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Controlled manipulation of oxygen vacancies using nanoscale flexoelectricity

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Oxygen vacancies, especially their distribution, are directly coupled to the electromagnetic properties of oxides and related emergent functionalities that have implications for device applications. Here using a homoepitaxial strontium titanate thin film, we demonstrate a controlled manipulation of the oxygen vacancy distribution using the mechanical force from a scanning probe microscope tip. By combining Kelvin probe force microscopy imaging and phase-field simulations, we show that oxygen vacancies can move under a stress-gradient-induced depolarisation field. When tailored, this nanoscale flexoelectric effect enables a controlled spatial modulation. In motion, the scanning probe tip thereby deterministically reconfigures the spatial distribution of vacancies. The ability to locally manipulate oxygen vacancies on-demand provides a tool for the exploration of mesoscale quantum phenomena and engineering multifunctional oxide devices.

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xygen vacancies (V_o°) are elemental point defects in oxides, and they generally function as mobile electron donors. At sufficiently high concentrations, they can disturb the ground state and promote emergent functional phenomena, such as superconductivity¹, ferromagnetism^{2, 3}, metalto-insulator transition⁴ and interface conductivity⁵. In addition, the distribution and dynamics of V_o° play a central role in many oxide-based energy and memory applications^{6, 7}. Hence, the ability to manipulate V_o° provides an opportunity to study the evolution of emergent phenomena and control numerous functionalities, which are essential for developing next generation oxide devices^{8, 9}.

Traditionally, modification of the vacancy concentration has been carried out by annealing oxides at high temperature in reducing/oxidising atmosphere. Recent works have shown that at room temperature, the vacancy concentration can instead be locally changed by employing an electrical bias from a scanning probe microscope (SPM) tip^{4, 10}. Such local manipulation enables reversible nanoscale control of metal-insulator transitions⁴ and the modulation of interface conductivity¹¹. However, in addition to the change in the vacancy concentration, the application of bias through an SPM tip is often accompanied by charge injection^{12, 13} and the formation of protons/ hydroxyls¹⁴, which complicates the practical implementation of this approach.

Recently, it has been shown that the mechanical force from the SPM tip can also deplete V_0° from the contact region^{15, 16}. However, because this mechanical depletion is less understood, the feasibility of using the force from an SPM tip as an active means of manipulating V_0° has not been explored. An explanation for the mechanical depletion of V_0° has been proposed through the so-called piezochemical coupling mechanism¹⁵⁻¹⁷, which involves the converse Vegard effect and the flexoelectric effect. The converse Vegard effect accounts for the decrease in vacancy concentration due to force-induced lattice compression. Meanwhile, the flexoelectric effect considers the electromigration of positively charged V_o^{-} under the stress-gradient-induced flexo-electric field. Notably, by definition, the flexoelectric effect refers to the generation of an electrical polarisation by stressgradients^{18, 19}. In this context, Yudin and Taganstev suggested that the flexoelectric field is not a macroscopic electric field¹⁹; instead, it should be understood as a pseudo-internal field that polarises a medium in the presence of a stress-gradient²⁰⁻²³. Hence, it remains unclear how this flexoelectric field acts on $V_0^{\cdot \cdot}$.

To be able to mechanically manipulate V_o° , we must, therefore, thoroughly understand how they respond to the mechanical force from the SPM tip. Subsequently, we have to devise a strategy to employ this force to increase as well as decrease the vacancy concentration in a controlled manner.

Here, we demonstrate a controlled manipulation of V_0° using the mechanical force from an SPM tip. As a model system, we used a homoepitaxial thin film of SrTiO3, which is an archetypal quantum paraelectric oxide with well-known flexoelectric coefficients^{24, 25}. Using a Kelvin probe force microscopy (KPFM)based imaging scheme, we show that besides pushing $V_0^{\cdot \cdot}$ away in the vertical direction, the force promotes the lateral transport of vacancies during the movement of the tip. Using phase-field simulations, we argue that this mechanical redistribution of $V_0^{\cdot \cdot}$ is driven by the depolarisation field associated with the stressgradient-induced flexoelectric polarisation. The depolarisation field underneath the tip promotes the vertical migration of vacancies, whereas around the contact edge, it traps V_0° that can move with the tip. Furthermore, we demonstrate that altering the tip geometry can tailor this depolarisation field to preferentially allow the lateral transport of V_0^{\cdot} . This approach enables a controlled spatial modulation of vacancies.

Results

Probing oxygen vacancies with Kelvin probe force microscopy. We start by discussing the concept of probing distribution of V_0° with the KPFM technique (Fig. 1a-c). KPFM is a surface sensitive technique that measures the contact potential difference (CPD) between the tip and SrTiO₃ (STO) surface. The CPD is defined as the offset in the respective vacuum energy levels (in units of V)²⁶. However, as schematically illustrated in Fig. 1b, this CPD would change if the STO surface contains V_0° , which can be locally accumulated by an electrical poling. This change in the CPD can originate from the workfunction of STO²⁷, chemical dipoles (including V_0^{\cdot} -electron pairs), and their orientation²⁸. Moreover, the tip bias used during the KPFM measurement has been argued to influence the measured CPD²⁹. The contribution of each factor cannot be individually separated, which inhibits a quantitative determination of the vacancy concentration with the KPFM technique. Nonetheless, as shown in Fig. 1c, the KPFM contrast across this V_o-rich region can be argued to scale proportionally with the vacancy concentration²⁷. To establish a proof of concept, in the following we elaborate on the application of KPFM technique to study the diffusion of V_o^{\cdot} using a 14 and 120-unit cell (uc)-thick STO film (details of the film are provided in the Methods section and in Supplementary Fig. 1).

Figure 1d, e show KPFM images after poling the pristine surface of STO films with a tip bias of -5 V. The images of the 14-uc (120-uc)-thick STO film were taken 20 (16) minutes and 380 (360) minutes after poling. An image contrast is clearly visible across the poled region, which is appearing as a dark rectangular patch. This implies surface charging, either by injected charges, protons/hydroxyls, and/or $V_0^{..30,31}$. The injected charges and protons/hydroxyls are expected to decay with a timescale, which is independent of the STO thickness³¹. In contrast, because of diffusion or surface reaction that enables the recombination of $V_0^{\cdot \cdot}$ with oxygen from the ambient, the vacancy concentration is expected to decrease with a pronounced thickness-dependent timescale³². Figure 1d, e indeed show that the contrast across the poled region diminishes over time, and the decrease is largest in the 14-uc-thick STO film. Therefore, we argue that the surface charging is caused by V_0° , which either undergo diffusion or recombine with oxygen from the ambient.

We can distinguish the dominating mechanism that causes the vacancy concentration to decay over time by analysing the timedependency of the degree of equilibrium, S(t) that can be calculated from the KPFM images (see Supplementary Note 1). The time-dependency of S(t) describes how the surface equilibrates after the electrical poling. S(t) will exhibit a semiparabolic (linear) time-dependency if diffusion (surface reaction) is the dominating mechanism^{27, 32}. Figure 1f plots S(t) as a function of time. Evidently, the time-dependencies of S(t) are semi-parabolic for both films-implying that the diffusion of V_o^- causes the vacancy concentration to decrease over time.

Arguably, during the poling, the applied tip bias perturbs the equilibrium V_0° -distribution of the entire film including the surface, which equilibrates through the diffusion of V_0° . This diffusion occurs both along the out-of-plane and in-plane directions. However, due to the high surface sensitivity of the KPFM technique, the surface-bulk diffusion of V_0° predominantly affects the time evolution of the KPFM contrast, and thus the time-dependency of S(t). Notably, during this surface-bulk diffusion, the repulsive vacancy-vacancy interaction inhibit V_0° to migrate independently along the out-of-plane direction³⁹. Thus, the time-dependency of S(t) effectively describes how the perturbed volume under the poled area (in Fig. 1d, e) equilibrates (see Supplementary Note 1 for a detailed discussion). Naturally, this volume would be smaller in the thinner STO film, and thus would equilibrate faster. This explains why the KPFM contrast

(S(t)) diminishes (grows) more rapidly in the 14-uc thick STO than in the 120-uc thick STO film (Fig. 1d–f).

Following the rationale above, we fit the time evolution of S(t) with Fick's 2nd law of diffusion (solid lines in Fig. 1f). From this fitting, we obtained the diffusion coefficient $D = 9.4(3) \times 10^{-19}$ and $3.8(2) \times 10^{-18}$ cm² s⁻¹ for the 14-uc and 120-uc-thick STO film, respectively. These values are well in the range of the bulk value $D_{\text{bulk}} \approx 10^{-(17\pm3)}$ cm² s⁻¹ (300 K-extrapolated)³⁴, which validates the conceptual schematic depicted in Fig. 1c. Subsequently, we utilised this correlation between the vacancy concentration and KPFM signal to image the vacancy redistribution under an applied bias and force.

Oxygen vacancy redistribution under applied bias and force. In this section using the 120-uc-thick STO film, we compare the response of V_0^{-} to the electrical bias and force from the SPM tip. For this study, we employed a sharp tip with a radius of curvature = 25 nm. As depicted in the KPFM image (Fig. 2a), we scanned the left side of a formerly V_0^{-} -enriched region with an increasingly positive tip bias (0–5 V) at a contact force = 0.6 μ N. Meanwhile, the right side was scanned with an increasing contact force (0.6–8.5 μ N) by holding the tip at the ground potential. In either case, the tip crossed the border between the formerly

 $V_{\rm o}^{-}$ -enriched and pristine regions. The central part of the KPFM image is uniformly dark, which indicates a uniform vacancy distribution. However, a change in the image contrast, which stems from the $V_{\rm o}^{-}$ -redistribution is visible within both electrically and mechanically scanned areas. Notably, these scans together with acquiring the KPFM image took about 20 min. Because of their ultra-slow decay as evident from Fig. 1e, during this time $V_{\rm o}^{-}$ -redistribution is due to the applied bias and force.

To quantify this V_o^{-} -redistribution, we constructed the vacancy concentration map from Fig. 2a by defining the normalised vacancy concentration, NVC = $\frac{(V_b - V)}{(V_b - V_{min})}$. Here, V_b and V_{min} represent the baseline and minimum KPFM signals, which were extracted from areas indicated by the black (top-right corner) and white (centre) squares, respectively. The reconstructed NVC map is shown in Fig. 2b. The positive (negative) NVC refers to a higher (lower) vacacny concentration compared to the intrinsic surface concentration of V_o^{-} (NVC = 0, at the top-right corner).

Profiling the NVC map along lines E and M indicates that both the applied bias and force depleted the formerly V_o° -enriched region (Fig. 2c). We find that this depletion can be modelled with a phenomenological Boltzmann sigmoid function in the following



Fig. 1 Studying diffusion characteristics of oxygen vacancies with KPFM. **a** Sketch of the sample geometry and KPFM measurement architecture. **b** Schematic illustration of the contact potential difference (CPD) contrast between the pristine (referred to as 1) and V_{o}^{-} -rich (referred to as 2) regions. E_{vac} denotes the vacuum energy level. **c** Illustrative KPFM signal from a line scan from position A to B across this V_{o}^{-} -rich region. ΔV_{s} and $[V_{o}^{-}]$ denote the net change in the measured KPFM signal and the concentration of V_{o}^{-} within the V_{o}^{-} -rich region, respectively. **d-f** Characterisation of diffusion of V_{o}^{-} with the KPFM technique. KPFM images around a V_{o}^{-} -enriched surface region of a 14-uc-thick **d** and 120-uc-thick **e** STO films. The time lag between poling the pristine surface and the time of acquiring an image is indicated on the *top-right corner* of KPFM image. The time evolution of the degree of equilibrium, *S*(*t*) (*solid symbols*) and fit (*solid line*) according to Fick's 2nd law of diffusion **f**. The *scale bar* in **d**, **e** represents 1µm



Fig. 2 Characterisation of oxygen vacancy redistribution by applied bias and force. **a** The KPFM image after electrical and mechanical scans were performed across borders between the V_{o}^{-} -enriched and pristine regions. The schemes for electrical and mechanical scans are overlaid on the image. *Horizontal arrows* mark the corresponding fast scan direction. Before electrical and mechanical sans, the V_{o}^{-} -enrichment was performed by poling a 5 × 7 µm² area of the pristine surface with a tip bias of -5 V. **b** The normalised vacancy concentration (NVC) map constructed from the KPFM image in **a**. **c** The NVC along lines E (*open circles*) and M (*open squares*) in **b** measured as a function of applied bias and contact force, respectively. The *solid lines* denote the Boltzmann sigmoid fit to the data, and Table 1 lists the corresponding best-fit parameters. The threshold voltage (V_{th}) and force (F_{th}) for the depletion of V_{o}^{-} are marked with stars. **d** The NVC along lines E_{L} (*black coloured circles*) and M_L (*dark yellow coloured circles*) in **b** measured as a function of applied bias and contact force, respectively. The *dashed lines* are a guide for eyes. Lines E_{L} and M_{L} are placed 1µm away from the borders between the V_{o}^{-} -enriched and pristine regions. The *thick horizontal line* in **d** marks the background along these lines. **e** Background-subtracted NVC (Δ NVC) along lines M (*turquoise coloured diamonds*) and M_L (*dark yellow coloured lines* are a guide for eyes. NVC at 0.6 µN is used as the background. The data plotted in **c**, **d** are extracted using a 0.8 µm-wide averaging window. The *scale bar* in **a**, **b** represents 1µm

Table 1 Best-fit parameters from the Boltzmann sigmoid fit to the normalised vacancy concentration (NVC) data in Fig. 2c

	A ₁	A ₂	Xo	м
Electrical	0.86 (3)	0.03 (4)	2.6 (1) V	0.6 (1)
Mechanical	0.93 (1)	0.004 (25)	6.8 (1) μN	1.9 (1)

form,

$$f(x) = A_2 + \frac{A_1 - A_2}{\left[1 + e^{\frac{x - X_0}{M}}\right]}$$
(1)

where A_1 , A_2 , X_0 , and M refer to the initial value, final value, center, and decay rate, respectively. The *solid lines* in Fig. 2c are fits to this function. Table 1 lists the best-fit parameters. This functional analysis suggests that the applied positive bias and force have a same qualitative effect along the lines E and M, respectively. By comparing the X_0 (= 0.5 A_1) values from the fits, we obtain a force-voltage equivalence factor of 0.4 V μ N⁻¹. The Boltzmann sigmoid fits in Fig. 2c also exhibit an onset. Defining this onset as 0.9 A_1 (indicated by stars), on an ad hoc basis, yields a threshold voltage (V_{th}) and force (F_{th}) of 1.3 V and 2.7 μ N or

equivalently 1.1 V, respectively. These threshold values are consistent with the activation barrier potential (=1–1.4 V) for the electromigration of V_o° in STO^{35, 36}, which further validates the force-voltage equivalence relationship.

Surprisingly, electrical and mechanical scans yield the opposite image contrast across borders in the NVC map. As shown in Fig. 2d, along line E_L , NVC monotonically decreases with the increasing bias. However, along line M_L , NVC varies nonmonotonously: first, it increases as the force increases and then gradually drops; the *horizontal line* in Fig. 2d marks the background (NVC=0.1 at 0 V and 0.6 μ N). We, therefore, conclude that the electrical scan depletes the pristine surface outside the left border, while the mechanical scan enriches the pristine surface outside the right border.

The force-induced vacancy-enrichment of the pristine region implies that some of the depleted V_o° moved laterally with the tip across the border during the mechanical scan. Additional experiments elaborate that the mechanical scan does not alter the background within the pristine region, and thus rule out the formation of V_o° and triboelectric charging of the STO surface during the mechanical scan (see Supplementary Note 2). To quantify the lateral motion of V_o° , in Fig. 2e we, therefore, show the NVC with the background (NVC at 0.6 μ N) subtracted (i.e., Δ NVC) along lines M and M_L. Because KPFM is a surfacesensitive technique, the remnant V_o° on the surface contribute to



Fig. 3 Phase-field simulations. **a** Simulated out-of-plane (*z*-*x* plane) vector map of flexoelectric polarisation induced by the scanning probe microscope (SPM) tip under a static contact force of 4 μ N. Arrows denote the direction of the polarisation vectors, and their lengths correspond to the magnitude of the induced polarisation. **b** Simulated in-plane (*x*-*y* plane) normalised vacancy concentration (NVC) map around the tip-STO contact region, which shows a depletion and enrichment of V_o^{c} underneath the tip and around the contact edge, respectively. **c**, **d** The component-resolved in-plane distribution of depolarisation field around the tip-STO contact region. The *z*-component, E_z^{dep} **c**, and the x-component, E_x^{dep} **d**. The in-plane distribution of the y-component, E_z^{dep} , should be viewed as the same as the one in **d** but rotated by 90° in the *x*-*y* plane

the NVC map after V_0^{-} -redistribution. Also, the possibility of recombination with oxygen from the ambient during the lateral motion of V_0^{-} can be ignored based on the following considerations. The influence of the surface reaction process, which could facilitate this recombination is negligible in our film. Furthermore, the use of a grounded tip during the mechanical scan rules out the bias-induced amplification of this surface reaction process³⁷. Hence, for a particular force, the ratio between the net gain (along M_L) and the net drop in NVC (along M) represents the fraction of depleted V_0^{-} that moved laterally with the tip. By comparing the maximum net gain (=0.1), and corresponding drop (=0.3) at force = 5.7 µN, we estimated that only approximately 1/3 of the depleted V_0^{-} moved with the tip along the surface, while the rest migrate into the bulk.

Overall, our main observations are as follows. First, the contact force is bifunctional: it depletes the formerly $V_0^{"}$ -enriched region and simultaneously enriches the pristine surface. Second, the mechanical $V_0^{"}$ -redistribution involves a predominant surface-bulk migration and a relatively weaker lateral motion of $V_0^{"}$ with the tip.

Modelling the mechanical redistribution of oxygen vacancies. To understand the mechanical redistribution of $V_o^{::}$ we first considered two mechanisms-the converse Vegard effect and the flexoelectric effect^{15, 16}. Recently, the magnitude of these two effects under an applied force from SPM tip has been compared in a PbTiO₃ (PTO) thin film³⁸. This study suggests that the converse Vegard effect is much weaker than the flexoelectric effect. Notably, both the PTO and STO have comparable flexoelectric and Vegard coefficients^{25, 38, 39}, which determine the relative contributions of these two effects for a given force. Based on these considerations, we thus conclude that the flexoelectric effect predominantly causes the mechanical redistribution of $V_o^{:}$, and the contribution from the converse Vegard effect is marginal.

For gaining a mechanistic understanding of this flexoelectric effect-driven V_0° -redistribution, we performed phase-field simulations; whereby we incorporated the flexoelectric effect⁴⁰ and coupled the time-dependent Ginzburg-Landau and the Nernst-

Planck equations^{41, 42}. The simulation was performed assuming that the STO is paraelectric (see Supplementary Note 3). Unlike in the experiment, the SPM tip was assumed to be static, and following the Hertzian model the contact radius was calculated to be 8 nm for a contact force of 4 μ N. Initially, V_o^{-} were assumed to be homogeneously distributed over the entire STO thickness, instead of being localised on the surface. Despite these oversimplified assumptions, our simulation still provides a qualitative insight into how V_o^{-} respond to mechanical stimuli. A detailed explanation of our model and a discussion on the redistribution of V_o^{-} under a positive tip bias are included in Supplementary Notes 4, 5.

The stress-gradient from the SPM tip locally polarises STO through the flexoelectric effect²⁴, as evident from the out-of-plane polarisation vector map in Fig. 3a. Since in the simulation the STO film is assumed to be in the paraelectric phase, the polarisation in Fig. 3a purely stems from the flexoelectric effect. This flexoelectric polarisation reaches a maximum (~ 0.04 C m⁻²) underneath the tip and spatially varies both in magnitude and direction. The resulting polarisation bound charge and the associated depolarisation field accordingly redistribute vacancies around the tip-STO contact region. This redistribution can be visualised from the simulated NVC map in Fig. 3b, which plots the in-plane distribution of $V_{\rm o}$ at the surface. Clearly, the vacancy concentration is decreased (enhanced) underneath the tip (around the contact edge).

An intuitive understanding of the simulated V_{o}^{-} -redistribution can be gained from the component-resolved distribution of the depolarisation field. As shown in Fig. 3c, the z-component, E_z^{dep} , points downward (upward) below the tip (around the contact edge), whereas the x-component, E_x^{dep} , exhibits a parentheses-like structure: a node at the contact point and antinodes around the contact edge (Fig. 3d). Effectively, E_x^{dep} points inwards, as indicated by the white arrows in Fig. 3d. The y-component (not shown), E_y^{dep} , forms an analogous structure to E_x^{dep} but is rotated by 90° in the x-y plane. The decrease in the vacancy concentration underneath the tip can be attributed to the downward E_z^{dep} component, which moves positively charged V_o^{-} from the surface into the bulk. In contrast, the combination of the upward E_z^{dep} and inwardly directed $E_{x,y}^{dep}$ components favours the accumulation



Fig. 4 Controlled manipulation of oxygen vacancies. **a** Simulated surface deformation profiles under a spherical (*upper panel*) and flat-ended (*lower panel*) tip for a static contact force of 4μ N. **b** Simulated in-plane distribution of the *z*-component, E_z^{dep} (*upper panel*) and *x*-component, E_x^{dep} (*lower panel*) of the depolarisation field induced by the flat-ended tip. The ripples in E_x^{dep} are numerical artefacts. **c**, **d** The normalised vacancy concentration (NVC) maps after mechanical scans were performed using a sharp **c** and blunt tip **d** with a contact force of 9.5 μ N within the *grey coloured boxes. Horizontal arrows* mark the corresponding fast scan direction. Before mechanical sans, the V_0^{-} -enrichment were performed by poling the pristine surface with a tip bias of -5 V. **e**, **f** NVC profiles along lines M1, M2, M3 and M4 in **c(e)** and in **d(f)**. M1 and M4 are placed 0.5 μ m away from the borders between the V_0^{-} -enriched and pristine regions. The *vertical arrow* marks the maximum net increase (Δ_{max}^{imc}) or decrease (Δ_{max}^{dex}) in NVC. *Horizontal black lines* in **e**, **f** mark the background, which is used to estimate the net change in the NVC. The NVC profiles are averaged over a 0.5- μ m-wide averaging window. Note that the boundaries between the V_0^{-} -enriched and pristine regions in **d** are more diffused compared to those in **c**. This is caused by the use of the blunt tip during the KPFM imaging. The *scale bar* in **c**, **d** represents 1 μ m

of V_o^{\cdot} around the contact edge, yielding an increase in the vacancy concentration.

The simulation results qualitatively explain the characteristics of the mechanical V_0^{-} -redistribution in Fig. 2. During a mechanical scan, a spatially extended and strong downward E_z^{dep} field acts over a larger fraction of V_0^{-} underneath the tip, which results in a dominant surface-bulk migration. In contrast, a small fraction of V_0^{-} becomes effectively trapped within a shallow annular region around the contact edge by the upward $E_{x,y}^{dep}$ and inward $E_{x,y}^{dep}$. These trapped vacancies can move laterally with the tip from the V_0^{-} -enriched region to the pristine region during the tip's lateral motion. Therefore, the contrasting roles of the depolarisation field underneath the tip and around the contact edge corroborate both the dominant surface-bulk migration and the relatively weaker lateral motion of V_0^{-} with the tip along the surface.

Notably, while scanning, the tip redistributes $V_o^{...}$ regardless whether it moves from left-right (trace) or right-left (retrace). Thus, the mechanical redistribution of $V_o^{...}$ should be understood as an average response of $V_o^{...}$ to the force applied during the trace and retrace. Moreover, the scanning velocity would influence the $V_o^{...}$ -redistribution–longer the tip spends in contact with STO, the larger number of $V_o^{...}$ it would redistribute. To check whether these factors could contribute to the weaker lateral motion of $V_o^{...}$, we performed additional experiments, whereby we applied force only during the trace, and varied the scanning velocity (see Supplementary Figs. 9–11). These experiments also yielded a weaker lateral motion but a stronger surface-bulk migration of $V_{\rm o}^{-}$ -highlighting the dominating influence of depolarisation field underneath the tip. In the following, we illustrate that the depolarisation field around the tip-STO contact junction can be tailored in favour of the lateral motion of $V_{\rm o}^{-}$, which enables controllably manipulating the vacancy distribution.

Controlled spatial modulation of oxygen vacancies. The basic concept of tailoring the SPM tip-induced depolarisation field can be understood with the aid of Fig. 4a, which compares the simulated surface deformation profiles under a static load of 4 µN using two different tip geometries. The upper panel corresponds to the spherical tip (contact radius = 8 nm) that is used in Fig. 3, and the lower panel corresponds to a flat-ended tip (contact radius = 15 nm). Compared to the spherical one, the flat-ended tip usually imparts a weaker stress on the STO surface underneath. Since the downward E_z^{dep} scales with the stress-gradient underneath the tip, the flat-ended tip induces a very small downward E_z^{dep} (Fig. 4b, upper panel). In contrast, the lateral deformation (indicated by curved arrows in Fig. 4a), which controls the depolarisation field around the contact edge, is alike for both geometries. Consequently, the flat-ended tip induces a depolarisation field distribution around the contact edge (Fig. 4b) similar to that of the spherical tip in Fig. 3c, d. Additionally, an enhanced contact radius enlarges its spatial extent. A selective suppression of E_z^{dep} underneath a flat-ended like tip should significantly reduce the surface-bulk V_0° migration. Meanwhile, the extended depolarisation field around the contact edge should improve the lateral transport of V_0° .

To validate our proposition, we performed experiments with a sharp and blunt tip. The estimated radius of curvature of this blunt tip is larger than 200 nm (see Supplementary Fig. 7). Thus, it effectively yields a flat contact junction underneath the tip. We used the 120-uc thick STO film in these experiments. Figure 4c, d show the NVC maps after mechanical scans were performed with these tips at a contact force of $9.5 \,\mu$ N. Notably, we scanned both the left and right boundaries between the V_0° -enriched and pristine regions.

To compare the sharp and blunt tip-induced V_0° -redistribution we profiled the NVC maps, as indicated by vertical lines in Fig. 4c, d. Figure 4e, f show the corresponding NVC profiles. The overlapping NVC profiles along lines M1/M4 and M2/M3 demonstrate that the V_0° -redistribution is reproducible for both tip geometries. However, the response of V_0^- to the applied force from these two tips are clearly different. The NVC profiles in Fig. 4e exhibit a maximum drop in NVC of $\Delta_{max}^{dec} = -0.75$ along lines M2 and M3 but no appreciable increase in NVC (Δ_{max}^{inc}) along lines M1 and M4. This implies that the sharp tip strongly depletes the V_0° -enriched regions but barely enriches the pristine regions. This result is in qualitative agreement with that in Fig. 2e, which shows that the fraction of the depleted V_0° that laterally move with the tip progressively decreases for applied forces larger than 6 µN. The NVC profiles in Fig. 4f, however, exhibit a maximum drop in NVC of $\Delta_{max}^{dec} = -0.25$ along lines M2 and M3 and increase by $\Delta_{max}^{inc} = +0.2$ along lines M1 and M4. This implies that every $\Delta_{max}^{inc} = +0.2$ along lines M1 and M4. implies that approximately 80% of the depleted $V_0^{...}$ laterally moved with the blunt tip. The strong reduction (improvement) of Δ^{dec}_{max} (Δ^{inc}_{max}) thus confirms an active suppression of the out-of-plane migration and a simultaneous enhancement in the lateral transportation of $V_0^{"}$, during scans with the blunt tip. Overall, the ability to deterministically move $V_0^{"}$ constitutes the first experimental demonstration of a controlled manipulation of $V_{\rm o}^{\cdot \cdot}$ in an oxide and the resulting two-dimensional spatial modulation.

Discussion

Through a combined experimental and theoretical approach, we demonstrated the flexoelectricity-mediated controlled manipulation of oxygen vacancies by the mechanical force from an SPM tip. A deterministic reconfiguration of spatial vacancy profile provides control over the electron density and related electronic correlation effects. This could enable, using an SPM-based all-inone platform, the investigation of mesoscale quantum phenomena in oxides⁴³. Ultimately, this creates the opportunity for developing mechanically sketched oxide devices, and ambipolar mechanical control of device functionalities such as electroresistance states. The voltage-free operation of the SPM tip would thereby eliminate the possibility of surface charging. At this point, we want to emphasise that flexoelectricity is a universal phenomenon, which can occur in any dielectric^{18, 44}. However, the flexoelectric coefficients of few oxides, such as SrTiO₃ and BaTiO₃, are currently known⁴⁵. Thus, our work should motivate the study of flexoelectricity in other oxides.

Broadly speaking, our KPFM-based imaging approach offers a time-efficient way of characterising the activation barrier potential for oxygen vacancy migration at room temperature to complement the conventional Arrhenius analysis⁴⁶. Combined with the feasibility of determining the diffusion coefficient, this technique could thus become an essential metrology tool for oxide-based energy and memory research. Furthermore, our theoretical model that couples the phase-field simulations to the Nernst-Planck equation, can be employed to elucidate how depolarisation fields cause oxygen vacancies., electrons, and holes to redistribute. Therefore, the model can be extended to the study of emergent problems such as the domain wall conductivity, high electrical conductivity of morphotropic phase boundaries, and leakage current in ferroelectric oxides^{47–50}.

Methods

Thin film growth. SrTiO₃ thin films were homoepitaxially grown on TiO₂-terminated Nb:SrTiO₃ (0.5% wt. doped) substrates using pulsed laser deposition technique. The growth dynamics and thickness were monitored by in-situ reflection high energy electron diffraction technique. The depositions were performed at 1000 °C and using an oxygen partial pressure of 5×10^{-7} torr. After deposition, films were annealed at 800 °C for an hour in a 1 torr oxygen atmosphere and subsequently cooled down to room temperature at a cooling rate of 20 °C per minute.

Kelvin probe force microscopy. KPFM measurements were carried out using the Asylum Research Cypher SPM at room temperature and under ambient conditions. Pt/Ir-coated metallic tips (NANOSENSORS[™] PPP-NCHPt) with a nominal spring constant ≈ 40 N/m were used for electrical/mechanical scans and KPFM imaging. The KPFM measurements were obtained in the non-contact mode using a lift height of 30 nm and the typical scan parameters used are as follows: $V_{ac} = 1 V$ (peak-to-peak), $f_{resonance} = 250$ kHz, and scan rate = 1 Hz. Before each experiment, the spring constant of the cantilever was accurately determined from force–distance measurements and thermal tuning methods. The contact force during mechanical scans was varied accordingly by controlling the set-point voltage.

Theoretical modelling. To model the oxygen vacancy redistribution by mechanical force, we performed phase-field simulations by coupling the time-dependent Ginzburg-Landau and Nernst-Planck equations.

$$\frac{\partial \mathbf{P}}{\partial t} = -L \frac{\delta F}{\delta \mathbf{P}} \tag{2}$$

$$\frac{\partial \left[V_{o}^{\cdot}\right]}{\partial t} = \nabla \left(D_{V_{o}^{\cdot}} \nabla \left[V_{o}^{\cdot}\right] + \mu_{V_{o}^{\cdot}} \left[V_{o}^{\cdot}\right] \nabla \phi\right)$$
(3)

In Eq. (2), **P** is the polarisation vector, *L* is the kinetic coefficient and *F* is the total free energy of the system, which includes Landau, electric, gradient and flexoelectric energy contributions. In Eq. (3), $[V_{\alpha}^{-}]$, $D_{V_{\alpha}^{-}}$, $\mu_{V_{\alpha}^{-}}$, and ϕ denote the concentration, diffusion coefficient, and mobility of the oxygen vacancies and the electric potential, respectively. Detailed descriptions of the energy functional F and other relevant simulation parameters are presented in the Supplementary Note 4.

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To solve Eqs. (2) and (3), the system was discretised into $100\Delta x \times 50\Delta y \times 500\Delta z$ grid points to implement the semi-implicit Fourier method⁴⁵. The 120-uc-thick STO film is simulated to be $480\Delta z$ in thickness, while the substrate and air are each $10\Delta z$ in thickness. The parameters for the total free energy of STO were adopted from work of Y.L. Li et al.⁴⁶. Following the work of R. Moos et al.⁴⁷, the initial concentration of oxygen vacancies in STO is assumed to be 3.66×10^{14} cm⁻³ based on our thin film growth conditions. In addition, the diffusion coefficient is assumed to be constant with regard to pressure and calculated as 1.23×10^{-15} cm² s⁻¹ at room temperature⁴⁷. A sufficiently long simulation time is used to ensure that the induced polarisation and oxygen vacancy concentration reach a quasi-steady state. At each time step, the electrostatic and elastostatic equilibrium equations are solved under the electric short-circuit⁴⁸ and mechanical mixed boundary conditions⁴⁹, respectively.

Data availability. The data that support the findings of this study are available from the corresponding authors upon reasonable request.

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References

- Kang, H. J. et al. Microscopic annealing process and its impact on superconductivity in T'-structure electron-doped copper oxides. *Nat. Mater.* 6, 224–229 (2007).
- Rice, W. D. et al. Persistent optically induced magnetism in oxygen-deficient strontium titanate. *Nat. Mater.* 13, 481–487 (2014).
- Santander-Syro, A. F. et al. Giant spin splitting of the two-dimensional electron gas at the surface of SrTiO₃. *Nat. Mater.* 13, 1085–1090 (2014).
- Szot, K., Speier, W., Bihlmayer, G. & Waser, R. Switching the electrical resistance of individual dislocations in single-crystalline SrTiO₃. *Nat. Mater.* 5, 312–320 (2006).
- Chen, Y. Z. et al. A high-mobility two-dimensional electron gas at the spinel/perovskite interface of γ-Al₂O₃/SrTiO₃. Nat. Commun. 4, 1371 (2013).
- Adler, S. B. Factors governing oxygen reduction in solid oxide fuel cell cathodes. *Chem. Rev.* 104, 4791–4844 (2004).
- Sawa, A. Resistive switching in transition metal oxides. *Mater. Today* 11, 28–36 (2008).
- Muller, D. A., Nakagawa, N., Ohtomo, A., Grazul, J. L. & Hwang, H. Y. Atomic-scale imaging of nanoengineered oxygen vacancy profiles in SrTiO₃. *Nature* 430, 657–661 (2004).
- Maier, J. Nanoionics: ion transport and electrochemical storage in confined systems. Nat. Mater. 4, 805–815 (2005).
- 10. Kumar, A. et al. Probing surface and bulk electrochemical processes on the LaAlO₃-SrTiO₃ interface. ACS Nano 6, 3841–3852 (2012).
- Bark, C. W. et al. Switchable induced polarization in LaAlO₃/SrTiO₃ heterostructures. *Nano Lett.* 12, 1765–1771 (2012).
- 12. Bühlmann, S., Colla, E. & Muralt, P. Polarization reversal due to charge injection in ferroelectric films. *Phys. Rev. B* **72**, 214120 (2005).
- Xie, Y., Bell, C., Hikita, Y. & Hwang, H. Y. Tuning the electron gas at an oxide heterointerface via free surface charges. *Adv. Mater.* 23, 1744–1747 (2011).
- 14. Bi, F. et al. 'Water-cycle' mechanism for writing and erasing nanostructures at the LaAlO₃/SrTiO₃ interface. *Appl. Phys. Lett.* **97**, 173110 (2010).
- Kim, Y. et al. Mechanical control of electroresistive switching. *Nano Lett.* 13, 4068–4074 (2013).
- Sharma, P. et al. Mechanical tuning of LaAlO₃/SrTiO₃ interface conductivity. Nano Lett. 15, 3547–3551 (2015).
- 17. Morozovska, A. N. et al. Thermodynamics of electromechanically coupled mixed ionic-electronic conductors: Deformation potential, Vegard strains, and flexoelectric effect. *Phys. Rev. B* **83**, 195313 (2011).
- Kogan, S. M. Piezoelectric effect during inhomogeneous deformation and acoustic scattering of carriers in crystals. *Sov. Phys. Solid State* 5, 2069–2070 (1964).
- Yudin, P. V. & Tagantsev, A. K. Fundamentals of flexoelectricity in solids. Nanotechnology 24, 432001 (2013).
- Catalan, G. et al. Flexoelectric rotation of polarization in ferroelectric thin films. *Nat. Mater.* 10, 963–967 (2011).
- Lee, D. et al. Giant flexoelectric effect in ferroelectric epitaxial thin films. *Phys. Rev. Lett.* 107, 057602 (2011).
- 22. Lu, H. et al. Mechanical writing of ferroelectric polarization. *Science* **336**, 59–61 (2012).
- Lee, D., Yang, S. M., Yoon, J. & Noh, T. W. Flexoelectric rectification of charge transport in strain-graded dielectrics. *Nano Lett.* 12, 6436–6440 (2012).
- Zubko, P., Catalan, G., Buckley, A., Welche, P. R. L. & Scott, J. F. Strain-gradient-induced polarization in SrTiO₃ single crystal. *Phys. Rev. Lett.* 99, 167601 (2007).
- 25. Stengel, M. Surface control of flexoelectricity. Phys. Rev. B 90, 201112 (2014).

- 26. Sadewasser, S. & Glatzel, T. (eds). Kelvin Probe Force Microscopy: Measuring and Compensating Electrostatic Forces (Springer, 2012).
- Andrä, M. et al. The influence of the local oxygen vacancy concentration on the piezoresponse of strontium titanate thin films. *Nanoscale* 7, 14351–14357 (2015).
- Liscio, A., Palermo, V. & Samorì, P. Nanoscale quantitative measurement of the potential of charged nanostructures by electrostatic and kelvin probe force microscopy: unraveling electronic processes in complex materials. *Acc. Chem. Res.* 43, 541–550 (2010).
- Nielsen, D. A., Popok, V. N. & Pedersen, K. Modelling and experimental verification of tip-induced polarization in Kelvin probe force microscopy measurements on dielectric surfaces. J. Appl. Phys. 118, 195301 (2015).
- Kim, Y. et al. Ionically-mediated electromechanical hysteresis in transition metal oxides. ACS Nano 6, 7026–7033 (2012).
- Balke, N. et al. Exploring local electrostatic effects with scanning probe microscopy: implications for piezoresponse force microscopy and triboelectricity. ACS Nano 8, 10229–10236 (2014).
- Bieger, T., Maier, J. & Waser, R. Kinetics of oxygen incorporation in SrTiO₃ (Fe-doped): an optical investigation. Sens. Actuators B Chem. 7, 763–768 (1992).
- Schie, M., Marchewka, A., Müller, T., De Souza, R.a. & Waser, R. Molecular dynamics simulations of oxygen vacancy diffusion in SrTiO₃. J. Phys. Condens. Matter 24, 485002 (2012).
- Paladino, A. E. Oxidation kinetics of single-crystal SrTiO₃. J. Am. Ceram. Soc. 48, 476–478 (1965).
- Waser, R. Bulk conductivity and defect chemistry of acceptor-doped strontium titanate in the quenched state. J. Am. Ceram. Soc. 74, 1934–1940 (1991).
- Shin, C. & Yoo, H. Al-doped SrTiO₃: Part II, unusual thermodynamic factor and chemical diffusivity. *Solid State Ion*. 178, 1089–1094 (2007).
- Kumar, A., Ciucci, F., Morozovska, A. N., Kalinin, S. V. & Jesse, S. Measuring oxygen reduction/evolution reactions on the nanoscale. *Nat. Chem.* 3, 707–713 (2011).
- Morozovska, A. N. et al. Flexocoupling impact on size effects of piezoresponse and conductance in mixed-type ferroelectric semiconductors under applied pressure. *Phys. Rev. B* 94, 174101 (2016).
- Freedman, D. A., Roundy, D. & Arias, T. A. Elastic effects of vacancies in strontium titanate: Short- and long-range strain fields, elastic dipole tensors, and chemical strain. *Phys. Rev. B* 80, 064108 (2009).
- Gu, Y., Hong, Z., Britson, J. & Chen, L.-Q. Nanoscale mechanical switching of ferroelectric polarization via flexoelectricity. *Appl. Phys. Lett.* **106**, 022904 (2015).
- Cao, Y., Shen, J., Randall, C. & Chen, L.-Q. Effect of ferroelectric polarization on ionic transport and resistance degradation in BaTiO₃ by phase-field approach. J. Am. Ceram. Soc. 97, 3568–3575 (2014).
- 42. Wang, J.-J. et al. Defect chemistry and resistance degradation in Fe-doped SrTiO₃ single crystal. *Acta Mater.* **108**, 229–240 (2016).
- 43. Cheng, G. et al. Electron pairing without superconductivity. *Nature* 521, 196–199 (2015).
- 44. Tagantsev, A. K. Piezoelectricity and flexoelectricity in crystalline dielectrics. *Phys. Rev. B* 34, 5883–5889 (1986).
- Zubko, P., Catalan, G. & Tagantsev, A. K. Flexoelectric effect in solids. Annu. Rev. Mater. Res. 43, 387-421 (2013).
- Arrhenius, S. A. Über die dissociationswärme und den einflusß der temperatur auf den dissociationsgrad der elektrolyte. Z. Physik. Chem. 4, 96–116 (1889).
- 47. Bednyakov, P. S., Sluka, T., Tagantsev, A. K., Damjanovic, D. & Setter, N. Formation of charged ferroelectric domain walls with controlled periodicity. *Sci. Rep.* **5**, 15819 (2015).
- Oh, Y. S., Luo, X., Huang, F.-T., Wang, Y. & Cheong, S.-W. Experimental demonstration of hybrid improper ferroelectricity and the presence of abundant charged walls in (Ca,Sr)₃Ti₂O₇ crystals. *Nat. Mater.* 14, 407–413 (2015).
- Seidel, J. et al. Electronic properties of isosymmetric phase boundaries in highly strained Ca-doped BiFeO₃. Adv. Mater. 26, 4376–4380 (2014).
- Cao, Y., Shen, J., Randall, C. & Chen, L.-Q. Effect of multi-domain structure on ionic transport, electrostatics, and current evolution in BaTiO₃ ferroelectric capacitor. *Acta Mater.* **112**, 224–230 (2016).
- Chen, L.-Q. & Shen, J. Applications of semi-implicit Fourier-spectral method to phase field equations. *Comput. Phys. Commun.* 108, 147–158 (1998).
- 52. Li, Y. L. et al. Phase transitions and domain structures in strained pseudocubic (100) SrTiO₃ thin films. *Phys. Rev. B* **73**, 184112 (2006).
- Moos, R. & Hardtl, K. H. Defect chemistry of donor-doped and undoped strontium titanate ceramics between 1000° and 1400 °C. J. Am. Ceram. Soc. 80, 2549–2562 (1997).
- Li, Y. L., Hu, S. Y., Liu, Z. K. & Chen, L.-Q. Effect of substrate constraint on the stability and evolution of ferroelectric domain structures in thin films. *Acta Mater.* 50, 395–411 (2002).
- Li, Y. L., Hu, S. Y., Liu, Z. K. & Chen, L.-Q. Effect of electrical boundary conditions on ferroelectric domain structures in thin films. *Appl. Phys. Lett.* 81, 427–429 (2002).

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Author contributions

S.D. conceived and planned this project under the direction of T.W.N. S.D. grew the films and performed structural characterisation with assistance from M.K. S.D. carried out KPFM measurements assisted by Y.J.S., S.M.Y., and L.F.W. and performed data analysis. B.W. and Y.C. performed theoretical modelling under the direction of L.-Q.C. and S.V.K. M.R.C. performed SEM measurements. S.D. and T.W.N. wrote the manuscript with inputs from all authors.

Additional information

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