

# Correlated X-ray/ultraviolet/optical variability in NGC 6814

Jon Troyer,<sup>1★</sup> David Starkey,<sup>2</sup> Edward M. Cackett,<sup>1</sup> Misty C. Bentz,<sup>3</sup>  
Michael R. Goad,<sup>4</sup> Keith Horne<sup>2</sup> and James E. Seals<sup>3</sup>

<sup>1</sup>Department of Physics and Astronomy, Wayne State University, 666 W. Hancock St, Detroit, MI 48201, USA

<sup>2</sup>SUPA, University of St Andrews, School of Physics and Astronomy, North Haugh, St Andrews, KY16 9SS, UK

<sup>3</sup>Department of Physics and Astronomy, Georgia State University, Atlanta, GA 30303, USA

<sup>4</sup>Department of Physics and Astronomy, College of Science and Engineering, University of Leicester, University Road, Leicester LE1 7RH, UK

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## ABSTRACT

We present results of a three-month combined X-ray/UV/optical monitoring campaign of the Seyfert 1 galaxy NGC 6814. The object was monitored by *Swift* from June through August 2012 in the X-ray and UV bands and by the Liverpool Telescope from May through July 2012 in *B* and *V*. The light curves are variable and significantly correlated between wavebands. Using cross-correlation analysis, we compute the time lag between the X-ray and lower energy bands. These lags are thought to be associated with the light travel time between the central X-ray emitting region and areas further out on the accretion disc. The computed lags support a thermal reprocessing scenario in which X-ray photons heat the disc and are reprocessed into lower energy photons. Additionally, we fit the light curves using CREAM, a Markov Chain Monte Carlo code for a standard disc. The best-fitting standard disc model yields unreasonably high super-Eddington accretion rates. Assuming more reasonable accretion rates would result in significantly underpredicted lags. If the majority of the reprocessing originates in the disc, then this implies the UV/optical emitting regions of the accretion disc are farther out than predicted by the standard thin disc model. Accounting for contributions from broad emission lines reduces the lags in *B* and *V* by  $\sim 25$  per cent (less than the uncertainty in the lag measurements), though additional contamination from the Balmer continuum may also contribute to the larger than expected lags. This discrepancy between the predicted and measured interband delays is now becoming common in AGN where wavelength-dependent lags are measured.

**Key words:** accretion, accretion discs – galaxies: active – galaxies: individual: NGC 6814 – galaxies: Seyfert.

## 1 INTRODUCTION

The current standard model of an active galactic nucleus (AGN) consists of a central supermassive black hole (SMBH) actively accreting matter (e.g. Rees 1984) which forms an accretion disc. As matter is drawn towards the black hole’s event horizon, gravitational potential energy is converted into kinetic and viscous internal energy. The accretion disc then radiates thermally with the majority of the flux in the UV/optical bands (e.g. Koratkar & Blaes 1999). X-rays from AGN are thought to be dominated by emission due to Compton upscattering of the thermally emitted photons from the accretion disc by hot electrons in the disc’s corona. Recent measurements from X-ray reverberation and gravitational microlensing both independently imply that the X-ray emitting region is small ( $\lesssim 10$

$GM/c^2$ ; e.g. De Marco et al. 2013; Reis & Miller 2013; Mosquera et al. 2013; Cackett et al. 2014; Blackburne et al. 2015).

In order to probe the interior structure of AGN, a method known as reverberation mapping (RM) (Blandford & McKee 1982) is used extensively (see Peterson 2014, for a recent review). RM involves measuring the time delay associated with some variable luminosity source and the ‘echo’ it produces as it interacts with matter. Most AGN host galaxies are at distances too far for the AGN to be spatially resolved. In these cases, RM provides the only direct method of probing the interior of an AGN. In addition, RM trades spatial resolution for time resolution. Through RM, the object’s size scale is resolved via a time delay i.e. the light crossing time between the source and the echo ( $R \simeq ct$ ). In principle, RM has few limitations with respect to AGN distance as long as sufficient signal-to-noise exists, the monitoring period is long enough to detect significant variability, and the sampling is dense enough to resolve time delays between different emission components.

\* E-mail: jon.troyer@wayne.edu

It has long been established that AGN spectra possess inherent variability. A correlation between light curves of different wavelengths has been detected in many AGN (e.g. Krolik et al. 1991; Ulrich, Maraschi & Urry 1997; McHardy et al. 2014; Shappee et al. 2014; Edelson et al. 2015; Fausnaugh et al. 2015). This suggests that the emission processes associated with different wavebands are related. If such a correlation exists for a particular object, the time lag between the X-ray and UV/optical light curves can be calculated in order to help understand the origin of the UV/optical variability. There are two favoured scenarios regarding the source of correlated UV/optical variability (e.g. Alston, Vaughan & Uttley 2013; Shappee et al. 2014). The first case is where the X-ray variability leads the UV/optical variability. In this case, it is thought that the X-ray flux heats the accretion disc and thus produces a portion of the thermal emission – the thermal reprocessing scenario. The second case is where the UV/optical variability leads the X-ray variability. In this case, it is thought that some intrinsic thermal variability in the accretion disc exists that produces the UV/optical variability. The UV/optical seed photons would carry their variability signature to the corona and cause the X-ray variability via Compton up scattering. In the UV/optical leading scenario, time lags associated with the accretion disc viscous time-scale would be expected. This time-scale quantifies how rapidly a perturbation in the accretion flow can propagate through the disc. For a typical AGN SMBH, the viscous time-scale is of the order of months to years (Czerny 2006).

Of course, it is also possible that both these scenarios are occurring simultaneously (likely on different time-scales), or that other mechanisms can contribute to the lags. For instance, observations of Mrk 79 (Breedt et al. 2009) show that on time-scales of days – weeks, the X-rays and optical bands are highly correlated, and easily explained by reprocessing, while on time-scales of years there is variability in the optical not observed in X-rays, requiring an additional mechanism to produce the variations. Similarly, in NGC 4051, while there is strong evidence for X-rays driving optical variability on short time-scales (days), there is a need for another mechanism (perhaps, reflected optical continuum flux from the dust torus) to account for all the optical variability observed (Breedt et al. 2010). Long-term monitoring of NGC 5548 has also shown that on long ( $\sim 1$  yr) time-scales the optical variability, while correlated with X-rays, has a higher variability amplitude. Therefore the long-term optical variability cannot be caused by reprocessing in this case, and is more likely due to inward propagation of accretion rate changes (Uttley et al. 2003). Finally, it is possible that reprocessed emission in the Broad Region (BLR) may contaminate accretion disc lags (e.g. Korista & Goad 2001; Breedt et al. 2010).

Short time-scale lags and lags that depend on wavelength are consistent with thermal reprocessing. Here, the X-ray photons are thermally reprocessed in the accretion disc. The simplest geometry for such a scenario is the ‘lamppost’ model where the X-rays are assumed to be emitted from a centrally located point source above the plane of the accretion disc. Given the compact size of the X-ray region compared to the UV/optical emitting region, this simplification is generally agreed to be a reasonable assumption. In the context of the lamppost model, X-ray flux is incident upon inner regions of the accretion disc before the outer regions, due to the shorter light crossing time. See Cackett, Horne & Winkler (2007) for a detailed description of the application of the lamppost model to continuum lags.

NGC 6814 has been part of a previous RM campaign (the LAMP project; Bentz et al. 2009b). Significant continuum variability was seen over the approximately 70 d of monitoring, with excess vari-

ance in the  $B$  band of  $F_{\text{var}} = 0.18$ . An  $H\beta$  lag of  $\tau_{\text{cent}} = 6.6 \pm 0.9$  d (rest frame) was measured, which, with the  $f$ -value from Grier et al. (2013) implies a black hole mass of  $(1.4 \pm 0.3) \times 10^7 M_{\odot}$  (Bentz & Katz 2015). Spectroscopic monitoring from the LAMP campaign also led to measured lags in  $H\alpha$ , He I, He II, and  $H\gamma$  (Bentz et al. 2010). Pancoast et al. (2014) perform dynamical modelling of the LAMP data on NGC 6814, resulting in a significantly lower black hole mass estimate of  $(2.6_{-1.1}^{+1.5}) \times 10^6 M_{\odot}$ . Their modelling also provides an estimate of the inclination of the system of  $i = 47_{-27}^{+17}$  deg.

In this paper, we present data from a combined monitoring campaign showing short time-scale ( $\sim 1$ – $3$  d), wavelength-dependent time lags between the X-ray and UV/optical bands for NGC 6814 for the first time. Observations of NGC 6814 were obtained in support of the AGN RM campaign STARE,<sup>1</sup> but provided an additional opportunity to study wavelength dependent lags of the accretion disc. In Section 2, we discuss the observations and data reduction. In Section 3, the light-curve analysis including computation of time lags between the X-ray and various wave bands, and modelling the light curve with a standard disc Markov Chain Monte Carlo (MCMC) code. Finally, in Section 4, we discuss the results of our time lag analysis and MCMC light-curve fitting analysis and possible physical interpretations.

## 2 OBSERVATIONS & DATA REDUCTION

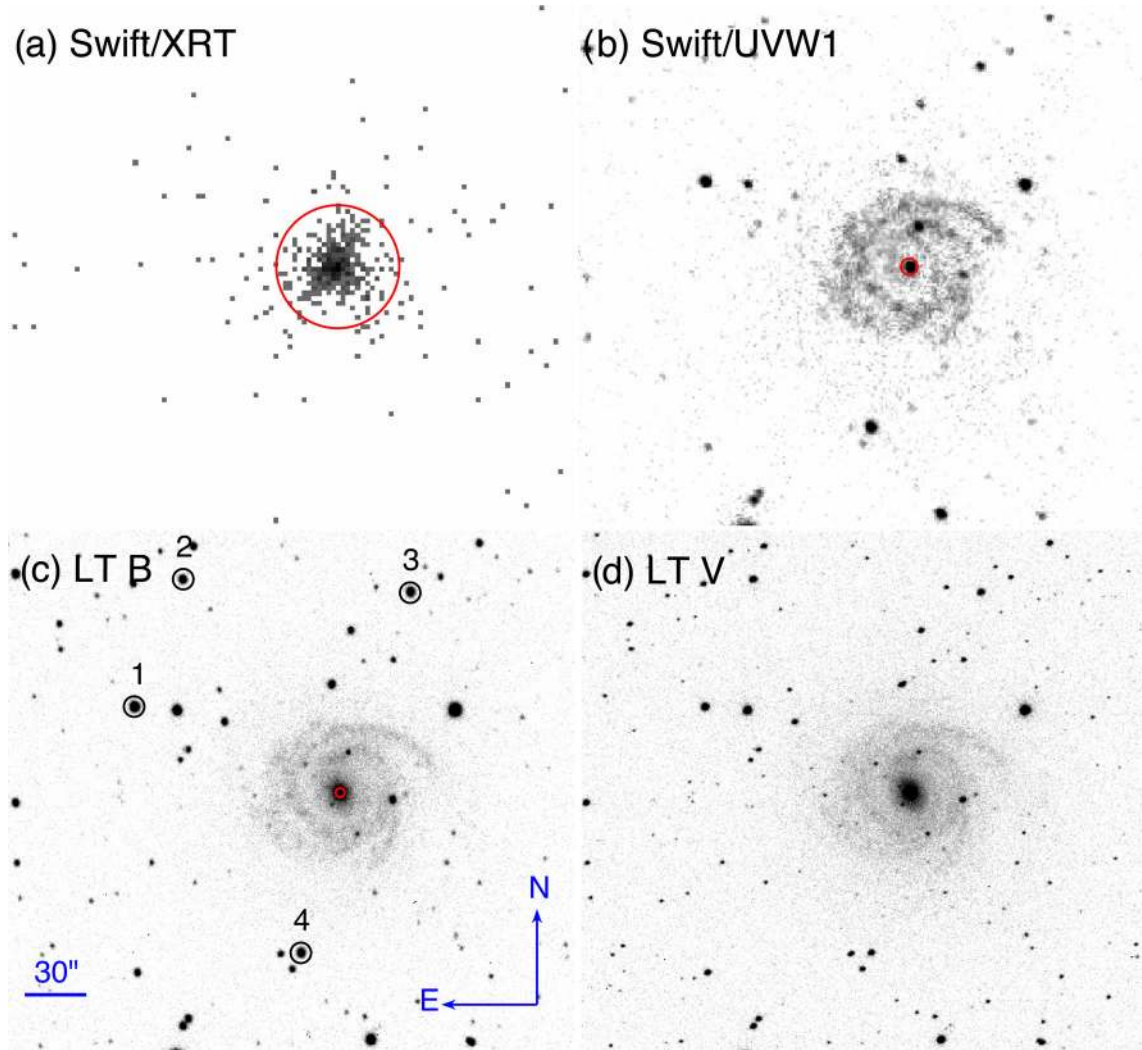
NGC 6814 is a Seyfert 1.5, face-on spiral galaxy with a Hubble classification of SBc and is located at  $\alpha_{2000} = +19$  h 42 m 40.6 s and  $\delta_{2000} = -10$  d 19 m 25 s and  $z = 0.00521$ . We use observed-frame wavelengths and flux densities in our analysis.

We used *Swift* (Gehrels et al. 2004) to monitor NGC 6814 in the X-ray and UV bands. The campaign took place over a three-month period in 2012 resulting in 75 observations. We also obtained optical images using the Liverpool Telescope (*LT*) (Steele et al. 2004) located on the island of La Palma in the Canary Islands at the Observatorio del Roque de los Muchachos. Representative images in each bandpass are shown in Fig. 1.

### 2.1 Swift monitoring

NGC 6814 was monitored by *Swift* for a three-month period from 2012 June 8, until 2012 September 12. All dates here and throughout are in UT. The length of the campaign and daily monitoring were selected to overlap with the concurrent STARE campaign on NGC 6814. Nearly daily observations of 1 ks were made with the XRT instrument (Burrows et al. 2005) in the 0.3–10 keV energy range and UVOT instrument (Poole et al. 2008), utilizing the UVW1 (UV) filter, with central  $\lambda = 2600$  Å and full width at half-maximum (FWHM) of 693 Å. The top two panels of Fig. 2 show the *Swift* X-ray and UVW1 light curves. Note that *Swift* did also obtain  $V$ -band images during the monitoring, however, the photometric accuracy is significantly lower than the *LT* data, and the shape of the light curve was poorly constrained. We do not consider the *Swift*  $V$ -band data further.

<sup>1</sup> <http://www.astro.gsu.edu/STARE/>



**Figure 1.** Representative images of NGC 6814 in each waveband. (a) *Swift*/XRT image when the X-ray light-curve peaks, ObsID=00032477003, MJD 56081, with a 954 s exposure time. For this observation, the count rate is  $0.71 \text{ counts s}^{-1}$ , corresponding to a 30 arcsec source extraction region shown in the figure. (b) *Swift*/UVW1 image, overlaid with the 4 arcsec source extraction region used in all the observations. This image is from ObsID=00032477024, MJD 56105, with a 663 s exposure time. (c) *LT/B*-band image from MJD 56092. Black numbered circles mark the four comparison stars used in the aperture differential photometry and the red circle indicates the 2.2 arcsec extraction region used on the AGN. The extraction region and comparison stars are common to all the *LT* observations. (d) *LT/V*-band image from MJD 56129.

### 2.1.1 *Swift* X-ray data

We reduce the *Swift* X-ray data using the online Build *Swift* XRT Products tool<sup>2</sup> developed by the UK *Swift* Science Center and described in detail in Evans et al. (2007, 2009). A brief overview of the data reduction follows. We use the X-ray (0.3–10 keV) data taken in photon counting (PC) mode. The background is calculated from an annular region around the source, and this background level is used to identify any sources detected above a  $3\sigma$  minimum. The size of the source extraction region is selected based on the background subtracted count rate of the source, with a larger source extraction region used when the source is brighter. The image shown in Fig. 1 panel (a) is the peak of the X-ray light curve. The count rate for this observation is  $0.71 \text{ counts s}^{-1}$  with a corresponding source extraction region of 30 arcsec.

We convert from the XRT count rate to flux by assuming an absorbed power law model using the best-fitting parameters from Walton et al. (2013), where they fit the broad-band (0.5–50 keV) *Suzaku* X-ray spectrum of NGC 6814. Using this model as an input, we obtain a flux conversion factor for the 0.3–10 keV band from WebPIMMS<sup>3</sup> of  $1 \text{ cps} = 5.0 \times 10^{-11} \text{ erg cm}^{-2} \text{ s}^{-1}$ , where cps is counts per second.

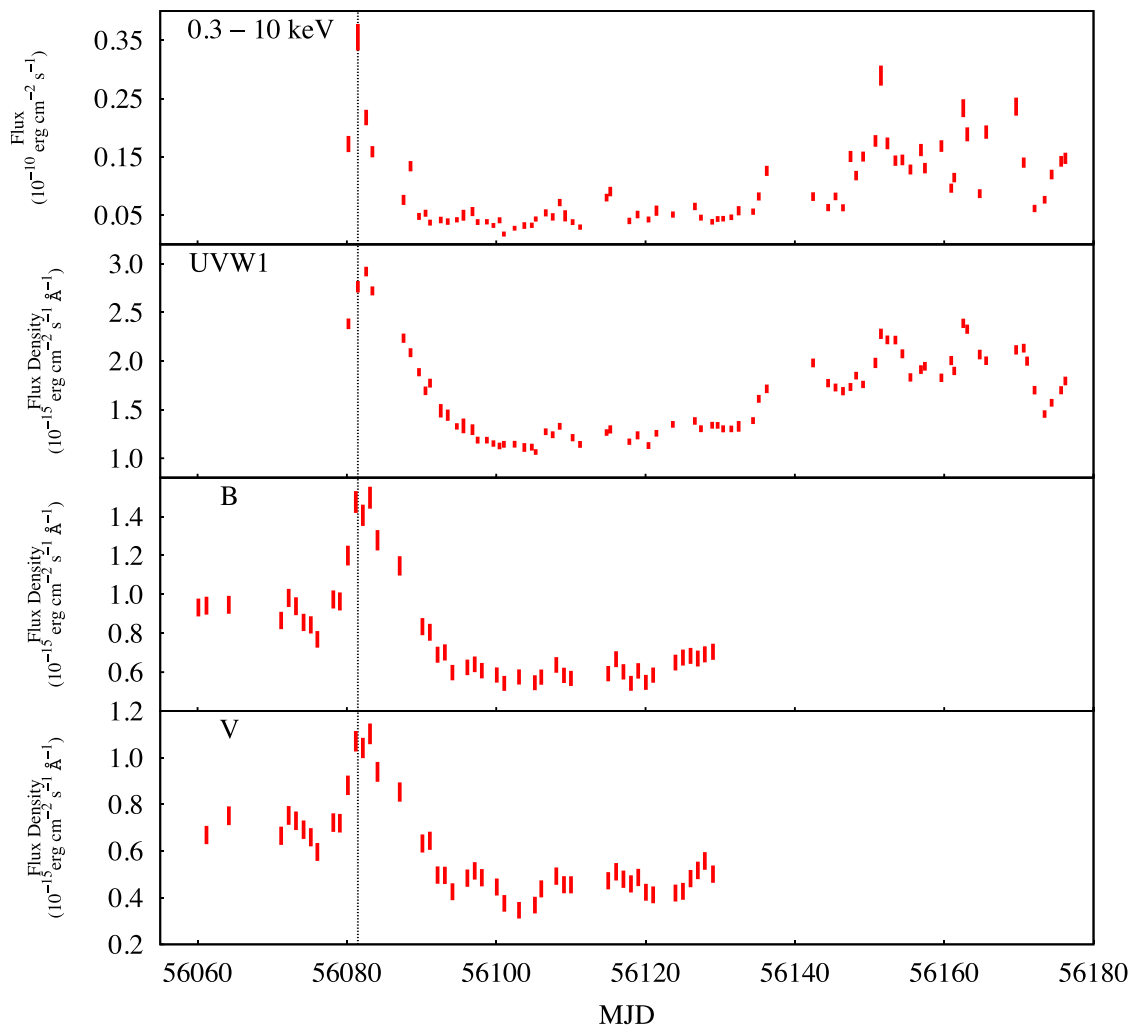
### 2.1.2 *Swift* UV data

We reduce the *Swift* UVW1 data using NASA's HEASOFT<sup>4</sup> data analysis package. We process the *Swift* UVOT image files with the uvotbadpix command to flag bad or damaged pixels. Exposure map images are created, the most recent *Swift* UVOT calibration

<sup>2</sup> [http://www.swift.ac.uk/user\\_objects](http://www.swift.ac.uk/user_objects)

<sup>3</sup> <https://heasarc.gsfc.nasa.gov/cgi-bin/Tools/w3pimms/w3pimms.pl>

<sup>4</sup> <http://heasarc.gsfc.nasa.gov/docs/software/heasoft/>



**Figure 2.** NGC 6814 light curves: the top two panels show the X-ray flux and UV-flux density. The bottom two panels are the host galaxy subtracted *B*-band and *V*-band flux densities. The vertical dotted line indicates the time of the X-ray flux peak. Visual inspection shows that the strong peak in the continuum (X-ray) band is echoed in all the response bands. Additionally, the decline from the peak in the response band light curves is clearly stretched with respect to the continuum, lending further support to the thermal reprocessing scenario.

is applied and images are converted to sky coordinates using the `uvotexpmap` command. Each *Swift* observation is often split into several shorter exposures; thus, we add the various image files for each observation using the `uvotimsum` command. By using the exposure map associated with each observation, all the images can be correctly oriented and summed, producing the deepest possible image. We then use the `uvotdetect` command to locate any source above the detection threshold in the image. The following parameters are used: `threshold = 3` and `chatter = 5`. Searching for sources within 0.001 deg in both RA and Dec. of the known AGN location, we identify the exact location of the AGN. We perform aperture photometry on the AGN via the `uvotsource` command using the `uvotdetect` source position. We take the source extraction region as a circle centred on the AGN, with a radius of 4 arcsec. This region is shown in Fig. 1, panel (b). We estimate the background rate from an annular region around the AGN with an inner radius of 6 arcsec and an outer radius of 9 arcsec. We use the following parameters: `sigma = 3`, `chatter = 1`, `apertcorr = CURVEOFGROWTH`. We perform the same procedure for all *Swift* observations in order to

create a light curve. Flux conversion for *UVW1* (Poole et al. 2008) is  $1 \text{ cps} = 4.3 \times 10^{-16} \text{ erg cm}^{-2} \text{ s}^{-1} \text{ \AA}^{-1}$ .

## 2.2 *LT* observations

NGC 6814 was monitored by the *LT* from 2012 May 12–July 20. The observations used the RATCam instrument, operated with  $2 \times 2$  pixel binning, which leads to a pixel scale of 0.277 arcsec per binned pixel, and  $1024 \times 1024$  pixel images. Observations were taken in pairs of exposures for each of the two filters used, *Bessel B* and *Bessel V*, on a nearly daily basis. A total of 92 pairs were taken over the roughly two-month campaign. Apart from the first five exposures which were single exposures, 45 s in length, the remaining pairs of exposures were  $60 \text{ s}^{-1}$  exposure (120 s total).

### 2.2.1 Aperture photometry

We perform aperture photometry on the AGN and comparison stars using a circular aperture with an 2.2 arcsec (8 pixel) radius, shown

in Fig. 1, panel (c). The aperture size is based on the seeing values. The mean seeing (FWHM) during the observations is 1.45 arcsec (5.2 pixels), with 90 per cent of the observations having seeing FWHM less than the aperture. The sky background is determined from the mode of values within an annulus with inner and outer radii of 4.2 arcsec (15 pixels) and 5.5 arcsec (20 pixels), respectively. The data are typically obtained as a pair of exposures taken sequentially. Thus, to maximize the signal-to-noise ratio we average the count rates between pairs of exposures.

We choose four comparison stars of comparable brightness to NGC 6814, shown in Fig. 1, panel (c). We perform differential photometry by calculating the average scale factor for each observation for the four comparison stars, assuming that they remain constant over time. We then apply this scale factor to NGC 6814 to recover the AGN light curve. We get standard deviations of 0.3, 0.7, 0.7 and 0.5 per cent for the four comparison star light curves in the *B* band, and 0.4, 0.3, 0.6 and 0.8 per cent in the *V* band. We find that the AGN light curve has a standard deviation of 11 per cent in the *B* band and 6 per cent in the *V* band, indicating significant variability.

A lower limit to the fractional uncertainty on the AGN count rates is 0.8 per cent from the highest standard deviation of the comparison stars. As another estimate of uncertainties in the AGN count rates, we look at the difference in rate between observations that are 1 d apart. We find the median difference to be 1.9 per cent for the *B* band, and 1.1 per cent for the *V* band, and we adopt these as the fractional uncertainties. This gives an upper limit on the uncertainty, since there will likely be some real variability on this time-scale.

We convert from relative rates to flux by obtaining the *B*- and *V*-band magnitude of the brightest comparison star, Star 1 shown in Fig. 1, panel (c), by using *HST* photometry from data in Bentz et al. (2013) to calibrate the *V*-band photometry of our image. This yields a Star 1 mag of 14.4 in the *V*-band, which differs slightly from the SIMBAD value of 14.2. As a check, we verified that this method recovers the published magnitudes of reference stars in Doroshenko et al. (2005). For the *B* band, where *HST* photometric calibration was unavailable, we used Doroshenko et al. (2005) stars to calibrate our *B*-band image, yielding a Star 1 mag of 15.1, which is in agreement with the the SIMBAD value. We used the zero-points for Vega fluxes from Colina, Bohlin & Castelli (1996).

### 2.2.2 Host Galaxy flux

In order to accurately quantify the AGN variability and flux obtained from the aperture photometry, we carry out subtraction of host galaxy light in the visual bands using methods detailed in Bentz et al. (2006, 2009a). Using an *HST* image of NGC 6814 (WFC3, *F547M* filter), with the AGN PSF and the sky subtracted (Bentz et al. 2013), we duplicate the circular aperture and its background annulus (which would include some host galaxy light) and measure the amount of host flux. In the *F547M* filter, the host galaxy flux is  $2.7 \times 10^{-15} \text{ erg s}^{-1} \text{ cm}^{-2} \text{ \AA}^{-1}$ . Assuming a typical bulge template (Kinney et al. 1996), and using *SYNPHOT*<sup>5</sup> to carry out synthetic photometry, we estimate a *B*-band host galaxy contribution of  $1.5 \times 10^{-15} \text{ erg s}^{-1} \text{ cm}^{-2} \text{ \AA}^{-1}$  and a *V*-band host galaxy contribution of  $2.6 \times 10^{-15} \text{ erg s}^{-1} \text{ cm}^{-2} \text{ \AA}^{-1}$ .

<sup>5</sup> [http://www.stsci.edu/institute/software\\_hardware/stsdas/synphot](http://www.stsci.edu/institute/software_hardware/stsdas/synphot)

### 2.2.3 Difference imaging photometry

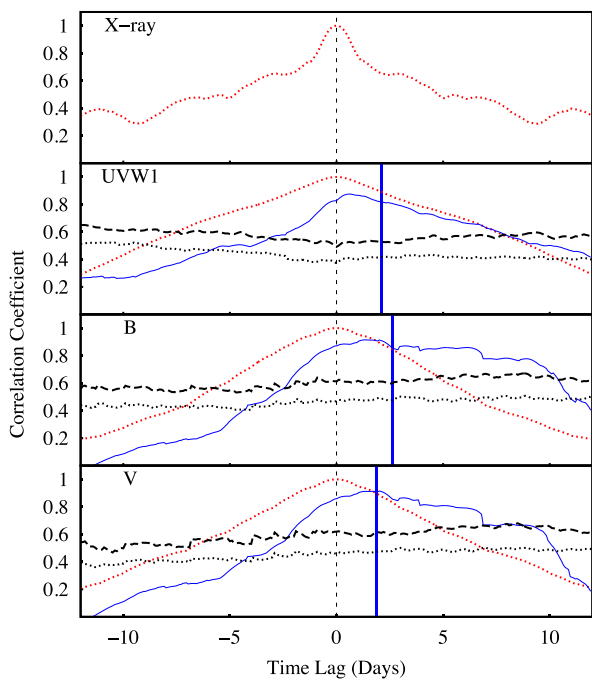
For comparison with the aperture photometry, we also derive the *B*- and *V*-band light curves by registering each set of images to a common alignment using *SEXTERP* (Sivert et al. 2012), and then applying the image subtraction software package *ISIS* (Alard & Lupton 1998; Alard 2000). *ISIS* builds a reference frame from the images that have been defined by the user to have the best seeing and lowest background levels. This reference frame is then convolved with a spatially variable kernel to match the point spread function of each individual image in the set. Subtraction of the frame from the convolved reference image results in a residual image where the only sources are regions of variable flux. The light curve is then derived from aperture photometry that is carried out on these residual images. All contributions from constant-flux components, such as an AGN host galaxy, are thus naturally removed.

To convert the image subtraction light curves from units of residual counts to calibrated fluxes, it is necessary to know the magnitude of the source in the reference frame. We determine this by modelling the *B*- and *V*-band reference frames with *GALFIT* (Peng et al. 2002, 2010). We first build a model point spread function for each frame by fitting three Gaussians to a non-saturated and well-isolated field star. We model the entire frame in each band with the host galaxy geometric parameters held fixed to the values determined from a high-resolution *HST* image by Bentz et al. (2013), but scaled to the appropriate plate scale. This method results in a clean subtraction of the main host galaxy features and allows us to accurately separate the host galaxy flux from the AGN flux in the reference images. By including a field star with known magnitudes in the modelling, we are able to simultaneously solve for the photometric solution in each bandpass. Once we determine the reference AGN flux in each band, we then convert the light curves from residual counts to calibrated fluxes.

We found that the fluxes derived from difference imaging are in excellent agreement with the host galaxy subtracted aperture photometry results. We therefore use the aperture photometry results throughout the rest of the analysis.

## 3 DATA ANALYSIS

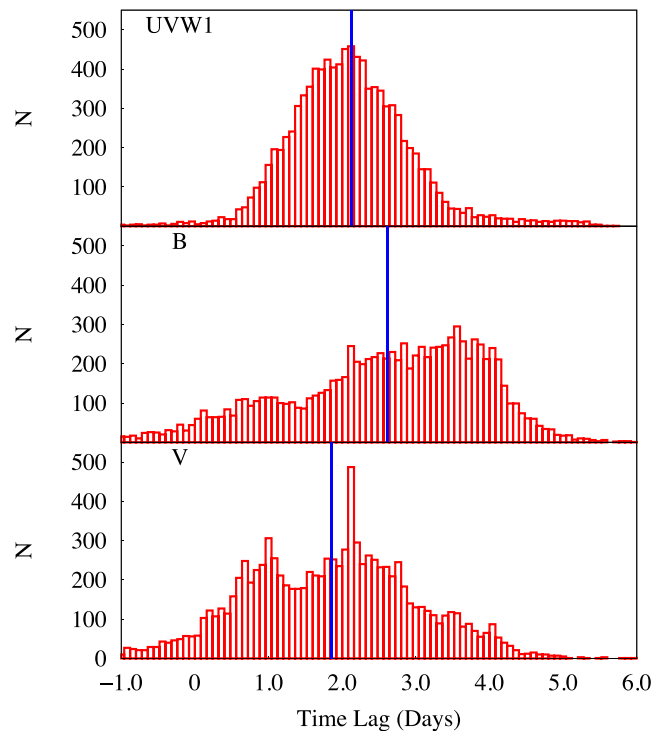
The time lags between wavebands are quantified by using the cross-correlation function (CCF) as described in White & Peterson (1994). We calculate three CCF( $\tau$ ), one for each of the response bands: UV, *B* band and *V* band. For each CCF( $\tau$ ), we take the X-ray light curve to be the driving light curve and set the UV, *B*- and *V*-band light curves as the responding light curve. For each CCF calculation, we interpolate the two light curves in order to obtain regular sampling. In this fashion, the CCF values are computed twice. The first by interpolating the continuum light curve so as to pair up all the continuum data points with the data points of the responding light curve. The second CCF value is computed in the same way, except the responding light curve is interpolated as to pair up with the continuum light curve. The two CCF values are then averaged at each time, yielding CCF( $\tau$ ). To avoid needing to extrapolate the light-curve data, the CCF sum is restricted to the intersection of the time intervals covered by the driving light curve and the shifted echo (response) light curve. For our data, the centroid is calculated using points above 80 per cent of the maximum value. The CCF( $\tau$ ) plots are shown in Fig. 3. Additionally, we computed the autocorrelation function (ACF) for each light curve. The FWHM values for the ACFs are 4.7 d for X-ray, 9.1 d for UV, 6.4 d for *B* band and 6.8 d for *V* band. The ACFs are also shown in Fig. 3.



**Figure 3.** The ACF of the X-ray light curve is shown in the top panel. In the lower panels, the CCFs of each band with respect to the X-ray light curve and ACFs are shown in increasing wavelength order. Blue solid lines show the CCFs while the red dotted lines show the ACF of each band. The centroid of the lags is shown by the vertical solid blue lines. The centroid values are listed in Table 1. The 95 and 99 per cent confidence limits in the CCF values are shown as black dotted and dashed lines respectively.

To determine confidence limits on the significance of the CCF values, we follow the method of Breedt et al. (2009). We simulate an X-ray light curve 10 times the length of the observing campaign using the algorithm of Timmer & Koenig (1995). We assume a power-density spectrum with slope of  $-1$  breaking to a slope of  $-2$  at frequencies above the characteristic break frequency. We determine the break frequency by assuming its scales with mass and Eddington fraction, following McHardy et al. (2006), and assuming the black hole mass from Pancoast et al. (2014) and Eddington fraction of 0.01. We sample the simulated X-ray light curve at the same time intervals as the real *Swift* light curve, and add random Gaussian noise based on the fractional uncertainties of the real data. We then calculate the CCF between the simulated X-ray light curve and the UVW1, B- and V-band light curves in turn. We perform this 1000 times and use the distribution of CCF values at each lag to determine the 95–99 per cent confidence levels, shown as dotted and dashed lines in Fig. 3. The observed CCFs all peak above the 99 per cent level, showing that the correlations are highly significant.

In order to quantify the uncertainty of our time lags, we use Monte Carlo and Bootstrap techniques to resample and randomize the data points on each light curve. See Peterson et al. (1998) for a discussion of CCF uncertainties. For each point, we add random Gaussian noise based on the uncertainty associated with the count rate measurement for that point. We then randomly resample the data (Bootstrap) with the temporal ordering intact, but allow for the possibility of sampling a particular data point more than once while keeping the same number of elements of the data set i.e. some points were excluded. We repeat the random resampling and compute the CCF( $\tau$ ) for each. This is done for 10000 realizations, allowing us to build a histogram of the centroid of the CCFs, which we show in



**Figure 4.** The histogram of lag centroids for each band. The light-curve data were randomly resampled and the CCFs computed for 10000 realizations. This Monte Carlo method allows us to estimate the uncertainty in the lag calculation (Peterson et al. 1998).

**Table 1.** Time lags.

Response band	Time lag (days)
UV (2600 Å)	$2.1 \pm 0.7$
B (4400 Å)	$2.6^{+1.3}_{-1.5}$
V (5500 Å)	$1.9^{+1.1}_{-1.2}$

Fig. 4. We take the mean of the distribution of centroids as the lag value ( $\tau$ ). The uncertainty in the lag is taken at the  $1\sigma$  value of the distribution. The values of time lags associated with UVW1, B- and V-band light curves are shown in Table 1. These data show the time delay between the X-ray and longer wavelength light curves.

### 3.1 Cross-correlation lag results

In order to conduct accurate analysis of the time lags of the response bands, several factors are needed. First, the dense monitoring campaign we undertook gave us the well-sampled data quality required to limit the uncertainties associated with the time delay. Second, the intrinsic variability of the source light curve, and the corresponding correlated response must also exist. This allows for the computation of the CCF( $\tau$ ) and the time lag. Indeed, the greater the variability, the more accurately we can compute the CCF( $\tau$ ). One measure of the intrinsic variability is the fractional root mean square variability amplitude or  $F_{\text{var}}$  which is described in Vaughan et al. (2003). This statistic is computed by subtracting the variance in the individual count rate measurement errors from the variance of the count rates themselves. This difference is called the excess variance.

$F_{\text{var}}$  is the normalized expression of the excess variance. The errors in  $F_{\text{var}}$  are computed assuming errors only due to Poisson noise. See Appendix B of Vaughan et al. (2003) for a discussion.

**Table 2.** Fractional variability.

Band	$F_{\text{var}}$
X-ray (8.3 Å)	0.70±0.01
UV (2600 Å)	0.267±0.002
B (4400 Å)	0.323±0.008
V (5500 Å)	0.320±0.010

Values of  $F_{\text{var}}$  are listed in Table 2 and provide a metric for measuring variability. In the B and V bands, we calculate it using the host galaxy subtracted fluxes.

Visual inspection of the light curves shown in Fig. 2 indicates good correlation of all bands, as is also apparent from the peak values of the CCFs. An initial large peak in the X-ray LC that is echoed in all the responding bands can be seen. Moreover, each of the longer wavelength responding bands shows a broader peak as expected if the continuum is thermally reprocessed – reprocessing on the near-side of the disc will be seen before reprocessing on the far-side of the disc – blurring out the sharp peak seen in X-rays.

Inspection of Fig. 3 reveals a moderately flat CCF( $\tau$ ) for the B band and V band. The large uncertainties in these lags arise from lack of significant overlap of the *Swift* and *LT* data as well as a period of low variability in the flux across all bands shortly after the large rise seen at the beginning of the monitoring period. As a test, we also carried out the lag analysis with only the overlapping portion of the LCs. We found the differences in lag distributions to be negligible.

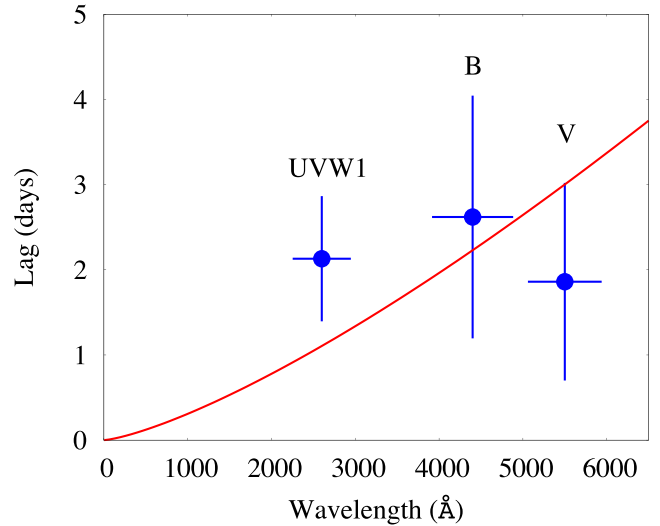
Our data support thermal reprocessing with an X-ray to UV lag of  $2.1^{+0.7}_{-0.7}$  d, an X-ray to B-band lag of  $2.6^{+1.3}_{-1.5}$  d, and an X-ray to V-band lag of  $1.9^{+1.1}_{-1.2}$  d. Thermal reprocessing of the X-ray continuum would result in wavelength-dependent time lags:  $\tau \propto \lambda^{\frac{4}{3}}$  (Collier et al. 1999). For a standard thin disc (Shakura & Sunyaev 1973), the temperature profile is given by (e.g. Collier et al. 1999; Frank, King & Raine 2002; Cackett et al. 2007):

$$T(R) = \left[ \frac{3GM\dot{M}}{8\pi R^3\sigma} + \frac{L_x H_x (1-A)}{4\pi R_x^3\sigma} \right]^{\frac{1}{4}}, \quad (1)$$

where  $G$  is Newton’s universal gravitational constant,  $M$  is the mass of the black hole,  $\dot{M}$  is the mass accretion rate,  $\sigma$  is the Stefan–Boltzmann constant,  $L_x$  is the luminosity of the continuum irradiating source,  $A$  is the disc albedo,  $R_x$  is the distance from the irradiating source to the disc element at distance  $R$  from the black hole, and  $H_x$  is the height of the irradiating continuum source above the disc. The first term in the temperature profile equation is the contribution of the viscous heating of the disc and is valid for  $R \gg R_*$ , where  $R_*$  is the innermost stable orbit of the black hole. The second term is the contribution associated with radiative heating of the disc. In the same regime:  $R \gg R_*$  and when  $R \gg H_x$ , the second term  $\propto R^{-\frac{3}{4}}$ . Overall, this suggests that  $T(R) \propto R^{-\frac{3}{4}}$ . If we assume a Wien’s Displacement Law relationship ( $\lambda \propto T^{-1}$ ) for each disc element a distance  $R$  from the central black hole and considering the previous relationship  $T(R) \propto R^{-\frac{3}{4}}$ , we obtain the relationship  $R^{-\frac{3}{4}} \propto \lambda^{-1}$ . Assuming  $R \simeq c\tau$ , we obtain  $\tau \propto \lambda^{\frac{4}{3}}$ .

In Fig. 5, we plot time lag versus wavelength for the UVW1, B- and V-band wavebands relative to the X-ray band. Additionally, we plot the function:

$$\tau = \tau_0 \left[ \left( \frac{\lambda}{\lambda_0} \right)^{\alpha} - 1 \right], \quad (2)$$



**Figure 5.** Time lags for the UVW1, B- and V-band calculated with respect to the X-ray band as a function of wavelength. The red line is the best-fitting  $\tau \propto \lambda^{4/3}$  relation, showing the data is broadly consistent with thermal reprocessing. The x-error bars indicate the filter bandpass HWHM, so together they show the FWHM.

where  $\lambda_0$  is the wavelength of the driving X-ray band (here, we use a value of  $\lambda_0 = 8.3$  Å),  $\tau_0$  is the continuum reference time, determined by fitting the data, and  $\alpha$  is the characteristic exponent. Fixing,  $\alpha = 4/3$ , the relation fits the data well, but given the large uncertainties in the B- and V-band lags, we cannot better constrain the exact wavelength dependence of the lags.

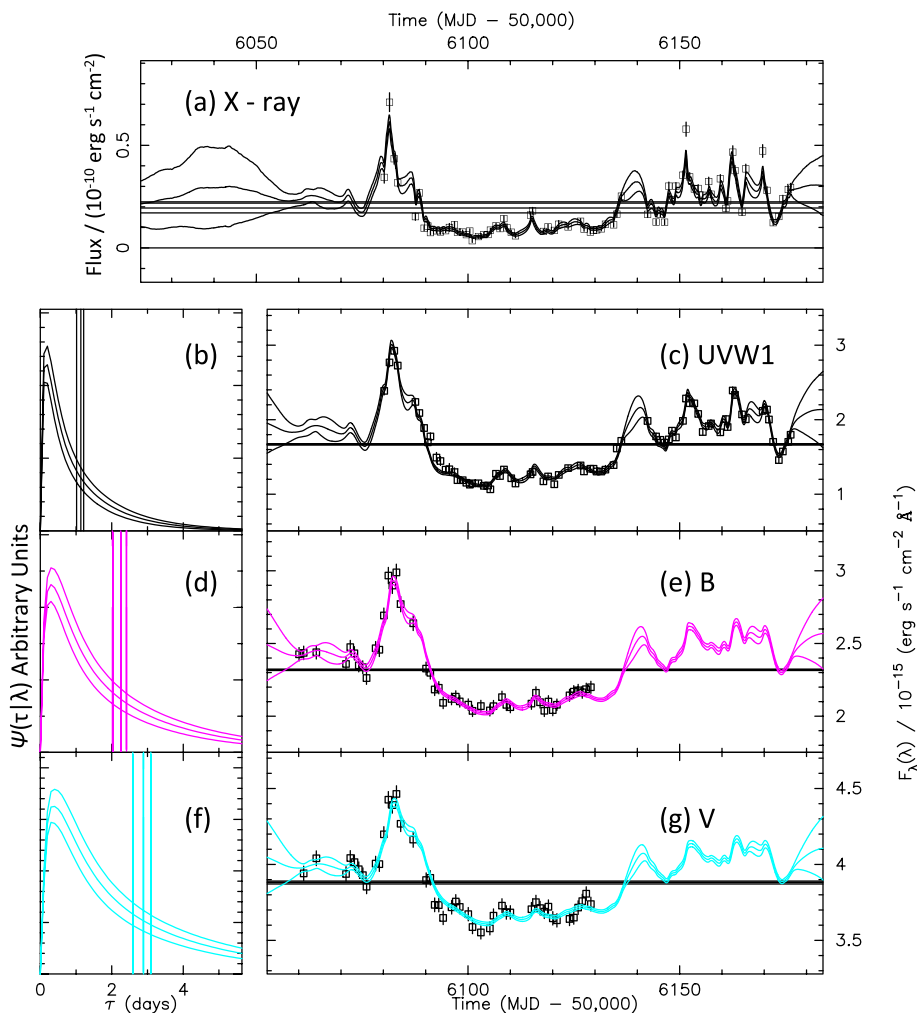
### 3.2 Monte Carlo Accretion Disc Lag distribution analysis

We now perform an additional analysis of the light-curve lags. We use the accretion disc modelling code *CREAM* (Starkey, Horne & Villforth 2015) to fit a lamp-post model (e.g. Collier et al. 1999; Cackett et al. 2007; Chelouche 2013) to the continuum emission; interpreting this as variable blackbody emission from a standard thin disc.

*CREAM* uses MCMC methods to fit a simple irradiated disc model to the observed light curves. The driving (X-ray) light curve is modelled as a Fourier time series in  $\log_{10} F_{\lambda}$ , with a random walk prior on the Fourier amplitudes. Each echo (UV and optical) light curve is modelled as a constant flux plus variations obtained by convolving the driving light curve with the time delay distribution appropriate for a flat steady-state blackbody accretion disc irradiated by a variable point source just above the disc centre.

The MCMC fit samples the joint posterior probability distribution of the model parameters. The parameters of primary interest are  $M\dot{M}$ , which controls the  $T(r)$  profile of the disc, and the disc inclination  $i$ . The  $M\dot{M}$  estimate maps directly on to a mean delay with a theoretical scaling of  $\langle \tau \rangle \propto (M\dot{M})^{1/3} \lambda^{4/3}$  (Collier et al. 1998), independent of  $i$ , and the shape of the delay distribution depends on  $i$ . The model has hundreds of nuisance parameters, including the Fourier amplitudes that define the X-ray light curve, and a mean and rms amplitude and an error bar scale factor for each echo light curve. For further details see Starkey et al. (2015).

While *CREAM* can be used to simultaneously fit both  $M\dot{M}$  and  $i$ , our data are too sparsely sampled with too little overlap between the X-ray and optical light curves to provide a simultaneous fit. To



**Figure 6.** CREAM fit for  $i = 50^\circ$  to the X-ray (a), *UVW1* and *LT* light curves (lower right, panels c, e and g). CREAM assumes the X-ray light curve drives the variability at the longer wavelengths and attempts to infer the disc response function (lower left, panels b, d and f). The vertical lines indicate the mean lag and  $1\sigma$  uncertainty envelope.

remedy this, we fix the inclination and allow the  $M\dot{M}$  parameter to vary. We do this for inclinations 0–50 deg in 10 deg increments. The CREAM fit for the 50 deg case is shown in Fig. 6 with a result of  $\log M\dot{M} = 7.92 \pm 0.11$ , where  $M$  is in units of  $M_\odot$  and  $\dot{M}$  is in  $M_\odot \text{ yr}^{-1}$ . We note from Fig. 7 that lower assumed inclinations result in lower estimates of  $M\dot{M}$ .

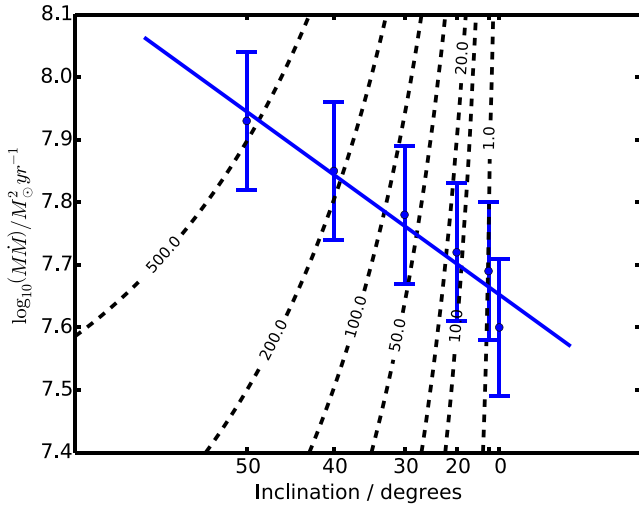
Modelling of the  $H\beta$  emission line in NGC 6814 by Pancoast et al. (2014) has allowed for a mass and inclination to be determined for this object, which, in turn allows us to determine the mass accretion rate implied by our best-fitting model. For  $i = 50^\circ$ , and  $M = 10^{6.42} M_\odot$ , we get  $\dot{M} = 31.6 M_\odot \text{ yr}^{-1}$ , which, assuming an accretion efficiency  $\eta = 0.1$  implies an Eddington fraction of  $L_{\text{bol}}/L_{\text{Edd}} = 546$ . Additionally, standard reverberation analysis gives a black hole mass of  $M_{\text{BH}} = 10^{7.04 \pm 0.06} M_\odot$  (Bentz & Katz 2015), using the weighted virial product of all broad lines from Bentz et al. (2009b) and the  $f$ -factor from Grier et al. (2013). For the updated Bentz et al. (2009b) mass, we get  $\dot{M} = 7.6 M_\odot \text{ yr}^{-1}$ , and an Eddington fraction of  $L_{\text{bol}}/L_{\text{Edd}} = 31.8$ .

### 3.3 Multicomponent spectral decomposition

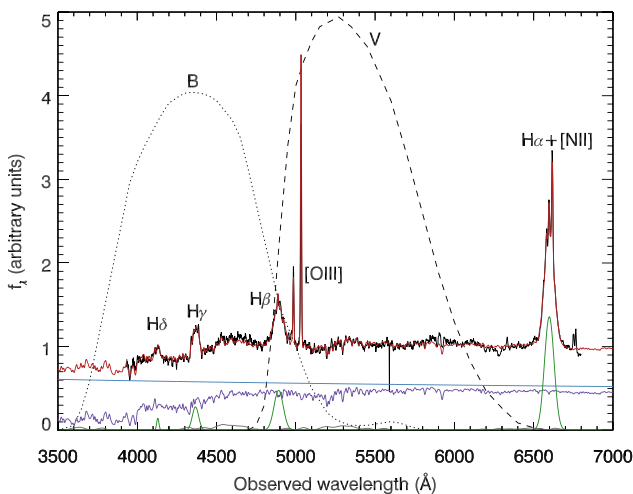
We estimate the contribution of the broad lines to the *B*- and *V*bands through fitting an archival spectrum of NGC 6814. We obtained the 6dF spectrum (Jones et al. 2009) of NGC 6814 from NED.<sup>6</sup> We then follow the spectral decomposition method described in Barth et al. (2013) in order to determine the flux of individual components. We fit the spectrum with a model consisting of a power-law continuum, galaxy stellar template, Fe II template and Gaussians for the broad and narrow emission lines. The model was convolved with a Gaussian to match the spectral resolution of 6dF. We use the Fe II template of Véron-Cetty, Joly & Véron (2004) convolved with a broad Gaussian, assuming it originates in the BLR. The best-fitting Gaussian width for the Fe II complex is consistent with the widths of the broad lines (approximately the same as  $H\gamma$ , but narrower than  $H\alpha$  or  $H\beta$ ). For the galaxy stellar template, we

<sup>6</sup> <https://ned.ipac.caltech.edu/>





**Figure 7.**  $\dot{M}$  parameters with uncertainties plotted versus assumed inclination. Contours show constant Eddington ratios evaluated assuming a black hole mass from Pancoast et al. (2014). To calculate the Eddington luminosity for our inclinations, we assume a disc-like BLR with a black hole mass that decreases towards edge-on inclinations as  $M_{\text{BH}} = M_{\text{BH}}(\frac{\sin 50}{\sin i})^2$ .



**Figure 8.** The 6dF optical spectrum of NGC 6814 (black). Dotted and dashed black lines show the transmission curves for the *LT* *B*- and *V* filters. The best-fitting composite model is shown in red. Also shown is the galactic stellar template (purple), continuum power law (blue) and broad emission lines (green).

use a model from Maraston & Strömbäck (2011) which assumes a stellar population of 11 Gyr, with solar-abundance, a Salpeter IMF and uses the MARCS theoretical stellar library. We fit the model to the data using the non-linear least squares curve fitting package of Markwardt (2009). The spectral fit is shown in Fig. 8.

Once we obtained a good fit, we calculate the fraction of the flux in both the *B*- and *V* bands from each component, weighting the best-fitting spectral model by the transmission curves for each filter. We compare only the power-law continuum flux with the broad line (including Fe II) flux in each filter, since the galaxy and narrow line fluxes will remain constant. We find that broad lines are  $\sim 9$  and 8 per cent of the AGN flux in the *B*- and *V* bands, respectively.

## 4 DISCUSSION

We observed the AGN NGC 6814 for  $\sim 100$  d with *Swift* and 70 d with the *LT*, obtaining X-ray, UV and optical light curves. The light curves are all strongly correlated, with the X-ray light curve showing the sharpest variability features and highest variability amplitude. Cross-correlation analysis shows that the UV and optical bands lag behind the X-ray by approximately 2 d. The lags, variability amplitude and the smoothing of longer wavelength light curves, are all consistent with a scenario where the X-rays irradiate, and are reprocessed in, the accretion disc to drive the UV/optical variability.

To investigate this scenario further, we fit the light curves using *CREAM*, a MCMC code that assumes a standard thin disc irradiated by the X-ray source. This model fits the data well, allowing us to constrain the product  $M\dot{M}$ . Using two different estimates of black hole mass, we calculated mass accretion rates and corresponding Eddington fractions, finding highly super-Eddington fractions. Based on the observed flux from NGC 6814, such highly super-Eddington accretion is clearly not occurring. The average host galaxy subtracted *V*-band flux density is  $\sim 5.9 \times 10^{-16}$  erg  $\text{cm}^{-2} \text{s}^{-1} \text{\AA}^{-1}$ . We use this to estimate the bolometric luminosity of NGC 6814 during our observations. We do this by assuming that the *V*-band flux density is approximately the flux density at 5100Å. We then apply an extinction correction assuming  $E(B - V) = 0.1586$  (the Schlafly & Finkbeiner 2011 corrected value from Schlafly, Finkbeiner & Davis 1998) and the extinction law of Cardelli, Clayton & Mathis (1989). We calculate the luminosity distance assuming a cosmology of  $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ,  $\Omega_M = 0.3$ ,  $\Omega_\Lambda = 0.7$ . We then apply a bolometric correction assuming  $L_{\text{bol}} = 9\lambda L_\lambda(5100\text{\AA})$  (while there are more nuanced bolometric corrections, this is sufficient for our basic estimate here). Doing this gives an estimated  $L_{\text{bol}} = 2.7 \times 10^{42}$  erg  $\text{s}^{-1}$ , which, corresponds to  $L_{\text{bol}}/L_{\text{Edd}} = 0.008$  for the Pancoast et al. (2014) mass, and 0.002 using the updated Bentz et al. (2009b) mass. Since  $\tau \propto \dot{M}^{1/3}$ , decreasing the mass accretion rate by a factor of 546/0.008 or 31.8/0.002 (depending on the mass assumed), would lead to predicted lags a factor of about 40 or 25 smaller, respectively. In other words, for realistic values of mass and mass accretion rate, the observed lags are significantly longer than predicted by the standard thin disc model, and hence, the UV/optical emitting region is further out.

This discrepancy between standard disc model and observed lags is common among AGN where wavelength-dependent lags have been observed. In Cackett et al. (2007), a standard thin disc model was fit to the lags and fluxes of a sample of 14 AGN and used to estimate the distances to those objects. However, the measured distances implied  $H_0 = 44 \pm 5 \text{ km s}^{-1} \text{ Mpc}^{-1}$ , a factor of 1.6 smaller than the generally accepted value. This is a different manifestation of the problem. The model used by Cackett et al. (2007) has  $D \propto \tau \lambda^{-3/2} f_v^{-1/2}$ . Since  $H_0 \propto 1/D$ , the discrepancy with  $H_0$  implies that the observed lags are too large by a factor of 1.6 on average.

More recently, wavelength-dependent lags in NGC 5548 measured from long-term monitoring campaigns in 2013 and 2014 also show that while the lags follow the expected  $\tau \propto \lambda^{4/3}$  dependence, they are also larger than expected given reasonable values for mass and mass accretion rate (McHardy et al. 2014; Edelson et al. 2015; Fausnaugh et al. 2015). For instance, McHardy et al. (2014) have to increase  $M\dot{M}$  by a factor of 3, as well as change other parameters in their model, in order to get good agreement with the lags. Edelson et al. (2015) compare both the wavelength-dependent lags in NGC 5548 and the lags in NGC 2617 measured by Shappee et al. (2014)

with predictions based on reasonable  $\dot{M}$  for those objects, again showing that both exhibit longer lags than expected. In MCG-6-30-15 Lira et al. (2015) also find larger than expected lags, showing that only with an unreasonable increase in X-ray luminosity (a factor of 4 higher) will the measured lags be in good agreement with theory.

McHardy et al. (2014) and Edelson et al. (2015) note that this discrepancy with the standard thin disc model is consistent with the results from gravitational microlensing, which have also found that the UV and optical emitting regions seem to be further out than predicted by the standard thin disc model (see Mosquera et al. 2013; Blackburne et al. 2015, and references therein). One possible explanation for this difference is that the accretion disc is inhomogeneous, with many different zones whose temperatures vary independently (Dexter & Agol 2011). In this model, the global time-averaged properties of the disc follow the standard thin disc temperature profile; however, instabilities in the disc can lead to local zones whose temperature varies. With a large enough number of zones and amplitude of temperature fluctuations, the half-light radius of the disc increases enough to match the observed microlensing results. This is just one of several scenarios discussed in the literature, and we refer the reader to other detailed discussions on this discrepancy (see Cackett et al. 2007; Dexter & Agol 2011; McHardy et al. 2014; Edelson et al. 2015; Lira et al. 2015; Fausnaugh et al. 2015, and references therein for detailed discussions).

The lags in NGC 5548 are the best constrained for any source thus far, so provide an interesting comparison to our results on NGC 6814. From the standard thin disc model, we would expect lags to scale like  $(\dot{M})^{1/3}$ . The mass and mass accretion rate for NGC 6814 are both estimated to be smaller than for NGC 5548. Using the Bentz et al. (2009b) and Pancoast et al. (2014) masses and the estimated mass accretion rates given above, we would expect the lags in NGC 6814 to be about a factor of 10–17 smaller than NGC 5548; yet, the lags are comparable between the two sources. The reason for the difference is not clear, and our interpretation is limited by the fact that the *B*- and *V*-band lags are not well constrained in NGC 6814. Future monitoring utilizing more wavebands and achieving better constrained lags could help understand the differences.

Since the lags are measured using broad-band photometric filters, broad emission lines falling within the filter can increase the measured lag (Chelouche 2013; Chelouche & Zucker 2013). We can do a simple estimate of this for NGC 6814 by considering the broad line contamination. If we assume 1.5 d continuum lag, and a BLR lag of 7 d (the  $H\beta$  lag for NGC 6814 is approximately this value; Bentz et al. 2009b), with 9 per cent of the flux originating in the BLR implies an observed lag of:  $\tau = 0.91 \times 1.5 \text{ d} + 0.09 \times 7 \text{ d} = 2.0 \text{ d}$ . Hence, the contribution from broad emission lines may increase the observed lag by 0.5 d, and the lags in *B* and *V* could be 25 per cent smaller than measured (though note that this is smaller than the size of the uncertainties in the lags). In addition to contamination from broad emission lines, diffuse continuum emission from broad-line clouds can also contaminate the lags. Korista & Goad (2001) show that reflected and thermal diffuse continuum can broadly mimic the  $\tau \propto \lambda^{4/3}$  dependence, and may account for about one-third of the lag between 1350 and 5100 Å. UV and optical Fe II pseudo-continuum emission from BLR clouds or an intermediate region between the accretion disc, and the BLR may also contribute (Edelson et al. 2015). Future spectroscopic measurements of wavelength-dependent lags to avoid BLR contamination in AGN will produce more accurately constrained continuum lags and help us further understand the structure of the accretion disc.

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