



Copper chalcogenide thermoelectric materials

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ABSTRACT Cu-based chalcogenides have received increasing attention as promising thermoelectric materials due to their high efficiency, tunable transport properties, high elemental abundance and low toxicity. In this review, we summarize the recent research progress on this large family compounds covering diamond-like chalcogenides and liquid-like Cu₂X (X=S, Se, Te) binary compounds as well as their multinary derivatives. These materials have the general features of two sublattices to decouple electron and phonon transport properties. On the one hand, the complex crystal structure and the disordered or even liquid-like sublattice bring about an intrinsically low lattice thermal conductivity. On the other hand, the rigid sublattice constitutes the charge-transport network, maintaining a decent electrical performance. For specific material systems, we demonstrate their unique structural features and outline the structure-performance correlation. Various design strategies including doping, alloying, band engineering and nanostructure architecture, covering nearly all the material scale, are also presented. Finally, the potential of the application of Cu-based chalcogenides as high-performance thermoelectric materials is briefly discussed from material design to device development.

Keywords: thermoelectric, Cu-based chalcogenides, sublattice, transport properties

INTRODUCTION

Thermoelectric materials can realize the direct conversion between heat and electricity, intriguing widespread interests in the situation of aggravating environment and energy crisis [1,2]. The performance of thermoelectric materials is usually evaluated by the dimensionless figure of merit (zT), defined as $zT = S^2\sigma T/\kappa$, where S is the Seebeck coefficient, σ is the electrical conductivity, κ is the thermal conductivity and T is the absolute temperature. These transport parameters are strongly

correlated to each other, and it is the key task to decouple transport properties for a better zT [3,4]. In the 1990s, Slack proposed the concept of “phonon-glass electron-crystal” (PGEC) [5], that is, a high-performance thermoelectric material should possess a certain structure that allows carriers’ efficient transfer while effectively blocking phonon propagation. In accordance with this principle, a bloom of new concepts, strategies, material systems as well as processing technologies has occurred in this field during the past twenty years, enhancing zT values well beyond unity, and even above two [6–11].

For a PGEC material, the crystal structure is usually composed of two sublattices: one constitutes the electrically conducting network while the other serves as thermal blocker and sometimes also charge reservoir. By virtue of such sublattices, Cu-based chalcogenides have emerged as one of the new, promising systems with potential for power generation [12] whose zT values as a function of emerging time are shown in Fig. 1. Also considering the high abundance and trivial toxicity of copper, Cu-based chalcogenides are expected to be inexpensive and environmentally friendly candidates for thermoelectric application.

In this review, we focus on the decoupled transport properties and the structural origins in Cu-based chalcogenides, covering liquid-like materials, diamond-like compounds, layered BiCuSeO, etc. The two sublattices commonly seen in this large family will be discussed in detail, and the relationship between the structures and the decoupled transport properties will be spotlighted. For each type of Cu-based chalcogenides, latest progress will be demonstrated.

DECOUPLED TRANSPORT PROPERTIES BY TWO INDEPENDENT SUBLATTICES

For ideal thermoelectric materials with two sublattices,

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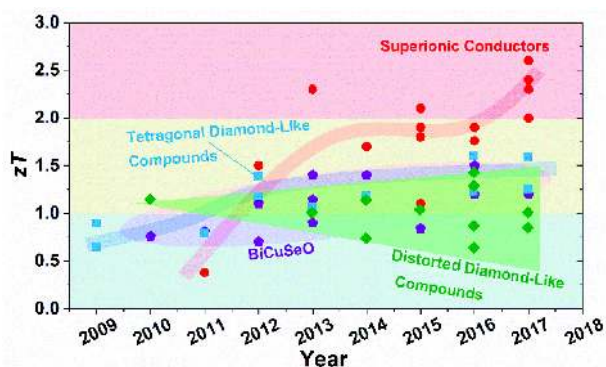


Figure 1 Timeline of zT for selected Cu-based superionic conductors [13–27] (red), tetragonal [28–37] (blue) and distorted [38–49] (green) diamond-like materials and BiCuSeO oxyselenides (purple) [50–61].

one sublattice should form a nice framework serving as carrier pathways, and the other is featured with certain disordered structures or soft bonds blocking phonon transport. Also, the features of crystal structures transform into certain band structures and phonon dispersion relations, yielding, for example, a combination of light and heavy bands that is favorable for a simultaneous realization of large Seebeck coefficient and high mobility. Certainly, the two cases in two spaces, i.e., crystal structure and band structure/phonon dispersion, are unified, thus going beyond the conventional realm of two sublattices or PGEC, offering more possibility for decoupling transport properties.

Complex/disordered sublattice and low thermal conductivity

As shown in Fig. 2a, Cu-based thermoelectric chalcogenides generally exhibit lower thermal conductivity especially at high temperatures than traditional thermoelectric

materials such as SiGe and CoSb₃. In a simple yet intuitive way, lattice thermal conductivity is related to the heat capacity (C_V), speed of sound (v) and mean free path of phonons (l) via $\kappa_L = 1/3C_Vvl$ [62]. Therefore κ_L can be lowered by suppressing the three parameters, which is determined by the complex or disordered crystal structures.

The mean free path of phonons, l , can be suppressed by introducing scattering centers with multiple scales. On the atomic scale, complex crystal structures featured by large unit cell or large atom number N intrinsically result in small l [63]. Basically, solids possess $3N$ vibrational modes including 3 acoustic modes and $3(N-1)$ optical modes [64]. The optical ones store most of the thermal energy, but contribute little to heat conduction because of their low group velocity. In addition, the heat-carrying acoustic modes are tend to be interacted with and hindered by the optical branches [65]. From another perspective, the cut-off frequency (or the Debye temperature) for the acoustic modes is considerably lower in these complex systems. As shown in Fig. 2b, κ_L for Cu-based chalcogenides exhibits a negative dependence on the primitive cell volume, showing that a large unit cell is a practical indicator for low thermal conductivity.

Normally, heat capacity is an inherent quality of a material, which is usually difficult to modulate. For conventional solids at room and high temperatures, C_V is close to or higher than the Dulong-Petit limit, $3Nk_B$ or $3R$ [65]. Inspiringly, the liquid-like character in Cu₂X compounds provides an effective solution to reducing C_V . As shown in Fig. 3a, Cu₂Se possesses two sublattices: the rigid FCC framework of Se atoms and the disordered and flowing sublattice of Cu. At high temperatures, Cu ions migrate from one site (interstitial one formed by Se) to another, exhibiting a flowing character that is

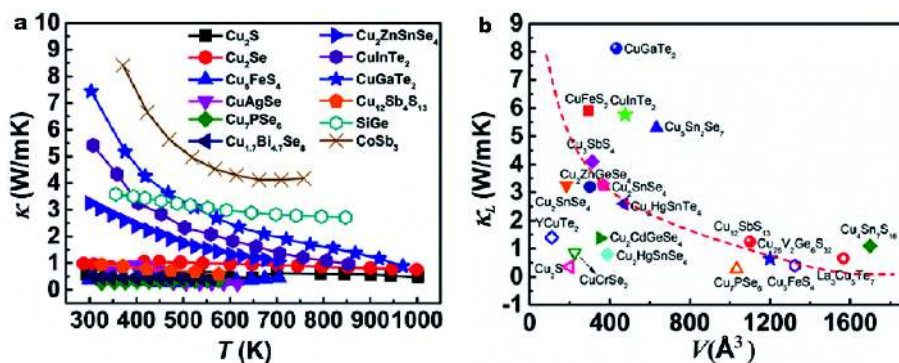


Figure 2 (a) Thermal conductivity for Cu-based chalcogenides; (b) lattice thermal conductivity as a function of the primitive cell volume in a variety of Cu-based chalcogenides at 300 K. The dashed line shows a negative correlation between the lattice thermal conductivity and the primitive cell volume. Data are taken from Refs. [14,16,29–31,42,45,66–77].

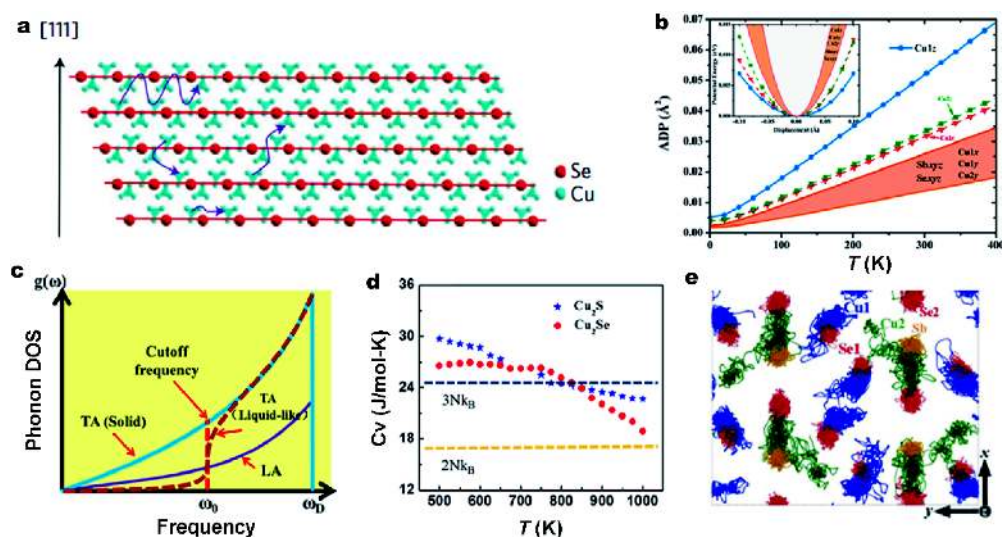


Figure 3 Liquid-like behavior in Cu-based materials. (a) Crystal structure of Cu_2Se where Cu atoms flow among the interstitial sites of Se rigid sublattice, reproduced from Ref. [14], Copyright 2012, Nature Publishing Group; (b) schematic phonon DOS for solid and liquid-like materials, adapted from Ref. [12], Copyright 2016, Elsevier; (c) temperature dependence of the specific heat in Cu_2Se and Cu_3Sb ; (d) atomic displacement parameter varying with temperature in Cu_3SbSe_3 and (e) trajectories of atoms from molecular dynamics simulations for Cu_3SbSe_3 at 400 K, reproduced from Ref. [79,80], Copyright 2014, National Academy of Sciences and Copyright 2014, Nature Publishing Group, respectively.

analogous to liquid [14,78]. It is known that transverse modes are missing in liquid (Fig. 3b), thus yielding a limit of heat capacity of $2Nk_B$. Therefore, C_V of Cu_2Se is noticeably suppressed as shown in Fig. 3c. Similarly, a “part-crystalline part-liquid” state is proposed in Cu_3SbSe_3 [79], which is constituted by a rigid crystalline sublattice and a noncrystalline sublattice. Cu atoms vibrate in large amplitude with a high atomic displacement parameter (ADP) as shown in Fig. 3d and e, and can be regarded as a liquid state.

In fact, the structural features and dynamic behaviour of liquid-like materials and the mechanism of suppressed thermal conductivity are more complicated than we discussed above. It is experimentally confirmed by Li *et al.* [81] that the transverse acoustic phonon modes are completely suppressed by ultrafast dynamic disorder in AgCrSe_2 . However, Voneshen *et al.* [82] argue that the fast local hops of Cu in Cu_2Se should be considered as anharmonic vibration, and the transitional diffusion of Cu is too slow to affect phonon propagation.

Low thermal conductivity can also come from lone pairs, as proposed by Skoug *et al.* [83] in nitrogen-group chalcogenides. Owing to the different delocalization behaviours of Sb 5s lone pair electrons, Cu_3SbSe_4 , CuSbSe_2 and Cu_3SbSe_3 exhibit different Se–Sb–Se angles as shown in Fig. 4. Essentially, the mutual repulsion between the lone pair electrons and the adjacent valence electrons during thermal agitation leads to large lattice

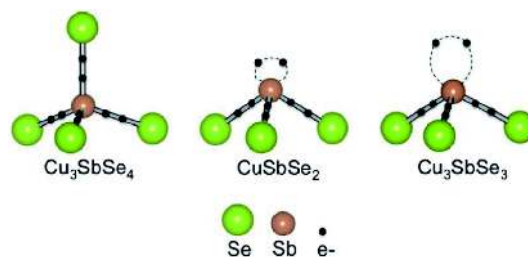


Figure 4 Schematic diagram of the lone pair electrons situation in Cu_3SbSe_4 , CuSbSe_2 , Cu_3SbSe_3 compounds, reproduced from Ref. [83], Copyright 2011, the American Physical Society.

anharmonicity.

Structural retainer and electrical transport

It is somewhat unexpected that Cu_{2-x}Se liquid-like materials with such a low thermal conductivity exhibit a decent electrical conductivity [14]. Based on the first-principle calculations, Sun *et al.* [84] found that the valence band maxima (VBM) and the transport of holes are dominated by Se orbitals while Cu vacancies serve as efficient acceptors, shifting the Fermi level, but do not change the band shape.

For many multinary Cu-based compounds, the electrically conducting channel (mostly VBM) is considered to be constituted by Cu–X bonds. Taking Cu_2SnSe_3 [39] as an example in Fig. 5a, the VBM is mostly occupied by the p-d hybridization from Cu–Se bonds, acting as the

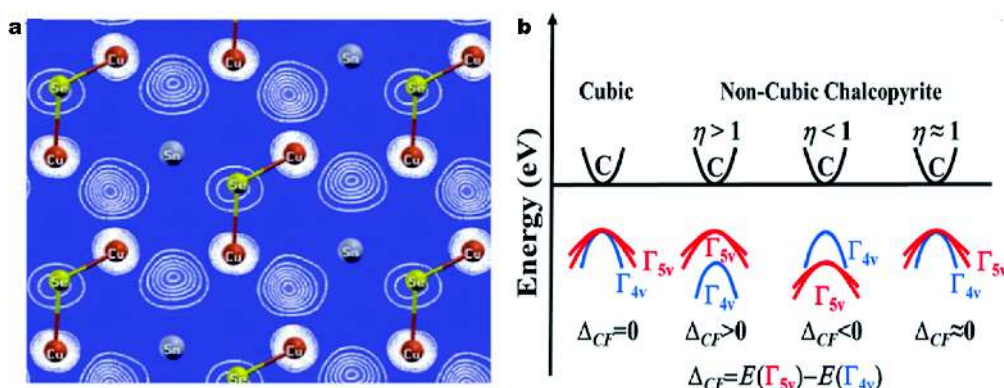


Figure 5 (a) Partial charge density of the state plots of Cu_2SnSe_3 , near the upper valence-band, reproduced from Ref. [39] Copyright 2010, the American Chemical Society; (b) band convergence in the pseudocubic diamond-like chalcogenides, reproduced from Ref. [32], Copyright 2014, Wiley-VCH GmbH&Co.

structural retainer and charge conduction path. Sn orbitals contribute little to the occupied states while predominantly affect the conductive band. The Cu–X conduction network has also been proposed in BiCuSeO [85], Cu_3SbSe_4 [86], $\text{Cu}_2\text{CdZnSe}_4$ [28], etc.

Derived from the high-symmetry diamond, the diamond-like Cu chalcogenides possess highly degenerate valence bands, ensuring a large Seebeck coefficient and power factor even at a high doping level. Particularly, the power factor (PF) can be maximized by reducing the band split off, which is proposed by Zhang *et al.* [32] as a pseudocubic approach to screen and develop high-performance non-cubic materials. Specifically, the tetragonal diamond-like chalcogenides form a long-range cubic-like and short-range non-cubic structure. As shown in Fig. 5b, when the bands are degenerate, that is, the valence band splitting energy Δ_{CF} approaches zero, the distortion parameter $\eta=c/2a$ gets close to 1, leading to the maximum PF. The unity- η rule and the pseudocubic approach have been found effective in screening high-performance tetragonal diamond-like compounds [87,88], which will be discussed later.

LIQUID-LIKE OR SUPERIONIC MATERIALS

Cu_2X (X=S, Se, Te) compounds and their alloys

Liquid-like materials may be the most typical examples of using two sublattices to optimize thermoelectric properties. As discussed above, Cu_2X materials at high temperatures exhibit superionic cubic phases where Cu atoms flow through the X rigid framework (Fig. 3a and 6b). Benefiting from this “phonon-liquid electron-crystal (PLEC)” structure, this family in the pristine form shows

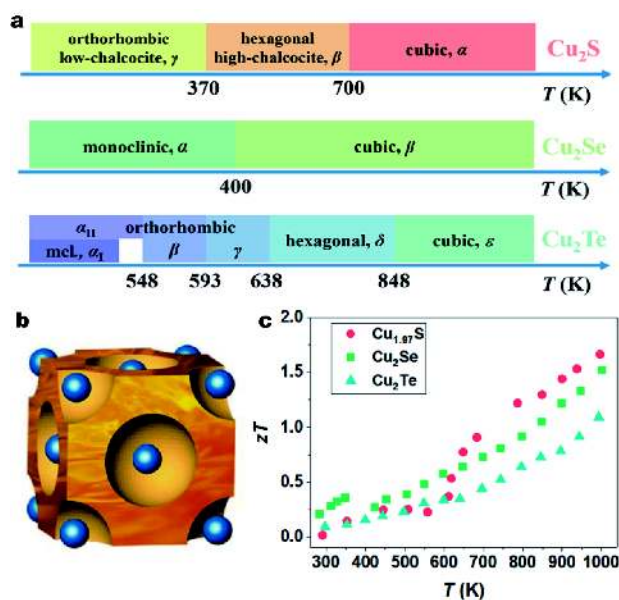


Figure 6 (a) Phases varying with temperature for Cu_2X compounds; (b) schematic depiction of high-temperature superionic crystal structure of Cu_2S , reproduced from Ref. [16], Copyright 2014, Wiley-VCH GmbH&Co. The blue spheres represent sulfur atoms, and the liquid-like copper ions (yellow) travel freely within the sulfide sublattice. (c) zT as a function of temperature for Cu_2X compounds [14,16,18].

high zT values ranging from 1.0 to 1.7 as demonstrated in Fig. 6c. The phase structures at low temperatures are quite complex for these compounds and vary with the ratio of Cu to X, and at least one phase transition occurs with increasing temperature as shown in Fig. 6a.

In 2012, Liu *et al.* [14] found the unique thermal transport behavior of Cu_{2-x}Se superionic conductor and proposed the concept PLEC as an extension to PGEC. Later in 2014 Cu_2S was found to exhibit similar liquid-like

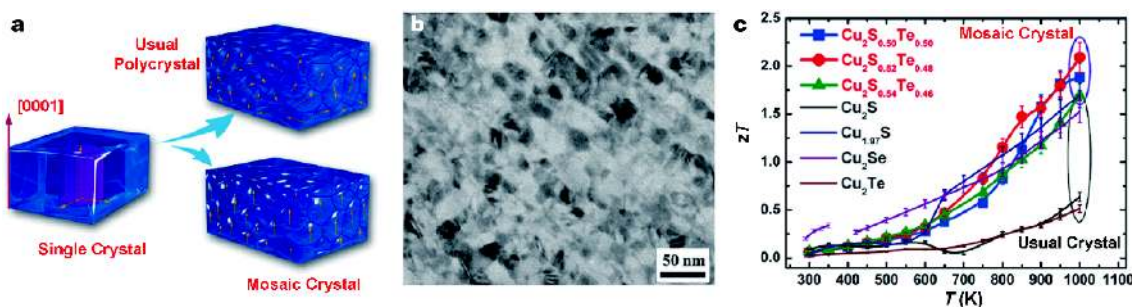


Figure 7 (a) Schematic depiction of mosaic structures, (b) TEM image for $\text{Cu}_2\text{S}_{0.5}\text{Te}_{0.5}$ as a mosaic crystal, (c) zT values for mosaic and usual crystals. Figures are adapted from Ref. [17], Copyright 2015, Wiley-VCH GmbH&Co.

behavior but with lower effective mass and higher deformation potential, showing a high zT of 1.7 at 1,000 K [16]. The phases in Cu_2Te are even more complex as shown in Fig. 6a. In 2015, He *et al.* [18] reported that Cu_{2-x}Te has many stable and meta-stable phases as well as much weaker ionic bonds than Cu_{2-x}S and Cu_{2-x}Se . Owing to the optimized carrier concentrations and lowered thermal conductivity, zT value in Cu_2Te was grossly improved from 0.55 in the SPS-ed samples to 1.1 in the directly annealed samples at 1,000 K.

Based on a simple chemical intuition [89], the increase of atomic size and mass from S to Te and the decrease of electronegativity lead to a weaker and less ionic Cu–X bond. This means that Cu vacancies are more prone to form, resulting in a higher carrier density. Meanwhile the lattice thermal conductivity is normally lower in tellurides than selenides or sulfides due to the larger Te atoms and weaker bonds. In addition, all of the three Cu_2X compounds exhibit similar disordered cubic structures at high temperatures. So alloying or forming solid solutions is likely to not only further reduce the already low thermal conductivity, but also tune the electrical transport properties.

Zhao *et al.* [90] found that Cu_2Se and Cu_2S can form a continuous solid solution over the entire composition range. The solid solutions are polymorphic materials composed of varied phases with different proportions at room temperature, and transform into single cubic phase at high temperatures. The lattice thermal conductivity was significantly lowered not only by alloy scattering of phonons but also due to the reduced sound speed. In addition, Cu–S bond is stronger than Cu–Se bond, leading to reduced amount of Cu vacancies and lower carrier concentration towards the optimal value. A maximum zT value of ~ 2.0 at 1,000 K was achieved in slightly S-doped Cu_2Se [23].

As for Cu_2S – Cu_2Te alloys, due to the large mass and size

contrast between S and Te, a special mosaic crystal structure [17] was built in $\text{Cu}_2(\text{S}, \text{Te})$ bulk single-phase polycrystalline materials as shown in Fig. 7. That is, the blocks exhibit a nearly identical orientation, so the bulk appears like a single crystal from the macroscale point of view but contains a number of small-angle boundaries. The electrons are freely transferred along the frames of quasi-single crystals and phonons are strongly scattered by lattice strains or interfaces of mosaic nanograins. When compared with the usual polycrystalline matrix Cu_2S or Cu_2Te , a simultaneous optimization of thermal conductivity and power factor were achieved, yielding a high zT of ~ 2.1 at 1,000 K, which goes beyond the traditional approaches using single crystals or nano-materials. The mosaic structures were also found in triple $\text{Cu}_{2-y}\text{S}_{1/3}\text{Se}_{1/3}\text{Te}_{1/3}$ solid solutions [91], and are considered to open a new window of realizing ultrahigh thermoelectric performance [92].

Studies on Cu_2X liquid-like materials have also been extended to nanostructured composites. By utilizing the special interaction between metal Cu and multi-walled carbon nanotubes (CNTs), Nunna *et al.* [21] realized the *in-situ* growth of Cu_2Se on the surface of CNTs and then fabricated a series of $\text{Cu}_2\text{Se}/\text{CNTs}$ hybrid materials. Due to the high-degree homogeneously dispersed molecular CNTs inside the Cu_2Se matrix, a zT of 2.4 at 1,000 K has been achieved. Olvera *et al.* [22] reported a record zT of 2.6 at 850 K in Cu_2Se – CuInSe_2 composites. It was suggested that the incorporation of a small fraction of In into the Cu_2Se lattice induced partial localization of Cu^+ ions, and a hybrid structure with same Se lattice was formed. This led to a simultaneous increase in the carrier mobility and a drastic reduction in the lattice thermal conductivity. Ge *et al.* [93] prepared nanostructured $\text{Cu}_{1.8}\text{S}$ (Cu_9S_5) by mechanical alloying. By doping Na at the interstitial sites, the carrier concentration was reduced to the optimal range, and nano pores were introduced

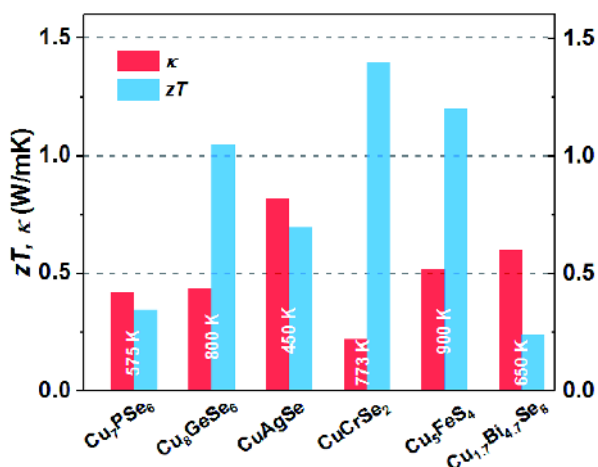


Figure 8 Thermal conductivity and maximum zT for selected ternary superionic conductors: Cu₇PSe₆ [68], Cu_{7.6}Ag_{0.4}GeSe_{5.1}Te_{0.9} [94], CuAgSe_{0.95}Te_{0.05} [95], CuCrSe₂-AgCrSe₂ [96], 0.8Cu₈S₄-0.2Cu₅FeS₄ [67] and Cu_{1.7}Bi_{4.7}Se₈ [97].

resulting in suppressed thermal conductivity. A high zT of 1.1 was obtained at a relatively low temperature of 773 K.

Ternary derivatives of Cu₂X

Besides the binary Cu₂X (X = S, Se, Te) compounds, there are many derivatives which also demonstrate superionic conduction with liquid-like behavior. High-temperature thermal conductivities and maximal zT values of typical materials are summarized in Fig. 8.

CuAgSe can be regarded as an alloy between Cu₂Se and Ag₂Se. Similarly, it undergoes a structural phase transition around 480 K. Owing to the superior carrier mobility [98] and the low lattice thermal conductivity, CuAgSe behaves as a potential thermoelectric material. Stoichio-

metric CuAgSe shows n-type conduction, but an n-to-p transition is observed when increasing temperature in the samples with slight deficiencies of Ag or Cu [66]. By doping Te at Se site, the thermal conductivity was significantly reduced, resulting in a $zT=0.7$ at 450 K in CuAgSe_{0.95}Te_{0.05} [66,95].

In CuCrSe₂, the CrSe₂⁻ layer distributes regularly and the Cu ions occupy the interlayer space and become disordered due to the migration from one to another tetrahedral site. zT around unity at 773 K was reported [70], and an even higher $zT=1.4$ was claimed in AgCrSe₂-CuCrSe₂ nanocomposites by virtue of all-wavelength phonon scattering [96]. The isostructural CuCrS₂ exhibits a much lower zT value of 0.15 at 673 K, mainly due to the larger band gap and deteriorated electrical performance [99].

Sulfide bornite Cu₅FeS₄, a widespread natural mineral, can be regarded as a Fe- and vacancy-doped derivative of Cu₂S. This compound exhibits three phases at different temperatures as shown in Fig. 9a. The S framework provides a good electrical transport and the disordered occupation of Cu, S and the vacancies suppressed the transport of the phonons, leading to a high zT of 1.2 at 900 K in 0.8Cu₈S₄-0.2Cu₅Fe□₂S₄ (□ represents a vacancy) [67]. Particularly, Cu migration was effectively hampered in the solid solution of Cu₅FeS₄-Cu₂S in comparing with Cu₂S due to the pinning effect from Fe atoms.

There are even more complex superionic derivatives. Argyrodite compounds possess a general chemical formula A^{x+}_{12-y/x}B^{y+}Q²⁻₆ (A = Li⁺, Cu⁺, Ag⁺; B = Ga³⁺, Si⁴⁺, Ge⁴⁺, Sn⁴⁺, P⁵⁺, As⁵⁺) [68,94,100]. In addition to the disordered Cu sublattice at high temperatures as shown in Fig. 10a and b, Cu₇PSe₆ and Cu₃GeSe₆ possess extremely low lattice thermal conductivity of

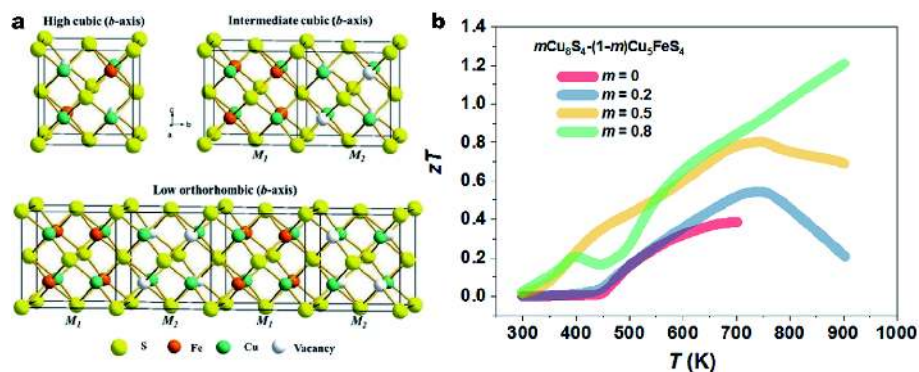


Figure 9 (a) The crystal structures of Cu₅FeS₄ for the low temperature phase and high temperature phase. Reproduced from Ref. [67], Copyright 2014, the Royal Society of Chemistry; (b) Temperature dependence for the zT value for the $m\text{Cu}_8\text{S}_4-(1-m)\text{Cu}_5\text{FeS}_4$ compound.

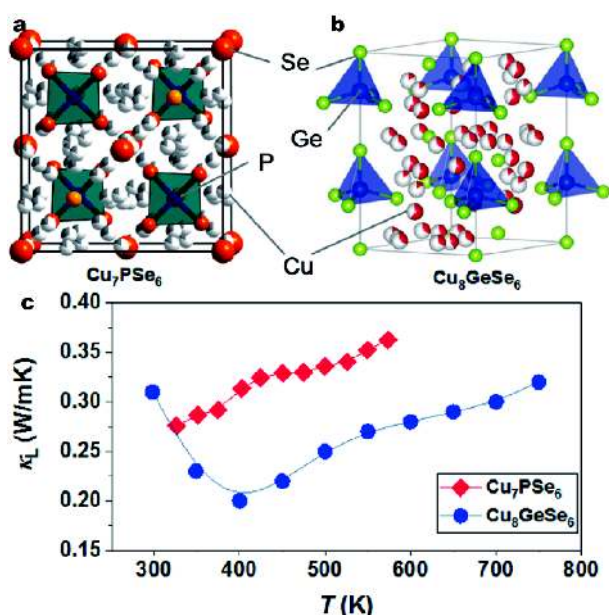


Figure 10 High-temperature crystal structure for (a) Cu_7PSe_6 (reproduced from Ref. [68], Copyright 2014, the American Chemical Society) and (b) Cu_8GeSe_6 (reproduced from Ref. [94], Copyright 2017, the Royal Society of Chemistry); (c) lattice thermal conductivity as a function of the temperature for the two compounds [68,94].

$\sim 0.3 \text{ W m}^{-1} \text{ K}^{-1}$ even at around room temperature (Fig. 10c). This is probably related to as many as 56 and 90 atoms per unit cell for the two compounds, respectively, where the low-frequency optical phonons make a difference by either trapping heat or interacting with acoustic phonons. By alloying with Ag and Te, the electrical conductivity of Cu_8GeSe_6 is greatly enhanced and the low lattice thermal conductivity is maintained, leading to a high zT of unity at 800 K [94].

Concerns about Cu migration and materials stability

The migration of Cu in liquid-like materials brings about the ultralow thermal conductivity and high zT values, but at the same time, raises widespread concerns on Cu precipitation and materials degradation. This phenomenon was clearly reported in Cu_2S by Miyatani *et al.* [101] in 1953 for the first time, and was also found within Cu_2Se by Ema [102] in 1990.

For the purpose of device application, great efforts have been made to suppress Cu drift in Cu_2X materials. It is desirable that the long-range ionic migration is suppressed while the short-range drift is maintained. For materials designing, foreign atoms [22,103] were added into the matrix with the intention to block the motion of Cu ions. The effect is observable but not considerable.

The ternary Cu_3FeS_4 can be regarded as Fe- and vacancy-co-doped Cu_2S , and the migration of Cu was significantly hampered by the immobile Fe [67]. Most recently, we have studied the mechanism of Cu migration in liquid-like materials and found it is possible to greatly improve material's stability by introducing electronically-conducting but ion-blocking barriers [104]. Similarly, Tang *et al.* [105] found that the incorporated graphene three dimensional (3D) network can provide another possibility to block the migration of Cu ions and to enhance the stability of Cu_2S .

DIAMOND-LIKE Cu-BASED CHALCOGENIDES

Diamond-like compounds are a big family structurally derived from IV elementary substance, covering binary II-VI and III-V compounds, ternary I-III-VI₂ and II-IV-V₂ chalcopyrites, I₃-V-VI₄ stannites, quaternary I₂-II-IV-VI₄ compounds, and even large-cell $\text{Cu}_{12}\text{Sb}_4\text{S}_{13}$ tetrahydrites and $\text{Cu}_{26}\text{V}_2\text{M}_6\text{S}_{32}$ ($\text{M}=\text{As}, \text{Ge}, \text{Sn}, \text{Sb}$) colusites. The diverse interatomic distances cation-X and the difference in electronegativity between the cations result in a natural superlattice structure. For nearly all the p-type semiconductors in this family, Cu-X constitutes VBM for the conduction of hole carriers while other cation atoms bond with X contributing to CBM.

Tetragonal diamond-like compounds

The tetragonal diamond-like compounds are composed of two cubic zinc-blended structure units, including I-III-VI₂, I₃-V-VI₄ and I₂-II-IV-VI₄ compounds as shown in Fig. 11. The crystal structures, band gaps and zT values for selected materials are displayed in Table 1.

Ternary I-III-VI₂ compounds can be regarded as the super cell of the zinc-blend structure as shown in Fig. 11. High zT values of 1.18 and 1.4 were realized in CuInTe_2 [30] and CuGaTe_2 [31], respectively, being the highest ones among diamond-like compounds. While ternary CuFeS_2 , namely chalcopyrite, an important natural copper ore, is one of the few n-type materials among the Cu-based diamond-like thermoelectric materials, which is attributed to the sulfur vacancies. Maximum zT values around 0.25 were reported for this material [74,111]. However, further enhancement of thermoelectric performance in CuFeS_2 is hindered by the low carrier mobility that is dominated by localized d electrons of Fe.

I₃-V-VI₄ compounds can be regarded as four-fold of ZnSe structure. Among them, Cu_3SbSe_4 with a narrow band gap of $\sim 0.3 \text{ eV}$ is a also promising candidate

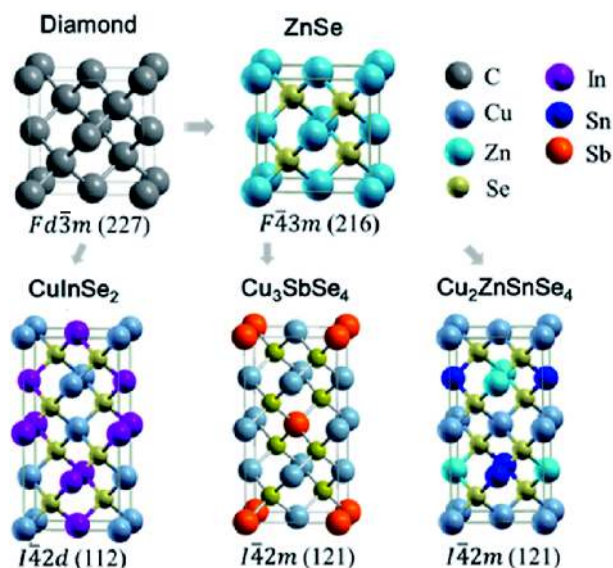


Figure 11 Crystal structure of diamond, zinc-blende ZnSe, chalcopyrite CuInSe₂, stannite Cu₃SbSe₄ and Cu₂ZnSnSe₄.

[35,36,112,113]. Quaternary I₂-II-IV-VI₄ (I=Cu; II=Zn, Cd, Fe, Co, Mn, Hg, Mg; IV=Ge, Sn; VI=S, Se, Te) compounds generally exhibit a larger band gap and lower mobility than the ternary counterparts, which is likely due to the localized *d*-orbitals of the transition metal elements.

The generally low carrier concentrations as well as the high lattice thermal conductivity in the pristine form especially in the low and medium temperature range may be the common disadvantages for these tetragonal diamond-like chalcogenides. Doping was widely employed to improve the carrier concentration and the electrical conductivity, such as CuIn(Ga)_{1-x}M_xTe₂ (M=Zn, Mn, Cd, Hg, Ni, Ag, Gd) [114–118], Cu_{1-x}Fe_{1+x}S₂ [119], Cu₃Sb_{1-x}M_xSe₄ (M=Al, In, Sn, Ge, Bi) [35,120–122] and

Table 1 Space group, band gap and *zT* for selected I-III-VI₂, I₃-V-VI₄ and I₂-II-IV-VI₄ tetragonal diamond-like compounds

Chemical formula	Space group	E_g (eV)	zT , T (K)	Ref.
CuGaTe ₂	<i>I</i> -42 <i>d</i>	1.2	1.4, 923	[31]
CuInTe ₂	<i>I</i> -42 <i>d</i>	1.02	1.18, 850	[30]
CuFeS ₂ (<i>n</i>)	<i>I</i> -42 <i>d</i>	0.34	0.21, 573	[74]
Cu ₃ SbSe ₄	<i>I</i> -42 <i>m</i>	0.31	1.26, 673	[35]
Cu ₃ SbS ₄	<i>I</i> -42 <i>m</i>	0.9	0.10, 300	[73]
Cu ₂ CdSnSe ₄	<i>I</i> -42 <i>m</i>	0.98	0.65, 700	[28]
Cu ₂ ZnSnSe ₄	<i>I</i> -42 <i>m</i>	1.41	0.95, 850	[29]
Cu ₂ HgSnSe ₄	<i>I</i> -42 <i>m</i>	1.81	0.2, 723	[71]
Cu ₂ HgGeSe ₄	<i>I</i> -42 <i>m</i>	/	0.34, 733	[106]
Cu ₂ HgSnTe ₄	<i>I</i> -42 <i>m</i>	1.62	/	[107]
Cu ₂ MgSnSe ₄	<i>I</i> -42 <i>m</i>	1.7	0.42, 700	[108]
Cu ₂ CdGeSe ₄	<i>I</i> -42 <i>m</i>	1.2	0.42, 723	[72]
Cu ₂ ZnGeSe ₄	<i>I</i> -42 <i>m</i>	1.4	0.55, 723	[109]
Cu ₂ ZnGeS ₄	<i>I</i> -42 <i>m</i>	1.5	/	[110]

Cu₂Cd_{1-x}In_xSnSe₄ [123]. Introducing vacancies is another practical way for the electrical transport optimization as well as the lattice thermal conductivity minimizing. Cu vacancy is the most common for p-type doping such as Cu_{1-x}In(Ga)Te₂ [87,124] and Cu_{3-x}SbSe₄ [125], which is due to the small formation energy of this defect, while anion vacancies are feasible for donor doping as seen in CuFeS_{2-x} [74] and Cu₂FeSnS_{4-x} [126].

The pseudocubic approach has been testified in several compounds such as CuGaTe₂ [87], Cu₂MGeSe₄ [127] and Cu₂TMSnSe₄ (TM=Mn, Fe, Co) [88]. The distortion parameter, η , as a function of the cell parameter *a* for the tetragonal diamond-like chalcogenides is shown in Fig. 12a. It can be qualitatively utilized as an indicator map to discover or optimize high-performance tetragonal dia-

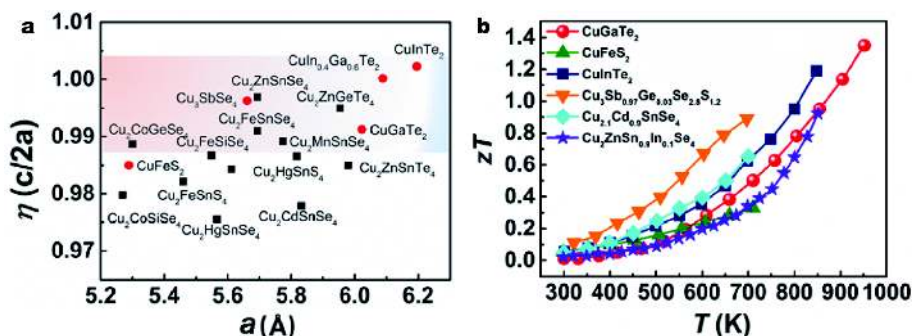


Figure 12 (a) Distortion parameter as a function of the lattice parameter *a* [28,72,87,106–108,119,123,126,136,137]. (b) Temperature dependence of *zT* for tetragonal diamond-like compounds [28,29,87,112,119].

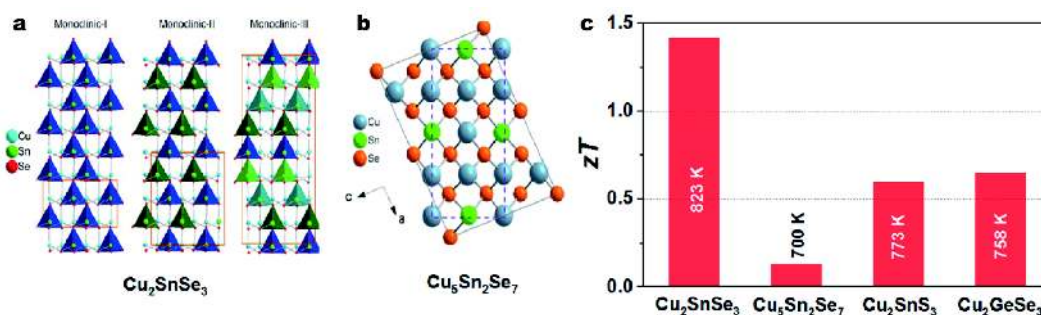


Figure 13 Crystal structure of (a) Cu_2SnSe_3 (reproduced from Ref. [140], Copyright 2013, the American Chemical Society) and (b) $\text{Cu}_5\text{Sn}_2\text{Se}_7$ (reproduced from Ref. [141], Copyright 2014, the American Chemical Society); (c) zT of distorted diamond-like Cu_2SnSe_3 [38], $\text{Cu}_5\text{Sn}_2\text{Se}_7$ [141], Cu_2SnS_3 [142] and Cu_2GeSe_3 [143].

mond-like thermoelectric materials, which can be confirmed by the thermoelectric performance of the reported diamond-like compounds as shown in Fig. 12b.

For thermal conduction suppression, alloying is an effective approach *via* intensifying phonon scattering by mass and strain fluctuations [128] as demonstrated in several solid solutions, such as $\text{CuGa}_{1-x}\text{In}_x\text{Te}_2$ [129], $\text{Cu}_3\text{SbSe}_{4-x}\text{S}_x$ [36,130], $\text{Cu}_2\text{Zn}_{1-x}\text{Fe}_x\text{GeSe}_4$ [131], $\text{Cu}_2\text{Cd}_{1-x}\text{Zn}_x\text{SnSe}_4$ [132] and $\text{Cu}_2\text{HgSnSe}_{4-x}\text{Te}_x$ [107]. In addition, the nanostructuring approach was also employed [133,134]. The enhanced thermoelectric performance can be attributed to the phonon scattering introduced by crystal defects and the increased density of states near the Fermi level, such as $(\text{CuInTe}_2)_{0.99}(\text{ZnTe})_{0.01}$ composited with 0.1 wt% TiO_2 nanofiber ($zT \sim 1.47$ at 823 K) [135], CuInTe_2 composited ZnO ($zT \sim 1.61$ at 823 K) [34].

Distorted diamond-like chalcogenides

There are also numerous diamond-like compounds which crystallize in much distorted structures far from tetragonal, including $\text{I}_2\text{-IV-VI}_3$ and $\text{Cu}_5\text{Sn}_2\text{X}_7$ ($\text{X}=\text{Se}, \text{Te}$) materials. On the one hand, the structural complexity endows them with intrinsically low thermal conductivity [138]; on the other hand, the delocalized p orbitals occupy the VBM, facilitating high mobility and good electrical performance [39,139].

Cu_2SnSe_3 can crystallize into a cubic ($F-43m$) or monoclinic phase (three types [140]) at room temperature. A high zT of 1.14 at 850 K was achieved *via* In substitution for Sn by Shi *et al.* [39]. Bulk (Ag, In)-co-doped Cu_2SnSe_3 samples were prepared by Li *et al.* [38] *via* a high-pressure combustion synthesis. It was found that Ag doping considerably enhances the Seebeck coefficient. The low electrical conductivity caused by Ag-doping was further compensated by In-doping at Sn

site, yielding the maximum $zT = 1.42$ in $\text{Cu}_{1.85}\text{Ag}_{0.15}\text{Sn}_{0.9}\text{In}_{0.1}\text{Se}_3$ at 823 K. For Cu_2GeSe_3 , the electrical conductivity is lower and the Seebeck coefficient is higher due to the large electronegativity of Ge. zT of ~ 0.5 at 750 K were obtained in Ga-doped Cu_2GeSe_3 samples [144]. Similar results are also found in Cu_2SnS_3 [142,145].

Doping towards higher carrier density is effective to enhance the performance of these Cu_2AX_3 compounds, but it goes the opposite for $\text{Cu}_5\text{Sn}_2\text{X}_7$ ($\text{X}=\text{Se}, \text{Te}$) with a carrier concentration on the order of 10^{21} cm^{-3} . This is a kind of mixed-valent compound crystallizing in C -centered monoclinic phase with a centrosymmetric space group $C2/m$, being regarded as a super structure of the non-centrosymmetric cubic structure (space group $F-43m$) as shown in Fig. 13b [141,146].

Tetrahedrite and colusite minerals

With even more complex crystal structures, the diamond-like tetrahedrites and colusites possess 58 and 66 atoms in a crystal cell as shown in Fig. 14a and c, respectively, leading to thermal conductivities smaller than $1 \text{ W m}^{-1} \text{ K}^{-1}$ at room temperature. Notably, the two systems are natural minerals, and both of them crystallize in a cubic structure with space groups of $I-43m$ and $P-43n$, respectively. Also, they share several common features. Firstly, both of them are very brittle, which is due to the rigid but weak covalent bonds. Secondly, they exhibit a metallic character in electrical transport, i.e., high carrier concentration (on the order of 10^{20} cm^{-3}) and low Seebeck coefficient. This may be related to the high concentration of the intrinsic Cu vacancies. In fact, the carrier concentration for tetrahedrites is too high, and doping or alloying is needed. Thirdly, from the perspective of material processing, it seems difficult to obtain the pure phase for both systems, which may also be related to the weak bonding. Binary and ternary

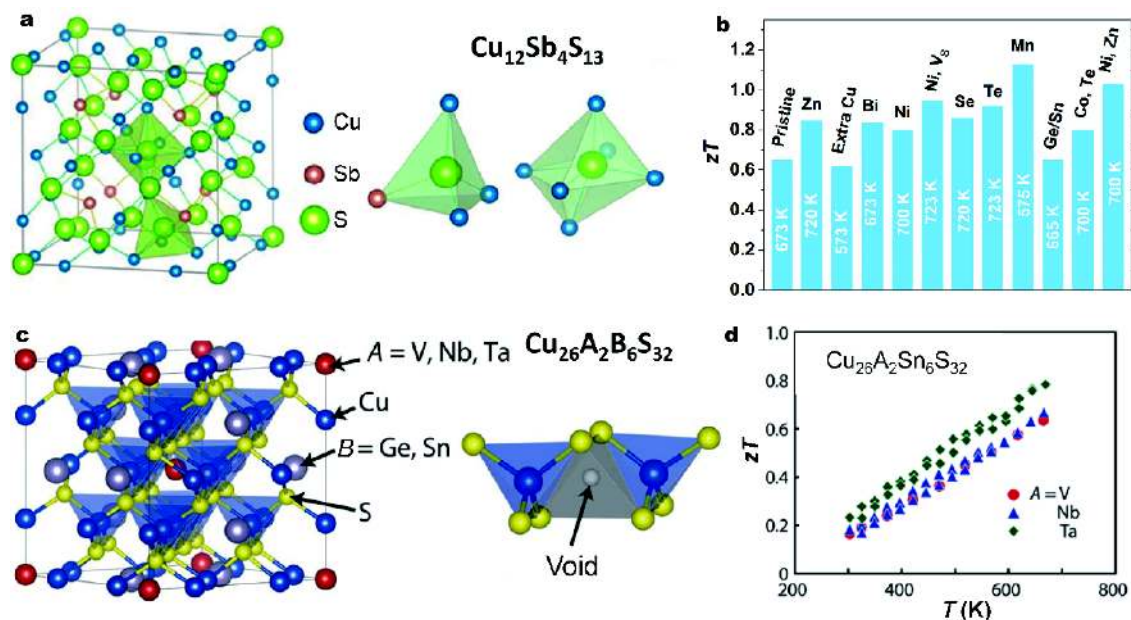


Figure 14 (a) Crystal structure of tetrahedrites, reproduced from Ref. [47], Copyright 2016, American Chemical Society; (b) zT of tetrahedrites [46–49,147–153]; (c) crystal structure and (d) zT of colusites, reproduced from Ref. [43], Copyright 2016, the Royal Society of Chemistry.

impurity phases often exist accompanying with the main phase, which can significantly influence the mechanical and transport properties of the materials.

In 2013, Lu *et al.* [45] reported a $zT=0.95$ at 720 K in Zn-doped $\text{Cu}_{12}\text{Sb}_4\text{S}_{13}$. Thereafter, various studies on tetrahedrites have been reported with further optimization by doping and alloying as shown in Fig. 14b. A detailed review of the studies on this compound can be found [154]. It is somewhat unexpected that few reports are available on electrical transport analysis probably due to the difficulty in accurate Hall measurement.

Suekuni *et al.* [42,43,155,156] conducted a series of studies on $\text{Cu}_{26}\text{A}_2\text{B}_6\text{S}_{32}$ (A=V, Nb, Ta; B=As, Ge, Sn, Sb) colusites. On the one hand, as shown in Fig. 14d, there is no obvious difference in thermoelectric performance among V-, Nb- and Ta-containing compounds, which is consistent with the calculation that VBM (where E_F lies) is composed mostly of Cu-3d and S-3p hybridized orbitals. This hybridization also brings about a large DOS effective mass ($4\text{--}7m_0$) and a decent Seebeck coefficient under a high carrier density. Maximum $zT\sim 1.0$ was achieved in $\text{Cu}_{26}\text{Nb}_2\text{Ge}_6\text{S}_{32}$ at 670 K [44].

OTHER HIGH-PERFORMANCE Cu-BASED CHALCOGENIDES

As shown in Fig. 15, RCuX_2 (R = rare earth metals or transition metals, X = S, Se, Te) chalcogenides adopt

space groups of $P21/c$, $P-3$ or $P-3m1$. Typically, TmCuTe_2 with a narrow band gap of 0.23 eV crystallizes in layered structure with a $P-3$ space group. Lin *et al.* [157] found that Tm ions break the metallic Cu–Cu and the covalent Te–Te bonds interaction. Combined with the intrinsically low thermal conductivity, a high zT of 0.81 was achieved at 745 K. Esmaili *et al.* [158] reported high electrical resistivity with values $\sim 0.5\text{--}500\ \Omega\ \text{cm}$ in RCuX_2 (R=Gd, Dy, Er) which are larger than the typical high-performance thermoelectric materials by 2–5 orders of magnitude. The thermoelectric performance can be further enhanced by doping at the R site in order to increase the carrier concentration. zT of ~ 0.75 at 780 K was achieved in $\text{Y}_{0.96}\text{Cu}_{1.08}\text{Te}_2$ owing to the low thermal conductivity with a value of $\sim 0.5\ \text{W}\ \text{m}^{-1}\ \text{K}^{-1}$ at 800 K and the optimized electrical transport being resulted from the Y deficiencies [69]. Other rare-earth metal Cu-based chalcogenides such as $\text{La}_2\text{CuBiS}_5$ [159] may also be potential thermoelectric materials.

Ba/Cu/X alkali-earth chalcogenides cover a large group of compounds. BaCu_2Ch_2 (Ch=S, Se) crystallizes in two stable structures, orthorhombic BaCu_2S_2 -type and tetragonal ThCr_2Si_2 -type as shown in Fig. 16 [161]. Kurosaki *et al.* [162] reported a zT of 0.28 at 820 K in potassium-doped $\beta\text{-BaCu}_2\text{S}_2$, characterized by layered structure with a space group $I4/mmm$. The decent thermoelectric performance comes from the low thermal conductivity

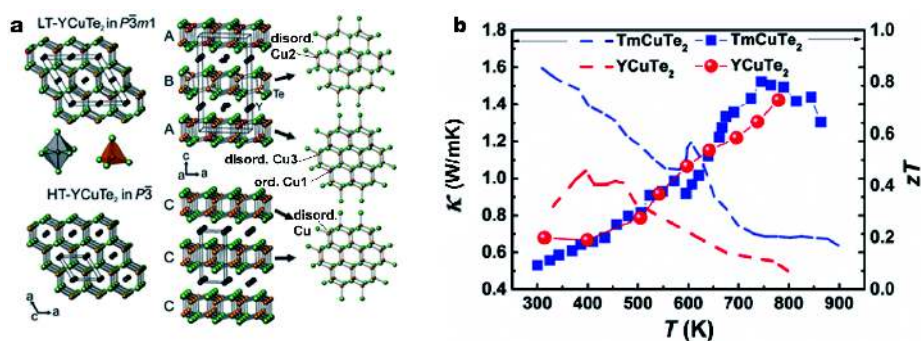


Figure 15 (a) The crystal structure for YCuTe₂ in low temperature phase ($P\bar{3}m1$) and high temperature phase ($P\bar{3}$), reproduced from Ref. [69], Copyright 2016, the Royal Society of Chemistry. (b) Thermal conductivity and zT for YCuTe₂ and TmCuTe₂ [69,157,160].

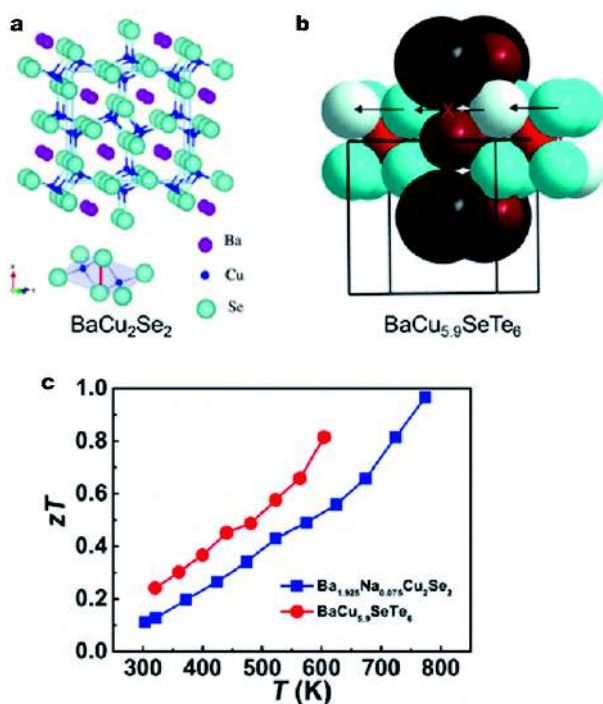


Figure 16 Crystal structure for (a) BaCu₂Se₂ (reproduced from Ref. [163], Copyright 2015, the Royal Society of Chemistry) and (b) BaCu_{5.9}SeTe₆ (reproduced from Ref. [161], Copyright 2014, American Chemical Society); (c) zT value as a function of the temperature for Ba_{1.925}Na_{0.075}Cu₂Se₂ and BaCu_{5.9}Se(S)Te₆, respectively [161,163].

($\sim 0.97 \text{ W m}^{-1} \text{ K}^{-1}$) and the increased carrier concentration by K-doping. The isostructural selenide Ba_{0.925}Na_{0.075}Cu₂Se₂ exhibits a higher zT of 1.0 at 773 K [163] (Fig. 16c). Oudah *et al.* [161] reported quaternary BaCu_{5.9}STe₆ and BaCu_{5.9}SeTe₆ chalcogenides with a zT exceeding 0.8 at around 600 K (Fig. 16c), which was attributed to the low thermal conductivity and the high Seebeck coefficient.

BiCuSeO oxyselenide adopts a layered, ZrCuSiAs-type

structure (Fig. 17a), consisting of fluorite (Bi₂O₂)²⁺ layers storing carriers and blocking phonons, and anti-fluorite (Cu₂Se)₂²⁻ layers transferring carriers [164]. Similar to most Cu-based chalcogenides, BiCuSeO shows p-type conductive behavior probably due to the intrinsic Cu vacancies. As a layered material, obvious anisotropy exists in both thermal and electrical transport along in-plane and out-plane directions. The anharmonic bonding and mixed-anion framework in BiCuSeO bring about a low thermal conductivity $< 1 \text{ W m}^{-1} \text{ K}^{-1}$. The zT of BiCuSeO has been increased to ~ 1.5 through various approaches (see Fig. 17 b–f) including element doping (Mg, Sr, Ca, Ba, Pb at Bi site, Cu vacancies) [51,53,59,165,166], alloying (S, Te) [167], modulation doping [57] and texture treatment [56]. The findings and design methodology of this material are of valuable significance to investigation on similar layered compounds such as SnSe. More details on thermoelectric BiCuSeO can be found in a review article [164].

SUMMARY AND OUTLOOK

In summary, various Cu-based chalcogenides with high abundance and low toxicity have been found to exhibit high zT values well above unity and even about two, which originates from the character of two sublattices and thus the decoupled transport properties. The complex unit cell, distorted or even liquid-like sublattice result in an intrinsically low thermal conductivity while the charge transport network and high band degeneracy guarantee a decent electrical performance.

New and fascinating physical phenomena were brought out along with the emergence of Cu-based chalcogenides, paving new ways for developing high-performance thermoelectric materials. The flowable Cu ions and the liquid-like behavior proposed in Cu₂Se have extended the “PGEC” concept to “PLEC” that has been widely applied

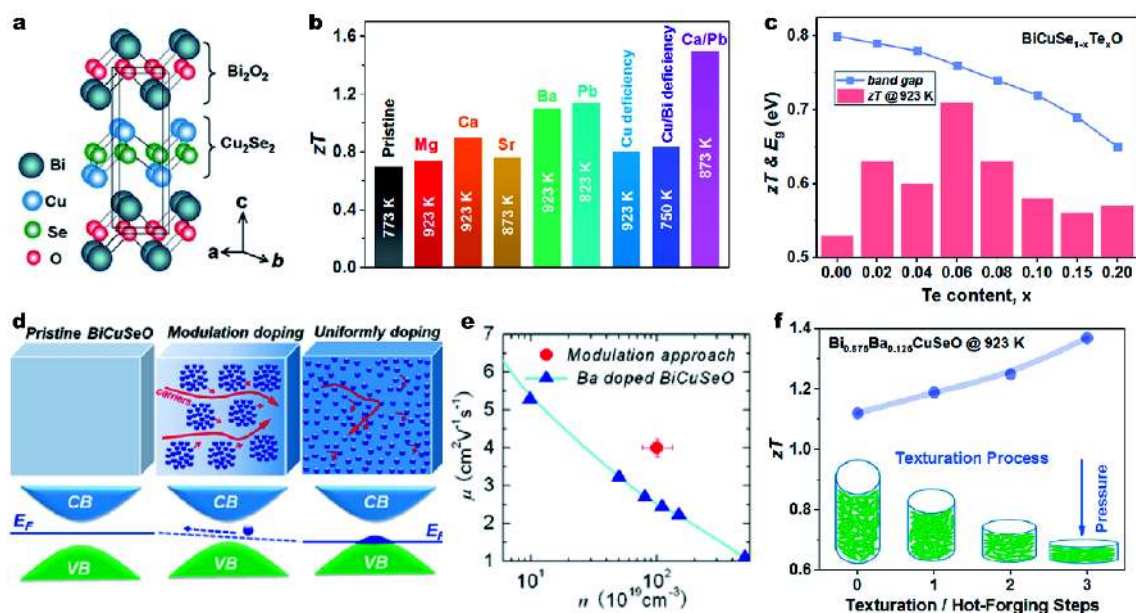


Figure 17 (a) Crystal structure of BiCuSeO, reproduced from Ref. [52] Copyright 2012, the Royal Society of Chemistry; (b) zT values for pristine [52], Bi-site-doped [50,53–55,59,165] and cation-deficient [51,58] BiCuSeO compounds; (c) band gap variation and zT values for BiCuSe_{1-x}Te_xO [167]; (d) schematic depiction of modulation doping and (e) mobility, reproduced from Ref. [57] Copyright 2014, American Chemical Society; (f) zT as a function of Bi_{0.875}Ba_{0.125}CuSeO samples before and after hot-forging [56,164].

to other Cu- or Ag-based superionic conductors with extremely low thermal conductivity. The pseudocubic approach has been found effective in screening and optimizing the diamond-like compounds.

There is no escaping the fact that challenges lie ahead for Cu-based chalcogenides operating as high-efficiency thermoelectric materials. Cu ion migration is the key to high zT values of liquid-like compounds but meanwhile seriously hampers the stability and reliability. It is desired to hinder the long-range migration of Cu ions and maintain the short-range motion. For diamond-like Cu-based chalcogenides without ionic migration, the brittle nature brings about the poor machinability, which limits the development of devices. For practical thermoelectric application, it is crucial to step from high-performance materials to high-efficiency devices. In this process, all the factors including the compatibility of materials with electrodes, processability, and stability should be investigated, which are even tougher for new thermoelectric materials. With deeper understanding on the transport mechanisms, availability of more advanced fabrication/processing techniques, we have been trying to solve these problems and it is expected that high-efficiency thermoelectric devices made of Cu-based chalcogenides will come soon.

Received 17 May 2018; accepted 20 June 2018;
published online 10 August 2018

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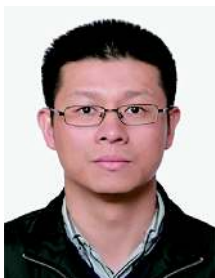
Acknowledgements This review is supported by the National Key Research and Development Program of China (2018YFB0703600), the National Natural Science Foundation of China (51625205), the Key Research Program of Chinese Academy of Sciences (KFZD-SW-421), Program of Shanghai Subject Chief Scientist (16XD1403900), Youth Innovation Promotion Association, CAS (2016232) and Shanghai Sailing Program (18YF1426700).

Author contributions Shi X and Chen L designed the topic and framework of this review; Wei TR, Qin Y and Qiu P collected and organized the data; Wei TR and Qin Y wrote the review with the support from Qiu P, Shi X and Chen L. All authors contributed to the general discussion.

Conflict of interest The authors declare no conflict of interest.



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铜基硫族化合物热电材料

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摘要 铜基硫族化合物因其高性能、可调的输运性质、高丰度和低毒性, 被认为是很有前景的新型热电材料, 引起了研究者的广泛关注. 本文总结了近年来铜基热电材料的研究进展, 包括类金刚石结构材料、声子液体二元及多元化合物等. 本文首先总体介绍了两套亚晶格的基本特征及其对热学、电学性质的影响: 一方面, 复杂晶体结构和无序、甚至液态化的亚晶格导致极低的热导率; 另一方面, 刚性亚晶格构成电荷传输通道, 保证了较高的电学性能. 然后, 本文针对特定的几类材料体系, 详细介绍了其典型结构特征与“结构-性能”构效关系, 以及掺杂、固溶、能带结构调控和纳米结构设计等多尺度优化手段. 最后, 本文从材料研发和器件研制的角度评述了铜基硫族化合物作为热电材料的应用前景及相关进展.