# Cryptanalysis of Twister 

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#### Abstract

In this paper, we present a semi-free-start collision attack on the compression function for all Twister variants with negligible complexity. We show how this compression function attack can be extended to construct collisions for Twister-512 slightly faster than brute force search. Furthermore, we present a second-preimage and preimage attack for Twister-512 with complexity of about $2^{384}$ and $2^{456}$ compression function evaluations, respectively.


Keywords: SHA-3, Twister, hash function, collision-, second-preimage-, preimage attack.

## 1 Introduction

In the NIST SHA-3 competition, many new hash function designs have been submitted. NIST published a list of 51 first round candidates, and Twister 445] is one of them. The next step is to reduce the list of 51 candidates to a small set of finalists within the next few years. As an input to this selection process, we describe several cryptanalytic results on Twister in this paper. Similar results on the Whirlpool [1, Grøstl [15] and GOST [14] hash functions, or the MerkleDamgård 311] constrution have been published in [10], 89] and [6]. Our results on Twister are summarized in Table 1 .

Table 1. Summary of cryptanalytic results on Twister

| type of attack | target | hash size | complexity | memory |
| ---: | :---: | :---: | :---: | :---: |
| semi-free-start collision | compression function | all | $2^{8}$ | - |
| collision | hash function | 512 | $2^{252}$ | $2^{9}$ |
| second preimage | hash function | 512 | $2^{384+s}$ | $2^{10}+2^{64-s}$ |
| preimage | hash function | 512 | $2^{456}$ | $2^{10}$ |

In the remainder of the paper, we first give a description of Twister in Section 2, outline a practical collision attack on its compression function in Section 3, and give theoretical collision-, second preimage-, and preimage attacks in Sections 4 5, and 6, respectively. We summarize and conclude in Section 7 .

## 2 Description of Twister

The hash function Twister is an iterated hash function based on the MerkleDamgård design principle. It processes message blocks of 512 bits and produces a hash value of $224,256,384$, or 512 bits. If the message length is not a multiple of 512 , an unambiguous padding method is applied. For the description of the padding method we refer to [4] and [5]. Let $m=m_{1}\left\|m_{2}\right\| \cdots \| m_{t}$ be a t-block message (after padding). The hash value $h=H(m)$ is computed as follows:

$$
\begin{aligned}
H_{0} & =I V \\
H_{i} & =f\left(H_{i-1}, m_{i}\right) \quad \text { for } 0<i \leq t \\
H_{t+1} & =f\left(H_{t}, C\right) \\
h & =\Omega\left(H_{t+1}\right),
\end{aligned}
$$

where $I V$ is a predefined initial value, $C$ is the value of the checksum and $\Omega$ is an output transformation. The checksum $C$ is computed from the intermediate values of the internal state after each Mini-Round. Note that while for Twister$224 / 256$ the checksum is optional it is mandatory for Twister-384/512.

The compression function $f$ of Twister basically consists of 3 Maxi-Rounds. Each Maxi-Rounds consist of 3 or 4 Mini-Rounds (depending on the output size of Twister) and is followed by a feed-forward XOR-operation.

The Mini-Round of Twister is very similar to one round of the Advanced Encryption Standard (AES) [13]. It updates an $8 \times 8$ state $S$ of 64 bytes as follows:

Messagelnjection. A 8-byte message block $M$ is inserted (via XOR) into the last row of the $8 \times 8$ state $S$.
AddTwistCounter. A 8-byte block counter is xored to the second column of the state $S$.


Fig. 1. The compression function of Twister-224/256


Fig. 2. The compression function of Twister-384/512


Fig. 3. The output transformation of Twister

SubBytes. is identical to the SubBytes operation of AES. It applies an S-Box to each byte of the state independently
ShiftRows. is a cyclic left shift similar to the ShiftRows operation of AES. It rotates row $j$ by $(j-1)(\bmod 8)$ bytes to the left.
MixColumns. is similar to the MixColumns operation of AES. It applies a $8 \times 8$ MDS matrix $A$ to each column of the state $S$. The matrix $A$ and its inverse $B$ are given in Appendix A.

After the last message block and/or the checksum has been processed, the final hash value is generated from the last chaining value $H_{t+1}$ by an output transformation $\Omega$ (see Figure (3).

In the output transformation, two Mini-Rounds are applied to subsequently output 64 bits of the hash value. The output stream consists of the XOR of the first column of the state prior and after the two Mini-Rounds. This 64 -bit output stream continues until the full hash size has been received. For a more detailed description of Twister we refer to [4] and [5].

## 3 Semi-Free-Start Collision for the Compression Function

In this section, we present a semi-free-start collision attack on the compression function of Twister for all output sizes. The complexity to find a differential characteristic is about $2^{8}$ compression function evaluations. However, for each differential characteristic, we can construct up to $2^{64}$ message pairs and the complexity to find one of these conforming message pairs is one.

In the attack we use the differential characteristic of Figure 4 for the first Maxi-Round (3 Mini-Rounds) of Twister. The 3 Mini-Rounds are denoted by $r_{1}, r_{2}$ and $r_{3}$ and the state after the Mini-Round $r_{i}$ is denoted by $S_{i}$ and the state after the corresponding feed-forward $S_{i}^{F}$. The initial state or chaining value is denoted by $S_{0}$. In the attack we add a difference in message word $M_{1}$ (8 active bytes) to the state $S_{0}$, which results in a full active state $S_{1}$ after the first MiniRound $r_{1}$. After the MixColumns transformation of the second Mini-Round $r_{2}$, the differences result in 8 active bytes of the last row of state $S_{2}$, which can be canceled by the message word $M_{3}$ in the third Mini-Round $r_{3}$.

The message differences and values for the state are found using a rebound approach as proposed in [10. Figure 5shows the characteristic in detail. We start with message word differences in $M_{1}$ and $M_{3}$ at states $S_{1}^{\prime}$ and $S_{2}$ (we do not use differences in $M_{2}$ to simplify the description of the attack). The differences can


Fig. 4. Characteristic to construct a semi-free-start collision in the first Maxi-Round


Fig. 5. We start with differences in states $S_{1}^{\prime}$ and $S_{2}$ injected by message words $M_{1}$ and $M_{3}$, and propagate backward and forward (Step 1) to find a match for the S-box of round $r_{2}$ (Step 2)
be propagated backward and forward through the MixColumns transformation with a probability of one (Step 1). Then, we simply need to find a match for the resulting input and output differences of the SubBytes layer of round $r_{2}$ (Step 2) and propagate outwards.

Step 1. We start the attack with 8 active bytes in state $S_{1}^{\prime \prime \prime}$ and $S_{2}$ (injected by message words $M_{1}$ and $M_{3}$ ) and compute backward and forward to two full active states $S_{2}^{\prime \prime}$ and $S_{2}^{\prime \prime \prime}$. This happens with a probability of one due to the properties of the ShiftRows and MixColumns transformations. Note that we can significantly reduce the complexity of the attack, if we first compute the full active state $S_{2}^{\prime \prime \prime}$ and then compute $S_{2}^{\prime \prime}$ column by column to find a match for 8 S-boxes at once (Step 2).

Step 2. Next, we show how to find a match for the input/output differences of the 64 active S-boxes of round $r_{2}$. Note that for a single S-box, the probability that a input/output differential exists is about one half, and for each valid input/output differential we can assign at least two possible values to the S-box (for more details we refer to [10]). Note that we can search for valid S-box differentials for each column independently. Hence, we start by choosing a random difference for the first active byte of $S_{1}^{\prime \prime \prime}$ and compute the corresponding row of $S_{2}^{\prime \prime}$. We find a valid differential match for these 8 S-boxes with a probability of $(1 / 2)^{8}=2^{-8}$. If we find a match, we continue with the remaining active bytes. Alltogether, this step has a complexity of less than $2^{8}$ compression function evaluations.

Once we have found a differential match for the SubBytes layer, we can choose from at least $2^{64}$ possible states for $S_{2}^{\prime \prime}$. Each of these states can be computed forward and backward and results in a semi-free-start collision for one

Maxi-Round. Further, this determines the state $S_{0}$ as well as the values and differences of $M_{1}$ and $M_{3}$ (we can freely choose the values of $M_{2}$ ). Note that the first Maxi-Round is the same for Twister-224/256 and Twister-384/512. Hence, by constructing a semi-free-start collision for the first Maxi-Round we already get a semi-free-start collision for the compression function of Twister-224/256 and Twister- $384 / 512$. Since we can find $2^{8}$ semi-free-start collisions with a complexity of $2^{8}$ compression function evaluations, the average complexity to find one semi-free-start collisions is one with negligible memory requirements. An example for a semi-free start collision is given in 2

Table 2. A colliding message pair $\left(M, M^{*}\right)$ for the semi-free-start collision of the first Maxi-Round ( $S_{3}, S_{3}^{*}$ ) of Twister. The corresponding semi-free-start collision for Twister-256 (with output transformation) is given by $H(256)$ and $H^{*}(256)$.


## 4 A Collision Attack on Twister-512

In this section, we show how the semi-free-start collision attack on Twister-512 can be extended to the hash function. We first show how to construct collisions in the compression function of Twister- 512 with a complexity of $2^{223}$ compression function evaluations. This collision attack on the compression function is then extended to a collision attack on the hash function. The extension is possible by combining a multicollision attack and a birthday attack on the checksum. The attack has a complexity of about $2^{252}$ evaluations of the compression function of Twister-512.

### 4.1 Collision Attack on the Compression Function

For the collision attack on the compression function of Twister-512 we can use the characteristic of the previous section in the last Maxi-Round (see Figure 6).


Fig. 6. The characteristic for the last Maxi-Round of Twister-512
Remember that in Twister-512 the 3 message words $M_{6}, M_{7}$ and $M_{8}$ are injected in the last Maxi-Round. Hence, we can use the first 5 message words $M_{1}-M_{5}$ for a birthday match on 56 state bytes with a complexity of $2^{8.56 / 2}=2^{224}$. Since the 8 bytes of the last row can always be adapted by using the freedom in the (absolute) values of the message word $M_{6}$, we only need to match 56 out of 64 bytes. It can be summarized as follows:

1. Compute $2^{224}$ semi-free-start collisions for the last Maxi-Round of Twister512 and save them in a list $L$. This has a complexity of about $3 \cdot 2^{224}$ MiniRound computations. Note that we can choose from $2^{3 \cdot 64}=2^{192}$ differences in $M_{6}, M_{7}$ and $M_{8}$ in the attack. Furthermore, by varying the values of $M_{7}$, we get additional $2^{64}$ degrees of freedom. Hence, we can construct up to $2^{256}$ semi-free-start collisions for the last Maxi-Round.
2. Compute the input of the last Maxi-Round by going forward and check for a match in the list $L$. After testing about $2^{224}$ candidates for the input of the last Maxi-Round we expect to find a match in the list $L$ and hence, a collision for the compression function of Twister-512. Finishing this step of the attack has a complexity of about $2^{224}$ Mini-Round computations.

Hence, we can find a collision for the compression function of Twister-512 for the predefined initial value with a complexity of about $2^{223}$ compression function evaluations ( $10 \cdot 2^{223}$ Mini-Round computations) and memory requirements of $2^{224}$. Note that memory requirements of this attack can significantly be reduced by applying a memory-less variant of the meet-in-the-middle attack introduced by Quisquater and Delescaille [16, and applied by Morita, Ohata and Miyaguchi [12].

### 4.2 Collision Attack on the Hash Function

In this section, we show how the collision attack on the compression function can be extended to the hash function. The attack has a complexity of about $2^{252}$ evaluations of the compression function of Twister-512. Note that the hash function defines, in addition to the common iterative structure, a checksum computed over the outputs of each Mini-Round which is then part of the final hash computation. Therefore, to construct a collision in the hash function we have to construct a collision in the iterative structure (i.e. chaining variables) as well as in the checksum. To do this we use multicollisions.

A multicollision is a set of messages of equal length that all lead to the same hash value. As shown in [7], constructing a $2^{t}$ collision, i.e. $2^{t}$ messages consisting
of $t$ message blocks which all lead to the same hash value, can be done with a complexity of about $t \cdot 2^{x}$ for any iterated hash function, where $2^{x}$ is the cost of constructing a collision in the compression function. As shown in the previous section, collisions for the compression function of Twister-512 can be constructed with a complexity of $2^{223}$. Hence, we can construct a $2^{256}$ collision with a complexity of about $256 \cdot 2^{223} \approx 2^{231}$ evaluations of the compression function of Twister-512 and memory requirements of $2^{9}$ (needed to store the $2^{256}$ collision). With this method we get $2^{256}$ values for the checksum $C$ that all lead to the same chaining value $H_{256}$.

To construct a collision in the checksum of Twister-512 we have to find 2 distinct messages consisting of 257 message blocks ( 256 message blocks for the multicollision and 1 message block for the padding) which produce the same value in the checksum. By applying a birthday attack we can find these 2 messages with a complexity of about $2^{256}$ checksum computations and memory requirements of $2^{256}$. Due to the high memory requirements of the birthday attack, one could see this part as the bottleneck of the attack. However, the memory requirements can be significantly reduced by applying a memory-less variant of the birthday attack [16]. Hence, we can find a collision for Twister-512 with a complexity of about $2^{231}$ compression function evaluations (10 Mini-Rounds) and about $2^{256}$ checksum computations ( 8 xor operations and 8 modular additions of 64 -bits). In general the cost for one checksum computation is smaller than one compression function evaluation. Depending on the implementation 1 checksum computation is $1 / x$ compression function evaluation. Assume $x=16$, then we can find a collision for Twister slightly faster than brute force search with a complexity of about $2^{252}$ compression function evaluations and negligible memory requirements.

### 4.3 A Remark on the Length Extension Property

Once, we have found a collision, i.e. collision in the iterative part (chaining variables) and the checksum, we can construct many more collisions by appending an arbitrary message block. Note that this is not necessarily the case for a straightforward birthday attack. By applying a birthday attack we construct a collision in the final hash value (after the output transformation $\Omega$ ) and appending a message block is not possible. Hence, we need a collision in the iterative part as well as in the checksum for the extension property. Note that by combining the generic birthday attack and multicollisions, one can construct collisions in both parts with a complexity of about $256 \cdot 2^{256}=2^{264}$ while our attack has a complexity of $2^{252}$.

## 5 A Second-Preimage Attack on Twister-512

In this section, we present a second-preimage for Twister- 512 with complexity of about $2^{384}$ compression function evaluations and memory requirements of $2^{64}$. Assume we want to construct a second preimage for the message $m=$ $m_{1}\|\cdots\| m_{513}$. Then, the attack can be summarized as follows.

1. Construct a $2^{512}$ collision for the first 512 message blocks of Twister-512. This has a complexity of about $512 \cdot 2^{256} \approx 2^{265}$ compression function evaluations (using a birthday attack to construct a collision for each message block) and needs $2^{10}$ memory to save the multicollision. Hence, we get $2^{512}$ values for the checksum which all lead to the same chaining value $H_{512}$.
2. Choose an arbitrary value for the message block $m_{513}$ with correct padding and compute $H_{513}$.
3. In the last iteration of the compression function, $H_{514}=f\left(H_{513}, C\right)$, we first choose arbitrary values for the five checksum words $C_{1}, \ldots, C_{5}$ with $C=C_{1}\|\cdots\| C_{8}$ and compute the state $S_{6}^{F}=H_{513} \oplus S_{3} \oplus S_{6}$. This also determines $S_{10}=H_{514} \oplus S_{6}^{F}$. Note that we know $H_{514}$ from the first preimage.
4. For all $2^{64}$ choices of $C_{8}$ compute backward from $S_{10}$ to the injection of $C_{7}$ and save the $2^{64}$ candidates for state $S_{7}^{\prime}=$ Messagelnjection $\left(\mathrm{S}_{7}, \mathrm{C}_{7}\right)$ in the list $L$.
5. For all $2^{64}$ choices of $C_{6}$ compute forward from $S_{6}$ to the injection of $C_{7}$ and check for match of $S_{7}^{\prime}$ in the list $L$. Since we can still choose $C_{7}$, we only need to match 448 (out of 512) bits. In total, we get $2^{128}$ pairs and this step of the attack will succeed with probability $2^{-448+128}=2^{-320}$. By repeating steps $3-5$ about $2^{320}$ times we can find a match and fulfill this step of the attack with a complexity of about $2^{320+64}=2^{384}$ compression function evaluations.
6. Once we have constructed a second-preimage for the iterative part, we still have to ensure that the value of the checksum $C$ is correct. Therefore, we now use the fact that the checksum of Twister is invertible and we have $2^{512}$ values for the checksum which all lead to the same chaining value $H_{512}$ and hence $H_{513}$ and $H_{514}$. By using a meet-in-the-middle-attack, we can construct the needed value in the checksum. This has a complexity of about $2^{257}$ checksum computations and memory requirements of $2^{256}$. Again the memory requirements can be significantly reduced by using a memory-less variant of the meet-in-the-middle attack [16].

Hence, we can construct a second-preimage for Twister-512 with complexity of about $2^{384}$ and memory requirements of $2^{10}+2^{64}$. The memory requirements can be significantly reduced at the cost of an higher attack complexity. Several time/memory tradeoffs are possible between $2^{384+s}$ compression function evaluations and memory requirements of $2^{10}+2^{64-s}$. Note that our attack requires that the first message consists of at least 513 message blocks. Due to the output transformation of Twister-512, the attack can not be extended to a preimage attack on Twister-512 in a straight-forward way.

## 6 A Preimage Attack on Twister-512

In order to construct a preimage, we have to invert the output transformation of Twister-512. Once we have inverted the output transformation, we can use the second preimage attack described in the previous section to construct a preimage


Fig. 7. The inversion of the first part of the output transformation of Twister
for Twister-512. Suppose we seek a preimage of $h=$ out $_{1}\|\cdots\|$ out $_{8}$ consisting of 513 message block. Then we have to find the chaining value $H_{514}$ such that $\Omega\left(H_{514}\right)=h$.

In the following, we show how to find a $H_{514}$ such that out $t_{1}$ is correct with a complexity of about $2^{8}$ instead of the expected $2^{64}$. This reduces the complexity of inverting the whole output transformation $\Omega$ to about $2^{456}$ instead of the expected complexity of $2^{512}$. The inversion of the first step of the output transformation can be summarized as follows (see also Figure 7):

1. Choose a random value for the first column of $H_{514}$. Use out ${ }_{1}$ and the first column of $H_{514}$ ( 8 bytes each) to compute the first column of $S_{2}$ ( 8 bytes).
2. Compute the 8 bytes $S_{1}^{\prime \prime \prime}[i][1+(9-i) \bmod 8]$ for $(1 \leq i \leq 8)$ of state $S_{1}^{\prime \prime \prime}$ using the first column of $H_{514}$.
3. Compute backward through the Mini-Round $r_{2}$ for the first column of $S_{2}$ to get the diagonal 8 bytes of $S_{1} \oplus H_{514}$.
4. Choose random values for the 8 diagonal bytes of $H_{514}$. Note that this determines the first column of $S_{1}^{\prime \prime \prime}$. Next, compute the 8 diagonal bytes of $S_{1}$ from the diagonal bytes of $H_{514} \oplus S_{1}$ and $H_{514}$ using the feed-forward.
5. Now, we need to connect the states $S_{1}^{\prime \prime \prime}$ and $S_{1}$ through the MixColumns operation of Mini-Round $r_{1}$. Note that the first column of $S_{1}^{\prime \prime \prime}$ is already fixed (due to step 4). If the first byte of $S_{1}[1][1]$ does not match, we need to go back to step 1 again. After repeating steps $1-4$ about $2^{8}$ times we expect to find a match for $S_{1}[1][1]$. Once, we have found a match, we have to modify column 2-8 of $S_{1}^{\prime \prime \prime}$ such that the remaining 7 bytes match as well.
(a) For each column $i=2 \ldots 8$ choose random values for the bytes $S_{1}^{\prime \prime \prime}[i][k]$ with $k \neq 10-i$. Note that the bytes $S_{1}^{\prime \prime \prime}[i][k]$ with $k=10-i$ are already fixed due to step 2 of the attack.
(b) Next, we compute the MixColumns operation and check if the byte $S_{1}[i][i]$ matches. If not, we repeat the previous step. This has a complexity of about $2^{8}$.

Since each column can be modified independently in the attack, finishing this step of the attack has a complexity of about $8 \cdot 2^{8} \approx 2^{11}$ Mini-Round computations.
6. After we have found a match for all columns, we can compute backwards from $S_{1}^{\prime \prime \prime}$ to determine $H_{514}$. Note that values fixed in step 1 and step 4 do not change anymore.

Hence, we can find a $H_{514}$ such that out $t_{1}$ is correct with a total complexity of about $2^{11}$ Mini-Round computations, respectively $2^{8}$ compression function evaluations. By repeating the attack about $2^{448}$ times, we can invert the output transformation of Twister-512 with a complexity of about $2^{438} \cdot 2^{8}=2^{456}$ compression function evaluations and memory requirement of $2^{10}$.

Once we have inverted the output transformation, i.e. we have found the chaining value $H_{514}$ such that $\Omega\left(H_{514}\right)=h$, we can apply the second preimage attack described in the previous section to construct a preimage for Twister512 consisting of 513 message blocks. The attack has a complexity of about $2^{448}+2^{456} \approx 2^{456}$ compression function evaluations and negligible memory requirements.

## 7 Conclusion

In this paper, we have shown two main results: Although Twister is heavily based on a Merkle-Damgård style iteration (as many other hash function like SHA-2), the corresponding reduction proof that reduces the collision resistance of the hash function to the collision resistance of the compression function is not applicable anymore. We show practical (in time and memory) attacks and give an example for a compression function collision. This clearly invalidates the collision resistance assumption of the compression function.

Secondly, we give a theoretical collision, second preimage and preimage attack on the hash function Twister-512. Although the practicality of the proposed attacks might be debatable, it nevertheless exhibits non-random properties that are not present in SHA-512.

## Acknowledgements

The authors wish to thank the designers of Twister for useful comments and discussions. The work in this paper has been supported in part by the European Commission under contract ICT-2007-216646 (ECRYPT II) and by the IAP Programme P6/26 BCRYPT of the Belgian State (Belgian Science Policy).

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## A MixColumns and Inverse MixColumns

The MDS matrix $A$ of the MixColumns operation of Twister and its inverse $B$ are given as follows:

$$
\begin{aligned}
& A=\left(\begin{array}{llllllll}
02 & 01 & 01 & 05 & 07 & 08 & 06 & 01 \\
01 & 02 & 01 & 01 & 05 & 07 & 08 & 06 \\
06 & 01 & 02 & 01 & 01 & 05 & 07 & 08 \\
08 & 06 & 01 & 02 & 01 & 01 & 05 & 07 \\
07 & 08 & 06 & 01 & 02010105 \\
05 & 07 & 08 & 06 & 01 & 020101 \\
01 & 05 & 07 & 08 & 06 & 01 & 0201 \\
01 & 01 & 05 & 07 & 08 & 06 & 01 & 02
\end{array}\right)
\end{aligned}
$$

