



# Article Contact Characteristics at Interface in Three-Body Contact Conditions with Rough Surfaces and Foreign Particles

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Abstract: Nanoparticles as lubricant additives under a certain average diameter and concentration may reduce wear, friction and scuffing damage. However, atmospheric dust particles affect not only human health but also the efficiency of components, and even cause component failures. Therefore, the contact characteristics at interfaces with foreign particles require careful investigation. In this work, a 3-body microcontact mechanics concept is used to analyze the effects of wear debris and foreign particles on real contact area, contact mode, asperity deformation type and separation at interface. The results show that the relationship profile between dimensionless real contact area  $(A_t^*)$  and dimensionless normal contact load  $(F_t^*)$  is wedge-shaped in a 3-body contact interface. Using surface-to-surface 2-body contact area as upper bound and surface-to-particle 3-body contact as lower bound, the 3-body hybrid contact situation is in between upper and lower bounds. As the dimensionless normal contact load increases,  $A_t^*$  increases gradually as well. The order of contact mode is p-s contact, hybrid contact and then s-s contact. If the 3-body contact interface is in hybrid contact mode, the decrease in the hardness and average third body diameter will cause the  $A_t^*$ to increase significantly at the same  $F_t^*$ . Conversely, the separation and real contact area ratio of plastic deformation decrease gradually. The turning point of contact area (TPCA) occurs when the contact mode is within hybrid contact mode and the ratio of average third body diameter to the composite equivalent surface RMS roughness is about 50-70% for foreign particles and wear debris. When the  $F_t^*$  is slightly larger than  $F_{tpca}^*$ , the third body and surface share the total interface load approximately equally which will help reduce the real contact pressure and plastic contact area to improve surface performance.

**Keywords:** 3-body microcontact mechanics; wear debris; real contact area; interface separation; deformation type; foreign particle

# 1. Introduction

In the recent development of lubricants, adding particles to lubricants is one of the important directions because they can enhance the lubricant's interfacial tribological properties. Among factors affecting the tribological performance of nanolubricants, the size and concentration of nanoparticles have been widely studied [1–8]. However, in the literature reports on particle additives, the optimal particle size or optimal concentration for different interface conditions varies greatly. Ghaednia et al. [1] conducted wear experiments with 0.5–2.0 wt% CuO nanoparticles added to the base oil. The results showed that the wear increased when the nanoparticle concentration reached 1.0 wt%, and then reduced at 2.0 wt%. Horng et al. [2] used the three-body microcontact temperature model and application analysis on high-speed ball screws to prove that the optimal particle size is 170–250 nm when the equivalent surface roughness value of the interface is 0.30–0.40  $\mu$ m. Awang et al. [3] proposed a novel Cellulose Nanocrystals (CNC) nanoparticle as a green lubricant, and conducted wear tests by adding 0.1–0.9 wt% to the engine oil. The results



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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). showed that the addition of 0.1% nanoparticles to the oil has excellent tribological properties. Cortes et al. [4] studied the effects of different concentrations (0.25–1.25 wt%) of  $SiO_2$  and  $TiO_2$  nanoparticles on the lubricity of sunflower oil.  $SiO_2$  and  $TiO_2$  nanoparticle were considered effective additives for sunflower oil as they can reduce friction coefficient and wear volume loss by 77.7% and 74.1%, and 93.7% and 70.1%, respectively. The optimal particle concentrations of SiO<sub>2</sub> and TiO<sub>2</sub> were obtained at 1.25 wt% and 1.0 wt%, respectively. Kumar et al. [5] studied the effect of various sizes of Polytetrafluoroethylene (PTFE) nanoparticles (50 nm, 6.0  $\mu$ m, 9.0  $\mu$ m and 12  $\mu$ m) in lithium-based grease. Results of tibo-tests revealed that the 6µm particles showed slightly better performance. In 2021, Kanojia et al. [6] added different concentrations of  $SiO_2$  nanoparticles (0.3, 0.9) and 1.5 wt%) in Mahua oil and performed tribological analysis. The addition of 0.3 wt% nanoparticles resulted in a good improvement in reducing friction, wear and scar formation on the surface. Ta et al. [7] added different concentrations (0.2 and 0.5 wt%) of CuO and ZnO nanoparticles to the ionic liquid. This method could enhance the anti-wear ability and reduce friction of the ionic liquid. The results illustrated that the best tribological performance was observed at the concentration of 0.2 wt% ZnO among the two types of nanoparticles and two concentrations tested. Abdel-Rehim et al. [8] proposed that Oleic Acid can be used as a surfactant and added three concentrations of nanoparticles (0.2, 0.5 and 1.0 wt%) to a mineral base lubricant. The experimental results showed that the optimal concentration of CuO nanolubricant was 0.5 wt%. Conversely, when the concentration was increased to 1.0 wt%, aggregation was observed leading to the deterioration of friction and dispersion. From the above research, it is found that the optimal values of nanoparticle concentration and size are clearly related to the material types of particles and interface, and even have a great influence on the surface roughness of the specimen. As a result, the analysis of the microcontact characteristics of the three-body interface is a basic but important first step in solving this problem.

In the past, the relative motion interface research was based on a two-body (2-body) contact model for mechanics, thermal, material, electrical and mechanism analysis. However, 2-body contact is the ideal condition of the machine interface, occurring at the moment when the moving interface of the machine parts start to operate. Due to the environmental particles–particle additives or wear debris, named the third body–the actual interface of machine parts is a three-body (3-body) contact. Therefore, the 3-body mechanics analysis of the interface will be more realistic to the actual characteristics of the interface. As said by Valentin L. Popov in a paper published in 2018 [9], one of the great challenges of the tribology future in tribology research is to solve the problem of the third body. The conclusion reached in a review paper by James A. Greenwood in 2020 [10] stated that [Yes, study the behavior of trapped particles: but if all transfer and wear is attributed to third bodies, the term has become too wide to be useful. But at least stop studying the purely normal contact of rough surfaces]. This explains why the use of the 2-body contacts analysis method of rough surface to solve the rubbing problem should be halted, and the relative motion interface analysis should at least consider the three solid body model.

Lots of 2-body classic microcontact mechanics models have been proposed in the past to study the contact behavior of the interface. Those models allow for the study of the basic mechanics of contact properties and predict the damage and failure characteristic at the interface. In 1966, Greenwood and Williamson [11] first proposed a 2-body contact model with multiple rough asperities. However, it is only applicable for elastic contact deformation (GW model). The plastic contact area of the rough surface is the main area where the wear occurs. Chang, Etsion and Bogy [12] proposed the CEB model combining elastic and plastic deformation phenomena. Nevertheless, this model still has the problem of discontinuity in the conversion process between elastic and plastic deformation. Zhao, Maietta and Chang [13] proposed a complete model of contact behavior from elastic to elastoplastic and then to plastic deformation (ZMC model). Kogut and Etsion [14] used a finite element model to simulate the discontinuity problems of the elastic–plastic region (KE model). Since the roughness of the general machined surface is directional, Horng [15] proposed a generalized ellipse asperity contact model. This model not only had simplified the CEB model, but also considered directional rough asperity (H model). Chen and Etsion [16] incorporated a GW statistical multi-coated-asperity surface model with existing single-coated-asperity contact models. Then an elastic–plastic coated rough surface contact model was proposed. In 2020, Li et al. [17] proposed a new contact model considering asperity interaction and surface waviness. Comparing with other models, the results obtained from this proposed model are more consistent with the experimental results.

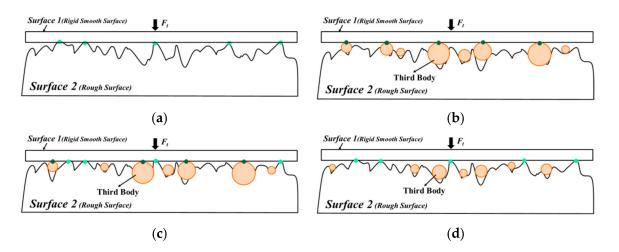
A 3-body contact system is formed when particles are found at the interfaces. Godet in 1984 first proposed the concept of "third body" and the importance of its influence [18,19]. Unfortunately, the subsequent relatively detailed analysis was somewhat paused. In the past, the fluid mechanics of the lubricant and the physical/chemical reactions of the surface were mainly discussed for the third body. By contrast, the contact mechanics of the solid particle at the interface, and the influence on tribological properties such as oil film thickness, viscosity, reaction film, and lubrication regime were rarely mentioned. For example, most studies ignored the force balance at the interface of the three bodies, or only discussed the dry abrasive wear of the three bodies [20–23]. Without considering the effect of the third body on the 2-body lubrication wear [24,25], resulting in assumptions about the load-sharing ratio of the liquid, surface and particle load are different from the actual load for the three bodies. The relationship between the real contact area and the separation between interfaces (considering different average third body diameter and equivalent surface RMS roughness) has not been analyzed.

In the study of 3-body contact simulations, Khonsari [26] focuses primarily on the application and analysis of elastohydrodynamic lubrication of fluid with particles, and gives examples to illustrate the modeling aspects of bearing lubrication at various particle concentrations. Zhang and Tanaka [27] studied the wear and friction mechanism in silicon induced by 2-body and 3-body sliding contact. They found that the friction force is a function of the real contact area. Amorphous phase transformation is the main deformation on the silicon surface. In the microscale abrasive wear test experiment by Trezona et al. [28], the maximum wear rate occurs at intermediate slurry concentrations. They also found that a transition from grooving to rolling wear could be identified by a critical ratio of load to slurry concentration. However, the contact mechanics of the above turning phenomena had not yet been thoroughly discussed. Stempfle et al. [29] used a scan thermal microscope to investigate the relationship between the contact temperature and thermal power dissipated in 3-body contact. Based on the GW microcontact model, the effect of applied force on the real contact area was also studied. Ghaednia and Jackson [30] studied the effect of nanoparticles on the real area of contact and friction based on fractal mathematics. The result found a linear relationship between dimensionless contact area and contact force. Particles reduce the real contact area at interface and, therefore, decrease the friction force. Ghaednia et al. [31] extended the 2-body GW model to 3-body contact simulation and application in electrical contact properties. They also found that particles could reduce the real contact area and contact thermal conduction. Eder [32] presented a molecular dynamics (MD) simulation to study nano-wear of rough surfaces under 2-body and 3-body contact conditions with abrasive particles. This method enables researchers to study the effect of multiple abrasives on changing nanoscale surface topography. The above numerical analysis studies are based on elastic contact mechanics. However, the contact area includes elastic, elastoplastic and plastic deformations at the actual interface. In 2015, Wu et al. [33] analyzed the peak contact temperature of rough surfaces under 3-body contact, but did not consider the transition mechanism of various 3-body contact modes and the change of micro-asperity deformation. Horng et al. [34] combined contact mechanics and lubrication theory to study the mixed lubrication properties at 3-body interfaces. They show that the conventional film parameter ( $\lambda$ ) was not a sufficient indicator of various lubrication regimes in 3-body contact. Thus, the  $\lambda$  of the 3-body interface should consider the third particle effect to confirm the mixed lubrication regime. In conclusion, the third body in the 3-body contact has a great influence on the thermal, electrical and tribological properties

of the interface [35]. Moreover, both the elastic deformation and plastic deformation of the contact zone make a large difference to the performance of the contact interface [36,37]. They definitely cause changes in surface stress, strain and failure, such as pitting [38] and scuffing [39] as surface damage. At the interface of mechanical components, not only the wear debris, but also the environmental particles often cause component damage. The foreign particles in this article include environmental particles and wear debris from the other machine components in a circulation system. This study mainly discusses: the influence of foreign particles on the different deformation areas of the total contact area; separation at interface; the difference between the foreign particles and wear debris under different average diameters of the third body; and equivalent surface RMS roughness and normal contact load. The influence of foreign particles on the contact modes and deformation characteristics of the 3-body contact interface is analyzed based on the force balance of the 3-body interface.

#### 2. Theoretical Analysis

When two rough surfaces are in contact with each other, this can be simplified into an equivalent rough surface and a flat surface (s-s 2-body contact) [40,41], as shown in Figure 1a. However, if third bodies exist at the contact interfaces, there will be three kinds of contact mode according to the relative values of the diameter of the third body to the separation of the two surfaces. In the first contact mode, namely 3-body particle-tosurface contact (3-body p-s contact), the diameter of the third body is much larger than the separation of the two surfaces. The particles completely separate the two surfaces. The normal contact load is borne by the contact points between the third bodies and the surface, as shown in Figure 1b. In the second contact mode, that is 3-body hybrid contact, the difference between the diameter of the third body and the separation between the two surfaces is small. The third bodies with surface and the two surface contact points share the normal contact load, as shown in Figure 1c. In the third contact mode, 3-body surface-to-surface contact (3-body s-s contact), the diameter of the third body is much smaller than the separation between the two surfaces and all the third bodies sink into the trough. The normal contact load is borne by the contact points of the two surfaces, as shown in Figure 1d.



**Figure 1.** The contact mode at the contact interfaces "Reprinted/adapted with permission from Ref. [42]. 2017, Wu, H.W.; Chen, Y.Y.; Horng, J.H." (a) for 2-body contact (b) for 3-body particle-to-surface contact (c) for 3-body hybrid contact and (d) for 3-body surface-to-surface contact.

In the contact model, the following assumptions were made [42]:

1. The peak of the surface roughness is hemispherical with constant radius of curvature (*R*) and the Gaussian distribution  $\phi(z)$  shows the change of the peak height.

- 2. All surface asperities are separated by a far distance and there is no interaction between them.
- 3. There is no bulk deformation, but the surface asperities may deform during contact.
- 4. The shape of the third body is spherical [43–46], and the average diameter of the third body is  $x_{a}$ .
- 5. The slopes of surface asperities are negligibly small.

A schematic diagram of the interface of surface 1, surface 2, and third bodies in a 3-body contact system is shown in Figure 2, where  $x_a$  is average diameter of the third body,  $\phi_a(x)$  is probability density function of the third body diameter and  $X_{max}$  is the maximum diameter of the third body. The 2-body microcontact model used in this study is the ZMC model. According to the 3-body microcontact model [26], the normal contact load  $F_t$  and total real contact area  $A_t$  are as follows:

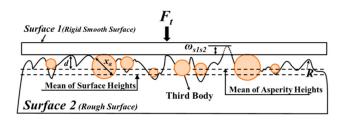


Figure 2. Schematic of a 3-body contact system.

$$F_{t} = F_{ss} + F_{sa}$$

$$= \left[\frac{4}{3}\eta A_{n}E_{ss}R^{\frac{1}{2}}\int_{d}^{d+\omega_{1}}\omega^{\frac{2}{3}}\phi(z)dz + \eta A_{n}\pi R\int_{d+\omega_{1}}^{d+\omega_{2}}\left[H - H(1-k)\frac{\ln\omega_{2} - \ln\omega}{\ln\omega_{2} - \ln\omega_{1}}\right] \times \left[1 - 2\left(\frac{\omega - \omega_{1}}{\omega_{2} - \omega_{1}}\right)^{3} + 3\left(\frac{\omega - \omega_{1}}{\omega_{2} - \omega_{1}}\right)^{2}\right]\omega\phi(z)dz + 2\pi\eta A_{n}HR\int_{d+\omega_{2}}^{\infty}\omega\phi(z)dz\right] \times \left(1 - \frac{\pi H_{s1}\eta_{a}}{H_{s1} + H_{s2}}\int_{X_{\min}}^{X_{\max}}x_{a}^{2}\phi_{a}(x)dx\right)$$

$$+ \frac{\pi H_{s1}H_{s2}\eta_{a}A_{n}}{H_{s2} + H_{s1}}\left[\frac{9\pi^{2}}{4}\left(\frac{H_{s1}^{2}}{E_{sa}^{2}} + \frac{H_{s2}^{2}}{E_{ss}^{2}}\right)\int_{d-h_{e}}^{d}x_{a}^{2}\phi_{a}(x)dx + \int_{d}^{x_{\max}}x_{a}^{2}\phi_{a}(x)dx\right]$$
(1)

$$A_{t} = A_{ss} + A_{sa} = \left[\eta A_{n} \pi R \int_{d}^{d+\omega_{1}} \omega \phi(z) dz + \eta A_{n} \pi R \int_{d+\omega_{1}}^{d+\omega_{2}} \omega \left[1 - 2\left(\frac{\omega-\omega_{1}}{\omega_{2}-\omega_{1}}\right)^{3} + 3\left(\frac{\omega-\omega_{1}}{\omega_{2}-\omega_{1}}\right)^{2}\right] \phi(z) dz + 2\eta A_{n} \pi R \int_{d+\omega_{2}}^{\infty} \omega \phi(z) dz \right] \times \left\{1 - \frac{\pi H_{s1} \eta_{a}}{H_{s1} + H_{s2}} \int_{d}^{x_{max}} x_{a}^{2} \phi_{a}(x) dx\right\} + \frac{\pi H_{s2} \eta_{a} A_{n}}{H_{s2} + H_{s1}} \left[\frac{9\pi^{2}}{4} \left(\frac{H_{s1}^{2}}{E_{sa}^{2}} + \frac{H_{s2}^{2}}{E_{ss}^{2}}\right) \int_{d-h_{e}}^{d} x_{a}^{2} \phi_{a}(x) dx + \int_{d}^{x_{max}} x_{a}^{2} \phi_{a}(x) dx\right]$$
(2)

where  $F_{ss}$  is the contact load of surface 1 and surface 2,  $F_{sa}$  is the contact load of the third body and surface 1,  $\eta$  is the asperity density, R is the radius curvature of surface asperity peak,  $A_n$  is the apparent contact area at the interface,  $\phi(z)$  is probability density function of the asperity height,  $H_{s1}$  is the hardness of surface 1,  $H_{s2}$  is the hardness of surface 2,  $\eta_a$  is number of third bodies per unit area,  $E_{sa}$  is equivalent elastic modulus of the third body and surface,  $E_{ss}$  is equivalent elastic modulus of the two surfaces,  $h_e$  is the maximum separation between the two surfaces with third bodies, d is separation between the surface 1 and mean height of asperities,  $A_{ss}$  is the real contact area of surface 1 and surface 2,  $A_{sa}$  is the real contact area of the third body and surface 1, and  $\omega$ ,  $\omega_1$ , and  $\omega_2$  are the interference, critical interference at the point of initial yield, and critical interference at the point of fully plastic flow, respectively. When  $x_a = 0$  nm, Equations (1) and (2) are the same as for the 2-body ZMC contact model. The relationship between the average interference  $\omega$  and the contact pressure  $P_a$  can be obtained from Hertz theory:

$$\omega = \left(\frac{3\pi P_a}{4E_{ss}}\right)^2 R \tag{3}$$

According to the theory proposed by Tabor [47], the relationship between the average contact pressure  $P_a$  at the initial yield point and the hardness *H* can be written as:

$$P_a = kH \tag{4}$$

where *k* is the mean contact pressure factor and its value is 0.4, and *H* is hardness of the softer material. Then, substituting Equation (4) into Equation (3), the critical interference  $\omega_1$  at the point of initial yield can be obtained as follows:

$$\omega_1 = \left(\frac{3\pi kH}{4E}\right)^2 R \tag{5}$$

According to the research result proposed by Johnson [48], the critical interference at the point of fully plastic flow can be expressed as:

$$\omega_2 > 54\omega_1 \tag{6}$$

From the above equations, when  $\omega < \omega_1$ , the surface only experiences elastic deformation; when  $\omega_1 < \omega < \omega_2$ , the surface experiences both elastoplastic and plastic deformation; and when  $\omega > \omega_2$ , the surface experiences only plastic deformation.

To simplify the analysis, this study assumes that both  $\phi_a(x)$  and  $\phi(z)$  are Gaussian distributions, as shown in Equation (7) and Equation (8) [42]:

$$\phi_a(x) = \frac{1}{\sqrt{2\pi} \times \sigma_a} \exp\left[-0.5\left(\frac{x-x_a}{\sigma_a}\right)^2\right]$$
(7)

$$\phi(z) = \frac{1}{\sqrt{2\pi} \times \sigma_s} \exp\left[-0.5\left(\frac{z-\sigma}{\sigma_s}\right)^2\right]$$
(8)

The relationship between  $\sigma$  and  $\sigma_s$  is shown in Equation (9) [49]:

$$\sigma_s / \sigma = \left(1 - \frac{0.8968}{\alpha_s}\right)^{0.5} \tag{9}$$

where  $\sigma_a$  is the standard deviation of the diameter of the third body,  $\sigma_s$  is the standard deviation of the asperity heights, and the value of  $\alpha_s$  is usually around 5.0 and tends to be a constant for a given type of surface finishing [50]. However, due to the different heights of the rough asperities at the interface, this contact deformation includes three types of deformation—elastic, elastoplastic and plastic—under the same contact load. Therefore, the total real contact area is the summation of the elastic, elastoplastic and plastic deformation areas, as shown in Equations (10)–(13).

$$A_t = A_e + A_{ep} + A_p \tag{10}$$

$$A_e = \eta A_n \pi R \int_d^{d+\omega_1} \omega \phi(z) dz \times \left( 1 - \frac{\pi H_{s1} \eta_a}{H_{s1} + H_{s2}} \int_d^{x_{\text{max}}} x_a^2 \phi_a(x) dx \right)$$
(11)

$$A_{ep} = \eta A_n \pi R \int_{d+\omega_1}^{d+\omega_2} \omega \left[ 1 - 2\left(\frac{\omega - \omega_1}{\omega_2 - \omega_1}\right)^3 + 3\left(\frac{\omega - \omega_1}{\omega_2 - \omega_1}\right)^2 \right] \phi(z) dz \times \left( 1 - \frac{\pi H_{s1} \eta_a}{H_{s1} + H_{s2}} \int_{d}^{x_{max}} x_a^2 \phi_a(x) dx \right)$$
(12)

$$A_{p} = 2\eta A_{n} \pi R \int_{d+\omega_{2}}^{\infty} \omega \phi(z) dz \times \left(1 - \frac{\pi H_{s1} \eta_{a}}{H_{s1} + H_{s2}} \int_{d}^{x_{max}} x_{a}^{2} \phi_{a}(x) dx\right) + \frac{\pi H_{s2} \eta_{a} A_{n}}{H_{s2} + H_{s1}} \left[\frac{9\pi^{2}}{4} \left(\frac{H_{s1}^{2}}{E_{sa}^{2}} + \frac{H_{s2}^{2}}{E_{ss}^{2}}\right) \int_{d-h_{e}}^{d} x_{a}^{2} \phi_{a}(x) dx + \int_{d}^{x_{max}} x_{a}^{2} \phi_{a}(x) dx\right]$$
(13)

Equations (1) and (2) will become the dimensionless normal contact load and dimensionless real contact area by dividing by  $A_n E_{ss}$  and  $A_n$ , respectively.

$$F_t^* = \frac{F_t}{A_n E_{ss}}, A_t^* = \frac{A_t}{A_n}$$
(14)

 $A_{ss}$ ,  $A_{sa}$ ,  $A_e$ ,  $A_{ep}$  and  $A_p$  can be divided by  $A_n$  or  $A_t$  to obtain the dimensionless contact area ratio. In addition, the parameters of related length are divided by  $\sigma$  to obtain the dimensionless value. The dimensionless parameters are defined in the Nomenclature section.

## 3. Results and Discussion

In this study, the material of the two relatively moving surfaces is S45C. In order to compare the difference between foreign particles and wear debris, the third bodies in this paper contain SiO<sub>2</sub> (foreign particles) and S45C (wear debris). SiO<sub>2</sub> particles are used as the third bodies because dust contains about 80% of SiO<sub>2</sub> and 10% of Al<sub>2</sub>O<sub>3</sub> in the environment [51]. It is also one of the materials used for particle additives in lubricants [6]. The wear debris does not consider the work hardening of the material rolling process, so the hardness is the same as that of surface 1 and surface 2. The material properties for surface 1, surface 2 and the third body are listed in Table 1. The operating conditions are as shown in Table 2.

Table 1. Properties of material for surface 1, surface 2 and the third body.

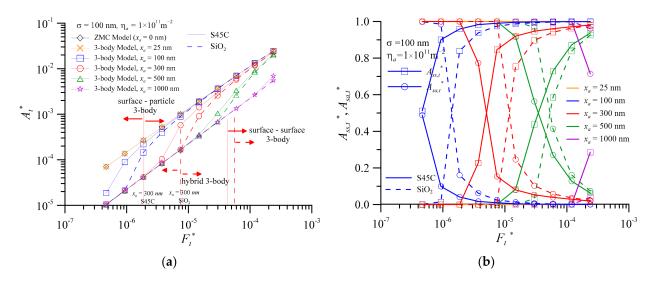
Surface 1 and Surface 2 (S45C)		
Property	Value	
Hardness, $H_{s1}$ , $H_{s2}$ (GPa) Young's modulus, E (GPa) Poisson ratio, v	5.0 205 0.29	
Third Body		
Property	Value	
Wear debris (S45C)		
Hardness, <i>H</i> <sub>a</sub> (GPa) Young's modulus, <i>E</i> (GPa) Poisson ratio, <i>v</i>	5.0 205 0.29	
Foreign particles (SiO <sub>2</sub> )		
Hardness, H <sub>a</sub> (GPa) Young's modulus, E (GPa) Poisson ratio, v	7.7 68 0.19	

Table 2. Operating conditions for this study.

Property	Value
Normal contact load, $F_t$ (N)	0.16–80
Equivalent surface RMS roughness, $\sigma$ (nm)	50-500
Number of particles per unit area, $\eta_a$ (m <sup>-2</sup> )	$10^{11}$
Average diameter of third body, $x_a$ (nm)	0–1000

Figure 3 shows the dimensionless real contact area versus dimensionless normal contact load for the third bodies at various average diameters of the third body when  $\sigma = 100$  nm. The dimensionless real contact area  $A_t^*$  versus dimensionless normal contact load is shown in Figure 3a. The real contact area ratio between surface 1 and surface 2  $(A_{ss,t}^*)$  and real contact area ratio between third body and surface 1  $(A_{sa,t}^*)$  versus dimensionless normal contact load is shown in Figure 3b. The curve for  $x_a = 0$  nm is obtained from the ZMC 2-body contact model. The  $A_t^*$  for  $x_a = 0$  nm overlaps the curve for  $x_a = 25$  nm. The

 $A_t^*$  increases with increase in dimensionless normal contact load and is larger than various average third body diameters and third body materials at any dimensionless normal contact load. Under the same dimensionless normal contact load, adding the average diameters of third bodies larger than 25 nm, the dimensionless real contact area will decrease. This result has the same trend as the experimental inference of Ghaednia et al. [1]. The reason for the overlap between  $x_a = 25$  nm and  $x_a = 0$  nm can be found in Figure 3b, since  $A_{ss,t} = 100\%$  for  $x_a = 25$  nm belongs to 3-body s-s contact. Therefore, the third bodies have almost no effect on the change of real contact area. This means that third bodies sink into surface roughness valleys. In addition, when  $x_a = 1000$  nm, the dimensionless real contact area between S45C and SiO<sub>2</sub> is almost the same. However, the SiO<sub>2</sub> curve with  $x_a = 1000$  nm is almost parallel to  $x_a = 0$  nm except for the high dimensionless normal contact load value of  $2.4 \times 10^{-4}$ . This means that for all the loads in this study, the contact is in 3-body p-s contact mode. The dimensionless real contact area is only about 15–22% for  $x_a = 0$  nm. The above results show that larger average diameter of third bodies makes a smaller dimensionless real contact area than in pure 2-body contact mode ( $x_a = 0$  nm). This means that the true contact pressure will increase at least 4.5 times or even greater, which will cause the interface contact temperature and wear to rise dramatically. Therefore, the presence of excessively large average diameter of third bodies at the interfaces is one of the important factors for excess wear failure of mechanical components.



**Figure 3.** Real contact area versus dimensionless contact load, with  $\sigma = 100$  nm, two kinds of third body materials and different average third body diameters (**a**) dimensionless real contact area ratio,  $A_t^*$  (**b**) real contact area ratio of surface 1 and surface 2,  $A_{ss,t}^*$  and real contact area ratio of third body and surface 1,  $A_{sa,t}^*$ .

This is shown by the circle symbol dotted line with  $x_a = 300$  nm of SiO<sub>2</sub> in Figure 3a. As the dimensionless normal contact load increases, the dimensionless real contact area can be roughly divided into three stages. The first stage overlaps the curve of  $x_a = 1000$  nm. Then, the second stage is the rapid increase in  $F_t^*$  from  $7.5 \times 10^{-6}$  to  $5.1 \times 10^{-5}$ . Finally, the third stage is moving to the curve of  $x_a = 0$  nm. This phenomenon can be found by the real contact area ratio between the third body and surface 1 ( $A_{sa,t}^*$ ) and the real contact area ratio between surface 1 and surface 2 ( $A_{ss,t}^*$ ) to the dimensionless real contact area in Figure 3b with  $x_a = 300$  nm of SiO<sub>2</sub> (circle symbol dotted line). When the  $F_t^*$  is less than  $7.5 \times 10^{-6}$  and  $A_{sa,t}^* = 100\%$ , the contact is in 3-body p-s contact mode.  $A_{sa,t}^*$  rapidly decreases and  $A_{ss,t}^*$  rapidly increases at the same time when the  $F_t^*$  is greater than  $5.1 \times 10^{-5}$  and  $A_{ss,t}^* > 95\%$ , the third contact stage is in 3-body s-s contact mode. For  $x_a = 0$  nm of SiO<sub>2</sub>, the slope of  $A_t^*$  to  $F_t^*$  curve is about 0.69. The real contact pressure slightly increases

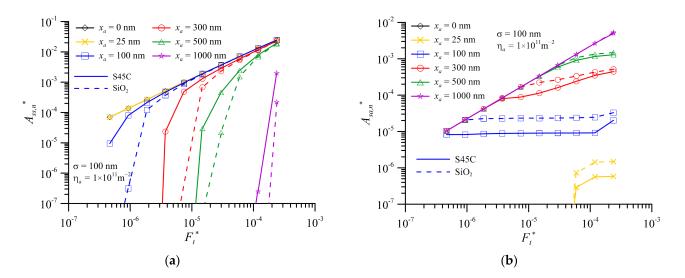
with the increase in  $F_t^*$ . When  $x_a = 1000$  nm, the value of slope increases to 1.03. However, the real contact pressure slightly decreases with the increase in  $F_t^*$ . For  $x_a = 300$  nm of SiO<sub>2</sub> and  $F_t^* = 7.5 \times 10^{-6}$ – $5.1 \times 10^{-5}$ , the contact is within a 3-body hybrid contact mode. The value of slope is significantly larger than that of  $x_a = 1000$  nm. Therefore, the real contact pressure decreases rapidly as the dimensionless normal contact load increases when the contact mode of interface is the 3-body hybrid contact.

From the previous discussions, the phenomena of 3-body contact can be summarized for various average diameters of the third body. First, the relationship between the dimensionless real contact area and the dimensionless normal contact load is wedge-shaped, approximately rectangular in shape. Second, the upper limit is the traditional 2-body s-s contact mode and the lower limit is the 3-body p-s contact mode. Third, as the dimensionless normal contact load increases, the 3-body p-s contact mode will shift into hybrid contact mode and then enter s-s contact mode.

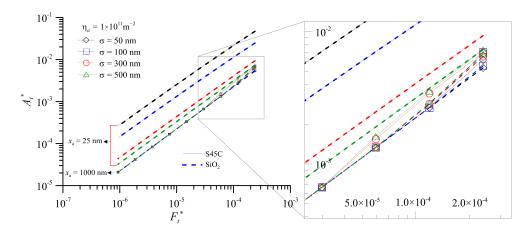
Two types of critical load were defined by the initial dimensionless normal contact load, as shown in Figure 3. The first critical load  $(F_{cr1}^*)$  is defined by the initial dimensionless normal contact load of 3-body p-s contact shift into 3-body hybrid contact mode. The second critical load  $(F_{cr2}^*)$  is defined by the initial dimensionless normal contact load of 3-body s-s contact mode. For the same  $F_t^*$ , the  $A_t^*$  of SiO<sub>2</sub> and S45C decreases with the increase in average third body diameter, as shown in Figure 3a. The  $A_t^*$  of SiO<sub>2</sub> is smaller than that of S45C for all dimensionless normal contact loads. These results indicate that the foreign particles (SiO<sub>2</sub>) cause the wear and contact temperature of the interface are higher than those for wear debris (S45C). The values of  $F_{cr1}^*$  (2.0 × 10<sup>-6</sup>) and  $F_{cr2}^*$  (4.0 × 10<sup>-5</sup>) for S45C with  $x_a = 300$  nm are smaller than those of foreign particles (SiO<sub>2</sub>), as shown in Figure 3b. Both values of  $F_{cr1}^*$  and  $F_{cr2}^*$  increase with the increase in the average diameter of the third body for the two materials. Furthermore, the value of  $F_{cr1}^*$  of SiO<sub>2</sub> is significantly larger than that of S45C. By contrast, the difference between the values of  $F_{cr2}^*$  is not obvious for the same average third body diameter.

When  $\sigma = 100$  nm and  $\eta_a = 10^{11}$  m<sup>-2</sup>, the components of dimensionless real contact area versus dimensionless normal contact load is shown in Figure 4 for two types of third body materials and various average third body diameters. The dimensionless real contact area of surface 1 and surface 2,  $A_{ss,n}^*$ , as shown in Figure 4a, has a linear relationship with  $F_t^*$  for  $x_a = 0$  nm. When  $x_a = 25$  nm, the results of  $A_{ss,n}^*$  for SiO<sub>2</sub> and S45C almost overlap with the results of  $x_a = 0$  nm. From the results of dimensionless real contact area of third body and surface1,  $A_{sa,n}^*$ , as shown in Figure 4b, particle contact phenomenon can only be found when the  $F_t^*$  is greater than  $5.1 \times 10^{-5}$ . This value of  $A_{sa,n}^*$  only accounts for less than 0.01% of the dimensionless real contact area. Since the average diameter of the third bodies is very small, they may sink into the valleys. Therefore, both SiO<sub>2</sub> and S45C are in the 3-body s-s contact mode for all dimensionless normal contact loads when  $x_a = 25$  nm. Conversely,  $A_{ss,n}^*$  starts to have value after  $F_t^* > 1.5 \times 10^{-4}$  for  $x_a = 1000$  nm. The value of  $A_{sa,n}^*$  has a linear relationship with  $F_t^*$  for SiO<sub>2</sub>, as shown in Figure 4. This means that it is in 3-body p-s contact mode for  $Ft^* < 1.5 \times 10^{-4}$ , and shifts into 3-body hybrid contact mode for  $F_t^* > 1.5 \times 10^{-4}$ .

Figure 5 shows the dimensionless real contact area versus dimensionless normal contact load at various equivalent surface RMS roughness of  $x_a = 25$  nm and  $x_a = 1000$  nm, respectively. For the SiO<sub>2</sub> with  $x_a = 25$  nm, the  $A_t^*$  increases linearly with increase in  $F_t^*$ for all equivalent surface RMS roughnesses. By contrast, the  $A_t^*$  decreases with increase in equivalent surface RMS roughness for the same  $F_t^*$ . For the same equivalent surface RMS roughness, the  $A_t^*$  of S45C almost overlaps with that of SiO<sub>2</sub>. At this moment, the contact is within 3-body s-s contact mode. When the SiO<sub>2</sub> with  $x_a = 1000$  nm and  $F_t^* < 6.0 \times 10^{-5}$ , the  $A_t^*$  increases linearly with the increase in  $F_t^*$  for all equivalent surface RMS roughnesses. The  $A_t^*$  almost overlaps for all different equivalent surface RMS roughnesses. For equivalent surface RMS roughness below 0.5 µm and average third body diameter of 1 µm, the contact is in 3-body p-s contact mode. At this time, the equivalent surface RMS roughness and third bodies have little effect on the dimensionless real contact area. When  $F_t^* > 3.0 \times 10^{-5}$ , the rising rate of  $A_t^*$  increases slightly, and the greater the equivalent surface RMS roughness, the greater the rise in  $A_t^*$ . Moreover, the  $A_t^*$  of S45C is greater than that of SiO<sub>2</sub> by about 6.8–26.6%. In addition, the  $A_t^*$  of  $x_a = 25$  nm and 1000 nm are almost parallel at the same equivalent surface RMS roughness as the dimensionless normal contact load increases when  $F_t^* < 3.0 \times 10^{-5}$ , as shown in Figure 5. The gap of  $A_t^*$  between  $x_a = 25$  nm and 1000 nm decreases with increase in equivalent surface RMS roughness. The gap of  $\sigma = 50$  nm is about 9.8 times that of  $\sigma = 500$  nm. This shows that when the equivalent surface RMS roughness gets smaller or the average third body diameter gets larger, the third body not only has a greater impact on the dimensionless real contact area, but is also more likely to cause unstable operation of the parts and surface damage. Therefore, the equivalent surface RMS roughness should not be as small as possible while conducting surface engineering design.



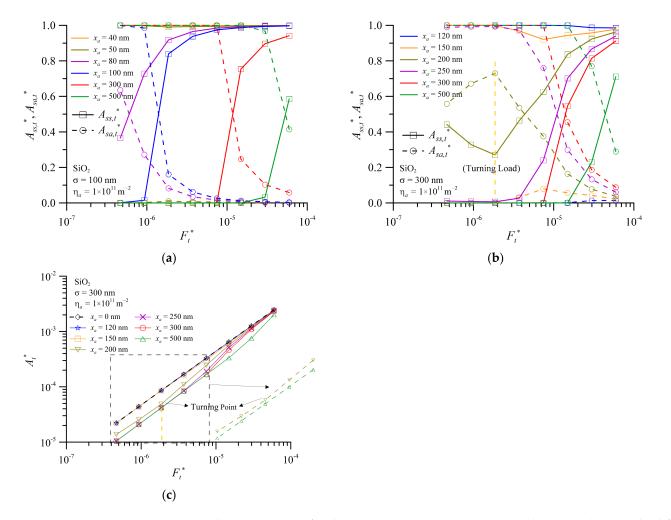
**Figure 4.** Components of dimensionless real contact area versus dimensionless normal contact load, with  $\sigma = 100$  nm,  $\eta_a = 10^{11}$  m<sup>-2</sup>, two kinds of third body materials and different average third body diameters (**a**) dimensionless real contact area of surface 1 and surface 2,  $A_{ss,n}^*$  (**b**) dimensionless real contact area of surface 1 and surface 2,  $A_{ss,n}^*$  (**b**) dimensionless real contact area of third body and surface 1,  $A_{sa,n}^*$ .



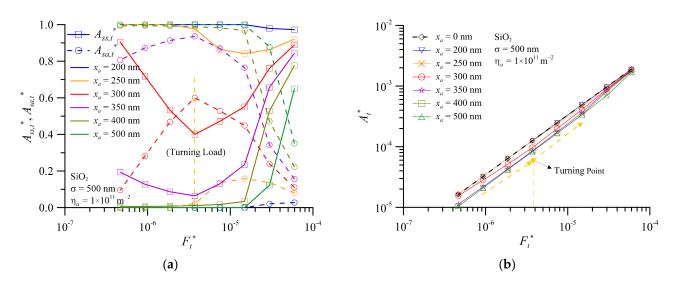
**Figure 5.** Dimensionless real contact area versus dimensionless normal contact load at various equivalent surface RMS roughnesses for  $x_a = 25$  nm and  $x_a = 1000$  nm of wear debris and foreign particles.

Figure 6 shows the components of real contact area ratio versus dimensionless normal contact load for foreign particles at (a)  $\sigma = 100$  nm, (b)  $\sigma = 300$  nm, and (c)  $A_t^*$  for  $\sigma = 300$  nm. From the results of SiO<sub>2</sub> with  $x_a = 300$  nm in Figure 4b, the increase in  $A_{sa,n}^*$  is smaller than that of the load at the 3-body hybrid contact mode. Moreover, the contact pressure

of particles increases gradually. Therefore, as shown in Figure 6a, the rapid drop in  $A_{sa,t}$ with  $x_a = 300$  nm causes the contact pressure of the third bodies to increase rapidly. This is prone to 3-body abrasive wear and increases the interface wear. It is well known that the dimensionless normal contact load of the interface is all borne by the third bodies or all the surface asperities will cause the real contact pressure to become too high. However, when the equivalent surface RMS roughness increases to 300 nm,  $x_a = 200$  nm and dimensionless normal contact load is between  $4.5 \times 10^{-7}$  and  $4.5 \times 10^{-6}$ . It is interesting to note that surface and third body have load-sharing conditions as shown in Figure 6b. This means that if the average diameter and concentration of nanoparticles are added at  $\sigma$  = 300 nm, the interface contact pressure can be balanced to improve the tribology efficiency. This situation can be clearly understood from Figure 6c. Similarly, both Figure 6b, c have a turning point at  $F_t^* = 1.9 \times 10^{-6}$ . When  $F_t^* < 1.9 \times 10^{-6}$ , the curve of  $A_t^*$  seems to coincide with  $x_a = 500$  nm. Due to the special ratio of average third body diameter to equivalent surface RMS roughness, the slope of dimensionless real contact area to dimensionless normal contact load turns a corner. The dimensionless normal contact load is shared by  $A_{ss,t}^*$  and  $A_{sa,t}^*$ , as shown in Figure 6c. This phenomenon is defined as turning point of contact area of the 3-body contact (TPCA). From the tribology engineering design point of view, the third bodies and the surface asperity crests can bear the load equally in the contact region nearby the turning point. In addition, the contact pressure in this area only increases slightly. Therefore, this will become a better design region. This phenomenon also occurs when the equivalent surface RMS roughness increases to 500 nm, as shown in Figure 7.



**Figure 6.** The components of real contact area ratio versus dimensionless normal contact load for foreign particles, SiO<sub>2</sub> at (**a**)  $\sigma$  = 100 nm (**b**)  $\sigma$  = 300 nm (**c**)  $A_t^*$  for  $\sigma$  = 300 nm.



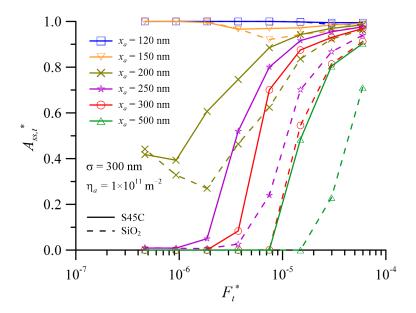
**Figure 7.** The real contact area ratio and dimensionless real contact area versus dimensionless normal contact load for foreign particles of SiO<sub>2</sub> at  $\sigma$  = 500 nm (**a**)  $A_{ss,t}^*$  and  $A_{sa,t}^*$  (**b**)  $A_t^*$ .

When the dimensionless normal contact load of turning point of contact area  $(F_{tpca})^*$ rises to  $3.0 \times 10^{-6}$ , the curve of  $A_t^*$  turns back to 3-body s-s contact mode ( $x_a = 0$  nm) from 3-body hybrid contact mode as the dimensionless normal contact load reduces, as shown in Figure 7b of  $x_a$  = 300 nm. Similarly, the curve of  $x_a$  = 150 nm in Figure 6b and the curve of  $x_a = 250$  nm in Figure 7a also return to the 3-body s-s contact mode only in the small recurve phenomenon. As shown in Figures 6 and 7, this TPCA phenomenon is found for the  $SiO_2$ particle concentration of  $1.0 \times 10^{11}$  m<sup>-2</sup> and  $x_a/\sigma \approx 0.5$ –0.7. This result is similar to the experimental results obtained by Peña-Parás et al. [52] when the effect of reducing friction and wear was observed at  $x_a/\sigma$  less than 0.7. Note that this ratio value is related to the material properties and operation conditions of the three bodies. This also shows that when nanoparticles are added to the lubricant under various operating conditions, the optimum wear and friction properties are obtained at the appropriate concentration and average third body diameter, rather than a higher average diameter being necessarily better [1-3,6]. Comparing Figures 3a, 6c and 7b, one can find that larger values of equivalent surface RMS roughness will result in a narrower area of relationship between the dimensionless real contact area and the dimensionless normal contact load under 3-body contact mode.

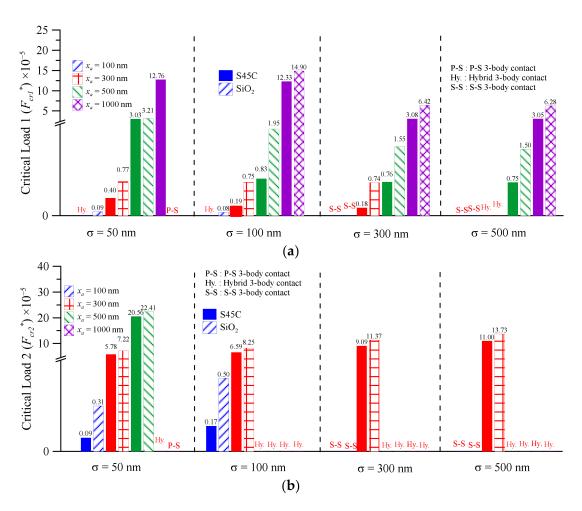
Figure 8 takes  $A_{ss,t}^*$  as an example to illustrate the difference between the two kinds of third body materials under the same conditions as shown in Figure 6b. At the same dimensionless normal contact load, because the hardness of SiO<sub>2</sub> is relatively larger than that of S45C, the greater hardness will decrease the value of  $A_{ss,t}^*$ . When the third body is SiO<sub>2</sub>, the value of  $F_{tpca}^*$  is larger than that of S45C. However, when  $x_a / \sigma \approx 0.5$ –0.7 and the dimensionless normal contact load is smaller, the value of  $A_{ss,t}^*$  of SiO<sub>2</sub> is greater than that of S45C. This is because the hardness of SiO<sub>2</sub> is greater, and the sinking amplitude of the third bodies is also greater. Therefore, when the third body is a foreign particle, the critical load of its interface from 3-body p-s contact mode to 3-body hybrid contact mode is greater than that of metal wear debris.

Figure 9 shows the critical load versus equivalent surface RMS roughness at various average third body diameters and third body material for first critical load  $(F_{cr1}^*)$  and second critical load  $(F_{cr2}^*)$ . For SiO<sub>2</sub> under the same equivalent surface RMS roughness, as shown in Figure 9a, the  $F_{cr1}^*$  increases with increase in the average third body diameter. However, the value of  $F_{cr1}^*$  decreases with increase in the equivalent surface RMS roughness at the same average third body diameter. The  $F_{cr1}^*$  value of S45C is less than that of SiO<sub>2</sub> at the same equivalent surface RMS roughness and average third body diameter. As shown in Figure 9a, SiO<sub>2</sub> needs a larger dimensionless normal load to make the contact interface enter the 3-body hybrid contact mode. This indicates that SiO<sub>2</sub> has a larger dimensionless

normal load range in 3-body p-s contact mode than in the two other modes. For 3-body p-s contact mode, maintaining the contact pressure at the interface for a long period of time will easily exceed the pressure limit and cause surface damage. For SiO<sub>2</sub> under the same equivalent surface RMS roughness, as shown in Figure 9b, the value of  $F_{cr2}$  increases with increase in the average third body diameter. Conversely, the value of  $F_{cr2}^{*}$  decreases with increase in the equivalent surface RMS roughness at the same average third body diameter. The  $F_{cr2}^*$  value of SiO<sub>2</sub> is larger than that of S45C under the same equivalent surface RMS roughness and average third body diameter. In addition, when  $x_a = 100$  nm,  $\sigma$  = 50 nm and  $\sigma$  = 100 nm, the  $F_{cr2}^*$  value of SiO<sub>2</sub> is about 2.9–3.4-fold larger than that of S45C. By contrast, for other average third body diameters under the same equivalent surface RMS roughness, the  $F_{cr2}^*$  value of SiO<sub>2</sub> is only about 1.1–1.3-fold larger than that of S45C. Therefore, the difference in  $F_{cr2}^*$  between the metal wear debris and foreign particles is relatively insignificant. From Figures 3–9, it can be found that the 2-body contact is an ideal contact mode at the contact interface. This is because its dimensionless real contact area is almost linear with the dimensionless normal contact load and it is easy to predict its changes under different operating conditions as shown in Figure 5. In fact, the actual contact interface is a 3-body contact system. It is not possible to maintain the ideal 2-body contact state. Although the dimensionless real contact area of the 3-body p-s contact mode is almost linear with the dimensionless normal contact load, as shown in Figure 5, the third bodies have completely separated the two surfaces. Consequently, this will cause the instability of the contact interface. The foreign particles are more likely to cause 3body p-s contact mode at the contact interface than the wear debris. This indicates that environmental dust is more likely to cause excess wear or failure of the contact interface. Therefore, it is recommended to change the lubricating oil regularly and appropriately maintain the oil circulation system, so as to ensure the stability of the contact interface and increase the service life of the components. From the present analysis, it is necessary to constrain the ratio of average third body diameter to equivalent surface RMS roughness  $(x_a/\sigma)$  to not exceed 0.7.



**Figure 8.** The contact area ratio of surface 1 and surface 2 versus dimensionless normal contact load at various average third body diameters for wear debris and foreign particles for  $\sigma$  = 300 nm.

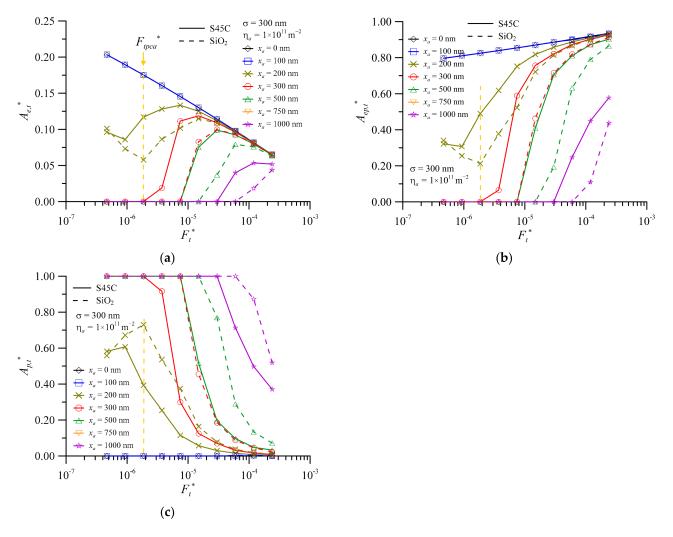


**Figure 9.** The critical load versus equivalent surface RMS roughness at various average third body diameters and third body materials for (**a**) first critical load (**b**) second critical load.

Figure 10 shows the deformation types of total contact area ratio versus dimensionless normal contact load at various average third body diameters for elastic, elastoplastic, and plastic material behaviors. For the real contact area ratio of elastic deformation, as shown in Figure 10a, the  $A_{e,t}$ \* value of 2-body contact model (diamond symbol curve) decreases with increase in dimensionless normal contact load. Moreover, this  $A_{e,t}$ \* value is larger than the  $A_{e,t}$ \* value of all 3-body contact models. For  $x_a = 300$ nm, the  $A_{e,t}$ \* value of SiO<sub>2</sub> rises rapidly when  $F_t^* > F_{cr1}^*$  (contact mode shift into 3-body hybrid contact). Then the  $A_{e,t}^*$  value decreases with the increase in the dimensionless normal contact load when approaching the 2-body contact curve. Finally, the  $A_{e,t}^*$  curve overlaps with the 2-body contact curve, indicating that the contact mode shifts into 3-body s-s contact mode at this moment. For all average third body diameters and dimensionless normal contact loads, the  $A_{e,t}^*$  is less than 20%, indicating that it has less effect on the total real contact area.

As shown in Figure 10b, more than 80% of the total real contact area is elastoplastic deformation for  $x_a < 100$  nm. The real contact area ratio of elastoplastic deformation increases with increase in the dimensionless normal contact load. The  $A_{ep,t}^*$  value of all cases of 3-body contact is smaller than for 2-body contact. For  $x_a = 300$  nm, the  $A_{ep,t}^*$  value of SiO<sub>2</sub> rises rapidly when  $F_t^* > F_{cr1}^*$  (7.4 × 10<sup>-6</sup>). Then the  $A_{ep,t}^*$  value approaches the 2-body contact curve. Finally, the  $A_{ep,t}^*$  curve overlaps with the 2-body contact curve, indicating that the contact enters 3-body s-s contact mode. Due to the hardness of SiO<sub>2</sub> (environment particles) being greater than that of S45C (wear debris), the  $A_{e,t}^*$  and  $A_{ep,t}^*$  values of SiO<sub>2</sub> are smaller than the values of S45C under the same dimensionless normal contact load. For  $x_a = 300$  nm, as shown in Figure 10c, the  $A_{p,t}^*$  value of SiO<sub>2</sub> decreases

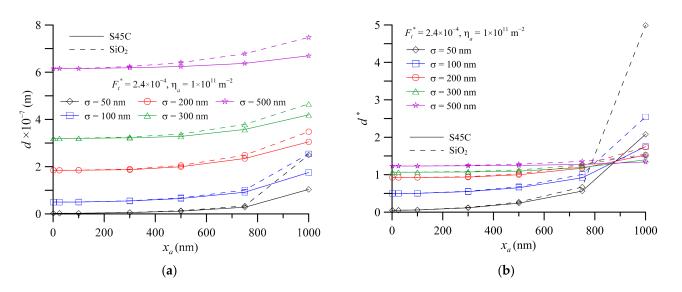
rapidly with the increase in dimensionless normal contact load. Finally, the  $A_{p,t}^*$  value approaches to 0% when  $F_t^* > F_{cr1}^*$ . Due to the greater hardness of SiO<sub>2</sub>, the  $A_{p,t}^*$  value of SiO<sub>2</sub> is larger than that of S45C and results in more plastic deformation at the contact interface for the same average third body diameter. When the dimensionless normal contact load is slightly larger than  $F_{tpca}^*$  (1.86 × 10<sup>-6</sup>), the TPCA phenomenon can be found in Figure 10 for SiO<sub>2</sub> of  $x_a = 200$  nm. By selecting the average third body diameter that will cause the TPCA phenomenon, it is possible to increase the values of  $A_{e,t}^*$  and  $A_{ep,t}^*$  and decrease the values of  $A_{p,t}^*$ . This is because the real contact area ratio of plastic deformation is the main factor of wear, as shown in Figures 8 and 6b. When  $F_{tpca}^* < F_t^* < 6.0 \times 10^{-6}$ , as shown in Figure 10, it will be a relatively good surface design, because both the third body and surface can share the contact load. In addition, the real contact area ratio of elastic and elastic and elastoplastic deformation area will increase as well.



**Figure 10.** The deformation components of total real contact area ratio versus dimensionless normal contact load at various average third body diameters for (**a**) elastic (**b**) elastoplastic (**c**) plastic.

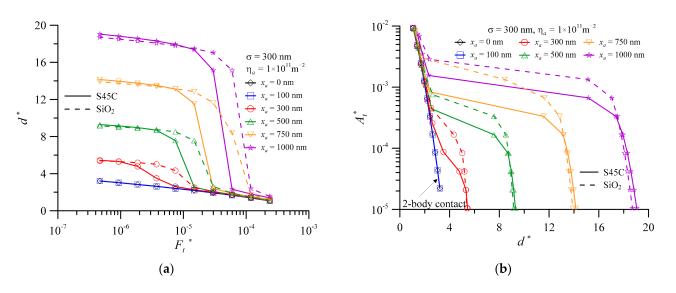
For the same dimensionless normal contact load, the values of  $A_{e,t}^*$  and  $A_{ep,t}^*$  decrease with the increase in the average third body diameter, as shown in Figure 10. By contrast, the value of  $A_{p,t}^*$  increases with the increase in the average third body diameter. Therefore, the larger the average third body diameter, the easier the plastic deformation of the contact surface. In addition, for SiO<sub>2</sub> of  $x_a = 300$  nm as an example, almost 100% plastic deformation will occur at the contact interface when the contact mode is 3-body p-s contact. This indicates that this contact mode is prone to cause surface damage. Under the same dimensionless normal contact load, the values of  $A_{e,t}^*$  and  $A_{ep,t}^*$  of SiO<sub>2</sub> are smaller than that of S45C. The value of  $A_{p,t}^*$  of SiO<sub>2</sub> is greater than that of S45C. The excessive plastic deformation of the contact surface will readily increase friction and cause a lot of surface wear. Therefore, this is also one of the reasons why strict conditions for the control of environmental dust are required during precision processing and manufacturing.

Under the same dimensionless normal contact load, Figure 11a,b show the separation between the surface 1 and mean height of asperities (*d*) and dimensionless separation  $(d^* = d/\sigma)$  versus average third body diameters for various equivalent surface RMS roughnesses and third body materials, respectively. Figure 11a shows that the separation increases with increase in the equivalent surface RMS roughness and average third body diameters. For the same equivalent surface RMS roughness, the separation value of SiO<sub>2</sub> is greater than that of S45C. Moreover, the disparity between SiO<sub>2</sub> and S45C increases as the average third body diameter increases. Figure 11b, which shows dimensionless separation, illustrates the amplitude of change at various equivalent surface RMS roughnesses and average third body diameters. When the ratio value of average third body diameter to equivalent surface RMS roughness increases, the contact readily enters into 3-body p-s contact mode, as shown in Figure 9. Moreover, the change amplitude of dimensionless separation increases as well. For  $x_a = 1000$  nm, the dimensionless separation value of SiO<sub>2</sub> is about 2.5 times larger than that of S45C. This confirms the importance of preventing foreign particles from entering the lubricated interface.



**Figure 11.** The separation between the surface 1 and mean height of asperities versus average third body diameters at various equivalent surface RMS roughnesses for wear debris and foreign particles (**a**) separation (**b**) dimensionless separation.

The curve of  $x_a = 0$  nm in Figure 12a is the traditional dimensionless separation curve of the 2-body contact, where dimensionless separation decreases with increase in dimensionless normal contact load. When the third body is present in the contact interface, the dimensionless separation will be greater than for the 2-body contact. For the same dimensionless normal contact load, it will increase as the average third body diameter increases. When the value of  $F_t^* < 2 \times 10^{-5}$ ,  $x_a = 1000$  nm and  $x_a = 500$  nm, the dimensionless separation of maximum value is about 5.8 and twice that of 2-body contact, respectively. Taking  $x_a = 500$  nm of SiO<sub>2</sub> as an example, when the value of  $F_t^*$  is  $5 \times 10^{-7}$ – $7 \times 10^{-6}$ , the contact is in 3-body p-s contact mode. The dimensionless normal contact load increases about 10 times from  $5 \times 10^{-7}$  to  $7 \times 10^{-6}$ . In the meantime, the value of  $d^*$  is reduced by only 6.89%. At this moment, the interface remains in 3-body p-s contact mode. The dimensionless separation of the contact interface is relatively larger than the ideal 2-body contact mode. When the contact shifts into 3-body hybrid contact mode after the value of  $F_t^* > 7 \times 10^{-6}$ , the dimensionless normal contact load is also increased 10 -fold from  $7 \times 10^{-6}$  to  $3 \times 10^{-5}$ . The value of  $d^*$  decreases rapidly by 69.24% from 8.52 to 2.62. Upholding the 3-body hybrid contact mode of the interface can quickly reduce the interface separation and avoid the instability of components caused by excessive separation. Therefore, both the wear debris and foreign particles have a great influence on the mechanical or electronic properties of the contact interface for the contact element. The curve of  $x_a = 0$  nm in Figure 12b shows that the value of  $A_t^*$  increases rapidly with decreasing value of  $d^*$ , demonstrating that a slight change in the 2-body contact interface will cause extreme variation in the contact area. However, it also shows that the separation between the contact surfaces is relatively stable when within the 2-body contact mode. As the contact area changes, the interface separation will not fluctuate too much during the operation of components. Taking SiO<sub>2</sub> with  $x_a = 500$  nm as an example, the value of  $A_t$ decreases as the value of  $d^*$  increases. The first overlaps with the 2-body curve indicating that it is in 3-body s-s contact mode. When the contact mode shifts to 3-body hybrid contact mode, the value of  $A_t^*$  decreases relatively slowly with the increasing value of  $d^*$ . The value of  $d^*$  increases about 30% and the value of  $A_t^*$  decreases by only about 9%. This indicates that the contact interface is within 3-body hybrid contact mode which can reduce the variation of the contact area. As shown by the results in Figure 12, larger separation variation at the contact interfaces will not only cause the machine to become unstable, but also cause excessive pressure on the local contact points due to the smaller contact area, which will eventually lead to surface damage. In general, 3-body hybrid contact mode has larger  $d^*$  variation and smaller  $A_t^*$  variation, whereas 3-body s-s and p-s contact mode has smaller  $d^*$  variation and larger  $A_t^*$  variation. The dimensionless separation variation increases with increase in average third body diameter.



**Figure 12.** (a) Dimensionless separation versus dimensionless normal contact load and (b) dimensionless real contact area versus dimensionless separation, at various average third body diameters for wear debris and foreign particles.

#### 4. Conclusions

The 3-body contact model reflects the real contact interface of general relative moving components. This work discusses particle effects and the difference in contact area, contact mode and separation between foreign particles and wear debris when the contact interface is in metal contact pair at various average third body diameters, equivalent surface RMS roughnesses and contact loads under dry contact conditions. The results of the analyses can be summarized as follows:

- 1. The value of  $A_t^*$  gradually increases with the increase in the load for 3-body contact interface where the third body exists. As the dimensionless normal contact load increases, the 3-body contact mode shifts from p-s mode into hybrid mode and then to s-s mode. When the interface becomes a 3-body s-s contact mode, the value of  $A_t^*$  is equal to that of 2-body contact mode.
- 2. The results show that the relationship profile between dimensionless real contact area ratio  $(A_t^*)$  and dimensionless normal contact load  $(F_t^*)$  is wedge-shaped in 3-body contact interface. Using surface-to-surface 2-body contact area as upper bound and surface-to-particle 3-body contact as lower bound, the 3-body hybrid contact situation is in between upper and lower bounds. Larger values of equivalent surface RMS roughness will result in a narrower wedge-shaped area.
- 3. Under 3-body contact interface conditions, the first critical load  $(F_{rc1}^*)$ , the second critical load  $(F_{rc2}^*)$ , and the real contact area ratio of plastic deformation increase with the increase in the average diameter and hardness of the third body. The interface real contact area ratio of plastic deformation of the SiO<sub>2</sub> particle is larger than that of general metal wear debris.
- 4. Under 3-body p-s contact interfaces, the dimensionless real contact area increases as the dimensionless normal contact load increases. Therefore, the real contact pressure decreases as the dimensionless normal contact load increases. Equivalent surface RMS roughness has little effect on dimensionless real contact area. Moreover, dimensionless normal contact load has little effect on interface dimensionless separation.
- 5. Under 3-body hybrid contact interfaces, the real contact pressure increases and dimensionless separation significantly decreases as the dimensionless normal contact load increases. However, the variation of dimensionless separation has little effect on the dimensionless real contact area. This phenomenon can prevent the rising contact temperature caused by the excessive separation and rapid increase in the contact pressure during operation.
- 6. Under the 3-body hybrid contact interface, there are many TPCA mechanisms that occur at  $x_a/\sigma \approx 0.5$ –0.7 for wear debris and foreign particles (SiO<sub>2</sub>). When the dimensionless normal contact load is slightly larger than the value of  $F_{tpca}$ <sup>\*</sup>, the average third body diameter and equivalent surface RMS roughness value of TPCA can be selected for interface design. In this case, the third body and the surface share the interface normal contact load approximately equally. The real contact area ratio of elastic to elastic–plastic deformation increases in the total real contact area, which is a relatively good choice of interface design.

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# Nomenclature

$A_n$	apparent contact area at the interface, m <sup>2</sup>
$A_e$	real contact area of elastic deformation, m <sup>2</sup>
$A_{e,t}^{*}$	real contact area ratio of elastic deformation, $A_e/A_t$
A <sub>ep</sub> *	real contact area of elastoplastic deformation, m <sup>2</sup>
$A_{ep,t}^{*}$	real contact area ratio of elastoplastic deformation, $A_{ep}/A_t$
$A_p$	real contact area of plastic deformation, m <sup>2</sup>
$A_{p,t}^{*}$	real contact area ratio of plastic deformation, $A_p/A_t$
$A_t$	total real contact area, m <sup>2</sup>
$A_t^*$	dimensionless real contact area, $A_t/A_n$
$A_{sa}$	real contact area of third body and surface 1, m <sup>2</sup>
$A_{sa,n}^{*}$	dimensionless real contact area of third body and surface 1, $A_{sa}/A_n$
$A_{sa,t}^{*}$	real contact area ratio between third body and surface 1, $A_{sa}/A_t$
$A_{ss}$	real contact area of surface 1 and surface 2, m <sup>2</sup>
$A_{ss,n}^{*}$	dimensionless real contact area of surface 1 and surface 2, $A_{ss}/A_n$
$A_{ss,t}^{*}$	real contact area ratio between surface 1 and surface 2, $A_{ss}/A_t$
d	separation between the surface1 and mean height of asperities, m
$d^*$	dimensionless separation, $d/\sigma$
$E_{sa}$	equivalent elastic modulus of the third body and surface, GPa
$E_{ss}$	equivalent elastic modulus of the two surfaces, GPa
$F_{cr1}^{*}$	initial dimensionless normal contact load of 3-body p-s contact shift into 3-body
r <sub>cr1</sub>	hybrid contact mode
$F_{cr2}^{*}$	initial dimensionless normal contact load of 3-body hybrid contact shift into
F <sub>cr2</sub>	3-body s-s contact mode
$h_e$	maximum separation of two surfaces with third bodies, m
$F_{tpca}^{*}$	dimensionless normal contact load of turning point of contact area
$F_t$	normal contact load, N
$F_t^*$	dimensionless normal contact load, $F_t/A_n E_{ss}$
$F_{sa}$	contact load of third body and surface 1, N
$F_{ss}$	contact load of surface 1 and surface 2, N
H	hardness of softer material for surface 1 and surface 2, GPa
$H_{s1}$	hardness of surface 1, GPa
$H_{s2}$	hardness of surface 2, GPa
k	mean contact pressure factor
R	radius curvature of surface peak, m
$x_a$	average third body diameter, m
$\phi(z)$	probability density function of the peak height
$\phi_a(x)$	probability density function of the third body diameter
η	asperity density, m <sup>-2</sup>
$\eta_a$	number of third bodies per unit area, $m^{-2}$
$\sigma$	equivalent surface RMS roughness, m
$\sigma_a$	standard deviation of the diameter of third body
$\sigma_s$	standard deviation of the asperity heights
ω	interference, m

- $\omega_1$  critical interference at the point of initial yield, m
- $\omega_2$  critical interference at the point of fully plastic flow, m

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