

## 14<sup>th</sup> International Conference on Automated Planning and Scheduling

Whistler, British Columbia, Canada - June 3-7, 2004

## ICAPS-04 Tutorial on Constraint Satisfaction for Planning and Scheduling

Organizer Roman Barták, Charles University (Czech Republic)

14<sup>th</sup> International Conference on Automated Planning and Scheduling June 3-7, 2004 in Whistler, British Columbia, Canada Conference Chairs: Shlomo Zilberstein, Jana Koehler, Sven Koenig Tutorial Chair: Sylvie Thiebaux

## ICAPS-04 Tutorial on **Constraint Satisfaction for Planning and Scheduling**

Organizer Roman Barták, Charles University (Czech Republic)

The material in these notes is copyrighted by its respective authors. It does not count as published. For more information on ICAPS, please visit www.icaps-conference.org.































































































| Lopez & Bacchus (2003)   | В                                       | oolean model  |
|--|---|---|
| precondition const   | raints                                  | Constraints   |
| $\Box \mathbf{A}_{i,m+1} \Rightarrow \mathbf{P}_{j,m}$ $\Box \mathbf{p}_{j} \text{ is a precondition}$   | of action a <sub>i</sub>                |   |
| next state constraints   |   |   |
| <ul> <li>P<sub>i,m</sub> ⇔ (∨<sub>pi∈add(aj</sub>) A<sub>j,m-1</sub>) ∨ (P<sub>i,m-2</sub> &amp; (∧<sub>pi∈del(aj</sub>) ¬A<sub>j,m-1</sub>)))</li> <li>p<sub>i</sub> is active if it is added by some action or if it is active in the previous propositional layer and it is not deleted by any action</li> <li>no-op actions are not used there.</li> <li>Beware! The constraint allows the proposition to be both added and deleted so mutexes are still necessary!</li> </ul> |   |   |
| ■ mutex constraints<br>□ ¬A <sub>i,m</sub> ∨ ¬A <sub>j,m</sub><br>□ ¬P <sub>i,n</sub> ∨ ¬P <sub>j,n</sub>  | for mutex between a for mutex between p | actions a <sub>i</sub> and a <sub>j</sub> at layer m<br>propositions p <sub>i</sub> and p <sub>j</sub> at layer n |
| ■ goals<br>□ P <sub>i k</sub> = true   |   |   |
| $\Box$ p <sub>i</sub> is a goal proposition and k is the index of the last propositional layer   |   |   |
| <ul> <li>other constraints</li> <li>no parallel actions – at most one action per layer is active</li> <li>no void layers – at least one action per layer is active</li> </ul>  |   |   |
| Constraint Satisfaction for Planning and Scheduling  |   |   |





































































## BIBLIOGRAPHY

- Baptiste, P. and Le Pape, C. (1996). Edge-finding constraint propagation algorithms for disjunctive and cumulative scheduling. Proceedings of the Fifteenth Workshop of the U.K. Planning Special Interest Group (PLANSIG).
- Baptiste, P.; Le Pape, C.; Nuijten, W. (1995). Constraint-Based Optimization and Approximation for Job-Shop Scheduling. Proceedings of the AAAI-SIGMAN Workshop on Intelligent Manufacturing Systems, IJCAI-95.
- Baptiste, P.; Le Pape, C.; Nuijten, W. (2001). Constraint-based Scheduling: Applying Constraints to Scheduling Problems. Kluwer Academic Publishers, Dordrecht.
- Barták, R. (1998). On-line Guide to Constraint Programming. http://kti.mff.cuni.cz/~bartak/constraints/
- Beck, J. Ch and Perron, L. (2000). Discrepancy-Bounded Depth First Search. Proceedings of Second International Workshop on Integration of AI and OR Technologies for Combinatorial Optimization Problems (CP-AI-OR00), 7-17.
- Beldiceanu, N.; Bourreau, E.; Chan, P.; Rivreau, D. (1997). Partial Search Strategy in CHIP. 2nd International Conference on Metaheuristics (MIC 97).
- Berlandier, P. and Neveu, B. (1994). Arc-Consistency for Dynamic Constraint Satisfaction Problems: a RMS free approach. Proceedings of the ECAI-94 Workshop on "Constraint Satisfaction Issues Raised by Practical Applications", Amsterdam, The Netherlands.
- Bessière Ch. (1991). Arc-Consistency in Dynamic Constraint Satisfaction Problems. Proceedings of the 9th National Conference on Artificial Intelligence (AAAI-91), Anaheim, CA, USA. AAAI Press, 221–226.
- Bessière, Ch. (1994). Arc-consistency and arc-consistency again. Artificial Intelligence 65(1), 179-190.
- Bessière, Ch.; Freuder, E.C.; Régin, J.-Ch. (1999). Using constraint metaknowledge to reduce arc consistency computation. Artificial Intelligence 107(1), 125-148.
- Bessière, Ch. and Régin, J.-Ch. (2001). Refining the Basic Constraint Propagation Algorithm. Proceedings of 17th International Joint Conference on Artificial Inteligence (IJCAI-01), 309-315.
- Bistarelli, S., Montanary, U., Rossi, F. (1997). Semiring-based Constraint Satisfaction and Optimisation, *Journal of ACM*.
- Blum, A. and Furst, M. (1997). Fast planning through planning graph analysis. Artificial Intelligence 90, 281-300.
- Brucker, P. (2001). Scheduling Algorithms. Springer Verlag.
- Carlier, J. and Pinson, E. (1994). Adjustment of heads and tails for the job-shop problem. European Journal of Operational Research 78(2), 146-161.
- Caseau, Y. and Laburthe, F. (1995). Disjunctive scheduling with task intervals. LIENS Technical Report 95-25, Laboratoire d'Informatique de l'Ecole Normale Superieure.

- Cesta, A. and Stella, C. (1997). A Time and Resource Problem for Planning Architectures. Recent Advances in AI Planning (ECP'97), LNAI 1348, Springer Verlag, 117-129.
- Cheadle, A.M.; Harvey, W.; Sadler, A.J.; Schimpf, J.; Shen, K. and Wallace, M.H. ECLiPSe: An Introduction. IC-Parc, Imperial College London, Technical Report IC-Parc-03-1, 2003.
- Constraints Archive (2003). http://4c.ucc.ie/web/archive/
- Debruyne R. (1996). Arc-Consistency in Dynamic CSPs is no more prohibitive. Proceedings of the 8th IEEE International Conference on Tools with Artificial Intelligence (ICTAI-96), Toulouse, France, 239–267.
- Dechter R. and Dechter A. (1988). Belief Maintenance in Dynamic Constraint Networks. Proceedings of the 7th National Conference on Artificial Intelligence (AAAI-88), St. Paul, MN, USA. AAAI Press, 37–42.
- Dechter, R.; Meiri, I.; Pearl, J. (1991). Temporal Constraint Networks. Artificial Intelligence 49, 61-95.
- Dechter, R. and Frost, D. (1998). Backtracking algorithms for constraint satisfaction problems; a survey. Constraints, International Journal, Kluwer.
- Dechter, R. (2003). Constraint Processing. Morgan Kaufmann.
- Do, M.B. and Kambhampati, S. (2000). Solving planning-graph by compiling it into CSP. Proceedings of the Fifth International Conference on Artificial Planning and Scheduling (AIPS-2000), AAAI Press, 82-91.
- Dorndorf, U. (2002). Project Scheduling with Time Windows: From Theory to Applications. Physica Verlag, Heidelberg.
- El-Kholy, A. and Richards, B. (1996). Temporal and Resource Reasoning in Planning: the parcPLAN approach. Proceedings of the 12th European Conference on Artificial Intelligence (ECAI 96). John Wiley & Sons, 614-618.
- Fernández, A. J. and Hill, P. M. (2000). A Comparative Study of Eight Constraint Programming Languages Over the Boolean and Finite Domains, Constraints Journal 5(3), Kluwer, 275-301.
- Frank, J. D.; Jonsson, A. K.; Morris, P.H. (2000). On Reformulating Planning As Dynamic Constraint Satisfaction. Proceedings of Symposium on Abstraction, Reformulation and Approximation.
- Gaschnig, J. (1979). Performance Measurement and Analysis of Certain Search Algorithms CMU-CS-79-124, Carnegie-Mellon University.
- Ginsberg, M.L. and Harvey, W.D. (1990). Iterative Broadening. Proceedings of National Conference on Artificial Intelligence (AAAI-90). AAAI Press, 216-220.
- Ginsberg, M.L. (1993). Dynamic Backtracking. Journal of Artificial Intelligence Research 1, 25-46.
- Graham, R.A.; Lawler, E.L.; Lenstra, J.K.; Rinnooy Kan, A.H.G. (1979). Optimization and approximation in deterministic sequencing and scheduling: a survey. Annals of Discrete Mathematics 4, 287-326.

- Han, C. and Lee, C. (1988). Comments on Mohr and Henderson's path consistency algorithm. Artificial Intelligence 36, 125-130.
- Haralick, R.M. and Elliot, G.L. (1980). Increasing tree search efficiency for constraint satisfaction problems. Artificial Intelligence 14:263-314.
- Harvey, W.D. and Ginsberg, M.L. (1995). Limited Discrepancy Search. Proceedings of the 14th International Joint Conference on Artificial Intelligence (IJCAI), 607-613.
- Harvey, W.D. (1995). Nonsystematic backtracking search. PhD Dissertation. Stanford University.
- Kautz, H. and Selman, B. (1992). Planning as satisfiability. Proceedings of the European Conference on Artificial Intelligence (ECAI), 359-363.
- Korf, R.E. (1996). Improved Limited Discrepancy Search. Proceedings of the National Conference on Artificial Intelligence (AAAI), 286-291.
- Kumar, V. (1992). Algorithms for Constraint Satisfaction Problems: A Survey. AI Magazine 13(1), 32-44.
- Laborie, P. (2003). Algorithms for propagating resource constraints in AI planning and scheduling: Existing approaches and new results. Artificial Intelligence 143, 151-188.
- Lever, J. and Richards, B. (1994). parcPlan: a Planning Architecture with Parallel Actions, Resources and Constraints. Methodologies for Intelligent Systems (Proceedings of 8th International Symposium ISMIS 94). LNAI 869, Springer Verlag.
- Lopez, A. and Bacchus, F. (2003). Generalizing GraphPlan by Formulating Planning as a CSP. Proceedings of the 18th International Joint Conference on Artificial Intelligence (IJCAI), 954-960.
- Mackworth, A.K. (1977). Consistency in Networks of Relations. Artificial Intelligence 8, 99-118.
- Mackworth, A.K. and Freuder E.C. (1985). The complexity of some polynomial network consistency algorithms for constraint satisfaction problems. Artificial Intelligence 25, 65-74.
- Marriott, K. and Stuckey, P.J. (1998). Programming with Constraints: An Introduction. MIT Press.
- Martin, P. and Shmoys, D.B. (1996). A new approach to computing optimal schedules for the job-shop scheduling problem. Proceedings of the 5th International Conference on Integer Programming and Combinatorial Optimization, 389-403.
- Meseguer, P. (1997). Interleaved Depth-First Search. Proceedings of the 15th International Joint Conference on Artificial Intelligence (IJCAI), 1382-1387.
- Mittal, S. and Falkenhainer, B. (1990). Dynamic Constraint Satisfaction Problems. Proceedings of the National Conference on Artificial Intelligence (AAAI), 25-32.
- Mohr, R. and Henderson, T.C. (1986). Arc and path consistency revised. Artificial Intelligence 28, 225-233.
- Montanari, U. (1974). Networks of constraints: fundamental properties and applications to picture processing. Information Sciences 7, 95-132.

- Mouhoub, M. (2003). Arc Consistency for Dynamic CSPs. In Vasile Palade, Robert J. Howlett, Lakhmi C. Jain (Eds.): Proceedings of the 7th International Conference on Knowledge-Based Intelligent Information and Engineering Systems – Part I (KES 2003), Oxford, UK. Springer Verlag LNCS 2773, 393–400.
- Prosser, P.; Stergiou, K.; Walsh, T. (2000). *Singleton Consistencies*. Proceedings Principles and Practice of Constraint Programming (CP2000), 353-368.
- Phan-Huy, T. (2000). Constraint Propagation in Flexible Manufacturing. LNEMS 492, Springer Verlag.
- Régin, J.-Ch. (1994). A filtering algorithm for constraints of difference in CSPs. Proceedings of 12th National Conference on Artificial Intelligence, AAAI Press, 362-367.
- Rudová, H. (2002). Random Placement Problem. http://www.fi.muni.cz/~hanka/rpp/
- Schulte, Ch. (2002). Programming Constraint Services. LNAI 2302, Springer Verlag.
- Singh M. (1995). Path Consistency Revised. Proceedings of the 7th IEEE International Conference on Tolls with Artificial Intelligence, 318-325.
- Smith, S.F. and Cheng, Ch.-Ch. (1993). Slack-Based Heuristics For Constraint Satisfaction Scheduling. Proceedings of the National Conference on Artificial Intelligence (AAAI), 139-144.
- Stergiou, K. and Walsh, T. (1990). *Encodings of Non-Binary Constraint Satisfaction Problems*. Proceedings National Conference on Artificial Intelligence (AAAI-99), Orlando, Florida.
- Torres, P. and Lopez, P. (2000). On Not-First/Not-Last conditions in disjunctive scheduling. European Journal of Operational Research 127, 332-343.
- Tsang, E. (1995). Foundations of Constraint Satisfaction. Academic Press, London.
- van Beek, P. and Chen, X. (1999). CPlan: A Constraint Programming Approach to Planning. Proceedings of National Conference on Artificial Intelligence (AAAI).
- van Hentenryck, P. (1989). Constraint Satisfaction in Logic Programming, MIT Press.
- van Hentenryck, P.; Deville Y.; Teng, C.-M. (1992). A generic arc-consistency algorithm and its specializations. Artificial Intelligence 57, 291-321.
- Vilím, P. and Barták, R. (2002). Filtering Algorithms for Batch Processing with Sequence Dependent Setup Times. Proceedings of the 6th International Conference on Artificial Intelligence Planning and Scheduling (AIPS). AAAI Press, 312-320.
- Vilím, P. (2004). O(n log n) Filtering Algorithms for Unary Resource Constraint. Proceedings of CP-AI-OR 2004. LNCS, Springer Verlag.
- Wallace, M. (1994). Applying Constraints for Scheduling. In Mayoh B. and Penjaak J. (eds.), Constraint Programming. NATO ASI Series, Springer Verlag.
- Walsh, T. (1997). Depth-bounded Discrepancy Search. Proceedings of the 15th International Joint Conference on Artificial Intelligence (IJCAI), 1388-1395.
- Waltz, D.L. (1975). Understanding line drawings of scenes with shadows. Psychology of Computer Vision. McGraw-Hill, New York.

- Wolf, A. (2003). Pruning while Sweeping over Task Intervals. Principles and Practice of Constraint Programming (CP 2003). LNCS 2833, Springer Verlag, 739-753.
- Würtz, J. (1996). Oz Scheduler: A Workbench for Scheduling Problems. Proceedings of the 8th IEEE International Conference on Tools with Artificial Intelligence, IEEE Computer Society Press, 132-139.
- Würtz, J. (1997). Constraint-Based Scheduling in Oz. Operations Research Proceedings 1996. Springer Verlag, 218-223.
- Zhang, Y. and Yap, R. (2001). Making AC-3 an Optimal Algorithm. Proceedings of 17th International Joint Conference on Artificial Intelligence (IJCAI-01), 316-321.