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Constraints on the unitarity triangle angle γ from Dalitz plot analysis of $B^0 \rightarrow DK^+\pi^-$ decays

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(LHCb Collaboration)

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The first study is presented of CP violation with an amplitude analysis of the Dalitz plot of $B^0 \rightarrow DK^+\pi^-$ decays, with $D \rightarrow K^+\pi^-$, K^+K^- , and $\pi^+\pi^-$. The analysis is based on a data sample corresponding to 3.0 fb^{-1} of pp collisions collected with the LHCb detector. No significant CP violation effect is seen, and constraints are placed on the angle γ of the unitarity triangle formed from elements of the Cabibbo-Kobayashi-Maskawa quark mixing matrix. Hadronic parameters associated with the $B^0 \rightarrow DK^*(892)^0$ decay are determined for the first time. These measurements can be used to improve the sensitivity to γ of existing and future studies of the $B^0 \rightarrow DK^*(892)^0$ decay.

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I. INTRODUCTION

One of the most important challenges of physics today is understanding the origin of the matter-antimatter asymmetry of the Universe. Within the Standard Model (SM) of particle physics, the CP symmetry between particles and antiparticles is broken only by the complex phase in the Cabibbo-Kobayashi-Maskawa (CKM) quark mixing matrix [1,2]. An important parameter in the CKM description of the SM flavor structure is $\gamma \equiv \arg[-V_{ud}V_{ub}^*/(V_{cd}V_{cb}^*)]$, one of the three angles of the unitarity triangle formed from CKM matrix elements [3–5]. Since the SM cannot account for the baryon asymmetry of the Universe [6] new sources of CP violation, that would show up as deviations from the SM, are expected. The precise determination of γ is necessary in order to be able to search for such small deviations.

The value of γ can be determined from the CP -violating interference between the two amplitudes in, for example, $B^+ \rightarrow DK^+$ and charge-conjugate decays [7–10]. Here D denotes a neutral charm meson reconstructed in a final state accessible to both \bar{D}^0 and D^0 decays, that is therefore a superposition of the \bar{D}^0 and D^0 states produced through $b \rightarrow cW$ and $b \rightarrow uW$ transitions (hereafter referred to as V_{cb} and V_{ub} amplitudes). This approach has negligible theoretical uncertainty in the SM [11] but limited data samples are available experimentally.

A similar method based on $B^0 \rightarrow DK^+\pi^-$ decays has been proposed [12,13] to help improve the precision. By studying the Dalitz plot (DP) [14] distributions of \bar{B}^0 and B^0 decays, interference between different contributions,

such as $B^0 \rightarrow D_2^*(2460)^-K^+$ and $B^0 \rightarrow DK^*(892)^0$ (Feynman diagrams shown in Fig. 1), can be exploited to obtain additional sensitivity compared to the “quasi-two-body” analysis in which only the region of the DP dominated by the $K^*(892)^0$ resonance is selected [15–17]. The method is illustrated in Fig. 2, where the relative amplitudes of the different channels are sketched in the complex plane. The $B^0 \rightarrow \bar{D}^0 K^{*0}$ (V_{cb}) amplitude is determined, relative to that for $B^0 \rightarrow D_2^{*-}K^+$ decays, from analysis of the Dalitz plot with the neutral D meson reconstructed in a favored decay mode such as $\bar{D}^0 \rightarrow K^+\pi^-$. The V_{ub} amplitude can then be obtained from the difference in this relative amplitude compared to the V_{cb} only case when the neutral D meson is reconstructed as a CP eigenstate. A nonzero value of γ causes different relative amplitudes for B^0 and \bar{B}^0 decays, and hence CP violation. The method allows the determination of γ and the hadronic parameters r_B and δ_B , which are the relative magnitude and strong (i.e. CP -conserving) phase of the V_{ub} and V_{cb} amplitudes for the $B^0 \rightarrow DK^{*0}$ decay, with only CP -even D decays required to be reconstructed in addition to the favored decays. This feature, which is in contrast to the method of Refs. [7,8] that requires samples of both CP -even and CP -odd D decays, is important for analysis of data collected at a hadron collider where reconstruction of D meson decays to CP -odd final states such as $K_S^0\pi^0$ is challenging. The Dalitz analysis method also has only a single ambiguity ($\gamma \leftrightarrow \gamma + \pi$, $\delta_B \leftrightarrow \delta_B + \pi$), whereas the method of Refs. [7,8] has an eight-fold ambiguity in the determination of γ .

This paper describes the first study of CP violation with a DP analysis of $B^0 \rightarrow DK^+\pi^-$ decays, with a sample corresponding to 3.0 fb^{-1} of pp collision data collected with the LHCb detector at center-of-mass energies of 7 and 8 TeV. The inclusion of charge conjugate processes is implied throughout the paper except where discussing asymmetries.

*Full author list given at the end of the article.

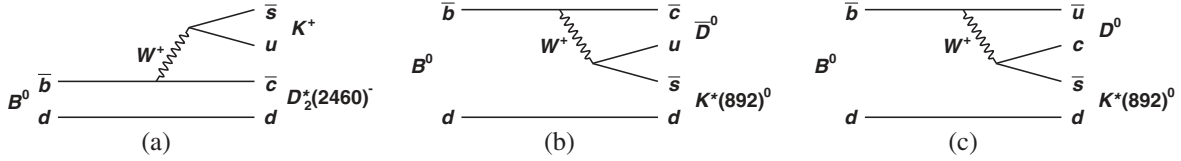


FIG. 1. Feynman diagrams for the contributions to $B^0 \rightarrow DK^+\pi^-$ from (a) $B^0 \rightarrow D_2^*(2460)^- K^+$, (b) $B^0 \rightarrow \bar{D}^0 K^*(892)^0$, and (c) $B^0 \rightarrow D^0 K^*(892)^0$ decays.

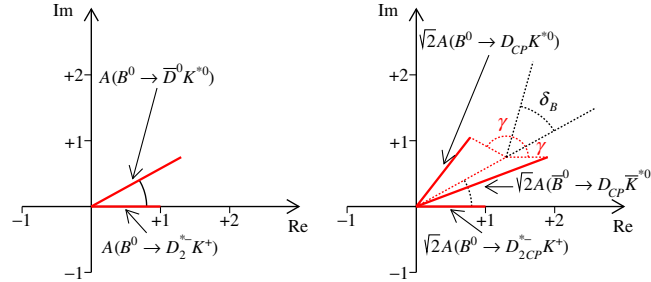


FIG. 2. Illustration of the method to determine γ from Dalitz plot analysis of $B^0 \rightarrow DK^+\pi^-$ decays [12,13]: (left) the V_{cb} amplitude for $B^0 \rightarrow \bar{D}^0 K^{*0}$ compared to that for $B^0 \rightarrow D_2^{*-} K^+$ decay; (right) the effect of the V_{ub} amplitude that contributes to $B^0 \rightarrow D_{CP} K^{*0}$ and $\bar{B}^0 \rightarrow D_{CP} \bar{K}^{*0}$ decays provides sensitivity to γ . The notation D_{CP} represents a neutral D meson reconstructed in a CP eigenstate, while D_{2CP}^{*-} denotes the decay chain $D_2^{*-} \rightarrow D_{CP} \pi^-$, where the charge of the pion tags the flavor of the neutral D meson, independently of the mode in which it is reconstructed, so there is no contribution from the V_{ub} amplitude.

II. DETECTOR AND SIMULATION

The LHCb detector [18,19] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing b or c quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the pp interaction region, a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm, and three stations of silicon-strip detectors and straw drift tubes placed downstream of the magnet. The tracking system provides a measurement of momentum, p , of charged particles with a relative uncertainty that varies from 0.5% at low momentum to 1.0% at 200 GeV/ c . The minimum distance of a track to a primary vertex, the impact parameter, is measured with a resolution of $(15 + 29/p_T) \mu\text{m}$, where p_T is the component of the momentum transverse to the beam, in GeV/ c . Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors. Photons, electrons, and hadrons are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers. The online event selection is performed by a trigger, which consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, in which all charged particles with $p_T > 500(300)$ MeV/ c are reconstructed for 2011 (2012) data. A detailed description of the trigger conditions is available in Ref. [20].

Simulated data samples are used to study the response of the detector and to investigate certain categories of background. In the simulation, pp collisions are generated using PYTHIA [21] with a specific LHCb configuration [22]. Decays of hadronic particles are described by EVTGEN [23], in which final-state radiation is generated using PHOTOS [24]. The interaction of the generated particles with the detector, and its response, are implemented using the GEANT4 toolkit [25] as described in Ref. [26].

III. SELECTION

Candidate $B^0 \rightarrow DK^+\pi^-$ decays are selected with the D meson decaying into the $K^+\pi^-$, K^+K^- , or $\pi^+\pi^-$ final state. The selection requirements are similar to those used for the DP analyses of $B^0 \rightarrow \bar{D}^0 K^+\pi^-$ [27] and $B_s^0 \rightarrow \bar{D}^0 K^-\pi^+$ [28,29] decays, where in both cases only the $\bar{D}^0 \rightarrow K^+\pi^-$ mode was used.

The more copious $B^0 \rightarrow D\pi^+\pi^-$ modes, with neutral D meson decays to one of the three final states under study, are used as control channels to optimize the selection requirements. Loose initial requirements on the final state tracks and the D and B candidates are used to obtain a visible peak of $B^0 \rightarrow D\pi^+\pi^-$ decays. The neutral D meson candidate must satisfy criteria on its invariant mass, vertex quality, and flight distance from any PV and from the B candidate vertex. Requirements on the outputs of boosted decision tree algorithms that identify neutral D meson decays, in each of the decay chains of interest, originating from b hadron decays [30,31] are also applied. These requirements are sufficient to reduce to negligible levels potential background from charmless B meson decays that

have identical final states but without an intermediate D meson. Vetoes are applied to remove backgrounds from $B^0 \rightarrow D^*(2010)^- K^+$, $B^0 \rightarrow D^\mp \pi^\pm$, $B_s^0 \rightarrow D_s^- \pi^+$, and $B_{(s)}^0 \rightarrow D^0 \bar{D}^0$ decays, and candidates consistent with originating from $B_{(s)}^0 \rightarrow \bar{D}^0 K^\pm \pi^\mp$ decays, where the \bar{D}^0 has been reconstructed from the wrong pair of tracks.

Separate neural network (NN) classifiers [32] for each D decay mode are used to distinguish signal decays from combinatorial background. The *sPlot* technique [33], with the $B^0 \rightarrow D\pi^+\pi^-$ candidate mass as the discriminating variable, is used to obtain signal and background weights,

which are then used to train the networks. The networks are based on input variables that describe the topology of each decay channel, and that depend only weakly on the B candidate mass and on the position of the candidate in the B decay Dalitz plot. Loose requirements are made on the NN outputs in order to retain large samples for the DP analysis.

IV. DETERMINATION OF SIGNAL AND BACKGROUND YIELDS

The yields of signal and of several different backgrounds are determined from an extended maximum likelihood fit,

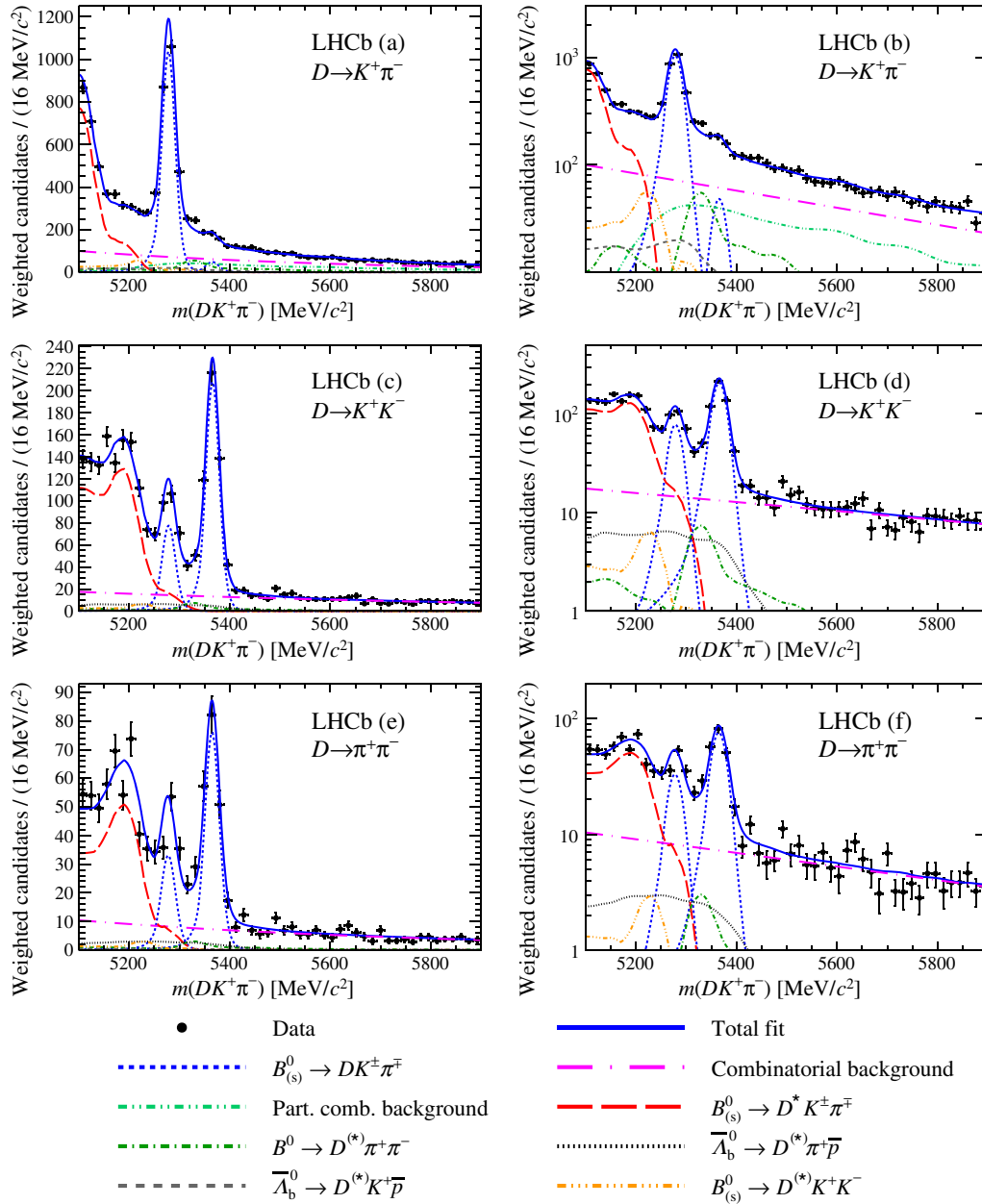


FIG. 3. Results of fits to $DK^+\pi^-$ candidates in the (a,b) $D \rightarrow K^+\pi^-$, (c,d) $D \rightarrow K^+K^-$, and (e,f) $D \rightarrow \pi^+\pi^-$ samples. The data and the fit results in each NN output bin have been weighted according to $S/(S+B)$ as described in the text. The left and right plots are identical but with (left) linear and (right) logarithmic y axis scales. The components are as described in the legend.

in each mode, to the distributions of candidates in B candidate mass and NN output. Unbinned information on the B candidate mass is used, while each sample is divided into five bins of the NN output that contain a similar number of signal, and varying numbers of background, decays [34,35].

In addition to $B^0 \rightarrow DK^+\pi^-$ decays, components are included in the fit to account for B_s^0 decays to the same final state, partially reconstructed $B_{(s)}^0 \rightarrow D^{(*)}K^\pm\pi^\mp$ backgrounds, misidentified $B^0 \rightarrow D^{(*)}\pi^+\pi^-$, $B_{(s)}^0 \rightarrow D^{(*)}K^+K^-$, $\bar{\Lambda}_b^0 \rightarrow D^{(*)}\bar{p}\pi^+$, and $\bar{\Lambda}_b^0 \rightarrow D^{(*)}\bar{p}K^+$ decays as well as combinatorial background. The modeling of the signal and background distributions in B candidate mass is similar to that described in Ref. [27]. The sum of two Crystal Ball functions [36] is used for each of the correctly reconstructed B decays, where the peak position and core width (i.e. the narrower of the two widths) are free parameters of the fit, while the B_s^0 - B^0 mass difference is fixed to its known value [37]. The fraction of the signal function contained in the core and the relative width of the two components are constrained within uncertainties to, and all other parameters are fixed to, their expected values obtained from simulated data, separately for each of the three D samples. An exponential function is used to describe combinatorial background, with the shape parameter allowed to vary. Because of the loose NN output requirement it is necessary, in the $D \rightarrow K^+\pi^-$ sample, to account explicitly for partially combinatorial background where the final state DK^+ pair originates from a B decay but is combined with a random pion; this is modeled with a nonparametric function. Nonparametric functions obtained from simulation based on known DP distributions [38–44] are used to model the partially reconstructed and misidentified B decays.

The fraction of signal decays in each NN output bin is allowed to vary freely in the fit; the correctly reconstructed B_s^0 decays and misidentified backgrounds are taken to have the same NN output distribution as signal. The fractions of combinatorial and partially reconstructed backgrounds in each NN output bin are each allowed to vary freely. All yields are free parameters of the fit, except those for misidentified backgrounds which are constrained within expectation relative to the signal yield, since the relative branching fractions [37] and misidentification probabilities [45] are well known.

The results of the fits are shown in Fig. 3, in which the NN output bins have been combined by weighting both the data and fit results by $\mathcal{S}/(\mathcal{S} + \mathcal{B})$, where \mathcal{S} (\mathcal{B}) is the signal (background) yield in the signal window, defined as $\pm 2.5\sigma(\text{core})$ around the B^0 peak in each sample, where $\sigma(\text{core})$ is the core width of the signal shape. The yields of each category in these regions, which correspond to 5246.6–5309.9 MeV/ c^2 , 5246.9–5310.5 MeV/ c^2 , and 5243.1–5312.3 MeV/ c^2 in the $D \rightarrow K^+\pi^-$, K^+K^- , and

TABLE I. Yields in the signal window of the fit components in the five NN output bins for the $D \rightarrow K^+\pi^-$ sample. The last column indicates whether or not each component is explicitly modeled in the Dalitz plot fit.

Component	Yield					Included?
	Bin 1	Bin 2	Bin 3	Bin 4	Bin 5	
$B^0 \rightarrow DK^+\pi^-$	597	546	585	571	540	Yes
$B_s^0 \rightarrow DK^+\pi^-$	1	1	1	1	1	No
Combinatorial background	540	58	16	6	1	Yes
$B^+ \rightarrow D^{(*)}K^+ + X^-$	305	33	9	3	1	Yes
$B^0 \rightarrow D^*K^+\pi^-$	1	1	1	1	1	No
$B^0 \rightarrow D^{(*)}\pi^+\pi^-$	20	18	20	19	18	Yes
$\bar{\Lambda}_b^0 \rightarrow D^{(*)}K^+\bar{p}$	21	19	21	20	19	Yes
$B^0 \rightarrow D^{(*)}K^+K^-$	8	7	8	7	7	No
$B_s^0 \rightarrow D^{(*)}K^+K^-$	10	9	10	10	9	No

TABLE II. Yields in the signal window of the fit components in the five NN output bins for the $D \rightarrow K^+K^-$ sample. The last column indicates whether or not each component is explicitly modeled in the Dalitz plot fit.

Component	Yield					Included?
	Bin 1	Bin 2	Bin 3	Bin 4	Bin 5	
$B^0 \rightarrow DK^+\pi^-$	70	63	68	73	65	Yes
$\bar{B}_s^0 \rightarrow DK^+\pi^-$	5	5	5	6	5	Yes
Combinatorial background	173	19	9	3	0	Yes
$B^0 \rightarrow D^*K^+\pi^-$	0	1	1	1	0	No
$\bar{B}_s^0 \rightarrow D^*K^+\pi^-$	19	28	34	28	20	Yes
$B^0 \rightarrow D^{(*)}\pi^+\pi^-$	4	3	4	4	3	Yes
$\Lambda_b^0 \rightarrow D^{(*)}p\pi^-$	11	10	10	11	10	Yes
$\bar{\Lambda}_b^0 \rightarrow D^{(*)}K^+\bar{p}$	2	1	2	2	2	No
$B^0 \rightarrow D^{(*)}K^+K^-$	2	1	2	2	1	No
$B_s^0 \rightarrow D^{(*)}K^+K^-$	1	1	1	2	1	No

TABLE III. Yields in the signal window of the fit components in the five NN output bins for the $D \rightarrow \pi^+\pi^-$ sample. The last column indicates whether or not each component is explicitly modeled in the Dalitz plot fit.

Component	Yield					Included?
	Bin 1	Bin 2	Bin 3	Bin 4	Bin 5	
$B^0 \rightarrow DK^+\pi^-$	36	31	38	32	31	Yes
$\bar{B}_s^0 \rightarrow DK^+\pi^-$	3	2	3	3	2	Yes
Combinatorial background	119	17	4	3	2	Yes
$B^0 \rightarrow D^*K^+\pi^-$	0	0	0	0	0	No
$\bar{B}_s^0 \rightarrow D^*K^+\pi^-$	9	16	15	12	10	Yes
$B^0 \rightarrow D^{(*)}\pi^+\pi^-$	2	2	2	2	2	Yes
$\Lambda_b^0 \rightarrow D^{(*)}p\pi^-$	6	5	6	5	5	Yes
$\bar{\Lambda}_b^0 \rightarrow D^{(*)}K^+\bar{p}$	1	1	1	1	1	No
$B^0 \rightarrow D^{(*)}K^+K^-$	1	1	1	1	1	No
$B_s^0 \rightarrow D^{(*)}K^+K^-$	1	1	1	1	1	No

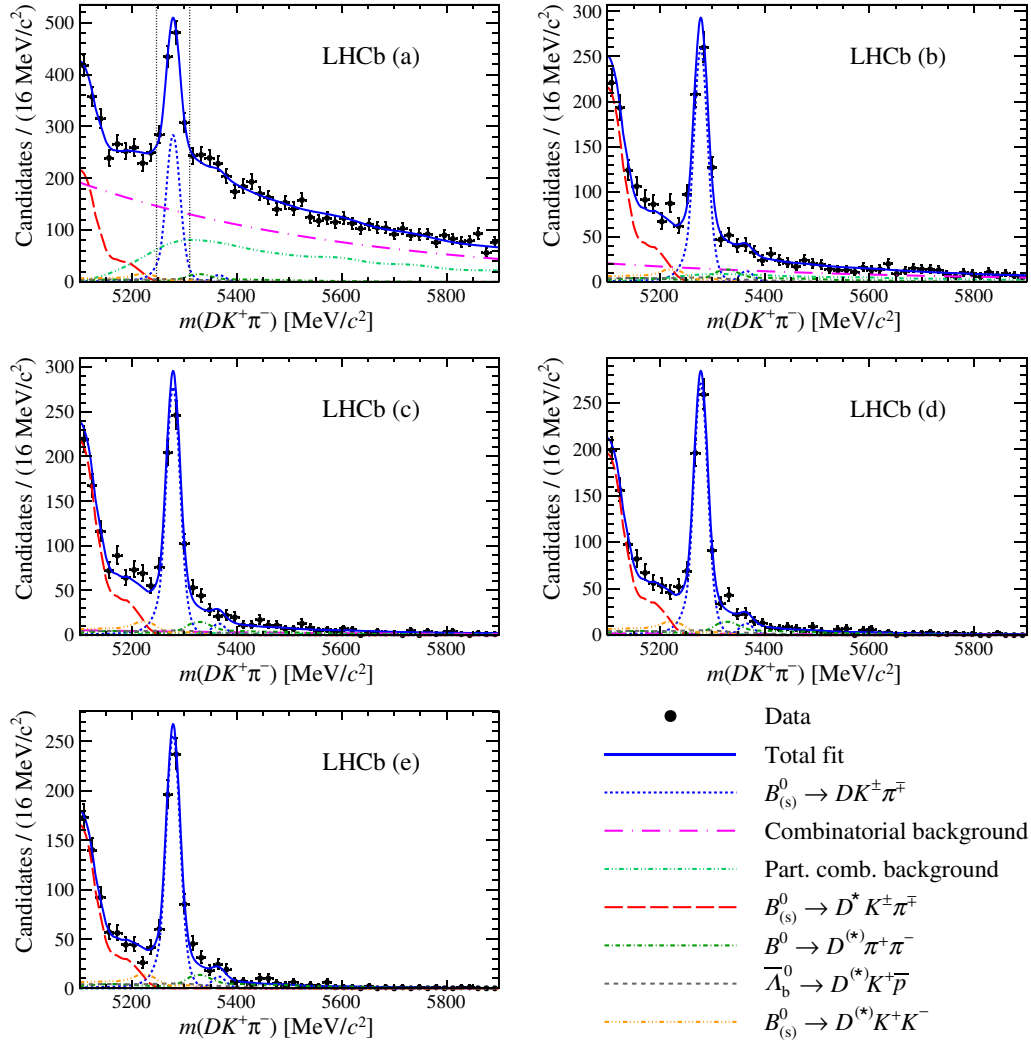


FIG. 4. Results of the fit to $DK^+\pi^-$, $D \rightarrow K^+\pi^-$ candidates shown separately in the five bins of the neural network output variable. The bins are shown, from (a)–(e), in order of increasing S/B . The components are as indicated in the legend. The vertical dotted lines in (a) show the signal window used for the fit to the Dalitz plot.

$\pi^+\pi^-$ samples, are given in Tables I, II and III. In total, there are 2840 ± 70 signal decays within the signal window in the $D \rightarrow K^+\pi^-$ sample, while the corresponding values for the $D \rightarrow K^+K^-$ and $D \rightarrow \pi^+\pi^-$ samples are 339 ± 22 and 168 ± 19 . The χ^2/ndf values for the projections of the fits to the $D \rightarrow K^+\pi^-$, $D \rightarrow K^+K^-$, and $D \rightarrow \pi^+\pi^-$ data sets are 171.5/223, 188.2/223, and 169.1/222, respectively, giving a total $\chi^2/\text{ndf} = 528.8/668$. Note that there are some bins with low numbers of entries which may result in this value not following exactly the expected χ^2 distribution.

Projections of the fits separated by NN output bin in each sample are shown in Figs. 4–6. The fitted parameters obtained from all three data samples are reported in Table IV. The parameters $\mu(B)$, $N(\text{core})/N(\text{total})$, $\sigma(\text{wide})/\sigma(\text{core})$ are, respectively, the peak position, the fraction of the signal function contained in the core, and the relative width of the two components of the B^0 signal

shape. Quantities denoted N are total yields of each fit component, while those denoted f_{signal}^i are fractions of the signal in NN output bin i (with similar notation for the fractions of the partially reconstructed and combinatorial backgrounds). The NN output bin labels 1–5 range from the bin with the lowest to highest value of S/B .

V. DALITZ PLOT ANALYSIS

Candidates within the signal region are used in the DP analysis. A simultaneous fit is performed to the samples with different D decays by using the J_{FIT} method [46] as implemented in the Laura++ package [47]. The likelihood function contains signal and background terms, with yields in each NN output bin fixed according to the results obtained previously. The NN output bin with the lowest S/B value in the $D \rightarrow K^+\pi^-$ sample only is found not to contribute significantly to the sensitivity and is susceptible

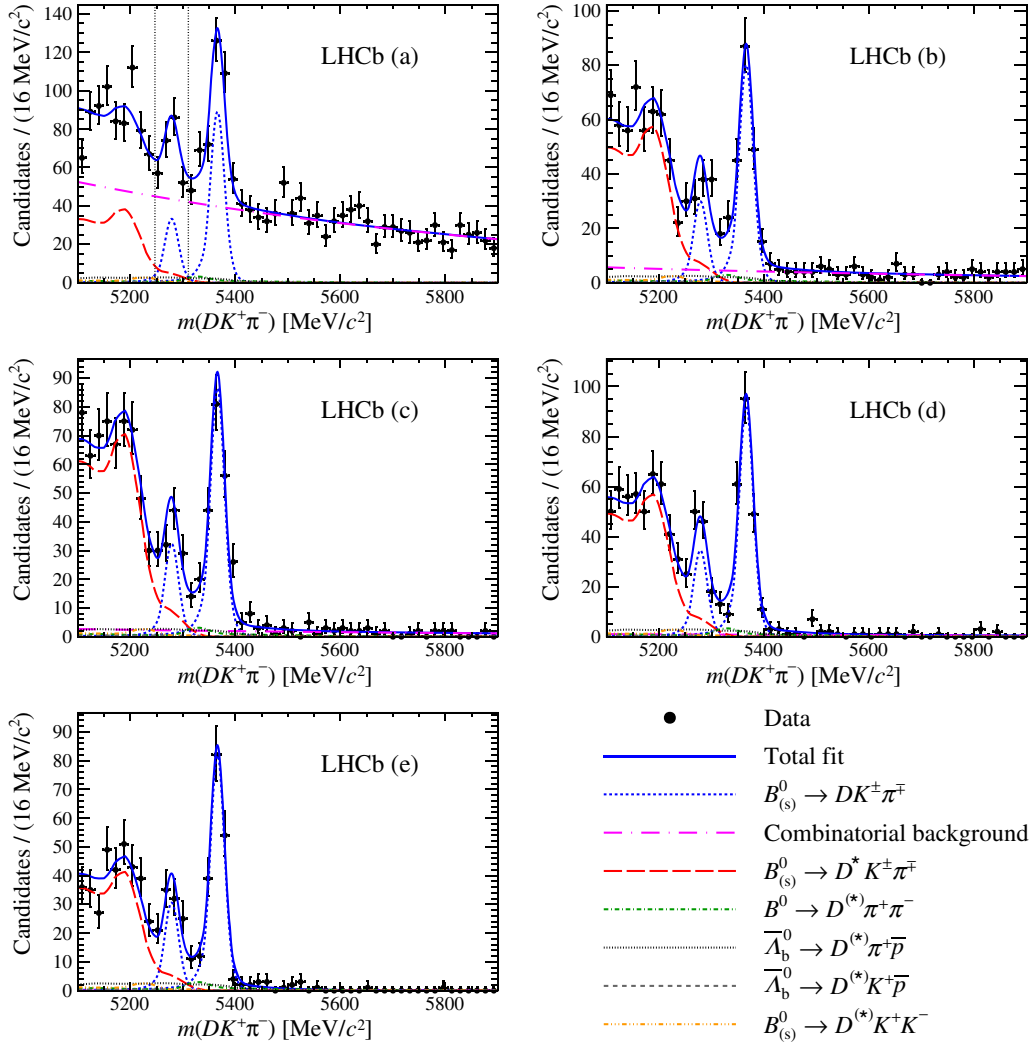


FIG. 5. Results of the fit to $DK^+\pi^-$, $D \rightarrow K^+K^-$ candidates shown separately in the five bins of the neural network output variable. The bins are shown, from (a)–(e), in order of increasing S/B . The components are as indicated in the legend. The vertical dotted lines in (a) show the signal window used for the fit to the Dalitz plot.

to mismodeling of the combinatorial background; it is therefore excluded from the subsequent analysis.

The signal probability function is derived from the isobar model obtained in Ref. [27], with amplitude

$$\begin{aligned} \mathcal{A}(m^2(D\pi^-), m^2(K^+\pi^-)) \\ = \sum_{j=1}^N c_j F_j(m^2(D\pi^-), m^2(K^+\pi^-)), \end{aligned} \quad (1)$$

where c_j are complex coefficients describing the relative contribution for each intermediate process, and the $F_j(m^2(D\pi^-), m^2(K^+\pi^-))$ terms describe the resonant dynamics through the line shape, angular distribution, and barrier factors. The sum is over amplitudes from the $D_0^*(2400)^-$, $D_2^*(2460)^-$, $K^*(892)^0$, $K^*(1410)^0$, and $K_2^*(1430)^0$ resonances as well as a $K^+\pi^-$ S-wave component and both S-wave and P-wave nonresonant $D\pi^-$

amplitudes [27]. The masses and widths of $K^+\pi^-$ resonances are fixed, and those of $D\pi^-$ resonances are constrained within uncertainties to known values [27,37,40,48]. The values of the c_j coefficients are allowed to vary in the fit, as are the shape parameters of the nonresonant amplitudes.

For the $D \rightarrow K^+\pi^-$ sample, the contribution from the V_{ub} amplitude followed by doubly Cabibbo-suppressed D decay is negligible. This sample can therefore be treated as if only the V_{cb} amplitude contributes, and the signal probability function is given by Eq. (1). For the samples with $D \rightarrow K^+K^-$ and $\pi^+\pi^-$ decays, the c_j terms are modified,

$$c_j \rightarrow \begin{cases} c_j & \text{for a } D\pi^- \text{ resonance,} \\ c_j[1 + x_{\pm,j} + iy_{\pm,j}] & \text{for a } K^+\pi^- \text{ resonance,} \end{cases} \quad (2)$$

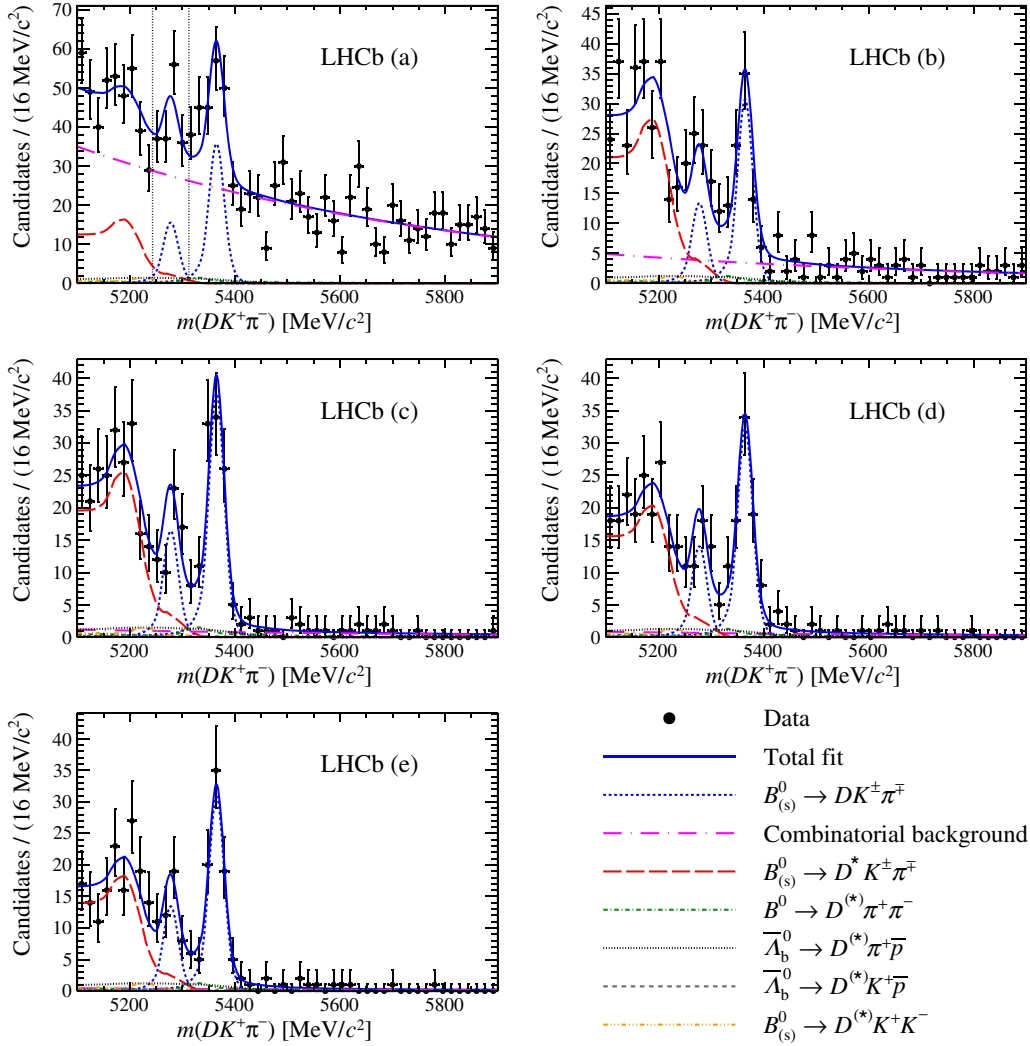


FIG. 6. Results of the fit to $DK^+\pi^-$, $D \rightarrow \pi^+\pi^-$ candidates shown separately in the five bins of the neural network output variable. The bins are shown, from (a)–(e), in order of increasing S/B . The components are as indicated in the legend. The vertical dotted lines in (a) show the signal window used for the fit to the Dalitz plot.

with $x_{\pm,j} = r_{B,j} \cos(\delta_{B,j} \pm \gamma)$ and $y_{\pm,j} = r_{B,j} \sin(\delta_{B,j} \pm \gamma)$, where the + and – signs correspond to B^0 and \bar{B}^0 DPs, respectively. Here $r_{B,j}$ and $\delta_{B,j}$ are the relative magnitude and strong phase of the V_{ub} and V_{cb} amplitudes for each $K^+\pi^-$ resonance j . In this analysis the $x_{\pm,j}$ and $y_{\pm,j}$ parameters are measured only for the $K^*(892)^0$ resonance, which has a large enough yield and a sufficiently well-understood line shape to allow reliable determinations of these parameters; therefore the j subscript is omitted hereafter. In addition, a component corresponding to the $B^0 \rightarrow D_{s1}^*(2700)^+\pi^-$ decay, which is mediated by the V_{ub} amplitude alone, is included in the fit with mass and width parameters fixed to their known values [37,49] and magnitude constrained according to expectation based on the $B^0 \rightarrow D_{s1}^*(2700)^+D^-$ decay rate [49].

The signal efficiency and backgrounds are modeled in the likelihood function, separately for each of the samples, following Refs. [27,38,39]. The DP distribution

of combinatorial background is obtained from a sideband in B candidate mass, defined as $5400(5450) < m(DK^+\pi^-) < 5900$ MeV/ c^2 for the samples with $D \rightarrow K^+\pi^-$ ($D \rightarrow K^+K^-$ or $\pi^+\pi^-$). The shapes of partially reconstructed and misidentified backgrounds are obtained from simulated samples based on known DP distributions [38–44]. Combinatorial background is the largest component in the NN output bins with the lowest S/B values, while in the purest bins in the $D \rightarrow K^+K^-$ and $\pi^+\pi^-$ samples the $B_s^0 \rightarrow D^*K^-\pi^+$ background makes an important contribution. Background sources with yields below 2% relative to the signal in all NN bins are neglected, as indicated in Tables I, II and III.

The fit procedure is validated with ensembles of pseudoexperiments. In addition, samples of $B_s^0 \rightarrow DK^-\pi^+$ decays are selected for each of the D decays. These are used to test the fit with a model based on that of Refs. [38,39] and where DK^- resonances have contributions only from

TABLE IV. Results for the unconstrained parameters obtained from the fits to the three data samples. Entries where no number is given are fixed to zero. Fractions marked * are not varied in the fit, and give the difference between unity and the sum of the other fractions.

Parameter	$D \rightarrow K^+\pi^-$	$D \rightarrow K^+K^-$	$D \rightarrow \pi^+\pi^-$
	Value		
$\mu(B)(\text{MeV}/c^2)$	5278.3 ± 0.4	5278.7 ± 0.5	5277.7 ± 1.0
$\sigma(\text{core})(\text{MeV}/c^2)$	12.7 ± 0.4	12.7 ± 0.5	13.9 ± 0.8
$N(\text{core})/N(\text{total})$	0.787 ± 0.017	0.798 ± 0.018	0.797 ± 0.018
$\sigma(\text{wide})/\sigma(\text{core})$	1.80 ± 0.05	1.75 ± 0.05	1.76 ± 0.05
Exp. slope (c^2/GeV)	-1.84 ± 0.13	-1.05 ± 0.19	-1.35 ± 0.26
$N(B^0 \rightarrow DK\pi)$	3125 ± 79	418 ± 27	185 ± 21
$N(B_s^0 \rightarrow DK\pi)$	146 ± 27	1014 ± 41	429 ± 28
$N(\text{comb bkgd})$	5694 ± 529	2092 ± 95	1288 ± 86
$N(B \rightarrow D^{(*)}K + X)$	2648 ± 454
$N(B^0 \rightarrow D^*K\pi)$	3028 ± 115	543 ± 48	183 ± 33
$N(B_s^0 \rightarrow D^*K\pi)$...	1493 ± 77	639 ± 52
$N(B^0 \rightarrow D^{(*)}\pi\pi)$	783 ± 67	146 ± 17	72 ± 11
$N(\Lambda_b^0 \rightarrow D^{(*)}p\pi)$...	241 ± 47	118 ± 26
$N(\Lambda_b^0 \rightarrow D^{(*)}pK)$	416 ± 64	34 ± 9	17 ± 5
$N(B^0 \rightarrow D^{(*)}KK)$	371 ± 51	64 ± 15	33 ± 8
$N(B_s^0 \rightarrow D^{(*)}KK)$	171 ± 47	25 ± 11	14 ± 6
f_{signal}^1	0.210 ± 0.012	0.187 ± 0.017	0.214 ± 0.029
f_{signal}^2	0.192 ± 0.008	0.186 ± 0.011	0.184 ± 0.019
f_{signal}^3	0.206 ± 0.008	0.201 ± 0.012	0.225 ± 0.019
f_{signal}^4	0.201 ± 0.007	0.215 ± 0.012	0.193 ± 0.018
f_{signal}^5 *	0.190 ± 0.007	0.211 ± 0.011	0.184 ± 0.017
$f_{\text{part rec bkgd}}^1$	0.214 ± 0.023	0.145 ± 0.020	0.152 ± 0.042
$f_{\text{part rec bkgd}}^2$	0.214 ± 0.010	0.217 ± 0.011	0.254 ± 0.021
$f_{\text{part rec bkgd}}^3$	0.215 ± 0.011	0.267 ± 0.013	0.237 ± 0.021
$f_{\text{part rec bkgd}}^4$	0.193 ± 0.010	0.215 ± 0.012	0.189 ± 0.019
$f_{\text{part rec bkgd}}^5$ *	0.164 ± 0.009	0.156 ± 0.010	0.169 ± 0.018
$f_{\text{comb bkgd}}^1$	0.870 ± 0.013	0.849 ± 0.012	0.828 ± 0.018
$f_{\text{comb bkgd}}^2$	0.094 ± 0.008	0.092 ± 0.009	0.116 ± 0.014
$f_{\text{comb bkgd}}^3$	0.025 ± 0.004	0.043 ± 0.007	0.027 ± 0.008
$f_{\text{comb bkgd}}^4$	0.009 ± 0.003	0.017 ± 0.005	0.019 ± 0.007
$f_{\text{comb bkgd}}^5$ *	0.002 ± 0.002	0.000 ± 0.000	0.010 ± 0.006

V_{cb} amplitudes, while the coefficients for $K^-\pi^+$ resonances are parametrized by Eq. (2). The results are

$$\begin{aligned}
x_+(B_s^0 \rightarrow D\bar{K}^*(892)^0) &= 0.05 \pm 0.05, \\
y_+(B_s^0 \rightarrow D\bar{K}^*(892)^0) &= -0.08 \pm 0.11, \\
x_-(B_s^0 \rightarrow D\bar{K}^*(892)^0) &= 0.01 \pm 0.05, \\
y_-(B_s^0 \rightarrow D\bar{K}^*(892)^0) &= -0.08 \pm 0.12,
\end{aligned}$$

where the uncertainties are statistical only. No significant CP violation effect is observed, consistent with the

expectation that V_{ub} amplitudes are highly suppressed in this control channel.

VI. SYSTEMATIC UNCERTAINTIES

Sources of systematic uncertainty on the x_{\pm} and y_{\pm} parameters can be divided into two categories: experimental and model uncertainties. These are summarized in Tables V and VI. The former category includes effects due to knowledge of the signal and background yields in the signal region (denoted “ S/B ” in Table V), the variation of

TABLE V. Experimental systematic uncertainties.

Parameter	Uncertainty							Total
	S/B	ϵ	\mathcal{B} DP	Fit bias	\mathcal{B} asym.	\mathcal{B} DP asym.	ϵ asym.	
x_+	0.010	0.035	0.046	0.021	0.007	0.049	0.000	0.079
x_-	0.026	0.028	0.063	0.019	0.010	0.045	0.001	0.089
y_+	0.019	0.042	0.122	0.066	0.017	0.027	0.000	0.149
y_-	0.024	0.022	0.054	0.035	0.018	0.071	0.000	0.103

TABLE VI. Model uncertainties.

Parameter	Uncertainty					Total
	Fixed parameters	Add/rem.	Alternative model	D_s^{**} CPV	$K\pi_{S\text{-wave}}$ CPV	
x_+	0.027	0.028	0.068	0.008	0.003	0.079
x_-	0.030	0.034	0.076	0.056	0.022	0.107
y_+	0.075	0.061	0.131	0.012	0.047	0.170
y_-	0.040	0.066	0.255	0.286	0.064	0.396

the efficiency (ϵ) across the Dalitz plot, the background Dalitz plot distributions (\mathcal{B} DP) and fit bias, all of which are evaluated in similar ways to those described in Ref. [27]. Additionally, effects that may induce fake asymmetries, including asymmetry between \bar{B}^0 and B^0 candidates in the background yields (\mathcal{B} asym.) as well as asymmetries in the background Dalitz plot distributions (\mathcal{B} DP asym.) and in the efficiency variation (ϵ asym.) are accounted for. The largest source of uncertainty in this category arises from lack of knowledge of the DP distribution for the $B_s^0 \rightarrow D^* K^- \pi^+$ background.

Model uncertainties arise due to fixing parameters in the amplitude model (denoted ‘‘fixed pars’’ in Table VI), the addition or removal of marginal components, namely the $K^*(1410)^0$, $K^*(1680)^0$, $D_1^*(2760)^-$, $D_3^*(2760)^-$, and $D_{s2}^*(2573)^+$ resonances, in the Dalitz plot fit (add/rem.), and the use of alternative models for the $K^+ \pi^-$ S-wave and $D\pi^-$ nonresonant amplitudes (alt. mod.); all of these are evaluated as in Ref. [27]. The possibilities of CP violation associated with the $D_{s1}^*(2700)^+$ amplitude

(D_s^{**} CPV), and of independent CP violation parameters in the two components of the $K^+ \pi^-$ S-wave amplitude [50] ($K\pi_{S\text{-wave}}$ CPV), are also accounted for. The largest source of uncertainty in this category arises from changing the description of the $K^+ \pi^-$ S-wave. Other possible sources of systematic uncertainty, such as production asymmetry [51] or CP violation in the $D \rightarrow K^+ K^-$ and $\pi^+ \pi^-$ decays [52–54], are found to be negligible.

The total uncertainties are obtained by combining all sources in quadrature. The leading sources of systematic uncertainty are expected to be reducible with larger data samples.

VII. RESULTS AND SUMMARY

The DPs for candidates in the B candidate mass signal region in the $D \rightarrow K^+ K^-$ and $\pi^+ \pi^-$ samples are shown separately for \bar{B}^0 and B^0 candidates in Fig. 7. Projections of the fit results onto $m(D\pi)$, $m(K\pi)$, and $m(DK)$ for the

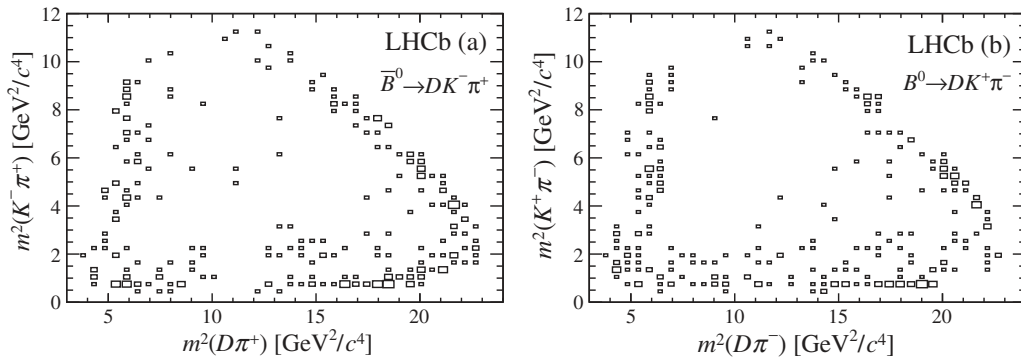


FIG. 7. Dalitz plots for candidates in the B candidate mass signal region in the $D \rightarrow K^+ K^-$ and $\pi^+ \pi^-$ samples for (a) \bar{B}^0 and (b) B^0 candidates. Only candidates in the three purest NN bins are included. Background has not been subtracted, and therefore some contribution from $\bar{B}_s^0 \rightarrow D^{*0} K^+ \pi^-$ decays is expected at low $m(DK^+)$ (i.e. along the top right diagonal).

$D \rightarrow K^+K^-$ and $\pi^+\pi^-$ samples are shown separately for \bar{B}^0 and B^0 candidates in Fig. 8. No significant CP violation effect is seen.

The results, with statistical uncertainties only, for the complex coefficients c_j are given in Table VII. Due to the changes in the selection requirements, the overlap between the $D \rightarrow K^+\pi^-$ sample and the data set used in Ref. [27] is only around 60%, and the results are found to be consistent.

The results for the CP violation parameters associated with the $B^0 \rightarrow DK^*(892)^0$ decay are

$$\begin{aligned} x_+ &= 0.04 \pm 0.16 \pm 0.11, \\ y_+ &= -0.47 \pm 0.28 \pm 0.22, \\ x_- &= -0.02 \pm 0.13 \pm 0.14, \\ y_- &= -0.35 \pm 0.26 \pm 0.41, \end{aligned}$$

where the uncertainties are statistical and systematic. The statistical and systematic correlation matrices are given in Table VIII. The results for (x_+, y_+) and (x_-, y_-) are shown as contours in Fig. 9.

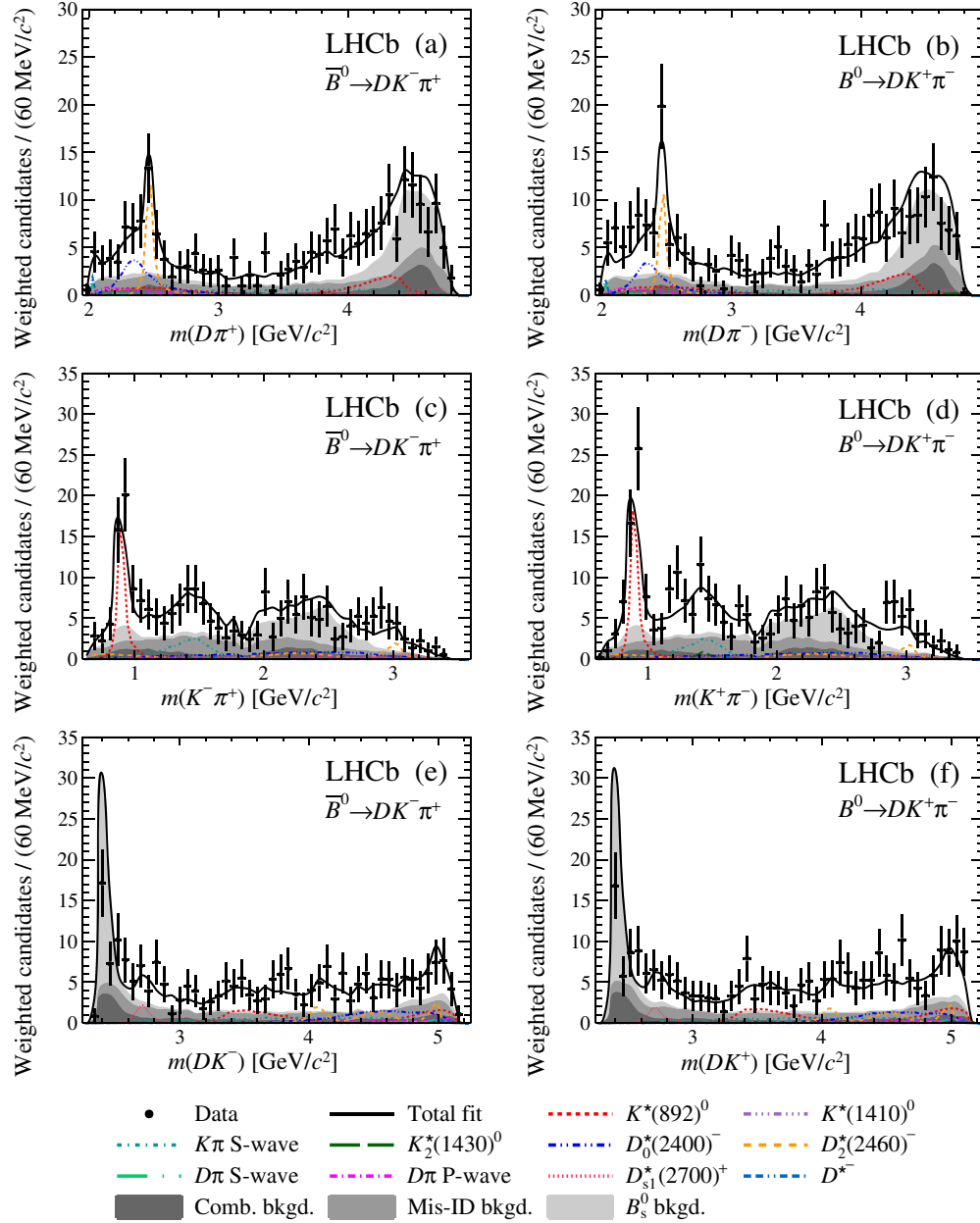


FIG. 8. Projections of the $D \rightarrow K^+K^-$ and $\pi^+\pi^-$ samples and the fit result onto (a),(b) $m(D\pi^\mp)$, (c),(d) $m(K^\pm\pi^\mp)$, and (e),(f) $m(DK^\pm)$ for (a),(c),(e) \bar{B}^0 and (b),(d),(f) B^0 candidates. The data and the fit results in each NN output bin have been weighted according to $S/(S+B)$ and combined. The components are described in the legend.

TABLE VII. Results for the complex coefficients c_j from the fit to data. Uncertainties are statistical only. All reported quantities are unconstrained in the fit, except that the $D_2^*(2460)^-$ component is fixed as a reference amplitude, and the magnitude of the $D_{s1}^*(2700)^+$ component is constrained. The $K^+\pi^-$ S-wave is the coherent sum of the $K_0^*(1430)^0$ and the nonresonant $K\pi$ S-wave component [50].

Resonance	Real part	Imaginary part
$K^*(892)^0$	-0.07 ± 0.10	-1.19 ± 0.04
$K^*(1410)^0$	0.16 ± 0.04	0.21 ± 0.06
$K_0^*(1430)^0$	0.40 ± 0.08	0.67 ± 0.06
Nonresonant $K\pi$ S-wave	0.37 ± 0.07	0.69 ± 0.07
$K_2^*(1430)^0$	-0.01 ± 0.06	-0.48 ± 0.04
$D_0^*(2400)^-$	-1.10 ± 0.05	-0.18 ± 0.07
$D_2^*(2460)^-$	1.00	0.00
Nonresonant $D\pi$ S-wave	-0.44 ± 0.06	0.02 ± 0.07
Nonresonant $D\pi$ P-wave	-0.61 ± 0.05	-0.08 ± 0.06
$D_{s1}^*(2700)^+$	0.57 ± 0.05	-0.09 ± 0.19

The GammaCombo package [55] is used to evaluate constraints from these results on γ and the hadronic parameters r_B and δ_B associated with the $B^0 \rightarrow DK^*(892)^0$ decay. A frequentist treatment referred to as the ‘‘plug-in’’ method, described in Refs. [56–59], is used. Figure 10 shows the results of likelihood scans for γ , r_B , and δ_B . Figure 11 shows the two-dimensional 68% confidence level for each pair of observables from γ , r_B , and δ_B . No value of γ is excluded at 95% confidence level (C.L.); the world-average value for γ [60,61] has a C.L. of 0.85.

The $B^0 \rightarrow DK^*(892)^0$ decay can also be used to determine parameters sensitive to γ with a quasi-two-body approach, as has been done with $D \rightarrow K^+K^-$, $\pi^+\pi^-$ [62], $K^\pm\pi^\mp$, $K^\pm\pi^\mp\pi^0$, $K^\pm\pi^\mp\pi^+\pi^-$ [62–64] and $D \rightarrow K_S^0\pi^+\pi^-$ decays [65–68]. In the quasi-two-body analysis, the results depend on the effective hadronic parameters κ , \bar{r}_B , and $\bar{\delta}_B$, which are, respectively, the coherence factor

TABLE VIII. Correlation matrices associated with the (left) statistical and (right) systematic uncertainties of the CP violation parameters associated with the $B^0 \rightarrow DK^*(892)^0$ decay.

	x_-	y_-	x_+	y_+
x_-	1.00			
y_-	0.34	1.00		
x_+	0.10	0.05	1.00	
y_+	0.13	0.15	0.50	1.00

	x_-	y_-	x_+	y_+
x_-	1.00			
y_-	0.87	1.00		
x_+	0.25	0.29	1.00	
y_+	0.37	0.41	0.73	1.00

and the relative magnitude and strong phase of the V_{ub} and V_{cb} amplitudes averaged over the selected region of phase space [17]. Precise definitions are given in the Appendix. These parameters are calculated from the models for V_{cb} and V_{ub} amplitudes obtained from the fit for the $K^*(892)^0$ selection region $|m(K^+\pi^-) - m_{K^*(892)^0}| < 50$ MeV/ c^2 and $|\cos\theta_{K^*0}| > 0.4$, where $m_{K^*(892)^0}$ is the known value of the $K^*(892)^0$ mass [37] and θ_{K^*0} is the K^*0 helicity angle, i.e. the angle between the K^+ and D directions in the $K^+\pi^-$ rest frame. To reduce correlations with the values for r_B and δ_B determined from the DP analysis, the quantities $\bar{R}_B = \bar{r}_B/r_B$ and $\Delta\bar{\delta}_B = \bar{\delta}_B - \delta_B$ are calculated. The results are

$$\begin{aligned} \kappa &= 0.958_{-0.010}^{+0.005+0.002}_{-0.045}, \\ \bar{R}_B &= 1.02_{-0.01}^{+0.03} \pm 0.06, \\ \Delta\bar{\delta}_B &= 0.02_{-0.02}^{+0.03} \pm 0.11, \end{aligned}$$

where the uncertainties are statistical and systematic and are evaluated as described in the Appendix.

In summary, a data sample corresponding to 3.0 fb $^{-1}$ of pp collisions collected with the LHCb detector has been used to measure, for the first time, parameters sensitive to the angle γ from a Dalitz plot analysis of $B^0 \rightarrow DK^+\pi^-$ decays. No significant CP violation effect is seen. The results are consistent with, and supersede, the results for $\mathcal{A}_d^{KK,\pi\pi}$ and $\mathcal{R}_d^{KK,\pi\pi}$ from Ref. [62]. Parameters that are needed to determine γ from quasi-two-body analyses of $B^0 \rightarrow DK^*(892)^0$ decays are measured. These results can be combined with current and future measurements with the $B^0 \rightarrow DK^*(892)^0$ channel to obtain stronger constraints on γ .

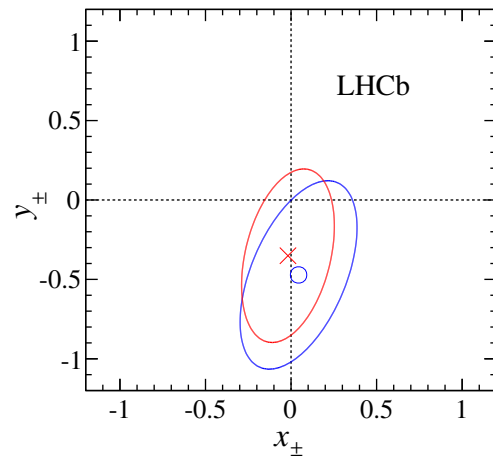
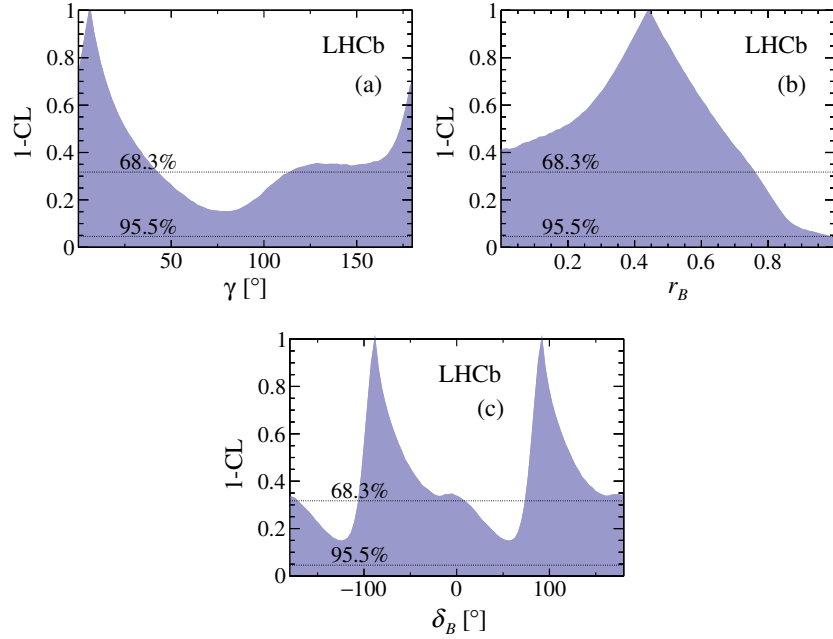
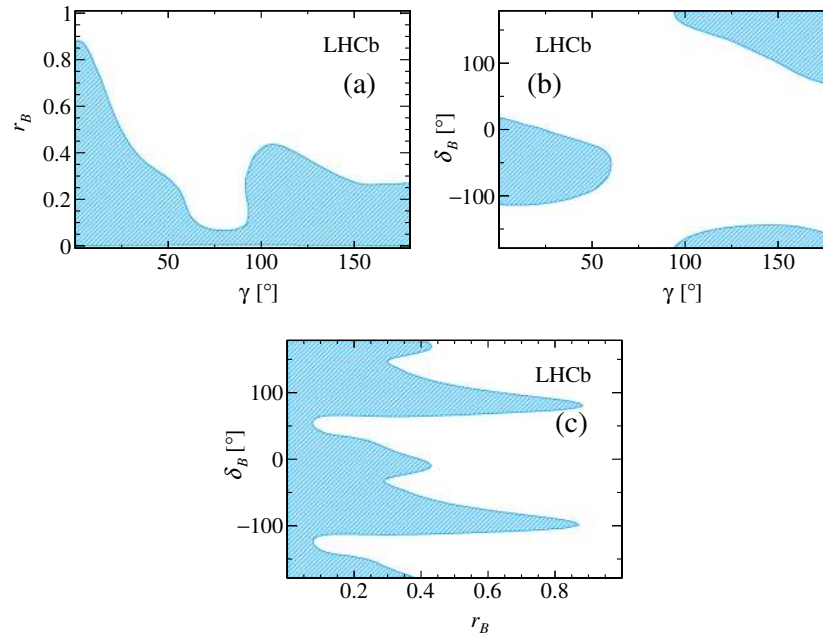


FIG. 9. Contours at 68% C.L. for the (blue) (x_+, y_+) and (red) (x_-, y_-) parameters associated with the $B^0 \rightarrow DK^*(892)^0$ decay, with statistical uncertainties only. The central values are marked by a circle and a cross, respectively.

FIG. 10. Results of likelihood scans for (a) γ , (b) r_B , and (c) δ_B .FIG. 11. Confidence level contours for (a) γ and r_B , (b) γ and δ_B , and (c) r_B and δ_B . The shaded regions are allowed at 68% C.L.

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APPENDIX: QUASI-TWO-BODY PARAMETERS

In the quasi-two-body analyses of $B^0 \rightarrow DK^*(892)^0$ decays, the following parameters are defined [17]:

$$\kappa = \left| \frac{\int |A_{cb}(p)A_{ub}(p)| \exp[i\delta(p)] dp}{\sqrt{\int |A_{cb}(p)|^2 dp \int |A_{ub}(p)|^2 dp}} \right|, \quad (\text{A1})$$

$$\bar{r}_B = \sqrt{\frac{\int |A_{ub}(p)|^2 dp}{\int |A_{cb}(p)|^2 dp}}, \quad (\text{A2})$$

$$\bar{\delta}_B = \arg \left(\frac{\int |A_{cb}(p)A_{ub}(p)| \exp[i\delta(p)] dp}{\sqrt{\int |A_{cb}(p)|^2 dp \int |A_{ub}(p)|^2 dp}} \right), \quad (\text{A3})$$

where all the integrations are over the part of the phase space p inside the used $K^*(892)^0$ selection window. In

these equations, $|A_{cb}(p)|$ and $|A_{ub}(p)|$ refer to the magnitudes of the total V_{cb} and V_{ub} amplitudes, and $\delta(p)$ is their relative strong phase. In terms of the parameters used in this analysis,

$$|A_{cb}(p)| = \left| \sum_j c_j F_j(p) \right|, \quad (\text{A4})$$

$$|A_{ub}(p)| = \left| \sum_j c_j r_{B,j} \exp[i\delta_{B,j}] F_j(p) \right|, \quad (\text{A5})$$

$$\delta(p) = \arg \left(\frac{\sum_j c_j r_{B,j} \exp[i\delta_{B,j}] F_j(p)}{\sum_j c_j F_j(p)} \right), \quad (\text{A6})$$

where the $r_{B,j}$, $\delta_{B,j}$ values are allowed to differ for each $K^+\pi^-$ resonance, and $r_{B,j} = 0$ for $D\pi^-$ resonances. [The r_B , δ_B notation without the j subscript is retained for the parameters associated with the $B^0 \rightarrow DK^*(892)^0$ decay.] In the limit that there is no amplitude (either resonant or nonresonant) contributing within the $K^*(892)^0$ selection window other than those associated with the $B^0 \rightarrow DK^*(892)^0$ decay, one finds $|A_{ub}(p)| \rightarrow r_B |A_{cb}(p)|$ and $\delta(p) \rightarrow \delta_B$, and hence $\kappa \rightarrow 1$, $\bar{r}_B \rightarrow r_B$, and $\bar{\delta}_B \rightarrow \delta_B$. In order to reduce correlations between \bar{r}_B and r_B and between $\bar{\delta}_B$ and δ_B , it is convenient to introduce the parameters

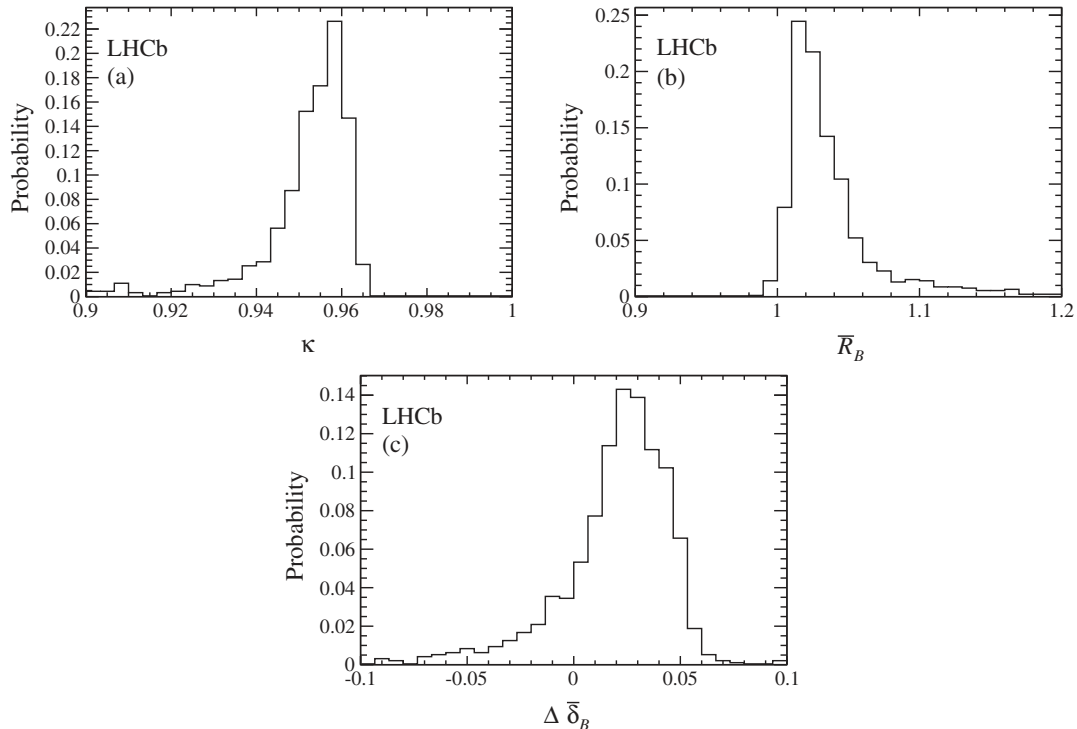


FIG. 12. Distributions of (a) κ , (b) \bar{R}_B , and (c) $\Delta \bar{\delta}_B$, obtained as described in the text.

$$\bar{R}_B = \frac{\bar{r}_B}{r_B}, \quad (\text{A7})$$

$$\Delta\bar{\delta}_B = \bar{\delta}_B - \delta_B, \quad (\text{A8})$$

which are obtained by replacing all $r_{B,j}$ by $r_{B,j}/r_B$ and all $\delta_{B,j}$ by $\delta_{B,j} - \delta_B$ in Eqs. (A4)–(A6).

These quantities are determined from the results of the Dalitz plot analysis. An alternative fit is performed with $x_{\pm,j} + iy_{\pm,j}$, defined in Eq. (2), replaced by $r_{B,j} \exp[i(\delta_{B,j} \pm \gamma)]$. The results of this fit are consistent with the values for γ , r_B , and δ_B obtained from the fitted x_{\pm} and y_{\pm} , and are used to evaluate $|A_{cb}(p)|$, $|A_{ub}(p)|$ and $\delta(p)$ at many points inside the selection window and thereby to determine κ , \bar{R}_B , and $\Delta\bar{\delta}_B$. The procedure is repeated many times with both V_{cb} and V_{ub} amplitude model parameters varied within their statistical

uncertainties from the fit, leading to the distributions shown in Fig. 12. Since the transformations from the fitted model parameters to the quasi-two-body parameters are highly nonlinear, the reported central values correspond to the peak positions of these distributions, while positive and negative uncertainties are obtained by incrementally including the most probable values until 68% of all entries are covered.

Sources of systematic uncertainty are accounted for by evaluating their effects on the quasi-two-body parameters. The dominant sources are from the use of an alternative description of the $K^+\pi^-$ S-wave, and from changing the treatment of CP violation in the $D_{s1}^*(2700)^+$ component and the $K^+\pi^-$ S-wave. Most systematic uncertainties are symmetrized for consistency with the rest of the analysis, but asymmetric systematic uncertainties are reported on κ since this quantity is ≤ 1 by definition.

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