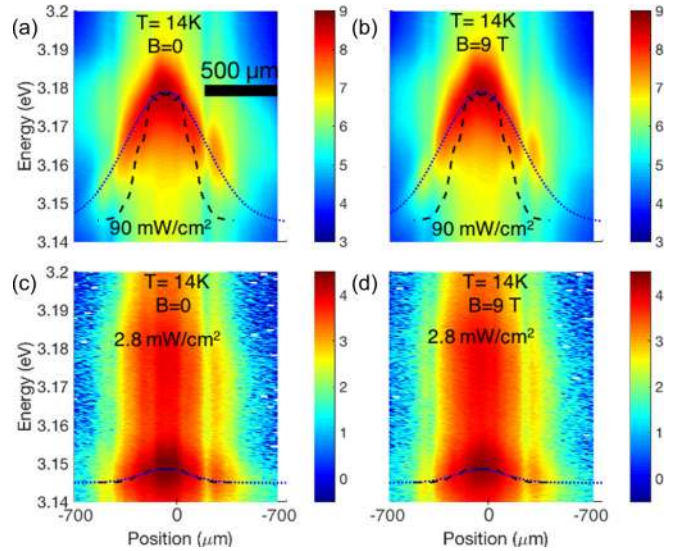


FIG. 3. PL intensities (color encoded in log scale) measured at $T = 14$ K and two different excitation power densities: $P = 90$ mW/cm² (a), (b); $P = 2.8$ mW/cm² (c), (d); and two magnetic-field values: $B = 0$ (a), (c); $B = 9$ T (b), (d). The measured laser intensity profile (normalized to unity) is shown by dashed lines. Dotted lines are Gaussian-shaped guides for the eye showing the decrease of the IX emission energy when the distance from the excitation center increases.

to be critically important to address the question of the Mott transition. As anticipated in the Introduction and as we explain in more detail in the next section, this allows us to detect the PL from IXs and from unbound electron-hole pairs that coexist spatially, and thus to monitor the reduction of the IX binding energy. This also gives us access to carrier transport properties, so we can directly verify the assumptions regarding transport in our modeling. More details on the sample parameters and on the setup are given in the Appendixes.

III. EXPERIMENTAL RESULTS AND DISCUSSION

A. Exciton transport

The exciton transport at $T = 7$ K and $T = 14$ K is presented in Figs. 2 and 3, respectively. They show color-encoded PL spectra, measured at various distances from the excitation spot for two different power densities, and at two values of the magnetic field, $B = 0$ and 9 T. Excitation spot intensity profile is shown by the dashed lines. The blue dotted lines are guides for the eye, helping to visualize the IX emission peak energy as a function of the distance from the spot center.

Let us first concentrate on the $B = 0$ transport. Clearly, the energy of the excitonic PL decreases when moving away from the excitation spot center, similar to the case of the pointlike excitation [32,47,50]. Such decrease of the emission energy and intensity indicates that the exciton density decreases. The relation between PL energy and IX density is particularly strong in wide QWs due to interactions between IXs that have large dipole moments, and the resulting screening of the electric field along the growth direction: the highest density under the pumping spot corresponds to the maximum screening (lowest electric field) and thus to the highest

emission intensity and energy [32,47,50,51]. The interaction-induced increase of the IX energy reaches 40 meV (10 meV) at the spot center and at highest (lowest) power densities that we could explore in our experiments. This shift can be used to estimate the IX density as $n = E_{\text{int}}/\phi_0$, where $\phi_0 = 1.5 \times 10^{-13}$ eV cm⁻² is the coefficient extracted from the self-consistent solution of the Schrödinger and Poisson equations (plate capacitorlike model) [32,47,50,51]. This estimate needs to be improved by taking into account the exciton binding energy (which decreases when the IX density increases) and excitonic correlations, which become significant at low temperatures and high densities. As we will discuss later on (see also Figs. 6, 13), both of these effects may substantially alter our estimation of the IX density needed to induce a given blue shift [17,38,39].

From the $B = 0$ emission profiles measured at highest power density $P = 90$ mW/cm², we deduce that despite spatially broad excitation as compared to previous experiments involving pointlike excitation, IX transport is still clearly observable both at 7 K and 14 K [32,47,50]. The full width at half maximum (FWHM) of the emission pattern is approximately 800 μ m. By contrast, for the lowest power density $P = 2.8$ mW/cm² the IX transport is only apparent at $T = 7$ K (same FWHM as at high power), while at $T = 14$ K the emission profile coincides with the excitation one. The quenching of the IX transport with decreasing power observed at $T = 14$ K is a usually observed and well-understood phenomenon [47,52–54]. Modelling IX transport by drift-diffusion equation shows that this is due to weaker dipole-dipole repulsion that depends on the density. More efficient localization on the QW interfaces at low IX densities may also hinder the transport [47,50,52–55]. By contrast, the persistence of the transport at 7 K is rather surprising, especially because carrier localization is expected to be enhanced at lower temperatures.

The persistence of the exciton transport at low temperature and low carrier density can be tentatively interpreted in terms of the condensation of the exciton gas into a liquid state, as described previously by Cohen *et al.* [12] for GaAs-hosted indirect excitons. To confirm this hypothesis, further experiments would be required, in particular at lower temperatures and with better spatial resolution. This will be the subject of further work.

The effect of the magnetic field up to 9 T on the IX transport appears to be very weak. From the color-encoded spectra in Figs. 2 and 3, one can see that the FWHM of the emission pattern does not change. This behavior differs significantly from that of IXs in GaAs/(Al,Ga)As coupled QWs, where a magnetic field of similar strength has been shown to strongly inhibit IX transport. [43,44]. This is due to the fact that IXs hosted by GaAs/(Al,Ga)As coupled QWs are much lighter particles, with much wider radii. Therefore, the ratio χ between cyclotron energy $\hbar\omega_c$ and exciton binding energy Ry , $\chi = \hbar\omega_c/2Ry$ increases much faster with magnetic field. When magnetic energy dominates over the electron-hole Coulomb interaction, $\chi \gg 1$, the system is described in terms of so-called magnetoexciton [56–58]. The magnetic field leads in this case to the strong reduction of the in-plane Bohr radius a_B and enhancement of the in-plane exciton mass M [43,44,57–63]. Therefore, the reduction of the diffusion coefficient $D = l\sqrt{2k_B T/M}$ and the mobility $\mu_X = D/k_B T$ is

observed [43,44]. Here l is the exciton scattering length and k_B is the Boltzmann constant. In GaN/(Al,Ga)N structures studied in this paper and up to 9 T, we seem to deal with the opposite limit: $\chi \ll 1$. Numerical modeling of the IX transport within a drift-diffusion model (see Appendixes) [32,47] allows us to estimate that the enhancement of the exciton mass $M(B)/M$ does not exceed a few percent at $B < 9$ T, consistent with estimations that can be done in the $\chi < 1$ regime [63,64]:

$$M(B)/M = (1 - 42\mu(a_B/l_B)^4/16^2M)^{-1}. \quad (1)$$

Here $l_B = \sqrt{\hbar/eB}$ is the magnetic length, e is the electron charge, \hbar is the reduced Planck's constant, μ is the exciton in-plane reduced mass. Thus, in the following we assume that the shift of the IX emission energy measured at the center of the exciton spot in the presence of the magnetic field is entirely local. This means that at given experimental conditions (temperature and laser excitation power), the IX density at the center of the spot does not change when an external magnetic field is applied. Or, in other words, the magnetic field has no effect on the in-plane distribution of the IX density, in contrast to the case of IXs in GaAs/(Al,Ga)As QWs. We use this result in the analysis of the magnetic field induced exciton energy shift that follows below.

B. Magnetic field induced exciton energy shift

The shift of the IX emission energy peak with respect to $B = 0$ (averaged over ≈ 25 μ m) measured as a function of the magnetic field at different excitation power densities is shown by symbols in Fig. 4 for $T = 7$ K (a), $T = 10$ K (b), and $T = 14$ K (c). Figures 4(d)– 4(f) indicate for each temperature the correspondence between the emission energy E_{IX} measured at $B = 0$ and the power density. The color code is the same as in Figs. 4(a)– 4(c). The energies used to extract these shifts are obtained by the spectrum fitting procedure described in Appendix A4. One can see that at maximum field $B = 9$ T the energy shift varies in the range from 0.2 to 3 meV. The largest shifts are achieved at highest powers and lowest temperatures. Except for the highest power at 7 K, the IX energy shifts quadratically with the magnetic field. This can be interpreted as a diamagnetic shift $\Delta E = \gamma_D B^2$, where $\gamma_D = e^2 a_B^2 / (8\mu)$ is the so-called diamagnetic coefficient [65]. The diamagnetic coefficient appears to increase with the excitation power, suggesting that IX Bohr radius increases as well. This is a signature of the progressive screening of the electron-hole Coulomb interaction within each IX. The reduced exciton mass in GaN being well known ($\mu = 0.18m_0$), fitting of the data to the quadratic dependence (solid lines in Fig. 4) allows us to extract the values of Bohr radii for all excitation power densities and temperatures.

The ensemble of the resulting values of a_B is presented in Figs. 4(g)–4(i). One can see that the Bohr radius can be as small as 5–6 nm. Note that relatively small values of Bohr radius (compared to the prediction of the self-consistent variational calculation of a_B [66,67]) are consistent with the large exciton binding energy that we deduce from the PL spectra, where both exciton and free carrier emission are observed (see Fig. 5). This will be further discussed in Sec. III C.

For each value of the sample temperature, the values of a_B are shown as a function of the emission energy shift

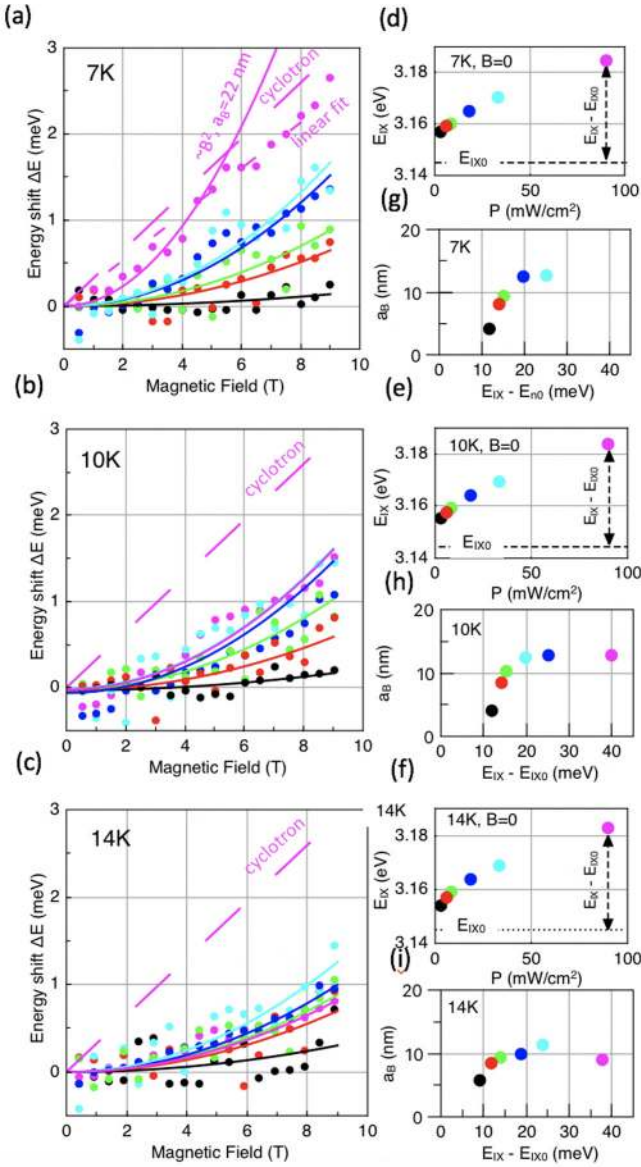


FIG. 4. (a)–(c) IX emission energy shift with respect to the $B = 0$ emission energy as a function of the magnetic field at $T = 7$ K (a), $T = 10$ K (b), $T = 14$ K (c) for various excitation power densities from $P = 2.8$ mW/cm² (black symbols) to $P = 90$ mW/cm² (magenta symbols). Solid lines are parabolic fits to the diamagnetic shift model. The model does not fit the highest power data in (a) and the linear fit is shown by the long-dashed line. Short-dashed line in (a) shows the cyclotron shift expected for unbound electron-hole pairs. (d)–(f) show the emission energy at $B = 0$ for each power density and three different temperatures. The horizontal dashed line shows zero-density limit E_{IX0} of the exciton emission energy. The vertical dashed arrow illustrates the density-induced blueshift of the emission line at $P = 90$ mW/cm². (g)–(i) Values of Bohr radius extracted from the quadratic fit (a)–(c) as a function of the zero-field density-induced energy shift. Excitation power density is shown with the same color code in (a)–(c), (d)–(f), and (g)–(i).

$E_{IX} - E_{IX0}$ at $B = 0$. This shift is related to the IX density in the QW and contains two contributions with different signs. The first one is the blueshift due to the interaction energy, and the second one is the redshift due to exciton binding energy

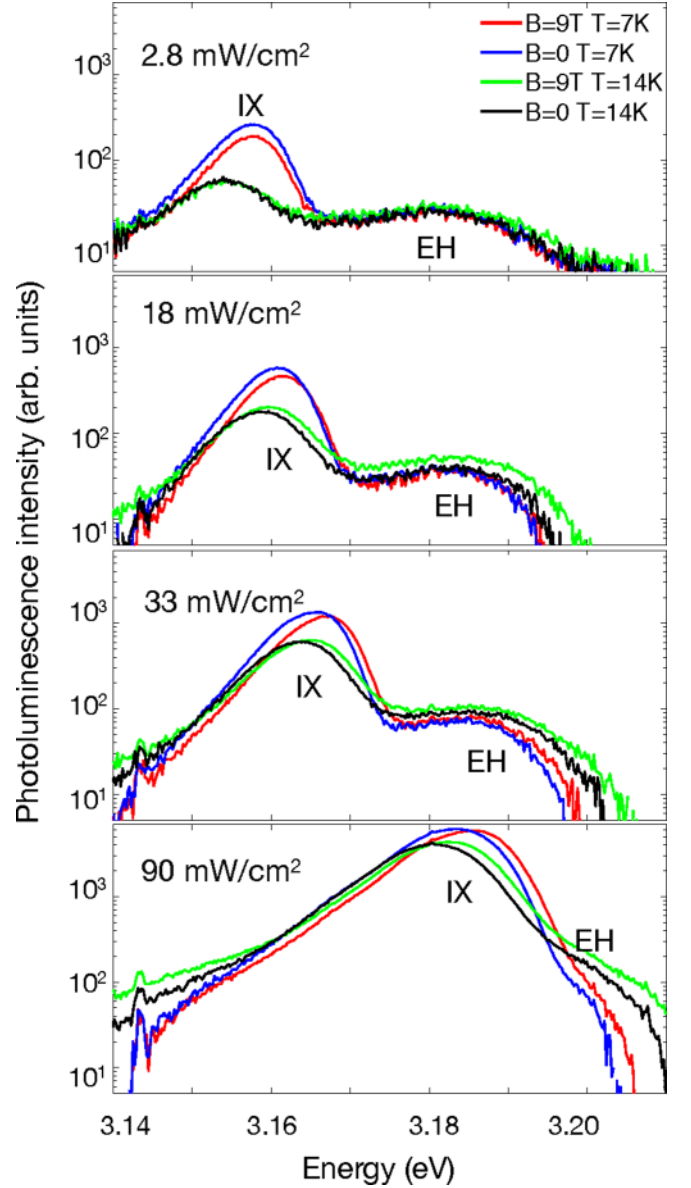


FIG. 5. PL spectra collected from 25- μ m-diameter area in the center of the excitation spot at different power densities. Two temperatures ($T = 7$ K, $T = 14$ K) and two magnetic field values ($B = 0$ and $B = 9$ T) are shown for each power. We identify the two emission lines as IXs and unbound electron-hole pairs (EH).

(see Fig. 1). Their relative contribution will be discussed in Sec. IV A.

Let us now consider the set of measurements at $T = 7$ K in Fig. 4(a) that corresponds to the highest excitation power $P = 90$ mW/cm² (magenta circles). In contrast with other measurements, the energy shift does not grow quadratically with magnetic field. For comparison, the solid magenta line in Fig. 4(a) corresponds to $a_B = 22$ nm, much larger than $a_B \approx 12$ nm at higher temperatures and maximum powers. Instead, the data are much better described by a linear function $\Delta E = \gamma_L B$, with the slope $\gamma_L = 0.27$ meV/T. Remarkably, the slope obtained from the linear fit is very close to $\gamma_c = e\hbar/(2\mu) = 0.32$ meV/T that one could expect for the cyclotron energy of the electron-hole pair. This suggests that,

indeed, the density of the electron-hole pairs in the QW plane is high enough to screen the Coulomb interaction within IX, so the Mott transition could be reached.

The reason why this transition could only be observed at 7 K needs to be elucidated. In particular, it is important to find out whether this is due to the higher density reached in this case (e.g. due to different nonradiative losses), or due to the screening of the exciton binding, that would be more efficient at low temperature. Below we try to answer this question and to determine n_{Mott} , the critical density at the Mott transition. We recall that the analysis made in this paper is based on the assumption that the magnetic field up to 9 T (that induces a cyclotron shift of the electron-hole pair emission $\hbar\omega_c/2 = 3$ meV) can be considered as a small perturbation with respect to the exciton binding energy, i.e. $Ry \gg \hbar\omega_c/2$. Therefore, the formation of magnetoexciton does not take place. This differs from the GaAs-based structures where the transition from Coulomb-bound exciton to magnetoexciton has been reported to occur at lower magnetic fields ≈ 2 T [5].

C. Photoluminescence of excitons vs free carriers

Let us consider in detail the PL spectra collected from the 25- μm -diameter area in the center of the excitation spot at different power densities and temperatures (Fig. 5). For the lowest excitation density (solid lines), we identify two emission lines, separated by ≈ 25 meV, the lowest energy line is the one that we have identified as the IX emission. It has higher intensity and it is shifted toward higher energy by the magnetic field (as shown in Fig. 4), while the second line is so wide that it is difficult to quantify the energy shift induced by the magnetic field. When the excitation power increases, the IX emission strongly shifts toward higher energies up to merging with the higher energy emission line, which shifts much less. Note also that the ratio between the intensities of the IX and the high energy line is ≈ 5 times higher at $T = 7$ K than at $T = 14$ K.

We tentatively interpret the higher energy line as an emission of the unbound electron-hole (EH) pairs that coexists with IXs even at the lowest excitation densities explored in this paper. This contribution is not negligible as compared to the lower energy IX, because the corresponding density of states is huge. EH emission can be spectrally separated from IX because the linewidth of IX emission is smaller than IX binding energy. Similar PL behavior has already been observed in both GaAs and InGaAs QWs [25,27,28]. In GaN-based heterostructures, the efficient formation of excitons even within a dense electron-hole plasma has already been observed by time-resolved terahertz spectroscopy [68]. Both energy and intensity of the EH emission with respect to the well-identified IX emission are consistent with this interpretation: IX line merges with the EH plasma at high density and the ratio between IX and EH intensity decreases when the temperature increases. The power-induced shift of the IX line is larger than that of the EH line. This is because EH transition energy is affected only by the screening of the built-in electrostatic potential, while IXs experience both this screening and the reduction of the binding energy. Note also that the EH emission line is much broader (30 meV at the lowest power, compared to 10 meV for IXs) and weaker

(≈ 5 times for the lowest power density) than the IX line. That is why it was not possible to quantify the magnetic field induced shift of the EH line that is expected to be smaller than 3 meV at highest accessible magnetic field.

The simultaneous observation of EH and IX emission provides us with some important information. Indeed, the energy splitting between IX and EH lines characterizes the exciton binding energy Ry , which, due to many-body effects, depends on the density of the particles in the QW [41]. From the measurements at the lowest power, we estimate $Ry_0 = 25$ meV, corresponding to the zero-density limit. Exciton binding energy is related to its Bohr radius $Ry = e^2/4\pi\epsilon a_B$, where ϵ is dielectric permittivity constant in the hosting semiconductor (here GaN). This yields $a_{B0} = 6$ nm in the zero-density limit. As already mentioned in Sec. III B, these values are not properly described by the self-consistent variational calculation of the excitonic properties [66,67,69]. The relevance of this model relies on the choice of the variational function, and so far has not been verified experimentally. Moreover, the model predicts that IX binding energy and Bohr radius remain constant up to approximately 10^{11} cm^{-2} pair density (corresponding to emission energy shift > 10 meV), which also contradicts our experiments. Thus, in what follows we rely on the experiments and use the value of $Ry_0 = 25$ meV and its relation to a_B to estimate the exciton density as a function of power and temperature and determine the Mott density.

IV. DISCUSSION

A. Determination of the exciton densities

Estimation of the exciton densities and the critical densities for exciton dissociation is an extremely delicate task, even in the case of traditional excitons with zero dipole moments. In particular, quantifying exchange and correlations within excitonic ensembles is a complex many-body problem. For IXs, density-dependent screening of the built-in electric field is another complicating factor, because it might be difficult to separate it from exciton-exciton interaction. We describe below the procedure that we adopted here to estimate power and temperature-dependent exciton densities, Bohr radii, and binding energies within available models.

The analysis is based on three experimentally determined (or deduced from them) parameters: (i) the value of the zero-density binding energy $Ry_0 = 25$ meV estimated from the spectral splitting between IX and EH emission lines at the lowest density, (ii) the corresponding zero-density Bohr radius $a_{B0} = 6$ nm, and (iii) zero-density IX emission energy $E_{\text{IX0}} = 3.145$ meV, measured ≈ 700 μm away from the excitation spot [see e.g. Figs. 2 and 3(c)]. These values are identical for all temperatures, within the accessible precision.

We start from the calculation of the electron-hole pair density corresponding to a given band-to-band transition energy,

$$E_{\text{EH}}(n) = E_{\text{EH0}} + E_{\text{int}}(n), \quad (2)$$

using self-consistent solution of the coupled Schrödinger and Poisson equations (see Appendix 5a). The result of such calculation is very well approximated by the plate capacitorlike model, where density-induced blueshift is given by $E_{\text{int}} = \phi_0 n$, with $\phi_0 = 1.5 \times 10^{-13}$ eV cm^{-2} . Here E_{EH0} is the zero-density band-to-band transition energy,

which does not yet account for the exciton binding energy $E_{\text{EH0}} = E_{\text{IX0}} + Ry_0 = 3.17$ eV.

As already mentioned, this approach completely neglects the correlation effects which, at sufficiently high density and low temperature, result in strong enhancement of the exciton density expected at a given PL energy shift [38,39]. We try to include these correlation effects in our model and calculate E_{int} using a more sophisticated approach [38]. Thus, we have two ways to calculate the band-to-band transition energy E_{EH} , either including (model C), or not including (model NC) exciton correlation effects. The details of these calculations are reported in Appendixes 5b and 5a.

Because in our system E_{int} can reach values of the same order as Ry_0 , that is, ≈ 10 – 20 meV, it is important to take into account the variations of binding energy when the IX density is increased:

$$E_{\text{IX}}(n) = E_{\text{EH}}(n) - Ry(n). \quad (3)$$

The simplest exponential model is chosen to account for the density-induced reduction of the exciton binding energy due to many-body effects:

$$Ry(n) = Ry_0 \times \exp(-n/n_{\text{Mott}}), \quad (4)$$

where n_{Mott} is a free parameter [70]. The corresponding Bohr radius $a_B(n)$ is calculated from $Ry(n)$ as

$$a_B(n) = a_{B0} \times Ry(n)/Ry_0. \quad (5)$$

Equations (2)–(5) can be solved for any value of the fitting parameter n_{Mott} . This allows us to establish the relation between IX Bohr radius and particle density, either including (model C) or not (model NC) the excitonic correlations, for each value of the excitation power and temperature. The value $n_{\text{Mott}} = (2 \pm 0.5) \times 10^{11} \text{ cm}^{-2}$ ensures the best fit between the values of a_B calculated from Eq. (5) and those extracted from the magnetic field induced diamagnetic shift.

The results of this analysis are summarized in Fig. 6 for three different temperatures. The correspondence between IX density and Bohr radius calculated within model C (open symbols) and model NC (filled symbols) is shown for all excitation powers. At 7 K, crosses on top of the circles indicate the highest density point ($P = 90 \text{ W/cm}^2$), where the energy shift induced by magnetic field is linear, so the interpretation in terms of diamagnetic shift is not satisfactory. Lines indicate the model assumption for $a_B(n)$ given by Eq. (5) (solid line) and Mott density resulting from the best fit to the data (dashed line).

One can see that within the relevant density/temperature parameter range, the difference in the density estimation between two models does not exceed a factor of 2. At all powers except the highest one (magenta symbols), both models describe the experimental data reasonably well. Namely, exciton density remains below n_{Mott} , consistent with the experimentally observed diamagnetic behavior. By contrast, at $P = 90 \text{ mW/cm}^2$ only model C allows us to describe the Mott transition observed at $T = 7$ K. Nevertheless, despite the temperature dependence that it intrinsically includes (see Appendix), model C fails to describe the absence of Mott transition at $T = 10$ and 14 K. It seems to overestimate the role of the correlations at $T > 10$ K, while the simpler model NC provides better agreement with the data. Thus, none of

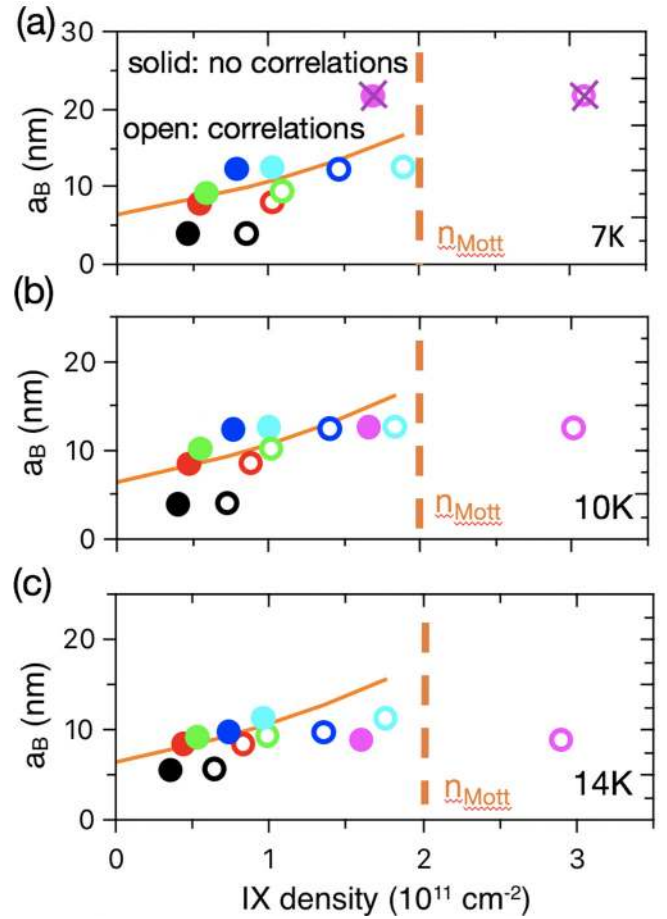


FIG. 6. Exciton Bohr radius (solid lines) as a function of the IX density calculated within exponential model assuming $n_{\text{Mott}} = 2 \times 10^{11} \text{ cm}^{-2}$ (dashed lines) and $Ry_0 = 25$ meV. These assumptions are identical for the three different temperatures (a)–(c). Symbols show the Bohr radii extracted from the diamagnetic shift at different powers (same as in Fig. 4, same color code) as a function of the carrier density calculated from the corresponding emission energy at $B = 0$. Open (filled) symbols show the calculation within Model C (Model NC). At 7 K, crosses on top of the circles indicate the density points where magnetic field induced energy shift is linear, so the interpretation in terms of the diamagnetic shift is not satisfactory (the emission is expected to be dominated by the electron-hole plasma).

the models fits to the ensemble of the data. In the attempt to reconstruct the IX phase diagram shown in Fig. 1, we assume that the densities are given by model C at $T = 7$ K and by model NC at higher temperatures.

B. IX phase diagram

The determination of the exciton densities and the Mott transition (only reached at $T = 7$ K) allows us to draw the parameter space explored in this work on the theoretical IX phase diagram presented in Fig. 1(a). The critical temperature for the formation of the BEC-like state is given by $k_B T_{\text{BEC}} = 2\pi \hbar^2 n/M$ (red area) and for the formation of the correlated dipolar liquid $k_B T_{\text{DL}} = (4\pi \epsilon n / (ed))^2/3$ (magenta area) [13,14,39]. Here ϵ is the dielectric constant in the matter (GaN). The exciton parameter space explored here (grey area)

is expected to span over three different phases: gas, dipolar liquid, and electron-hole plasma.

The Mott transition from excitons to ionized electron-hole pairs at $n_{\text{Mott}} \approx 2 \times 10^{11} \text{ cm}^{-2}$ has only been observed at 7 K because only at this lowest explored temperature such high density could be reached. Indeed, the experimental configuration that we used relies on broad excitation, which limits accessible laser power density. Some nonradiative losses could be sufficient to reduce the carrier density by a factor of the order of 2, making the transition inaccessible. Since we have no experimental determination of the temperature dependence of the Mott density, it is represented in Fig. 1(a) as a temperature-independent phase boundary. Note that in narrow GaN/(Al,Ga)N, QWs hosting excitons such that their dipolar moment is negligibly small and n_{Mott} is three times higher than in our structure, no temperature dependence of the Mott density have been found up to 150 K [49]. The estimated value of n_{Mott} is three times lower than the one reported in similar structures but with narrow QWs, and thus nondipolar excitons [49].

The interpretation of the Mott transition observed at 7 K is complex. Our analysis of the underlying densities as well as the theoretically expected formation of the liquid stated suggests the importance of the excitonic correlations at this temperature. Another indication on the onset of the correlations is the differences in the excitonic transport at 7 K and at higher temperatures. As pointed out in Sec. III A (Fig. 2), at 7 K the excitonic drift remains efficient even at the lowest density used in this work. This behavior is not correctly described by the simple transport model that does fit properly the transport at 14 K. Note that the enhancement of the exciton propagation at low temperature excludes the localization effects as a possible cause of the observed effects.

The precision of the procedure used in this paper to explore the onset of the many-body effects has, of course, a number of limitations. In particular, we use an oversimplified relation between exciton Bohr radius and its binding energy and neglect nonradiative effects. Moreover, our considerations neglect possible magnetic field dependence of the exciton Bohr radius and eventual transition toward magnetoexciton states at highest magnetic fields [5]. Although electron-hole binding energy seems to remain higher than the cyclotron energy, these effects may affect the results. To confirm and better quantify the onset of many-body effects (dipole-dipole excitonic correlations and Mott transition), future work should focus on (i) lowering down the temperature of the carriers in this system and (ii) comparing the systems hosting IXs with different dipole length. Measurable effects can be expected already at $T = 2 \text{ K}$, and with a 2–3 nm variation of the QW width.

V. CONCLUSIONS

In conclusion, using the PL spectroscopy in Faraday configuration, we demonstrated the transition from the dipolar IX fluid to the EH plasma in wide polar GaN/(AlGa)N QWs at 7 K. The corresponding pair density $n_{\text{Mott}} = (2 \pm 0.5) \times 10^{11} \text{ cm}^{-2}$ could not be reached at higher temperatures, presumably due to nonradiative losses. We have shown that below Mott transition, IX fluid and unbound EH

pairs coexist and can be spectrally separated. The increase of carrier density in the system is accompanied by the screening of both the built-in electric field and the IX binding energy. In the explored parameter range, these two contributions are of the same order. Our modeling suggests the build-up of the exciton-exciton correlations and the possible formation of the dipolar liquid at lowest temperature $T = 7 \text{ K}$. These correlations may also be responsible for the particularities discovered in the IX transport. Indeed, we have observed that at this lowest temperature IX in-plane transport is almost density-independent, consistent with the results of Cohen *et al.* for dipolar liquids [12]. Finally, in contrast with GaAs-hosted IXs, the radial transport of the IXs GaN/(Al,Ga)N QWs appears to be preserved under magnetic field up to $B = 9 \text{ T}$.

ACKNOWLEDGMENTS

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APPENDIX

1. Sample structure

The sample is grown by molecular beam epitaxy on a *c*-plane oriented n-type GaN LUMILOG substrate with $\sim 2 \times 10^7 \text{ cm}^{-2}$ threading dislocation density. The substrate is covered by a 0.8- μm -thick GaN buffer layer under the active zone. The active zone consists of a 7.8-nm-wide GaN QW sandwiched between 50-nm (top) and 100-nm-wide (bottom) $\text{Al}_{0.11}\text{Ga}_{0.89}\text{N}$ barriers. The main characteristics of the sample, material properties used in calculations, and the results of various calculations are summarized in Tables I and II.

2. Spatially resolved PL setup under magnetic field

The sample is placed in the chamber of a variable temperature insert of the magneto-optical cryostat (Cryogenic Limited). The magnetic field up to 9 T is created by superconducting coils in Faraday geometry.

Optical setup is shown in the Fig. 7. The laser source is a continuous emission at 355 nm (Coherent OBIS, nominal power 20 mW). The beam is first shaped by an expander (L1, L2) to increase the numerical aperture incident on the objective lens (LO) which focuses the excitation on the sample surface. The diameter of the laser spot thus focused can be reduced up to about 20 μm . We deliberately deregulated the beam expander to increase the size of the incident spot on the sample up to 300 μm . The luminescence is collected by the same objective lens (L3). A bandpass filter (F, Semrock 400/16 nm) placed behind a power-splitter (PS) eliminates the reflection of the laser beam. The sample is imaged on the spectrometer (Horiba Jobin Yvon iHR550) entrance slit (80 μm). The signal is then sent to a CCD camera: each pixel corresponds to 27 μm on the sample.

TABLE I. Sample and material parameters used in various calculations [71–74].

Parameter	Units	Value
QW width	(nm)	7.8
Al composition in the (Al,Ga)N barriers	(%)	11
Al _{0.11} Ga _{0.89} N cap layer thickness	(nm)	50
Al _{0.11} Ga _{0.89} N bottom layer thickness	(nm)	100
GaN buffer layer thickness	(nm)	800
Dislocation density in GaN substrate	(cm ⁻²)	~2 × 10 ⁷
IX emission energy E_{IX0} at $n \approx 0$	(eV)	~3.145
IX binding energy $R\gamma_0$ at $n \approx 0$	(meV)	~25
IX radiative lifetime τ_0 at $n \approx 0$	(μ s)	~40
m_e^z for electron in GaN	(m_0)	0.200
m_h^z for hole in GaN	(m_0)	1.1
m_e^z for electron in Al _{0.11} Ga _{0.89} N	(m_0)	0.213
m_h^z for hole in Al _{0.11} Ga _{0.89} N	(m_0)	1.367
m_e^\perp transverse electron mass in QW	(m_0)	0.2
m_h^\perp transverse hole mass in QW	(m_0)	1.6
ϵ Dielectric constant in GaN	(ϵ_0)	8.9
ϵ_B Dielectric constant in (Al,Ga)N	(ϵ_0)	8.926
GaN band-gap energy at 7 K	(eV)	3.507
(Al,Ga)N band-gap energy at 7 K	(eV)	3.709
Band offset in GaN and (Al,Ga)N	(%)	80

3. Modeling of the IX transport

The model used here is identical to the one that we used in Refs. [32,47]. It is based on the equation for the in-plane transport of indirect excitons. In its most general form, it reads [54,55]

$$\frac{\partial n}{\partial t} = -\nabla \cdot \mathbf{J} + G - Rn, \quad (\text{A1})$$

where n is the exciton density,

$$G = \frac{N_p}{(\pi a_0^2 + \pi w^2/2)} \times \text{erfc}\left(\frac{r - a_0}{w}\right) \quad (\text{A2})$$

is the exciton density generation rate, N_p is the number of excitons generated per second, a_0 and w are the laser spot geometric factors, R is the recombination rate, and \mathbf{J} is the IX current density. To describe the spatial profile of the spot, we have chosen the parameters in Eq. (A2) as $w = 100 \mu\text{m}$, $a_0 = 200 \mu\text{m}$. The exciton current \mathbf{J} can be split into drift and diffusion components: $\mathbf{J} = \mathbf{J}_{\text{drift}} + \mathbf{J}_{\text{diff}}$.

The diffusion current \mathbf{J}_{diff} is given by

$$\mathbf{J}_{\text{diff}} = -D\nabla n, \quad (\text{A3})$$

TABLE II. Sample parameters from self-consistent solution of Schrödinger and Poisson equations.

Parameter	Units	Value
Built-in electric field F	(kV/cm)	980
Exciton radiative lifetime factor γ	(cm ⁻²)	2.7 × 10 ¹¹
IX-IX interaction constant ϕ_0	(eV·cm ²)	1.50 × 10 ⁻¹³
IX Bohr radius a_{B0} at $n \approx 0$	(μm)	~6
Band-to-band transition E_{EH0}	(eV)	~3.17

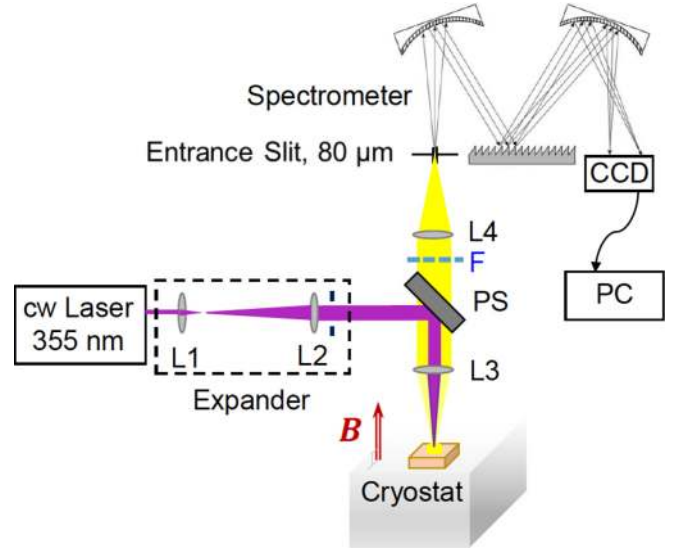


FIG. 7. Experimental setup.

where D is the exciton diffusion coefficient $D = l\sqrt{2k_B T/M}$. It depends on the exciton scattering length l [47,54] but also on the exciton in-plane mass $M = m_e^\perp + m_h^\perp$ that can be affected by the magnetic field: $M(B)/M = 1 + \delta M$. The drift term $\mathbf{J}_{\text{drift}}$ in Eq. (A1) can be rewritten as

$$\mathbf{J}_{\text{drift}} = -\mu_X n \nabla(\phi_0 n), \quad (\text{A4})$$

where the exciton mobility μ_X is connected to the diffusion coefficient D via the Einstein relation: $\mu_X = D/k_B T$. In Eq. (A4), the drift is governed by the exciton-exciton interaction energy $\phi_0 n$ only. The recombination rate R is assumed to be dominated by radiative mechanisms $R = 1/\tau_{\text{rad}}$, where density-dependent radiative recombination time is given by $\tau_{\text{rad}} = \tau_0 \exp(-n/\gamma)$ and γ is obtained from the solution of the coupled Schrödinger and Poisson equations [32,47,51] and $\tau_0 = 40$ ms (see Table II).

We look for the steady-state solutions $n(r)$ of Eq. (A1) at $T = 14$ K to evaluate the eventual effect of the IX mass enhancement on the in-plane transport. The emission profiles measured experimentally are compared with the calculated spatial profiles of (i) the exciton emission energy shift $\Phi_0 n$ and (ii) the exciton PL intensity $I = nR$ at two different power densities, the lowest and the highest ones. The corresponding values of N_p in Eq. (A2) are $N_p = 1.2 \times 10^{12} \text{ s}^{-1}$ for $P = 2.8$ mW/cm² and $N_p = 40 \times 10^{12} \text{ s}^{-1}$ for $P = 90$ mW/cm².

Figure 8 shows how the emission energy shift and the intensity profiles calculated for three different values $M(B)/M$ and two power densities. One can see that while the modification of the emission profile would be hardly detectable experimentally even for $M(B)/M = 4$, the energy shift in the spot center is sensible to the mass enhancement and is accompanied by the significant enhancement of the emission intensity. This effect is strongest at high power.

Figure 9 shows the calculated energy shift and emission intensity in the spot center as a function of $M(B)/M$. Since experimentally we do not observe any detectable increase of the emission intensity at $B = 9$ T with respect to zero field emission, we estimate that the corresponding mass

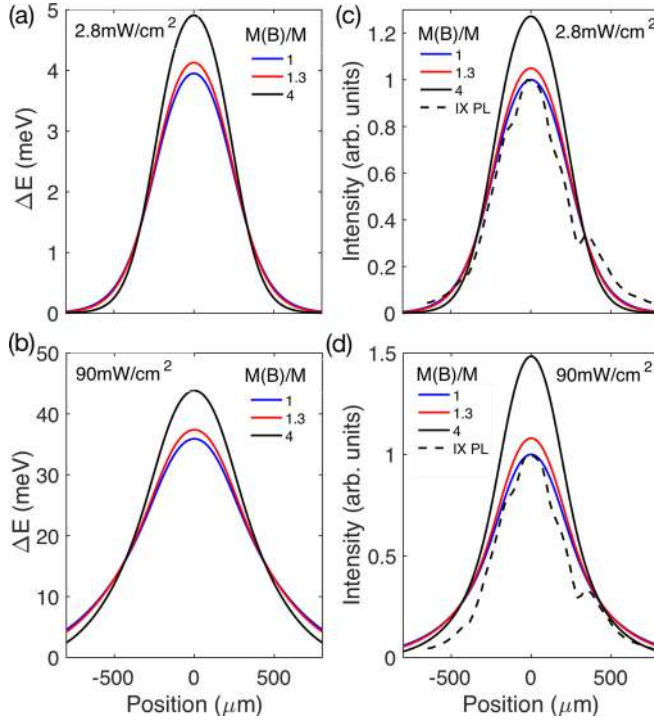


FIG. 8. Calculated spatial distribution of the emission energy shift (a), (b) and the intensity (c), (d) for three different values $M(B)/M$ and two power densities. Dashed lines in (c), (d) show measured IX intensity at $T = 14$ K (there is no difference in the $B = 0$ and $B = 9$ T profiles).

enhancement does not exceed $M(B)/M < 1.3$ (dashed lines in Fig. 9). Assuming that $M(B)/M$ is described by Eq. (1), we obtain that $a_B < 16$ nm, which is consistent with our results.

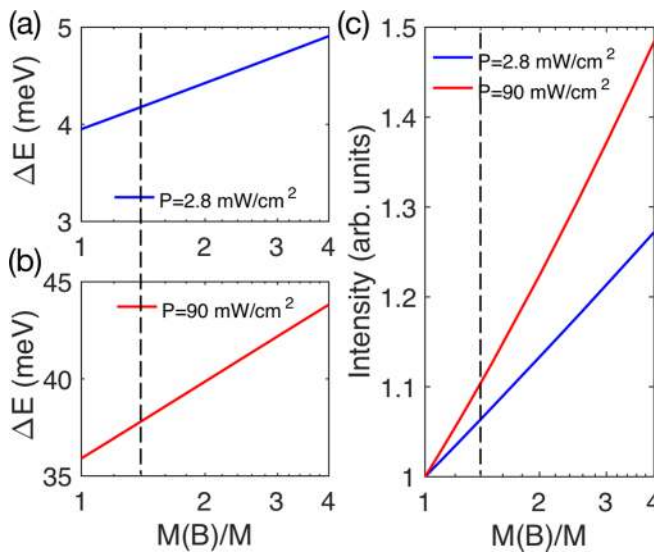


FIG. 9. Energy shift (a), (b) and intensity increase (c) in the center of the excitation spot calculated as a function of $M(B)/M$ for two different values of power density. Dashed lines point to the value $M(B)/M = 1.3$, the estimated limit for our system.

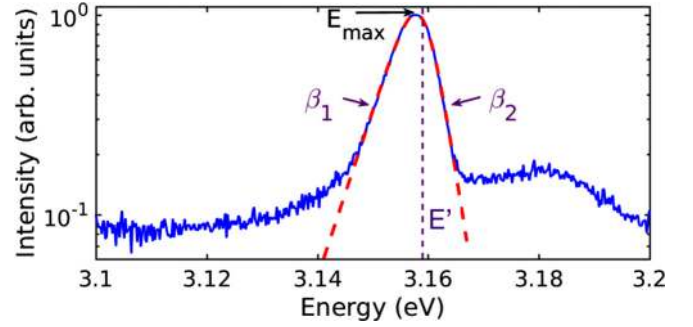


FIG. 10. A typical IX photoluminescence spectrum (blue) and the result of the fitting procedure (red dashed).

4. Modelling of the PL line shape

The spectral profile of the excitonic luminescence have in semilogarithmic representation a triangular shape whose low (high) energy tails can be modeled by an exponential $\exp(\pm\beta_{1(2)}E)$, where $\beta_{1(2)}$ characterizes the slope of the low (high) energy tail.

We use the following generic function to describe the the IX spectrum:

$$I = f_{\theta}(E) = A \frac{\exp(\beta_1(E - E'))}{1 + \exp(\beta_2(E - E'))}, \quad (\text{A5})$$

where $\theta = \{A, \beta_1, E', \beta_2\}$ is the set of parameters to be optimized. Our algorithm employs a least-squares regression from a suitably predetermined initial condition. Note that the parameter E' does not correspond to the spectral maximum, E_{max} : the latter is thus obtained by a simple numerical search of the maximum value on a list of energy values applied to the model function $x \rightarrow f_{\theta_0}(x)$, where θ_0 is the optimum in the sense of least squares.

Figure 10 illustrates the relevance of the chosen fitting function and the quality of the line shape modeling.

5. Estimation of density-dependent exciton energy shift

We use two models to establish the relation between exciton density and the emission energy shift. The first model (model NC, Appendix 5a) is based on the solution of the coupled Schrödinger and Poisson equations [51]. It accounts for the screening of the built-in electric field by the photocreated carriers, but neglects the correlations that can settle between them at low temperature and high densities. The second model (model C, Appendix 5b) accounts for both screening and correlations. Both models are described below.

a. Self-consistent solution of SP equations (NC model)

Electron and hole wave functions are calculated by solving the 1D Schrödinger equation for the envelope function, $\Psi(z)$:

$$-\frac{\hbar^2}{2} \frac{d}{dz} \left(\frac{1}{m^z(z)} \frac{d}{dz} \Psi(z) \right) + V(z) \Psi(z) = E \Psi(z). \quad (\text{A6})$$

Here $V(z)$ ($m^z(z)$) stands for the corresponding band potential (effective mass). We implement a second-order finite difference scheme of uniform spatial step, Δz , that leads to the

following secular equation:

$$(H_{ij} + V_i \delta_{ij}) \Psi_j = E_j \Psi_j. \quad (\text{A7})$$

Here $H \equiv (H_{ij})$ is a $N \times N$ tridiagonal matrix given by

$$H = \begin{pmatrix} D_1 & U_1 & & \dots & 0 \\ L_2 & D_2 & U_2 & \dots & 0 \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ 0 & \dots & 0 & L_N & D_N \end{pmatrix}. \quad (\text{A8})$$

Here N is the number of nodes in the grid, while upper (U_i), lower (L_i), and diagonal (D_i) coefficients are given, for $1 < i < N$, by

$$U_i = \frac{\hbar^2}{4\Delta z^2} \left(\frac{1}{m_{i+1}} + \frac{1}{m_i} \right), \quad (\text{A9})$$

$$L_i = \frac{\hbar^2}{4\Delta z^2} \left(\frac{1}{m_i} + \frac{1}{m_{i-1}} \right), \quad (\text{A10})$$

$$D_i = -\frac{\hbar^2}{4\Delta z^2} \left(\frac{1}{m_{i+1}} + \frac{2}{m_i} + \frac{1}{m_{i-1}} \right). \quad (\text{A11})$$

Using $\Delta z \sim 0.1$ nm, the eigenvalues are computed with $\sim 10^{-6}$ relative precision. By applying the above formalism to both conduction and valence bands we obtain the corresponding ground state confinement energies. Their difference gives us the energy of the fundamental optical transition E_{EH0} .

Note that we implement the simplest Born-Von Karman cyclic boundary conditions that imply that the band potential is identical at the two boundaries of the active layer [33]. One must bear in mind, however, that in reality the situation is more complex and the potential drops across the active layer. Fermi level is known to be pinned at the surface, where a depletion region forms [75]; a two-dimensional electron gas resulting from residual doping and surface states accumulates on the back side of the active structure (at the bottom (Al,Ga)N/GaN interface). We checked that, for this sample structure, the Fermi level is well below the bottom of the QW [32], which means that one should not expect the presence of the residual carriers in the active layer.

Photoinjected carriers affect the band potential that confines electrons and holes in the QW. For a given charge density profile $\rho(z)$, the resulting potential is given by the Poisson equation,

$$\frac{d}{dz} \left(\varepsilon(z) \frac{d}{dz} V(z) \right) = -\rho(z), \quad (\text{A12})$$

where $\varepsilon(z)$ is the local dielectric permittivity.

Using boundary conditions at $z = 0$ (nullity of both electric potential and field) yields

$$V(z) = - \int_0^z d\xi \left[\frac{1}{\varepsilon(\xi)} \int_0^\xi d\xi' \rho(\xi') \right]. \quad (\text{A13})$$

Thus, to account for the screening of the built-in potential by the photoinjected carriers, we solve Poisson and Schrödinger equations self-consistently.

An example of such calculation for the electron-hole pair density $n = 2 \times 10^{11} \text{ cm}^{-2}$ and for $n = 0$ in our sample is shown in Fig. 11. One can see that the band diagram is less

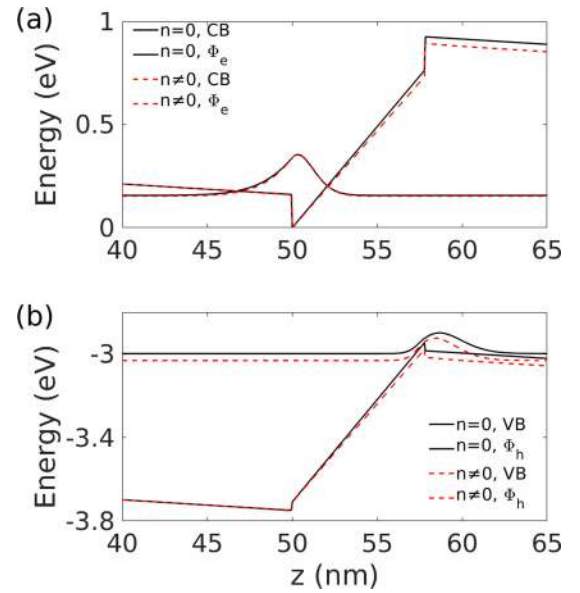


FIG. 11. Effect of the photoinjected carriers on the conduction (a) and valence (b) band diagram and wave function. The band profiles and wave functions are calculated for an empty QW (black lines) and for a pair density of $n = 2 \times 10^{11} \text{ cm}^{-2}$ (red dashed lines).

tilted in the presence of the carriers, due to the electrostatic screening effect. This implies the modification of both optical transition energy and the overlap $\Omega = \left| \int dz \Phi_e(z) \Phi_h(z) \right|^2$ between the electron and hole wave functions (Ω is proportional to the radiative emission rate).

The transition energy increases almost linearly with density (figure not shown), at least in the density limit of interest. The slope $\phi_0 = 1.50 \times 10^{-13} \text{ eV cm}^{-2}$ is obtained from the linear fitting procedure. It differs only slightly from the value given by a simple plate capacitor model:

$$\phi_0^{\text{PC}} = \frac{e^2 d}{\varepsilon} \approx 1.59 \cdot 10^{-13} \text{ eV cm}^{-2}. \quad (\text{A14})$$

This difference is due to the localization of the electron and hole wave functions in the inner part of the QW, which tends to reduce the effective QW width. The interaction energy E_{int} given by $E_{\text{int}} = \phi_0 n$ is shown in Fig. 13 by the black line.

b. Taking into account excitonic correlations (model C)

A more accurate estimate of the excitonic density from the energy shift is based on taking into account the repulsive interactions between excitons. This means that one should go beyond the assumption of the uniform distribution of charges in the plane of the QW, on which the plate capacitor and the Schrödinger-Poisson models are based.

The energy of an exciton in the field of its neighbors can be written as

$$E_{\text{int}}^{\text{corr}}(n, T) = \int n_\ell(r, T, n) U(r) d\mathbf{r}, \quad (\text{A15})$$

where $U(r) = \frac{2e^2}{4\pi\varepsilon} \left(\frac{1}{r} - \frac{1}{\sqrt{d^2+r^2}} \right)$ is the exciton-exciton interaction potential and $n_\ell(r, n, T)$ is the local density of excitons in equilibrium at temperature T and for a global density n .

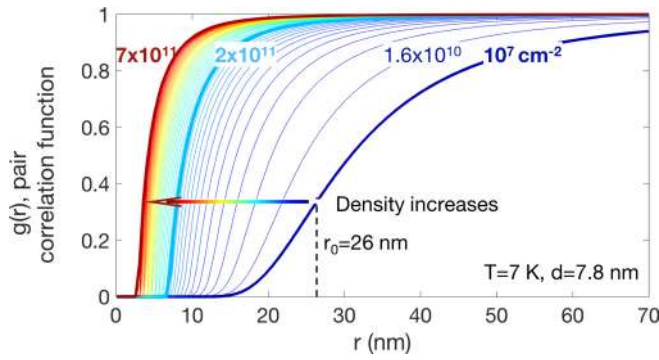


FIG. 12. Pair correlation function calculated for various values of the particle density at $T = 7$ K and dipole length $d = 7.8$ nm. Thick lines indicate the calculations in the low density limit ($n = 10^7$ cm $^{-2}$, dark blue), at Mott density estimated in this paper ($n = 2 \times 10^{11}$ cm $^{-2}$, cyan) and at $n = 7 \times 10^{11}$ cm $^{-2}$, corresponding to the saturation of $g(r)$. Dashed line points to r_0 , the mean-field exclusion radius given by Eq. (A17).

According to Refs. [38,76], this local quantity is given by the equation

$$1 - e^{-T_0(r)/T} = (1 - e^{-T_0^{(0)}/T})e^{-(U(r) + \phi_0(n_\ell - n))/(k_B T)}, \quad (\text{A16})$$

where $k_B T_0(r) = \pi \hbar^2 n_\ell(r, T, n)/2M$ represents the local chemical potential and $k_B T_0^{(0)} = \pi \hbar^2 n/(2M)$, represents chemical potential in the $r \rightarrow \infty$ limit.

The numerical resolution of this equation makes it possible to evaluate the local density $n_\ell(r, T, n)$. We push the numerical solution slightly further that the implementation presented in Ref. [76]. Our method is based on an adaptive calculation.

The solution $n_\ell(r, T, n)$ of Eq. (A16) is reinjected back in Eq. (A15). The resulting $E_{\text{int}}^{\text{corr}}(n, T)$ is used to replace the mean-field term $\phi_0(n_\ell - n)$ in Eq. (A16) by $E_{\text{int}}^{\text{corr}}(n_\ell, T) - E_{\text{int}}^{\text{corr}}(n, T)$. The procedure is repeated until convergence.

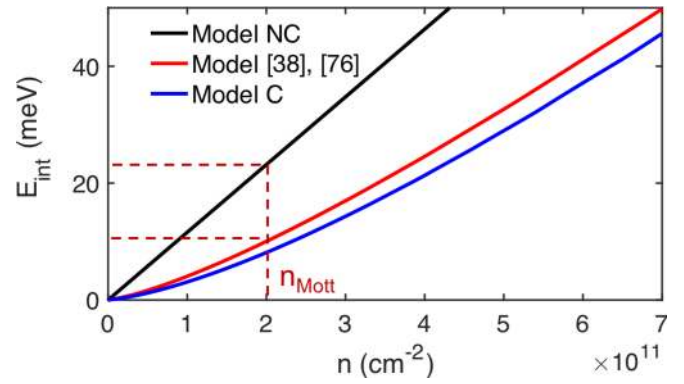


FIG. 13. (a) Interaction energy (or, equivalently, density-induced energy shift) as a function of particle density for $T = 7$ K. Model NC (self-consistent solution of the coupled Schrödinger and Poisson equations, Appendix 5a), black line; model C solved with (blue line) and without adaptive procedure, see Appendix 5b. Dashed lines indicate the estimated Mott density and the corresponding interaction-induced energy shift.

The density dependence of the pair correlation function $g(r) = n_\ell(r, T, n)/n$ obtained within this model is shown in Fig. 12. Because of the indirect nature of the excitons, a depletion area appears around each exciton. This area is characterized by an exclusion radius $r_0(T, n)$. One can clearly see in Fig. 12 that the shape of the $g(r)$ gets steeper when the pair density increases. At low density, the exclusion radius is given by the mean-field value

$$r_0(n = 0, T) = \left(\frac{e^2 d^2}{4\pi\epsilon k_B T} \right)^{1/3}, \quad (\text{A17})$$

that is, ~ 30 nm at 7 K, and it shrinks down up to ~ 5 nm at highest densities. Interaction energy $E_{\text{int}}(n, T)$ calculated within model C is shown in Fig. 13, for $T = 7$ K. The red line corresponds to the implementation Refs. [38,76] and the blue line to the adaptive calculation described above and implemented in the main text to estimate the densities.

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