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Radovan Dermisek, Stuart Raby, Leszek Roszkowski, Roberto Ruiz de Austri

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# Dark Matter And $B_s ightarrow \mu^+ \mu^-$ With Minimal $SO_{10}$ Soft SUSY Breaking

#### Radovan Dermíšek

Davis Institute for High Energy Physics, University of California, Davis, CA 95616, USA E-mail: dermisek@physics.ucdavis.edu

#### Stuart Raby

Department of Physics, The Ohio State University, 174 W. 18th Ave., Columbus, Ohio 43210, USA; On leave of absence, School of Natural Sciences, Institute for Advanced Study, Princeton, NJ 08540, USA E-mail: raby@pacific.mps.ohio-state.edu

#### Leszek Roszkowski

Department of Physics, Lancaster University, Lancaster LA1 4YB, England E-mail: L.Roszkowski@lancaster.ac.uk

#### Roberto Ruiz de Austri

Physics Division, School of Technology, Aristotle University of Thessaloniki, GR - 540 06 Thessaloniki, Greece E-mail: rruiz@gen.auth.gr

ABSTRACT: CMSSM boundary conditions are usually used when calculating cosmological dark matter densities. In this paper we calculate the cosmological density of dark matter in the MSSM using minimal  $SO_{10}$  soft SUSY breaking boundary conditions. These boundary conditions incorporate several attractive features: they are consistent with  $SO_{10}$  Yukawa unification, they result in a "natural" inverted scalar mass hierarchy and they reduce the dimension 5 operator contribution to the proton decay rate. With regards to dark matter, on the other hand, this is to a large extent an unexplored territory with large squark and slepton masses  $m_{16}$ , large  $A_0$  and small  $\{\mu, M_{1/2}\}$ . We find that in most regions of parameter space the cosmological density of dark matter is considerably less than required by the data. However there is a well-defined, narrow region of parameter space which provides the observed relic density of dark matter, as well as a good fit to precision electroweak data, including top, bottom and tau masses, and acceptable bounds on the branching fraction of  $B_s \to \mu^+ \mu^-$ . We present predictions for Higgs and SUSY spectra, the dark matter detection cross section and the branching ratio  $BR(B_s \to \mu^+ \mu^-)$ in this region of parameter space. KEYWORDS: Supersymmetric Effective Theories, Cosmology of Theories beyond the SM, Dark Matter.

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## 1. Introduction

The constrained minimal supersymmetric standard model [CMSSM] [1] is a well defined model for soft SUSY breaking with five independent parameters given by  $m_0$ ,  $M_{1/2}$ ,  $A_0$ ,  $\tan \beta$  and  $sign(\mu)$ . It has been used extensively for benchmark points for collider searches, as well as for astrophysical and dark matter analyses. The economy of parameters in this scheme makes it a useful tool for exploring SUSY phenomena. However the CMSSM may miss regions of soft SUSY breaking parameter space which give qualitatively different predictions. In this paper we consider an alternate scheme, the minimal  $SO_{10}$  supersymmetric model [MSO<sub>10</sub>SM], which is well motivated and opens up a qualitatively new region of parameter space.

In the MSO<sub>10</sub>SM there are 7 soft SUSY breaking parameters  $\mu$ ,  $M_{1/2}$ ,  $A_0$ ,  $\tan \beta$ ,  $m_{16}$ (a universal squark and slepton mass),  $m_{10}$  (a universal Higgs mass) and  $\Delta m_H^2$  (Higgs up/down mass splitting). Moreover the parameters  $A_0$ ,  $m_{10}$ ,  $m_{16}$  must satisfy the constraints [2, 3, 4]  $A_0 \approx -2 m_{16}$ ,  $m_{10} \approx \sqrt{2} m_{16}$ ,  $m_{16} > 1.2$  TeV with  $\mu$ ,  $M_{1/2} \ll m_{16}$  and  $\tan \beta \approx 50$ . Note, with these values of the soft SUSY breaking parameters, we can explore SUSY phenomena with qualitatively different behavior than in the CMSSM. This is mainly due to the Higgs splitting ( $\Delta m_H^2$ ) which, as is well known [5], enables one to obtain electroweak symmetry breaking with values  $m_{16} \gg \mu$ ,  $M_{1/2}$ . Also, radiative EWSB with  $\tan \beta \approx 50$  requires significantly less fine tuning with Higgs mass splitting (see Rattazzi and Sarid [5]). Furthermore, with 3 Higgs mass parameters  $\mu$ ,  $m_{10}$ , and  $\Delta m_H^2$  we find that the latter two are strongly constrained by EWSB, once we fix the value of  $\mu$ , which we treat as a free parameter. This is unlike the CMSSM where  $\mu$  is fixed by EWSB. Also note that small changes in  $\Delta m_H^2$  lead to big changes in the CP odd Higgs mass  $m_A$  [2].

It is not at all obvious that the  $MSO_{10}SM$  region of soft SUSY breaking parameter space is consistent with cosmology [3, 4].<sup>1</sup> The dark matter candidate in this model is

<sup>&</sup>lt;sup>1</sup>See also other recent articles discussing Yukawa unification and dark matter [6, 7]

the lightest neutralino. However, since the scalar masses of the first two families are of order  $m_{16} > 1.2$  TeV, and the third generation sfermions (except for the stops) also tend to be heavy, the usually dominant annihilation channels, for the neutralino LSP to light fermions via *t*-channel sfermion exchange, are suppressed. On the other hand, the process  $\chi\chi \to f\bar{f}$  via *s*-channel *A* exchange becomes important. This is due to the enhanced CP odd Higgs coupling to down-type fermions, which is proportional to tan  $\beta$ , and because, in contrast to heavy scalar exchange, the process is not *p*-wave suppressed. In an earlier analysis, our  $\chi^2$ -analysis favored a light CP odd Higgs mass  $m_A \sim 100$  GeV [2], although heavier *A* were also allowed. Such light *A* are however disfavored for two reasons. In order to provide efficient annihilation for the LSPs, one would be squeezed into a rather low LSP mass region  $m_{\chi} \approx m_A/2$ , which would require extreme fine-tuning at best. In addition, such low  $m_A$  are anyway inconsistent with the current limits on BR( $B_s \to \mu^+ \mu^-$ ). In this analysis, we vary the *A* mass.

We study the cosmology of the MSO<sub>10</sub>SM in this paper. Obtaining the observed relic abundance of cold dark matter, which along with other cosmological parameters has recently been determined with an unprecedented accuracy [8], will provide a new important constraint on the model. We also compute the branching ratio for the process  $B_s \rightarrow \mu^+ \mu^$ due to A exchange [9]. It is absolutely essential to include this latter constraint in our analysis. Note, the CDF bound BR $(B_s \rightarrow \mu^+ \mu^-) < 2.6 \times 10^{-6}$  [10]. The cross section for the direct detection of dark matter is also computed. In section 2 we define the MSO<sub>10</sub>SM, describe its virtues and outline the analysis. In section 3 we compute the cosmological dark matter density and discuss our results. Then in section 4 we discuss our predictions for underground dark matter searches and for collider Higgs and SUSY searches.

## 2. Minimal $SO_{10}$ SUSY Model – $MSO_{10}SM$

#### 2.1 Framework

Let us define the minimal  $SO_{10}$  SUSY model. Quarks and leptons of one family reside in the **16** dimensional representation, while the two Higgs doublets of the MSSM reside in one **10** dimensional representation. For the third generation we assume the minimal Yukawa coupling term given by

$$\lambda$$
 **16 10 16**. (2.1)

On the other hand, for the first two generations and for their mixing with the third, we assume a hierarchical mass matrix structure due to effective higher dimensional operators. Hence the third generation Yukawa couplings satisfy  $\lambda_t = \lambda_b = \lambda_\tau = \lambda_{\nu_\tau} = \lambda$ .

Soft SUSY breaking parameters are also consistent with  $SO_{10}$  with

- a universal gaugino mass  $M_{1/2}$ ,
- a universal squark and slepton mass  $m_{16}$ ,<sup>2</sup>

 $<sup>^{2}</sup>SO_{10}$  does not require all sfermions to have the same mass. This however may be enforced by non-abelian family symmetries or possibly by the SUSY breaking mechanism.

- a universal scalar Higgs mass  $m_{10}$ ,
- and a universal A parameter  $A_0$ .

In addition we have the soft SUSY breaking Higgs mass parameters  $\mu$  and  $B\mu$ .  $B\mu$  may, as in the CMSSM, be exchanged for tan  $\beta$ . Note, not all of these parameters are independent. Indeed, in order to fit the low energy electroweak data, including the third generation fermion masses, it has been shown that  $A_0$ ,  $m_{10}$ ,  $m_{16}$  must satisfy the constraints [2]

$$\begin{array}{l}
A_0 \approx -2 \ m_{16} \\
m_{10} \approx \sqrt{2} \ m_{16} \\
m_{16} > 1.2 \ \text{TeV} \\
\mu, \quad M_{1/2} \ll m_{16}
\end{array}$$
(2.2)

with

$$\tan\beta \approx 50. \tag{2.3}$$

This result has been confirmed in two recent analyses [3, 4].<sup>3</sup> The first property (Eqn. (2.2)) is necessary to fit the top, bottom and  $\tau$  masses, in addition to the precision electroweak data [2, 3, 4]. The second property (Eqn. (2.3)) is a consequence of third generation Yukawa unification, since  $m_t(m_t)/m_b(m_t) \sim \tan \beta$ .

One loop threshold corrections at the GUT scale lead to two significant parameters we treat as free parameters, although they are calculable in any GUT. The first is a correction to gauge coupling unification given by

$$\epsilon_3 \equiv \left[\alpha_3(M_G) - \tilde{\alpha}_G\right] / \tilde{\alpha}_G \tag{2.4}$$

where the GUT scale  $M_G$  is defined as the scale where  $\alpha_1(M_G) = \alpha_2(M_G) \equiv \tilde{\alpha}_G$ . The second is a Higgs splitting mass parameter defined by

$$\Delta m_H^2 \equiv (m_{H_d}^2 - m_{H_u}^2)/2m_{10}^2. \tag{2.5}$$

In order to fit the low energy data we find  $\epsilon_3 \approx -4\%$  and  $\Delta m_H^2 \approx 13\%$  [2]. The largest corrections to  $\epsilon_3$  come from the Higgs and  $SO_{10}$  breaking sectors, while the correction to  $\Delta m_H^2$  is predominantly due to the right-handed  $\tau$  neutrino. For  $M_{\bar{\nu}_{\tau}} \approx 10^{13-14}$  GeV (appropriate for a light  $\tau$  neutrino mass  $\approx 0.06$  eV) we obtain  $\Delta m_H^2 \approx 10 - 7\%$ .

Finally, as a bonus, these same values of soft SUSY breaking parameters, with  $m_{16} \gg$  TeV, result in two very interesting consequences. Firstly, it "naturally" produces an inverted scalar mass hierarchy [ISMH] [12]. With an ISMH squarks and sleptons of the first two generations obtain mass of order  $m_{16}$  at  $M_Z$ . The stop, sbottom, and stau, on the other hand, have mass less than a TeV. An ISMH has two virtues.

1. It preserves "naturalness" (for values of  $m_{16}$  which are not too large), since only the third generation squarks and sleptons couple strongly to the Higgs.

 $<sup>^{3}</sup>$ Note, different regions of parameter space consistent with Yukawa unification have also been discussed in [3, 4, 11]

2. It ameliorates the SUSY CP and flavor problems, since these constraints on CP violating angles or flavor violating squark and slepton masses are strongest for the first two generations, yet they are suppressed as  $1/m_{16}^2$ . For  $m_{16} > a$  few TeV, these constraints are weakened [13].

Secondly, Super–Kamiokande bounds on  $\tau(p \to K^+ \bar{\nu}) > 1.9 \times 10^{33}$  yrs. [14] constrain the contribution of dimension 5 baryon and lepton number violating operators. These are however minimized with  $\mu$ ,  $M_{1/2} \ll m_{16}$  [15].

#### 2.2 Analysis

We use a top-down approach with a global  $\chi^2$  analysis [16]. The input parameters are defined by boundary conditions at the GUT scale. The 11 input parameters at  $M_G$  are given by — three gauge parameters  $M_G$ ,  $\alpha_G(M_G)$ ,  $\epsilon_3$ ; the Yukawa coupling  $\lambda$ , and 7 soft SUSY breaking parameters  $\mu$ ,  $M_{1/2}$ ,  $A_0$ ,  $\tan \beta$ ,  $m_{16}^2$ ,  $m_{10}^2$ ,  $\Delta m_H^2$ . These are fit in a global  $\chi^2$  analysis defined in terms of physical low energy observables. Note we keep three parameters  $(m_{16}, \mu, M_{1/2})$  fixed; while minimizing  $\chi^2$  with the remaining 8 parameters. Below we will plot  $\chi^2$  contours as a function of  $\mu$ ,  $M_{1/2}$  for different values of  $m_{16}$ . We use two (one) loop renormalization group [RG] running for dimensionless (dimensionful) parameters from  $M_G$  to  $M_Z$ .<sup>4</sup> We require electroweak symmetry breaking using an improved Higgs potential, including  $m_t^4$  and  $m_b^4$  corrections in an effective 2 Higgs doublet model below  $M_{SUSY} = \sqrt{\frac{1}{2}(m_{\tilde{t}_1}^2 + m_{\tilde{t}_2}^2)}$  [17].

The  $\chi^2$  function includes 9 observables; 6 precision electroweak data  $\alpha_{EM}$ ,  $G_{\mu}$ ,  $\alpha_s(M_Z)$ ,  $M_Z$ ,  $M_W$ ,  $\rho_{NEW}$  and the 3 fermion masses  $M_{top}$ ,  $m_b(m_b)$ ,  $M_{\tau}$ . In our analysis we fit the central values [18]:  $M_Z = 91.188$  GeV,  $M_W = 80.419$  GeV,  $G_{\mu} \times 10^5 = 1.1664$  GeV<sup>-2</sup>,  $\alpha_{EM}^{-1} = 137.04$ ,  $M_{\tau} = 1.7770$  GeV with 0.1% numerical uncertainties; and the following with the experimental uncertainty in parentheses:  $\alpha_s(M_Z) = 0.1180 (0.0020)$ ,  $\rho_{new} \times 10^3 = -0.200 (1.1)$  [20],  $M_t = 174.3 (5.1)$  GeV,  $m_b(m_b) = 4.20 (0.20)$  GeV.<sup>5</sup> We include the complete one loop threshold corrections at  $M_Z$  to all observables. In addition we use one loop QED and three loop QCD RG running below  $M_Z$ .

The output of this analysis is a set of weak scale squark, slepton, gaugino and Higgs masses. With regards to the calculated Higgs and sparticle masses, the neutral Higgs masses h, H, A are pole masses calculated with the leading top, bottom, stop, sbottom loop contributions; while all other sparticle masses are running masses. This output is then used to compute the cosmological dark matter density of the lightest neutralino which is the LSP. The dark matter analysis is discussed in more detail in section 3.

Using  $\chi^2$  penalties<sup>6</sup> we apply two additional constraints:

 $<sup>^{4}</sup>$ Note, we have checked that switching to 2 loop RGEs for dimensionful parameters can be compensated for by small changes in the GUT scale parameters, without significant changes in the low energy results.

<sup>&</sup>lt;sup>5</sup>Note we take a conservative error for  $m_b(m_b)$  [18] in view of recent claims to much smaller error bars [19]. <sup>6</sup>In order to constrain the values of some physical observables in our  $\chi^2$  analysis, such as  $m_{\tilde{t}_1}$  or  $m_A$ , we

add a significant contribution to the  $\chi^2$  function for values of these observables outside the desired range. We refer to this additional contribution as a  $\chi^2$  penalty. Minimization of  $\chi^2$  with Minuit, then pushes the fits to the desired range. Of course the  $\chi^2$  penalties then vanish.

- $m_{\tilde{t}_1} \ge 300 \text{ GeV}$
- $m_A$  fixed.

The first is chosen to be consistent with  $BR(B \to X_s \gamma)$  [2]. Note, although we do calculate  $BR(B \to X_s \gamma)$ , we do not use it as a constraint in the analysis. This is for two reasons — 1) this decay mode depends on 3–2 generation mixing which is model dependent and 2) it is not difficult to fit  $BR(B \to X_s \gamma)$  for values of  $m_{\tilde{t}_1} \ge 300$  GeV. Hence, in order to be generally consistent with the measured value of  $BR(B \to X_s \gamma)$ , we impose  $m_{\tilde{t}_1} \ge 300$  GeV. With regards to the second constraint, since  $\Omega_{\chi}h^2$  and  $BR(B_s \to \mu^+ \mu^-)$  are both sensitive to the value of  $m_A$ , we fix it's value and present our results for different values of  $m_A$ .<sup>7</sup>

Finally, we apply the experimental limits:

- lower bound on the lightest chargino mass  $m_{\chi^+} > 104 \text{ GeV}$ ,
- lower bound on the light Higgs mass  $m_h > 111$  GeV.

Note, because of the theoretical uncertainty in the calculation of  $m_h$  (~ 3 GeV), we conservatively impose  $m_h > 111$  GeV, instead of the LEP bound for SM Higgs  $m_h > 114.4$  GeV.

## 3. Cosmological Dark Matter Density

We compute the relic abundance  $\Omega_{\chi}h^2$  of the lightest neutralino using exact expressions for neutralino pair annihilation into all allowed final-state channels, which are valid both near and further away from resonances and thresholds [21]. We further treat the neutralino coannihilation with the lightest chargino and next-to-lightest neutralino [22] and with the lighter stau [23] with similar precision. We only neglect the neutralino coannihilation with the stop which would only affect  $\Omega_{\chi}h^2$  in the regions of parameter space which are uninteresting for other reasons, as we comment below. We solve the Boltzmann equation numerically as in [24] and compute  $\Omega_{\chi}h^2$  with an error of a few per cent, which is comparable with today's accuracy on the observational side. The latest determinations of cosmological parameters [8] give  $\Omega_M h^2 = 0.135^{+0.008}_{-0.009}$  for the total matter content and  $\Omega_b h^2 = 0.0224 \pm 0.0009$  for the baryonic component. The difference, attributed to cold dark matter (CDM), is then

$$\Omega_{CDM}h^2 = 0.113 \pm 0.009, \tag{3.1}$$

which is significantly narrower than previous ranges. We then apply two constraints on the dark matter abundance:

- the upper bound  $\Omega_{\chi} h^2 < 0.13$ ,
- $2\sigma$  preferred range  $0.095 < \Omega_{\chi} h^2 < 0.13$ .



**Figure 1:** Contours of constant  $\chi^2$  for  $m_{16} = 3$  TeV and  $m_A = 500$  GeV. The red regions are excluded by  $m_{\chi^+} < 104$  GeV (below and to the left of a black solid curve),  $m_h < 111$  GeV (on the right) and by  $\Omega_{\chi}h^2 > 0.13$ . To the right of the black broken line one has  $m_h < 114.4$  GeV. The green band corresponds to the preferred  $2\sigma$  range  $0.095 < \Omega_{\chi}h^2 < 0.13$ , while the white regions below it correspond to  $\Omega_{\chi}h^2 < 0.095$ .

In Figs. 1–3 we present our results for different values of  $m_{16}$  and  $m_A$  in the  $\mu$ ,  $M_{1/2}$  plane. In particular in Fig. 1 we present, for  $m_{16} = 3$  TeV and  $m_A = 500$  GeV, the (magenta) lines of constant  $\chi^2$  with the cosmologically preferred dark matter region (shaded green) satisfying 0.095  $< \Omega_{\chi}h^2 < 0.13$ . We find significant regions of parameter space which gives  $\chi^2 \leq 2$ ,  $\Omega_{\chi}h^2$  as above, and satisfies all other phenomenological constraints. In addition we have shaded (light red) the regions excluded by collider limits and by  $\Omega_{\chi}h^2 > 0.13$ .<sup>8</sup>

In Fig. 2 we present a more detailed analysis of the same  $m_{16} = 3$  TeV,  $m_A = 500$ 

<sup>&</sup>lt;sup>7</sup>The calculation of BR( $B \to X_s \gamma$ ) and BR( $B_s \to \mu^+ \mu^-$ ) requires a model for fermion mass matrices. In the absence of such a model we use the observed CKM matrix elements to calculate these flavor violating branching ratios.

<sup>&</sup>lt;sup>8</sup>A similar analysis was performed in the recent paper [4]. However, they were not able to find acceptable



Figure 2: Same as Fig. 1 with contours of constant BR $(B_s \to \mu^+ \mu^-)$  (upper left),  $m_h$  (upper right),  $\Omega_{\chi}h^2$  (lower left) and  $\sigma_p^{SI}$  (lower right) for  $m_{16} = 3$  TeV and  $m_A = 500$  GeV.

GeV case given in Fig. 1. We now include lines of constant BR( $B_s \to \mu^+ \mu^-$ ) (upper left),  $m_h$  (upper right),  $\Omega_{\chi}h^2$  (lower left), and  $\sigma_p^{SI}$  (lower right).  $\sigma_p^{SI}$  is the spin independent neutralino dark matter cross–section relevant for direct dark matter searches. We now consider each one of these features further.

Recall, the branching ratio  $BR(B_s \to \mu^+ \mu^-)$  is sensitive to the value of the CP odd Higgs mass  $m_A$  [9]. For  $m_A = 500$  GeV, the branching ratio satisfies  $2 \times 10^{-7} < BR(B_s \to \mu^+ \mu^-)$ 

cosmological solutions. It appears that they did not find any acceptable solutions because they find Yukawa unification only for  $M_{1/2} \sim 100$  GeV and large  $\mu \sim 300$  GeV. In this region we probably would not find acceptable solutions for  $\Omega_{\chi}h^2$ , no matter what value we take for  $m_A$ .



Figure 3: The same as in Fig. 1 but for  $m_{16} = 2.5$  TeV and  $m_A = 500$  GeV (upper left),  $m_{16} = 5$  TeV and  $m_A = 500$  GeV (upper right),  $m_{16} = 2.5$  TeV and  $m_A = 300$  GeV (lower left) and  $m_{16} = 3$  TeV and  $m_A = 300$  GeV (lower right). Also marked are contours of constant BR( $B_s \rightarrow \mu^+ \mu^-$ ). The blue regions in the lower two panels are excluded by BR( $B_s \rightarrow \mu^+ \mu^-$ ) >  $2.6 \times 10^{-6}$ . Note the different mass ranges for  $M_{1/2}$  and  $\mu$  in the different panels.

 $\mu^+ \ \mu^-) < 8 \times 10^{-7}$  for acceptable values of  $\Omega_{\chi} h^2$  and  $\chi^2 < 2$ . In a recent analysis it has been shown that, with an integrated luminosity of 15 fb<sup>-1</sup>, CDF can discover this process if BR $(B_s \to \mu^+ \ \mu^-) > 1.2 \times 10^{-8}$  [25]. Hence most acceptable regions of parameter space lead to observable rates for BR $(B_s \to \mu^+ \ \mu^-)$ .

In Fig. 2 (upper right) we see that the light Higgs mass increases as  $M_{1/2}$  decreases. In the acceptable regions of parameter space we find  $116 < m_h < 121$  GeV. The value of the light Higgs mass is however fairly insensitive to  $m_{16}$ .

The cosmological relic abundance of the neutralino  $\Omega_{\chi}h^2$  (Fig. 2 (lower left)) is primarily determined by the direct s-channel pair-annihilation into SM fermion pairs through the CP odd Higgs. Since all the sfermions are very heavy, their contribution to reducing the neutralino number density is strongly suppressed. In contrast, because of the coupling  $Ab\bar{b} \propto \tan\beta$  (and similarly for the  $\tau$ 's), the A-resonance is effective and broad. Near  $m_{\chi} \approx m_A/2$  it reduces  $\Omega_{\chi} h^2$  down to allowed but uninterestingly small values  $\ll 0.1$ . As one moves away from the resonance,  $\Omega_{\chi}h^2$  grows, reaches the preferred range  $0.095 < \Omega_{\chi}h^2 < 0.13$ , before becoming too large  $\Omega_{\chi}h^2 > 0.13$ .<sup>9</sup> (A similar, but much more narrow resonance due to  $h^0$  is also present at  $M_{1/2} \approx 150$  GeV and small  $\mu$ .) When  $m_{\chi} \gtrsim m_t \ (M_{1/2} \gtrsim 420 \text{ GeV})$  and the stops are not too heavy, the LSP pairs annihilate to  $t\bar{t}$ -pairs. In the region of large  $M_{1/2}$ , often where  $m_h$  is already too low, two additional channels become effective. First, in this region the neutralino becomes almost mass degenerate with the lighter stau which leads to reducing  $\Omega_{\rm v} h^2$  through coannihilation. Second, if  $m_A$  is not too large, neutralino pair-annihilation into Higgs boson pairs AA and HH opens up. Finally, at  $\mu \ll M_{1/2}$ , the relic abundance is strongly reduced due to the increasing higgsino component of the LSP.

Finally, the spin independent neutralino cross–section  $\sigma_p^{SI}$  in the lower right window of Fig. 2 is predominantly determined by the contribution of the heavy CP even scalar *t*-channel exchange to both tree–level and one–loop diagrams. Note that in the preferred region of  $\chi^2 < 2$  and  $0.095 < \Omega_{\chi}h^2 < 0.13$  we find  $10^{-9}$  pb  $\lesssim \sigma_p^{SI} \lesssim 10^{-7}$  pb. We will comment further on our predictions for  $\sigma_p^{SI}$  below.

In Fig. 3 we display the dependence of our constraints,  $\Omega_{\chi}h^2$  and  $\operatorname{BR}(B_s \to \mu^+ \mu^-)$ on  $m_{16}$  and  $m_A$ . By comparing the upper two windows with Fig. 1 we can see that, as  $m_{16}$ increases, the region with  $\chi^2 < 2$  rapidly grows. Note, the dominant pull in  $\chi^2$  is due to the bottom quark mass. In order to fit the data, the total SUSY corrections to  $m_b(m_b)$  must be of order -(2-4)% [2]. In addition there are three dominant contributions to these SUSY corrections, a gluino loop contribution  $\propto \alpha_3 \mu M_{\tilde{g}} \tan \beta/m_{\tilde{b}_1}^2$ , a chargino loop contribution  $\propto \lambda_t^2 \mu A_t \tan \beta/m_{\tilde{t}_1}^2$ , and a term  $\propto \log M_{SUSY}^2$ . When  $m_{16}$  increases (with  $M_{1/2}$  fixed) the parameter  $A_t$  becomes more negative, since  $A_0 \approx -2 m_{16}$  and  $A_t \approx -3 M_{1/2} + \epsilon A_0$ where  $\epsilon \ll 1$ . Also, larger values of  $m_{16}$  permit a larger range for the ratio  $m_{\tilde{b}_1}/m_{\tilde{t}_1}$ . Thus larger values of  $m_{16}$  allows more freedom in parameter space for fitting the data at both smaller or larger values of  $\mu$ ,  $M_{1/2}$ .

In the lower two windows in Fig. 3 we consider two regions with  $m_A = 300$  GeV with  $m_{16} = 2.5$  TeV (lower left) and  $m_{16} = 3$  TeV (lower right). The blue regions are excluded by the CDF bound BR $(B_s \rightarrow \mu^+ \mu^-) < 2.6 \times 10^{-6}$  [10]. Note for  $m_{16} = 2.5$  TeV, the region with  $\chi^2 < 2$  does not overlap the region with acceptable dark matter abundance (green shaded). However for  $m_{16} = 3$  TeV,  $m_A = 300$  GeV, Fig. 3 (lower right), we find a small region with acceptable  $\chi^2 < 1$  and  $\Omega_{\chi}h^2$ . Moreover the branching ratio BR $(B_s \rightarrow \mu^+ \mu^-)$  is now close to the CDF bound. On the other hand for  $m_{16} = 5$  TeV,  $m_A = 500$  GeV, in Fig. 3 (upper right), a new region of parameter space consistent with all the data now

<sup>&</sup>lt;sup>9</sup>Note that at one loop we have  $M_1(M_Z) = M_{1/2} * \alpha_1(M_Z)/\alpha_G$  so  $M_1(M_Z) \approx 0.4M_{1/2}$ . For bino–like neutralino (which is true for larger  $\mu$ ), we thus have  $m_{\chi} \approx 0.4M_{1/2}$ . Hence for s–channel annihilation we have  $m_A \approx 2m_{\chi} \approx 0.8 M_{1/2}$  or  $M_{1/2} \approx (5/4) m_A$  for the position of the "peak suppression."

opens up with larger  $\mu$ ,  $M_{1/2}$ . This new region becomes cosmologically allowed due to neutralino annihilation into Higgs boson pairs AA and HH and due to coannihilation with the lighter stau.

Hence we see that increasing  $m_A$  has two effects. It suppresses the branching fraction  $BR(B_s \to \mu^+ \mu^-)$ . At the same time it moves the s-channel neutralino annihilation channel to larger values of  $M_{1/2}$ ; hence providing larger regions with  $0.095 < \Omega_{\chi}h^2 < 0.13$  (compare Figs. 1 and 3 (lower right) or Figs. 3 (upper and lower left)). In fact, the two (green) branches of the preferred range  $0.095 < \Omega_{\chi}h^2 < 0.13$  correspond to the two sides (except for the upper left window of Fig. 3 where just one side is evident) of the wide A resonance in the neutralino pair-annihilation. On the other hand, increasing  $m_A$  above 1 TeV or so would move the regions of preferred  $\Omega_{\chi}h^2$  too far to the right, in potential conflict with a lower bound on  $m_h$ .

Finally, we comment on  $\operatorname{BR}(B \to X_s \gamma)$ . The current experimental range [26, 27] is  $\operatorname{BR}(B \to X_s \gamma)_{\exp t} = (3.41 \pm 0.36) \times 10^{-4}$ , while the SM prediction, including full NLO QCD corrections [28, 29], is  $\operatorname{BR}(B \to X_s \gamma)_{\rm SM} = (3.70 \pm 0.30) \times 10^{-4}$ . In computing the SUSY contribution to  $b \to s\gamma$  we further include full LO and dominant NLO–level tan  $\beta$ –enhanced contributions [30, 31]. Conservatively allowing for the SM+SUSY contribution to be in the range  $(3.41 \pm 0.67) \times 10^{-4}$  [32, 27] selects a band 300 GeV  $\leq \mu \leq 400$  GeV which slowly decreases with increasing  $M_{1/2}$ . (This remains approximately true for all the cases that we have analyzed except  $m_{16} = 5$  TeV and  $m_A = 500$  GeV where one finds a narrower range at  $\mu \leq 200$  GeV.) However,  $\operatorname{BR}(B \to X_s \gamma)$  is strongly sensitive to the 2–3 generation down–type squark mixings [27] which are model dependent and which we do not include here. In summary, the process is generally consistent with the most preferred regions of  $M_{1/2}$  and  $\mu$  but we do not use it here as a constraint, since it can be easily relaxed by employing parameters which are less relevant for our analysis.

To summarize, we find that regions satisfying all three constraints exist for  $m_{16} \geq 3$ TeV and  $m_A \geq 300$  GeV. The acceptable range for  $\mu, M_{1/2}$  grows with increasing  $m_A$ (for fixed  $m_{16} = 3$  TeV) from approximately 260 GeV  $\leq \mu \leq 295$  GeV, 140 GeV  $\leq M_{1/2} \leq 200$  GeV for  $m_A = 300$  GeV to 160 GeV  $\leq \mu \leq 520$  GeV, 140 GeV  $\leq M_{1/2} \leq 530$  GeV for  $m_A = 500$  GeV. In addition, the allowed regions grow as  $m_{16}$  increases and for  $m_A = 500$  GeV,  $m_{16} = 5$  TeV there is also a large  $\mu$ ,  $M_{1/2}$  solution satisfying 480 GeV  $\leq \mu \leq 820$  GeV, 640 GeV  $\leq M_{1/2} \leq 1020$  GeV. In the Table we present the input and output data from the  $\chi^2$  analysis for three points satisfying all the phenomenological constraints.

## 4. Predictions and Summary

In this paper we have analyzed the MSO<sub>10</sub>SM and found regions of soft SUSY breaking parameter space which fit precision electroweak data, including the top, bottom and tau masses and, in addition, fit the cosmological dark matter abundance for the neutralino LSP and satisfy BR( $B_s \rightarrow \mu^+ \mu^-$ ). Generically, we find solutions to all the constraints with  $m_{16} \geq 3$  TeV. The squark and slepton masses have an inverted scalar mass hierarchy with the first and second generation scalar masses of order  $m_{16}$ , while the third generation has



Figure 4: The upper and lower limits on BR $(B_s \to \mu^+ \mu^-)$  as a function of  $m_A$  in the  $\mu$ ,  $M_{1/2}$  region of parameter space satisfying all the collider constraints,  $0.095 < \Omega_{\chi}h^2 < 0.13$  and  $\chi^2 < 2$  for fixed  $m_{16} = 3$  TeV.

mass less than 1.3 TeV for  $m_{16} = 5$  TeV. This nice feature of the model suppresses SUSY CP and flavor problems. In addition the gaugino masses are typically much lighter, except for the large  $\mu$ ,  $M_{1/2}$  region for  $m_{16} = 5$  TeV with a gluino mass of order 1.7 TeV (see spectrum in Table for selected acceptable points).

Note an immediate consequence of such heavy first and second generation sleptons is the suppression of the SUSY contribution to the anomalous magnetic moment of the muon. We find  $a_{\mu}^{SUSY} \leq 2.8 \times 10^{-10}$  (see Table). This is consistent with the most recent experimental [33] and theoretical results at  $1\sigma$  if one uses  $\tau$ -based analysis [34]. However it is only consistent with an  $e^+e^-$ -based analysis at  $3\sigma$ .

Another interesting result is the enhanced branching ratio for the process  $B_s \to \mu^+ \mu^-$ . In Fig. 4 we show the ranges of values of BR $(B_s \to \mu^+ \mu^-)$  in the low  $\mu$ ,  $M_{1/2}$  region of parameter space satisfying all the phenomenological constraints with  $0.095 < \Omega_{\chi} h^2 < 0.13$  and  $\chi^2 < 2$  as a function of  $m_A$  for fixed  $m_{16} = 3$  TeV. The horizontal red line is the CDF bound. Over a significant region of parameter space BR $(B_s \to \mu^+ \mu^-) > 1 \times 10^{-7}$  and may be observable at the Tevatron (Run II) [25].

Finally in Fig. 5 we present the cross-section for elastic neutralino-proton scattering due to scalar interactions  $\sigma_p^{SI}$  for all regions satisfying the collider constraints, 0.095  $< \Omega_{\chi}h^2 < 0.13$  and  $\chi^2 < 2$ . The green bands are for  $m_{16} = 2.5$  TeV, the red for 3 TeV and the blue for 5 TeV. The lighter shading is for  $m_A = 300$  GeV, the darker for  $m_A = 500$  GeV. In the last case ( $m_{16} = 5$  TeV and  $m_A = 500$  GeV) there are two branches which correspond



**Figure 5:** Predictions for  $\sigma_p^{SI}$  vs.  $m_{\chi}$  for different choices of  $m_{16}$  and  $m_A$ , subject to the collider constraints,  $0.095 < \Omega_{\chi}h^2 < 0.13$  and  $\chi^2 < 3$ . The green bands are for  $m_{16} = 2.5$  TeV, the red for 3 TeV and the blue for 5 TeV. The lighter shading is for  $m_A = 300$  GeV, the darker for  $m_A = 500$  GeV. In the last case ( $m_{16} = 5$  TeV and  $m_A = 500$  GeV) there are two branches which correspond to the two cosmologically preferred regions in the upper right panel in Fig. 3.

to the two cosmologically preferred regions in the upper right panel in Fig. 3. Note that lower  $m_A$  generally gives larger  $\sigma_p^{SI}$  as expected. For comparison, we also show the bounds from the present dark matter searches and the predictions of the general MSSM [35]. (Other recent studies of  $\sigma_p^{SI}$  in the case of non–universal Higgs mass in a variant of the CMSSM can be found in [36].) Over the next two to five years the experimental sensitivity is expected to gradually improve by some three orders of magnitude. This will cover large parts of the predicted ranges of  $\sigma_p^{SI}$ , especially at lower values of  $m_A$  where  $B_s \to \mu^+ \mu^$ will be accessible at the Tevatron (Run II).

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Data points		1	2	3
Input parameters				
$\alpha_G^{-1}$		24.66	24.92	25.28
$M_G \times 10^{-16}$		3.51	2.83	2.43
$\epsilon_3$		-0.038	-0.034	-0.029
$\lambda$		0.66	0.66	0.66
$m_{16}$		3000	3000	5000
$m_{10}/m_{16}$		1.30	1.33	1.33
$\Delta m_H^2$		0.14	0.15	0.14
$M_{1/2}$		180	400	700
$\mu$		270	350	600
aneta		50.9	50.6	50.5
$A_0/m_{16}$		-1.85	-1.88	-1.91
$\chi^2$ observables	$\operatorname{Exp}\left(\sigma\right)$			
$M_Z$	91.188 (0.091)	91.18	91.19	91.20
$M_W$	80.419 (0.080)	80.42	80.42	80.41
$G_{\mu} \times 10^5$	1.1664(0.0012)	1.166	1.166	1.166
$\alpha_{EM}^{-1}$	137.04(0.14)	137.0	137.0	137.0
$\alpha_s(M_Z)$	0.118(0.002)	0.1177	0.1176	0.1179
$\rho_{new} \times 10^3$	-0.200(1.10)	0.427	0.498	0.162
$M_t$	174.3(5.1)	173.9	174.7	174.7
$m_b(m_b)$	4.20(0.20)	4.28	4.28	4.21
$M_{ au}$	1.7770(0.0018)	1.777	1.777	1.777
TOTAL $\chi^2$		0.53	0.61	0.13
h		120	119	117
H		329	556	557
A		299	499	501
$H^+$		329	540	541
$\chi^0_1$		72	163	293
$\chi^0_2$		133	288	536
$\chi_1^+$		133	287	535
$\tilde{g}$		474	1032	1768
$\tilde{t}_1$		300	300	576
${ ilde b}_1$		679	736	1262
$ ilde{ au}_1$		870	721	1180
$a_{\mu}^{SUSY} \times 10^{10}$	25.6(16)	2.7	2.8	1.0
$\Omega_\chi h^2$	0.095 - 0.130	0.099	0.130	0.097
$\sigma_p^{SI}(pb) \times 10^7$		1.020	0.158	0.049
$BR(B_s \to \mu^+ \ \mu^-) \times 10^6$	< 2.6	2.58	0.61	0.66
$BR(B \to X_s \gamma) \times 10^4$	$3.41 \ (0.67)$	5.36	4.34	0.81