



# Coulomb blockade phenomena observed in supported metallic nanoislands

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The electron transport properties of single crystalline metallic nanostructures in the Coulomb blockade (CB) regime have been investigated by low-temperature scanning tunneling spectroscopy. To this end, nanoscale flat-top Pb islands with well-defined geometries are grown on NaCl-covered Ag(111) substrates. The tunneling spectra acquired at 4.6 K on the Pb nanoislands reflect the presence of single electron tunneling processes across the double-barrier tunnel junction (DBTJ). By a controlled change of the tip-island tunnel distance, the spectra display the characteristic evolution from CB to Coulomb staircase (CS) regime. Simulations within the semi-classical orthodox theory allow us to extract quantitatively the parameters characterizing the DBTJ, i.e., the resistances, capacitances, and the residual charge  $Q_0$ . Manipulation of  $Q_0$  is achieved by controlled application of voltage pulses on the Pb islands. Moreover, under specific tunneling conditions, the influence of the tip-island junction on  $Q_0$  is revealed in topographic images of the Pb islands.

**Keywords:** coulomb blockade, STM, STS, Pb-nanoislands, dielectric support

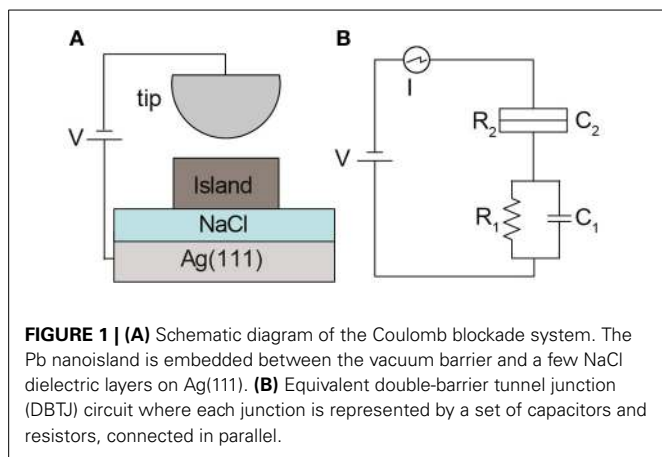
## 1. INTRODUCTION

The study of Coulomb blockade (CB) phenomena in nanostructures is a very attractive area of condensed matter physics, because single electron electronics is considered to have a high potential for basic research and for technological applications (1–5). The field started more than 40 years ago with the investigation of small metal particles embedded in an oxide layer between two planar metal electrodes (6, 7). Subsequently, in order to avoid ensemble effects and to study single double-barrier tunnel junctions (DBTJ), CB phenomena have been investigated in small-area tunnel junctions prepared by lithographic methods developed for microelectronics (8, 9). More recently, junctions using a scanning tunneling microscope (STM) tip as one adjustable electrode came into the focus of research (10–13).

Consider single electron transport in the system shown in **Figure 1**: the two barriers constitute a DBTJ. For each junction the barriers are modeled by an ohmic resistor  $R_i$  in parallel with a capacitor  $C_i$ ,  $i = 1$  for the substrate-island junction and  $i = 2$  for the island-tip junction, as shown in the equivalent electronic circuit in **Figure 1B**. In order to transfer a single electron through the DBTJ, the electron must overcome the Coulomb charging energy  $E_c = e^2/C_\Sigma$ , where  $C_\Sigma = \sum C_i$ . If the charging energy  $E_c$  is much larger than the thermal energy  $k_B T$ , the tunneling of an electron is blocked for bias voltages smaller than  $U_c = e/C_\Sigma$ . This phenomenon has been termed CB (CB) (2, 3, 14–16). Moreover, in order to keep charge fluctuations sufficiently small, the coupling resistance of each junction has to be significantly larger than the quantum resistance:  $R_i \gg R_Q = h/(2e^2) \approx 12.9 \text{ k}\Omega$ . These

conditions imply that extremely small metal clusters have to be probed, or that the measurements have to be performed at low temperature.

Previous studies of nanostructures in the CB regime by STM were performed on amorphous particles (11, 13, 17, 18), on particles covered by shells consisting of specific ligands and/or molecules (19–22), and to a lesser extent on supported clusters and metal islands (18, 23–26). The vast majority of the CB spectroscopy results have been successfully described within the orthodox theory of the DBTJ (2), which allowed the authors to determine quantitatively the tip-particle and the particle-substrate junction parameters (see **Figure 1B**). Within the context of single electron tunneling, the “orthodox theory,” a semi-classical theory, is based on the following three assumptions (3). (1) The electron energy quantization inside the conductors is ignored, i.e., the electron energy spectrum is continuous. (2) Coherent quantum processes consisting of several simultaneous tunneling events (“cotunneling”) are ignored. This assumption is valid if the resistance of all tunneling barriers of the system is much higher than the quantum unit of resistance. Only under this condition the quantum-mechanical uncertainty of electrons is suppressed because of the high tunneling resistance (i.e., less tunneling events). Thus one can neglect the concurrent tunneling events and treat one electron at a time, which makes controllable single-electron manipulation possible. (3) The tunneling time  $\tau_t$  of an electron tunneling through the barrier is assumed to be negligible compared to other time scales (including the interval between subsequent tunneling events). For a typical tunneling event in a practical junction (3),  $\tau_t$  is around  $10^{-15}$  s. For



a typical STM tunneling junction with 1 nA tunneling current, on average one electron tunnels per  $10^{-10}$  s. Considering that the electronic lifetime of an electron in the states of the islands is around  $10^{-13}$ – $10^{-15}$  s, electrons tunnel one at a time and consequently under these conditions cotunneling processes can be neglected.

Recently, in a low-temperature scanning tunneling spectroscopy (STS) study, we reported (27) on the observation of the dynamical Coulomb blockade (DCB) (28–30) in nanosized electrical contacts consisting of small Pb islands on various conducting, semiconducting, and partially insulating substrates. We observed a suppression of the differential tunnel conductance at small bias voltages due to DCB effects. The differential conductance spectra allowed us to determine the capacitances and resistances of the electrical contact which depend systematically on the island-substrate contact area. Calculations based on the theory of environmentally assisted tunneling agree well with the measurements.

Here, we extend the previous observations from the DCB to the orthodox CB and Coulomb staircase (CS) regime. We report on the observation of CB phenomena in Pb nanoislands, ranging from a lateral size of a few nanometers to tens of nanometers and a thickness of a few monolayers, grown on ultrathin dielectric films of NaCl deposited on Ag(111). For selected Pb islands of well-defined area, the local tunneling spectra reflect CB and CS phenomena in the DBTJ (see **Figure 1**) characteristic for single electron tunneling: Every additional electron tunneling to or from the Pb nanoisland is counted one by one. Using a model based on the orthodox theory of single electron tunneling (12, 16), we are able to simulate the experimental tunneling spectra and to extract the relevant parameters of the DBTJ, i.e., the resistances of island-substrate and tip-island junctions ( $R_1$  and  $R_2$ ), the capacitances of island-substrate and tip-island junctions ( $C_1$  and  $C_2$ ), and the residual charge ( $Q_0$ ) on the island. The extracted  $C_1$  capacitances fit well with the values corresponding to a planar capacitor,  $C_1 = \epsilon_0 \epsilon_r A_{\text{island}}/d$ , the island area  $A_{\text{island}}$  being measured from the STM topography and the insulator thickness determined by field emission resonances (FERs) analysis. Manipulation of  $Q_0$  is achieved by controlled application of voltage pulses on the Pb islands. Moreover, under specific tunneling conditions, the

influence of the adjustable tip-island junction on  $Q_0$  is revealed in topographic images of the Pb islands.

In an STM measurement of a DBTJ, in general the tip-island junction resistance  $R_2$  is always much larger than the quantum resistance  $R_Q$ . Then the electron transport through such a DBTJ can be separated into three different regimes (16): if the island-substrate resistance  $R_1 \ll R_Q$ , the whole system corresponds to a single junction; if  $R_1$  is of the order of  $R_Q$ , the dynamical Coulomb blockade (DCB) regime is reached; if  $R_1 \gg R_Q$ , the CB and CS regime is entered. These different conditions can be selectively and controllably fulfilled in our experimental setup by choosing the appropriate size of the islands (by changing the growth parameters) and the pertinent tunnel parameters, including an adjustable tip-island distance (by changing the tip-island resistance  $R_2$ ). In this way island-size-dependent CB gaps and CS have been unambiguously identified in the tunneling spectra obtained on the Pb quantum dots on NaCl/Ag(111).

## 2. EXPERIMENTAL

The Ag(111) single crystal substrate was cleaned by  $\text{Ar}^+$  sputtering and subsequent annealing cycles. NaCl powder was thermally evaporated from a crucible at a temperature of  $T = 620^\circ\text{C}$  onto the Ag substrate held at room temperature or heated to  $\approx 420$  K. Subsequently, Pb islands were grown by evaporation of Pb from a W filament onto the NaCl-covered Ag substrate cooled to 130 K to obtain Pb islands of the desired size.

The experiments were conducted in a homebuilt STM operated at 4.6 K (31). Differential conductance ( $dI/dV$ ) measurements were performed with an open feedback loop using a lock-in technique with modulation voltage from 2 to 10 mV<sub>pp</sub> at 300–400 Hz frequency with tunneling current ranging from 100 pA to a few nA.

## 3. RESULTS AND DISCUSSION

### 3.1. GROWTH OF Pb NANOISLANDS ON NaCl/Ag(111)

A bulk NaCl crystal is a dielectric material with a wide band gap in the range of 8.5 – 9 eV (32–34). For thin NaCl films, the band gap is reported to be close to the bulk value (35) For 1 – 3 ML of NaCl on Ag(100), recent STS measurements of the energy positions of field emission resonances propose a work function of 3.2 eV (36), while ultraviolet photoemission spectroscopy (UPS) yields 3.5 eV (36, 37). From  $dI/dV$  spectra measured on top of a 2 ML NaCl film, we deduce that the gap lies within the voltage range of  $\pm 2$  eV around  $E_F$ , which is the energy range selected for the measurement of the  $dI/dV$  spectra of the Pb nanoislands on NaCl.

Studies of NaCl layers on other substrates abound, e.g., on Al(111) (35, 38), on Cu(111) (39), on Ag(100) (36, 40, 41), and on Au(111) (42–44). NaCl(100) layers are very versatile as a dielectric ultrathin film for the electronic decoupling of supported molecules (39, 42, 43) or other nanostructures (27) from a metallic substrate.

Here, NaCl was deposited on the substrate held at two different temperatures, 300 K, and  $\approx 420$  K, the latter favoring the formation of more extended, flatter, and defect-free layers. **Figures 2A,B** show STM images corresponding to these two different sample preparations, yielding Pb islands of different average size. This

behavior is mainly due to the higher density of nucleation points on the NaCl layer in (b) with respect to (a). The NaCl layer has different characteristics in the two cases: the layer is flat and presents very few defect in (a), while it shows the coexistence of various thicknesses and a higher density of edges in (b). In (a) the side length of the equilateral triangular Pb islands is in the range of 25 to 60 nm, while in (b) it is  $\leq 10$  nm. For the STS measurements, triangular islands of various sizes were selected. The Pb islands expose (111) crystal faces. A determination of the thickness of NaCl layers at a given location is not straightforward. Moreover, the apparent height of NaCl layers varies depending on tunneling conditions, such as bias voltage and tip conditions.

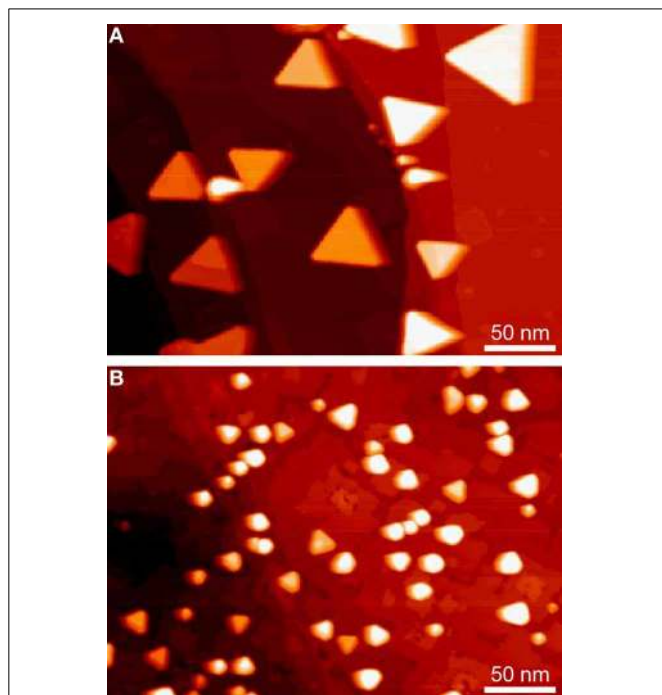
### 3.2. COULOMB BLOCKADE AND COULOMB STAIRCASE ON Pb NANOISLANDS

In a STM double junction geometry, there are some intrinsic limitations in the relations between resistances and capacitances of the two junctions. As discussed in the introduction, in order to observe CB phenomena, the condition  $R_i \gg R_Q$  has to be satisfied. In the tunneling regime, this condition is easily satisfied for junction 2 (tip-vacuum-island), for which resistances  $R_2$  of 1 M $\Omega$  to 1 G $\Omega$  are usual. For junction 1, this condition requires the presence of an insulating layer of sufficient thickness, leading in our case to resistances  $R_1$  of the order of 1 M $\Omega$  to 100 M $\Omega$ . Concerning the capacitance, although the tip-island distance is of the same order as the insulating layer thickness (0.5

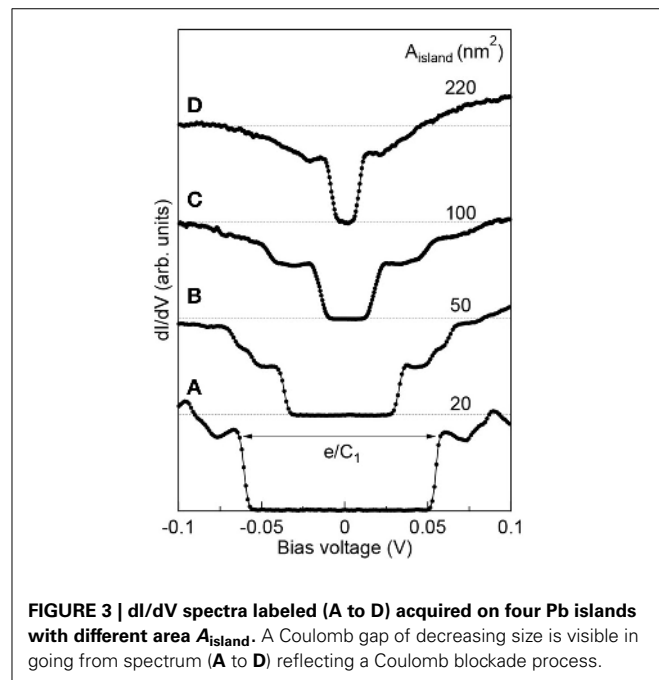
to 1 nm), the NaCl dielectric constant plays an important role, leading to capacitances  $C_1$  ten times larger than typical values for  $C_2$ . By varying the set-point current, the tip-island distance is modified and consequently also  $R_2$  and  $C_2$ . The resistance, however, decreases exponentially with decreasing distance, while the capacitance increases only weakly.

**Figure 3** shows  $dI/dV$  spectra acquired on four different Pb islands. The spectra present the typical signature of CB, i.e., a zero-conductance gap around the Fermi energy ( $E_F$ ). Notice that bulk Pb is superconducting at the measurement temperature of  $T = 4.6$  K. We neglect here the possible existence of the superconducting gap in the Pb islands because the energy scale of the Coulomb gap is much larger than the one of the superconducting gap of  $\leq 1$  meV (45). Consequently, we treat the tunneling junctions as if they are in the normal state. The width of the gap is inversely proportional to the island area  $A_{\text{island}}$ : the gap is  $\approx 120$  mV wide for the smallest island ( $A_{\text{island}} \approx 20$  nm<sup>2</sup>), and  $\approx 18$  mV for the largest one ( $A_{\text{island}} \approx 220$  nm<sup>2</sup>). This is the expected behavior, since for  $C_2 < C_1$  the gap width is governed by the tip-substrate capacitance  $C_1$ . Therefore, as  $C_1$  increases for increasing island area, it leads to narrower gaps. The 220 nm<sup>2</sup>-island (a triangle with 22 nm side) represents the upper limit for an unambiguous observation of a zero-conductance gap at this temperature. From the measured gap, we estimate  $C_1$  to approximately 10 aF. For the 20 nm<sup>2</sup>-island,  $C_1$  is ten times smaller. These values are in agreement with values calculated using the expression for a parallel plate capacitor  $C_1 = \epsilon_0 \epsilon_r A_{\text{island}} / d_{\text{NaCl}}$ , with the island supported on a 3 ML NaCl film of thickness  $d_{\text{NaCl}} = 0.8$  nm and dielectric constant of bulk NaCl  $\epsilon_r = 5.5$  (46) The small features in **Figure 3A** just below  $\pm 0.1$  eV are related to the capacitance  $C_2$  (see discussion of **Figure 5**).

**Figure 4** displays the typical evolution of the tunneling spectra from the CB to the CS regime for a selected Pb triangular



**FIGURE 2 | STM topographies acquired on two different samples with Pb islands grown on NaCl/Ag(111).** Pb islands are visible in both images, most of them with triangular shape and a few with rounded shape. The smaller island size in (B) as compared to (A) is obtained on a NaCl film exhibiting more defects. (A): +1 V, 20 pA; (B): +4 V, 20 pA.

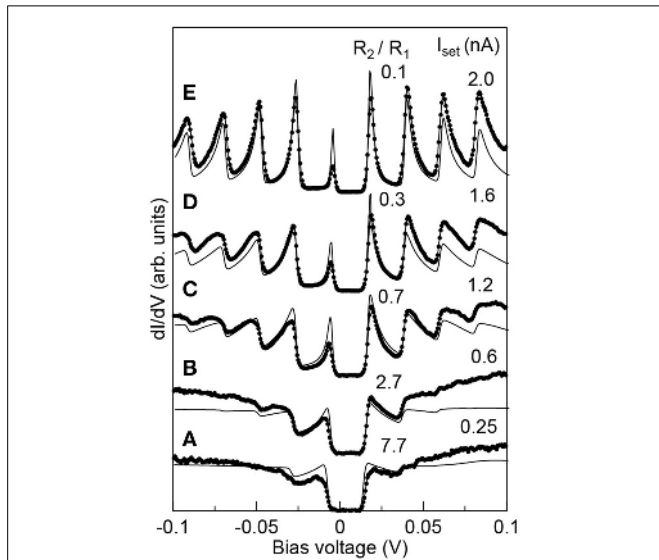


**FIGURE 3 |  $dI/dV$  spectra labeled (A to D) acquired on four Pb islands with different area  $A_{\text{island}}$ .** A Coulomb gap of decreasing size is visible in going from spectrum (A to D) reflecting a Coulomb blockade process.

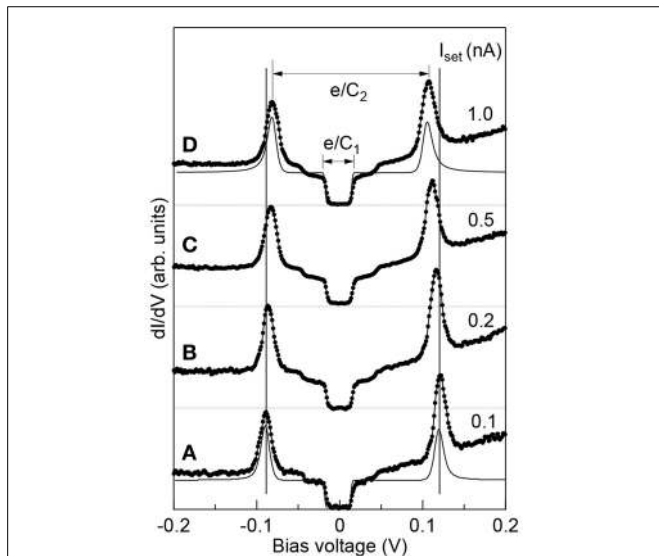
island with a side length of 14 nm. The  $dI/dV$  spectrum A shows a simple Coulomb gap while spectra B to E display a series of equidistant peaks (steps in the  $I - V$  characteristics, a CS) with increasing intensity. This progression is achieved by measuring

the tunnel spectra with increasing initial current, corresponding to decreasing tip sample separation and decreasing resistance  $R_2$ , in going from spectrum A to E. Our simulation within the orthodox theory reproduces the general features of the measured spectra revealing CB and CS characteristics. The simulation of these spectra within orthodox theory allows us to extract the pertinent parameters of the double barrier system, i.e., the capacitances and resistances of both junctions, as well as the residual non-integer charge  $Q_0$  on the Pb island, see figure caption. Notice that, with decreasing tip-sample distance,  $R_2$  decays exponentially, whereas  $C_2$  increases linearly (13, 18). As this latter variation is small,  $C_2$  is assumed to be constant throughout this series of simulations. To summarize, tunneling spectra on such nanoislands may display a simple CB gap or a CS depending on the parameters of the DBTJ. Well-developed CS's are observed with an asymmetric resistance ratio  $R_2 < R_1$ .

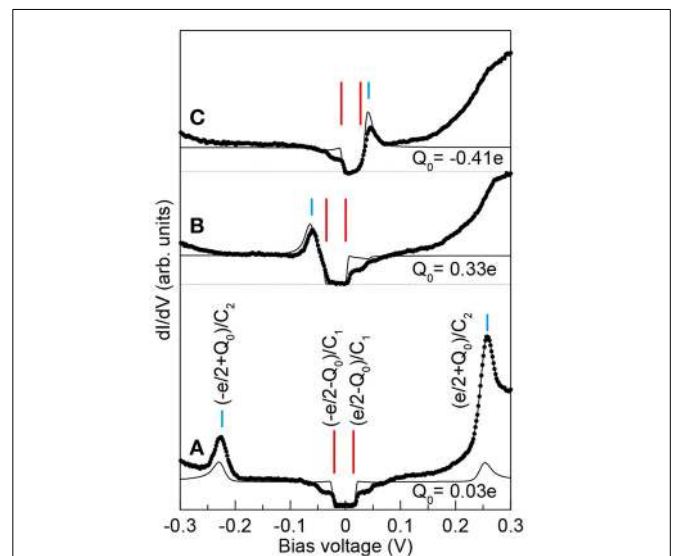
Concerning the robustness of the simulations and the precision of the derived parameters we note that  $Q_0$  is always determined with an error of  $< 10\%$ , as it corresponds to an energy shift of the tunneling spectra with respect to zero bias voltage. The capacitances  $C_1$  and  $C_2$  are also reasonably well determined, especially in situations like those depicted in **Figure 5** or **Figure 6** where two well separated energies are well-defined. The errors of the determined values are thus also  $< 10\%$ . The sum of  $R_1$  and  $R_2$  is fixed by the experimentally determined  $I(V)$  characteristics. Their ratio is most favorably evaluated in the CS regime, as the height and the width of the various peaks are linked directly to their ratio. In this situation a precision of the order of 10% is obtained (see **Figure 4**). In the simple CB case, the precision of the resistance ratio is  $\geq 10\%$ .



**FIGURE 4 | Evolution from Coulomb blockade to Coulomb staircase: experimental STS data acquired on a Pb island with 14 nm side ( $A_{\text{island}} \approx 85 \text{ nm}^2$ ) (dots) and simulation (black line) based on the orthodox theory.** The spectra are offset for clarity. Parameters of the simulation:  $R_1 = 39 \text{ M}\Omega$ ,  $C_1 = 7.46 \text{ aF}$ , and  $C_2 = 0.7 \text{ aF}$ ; **(A):**  $R_2 = 300 \text{ M}\Omega$  and  $Q_0 = -0.15 e$ , **(B):**  $R_2 = 105 \text{ M}\Omega$  and  $Q_0 = -0.2 e$ , **(C):**  $R_2 = 26 \text{ M}\Omega$  and  $Q_0 = -0.26 e$ , **(D):**  $R_2 = 13 \text{ M}\Omega$  and  $Q_0 = -0.26 e$ , **(E):**  $R_2 = 4.5 \text{ M}\Omega$  and  $Q_0 = -0.28 e$ .



**FIGURE 5 | Spectra (A to D): increase of the tip-island capacitance  $C_2$  with decreasing tip-island distance (increasing tunnel current).** The spectra, offset for clarity as  $dI/dV(0V) = 0$ , have been acquired on a Pb island of 14 nm side. Parameters of the simulation, performed for spectra **(A)** and **(D)** curve:  $C_1 = 5.0 \text{ aF}$ ,  $C_2 = 0.77 \text{ aF}$ ,  $R_1 = 5 \text{ M}\Omega$ ,  $R_2 = 1700 \text{ M}\Omega$ ,  $Q_0 = 0.062 e$ ; **(D)** curve:  $C_1 = 5.0 \text{ aF}$ ,  $C_2 = 0.86 \text{ aF}$ ,  $R_1 = 5 \text{ M}\Omega$ ,  $R_2 = 145 \text{ M}\Omega$ ,  $Q_0 = 0.07 e$ .



**FIGURE 6 | Manipulation of the residual charge  $Q_0$ .**  $dI/dV$  spectra measured on the same island with 7.9 nm side, showing features related to both,  $C_1$  and  $C_2$ , with varying  $Q_0$ , and corresponding simulations. The residual charge ( $Q_0$ ) of the island is changed by a bias voltage pulse (duration:  $50 \mu\text{s}$ , current:  $1 \text{ nA}$ ). Parameters of the simulation:  $C_1 = 3.8 \text{ aF}$ ,  $C_2 = 0.335 \text{ aF}$ ,  $R_1 = 25 \text{ M}\Omega$ ,  $R_2 = 2300 \text{ M}\Omega$ ; **(A):**  $Q_0 = 0.03 e$ , **(B):**  $Q_0 = 0.33 e$ , **(C):**  $Q_0 = -0.41 e$ .

A closer comparison of calculations and data in **Figure 4** shows that there are some deviations in the intensity of the structures. For the present island of a thickness of 11 ML, a quantum well state, reflecting the vertical confinement, located at +0.2 eV above  $E_F$  contributes a considerable background to the spectra (47). Therefore, a quantitative fitting of the tunnel spectra within the orthodox theory should consider the density of states (DOS) of the sample (48).

If the parameters of the DBTJ are appropriately chosen, spectral features reflecting both, tip-island ( $C_2$ ) and island-substrate ( $C_1$ ) capacitance can be observed simultaneously. Note that the electrostatic energy of the island is given by the Coulomb charging energy  $E_c = e^2/C_\Sigma$ , where  $C_\Sigma = \sum C_i$ . However, the threshold voltage necessary for the transfer of an electron across the tip-island (island-substrate) junction is inversely proportional to the capacitance  $C_2$  ( $C_1$ ) (12, 13). Spectra of **Figure 5** were acquired on a Pb island of  $\approx 14$  nm side length. Spectrum A shows a Coulomb gap around  $E_F$  as well as two peaks at  $\approx \pm 0.1$  V, which are related to the  $C_2$  capacitance. For decreasing tip-island distance (increasing tunnel current), the tip-island capacitance  $C_2$  is expected to increase slightly. This behavior is observed in **Figure 5B**: by approaching the tip to the island from A to D, the value of  $C_2$  increases leading to a decreased separation between the two  $C_2$  peaks, as indicated by the vertical lines. In addition, if the island area  $A_{\text{island}}$  becomes comparable to the effective tip area  $A_{\text{tip}}$ , there will be also a contribution to  $C_2$  due to the tip-substrate capacitance. In the present measurement  $A_{\text{island}}$  turns out to be smaller than  $A_{\text{tip}}$ .  $C_2$  is then evaluated using the simple parallel-plate capacitance formula. In addition to the capacitance between the metallic island and the tip, the capacitance between the tip and the substrate, including the vacuum and the NaCl layers, is considered in the model.

The present measurements and their analysis allow us to obtain the dielectric constant of the ultrathin NaCl film within a parallel plate capacitor model, if we take the island substrate capacitance  $C_1$  from the simulation of the spectra, the area  $A_{\text{island}}$  of the capacitor plate from the STM topographies, and the thickness  $d_{\text{NaCl}}$  of the NaCl film as deduced from STS of FERs (36) With a typical island size of  $A_{\text{island}} = 100 \text{ nm}^2$  and  $d_{\text{NaCl}} = 0.8 \text{ nm}$  (3 ML), we obtain  $\epsilon_r = 4$ , a reasonable value compared to the one of  $\epsilon = 5.5$  for bulk NaCl (46), and the one extracted from FERs measurements,  $\epsilon = 3.5$  (36).

In contrast to the situation in a planar tunnel junction (49), our setup has no gate electrode. However, by externally applying a bias voltage pulse to the junction (12), a gate voltage change is mimicked. In **Figure 6** we present three tunneling spectra, obtained on the same position on a triangular island of 7.9 nm side, where subsequently a bias voltage pulse of  $\pm 5$  V has been applied to the junction. The spectra clearly show the result of this action, a pulse-bias-dependent shift of the central Coulomb gap away from the symmetric zero-voltage position, accompanied by a shift of the  $C_2$ -related spectral features. The background above +0.2 V originates from the tail of a quantum well state at higher energy (47). This background contributes also to the observed intensity variations of the spectral features. The asymmetric displacement of the central Coulomb gap and of the  $C_2$ -related peaks under the action of an external voltage pulse reflects the different

values of the fractional residual charge  $Q_0$ , obtained from our simulation, on the Pb island.

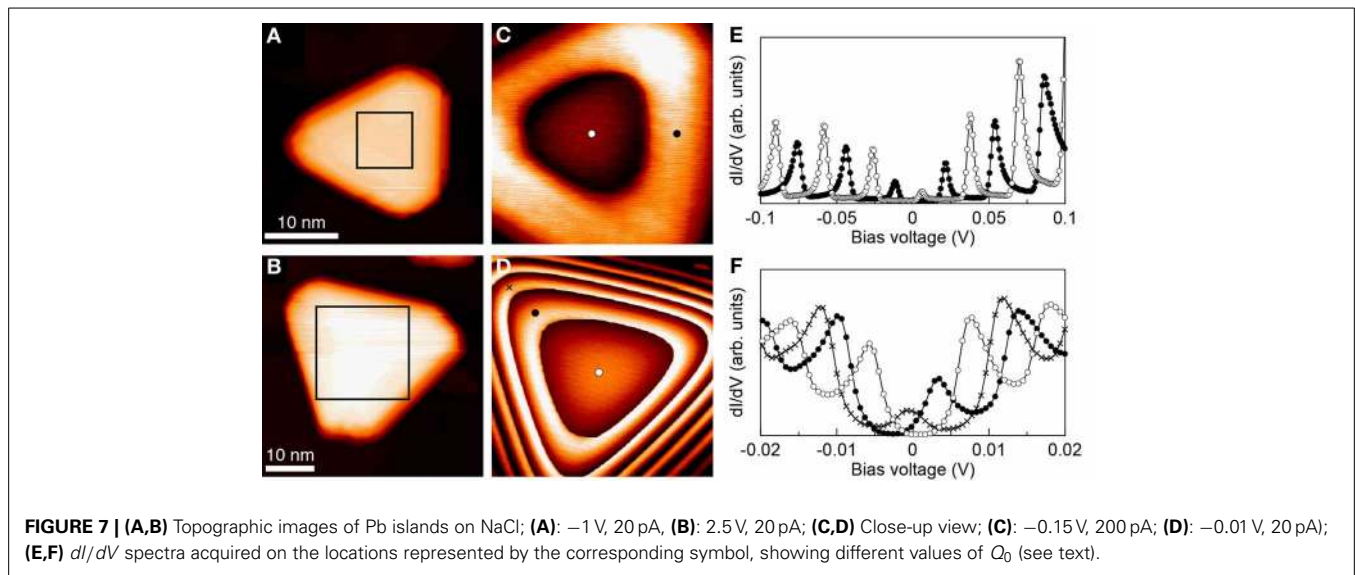
It has been proposed that the residual charge  $Q_0$  is related to the difference in work function of the various metals constituting the junctions (12):

$$Q_0 = [C_2(\Delta\phi_2) - C_1(\Delta\phi_1)]/e \quad (1)$$

where  $\Delta\phi_1$  is the difference between substrate and island work functions, and  $\Delta\phi_2$  the difference between tip and island work functions. As a result of voltage pulses, charge can be trapped in defects or impurities in the NaCl layer beneath the Pb nanoisland, leading to a permanent modification of the residual charge  $Q_0$ .

In the following section we demonstrate the influence of the tip-island junction on the residual charge  $Q_0$  via the variation of  $C_2$ , variation due to the displacement of the tip with respect to the Pb island during scanning. In **Figures 7A,B** two different Pb islands are displayed. In the closeup-view topographic images of **Figures 7C,D**, very striking concentric lines following the contours of the island are visible. **Figures 7E,F** shows typical  $dI/dV$  spectra obtained on these islands. Our measurements show that, by scanning laterally across the surface, an energy shift of the spectrum is observed which corresponds to a maximum fluctuation of the residual charge  $Q_0 = \pm e/2$ . We deduced the  $Q_0$  values by simulating each local STS spectrum in the CS regime. For the Pb island shown in **Figures 7A,C**, we obtain a value of  $Q_0 \approx +0.35e$  for the spectrum acquired at the center of the island, and  $Q_0 \approx -0.15e$  for the one acquired in the surrounding region. For the system of **Figures 7B,D**, up to six regions of alternating negative and positive  $Q_0$  are detected.

In order to explain this surprising effect we have to consider that the parameters of junction 2 depend on the tip position with respect to the island. As already mentioned, the residual charge  $Q_0$  is related to the difference in work function of the various metals constituting the junctions, see Equation 1. For a given set of measurements  $C_1$  is fixed by the Pb island and the NaCl layer characteristics and the work functions are well defined. In these conditions, Equation 1 shows that a variation of  $Q_0$  can only originate from a variation of  $C_2$ . As discussed above, the lateral extension of the tip can exceed the island area. Therefore, to evaluate  $C_2$ , not only the capacitance between tip and island, but also the one between tip and substrate has to be included. When scanning over a Pb island, the ratio between these two contributions changes continuously, leading to variations of the residual charge within the island. Now, considering the CS spectra shown in **Figures 7E,F**, we recall that with increasing bias voltage every additional CS peak in the differential conductance spectrum indicates the hopping of an additional electron to/from the island. In an STM scan at a bias voltage close to a CS peak, e.g., at 0.075 eV in **Figure 7E**, a small change in  $Q_0$  (due to the changing tip-island capacitance) will lead to a situation where the measurement will be performed above or below the respective CS peak, corresponding to one more (above the peak) or one less electron (below the peak) tunneling to the island. This effect leads to the observed symmetric triangular step patterns in the STM



topographies shown in **Figures 7A,B**. Evidently, the sharp apparent height steps visible in the STM images reflect the hopping of one additional electron on/off the Pb island, while the transition regions correspond to a continuous variation of  $Q_0$ . Notice that, contrary to the first impression gained from the images, at each instant the value of the charge  $Q_0$  is the same over the entire island, as expected for a conducting object. These features are visible when  $C_1 \Delta\phi_1 \approx C_2 \Delta\phi_2$ , a condition which can be fulfilled for  $\Delta\phi_1$  ten times smaller than  $\Delta\phi_2$ , since  $C_1$  is typically ten times larger than  $C_2$ . This implies that  $\Delta\phi_1$  has to be small in order to observe these features. Moreover,  $\Delta\phi_2$  strongly depends on the specific tip conditions, explaining the fact that these effects were not systematically observed. In this situation, a  $C_2$  variation of the order of 10% can induce a modification of  $Q_0$  as large as  $\pm e/2$ .

Finally, we note that the observation of Coulomb charge rings with scanning probe methods has been made before for quantum dots inside carbon nanotubes (50), for quantum dots of a two-dimensional electron gas inside semiconductor heterostructures (51), and for quantum dots inside InAs nanowires (52). Controlled charge switching has been performed for single Au atoms on NaCl (53), for a single Si donor in Si doped GaAs (54), and for a small conductive grain on an InAs surface (55). The present measurements on Pb nanoislands show that these intriguing CB phenomena and the related charging effects are also observed in metallic quantum dots. While the observed phenomena are similar they are not identical. The essential difference between the present measurements and the SPM investigations on the quantum dots before is that in our case the STM tip is in the tunneling mode measuring the conductance through the Pb island without a gate electrode, while the former investigations use a standard conductance measurement of the nanowires (quantum dots) and there the SPM tip represents an external electrode the field of which shifts the CS spectra of the observed quantum dots.

#### 4. CONCLUSIONS AND OUTLOOK

We investigated the transport properties of single crystalline metallic nanostructures in the CB regime. To this end, small Pb islands with well-defined geometries, ranging from a diameter of a few to tens of nanometers and a thickness of a few monolayers are grown on crystalline NaCl layers on Ag(111) substrate. The tunneling spectra obtained at 4.6 K on the metallic quantum dots show clearly the presence of CB phenomena. By reducing the tip-island distance, the tunneling spectra reflect the evolution from CB to CS. Our simulations employing the semi-classical orthodox theory describe well the observed spectra in both regimes allowing us to extract quantitatively the parameters of the DBTJ, i.e., the resistances, capacitances, and the residual charges.

The present STM/STS studies have shown that not only the size and shape of the metallic nanoislands can be well determined but that, importantly, also their local electronic structure and their transport properties can be quantitatively elucidated. In the past, e.g., the superconducting properties of small particles have been investigated (56) revealing a *number parity* property. STS experiments of isolated superconducting islands would allow us to observe simultaneously the pairing correlation on islands with different parity. Moreover, in small metallic particles containing magnetic impurities, the Kondo resonance was predicted to be strongly affected in a parity-dependent way (4), another exciting phenomenon to look at with local probes. We believe that STM/STS will continue to be a decisive player for the elucidation of the mesoscopic physics of nanostructures.

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