



Crowdsourcing to Smartphones: Incentive Mechanism Design for Mobile Phone Sensing

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Global Smartphone Users

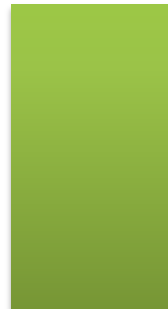


500M



2010

1.08B



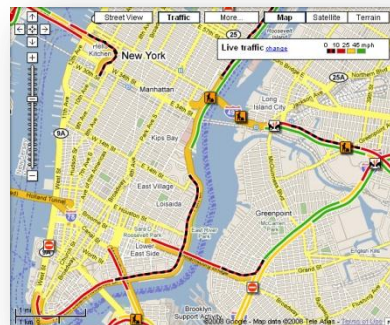
2012

>2B



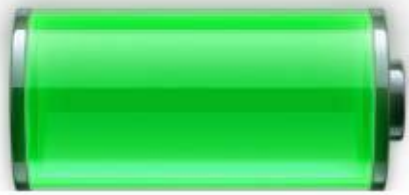
2015

Mobile Phone Sensing Apps



What is Missing?

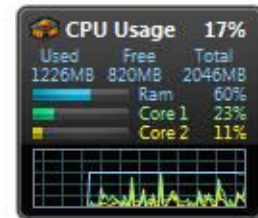
Smartphone users consume their own resource



Power



Memory



CPU



Related Works



S. Reddy D. Estrin M.B. Srivastava

- Developed recruitment frameworks
- Focused on user selection, not incentive design

- Developed a sealed-bid second-price auction
- The platform utility was not considered



G. Danezis S. Lewis R. Anderson

- Designed an auction based dynamic price incentive mechanism
- Truthfulness was not considered



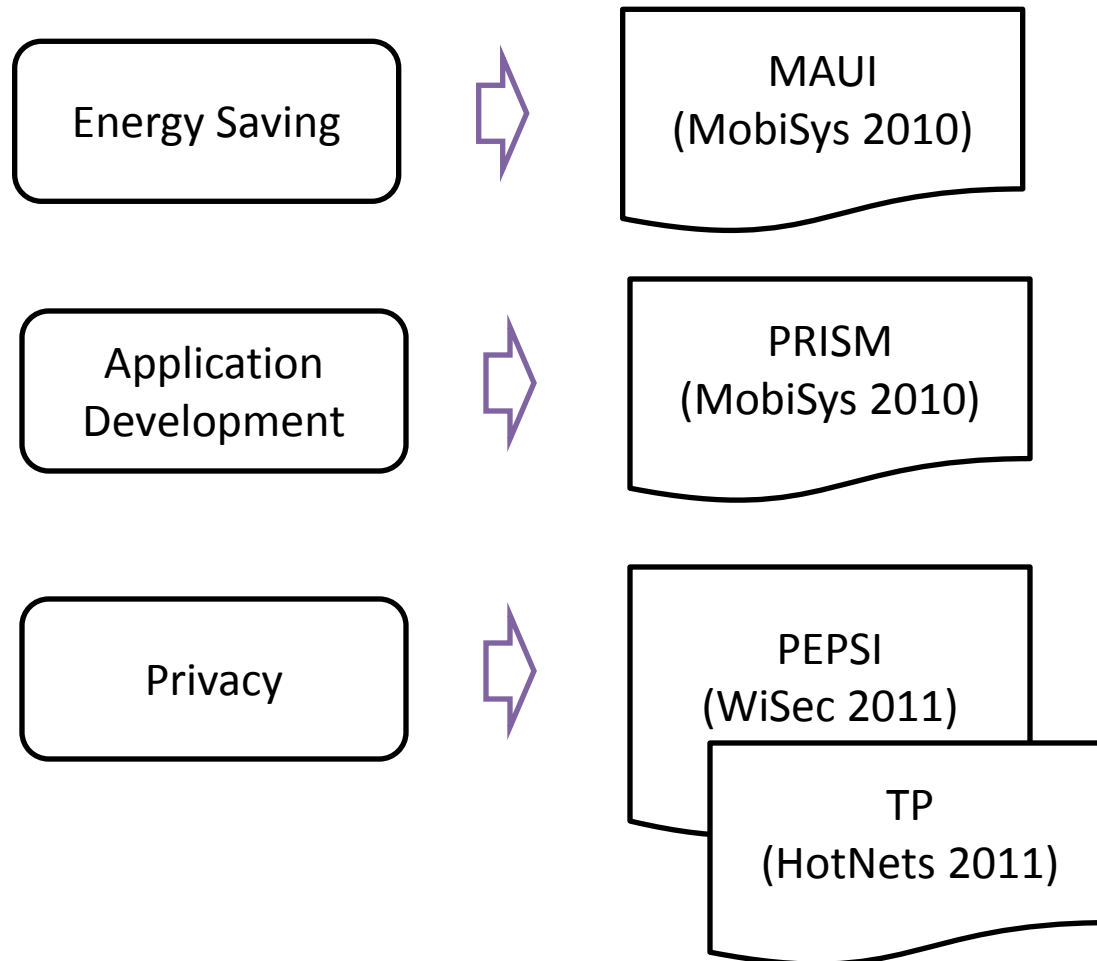
J-S. Lee B. Hoh

S. Reddy, D. Estrin, and M.B. Srivastava; "Recruitment framework for participatory sensing data collections" in PERVASIVE 2010

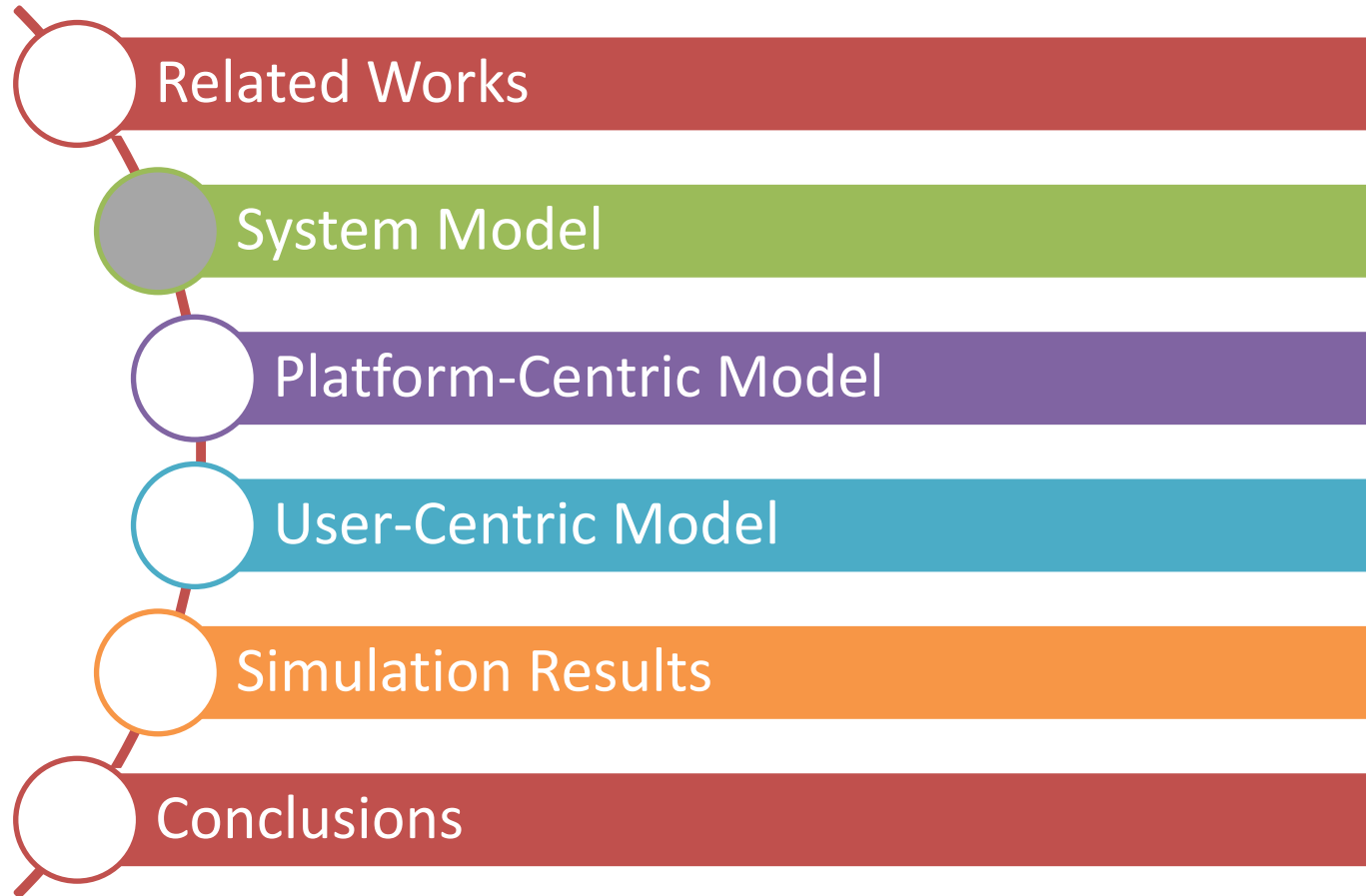
G. Danezis, S. Lewis, and R. Anderson; "How Much is Location Privacy Worth?" In WEIS 2005.

J-S. Lee and B. Hoh; "Sell Your Experiences: Market Mechanism based Participation Incentive for Participatory Sensing" in PERCOM 2010

Other Related Works



Outline/Progress



System Model

$$U = \{1, 2, \dots, n\}, n \geq 2$$

Platform-Centric Model



User-Centric Model

Platform-Centric Model



- Platform announces a **total reward R**
- Each user i has the **sensing time $t_i \geq 0$** and sensing cost $\kappa_i \times t_i$, where **κ_i is its unit cost**
- The utility of user i is

$$\bar{u}_i = \frac{t_i}{\sum_{j \in U} t_j} R - t_i \kappa_i$$

- The utility of the platform is

$$\bar{u}_0 = \lambda \log \left(1 + \sum_{i \in U} \log(1 + t_i) \right) - R$$

where $\lambda > 1$ is a system parameter.

User-Centric Model

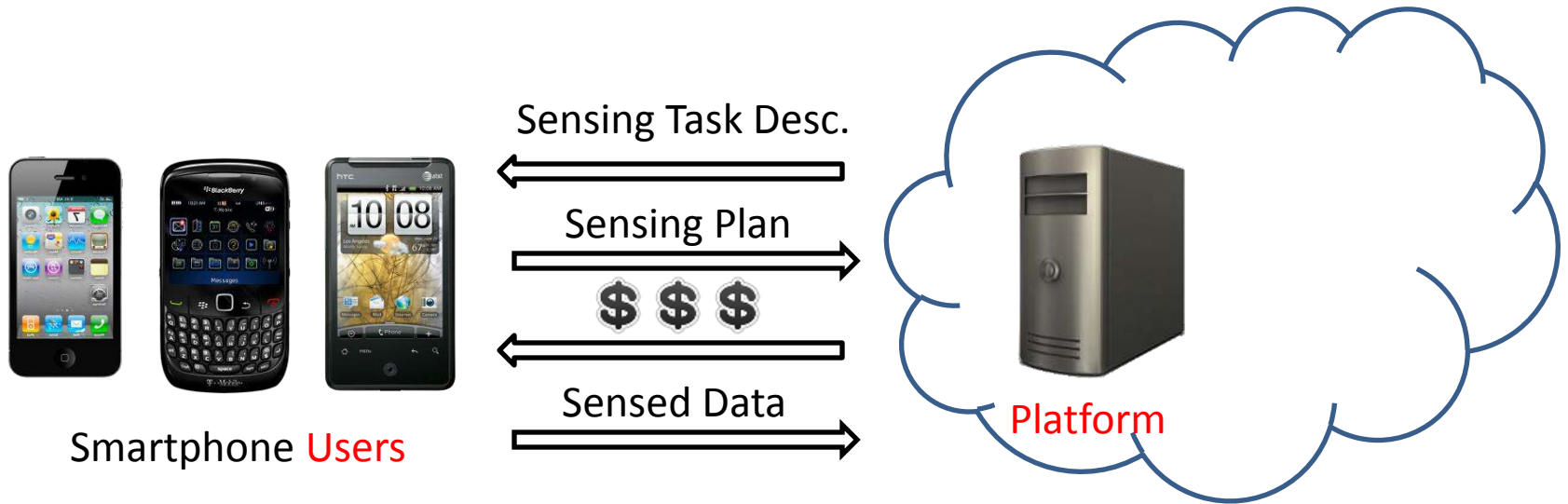


- Platform announces a set $\Gamma = \{\tau_1, \tau_2, \dots, \tau_m\}$ of tasks, where each τ_j has a (private) value $v_j > 0$.
- Each user $i \in U$ selects a subset $\Gamma_i \subseteq \Gamma$, based on which user i has a (private) cost c_i

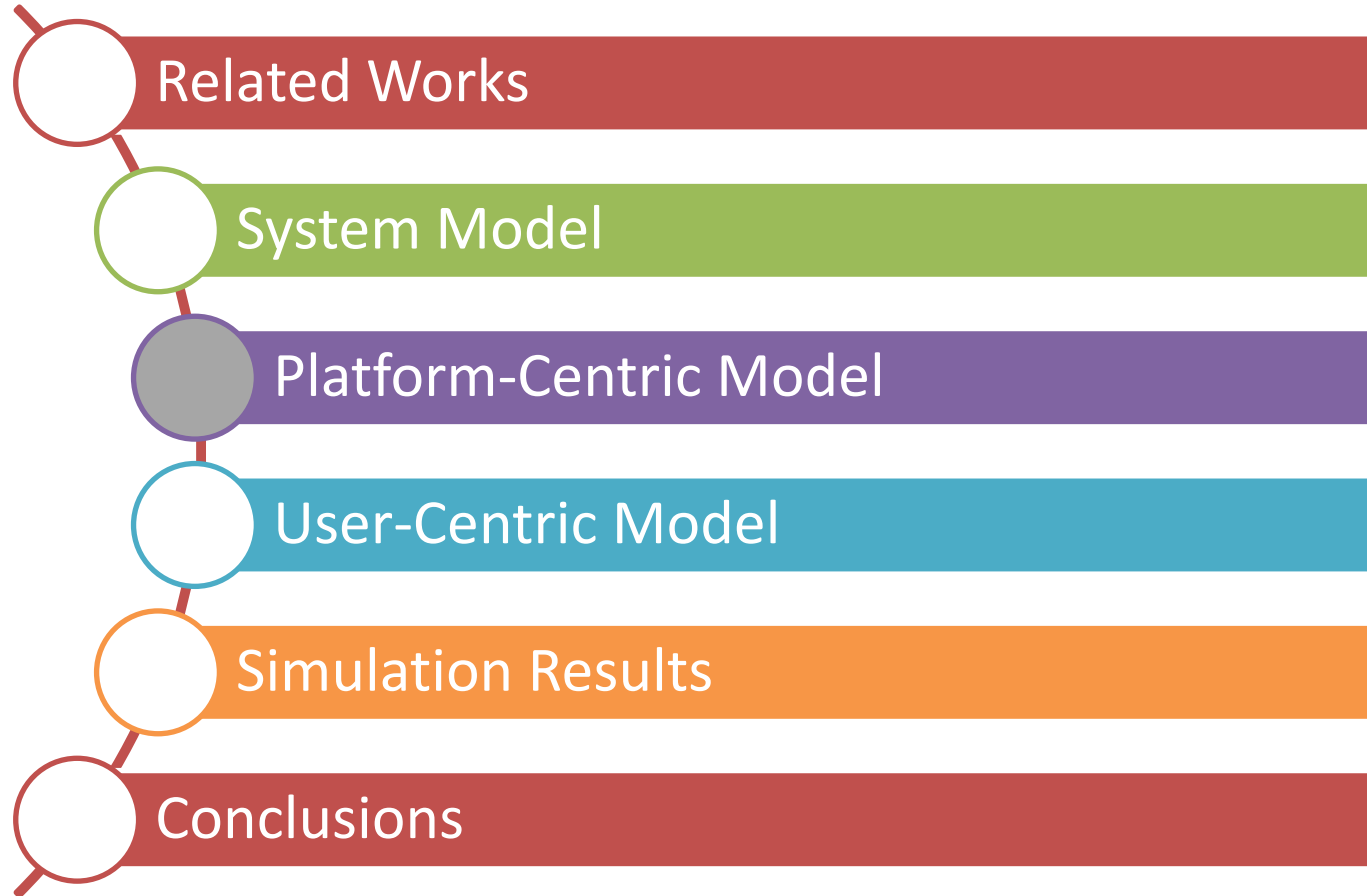


- Utility of user i is $\tilde{u}_i = \begin{cases} p_i - c_i, & \text{if } i \in S, \\ 0, & \text{otherwise.} \end{cases}$
- Utility of the platform is $\tilde{u}_0 = v(S) - \sum_{i \in S} p_i$, where $v(S) = \sum_{\tau_j \in \cup_{i \in S} \Gamma_i} v_j$.

Mobile Phone Sensing System



Outline/Progress



Stackelberg Game (Platform-Centric)



Stackelberg Equilibrium:

- Each follower tries to maximize its utility, given the leader's strategy
- The leader tries to maximize its utility, given the knowledge of the followers' behavior

User Sensing Time Determination



Sensing Time Determination (STD) game:

Players: Users

Strategy: Sensing Time

Utility: $\bar{u}_i = \frac{t_i}{\sum_{j \in U} t_j} R - t_i \kappa_i$

NE Computation

Leader



Followers

Sort users according to their unit costs, $\kappa_1 \leq \kappa_2 \leq \dots \leq \kappa_n$.
 $S \leftarrow \{1, 2\}, i \leftarrow 3$;

while $i \leq n$ and $\kappa_i < \frac{\kappa_i + \sum_{j \in S} \kappa_j}{|S|}$

$S \leftarrow S \cup \{i\}, i \leftarrow i + 1$;

end

for each $i \in U$

if $i \in S$ then $t_i^{ne} = \frac{(|S|-1)R}{\sum_{j \in S} \kappa_j} \left(1 - \frac{(|S|-1)\kappa_i}{\sum_{j \in S} \kappa_j} \right)$;

else $t_i^{ne} = 0$;

return $(t_1^{ne}, t_2^{ne}, \dots, t_n^{ne})$

THEOREMS 1&2: The strategy profile $t^{ne} = (t_1^{ne}, t_2^{ne}, \dots, t_n^{ne})$ is the **unique NE** of the STD game.

Platform Reward Determination

Leader



Followers

$$\bar{u}_0 = \lambda \log \left(1 + \sum_{i \in \mathcal{U}} \log(1 + t_i) \right) - R$$

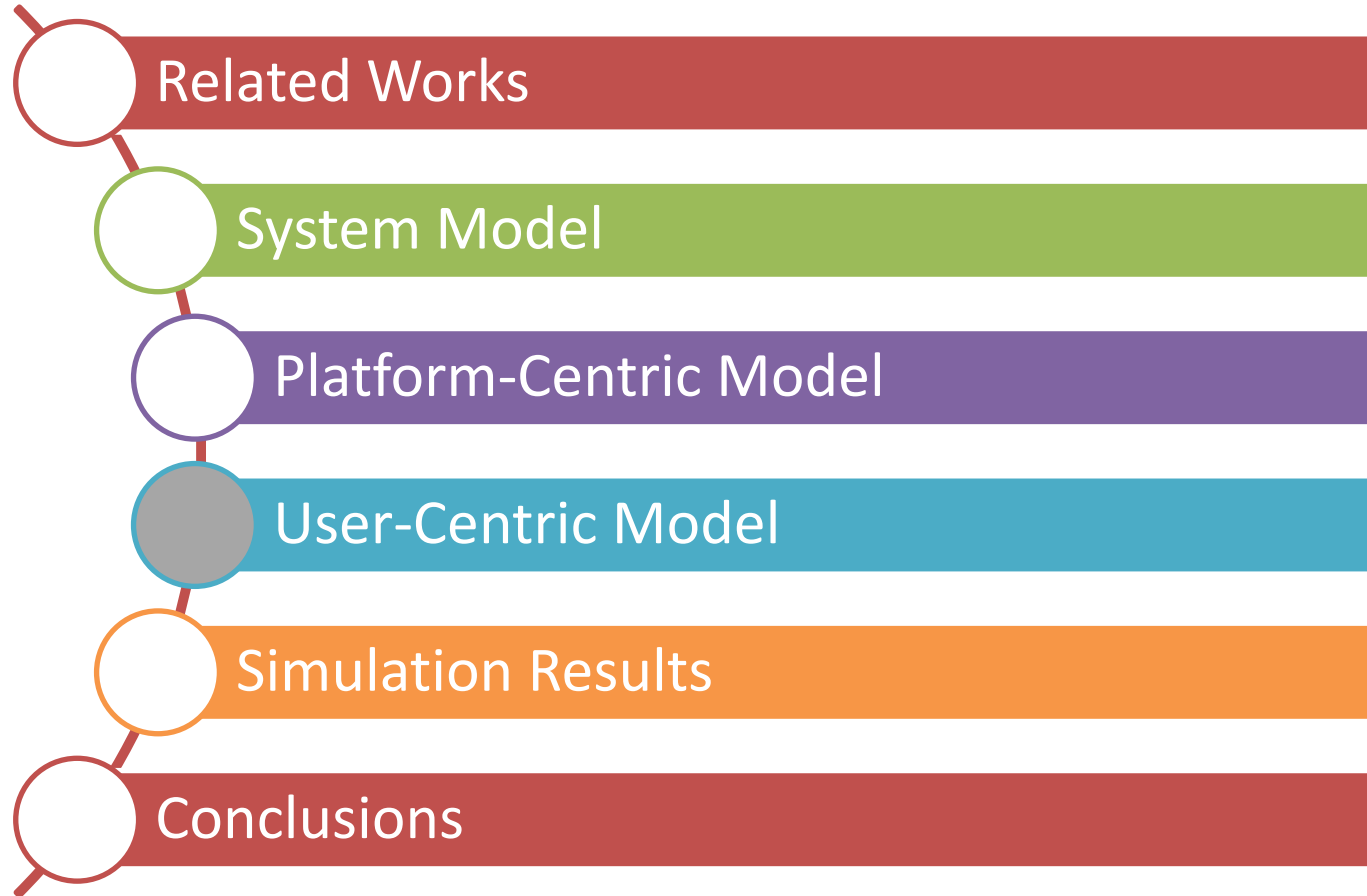


$$\bar{u}_0 = \lambda \log \left(1 + \sum_{i \in \mathcal{S}} \log(1 + X_i R) \right) - R$$

$$\text{where } X_i = \frac{(|\mathcal{S}|-1)}{\sum_{j \in \mathcal{S}} \kappa_j} \left(1 - \frac{(|\mathcal{S}|-1)\kappa_i}{\sum_{j \in \mathcal{S}} \kappa_j} \right)$$

THEOREM 3: There exists a **unique SE** (R^*, t^{ne}) in the MSensing game, where R^* is the unique maximizer of the above utility function, which is strictly concave.

Outline/Progress



LSB Auction (Not Truthful)

```
S ← {i}, where i ← arg maxi ∈ U f({i});
*while ∃ i ∈ U \ S such that f(S ∪ {i}) > (1 +  $\frac{\epsilon}{n^2}$ ) f(S)
  S ← S ∪ {i};
if ∃ i ∈ S such that f(S \ {i}) > (1 +  $\frac{\epsilon}{n^2}$ ) f(S)
  S ← S \ {i}; go to *;
if f(U \ S) > f(S) then S ← U \ S;
for each i ∈ U
  if i ∈ S then p_i ← b_i;
  else p_i ← 0;
return (S, p)
```

$f(S) = \tilde{u}_0(S) + \sum_{i \in U} b_i$ is *submodular* and nonnegative

Truthful Auction

THEOREM 5: An auction mechanism is **truthful** if and only if, for any bidder i and any fixed choice of bid b_{-i} by other bidders,

1) The selection rule is **monotonically nondecreasing** in b_i ;

2) The payment p_i for any winning bidder i is set to the **critical value**.

MSensing Auction

Winner
Determination



Pricing

$S \leftarrow \emptyset, i \leftarrow \arg \max_{j \in U} (v_j(S) - b_j);$
while $b_i < v_i$ and $S \neq U$
 $S \leftarrow S \cup \{i\};$
 $i \leftarrow \arg \max_{j \in U \setminus S} (v_j(S) - b_j);$

MSensing Auction

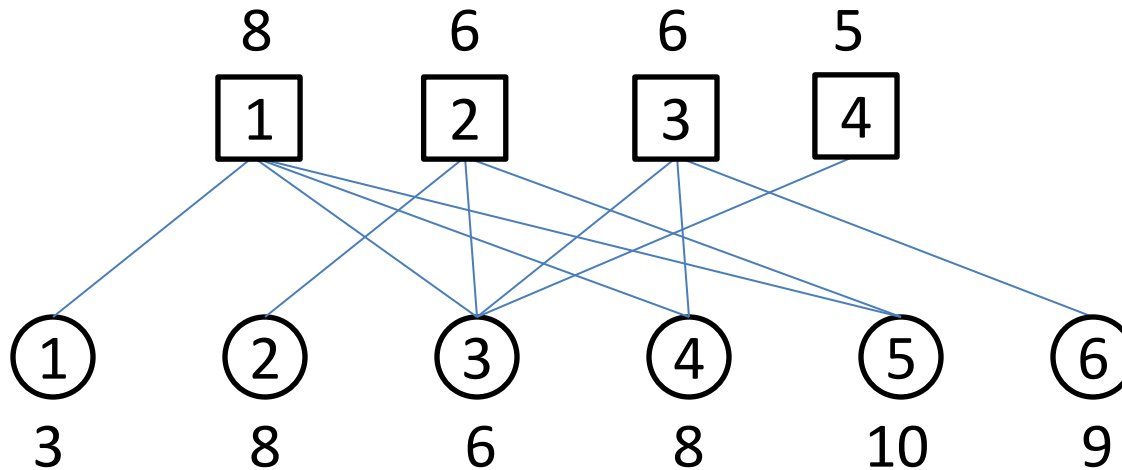
Winner
Determination



Pricing

```
 $p_i \leftarrow 0$  for all  $i \in U$ ;  
for each  $i \in S$   
   $U' \leftarrow U \setminus \{i\}, T \leftarrow \emptyset$ ;  
  repeat  
     $i_j \leftarrow \arg \max_{j \in U' \setminus T} (v_j(T) - b_j)$ ;  
     $p_i \leftarrow \max \{p_i, \min \{v_i(T) - (v_{i_j}(T) - b_{i_j}), v_i(T)\}\}$ ;  
     $T \leftarrow T \cup \{i_j\}$ ;  
  until  $b_{i_j} \geq v_{i_j}$  or  $T = U'$ ;  
  if  $b_{i_j} < v_{i_j}$  then  $p_i \leftarrow \max \{p_i, v_{i_j}(T)\}$ ;
```

Walk-through Example (MSensing)



Winner Selection:

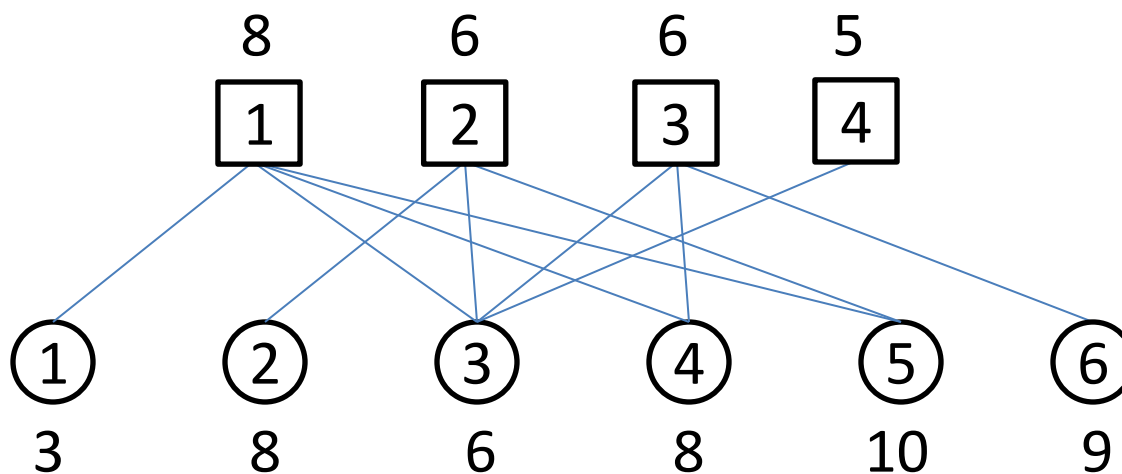
$S = \emptyset$: $v_1(\emptyset) - b_1 = (v(\emptyset \cup \{1\}) - v(\emptyset)) - b_1 = 19$, $v_2(\emptyset) - b_2 = 18$, $v_3(\emptyset) - b_2 = 17$
 $v_4(\emptyset) - b_4 = 1$.

$S = \{1\}$: $v_2(1) - b_2 = (v(\{1\} \cup \{2\}) - v(\{1\})) - b_2 = 2$, $v_3(1) - b_3 = 3$,
 $v_4(\{1\}) - b_4 = -5$.

$S = \{1,3\}$: $v_2(\{1,3\}) - b_2 = (v(\{1,3\} \cup \{2\}) - v(\{1,3\})) - b_2 = 2$, $v_4(\{1\}) - b_4 = -5$.

$S = \{1,3,2\}$: $v_4(\{1,3,2\}) - b_4 = -5$.

Walk-through Example (MSensing)



Payment Determination:

p_1 : Winners are {2,3}.

$$v_1(\emptyset) - (v_2(\emptyset) - b_2) = 9, v_1(\{2\}) - (v_3(2) - b_3) = 0, v_1(\{2,3\}) = 3. \mathbf{p_1 = 9} \geq 8.$$

p_2 : Winners are {1,3}.

$$v_2(\emptyset) - (v_1(\emptyset) - b_1) = 5, v_2(\{1\}) - (v_3(1) - b_3) = 5, v_2(\{1,3\}) = 8. \mathbf{p_2 = 8} \geq 6.$$

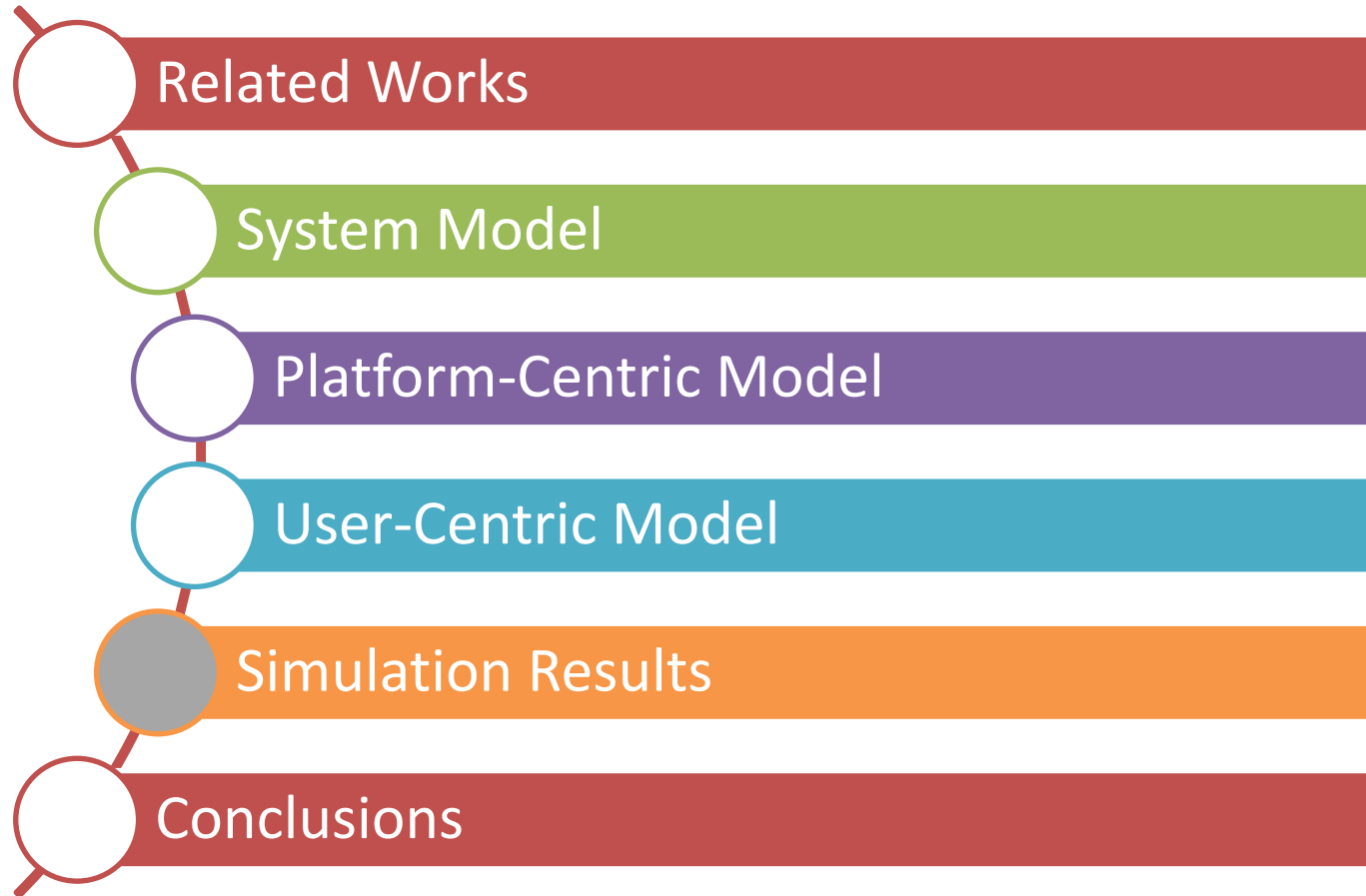
p_3 : Winners are {1,2}.

$$v_3(\emptyset) - (v_1(\emptyset) - b_1) = 4, v_3(\{1\}) - (v_2(1) - b_2) = 7, v_3(\{1,2\}) = 9. \mathbf{p_3 = 9} \geq 6.$$

MSensing is Truthful

THEOREM 6. MSensing is computationally efficient, individually rational, profitable and truthful.

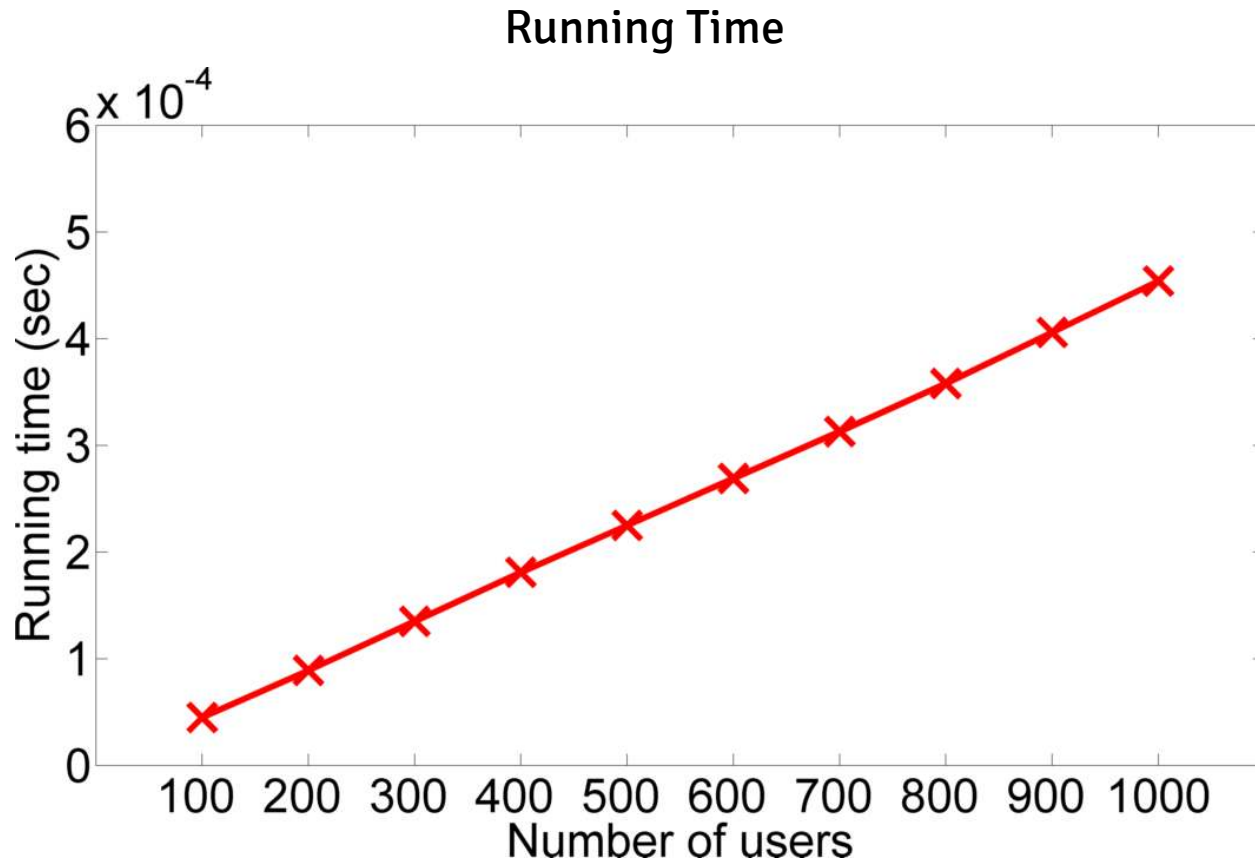
Outline/Progress



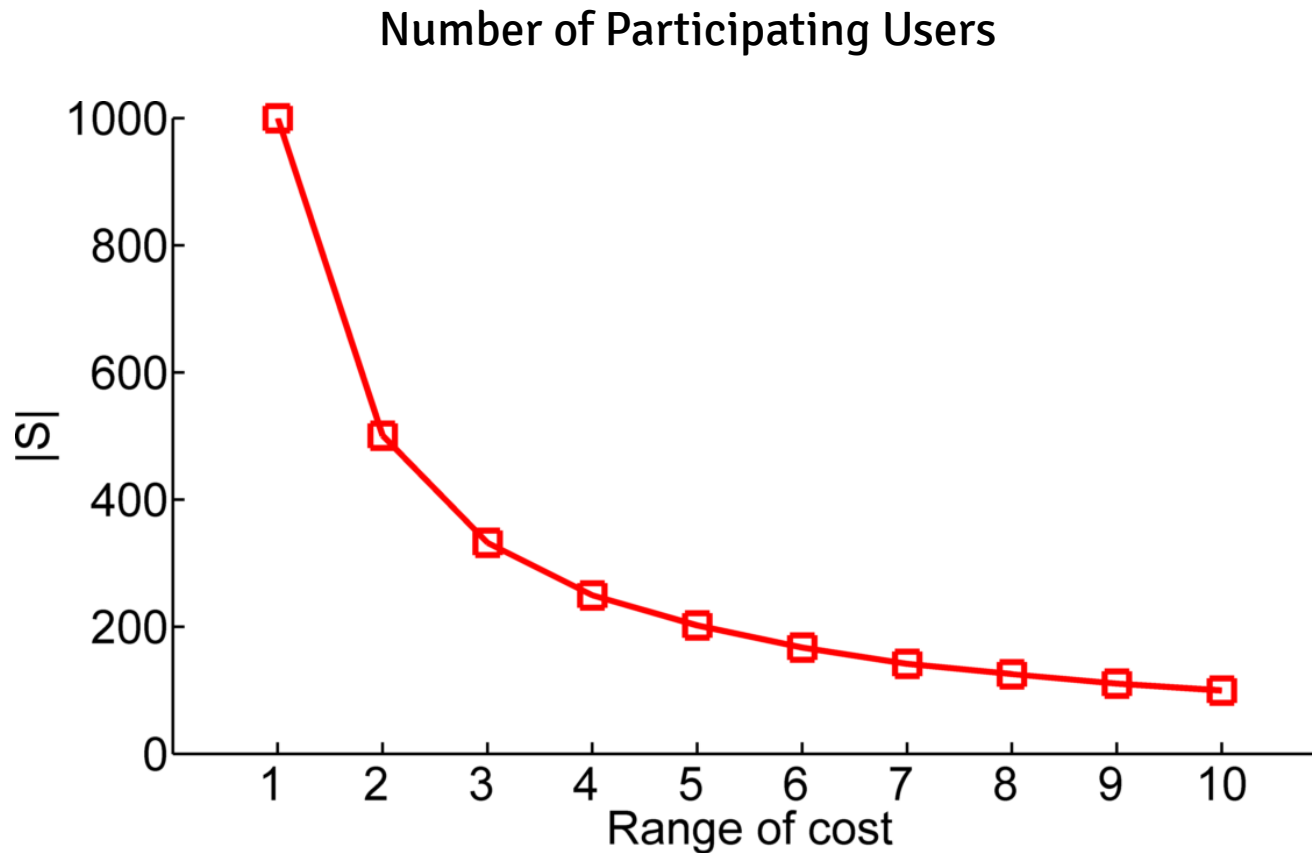
Simulation Setup

- Platform-Centric Model
 - n is varied from 100 to 1000
 - Cost is uniformly distributed over $[1, \kappa_{max}]$, where κ_{max} is varied from 1 to 10
 - λ is set to 3, 5, 10
- User-Centric Model
 - n is varied from 1000 to 10000
 - m is varied from 100 to 500
 - ϵ is set to 0.01

Platform-Centric Incentive Mechanism

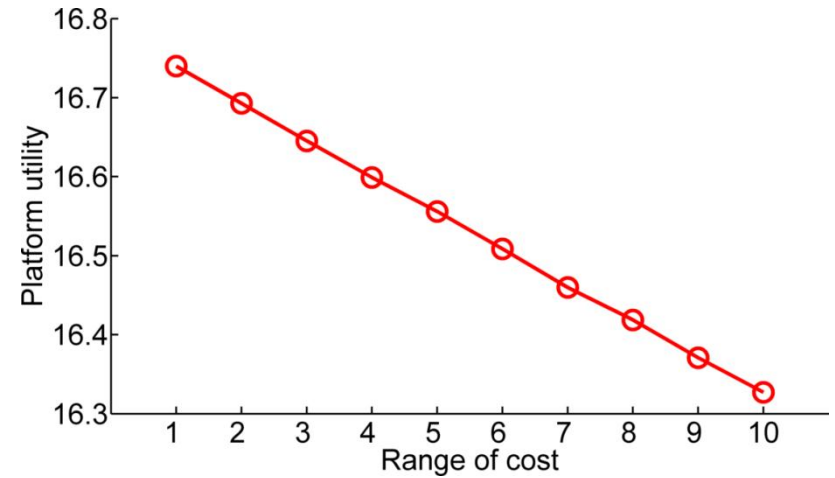
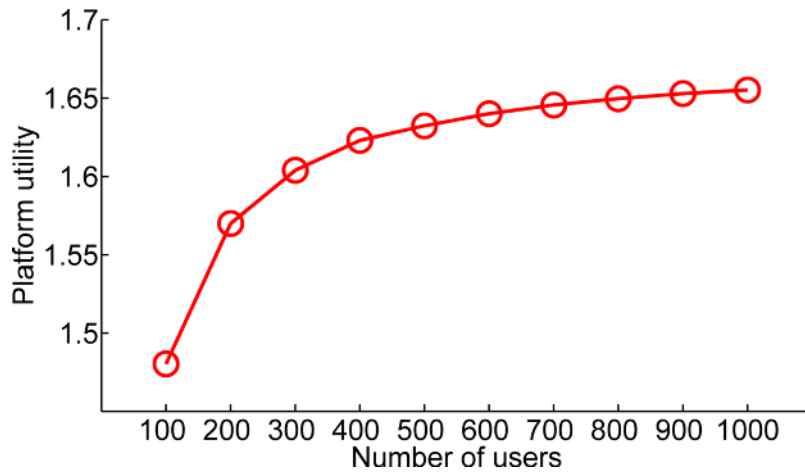


Platform-Centric Incentive Mechanism



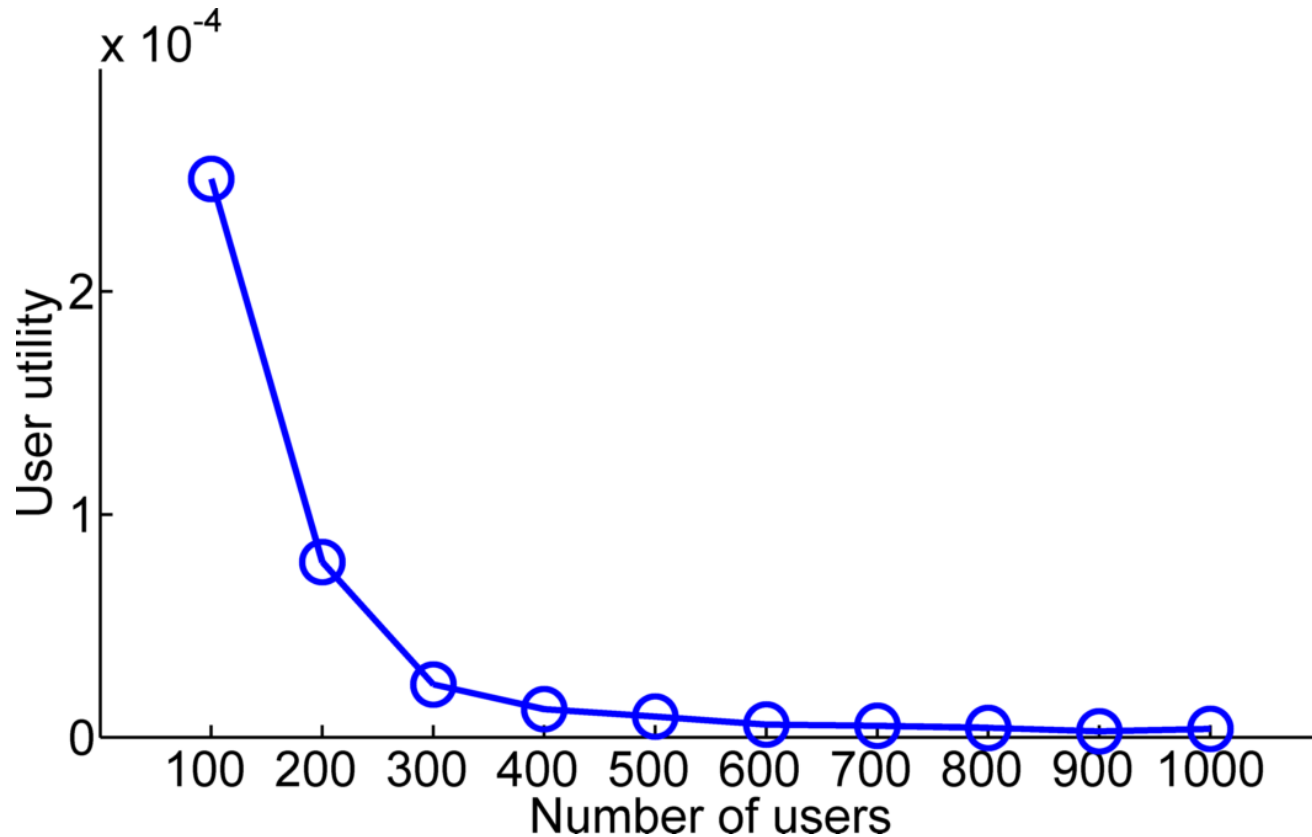
Platform-Centric Incentive Mechanism

Platform Utility



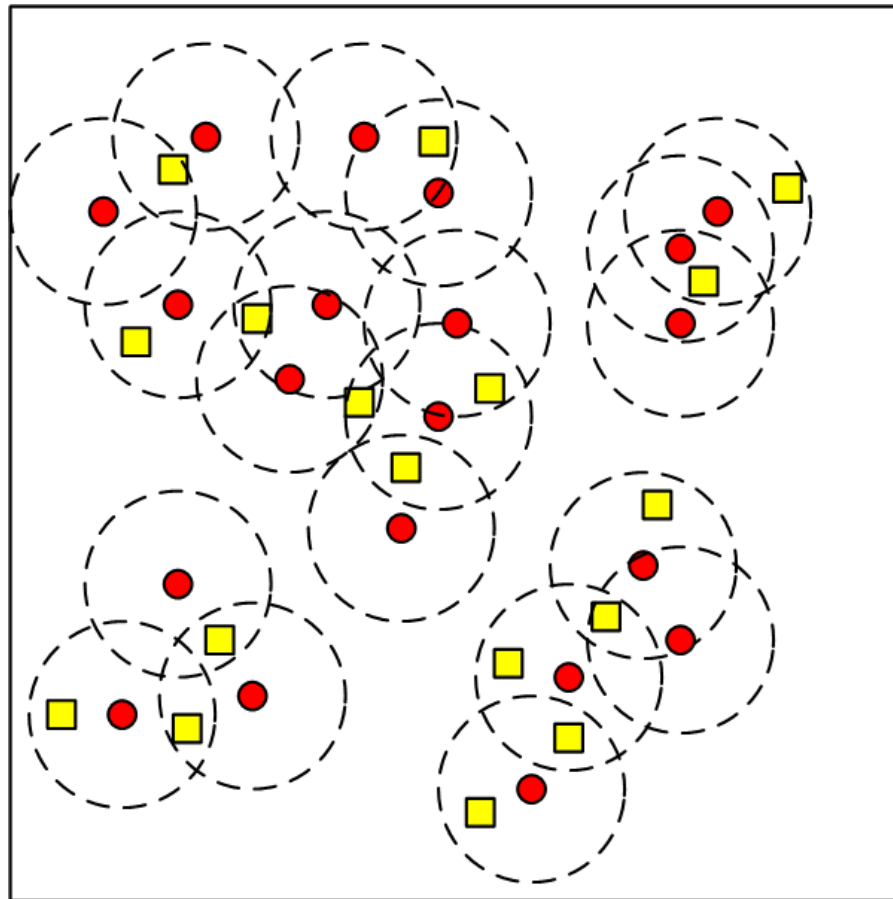
Platform-Centric Incentive Mechanism

User Utility



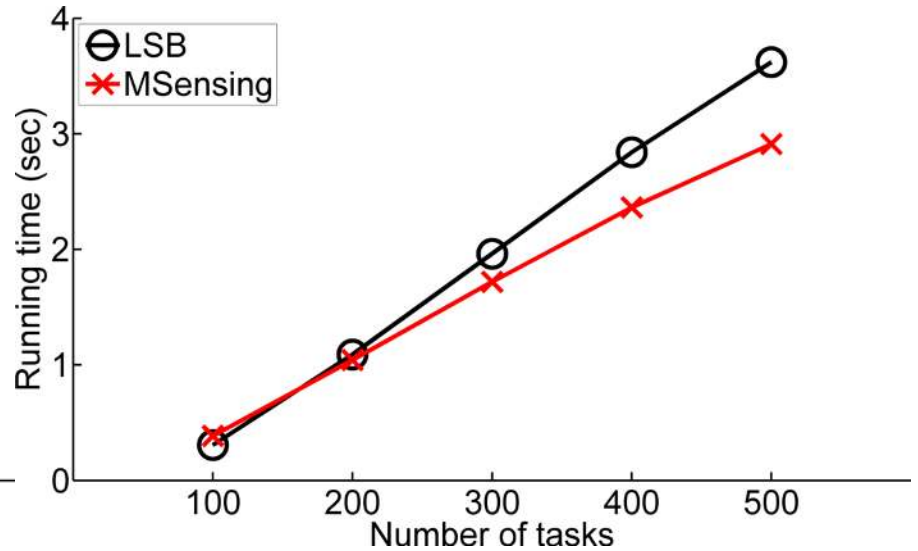
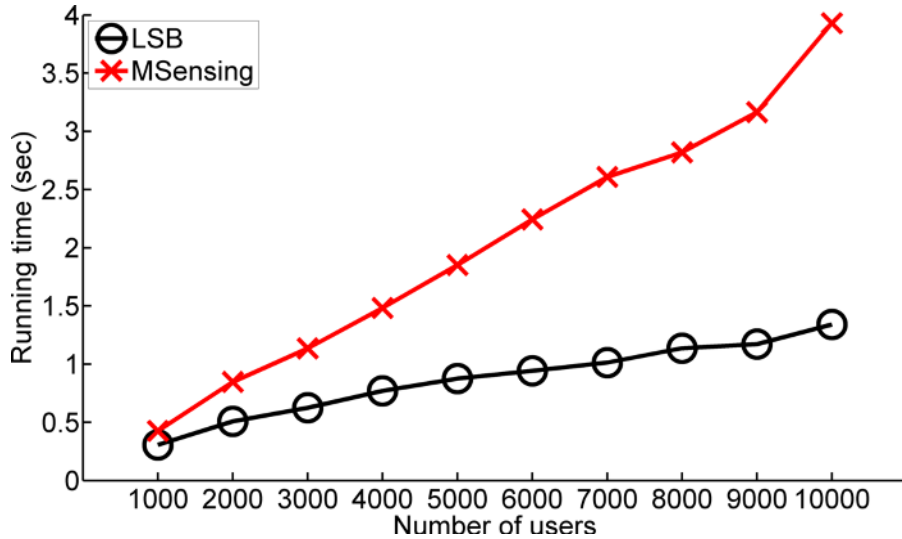
Simulation Setup

- User-Centric Model



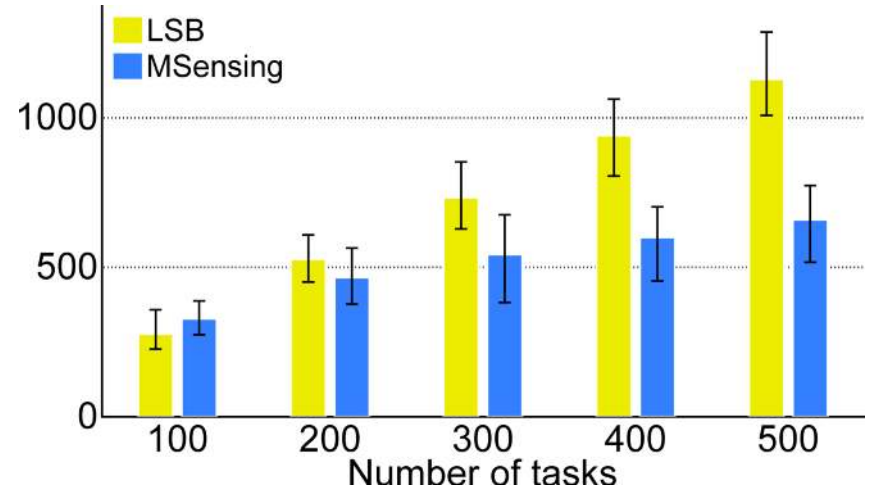
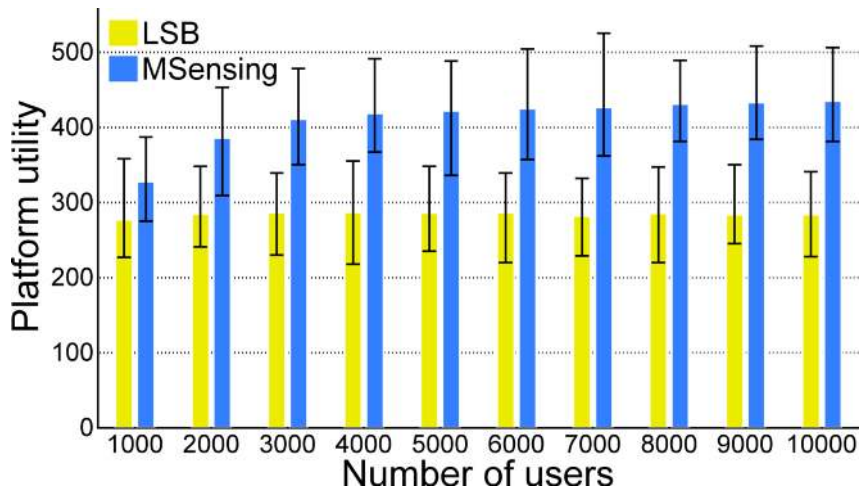
User-Centric Incentive Mechanism

Running Time



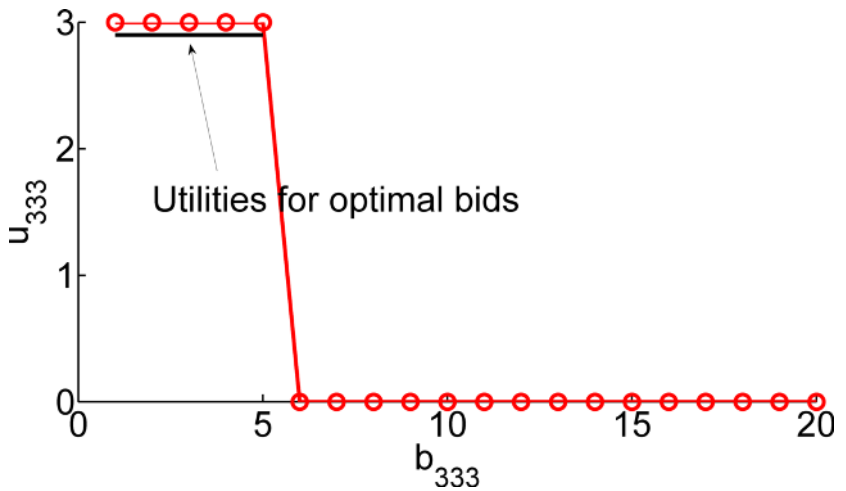
User-Centric Incentive Mechanism

Platform Utility

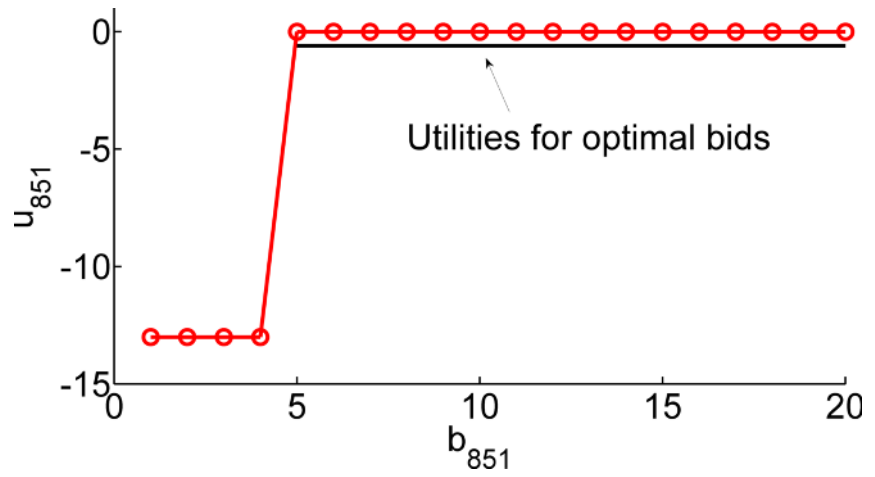


User-Centric Incentive Mechanism

Verification of Truthfulness

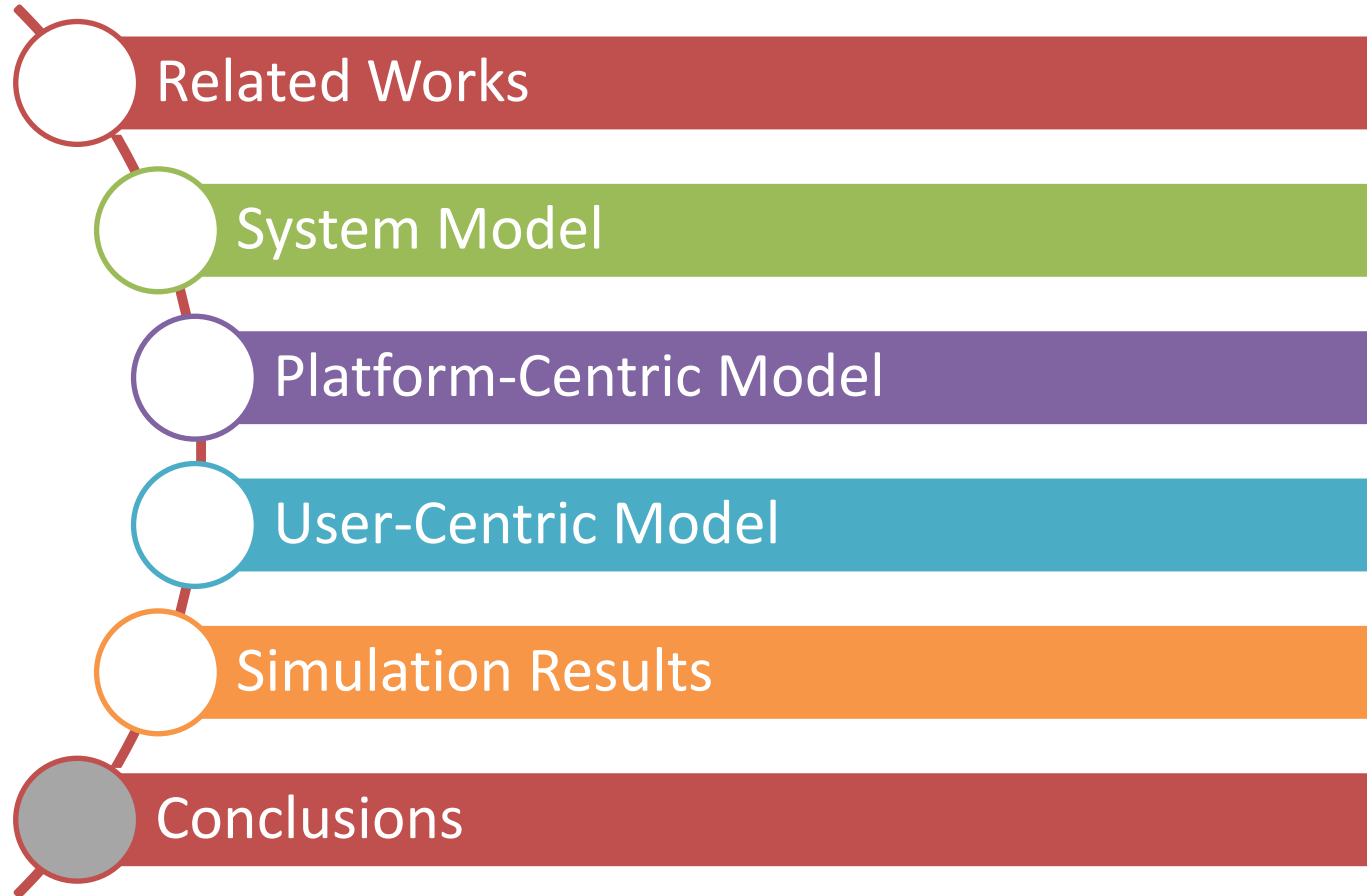


$$c_{333} = 3$$



$$c_{851} = 18$$

Outline



Conclusions

Designed incentive mechanisms for mobile phone sensing

Platform-Centric Model

- Modeled as a Stackelberg game
- Proved the uniqueness of Stackelberg Equilibrium, which can be computed efficiently

User-Centric Model

- Modeled as an auction
- Proved the computational efficiency, individual rationality, profitability and truthfulness