# Crypto-analyses on “secure and efficient privacy-preserving public auditing scheme for cloud storage”

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## Abstract

Recently, Worku et al. pointed out that the work “privacy-preserving public auditing for data storage security in cloud computing” proposed by Wang et al. is insecure and their second work “privacy- preserving public auditing for secure cloud the storage” is inefficient. Thus, they offered a secure and efficient-privacy public auditing scheme for cloud storage. They claimed that their system is provably secure in the random oracle model and the operation is effective. However, after crypto-analysis, we found that the scheme cannot reach the security goal, it has the existential forgery attack. We, therefore, alter it to incorporate the desired privacy preserving requirement, which is very significant in a privacy-preserving public auditing protocol for cloud storage.

## 1. Introduction

By NIST’s definition, cloud computing has five essential characteristics, three cloud service models, and four cloud deployment models. Besides, cloud security alliance (CSA) has identified multi-tenants as an important element of cloud [1]. From the statement, we can see that cloud computing environments provide human beings many conveniences, whereas they also bring many problems such as, cloud storage security, due to its multi-tenancy nature and the cloud server may itself be un-trustable. In the privacy-preserving public auditing scheme literature, the users don’t possess the outsourced data physically. Hence, checking the integrity of the outsourced encrypted data on the cloud server becomes important. There have been many cryptographic works within this field roughly named privacy-preserving public auditing for cloud storage system designs [2-17]. In 2014, Worku et al. [2] pointed out that Wang et al.s’ work “privacy-preserving public auditing for data storage security in cloud computing” [3] is insecure and their second work “privacy- preserving public auditing for secure cloud the storage” [4] is inefficient. Therefore, they proposed a secure and efficient-privacy public auditing scheme for cloud storage. They claimed that their

scheme is provably secure in the random oracle model and the performance is efficient. However, after crypto-analysis, we found that the scheme cannot reach the security goal. It has the existential forgery attack. We, therefore, modify it to comprise the desired requirement, which is very important in a privacy-preserving public auditing protocol for cloud storage. We demonstrate it in this article.

## 2. Review of Worku et al.'s auditing scheme

Worku et al.'s public auditing for cloud storage design [2], which adopts the framework of an independent third-party auditor (TPA) to audit the outsourced data when needed as does in [3, 4], consists of four basic algorithms; KeyGen, SigGen, ProofGen and VerifyProof. The used notations can be referred to the original article. We briefly describe them below.

### 2.1 KeyGen

The client generates a random signing key pair *(ssk, spk)*, chooses $x \in_R Z_p$, $u \in_R G$ and computes $v = g^x \in G$. He then uses, *sk =(x, ssk)* as his secret key and *pk =(u, v, g, spk)* as public parameters.

### 2.2 SigGen

The client chooses a random element in $Z_p$ as the file name $F = \{m_i\}_{1 \le i \le n}$ and computes the file tag t as name||Sigssk(name) with signature on name. Subsequently, for each block $m_i \in Z_p$, the user generates a signature $\sigma_i = (H(i) \cdot u^{m_i})^x \in G (1 \le i \le n)$ and sends to the server for storage. Afterwards, the user deletes the file and its corresponding signatures from local storage. Later, when *TPA* wants to start the auditing protocol, he retrieves the file tag *t* for *F* and checks its validity using *spk*. If the proof of t is correct, the client or *TPA* constructs and sends a challenge *chal* to the server. That is, *TPA* picks random elements $c, k_1, k_2$ in $\in Z_p$ and sends $chal = (c, k_1, k_2)$ to the server, where $k_1, k_2$ are randomly chosen as pseudorandom permutation keys by the user for each auditing.

### 2.3 ProofGen

After receiving *chal*, the server determines the subset $I = \{s_j\}$ $(1 \le j \le c)$ of set [1, n] using pseudorandom permutation $\pi_{key}(\cdot)$ as $S_j = \pi_{k_1}(j)$, and also determines

$v_{s_j} = f_{k_2}(j)(1 \le j \le c)$ using pseudorandom function $f_{key}(.)$. Finally, for $i \in I$, the server computes:

$$\mu^* = \sum_{i=s_1}^{s_c} v_i m_i ,$$

$$\sigma = \prod_{i=s_1}^{s_c} \sigma_i^{v_i}$$

Moreover, the server chooses a random $r \in_R Z_p$ for blinding, using the same function $f$, as $r = f_{k3}(chal)$, where $k_3$ is a pseudorandom function key generated by the server for each auditing. It then calculates $R = u^r \in G$, computes $\mu = \mu^* + rh(R) \in Z_p$ and sends $(\mu, \sigma, R)$ to *TPA*.

2.4 VerifyProof(*pk, chal*)

Upon receiving the proof $(\mu, \sigma, R)$, *TPA* computes $S_j = \pi_{k_1}(j)$, $v_{s_j} = f_{k_2}(j)(1 \le j \le c)$, and verifies the proof by checking Eq. (1) below.

$$e(\sigma, g) ? = e(\prod_{i \in I} H(i)^{v_i} \cdot u^{\mu} \cdot R^{-h(R)}, v) \text{ .....Eq. (1)}$$

The correctness of the verification equation can be shown as follows:

$$e(\sigma, g) = \quad e(\prod_{i=s_1}^{s_c} \sigma_i^{v_i}, g) = e(\prod_{i=s_1}^{s_c} (H(i) \cdot u^{m_i})^{x \cdot v_i}, g)$$

$$= e(\prod_{i=s_1}^{s_c} (H(i)^{v_i} \cdot u^{v_i m_i}), g)^x = e(\prod_{i=s_1}^{s_c} (H(i)^{v_i} \cdot u^{\sum_{i=s_1}^{s_c} v_i m_i}, g^x)$$

$$= e(\prod_{i=s_1}^{s_c} (H(i)^{v_i} \cdot u^{\mu^*}, v) = e(\prod_{i=s_1}^{s_c} (H(i)^{v_i} \cdot u^{\mu - rh(R)}, v)$$

$$= e(\prod_{i \in I} H(i)^{v_i} \cdot u^{\mu} \cdot R^{-h(R)}, v)$$

If Eq. (1) holds, the proof $(\mu, \sigma, R)$ is valid.

## 3. The weaknesses

For blinding, the server chooses a random element $r \in_R Z_p$, using the same pseudorandom function, as $r = f_{k3}(chal)$, where $k_3$ is a pseudorandom function key generated by the server for each auditing. It then calculates $R = u^r \in G$ and computes $\mu^* = \sum_{i=s_1}^{s_c} v_i m_i$, $\mu = \mu^* + rh(R) \in Z_p$, and $\sigma = \prod_{i=s_1}^{s_c} \sigma_i^{v_i}$.

Then, the server sends ($\mu$, $\sigma$, R) to *TPA*.

From the received $(\mu, \sigma, R)$, we can see that since $\sigma = \prod_{i=s_1}^{s_c} \sigma_i^{v_i} = \prod_{i=s_1}^{s_c} (H(i)^{v_i} \cdot u^{\sum_{i=s_1}^{s_c} v_i m_i})^x$, a malicious server can regard $v_i s$ as constants and $m_i s$ as variables. He computes $\mu^* = \sum_{i=s_1}^{s_c} v_i m_i$ using the constants $v_i s$ and the message blocks stored. That is, he can obtain an equation containing multiple variables, the $m_i s$, which in mathematics has more than one solution. This means that other than the original $m_i s$, the malicious server can find out the message blocks satisfying the equation without alerting $\sigma$. We take $S_c$=3 as an example. Suppose the values of $v_i s$ are (6, 8, 9), and the values of $m_i s$ are (1, 4, 2) respectively, then the plan can be defined by $6x + 8y + 9z = 56 (= 6m_1^* + 8m_2^* + 9m_3^*)$, where $m_i^*$, *i=1 to 3*, are the forged message blocks. We know that this plane also passes through the point (4, 1, 2). This implies that the malicious server can forge the message blocks from (1, 4, 2) to (4, 1, 2) without alerting the value $\sigma$.

Moreover, due to the independence between $\mu^* (= \sum_{i=s_1}^{s_c} v_i m_i)$ and *R*, after intercepting $(\mu, \sigma, R)$, the attacker can set $R' = u^{r'}$ and $\mu' = \mu^* + r' h(R') \in Z_p$ and sends $(\mu', \sigma, R')$ to *TPA*. *TPA* will accept the verification without detection.

## 4. Modification

From the weaknesses found in section 3, we see that the key point is that the malicious server has the message blocks and the values of $v_i s$. This result in that he

can easily find forged message blocks $m_i^*$ to satisfy the value $\mu^* (= \sum_{i=s_1}^{s_c} v_i m_i^*)$ without alerting the value $\sigma$. Therefore, we must try to break down the linear structure of value $\mu^* (= \sum_{i=s_1}^{s_c} v_i m_i)$. As a result, we set $\mu^* (= \sum_{i=s_1}^{s_c} v_i m_i h(H(m_i \oplus i)))$ and add the relationship into $\mu^*$ and $R$ by setting $\mu = \mu^* + r(h(R) + \mu^*) \in Z_p$ to prevent the found problem. Certainly, we must first let the client's signature $\sigma_i$ on $m_i$ to be $(H(i) \cdot u^{m_i h(H(m_i \oplus i))})^{x \cdot}$.

Accordingly, if a malicious server launches the above attack on our modification; although, he knows the values of $v_i$s and $m_i$s, he cannot break the modification. Thus, the privacy is preserved. The correctness of the verification equation can be shown as follows:

$$e(\sigma, g) = e(\prod_{i=s_1}^{s_c} \sigma_i^{v_i}, g) = e(\prod_{i=s_1}^{s_c} (H(i) \cdot u^{m_i h(H(m_i \oplus i))})^{x \cdot v_i}, g)$$

$$= e(\prod_{i=s_1}^{s_c} (H(i)^{v_i} \cdot u^{v_i m_i h(H(m_i \oplus i))}), g)^x = e(\prod_{i=s_1}^{s_c} (H(i)^{v_i} \cdot u^{\sum_{i=s_1}^{s_c} v_i m_i h(H(m_i \oplus i))}, g^x)$$

$$= e(\prod_{i=s_1}^{s_c} (H(i)^{v_i} \cdot u^{\mu^*}, v) = e(\prod_{i=s_1}^{s_c} (H(i)^{v_i} \cdot u^{\mu - r(h(R) + \mu^*)}, v)$$

$$= e(\prod_{i \in I} H(i)^{v_i} \cdot u^{\mu} \cdot R^{-(h(R) + \mu^*)}, v)$$

## 5. Conclusion

In this paper, we showed that Worku et al.'s work privacy-preserving public auditing for data storage security in cloud computing is flawed. It suffers from the existential forgery attack. For enhancing its security, we therefore modified it to avoid the weaknesses. From the analysis shown in section 4, we see that we have reached the goal of the security promotion.

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