

# Constraining the internal dynamics of stellar systems using the NMAGIC particle code

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**Abstract.** NMAGIC is a parallel implementation of our made-to-measure ( $\chi^2$ M2M) algorithm for constructing N-particle models of stellar systems from observational data, which extends earlier ideas by Syer & Tremaine (1996). The  $\chi^2$ M2M algorithm properly accounts for observational errors, is flexible, and can be applied to various systems and geometries. We show its ability to reproduce the internal dynamics of an oblate isotropic rotator model and report on the modeling of the dark matter (DM) halo of NGC 3379 combining SAURON and P.N.S kinematic data. The  $\chi^2$ M2M algorithm is practical, reliable and can be applied to various dynamical systems without symmetry restrictions. We conclude that  $\chi^2$ M2M holds great promise for unraveling the internal dynamics of bulges.

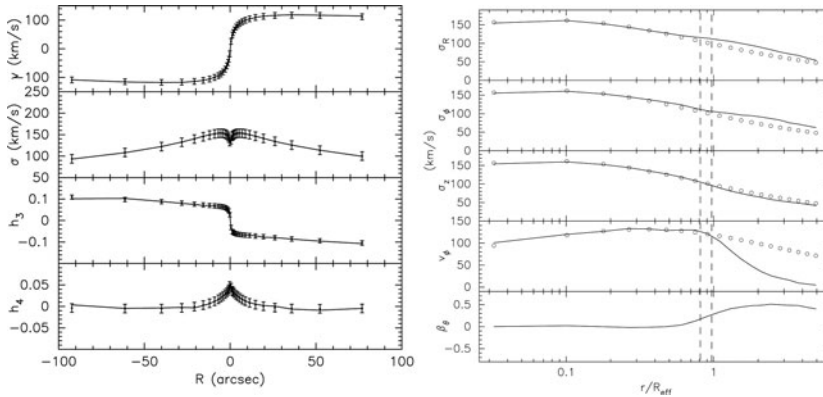
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## 1. Introduction

Syer & Tremaine (1996) invented a method to construct “made-to-measure” (M2M) particle models of stellar systems. The M2M method works by gradually changing the weights of the particles with time, until the model reproduces a set of observational constraints. Bissantz *et al.* (2004) made a first practical application of the M2M method and modeled the face-on density distribution of the Milky Way. Their model was able to match the microlensing event timescale distribution towards the galactic bulge. De Lorenzi *et al.* (2007) improved the M2M algorithm to account for observational errors and implemented their  $\chi^2$ M2M algorithm in a parallel code NMAGIC. Here, after describing some tests of the method, we report on one of the first applications of NMAGIC, modeling the halo of the elliptical galaxy NGC 3379.

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**Figure 1.** (a) Left: NAGIC model fit to the isotropic rotator mock kinematic data along the major axis. The data points show the target data and the lines represent the model. (b) Right: Internal velocity moments and anisotropy parameter  $\beta_\theta = 1 - \sigma_\theta^2/\sigma_r^2$  in the meridional plane for the self-consistent isotropic rotator model. The data points represent the input model and the lines correspond to the final particle model. The dashed lines indicate the extent of the data on both sides of the major axis.

## 2. Testing NAGIC with isotropic rotator models

We test our modeling with an axisymmetric, isotropic rotator model with known intrinsic properties. We have chosen to describe the luminosity density of the mock galaxy by one of the flattened  $\gamma$ -models of Dehnen & Gerhard (1994):

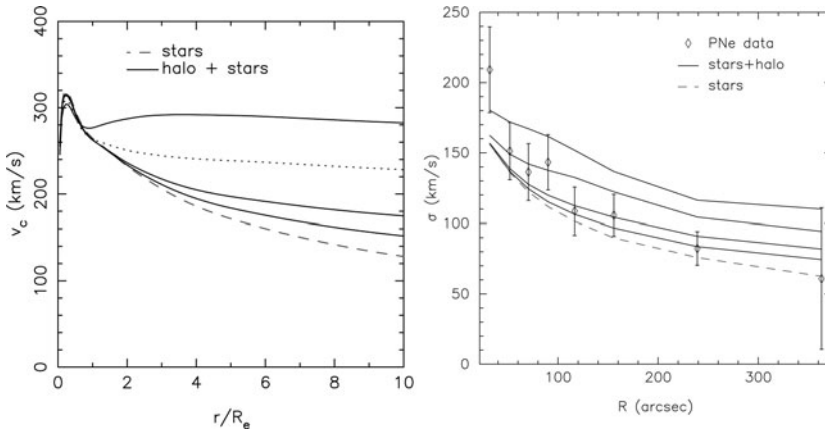
$$j(m) = \frac{(3 - \gamma)L}{4\pi q} \frac{a}{m^\gamma (m + a)^{4-\gamma}}, \quad (2.1)$$

where  $L$  and  $a$  are the total light and scale radius,  $m^2 = R^2 + (z/q)^2$ , with the flattening  $q=0.7$ ,  $\gamma=1.5$ ,  $L=2 \times 10^{10} L_{\odot,R}$  and  $a=2.5$  kpc ( $a \approx 49''$  for the adopted distance  $D=10.5$  Mpc). We further assume that the galaxy is seen under  $i=80^\circ$ . For this target model, we compute photometric and kinematic observables, which are then used as constraints in building the particle model with NAGIC. The photometric observables are given by a spherical harmonics decomposition of the luminosity density given in equation 2.1. The target kinematics are computed from internal velocity moments obeying higher-order Jeans equations (Magorrian & Binney 1994) in the self-consistent potential generated by the density, assuming a mass-to-light ratio  $\Upsilon = 5$ .

We construct a self-consistent particle model in a two step process. First, we start with spherical initial conditions made from distribution function (Debattista & Sellwood 2000) and evolve it using NAGIC to generate a self-consistent particle realization with the desired luminosity distribution ( $\gamma$ -particle model), fitting only the luminosity constraints. We then switch retrograde particles of the  $\gamma$ -particle model with a probability

$$p(L_z) = p_0 \frac{L_z^2}{L_z^2 + L_0^2}, \quad (2.2)$$

where  $p_0 = 0.3$  and  $L_0 = 0.02$  given in internal units. We then use the rotating, anisotropic  $\gamma$ -particle model as a starting point for a self-consistent model fit to the photometric and kinematic constraints. Figure 1 shows the fit to the kinematic data achieved by the final particle model, and compares the intrinsic velocity moments of the input model with those of the particle model. The input model is well reproduced within the constraint region.



**Figure 2.** (a) Left: Circular velocity curves for mass models consisting of the stellar mass distribution of NGC 3379 plus various logarithmic DM halo profiles. The self-consistent model is shown by the dashed line. (b) Right: PN.S velocity dispersion data of NGC 3379 with superimposed spherical NMAGIC fits using the mass models of the left panel.

### 3. NGC 3379

We now use NMAGIC to construct spherical and axisymmetric dynamical models of NGC 3379, the strongest case of Romanowsky *et al.* (2003) for a diffuse DM halo. NGC 3379 is an intermediate luminosity E1 galaxy with distance  $D = 9.8$  Mpc and effective radius  $R_e = 47''$ . We generate NMAGIC models including various DM halos as illustrated by the circular velocity curves in the left panel of Figure 2. We constrain the models using wide field B-band photometry of Capaccioli *et al.* (1990) combined with the HST V-band observations of the inner  $10''$  of Gebhardt *et al.* (2000), SAURON integral field kinematics from Shapiro *et al.* (2006), and PN.S kinematic data from Douglas *et al.* (2007).

#### 3.1. Spherical models

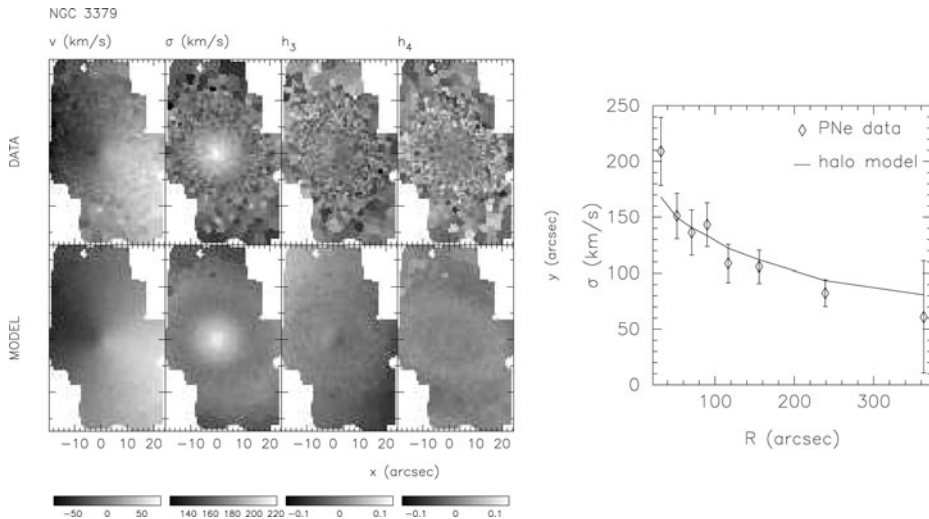
The right panel of Figure 2 shows the PN.S velocity dispersion data with superimposed spherical NMAGIC fits using the mass models shown in the left panel of Figure 2. The spherical models fit the combined data only in the presence of a diffuse DM halo.

#### 3.2. Oblate models

There is some evidence that NGC 3379 is non-spherical (*e.g.* Statler 2001, and the cold ring in  $\sigma$  of the SAURON data shown in Figure 3 at  $R \approx 15''$ ). Therefore, we construct an axisymmetric dynamical model, assuming an inclination  $i = 40^\circ$  and including the DM halo indicated by the dotted line in the left panel of Figure 2. Figure 3 shows a comparison of the model with the SAURON and PN.S data. The axisymmetric model in a massive DM halo provides a viable fit to the data. It works by increasing  $\sigma_R/\sigma_\phi$  and by decreasing  $\sigma_z$ , preferentially flattening the outer galaxy.

### 4. Conclusion

As a test of our modeling, we have constructed NMAGIC dynamical models of an isotropic rotator mock galaxy and showed that the internal velocity moments of the input system are well reproduced by the particle model. After this we have constructed spherical and axisymmetric dynamical models for NGC 3379, including different DM halos. The PN.S velocity dispersion profile is consistent with a wide range of DM halos, and is not in contradiction with  $\Lambda$ CDM. A similar conclusion was obtained in work not



**Figure 3.** (a) Left: The top panels show the SAURON kinematic data for NGC 3379 and the bottom panels show the axisymmetric particle model fit. (b) Right: PNe velocity dispersion data of NGC 3379 with superimposed axisymmetric model. The NMAGIC fit was generated using the mass model indicated by the dotted line in the left panel of Figure 2.

reported here for the nearly edge-on elliptical galaxy NGC 4697 (see Méndez *et al.* 2001 and De Lorenzi *et al.* 2008).

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