

# Computer-Aided Diagnosis of Malignant Mammograms using Zernike Moments and SVM

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**Abstract** This work is directed toward the development of a computer-aided diagnosis (CAD) system to detect abnormalities or suspicious areas in digital mammograms and classify them as malignant or nonmalignant. Original mammogram is preprocessed to separate the breast region from its background. To work on the suspicious area of the breast, region of interest (ROI) patches of a fixed size of  $128 \times 128$  are extracted from the original large-sized digital mammograms. For training, patches are extracted manually from a preprocessed mammogram. For testing, patches are extracted from a highly dense area identified by clustering technique. For all extracted patches corresponding to a mammogram, Zernike moments of different orders are computed and stored as a feature vector. A support vector machine (SVM) is used to classify extracted ROI patches. The experimental study shows that the use of Zernike moments with order 20 and SVM classifier gives better results among other studies. The proposed system is tested on Image Retrieval In Medical Application (IRMA) reference dataset and Digital Database for Screening Mammography (DDSM) mammogram database. On IRMA reference dataset, it attains 99 % sensitivity and 99 % specificity, and on DDSM mammogram database, it obtained 97 % sensitivity and 96 % specificity. To verify the applicability of Zernike moments as a fitting texture descriptor, the performance of the proposed CAD system is compared with the

other well-known texture descriptors namely gray-level co-occurrence matrix (GLCM) and discrete cosine transform (DCT).

**Keywords** Computer-aided diagnosis (CAD) · Mammograms · Preprocessing · Segmentation · Zernike moments · Support vector machine (SVM)

## Introduction

Breast cancer has become one of the significant and frequent forms of cancer for women all over the world. Presently, risk factors of breast cancer cannot be avoided, and the survival rate of the patient is only related to early detection. A mammogram is an x-ray image of the breast tissue which allows better visualization of internal structure of the breast. Computer-aided techniques for detecting, classifying, and annotating diagnostic features on the mammogram images is a reliable tool for screening and early detection of breast cancer. The sensitivity of screening mammography is affected by image quality and the radiologist's level of expertise. It is difficult for the radiologists to provide both accurate and uniform evaluation for the huge number of mammograms generated in widespread screening. Lesions often occur in dense breast tissue areas in a number of different shapes such as circumscribed, speculate, lobulated, or ill-defined. Microcalcifications are deposited tiny calcium which accumulates in breast tissue [13]. It is shown that 90 % of impalpable ductal carcinomas in situ and 70 % of impalpable minimal carcinomas were visible as microcalcification alone [7]. Advance image processing can improve the odds of mammograms in detecting breast cancer early [28]. On an average, mammography detection rate of the breast cancer is 80–90 % [19]. High-resolution

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mammographic images can be used to detect the signs of breast cancer such as microcalcifications and masses. A fast and an efficient computer-aided diagnosis (CAD) system to detect the presence of microcalcifications and masses from the breast mammogram images is the need of the hour. It would be of great help to humanity especially for people living in those places where human expertise is not so easily available.

This work proposes a CAD system to classify malignant and nonmalignant mammogram patches. The study is focused on two different types of available datasets. One is a complete mammogram dataset, Digital Database for Screening Mammography (DDSM), and another is of mammogram patches (Image Retrieval In Medical Application (IRMA) reference). The rest of the paper is organized as follows. The “Literature Survey” section gives a brief review on mammogram-based CAD systems. The “Overview of the Proposed CAD System” section gives an overview of the proposed CAD system. Preprocessing steps for enhancement of mammogram image are described in the “Preprocessing” section. Region of interest (ROI) extraction technique is described in the “ROI Patch Extraction” section. The “Feature Extraction and Classification” section explains Zernike moments used as features along with support vector machine (SVM) used for mammogram classification. Experimental setup and results are summarized in the “Experimental Setup and Results” section. Finally, the “Conclusion” section concludes the work.

## Literature Survey

CAD for mammography began in the 1990s, and the first mammography CAD unit was approved in 1998 as a second reader [18, 27]. It has been shown that the performance of radiologists can be increased by providing them the results of a CAD system [3, 39]. Mammogram-based CAD systems were designed with the aim of increasing the effectiveness and efficiency of screening procedures. With the use of computer, diagnostic accuracy is improved by reducing the numbers of false-positive diagnoses of varying lesions in an objective manner. As shown in Fig. 1, four basic modules are required to develop a CAD system for breast cancer detection. In order to get a better diagnostic system, automatic segmentation, feature extraction, suspicious area detection, and classification techniques can be improved.

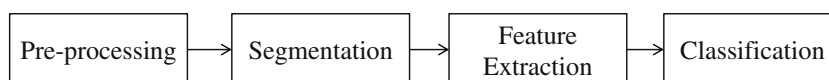
Preprocessing steps are very important to limit the search for abnormalities without undue influence from background

of the mammogram. Preprocessing involves removal of artifacts and unwanted parts from the background of the mammogram. Breast border contour extraction, pectoral muscle extraction, and nipple identification are also performed at this stage. Segmentation of breast mass plays an important role in the quantitative and qualitative analysis of mammograms. It has a direct impact on subsequent analysis and processing. The goal of segmentation is to isolate the ROI from the preprocessed image. Mammograms are rich with the presence of texture and shape. Hence, extraction of appropriate textural and shape features from extracted ROI is one of the necessary steps. Performance of the developed CAD system is measured by matching the features of query mammogram with the extracted stored features of the mammogram database.

Méndez et al. [32] developed a fully automatic technique to detect the border of the breast and the nipple. An algorithm that computes the gradient of gray levels is used to detect the breast border. To detect the nipple, three algorithms, maximum height of the breast border, maximum gradient, and maximum second derivative of the gray levels across the median top section of the breast, were used and compared. Yu and Guan [51] developed a CAD system that automatically detects the clustered microcalcifications in digitized mammograms. Wavelet and gray-level statistical features were used to categorize potential microcalcification objects according to their spatial connectivity. Table 1 summarizes most of the mammogram-based CAD systems developed in the last one and a half decades.

Verma and Zakos [47] presented a system for detection and classification of microcalcification in digital mammograms. They investigated and analyzed 14 feature extraction techniques with neural network classification. Bagui et al. [4] proposed a new generalization of the rank nearest neighbor (RNN) rule for the diagnosis of breast cancer from multivariate data. Cheng et al. [9] summarized enhancement and segmentation algorithms, mammographic features, and classifiers used in various stages of the CAD and compared their performances. They discussed and compared approaches for automatic mass detection and classification in mammograms. Ferrari et al. [15] proposed a segmentation technique for the fibro-glandular disc in mammograms using the Gaussian mixture modeling. The results were assessed by the radiologists using original and segmented image with referencing to a ranking table categorizing the segmentation result as excellent, good, average, poor, and complete failure. Ferrari et al. [16] presented a method for the identification of the pectoral muscle in MLO

**Fig. 1** Four main stages of a CAD system for breast cancer detection



**Table 1** Summary of some mammogram based CAD systems

Methods	Feature Vectors	Classifier	Database
Yu and Guan [51], 2000	Statistical features	MLFFNN	Nijmegen Database
Verma and Zakos [47], 2001	Entropy, standard deviation and number of pixels	BPNN	Nijmegen Database
Bagui et al. [4], 2003	Radius, texture, perimeter, area, smoothness, compactness, concavity, concave points, symmetry, fractal dimensions	<i>k</i> -NN	WDBC, WBC
Fu et al. [17], 2005	Texture, spatial and spectral domain	SVM	Nijmegen Database
Hwang and Kim [23], 2006	Zernike moments	–	–
Oliver et al. [35], 2007	Local binary patterns (LBP)	SVM	DDSM
Jasmine et al. [24], 2007	2D Wavelet transform	–	MIAS
Xu et al. [50], 2007	DWT	MLP	Private
Zhang et al. [52], 2008	Contrast, energy, entropy, standard deviation, skew, difference, average bound gray, average gray level, no. of pixels, and average histogram	BPNN	
Rabottino et al. [38], 2008	Shape and texture features	Fuzzy classifier	DDSM
Mencattini [31], 2009	Shape features	–	DDSM
Wang et al. [48], 2009	Zernike moment-mode shape descriptor	–	–
Rejani and Selvi [40], (2009)	Shape feature	SVM	MIAS
Alofe et al. [1], (2009)	Wavelet, first and second order statistics, shape and fractal dimensional features	SVM	MIAS
Mazurowski et al. [30], 2011	Histogram		DDSM, DBT
Zhang et al. [53], 2011	Shape features	<i>k</i> -NN	MIAS, DDSM
Xu et al. [49], 2011	Statistical and shape features	–	DDSM
Tahmasbi et al. [43], 2011	Shape features	MLP	MIAS
Oliveira et al. [33], 2011	Texture features	SVM	IRMA
Balakumaran and Vennila [5], 2011	Skewness, kurtosis and wavelet transform	–	DDSM
Deserno et al. [11], 2012	2DPCA	SVM	IRMA
Dheeba and Tamil [12], 2010	Gabor features	RBFNN	MIAS
Oliver [35], 2012	Local features based on morphology	Gentle boost Classifier	MIAS
Kabbadj et al. [25], 2012	Statistical and geometric features	SVM	MIAS
Shanthi and Bhaskaran [41], 2012	Mean, standard deviation, skewness, kurtosis, entropy	Self-adaptive resource Allocation network	MIAS
Cabrera et al. [20], 2012	Texture features	–	DDSM

mammograms using Gabor filters based on a multiresolution technique. A method for breast boundary identification in mammograms using active contour models is developed by Ferrari et al. [14] that can be used for the preprocessing of

mammogram. Fu et al. [17] proposed a two-stage procedure to detect microcalcifications.

Rangayyan et al. [39] gave an overview of techniques for detection and analysis of calcifications, masses, tumors,

bilateral asymmetry, and architectural distortion. Xu et al. [50] gave a new algorithm based on two artificial neural networks (ANNs). Rabottino et al. [38] proposed a region growing segmentation algorithm for mass contour extraction. Zhang et al. [52] developed a fully automated CAD system with the help of back propagation neural network (BPNN) technique. Alope et al. [1] proposed a CAD system based on SVM and linear discriminant analysis classification (LDA). Jasmine et al. [24] combined wavelet analysis of the image with ANNs for building the classifiers. Mencattini et al. [31] also introduced region growing tumoral mass segmentation and characterization algorithms by implementing uncertainty propagation through blocks. SVM has been a widely used classifier in medical diagnosis of mammography images [40]. Tang et al. [44] presented an overview of CAD systems and related techniques developed in the recent years such as radiological imaging. Dheeba and Tamil [12] developed a method with the help of Gabor features for detecting tumors in mammograms using RBFNN.

Balakumaran and Vennila [5] presented a multiresolution-based foveal algorithm for microcalcification detection. Mammograms were decomposed through wavelet transform without a sampling operator into different sub-bands, suppressing the coarsest approximation sub-band, and finally reconstructing the mammogram from the sub-bands containing only significant detailed information. Mazurowski et al. [30] developed a CAD system that uses mutual information-based template matching scheme with intelligently selected templates for diagnosing the mammographic masses. Tahmasbi et al. [43] developed a CADx system by utilizing Zernike moments as descriptors of shape and margin characteristics. Xu et al. [49] used traditional watershed transformation to obtain a boundary in the belt between the internal and external markers. The rough region of the lesion is identified by template matching and thresholding. Zhang et al. [53] applied a marker-controlled watershed algorithm on mammograms as an initial segmentation. Then, the contour line obtained by watershed is regarded as the initial curve, and a level set evolution without re-initialization is utilized for further segmentation.

It is well known that the best prevention method is early detection, but primary prevention in early stages of the disease becomes complex as the causes remain almost unknown. Nevertheless, some typical signatures of this disease can be targeted such as masses and microcalcifications appearing on mammograms, which can be used to improve early diagnostic techniques. As a result, most of the techniques focus on two types of breast cancer: microcalcifications and masses [20]. Oliver et al. [35] presented a knowledge-based approach for automatic detection of microcalcifications and clusters in mammographic images by using local features extracted from a bank of

filters to obtain a local description of the microcalcifications morphology. Kabbadj et al. [25] also presented a novel approach to detect microcalcifications on digitized mammograms using shape features, fuzzy logic, and SVM. Deserno et al. [11] proposed a CAD system which classifies the suspicious tissue pattern based on the SVM. Shanthy and Bhaskaran [41] proposed an integrated methodology of intuitionistic fuzzy C-means clustering, discrete wavelet feature extraction technique, and a self-adaptive resource allocation network classifier for automatic detection and classification of breast cancer in mammogram images. Oliveira et al. [35] developed content-based image retrieval (CBIR) system in support with the classification of breast tissue density which can be used in the processing chain for lesion segmentation and classification.

Maitra et al. [29] enhanced the contrast of mammogram by using the contrast-limited adaptive histogram equalization (CLAHE) technique initially. Then a rectangle is defined to isolate the pectoral muscle from the ROI, and finally, the pectoral muscle was suppressed by using the modified seeded region growing (SRG) algorithm. The algorithm separates background region and removes the pectoral muscle to accentuate the breast profile region.

## Overview of the Proposed CAD System

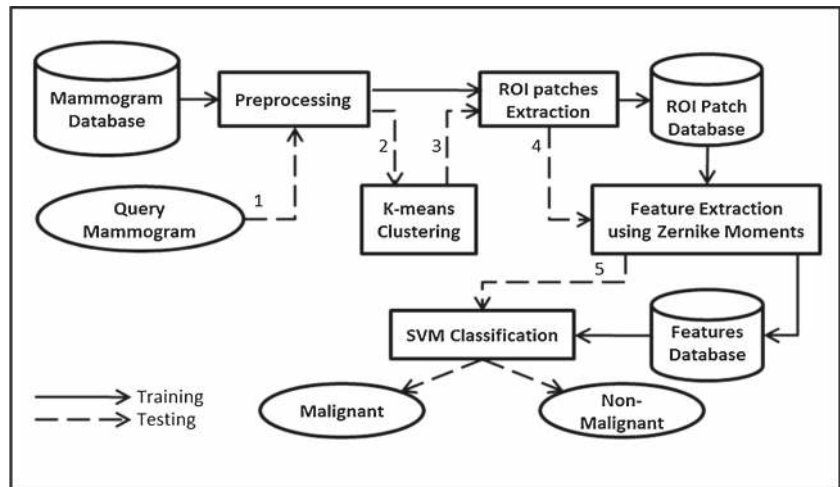
Figure 2 gives the block diagram of the proposed CAD system for large-sized full mammogram images. An image may contain several regions to examine, and the efficiency of the system depends on the successful identification of these ROI patches. These ROI patches are analyzed for the presence of malignancy.

The system works through several consecutive steps, which are visualized in Fig. 2. Here, *solid lines* are representing the steps followed for training of the system and *dashed lines* are representing the steps for testing. The four basic modules, preprocessing, ROI patches extraction, feature extraction, and classification, are discussed in detail in the following subsections.

### Preprocessing

The presence of a lot of irrelevant and futile information can be noticed in the mammogram images shown in Fig. 3. The objective of preprocessing is to improve the quality of image in order to limit the search for abnormalities by removing artifacts and unwanted parts without having undue influence on the background of mammograms [37]. Preprocessing aims to enlarge the intensity difference between objects and background to produce reliable representation of breast tissue structures. Preprocessing not only removes the noise

**Fig. 2** Block diagram of the proposed CAD system



but also finds the orientation of the mammogram [29]. Preprocessing also helps in the standardization of the mammogram image along with the reduction of its size without losing the useful information required for any CAD system.

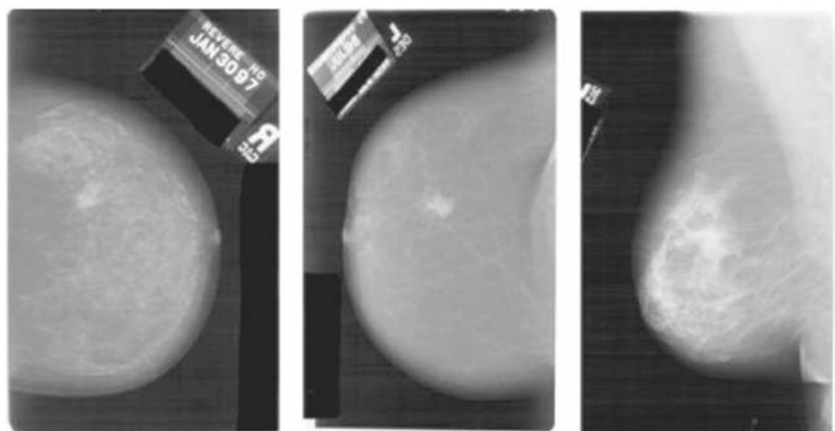
Preprocessing steps consist of scaling, binarization, erosion, and region identification. The effect of each step on a mammogram image is shown in Fig. 4. Due to their large size, mammograms are rescaled for further analysis. Original mammograms from the DDSM dataset are of  $4,000 \times 3,000$  pixel resolution, which is scaled down to  $1,024 \times 1,024$  pixels using the nearest-neighbor interpolation method. Binary erosion is applied to remove the “small” objects present in the binary image for cleaning the background texture. A disk-type structuring element is used here. Even after applying binary erosion, sometimes the binary image may contain some small-sized irrelevant components. In the binarized image, the large foreground area is of the breast that contains the useful information. Therefore, in the eroded binary image, connected components (of white color) are identified as regions, and the region with the maximum area is considered as a final mask image.

Exterior boundary of the region is traced using a mask image and is plotted on the original image using the same pixel coordinate values. This mask image is superimposed on the original image to get clear boundary of the breast area in the image. Some of the results obtained with this preprocessing method are shown in Fig. 5.

### ROI Patch Extraction

A mammogram image is very large in size consisting of both useful and nonuseful information. Instead of processing a complete mammogram, focus is enlightened only on the area containing some abnormality (intensity variations). The ROI is an abnormal region on the mammogram, segmented on the basis of visual textural information. ROI patches of  $128 \times 128$  pixels are extracted from the segmented region and are used for training and testing purposes. A mammogram may contain many such patches. Extracting patches from the segmented regions also limits the processing time and speed of the system. Figure 6 shows ROI patches extracted from the preprocessed mammogram

**Fig. 3** Original mammograms containing noise and useless information [22]



**Fig. 4** Results of intermediate stages of preprocessing **a** scaled mammogram, **b** binarization, **c** binary eroded image with an identified region, and **d** preprocessed image

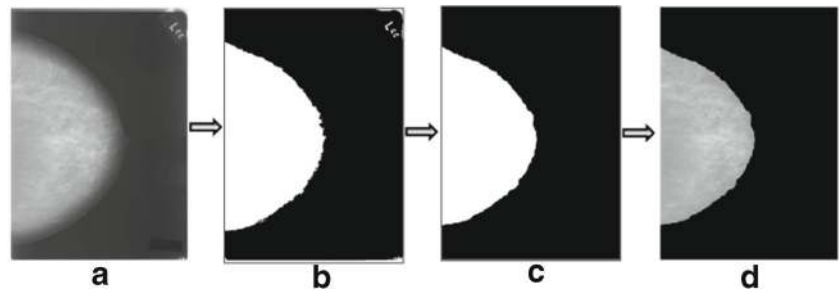
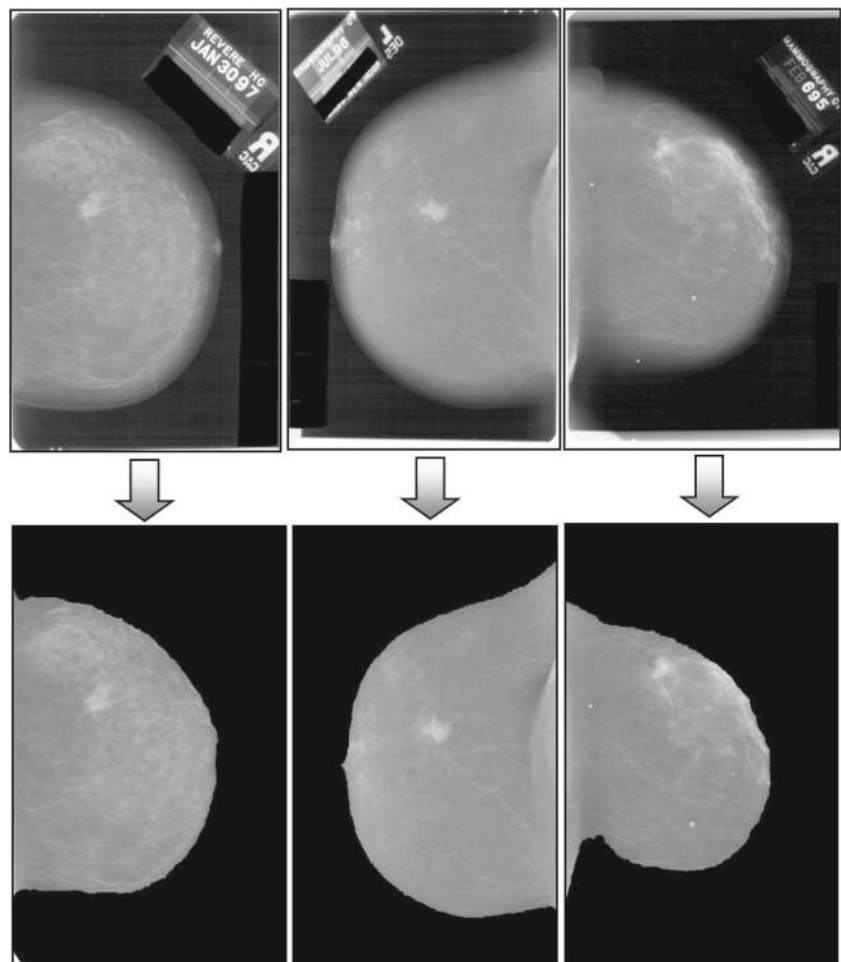


image. Patches are extracted in two different ways for training and testing separately. In training, the patches are extracted by selecting abnormal regions manually; while for testing, patches are extracted manually from the dense areas of the mammograms which are identified by *k*-means clustering automatically. Manual selection is a time-consuming task but promises a better result. Patches belonging to the respective classes are stored separately to facilitate training of the system.

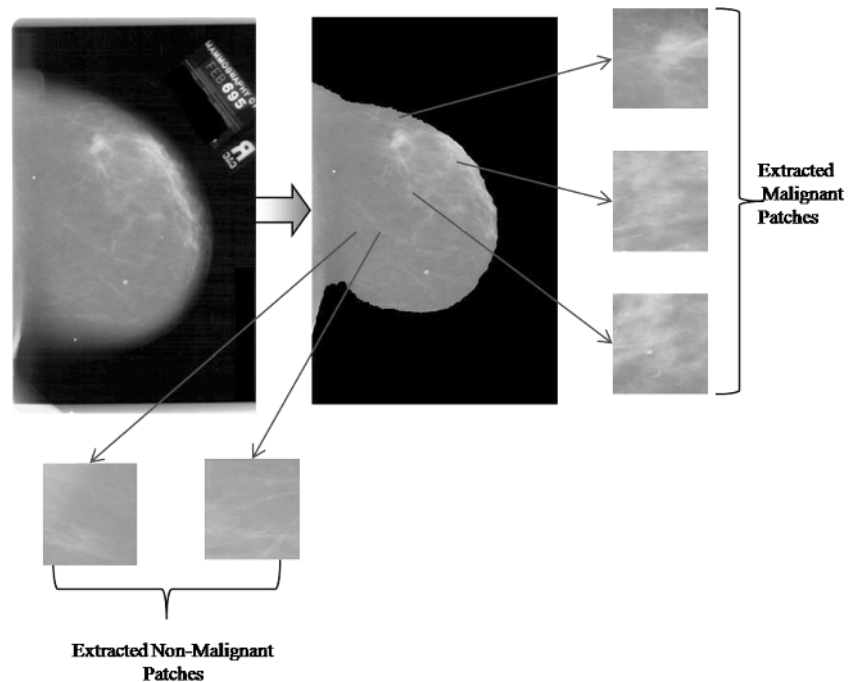
#### Dense Area Identification in Test Mammogram

The present work uses image enhancement followed by *k*-means algorithm to cluster pixels. Further, the concept of entropy is used to identify dense clusters. ROI patches of size  $128 \times 128$  pixels are extracted from these dense areas and are further classified as malignant/nonmalignant. The process of cluster identification for ROI patch extraction is shown in Fig. 7.

**Fig. 5** Original and preprocessed mammograms. The *first row* shows the original mammograms, and the *second row* shows preprocessed mammograms of the corresponding images



**Fig. 6** From left to right: original mammogram, preprocessed mammogram, and extracted patches from the preprocessed mammogram



The preprocessed image is further enhanced through histogram equalization to emphasize certain interesting features of the image and restraining indifferent characteristics. Gray-scale erosion applied on the enhanced image shrinks the area of the foreground pixels and enlarges the holes within that area. The resultant eroded image is used for image reconstruction to remove the fine lines, or noncancerous parts, and enhances the visibility of malignant mass. Let enhanced image be represented as  $I_e$  and its eroded image be represented by  $I_{er}$ . *Morphological reconstruction* (MR) of the image component from the eroded image is defined as follows:

$$MR(I_e)(I_{er}) \equiv (\text{connected component of } I_e \text{ containing } I_{er}) \tag{1}$$

In reconstruction,  $I_{er}$  is used as a marker image and  $I_e$  as a mask image [6]. Figure 7(d) shows the enhanced image after reconstruction. This is a smooth image as compared to the image given in Fig. 7(b).

Although it has been observed that many similar and adjacent components are still unconnected, gray-scale dilation is applied to connect these components. Morphological reconstruction (MR) of the image component from the dilated image is done in a similar way as given in Eq. 1. Figure 7(f) is the resultant image.

Three types of components with different shades of gray are identified from the image shown in Fig. 7(f), i.e., light gray, gray, and dark gray. These components, regions of masses, normal, and dense tissues are required to be separated and checked for the malignancy.  $k$ -means clustering is applied to form clusters of these components.  $k$ -means

algorithm is an unsupervised clustering algorithm that is used in this work to cluster gray levels of input image. The algorithm assumes that gray levels of input 2D image form 1D vector space and tries to find natural clustering in them [45]. The gray values of image are clustered around mean gray value of cluster  $c_i \forall i = 1, 2, \dots, k$  which are obtained by minimizing the objective function:

$$\min \left[ \sum_{i=1}^k \sum_{x_j \in s_i} \|x_j - c_i\| \right] \tag{2}$$

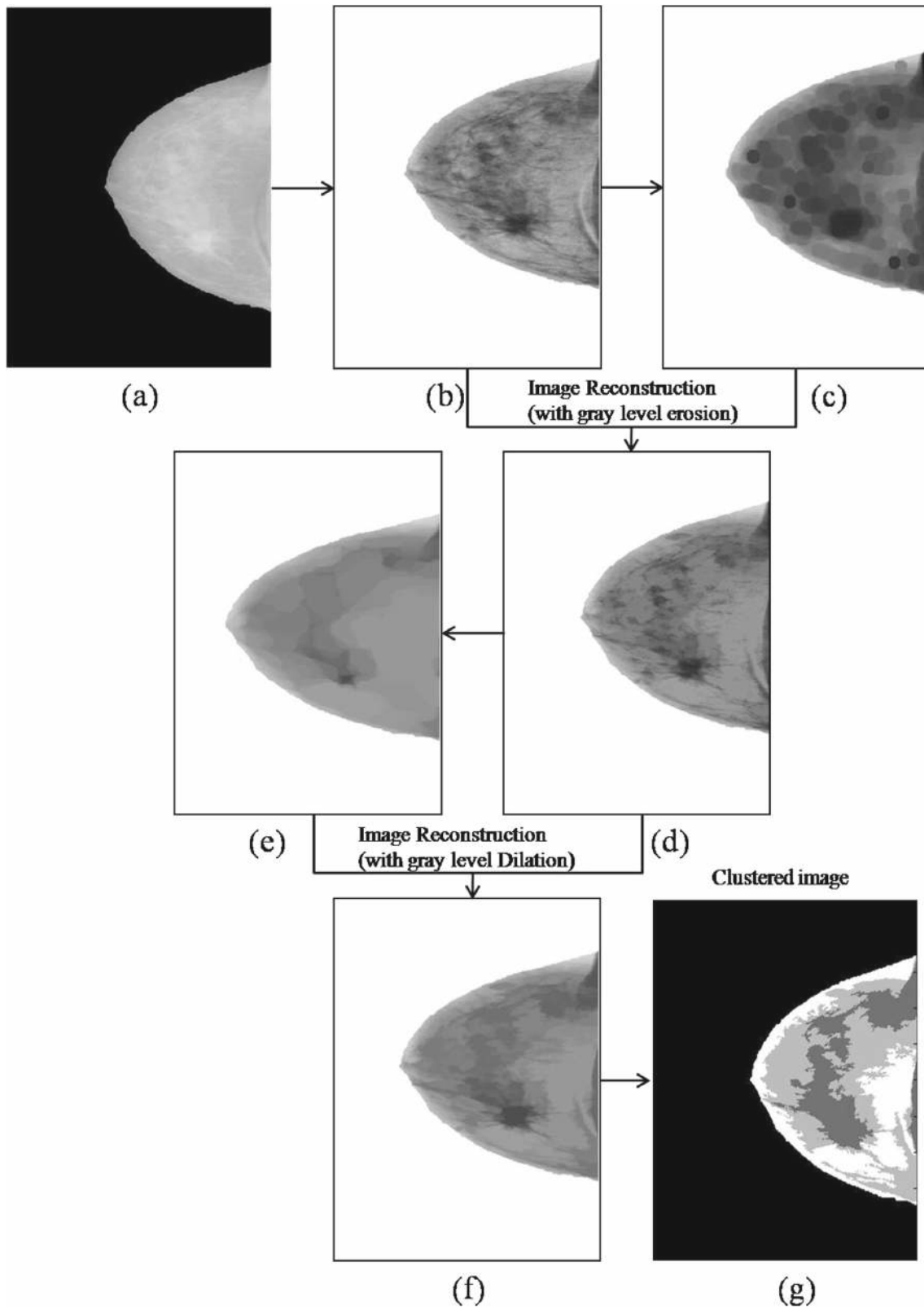
This method can be applied for the clustering of the same type of components present in the mammogram image in the following way:

- Initialize  $k$ -clusters  $s_i (i = 1, 2, \dots, k)$  with a random mean gray value  $(c_1, c_2, \dots, c_k)$ .
- Each pixel of the image is assigned to its closed cluster based on the distance between its gray value from mean gray value of the cluster.
- Compute the new mean gray value of each cluster.

$$new(c_i) = \frac{\sum_{x_i \in s_i} x_i}{\text{number of pixels belong to } i\text{th cluster}} \tag{3}$$

- where  $x_i$  is gray values of set of pixels which belong to cluster  $s_i$ .
- Repeat steps 2 and 3 until the cluster labels do not change anymore.

Entropy is the measure of randomness present in the image. Entropy of these clusters is calculated from the



**Fig. 7** Cluster identification for ROI patch extraction



distribution of gray-level intensities of corresponding pixel clusters in preprocessed query mammogram (Fig. 8).

$$\text{Entropy of } i\text{th cluster} = - \sum_{x_i \in S_i} x_i P(x_i) \log P(x_i) \quad (4)$$

A cluster having a maximum entropy represents the presence of more texture information. The patches obtained from this cluster are required to be tested for malignancy. The centroid of this cluster is taken as a reference point, and patches of size  $128 \times 128$  are extracted from preprocessed mammogram as shown in Fig. 8.

### Feature Extraction and Classification

This work utilizes the properties of Zernike moments to analyze texture properties of ROI patches. Zernike moments are rotation invariant, nonredundant, robust to noise and shape, and have a multilevel representation [21, 23, 43, 48]. An image can be better described by a small set of its Zernike moments than any other types of moments such as geometric moments, Legendre moments, rotational moments, and complex moments in terms of mean-square error.

#### Zernike Moments

Mapping of an image onto a set of complex Zernike polynomials are Zernike moments. Zernike polynomials are orthogonal to each other in nature, and therefore, they can represent the properties of an image with no redundancy or overlap of information between the moments [43, 48]. The procedure for obtaining Zernike moments from an input image begins with the computation of Zernike radial polynomials. It consists of three steps:

- computation of radial polynomials
- computation of Zernike basis functions

- computation of Zernike moments by projecting the image on to the basis functions

The real-valued 1D radial polynomial is defined as

$$R_{pq}(r) = \sum_{k=0}^{\frac{p-|q|}{2}} (-1)^k \frac{(p-k)!}{k! \left(\frac{p+|q|}{2} - k\right)! \left(\frac{p-|q|}{2} - k\right)!} r^{(p-2k)} \quad (5)$$

where  $p$  is a nonnegative integer representing the order of the radial polynomial, and  $q$  is a positive or negative integer satisfying that  $p \geq 0$ ,  $0 \leq q \leq p$ , and  $p - |q|$  are even. Complex-valued 2D Zernike basis functions within a unit circle using the radial polynomial are defined as

$$V_{pq}(r, \theta) = R_{pq}(r) e^{-jq\theta}; j = \sqrt{-1}, |r| \leq 1 \quad (6)$$

Zernike basis function satisfies orthogonality condition as

$$\int_0^{2\pi} \int_0^1 V_{pq}^*(r, \theta) V_{nm}(r, \theta) r dr d\theta = \begin{cases} \frac{\pi}{p+1} & \text{if } p = n, q = m \\ 0 & \text{otherwise} \end{cases} \quad (7)$$

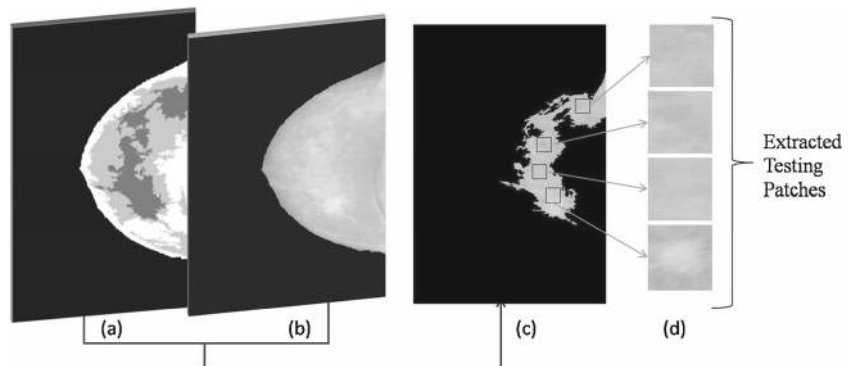
Complex Zernike moments of order  $p$  with repetition  $q$  are finally defined as

$$Z_{pq} = \frac{p+1}{\pi} \int_0^{2\pi} \int_0^1 f(r, \theta) V_{pq}^*(r, \theta) r dr d\theta; |r| \leq 1 \quad (8)$$

where  $f(r, \theta)$  is polar form of  $f(x, y)$  image function, and  $*$  denotes the complex conjugate. To compute Zernike moments from a digital image, the integrals in Eq. 8 are replaced by summations and the coordinates of the image must be normalized by a mapping transform. The discrete form of Zernike moments for an image of size  $N \times N$  is expressed as follows:

$$Z_{pq} = \frac{(p+1)}{\lambda_N} \sum_{x=0}^{N-1} \sum_{y=0}^{N-1} f(x, y) V_{pq}^*(x, y) \quad (9)$$

**Fig. 8** ROI patch extraction for testing (a) clustered image, (b) preprocessed mammogram, (c) segmented image, and (d) extracted patches



$$Z_{pq} = \frac{(p+1)}{\lambda_N} \sum_{x=0}^{N-1} \sum_{y=0}^{N-1} f(x, y) R_{pq}(x, y) e^{-jq\theta_{xy}} \quad (10)$$

where  $0 \leq r_{xy} \leq 1$ , and normalization factor  $\lambda_N$  must be the number of pixels located in the unit circle  $\pi$  in the continuous domain. The transform distance  $r_{xy}$ , and the phase  $\theta_{xy}$ , at the pixel  $(x, y)$  are calculated as

$$r_{xy} = \frac{\sqrt{(2x - N + 1)^2 + (2y - N + 1)^2}}{N} \quad (11)$$

$$\theta_{xy} = \tan^{-1} \left( \frac{N - 1 - 2x}{2y - N + 1} \right) \quad (12)$$

Zernike moments are extremely dependent on the scale factor and translation of objects. Their magnitude is independent of the angle of rotation [26]. Therefore, the magnitude of the Zernike moment can be used as a descriptor to describe the characteristics of texture regardless of the rotation of the mass. Rotating the object around the Z-axis does not influence the magnitude response of the Zernike moments but influences only the phase response of Zernike moments [26]. It can also be explained as Eq. 13:

$$Z_{pq}^x = Z_{pq} e^{-jq\alpha} |Z_{pq}^x| = |Z_{pq}| \quad (13)$$

where  $Z_{pq}^x$  and  $Z_{pq}$  are moments extracted from the rotated object with an angle  $\alpha$  and from the original object, respectively. Thus, the magnitudes of Zernike moments are proposed as features in this work.

### Support Vector Machine

In the field of medical sciences, SVM has proved to be a good classifier in the diagnosis of mammograms [5]. SVM is a supervised learning algorithm based on the concept of hyperplane that aims to separate a set of objects with maximum margin. SVM determines some support vectors from the feature space which are helpful to determine the optimal hyperplane [10].

Let  $X\{x_1, x_2 \dots x_N\}$  be a training set containing  $N$  feature vectors in  $d$ -dimensional feature space and associated with two class labels  $z_i \in \{-1, +1\}$ . For this work, two classes, malignant and nonmalignant, are labeled as  $(+1)$  and  $(-1)$ , respectively. Two-class linear separable task is

accomplished by defining a hyperplane that separates these feature vectors as follows:

$$\omega \cdot x_i + b \geq +1 \text{ for } z_i = +1 \quad (14)$$

$$\omega \cdot x_i + b \leq -1 \text{ for } z_i = -1 \quad (15)$$

These equations can be expressed in the general form as

$$z_i(\omega x_i + b) \geq 1, \quad i = 1, 2, 3, \dots, N \quad (16)$$

The distance between two hyperplanes is  $\frac{2}{\|\omega\|}$ . To get a better separation between the classes, this distance should be maximized by minimizing  $\|\omega\|$  by using the Lagrangian function. Application of the Lagrangian function as given in Eq. 17 gives the most suitable optimal hyperplane.

$$f(x) = \sum_{i=1}^N \alpha_i w_i(x_i \cdot x) + b \quad (17)$$

where  $\alpha_i$  is the Lagrange multiplier of a dual optimization problem that describes the separating hyperplane  $w_i(x_i \cdot x)$  and  $b$  is the threshold parameter of the hyperplane. If  $f(x) \geq 0$ , then  $x$  is classified as a member of the class  $+1$ ; otherwise, it would be classified as a member of the second class  $(-1)$  [10]. This discrimination function will not work for linearly nonseparable dataset. Therefore, the kernel function is applied to get the optimal hyperplane in nonseparable datasets. SVM uses kernel function to map nonseparable data into kernel space. The resulting discrimination function is formally the same, except that every dot product used earlier is replaced by a nonlinear kernel function as follows:

$$f(x) = \sum_{i=1}^N \alpha_i w_i k(x_i \cdot x) + b \quad (18)$$

As this is a linear nonseparable problem, the radial basis function (RBF) kernel given in Eq. 19 is used here to map the dataset into linear separable feature space.

$$k(x_i \cdot x) = \exp(-\lambda \|x_i - x\|^2) \text{ for } \lambda > 0 \quad (19)$$

**Table 2** Summary of the databases used for experimentation

Databases	Number of mammograms	Number of patches	Training cases		Testing cases	
			Malignant	Nonmalignant	malignant	Nonmalignant
IRMA reference (DDSMpatches)	–	800	178	88	360	174
DDSM	200	1,264	285	135	572	272

**Table 3** Sensitivity and specificity achieved with the proposed CAD system

Dataset	Order of Zernike moments	<i>k</i> -NN		SVM	
		Sensitivity	Specificity	Sensitivity	Specificity
IRMA reference DDSM	20	0.83	0.77	0.99	0.99
	25	0.94	0.90	0.97	0.96
	30	0.95	0.91	0.94	0.94
	35	0.97	0.92	0.91	0.91
DDSM	20	0.89	0.88	0.96	0.96
	25	0.90	0.89	0.92	0.90
	30	0.92	0.90	0.91	0.90
	35	0.94	0.93	0.89	0.90

### Experimental Setup and Results

#### Mammogram Datasets

The proposed CAD system is validated by performing experiments on the following two datasets of mammograms.

#### IRMA reference database (DDSM mammographic patches)

Out of 800 patches taken from classes 1 and 5, 534 belong to class 5 and the remaining 266 belong to class 1. The data for training and testing has been separated into a ratio of 1:2. The system is trained with 178 malignant patches and 88 normal patches. The remaining 360 malignant and 174 normal patches are taken for testing.

#### DDSM mammogram database

A total of 200 mammograms (80 from class 1 and 120 from class 5) are taken. From these 200 mammograms, 1,264 patches are extracted, out of which 407 belongs to class 1 and the remaining to class 5. For this database also, the training-testing ratio is maintained to 1:2. Accordingly, 135 normal and 285 malignant patches are used to train the system. Testing is then performed on the remaining 272 and 572 patches from normal (class 1) and malignant (class 5) categories, respectively. This distribution of mammograms is tabulated in Table 2.

**Table 4** Results obtained with different texture features on IRMA reference dataset (DDSM patches)

Feature vector	<i>k</i> -NN		SVM	
	Sensitivity	Specificity	Sensitivity	Specificity
GLCM	0.67	0.72	0.90	0.93
DCT	0.54	0.61	0.78	0.78
Zernike	0.83	0.87	0.99	0.99

#### Performance Measures

Performance of the proposed CAD system is evaluated in terms of sensitivity and specificity. *Sensitivity* measures the proportion of actual positives which are correctly identified as malignant, and *specificity* measures the proportion of actual negative which are correctly identified as nonmalignant negative. These are calculated as follows:

$$Sensitivity = \frac{TP}{(TP + FN)} \tag{20}$$

$$Specificity = \frac{TN}{(FP + TN)} \tag{21}$$

where, TP, FP, TN, and FN denote true positive, false positive, true negative, and false negative, respectively.

#### Experiment Results

Features are generated with different orders of Zernike moments. The aim is to achieve a higher sensitivity rate with as small feature size as possible. It has been observed that with *k*-NN classifier sensitivity of the proposed CAD system was low with low-order moments (below 20), but it increases with increasing order of moments. With SVM classifier sensitivity increases up to moments of order 20, but decreases with high-order moments. Table 3 compares

**Table 5** Comparison with other techniques

Methods	Features	Classifier	Dataset	Results
Proposed method	Zernike (texture descriptor)	SVM	IRMA reference DDSM	99 % Sensitivity 99 % specificity
Proposed method	Zernike (texture descriptor)	SVM	DDSM	96 % Sensitivity 96 % specificity
Tahmasbi et al. [43]	Zernike (shape descriptor)	MLP	MIAS	97.6 % Area under curve
Deserno et al. [11]	2DPCA	SVM	IRMA reference DDSM	80.07 % Accuracy
Alolfe et al. [2]	Texture and shape	<i>k</i> -NN	DDSM	71.93 % Sensitivity 75 % specificity
Oliver et al. [35]	Local morphological	Gentle boost classifier	MIAS, DDSM	80 % Area under curve
Oliver et al. [34]	Local binary pattern (LBP)	SVM	DDSM	90 % Value index curve
Subashini et al. [42]	Statistical	SVM	MIAS	94 % Accuracy
Varela et al. [46]	Gray level, contour-related, and morphological	BPN	Private	94 % Sensitivity
Polakowski et al. [36]	Size, shape, and texture	MLP	Private	92 % TPR/FPR

the classification rates of both the classifiers with different orders of Zernike moments on the two datasets. All results of *k*-NN classifier are generated with  $k = 10$ . RBF kernel function is used for SVM classifier.

It is evident from Table 3 that SVM classifier performs better as compared to *k*-NN classifier. It gives a better classification rate at a small feature size. In general, a method is accurate if the percentage of both sensitivity and specificity is greater than 95 %. The system achieves 99 % TP rate for IRMA reference dataset (DDSM patches) with Zernike moments of order 20 and SVM classifier. It also gives 96 % TP rate for DDSM mammogram images. Achieving more than 96 % sensitivity and specificity at the moments of order 20 shows that the system is computationally efficient.

Table 4 compares features obtained with the Zernike moment sensitivity with two other well-known texture features: gray-level co-occurrence matrix (GLCM) and discrete cosine transform (DCT) for IRMA reference dataset (DDSM patches). GLCM gives 90 % sensitivity with SVM classifier, while the proposed system with Zernike moment gives 99 % sensitivity for the same dataset. The performance of the system with DCT features is only 78 %, which is not up to the mark. This shows that the proposed system performs well with Zernike moments used as features.

Objective comparison of the performance of different CAD methods is difficult due to the use of different datasets,

feature sets, and classification methods [8]. Even if a common dataset is used to test different methods, different preprocessing steps used by various researchers lead to development of CAD systems with varied accuracy. In most of the works, the size of feature vector is not mentioned, which is an important aspect in case the system is to be deployed for real-time applications. Moreover, different performance measures are used by researchers, and hence, a direct comparison of approaches is not possible. In order to compare different CAD systems, Table 5 summarizes the performance of the proposed system along with other existing methods in this field. Although various classifiers are used in these works, it is clearly visible that most of the existing methods rely on the SVM classifier. The results achieved by the proposed system are quite promising.

## Conclusion

This work proposes a CAD system to classify malignant and nonmalignant mammogram patches. Suitable methods are suggested for preprocessing, which not only removes the artifacts, unwanted components, and extracts the breast region from its background but also helps to extract abnormal regions from mammograms. To avoid processing of whole mammogram, methods to extract fix-sized ROI

patches are also proposed. The Zernike moments-based texture feature extraction technique is used to recognize the pattern of malignancy/nonmalignancy in the mammogram patches. The variations in the results are observed by experimenting with the low- and high-order Zernike moments. Experiments are performed with other well-known texture descriptors GLCM and DCT, and it is observed that the proposed CAD system works well with Zernike moments. SVM with RBF kernel attains the highest sensitivity and specificity values at lower orders of Zernike moments. The proposed CAD system improves the accuracy of diagnosis and promises to perform a second-reader role.

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