

# Delegated Portfolio Management with Socially Responsible Investment Constraints

A. Fabretti


[Joint work with S. Herzel]

[annalisa.fabretti@uniroma2.it](mailto:annalisa.fabretti@uniroma2.it)

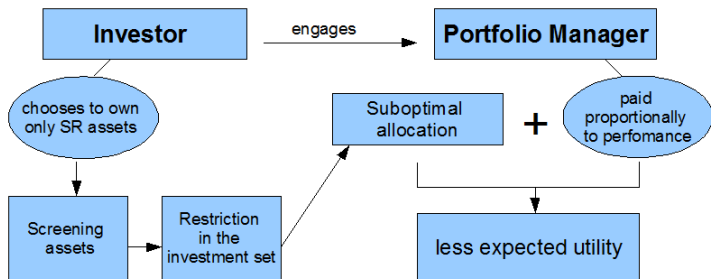
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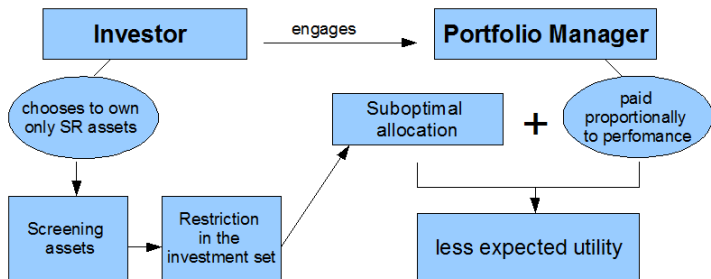
# What is Socially Responsible Investment?

- ▶ Any investment process that combines investors' financial objectives with their concerns about environmental, social and governance issues (ESG).
- ▶ Example: Principles for Responsible Investment (PRI) provide a menu of possible actions for incorporating ESG issues into mainstream investment decision-making and ownership practices.
- ▶ Growing Interest 

## Incentives for portfolio managers



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How to set incentives to compensate Portfolio Manager for the investment restriction?

# The Market

Single period market with

- ▶  $n$  risky assets with return  $\mathbf{X}$  distributed as a multivariate normal:

$$\mathbf{X} \sim N(\bar{\mathbf{X}}, \Sigma);$$

- ▶ a risk free asset, with return  $R$ .

The first  $p$  components of  $\mathbf{X}$  represent green assets  $\mathbf{P}$ , the remaining  $q$  components represent non-green assets  $\mathbf{Q}$ :

$$\mathbf{X} = \begin{pmatrix} \mathbf{P} \\ \mathbf{Q} \end{pmatrix}, \quad \bar{\mathbf{X}} = \begin{pmatrix} \bar{\mathbf{P}} \\ \bar{\mathbf{Q}} \end{pmatrix}, \quad \Sigma = \begin{pmatrix} \Sigma_P & \Sigma_{PQ} \\ \Sigma_{PQ}^T & \Sigma_Q \end{pmatrix}.$$

# Agents

- ▶ The Investor
  - ▶ risk neutral
  - ▶ providing an *initial wealth*  $W_0$  to the Portfolio Manager to be invested
  - ▶ aware of SR: she maximizes her expected wealth but she wants only "Green" assets.

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- ▶ The Portfolio Manager
  - ▶ risk averse with utility function  $u(x) = e^{-\alpha x}$
  - ▶ paid proportionally to the portfolio performances
  - ▶ receiving a private signal
  - ▶ accepting the contract iff the expected utility is greater than his reservation utility

## The contract

The contract offered by the investor:

$$f(W) := AR + b_g W,$$

$W$  is the portfolio composed only by green assets  $\mathbf{P}$

The reservation contract :

$$r(W') := AR + bW',$$

$W'$  is the portfolio composed by all assets  $\mathbf{X}$

The quantity  $\Delta = b_g - b$  is the “Green bonus”.



## The information

The manager receives a signal

$$\mathbf{S} = \mathbf{X} + \epsilon$$

where  $\mathbf{X}$  and  $\epsilon$  are uncorrelated and  $\epsilon \sim N(\mathbf{0}, \Sigma_\epsilon)$ ,  $\Sigma_\epsilon$  represents the skill of the manager.

The conditional distribution of  $\mathbf{X}$  given  $\mathbf{S} = S$  is normal with mean

$$\mathbf{M}(S) = E(\mathbf{X} | \mathbf{S} = S) = \bar{\mathbf{X}} + \Sigma \Sigma_S^{-1} (S - \bar{S}),$$

and variance

$$V = \text{Var}(\mathbf{X} | \mathbf{S} = S) = \Sigma - \Sigma \Sigma_S^{-1} \Sigma.$$

## The principal optimization problem

- ▶ Principal optimization problem

$$\max_{\Delta} \mathbb{E} [ W(\omega_P^*(\Delta, \mathbf{S})) - f(W(\omega_P^*(\Delta, \mathbf{S}))) ]$$

- ▶ subject to

$$\omega_P^*(\Delta, S) = \arg \max_{\omega_P} \mathbb{E} [ u(AR + (b + \Delta)W(\omega_P)) | \mathbf{S} = S ]$$

- ▶ and the manager's participation constraint

$$\mathbb{E} [ u(f(W)) ] \geq \mathbb{E} [ u(r(W')) ]$$

## Compensation bonus

The solution of principal optimisation problem is

$$\bar{\Delta} = c(\Psi + \Phi)$$

where

- ▶  $c$  depends on manager's risk aversion, risk free rate and AUM.
- ▶  $\Psi$  is the minimum required by any manager of whatever ability level. It is related to the differences, in terms of market properties, between green and non-green assets.
- ▶  $\Phi$  is the compensation for the unexploited ability due to the restriction. It is related to manager's expertise.

The minimum required when  $\Phi = 0$  is  $\bar{\Delta}_0 = c\Psi$

$$\Psi = \mathcal{H} - \mathcal{H}_P, \quad c = \frac{1}{2\alpha W_0 R}$$

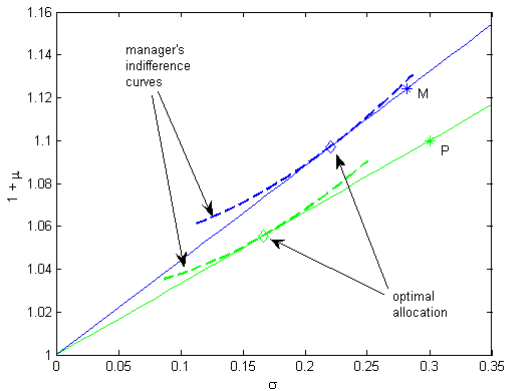
where

$$\mathcal{H}_P = (\bar{\mathbf{P}} - R\mathbf{1}_p)^T \Sigma_P^{-1} (\bar{\mathbf{P}} - R\mathbf{1}_p)$$

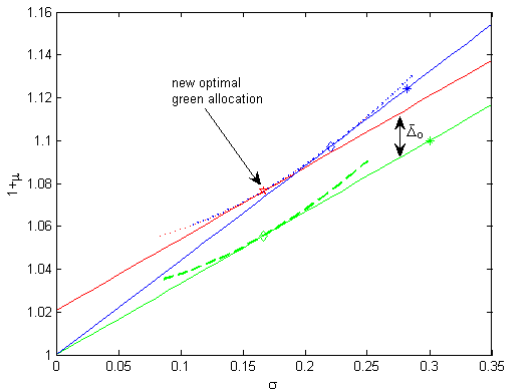
and

$$\mathcal{H} = (\bar{\mathbf{X}} - R\mathbf{1}_n)^T \Sigma^{-1} (\bar{\mathbf{X}} - R\mathbf{1}_n).$$

# The effect of $\bar{\Delta}_0$

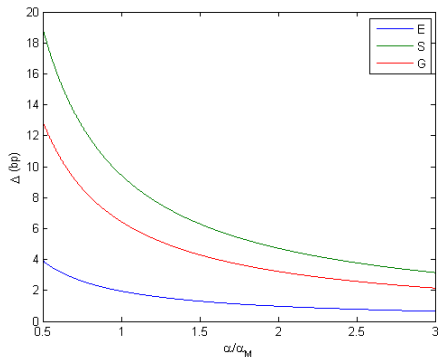


# The effect of $\bar{\Delta}_0$



# $\bar{\Delta}$ when $\Phi = 0$

Data: S&P500 December 2006 by KLD



E-AllCon  $n_p = 341$   
 G-AllCon  $n_p = 152$   
 S-allCon  $n_p = 71$

## Green Bonus: the ability term $\Phi$

The compensation for the missed exploitation of part of the signal

$$\Phi = \log \left( \frac{H}{H^g} \right)$$

$$H = \frac{\det(\Sigma)}{\det(V)} \qquad H^g = \frac{\det(\Sigma_P)}{\det(V_P)}$$

are the global and the green *expertise* of a manager.



## Comments on Expertise $H = \frac{\det(\Sigma)}{\det(V)}$

- ▶ Two managers with different skills (represented by the variance of the signal) may have the same expertise  $H$ .
- ▶  $\Phi$  is decreasing with respect to  $H^g$ , hence higher the green expertise  $\rightarrow$  lower the bonus required. More

$$\lim_{H^g \rightarrow H} \Phi = 0$$

When the agent's expertise is concentrated in the green assets, no efficiency bonus is required.

# Conclusion

Under very simple assumptions we tackle the problem to compensate the screening effects by the use of a green bonus, decomposing it into

- ▶ manager's risk aversion
- ▶ loss in Sharpe Ratios
- ▶ loss in expertise

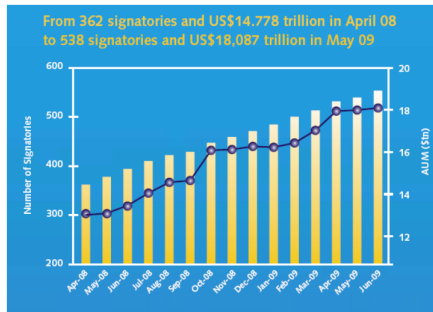
download: Sirp Working Paper 10-07 on [www.sirp.se](http://www.sirp.se)

thanks: MISTRA, The foundation for strategic environmental research, Sweden

## References: DPM

- ▶ S. Bhattachary and P. Pfleiderer, "Delegated Portfolio Management", *JET*, 36 1985
- ▶ DPM literature has devoted little attention to constraints in asset allocations  
A. Almazan et al. , "Why constraint your mutual fund manager", *JFE*, 73, 2004
- ▶ DPM with short selling constraints  
J. P. Gomez and T. Sharma , "Portfolio Delegation under Short-selling Constraints", *Economic Theory*, 28, 2006

## Growing interest in SRI



Source: Annual Report of PRI Initiative, 2009 [▶ back](#)