Control System Design Guide

USING YOUR COMPUTER TO DEVELOP AND DIAGNOSE FEEDBACK CONTROLLERS

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Preface

 $\gamma \in \mathbb{R}^{n}$

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