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# Crystallographic texture in an additively manufactured nickel-base superalloy

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## Abstract

Laser-based directed energy deposition was used to additively manufacture a wall out of pre-alloyed powder of a nickel-base superalloy–Inconel 625. The crystallographic texture of the wall has been characterized using neutron diffraction and electron backscatter diffraction. The measured pole figures show a strong Goss texture component ( $\{011\}\langle 100\rangle$ ) plus a comparatively much weaker cube component ( $\{001\}\langle 100\rangle$ ), both indicating that the  $\langle 100\rangle$ -direction of the majority of grains lies along the laser-scanning direction (or the length direction). The origin of the Goss texture is hypothesized to be a result of the preferential  $\langle 100\rangle$ -oriented dendritic solidification driven by the laser-induced heat flow which is affected by the combined effect of laser power, absorption of powder, and laser scanning speed. The texture-induced mechanical softening is also presented. This study aids in understanding the processing-structure-property relationship in additive manufacturing.

Keywords: Texture; Inconel 625; Superalloy; Additive manufacturing; Neutron diffraction.

## **1. Introduction**

Nickel-base superalloys are of particular interest to numerous industries, including the aerospace industry, due to their high strengths and high creep resistance at high temperatures. Among these, Inconel 625 (IN625) is a solid-solution strengthened alloy and is attractive for fabrication by additive manufacturing (AM), owing to the high cost of fabricating its components through traditional subtractive manufacturing methods [1, 2].

Additive manufacturing using metallic powder is a rapidly growing technology in which near-net shape components are built a layer at a time by the deposition, melting, and fusion of subsequent layers of material [3]. In laser-based directed energy deposition (DED), metal powder feedstock is delivered to the desired location through a nozzle that is coaxial with a laser. The laser melts the powder and creates a melt pool in the material below. As the laser advances, the melt pool cools and the metal solidifies and fuses to the layer below. As subsequent layers are deposited to build up a 3D component, the surrounding metal of the part is subjected to rapid thermal cycles, which results in microstructures drastically different from those in wrought counterparts. As such, understanding the influence of AM processing on microstructure and mechanical properties is essential for qualification of the AM process, enabling future engineering designs to take advantage of these new techniques. The present study has focused on neutron diffraction characterization of crystallographic texture present in an IN625 wall made by laser-based DED, as well as the texture-induced mechanical anisotropy.

## **2. Materials and Methods**

### **2.1. Processing by additive manufacturing**

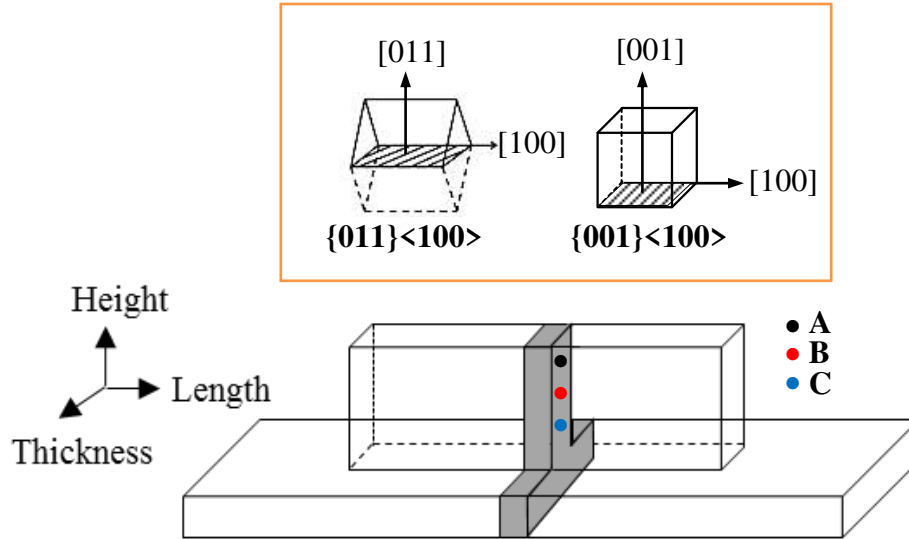
In the present study, a 101 mm long, 28 mm tall, 7 mm thick IN625 wall was deposited by laser-based DED, with pre-alloyed IN625 powder, onto an annealed Inconel 625 (AN IN625)

substrate plate (measuring 152.4 mm long, 38.1 mm wide and 12.7 mm thick) [4]. A laser power of 2 kW (IPG Photonics YLR-12000) with a scanning speed of 10.6 mm/s was used to deposit the powder, which was delivered by a cladding head (Precitec YC-50) at a powder feed rate of 16 g/min in an argon gas flow of 9.4 L/min. The wall was constructed from 3-bead wide depositions (or 3 passes) for each layer, with a bead thickness of ~0.89 mm and a step-over of ~2.29 mm. The deposition direction changes based on layer number, with even numbered layers deposited in the opposite direction of odd numbered layers. All three passes within a single layer were deposited along the length direction. More details of the AM process have been described elsewhere [5].

The spherical IN625 powder were made by gas atomization and sieved using -100/+325 meshes, providing a powder diameter range from 44 to 149  $\mu\text{m}$ . The elemental compositions of the IN625 powder are listed in Table 1, and the AM IN625 wall is schematically shown in Figure 1, with respect to three orthogonal directions along the height (H or HD), the thickness (T or TD) and the length (L or LD), respectively.

**Table 1.** Nominal composition (wt.%) of Inconel 625 used for Additive Manufacturing.

Ni	Cr	Mo	Fe	Nb+Ta	Co	Mn
59.78	21.51	8.75	4.58	3.49	0.28	0.26
Si	Ti	Al	C	P	S	
0.25	0.24	0.19	0.027	<0.005	<0.002	



**Figure 1.** Schematic of the IN625 wall made by laser DED on top of an IN625 substrate plate. The shaded region was removed from the wall and substrate for characterization of texture. Letters (A, B and C) mark the locations where texture was measured by neutron diffraction. The top inset shows the Goss texture component ( $\{011\}\langle 100\rangle$ ) and the cube texture component ( $\{001\}\langle 100\rangle$ ) with respect to the sample coordinate system.

## 2.2 Microstructural characterization

For microstructural evaluation, the samples extracted from the annealed IN625 substrate plate and from the as-deposited AM-IN625 wall were polished using standard metallographic procedures. These samples were examined in a scanning electron microscope (SEM, FEI Quanta 200). Electron backscatter diffraction (EBSD) was used to determine grain sizes, orientations, and shapes in a random cross-section of annealed IN625 and in three cross-sections of AM-IN625 which are normal to the LD, TD and HD, respectively.

## 2.3 Texture characterization by neutron diffraction

As shown by the shaded region in Figure 1, a representative  $\sim 7.0$  mm thick slice was extracted from the AM IN625 wall. Texture characterization was conducted at three depths with

respect to the top of the wall, which are 7 mm apart and marked as A, B and C. Time-of-flight neutron diffraction characterization of the texture was carried out on VULCAN, the Engineering Diffractometer at the Spallation Neutron Source, Oak Ridge National Laboratory [6]. VULCAN has two detector banks, centered at scattering angles of  $\pm 90^\circ$  to the incident neutron beam, enabling simultaneous measurements of two perpendicular scattering vectors. More details of VULCAN's instrumentation and experimental setup can be found elsewhere [7, 8].

In order to obtain full pole figures, two orthogonal rotations of the sample were implemented by the sample stage and a goniometer (HROT) attached to the stage. In the present measurement, the rotation about the vertical axis,  $\Omega$ , was conducted through the sample stage by a step of  $5^\circ$  ranging from  $\pm 45^\circ$  to  $\pm 90^\circ$  with respect to the incident beam, while the horizontal rotation,  $\Phi$ , was implemented by the HROT goniometer by a step of  $30^\circ$  ranging from  $0^\circ$  to  $360^\circ$ . The piece extracted from the AM IN625 wall (see Fig. 1) was centered onto a holder with the wall thickness direction parallel to the HROT's rotation axis. A total of 120 sample positions ( $\Omega$ ,  $\Phi$ ) were measured with a neutron data collection time of 2 minutes for each position. GSAS-based single-peak fitting was used to obtain integrated intensities of selected reflections (or poles) in each diffraction pattern. Pole figures were then obtained by representing the integrated peak intensities, after appropriate normalization as well as corrections of sample absorptions and sampling volumes for each sample position, as a function of the polar coordinates ( $\chi$ ,  $\varphi$ ) that are converted from corresponding ( $\Omega$ ,  $\Phi$ ) with respect to each detector bank [9, 10].

## **2.4 Mechanical deformation**

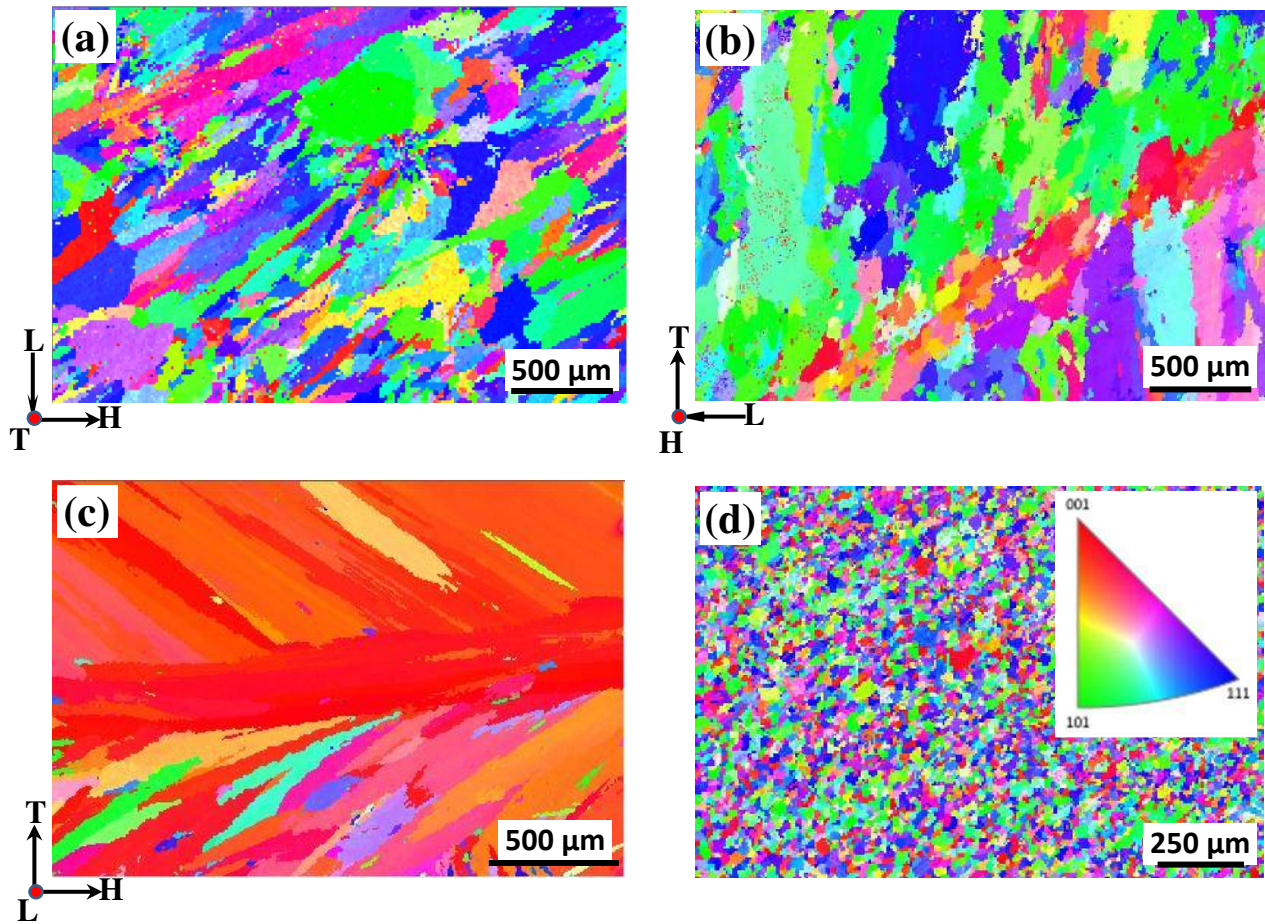
Cylindrical specimens (5 mm diameter and 10 mm long) were extracted using wire electrical discharge machining (EDM) from the AM-IN625 wall (at the depth similar to that of

Location A) with the cylinder axis lying along the LD, as well as from the annealed IN625 substrate plate. These specimens were compressed at a strain rate of  $\sim 2.5 \times 10^{-5} \text{ s}^{-1}$  at room temperature using a MTS load frame with a pair of high-density alumina platens. Engineering strains were calculated from the relative cross-head displacements after corrections of the machine compliance. The samples were not polished for mechanical testing. The ends of the samples were machined with milling in order to ensure that the end faces of the EDM-cut samples are parallel and perpendicular to the load axis. Carbon films were applied between each end surface and the platen, which served as a lubricant during deformation to minimize barreling.

Compression tests provide us with a large available plastic strain regime before localization compared with tension. Compression tests also provide a uniform stress state, as opposed to bending, which would result in a gradient of stress states across the gage section. The specimen aspect ratio of 2:1 and the applied strain rate are commonly used for compression tests to avoid buckling and barreling. Therefore, compression testing provides us with a uniform large deformation range for studying plastic deformation up to a plastic strain of  $\sim 10\%$ .

### **3. Results**

Figures 2(a), 2(b) and 2(c) depict three typical EBSD maps of AM IN625 obtained from cross-sections perpendicular to the TD, HD and LD, respectively, indicative of elongated grains with a high aspect ratio ranging from 2.5 to 4.3 and preferred orientations. In comparison, Fig. 2(d) shows an EBSD map of annealed IN625 obtained from a random cross-section, indicative of equiaxed grains with much smaller sizes and randomly distributed orientations.

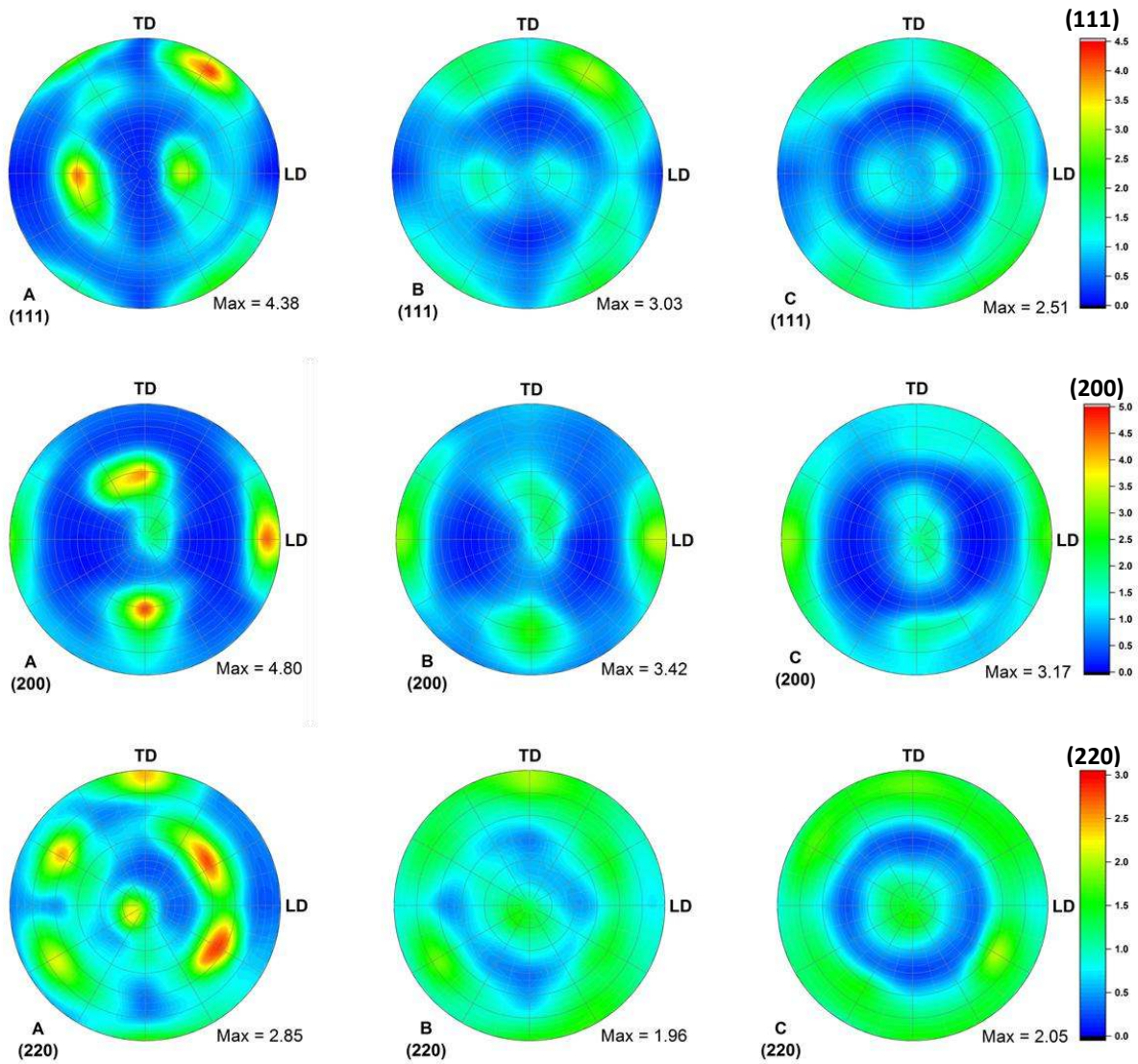


**Figure 2.** EBSD maps of (a) the cross-section (near location A) whose normal is parallel to the thickness (T) direction of AM-IN625, (b) the cross-section (near location A) whose normal is parallel to the height (H) direction of AM-IN625, and (c) the cross-section (near location B) whose normal is parallel to the length (L) direction of AM-IN625 and (d) a representative cross-section of annealed IN625. In all plots, the colors represent the  $hkl$  plane normals coming out of the page.

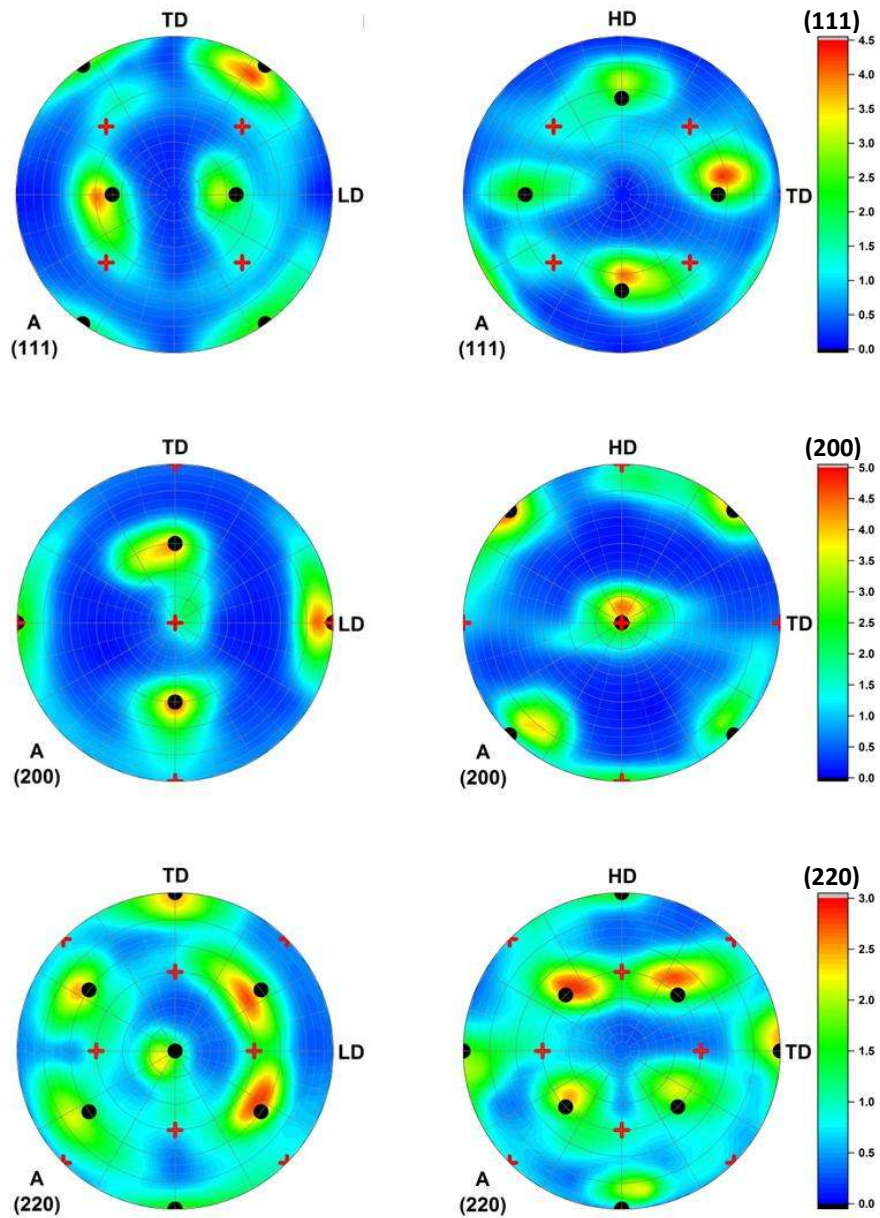


Figure 3 shows the (200), (220) and (111) pole figures determined for locations A, B and C, with HD being aligned to the center of the pole figures while LD and TD are the horizontal and vertical axes, respectively. Using an identical intensity color scale for each type of pole figure, Fig. 3 demonstrates dramatic strengthening of texture as deposition advances from location C to A. For identification of the texture components, both HD-centered and LD-centered pole figures for location A are presented in Fig. 4, where the ideal pole locations of the  $\{011\}\langle 100\rangle$  (Goss) texture are marked as filled circles. The observed texture maxima match very well with the ideal Goss distribution of poles, indicating that, within a small angular deviation, the predominant texture component at location A is of Goss type. For instance, this is clearly visible in the HD-centered (220) pole figure which shows a texture maximum in the center, indicative of  $\langle 110\rangle//\text{HD}$ , while in the LD-centered (200) pole figure, the presence of a strong maximum in the center indicates  $\langle 100\rangle//\text{LD}$ . An additional weak component can be also identified, which is attributed to the minority  $\{100\}\langle 001\rangle$  (Cube) texture component, as marked as red crosses in Fig. 4.

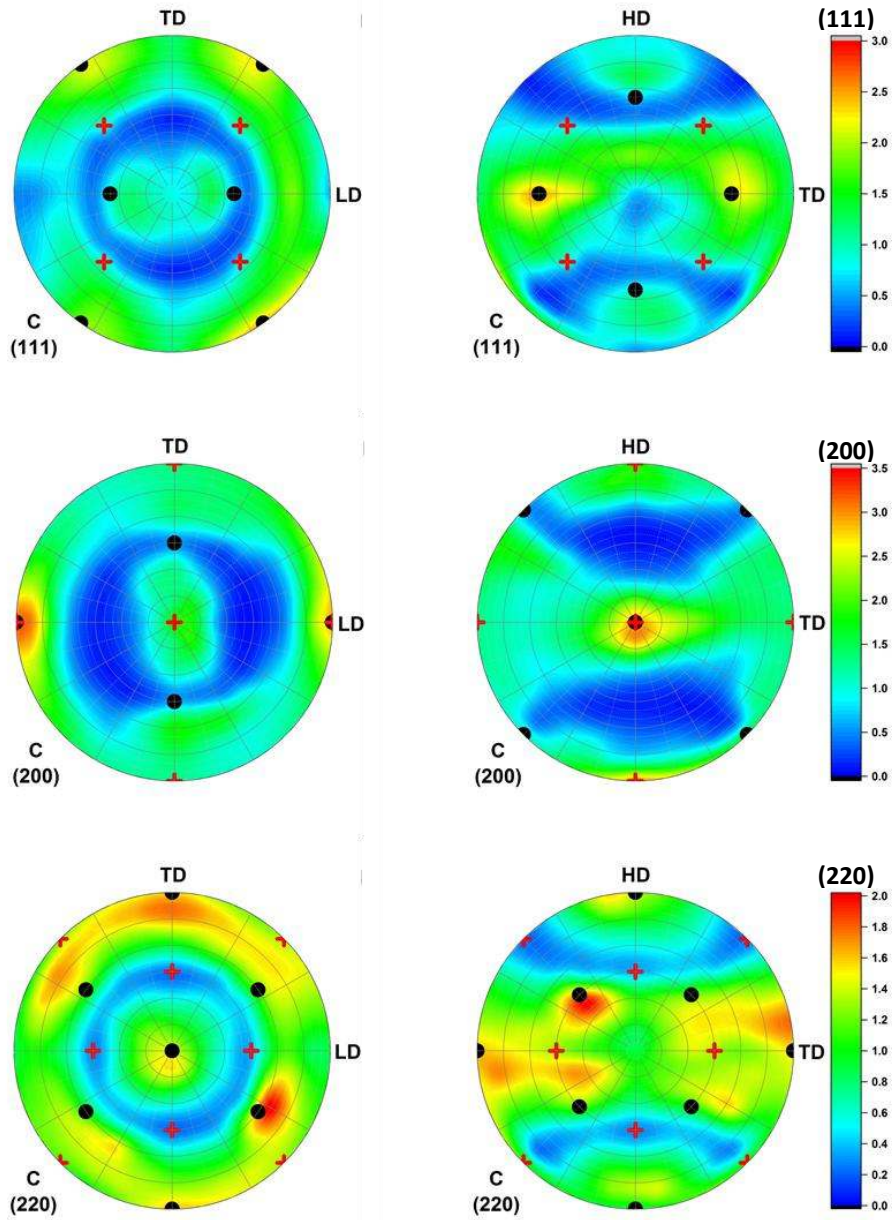
The texture features characteristic of location A are significantly reduced toward locations B and C. Figure 5 illustrates in more details the HD-centered and LD-centered pole figures corresponding to location C. Broader fiber type features are evident in the HD-centered pole figures. The central texture maxima of the (200) and (220) pole figures suggest  $\langle 100\rangle$  as the fiber axis. For comparison, the ideal locations of  $\{100\}\langle 001\rangle$  (Cube) texture components are also included in Fig. 5. It can be concluded that the  $\langle 100\rangle //\text{HD}$  fiber encompasses a rather large angular range of crystallographic directions around  $\langle 100\rangle$  while the Goss component still has an important contribution.



**Figure 3.** (111), (200) and (220) pole figures of the AM build determined for locations A, B and C, respectively. LD denotes the length direction, TD is the thickness direction, and the center of the pole figures is the height direction (HD).



**Figure 4.** (111), (200) and (220) pole figures determined at location A, being centered on HD (left columns) and LD (right columns), respectively. Filled circles denote the  $\{011\}\langle 100\rangle$  (Goss) texture component, and red crosses represent the  $\{001\}\langle 100\rangle$  (Cube) texture component.



**Figure 5.** (111), (200) and (220) pole figures determined at location C, being centered on HD (left columns) and LD (right columns), respectively. Filled circles denote the  $\{011\}\langle 100\rangle$  (Goss) texture component, and red crosses represent the  $\{001\}\langle 100\rangle$  (Cube) texture component.

#### 4. Discussion

Table 2 provides a summary of the texture components observed in Inconel 718 (IN718) and IN625 made by two types of AM techniques, *i.e.*, laser-based DED and electron beam freeform fabrication (EBF<sup>3</sup>). While the Goss component observed in IN625 in the present study is consistent with that in IN718 made by EBF<sup>3</sup> as reported by Tayon *et al.* [11], it is distinctly different from that of the *rotated* cube texture component found in both IN718 and IN625 also made by laser-based DED [12, 13]. As pointed out by Dinda *et al.* [13] and Wei *et al.* [14], the rotated cube texture was due to the formation of zigzag-shaped <100>-oriented columnar grains across neighboring layers that underwent alternating forward and backward depositions; these preferentially oriented grains resulted from the <100>-oriented primary dendritic solidification driven by the heat flow, which was generated by the advancing of laser-melted pool and was aligned at ~45°-60° to the substrate or previous deposited layers. In contrast, the Goss component observed in AM IN625 in the present study indicates that, during solidification, columnar dendrites grew along one of the <100>-directions that was nearly parallel to the laser-scanning direction while the other two <001> directions are aligned at ~45° to the substrate. Accordingly, the heat flow direction in the present AM case is distinctly different from that of aligning at ~45°-60° to the laser scanning direction as reported by Dinda *et al.* [13] and Wei *et al.*[14]. In what follows, we hypothesize that the combined effects of laser power, absorption of powder, and laser scanning speed affect the predominant direction of heat flow which drives dendritic growth, accounting for solidification texture variations.

While there is no single parameter that can capture the differences in thermal history between additively manufactured components made using different processing parameters and conditions, a typical method for comparing studies is to compute the linear heat input used. The

linear heat input is defined as the laser power divided by the scanning speed. However, given that the present study used a Nd:YAG laser, and the studies in [12-14] used a CO<sub>2</sub> laser, the actual energy available to melt the substrate (or effective energy input) would differ for the same linear heat input because the absorptivity of Ni for these two laser wavelengths differs. As shown in Table 2, the absorptivity of a CO<sub>2</sub> ( $\lambda = 10.6 \mu\text{m}$ ) is significantly lower than that of Nd:YAG laser ( $\lambda = 1.06 \mu\text{m}$ ), meaning that, for the same linear heat input, less of the energy from a CO<sub>2</sub> laser is absorbed by the solid material, therefore, there is a lower effective energy input. Additionally, while the absorptivity of electron beams is not well defined, photons are either reflected or absorbed within a few nanometers of the surface of a material, while the kinetic energy of electrons is deposited a few  $\mu\text{m}$  below the surface of a material, indicating a more efficient transfer of energy in EBM versus laser deposition [15].

Based on the work by Wei *et al.* [14], the angle,  $\theta$ , between the heat flow direction, which is nearly opposite to the <100>-dendritic growth direction, and the laser scanning direction at the solid-liquid interface can be written as:  $\cos \theta = \frac{\frac{\partial T}{\partial x}}{\sqrt{\left(\frac{\partial T}{\partial x}\right)^2 + \left(\frac{\partial T}{\partial z}\right)^2}}$ , where  $T$  is temperature,  $x$  and  $z$  are the axes pointing to the laser scanning direction and the build height direction, respectively,  $\frac{\partial T}{\partial x}$  is the partial temperature gradient along the laser scanning direction and  $\frac{\partial T}{\partial z}$  is the partial temperature gradient along the height direction. As inferred from the three-dimensional heat transfer and material flow model and simulations by Manvatkar and DebRoy [16], the increase in laser power and absorptivity of powder at the same scanning speed leads to the increase in the rate of heat input (i.e., effective energy input), increasing the pool depth/volume, thus reducing  $\frac{\partial T}{\partial z}$ . On the other hand, a higher laser scanning speed at the same

efficient energy input increases  $\frac{\partial T}{\partial x}$ . As such,  $\theta$  is reduced significantly in our case with respect to those reported by Dinda *et al.* [12, 13] and Wei *et al.* [14], due to the application of much higher efficient energy input and higher scanning speed, causing the <100>-dendritic growth more inclined to the laser scanning direction and resulting in the Goss texture. Another factor affecting the heat flow direction is the dependency of  $\frac{\partial T}{\partial z}$  on the position (or height) of the deposition layers, with subsequent or higher-level layers exhibiting smaller  $\frac{\partial T}{\partial z}$ , owing to the increased temperature of the build; this may explain why the Goss component at location A is much stronger than those at locations B and C.

Multi-pass depositions used in the present study may also contribute to the difference in the heat flow direction, especially along the thickness direction. In addition, the weak cube texture component present in AM IN625 may also originate from the application of multi-passes, which produced <100>-oriented dendrites/grains sandwiched between two neighboring passes but elongated along the HD, as shown in Fig. 2(c).

As mentioned above, the cylindrical compression sample of AM IN625 was cut at a depth similar to that of Location A such that the axial axis was parallel to the length direction of the AM IN625 wall. Thus, the majority of the grains, belonging to either the Goss or the Cube component, were aligned along the sample-axial axis, forming essentially a <100>-type fiber texture with respect to the loading axis during the compression tests. As pointed out by Chin and Mammel [17], for  $\{111\}$ <110> slip in the axisymmetric flow case, fiber textures near the <100> orientation are expected to be ~50% weaker than for orientations near <111> and/or <110>, as a result of having much smaller Taylor factors for grains whose plane normals are near the <100> orientation. This largely explains why, when comparing with the texture-free, annealed IN625, the AM-IN625 samples exhibit a smaller yield stress as well as a lower work-hardening rate, as

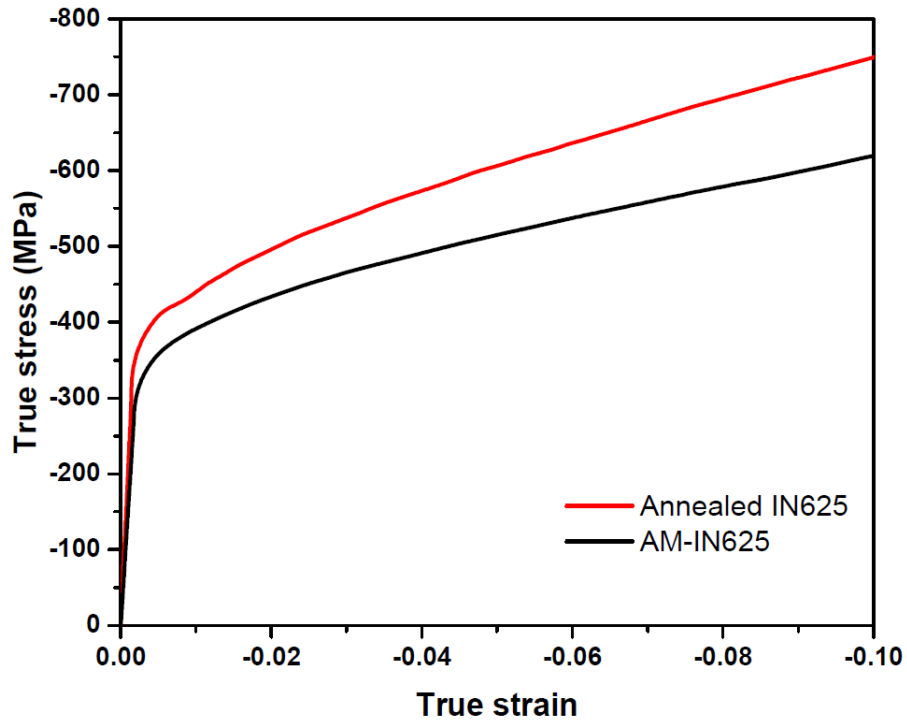
determined from the stress-strain curves in Fig. 6 and listed in Table 3. The  $\langle 100 \rangle$  texture in AM-IN625 also accounts for the decrease in Young's modulus, which is  $\sim 27\%$  smaller than that of annealed IN625 [18]. The texture also drastically affects the thermomechanical stability of AM IN625 when plastically deformed at elevated temperatures [19].

**Table 2.** Comparison of textures observed in IN718 and IN625 made by AM.

AM	Alloy	Laser Type & Power	Scan Speed (mm/s)	Absorptivity	Effective energy input (J/mm)	Texture	Ref.
Laser-DED	IN718	CO <sub>2</sub> 750W	6.25	0.05-0.15 <sup>†</sup>	$\sim 12$	<i>Rotated</i> cube [011]//HD [01 $\bar{1}$ ]//LD [100]//TD	[13, 14]
Laser-DED	IN625	CO <sub>2</sub> 900W	5.0	0.05-0.15 <sup>†</sup>	$\sim 18$	<i>Rotated</i> cube [011]//HD [01 $\bar{1}$ ]//LD [100]//TD	[12]
Laser-DED	IN625	Nd:YAG 2,000W	10.6	0.15-0.35 <sup>†</sup>	$\sim 47$	Goss (predominant) + cube (weak)  Goss- $\{011\}\langle 100 \rangle$ [011]//HD [100]//LD [01 $\bar{1}$ ]//TD  Cube- $\{001\}\langle 100 \rangle$ [001]//HD [100]//LD [010]//TD	This work
EBF <sup>3</sup>	IN718	High-power Electron Beam	32	–	–	Goss- $\{011\}\langle 100 \rangle$ [011]//HD [100]//LD [01 $\bar{1}$ ]//TD	[11]

<sup>†</sup> Data from Ref. [20]





**Figure 6.** True stress-strain curves of AM IN625 and annealed IN625 determined under compression at room temperature.

**Table 3.** Comparison of mechanical properties between AM IN625 and annealed IN625.

	Young's Modulus (GPa)	Yield Strength (0.2% offset, MPa)	Work-hardening rate* (MPa per 1% strain)
AM-IN625	152±8	352±18	21.5±0.2
Annealed IN625	207±11	395±20	29.8±0.3

\*Value determined between plastic strains of 3% and 10%.

## 5. Summary and Conclusions

Crystallographic texture in an additively manufactured Inconel 625 superalloy has been characterized by neutron diffraction and EBSD, showing that:

- (1) A Goss component ( $\{011\}\langle 100\rangle$ ) is predominant, originating from solidification of  $\langle 100\rangle$ -oriented dendrites/grains driven by the high power laser-induced heat flow, which is locally perpendicular to the laser scanning direction while aligned at  $45^\circ$  to the substrate or previous-deposited layers.
- (2) A comparatively much weaker cube component ( $\{001\}\langle 100\rangle$ ) is also present, whose magnitude varies depending on the depths of deposited layers from the substrate.
- (3) Both texture components contribute to  $\langle 100\rangle$ -oriented grains preferentially lying along the length direction, giving rise to significant texture-induced softening in comparison with its texture-free counterpart (annealed IN625).

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