Design and Analysis of Switched-Capacitor-Based Step-Up Resonant Converters

K. K. Law, K. W. E. Cheng, and Y. P. Benny Yeung

Abstract—A switched-capacitor-based step-up resonant converter is proposed. The voltage conversion of the converters is in step-up mode. By adding a different number of switched-capacitor cells, different output voltage conversion ratios can be obtained. The voltage conversion ratio from 2 to any whole number can therefore be generated by these switching-capacitor techniques. A resonant tank is used to assist in zero-current switching hence the current spike, which usually exists for classical switched-capacitor can be eliminated. Both high-frequency operations and high efficiency are possible. Generalized analysis and design method of the converters are also presented. Experimental results verified the theoretical analysis.

Index Terms—Capacitor switching, charge transfer, resonant converter, switched capacitor.

I. INTRODUCTION

N RECENT YEARS, switched-mode power supplies (SMPS) become very popular for power conversions and conditionings. Some soft-switching resonant converters can operate in very high frequency so that the power density is high [1]. Energy storage of most SMPS circuits is based on large inductors or transformers. The weight and the size of the circuits are usually dominated by these magnetic components.

For DC–DC power conversion, a kind of switched-mode converters was proposed [2]–[4]. Voltage control investigation can be found in [5], [6]. These kinds of converters have no magnetic components. They use capacitors for storing energy so that the size of the converter is small. Also, it can be fabricated in integrated circuit chips. However, high current spikes are usually occurred in all devices in these circuits for charging or discharging the switching-capacitors. As a result, these kinds of converters are usually used on low power conditions.

In this paper, a family of novel resonant converters is presented. These converters have both the advantages of traditional SMPSs and switched-capacitor converters. The circuits consist of two switches, some diodes, and a number of switching-capacitor cells. Energy is stored by the switching-capacitors. All switching devices inside circuit are operated under zero-current switching condition by the resonance of the switching-capacitors and a very small resonant inductor. The circuit is also similar to the classical resonant circuit [7] where the resonant cur-

Manuscript received September 28, 2001; revised May 13, 2004. This work was supported by the Research Committee, The Hong Kong Polytechnic University, under Project: G-V983. This paper was recommended by Associate Editor D. Czarkowski.

The authors are with the Power Electronics Research Centre, Department of Electrical Engineering, The Hong Kong Polytechnic University, Hong Kong (e-mail: eeecheng@polyu.edu.hk).

Digital Object Identifier 10.1109/TCSI.2004.840482

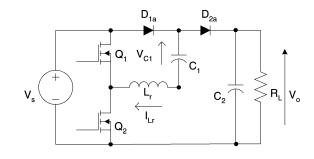


Fig. 1. Double-mode switched-capacitor resonant converter.

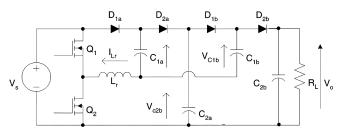


Fig. 2. Triple-mode switched-capacitor resonant converter.

rent/voltage is used as the power transfer. However, in the proposed circuit, the resonant current is used as assisting zero-current switching and is a quasiresonant manner [8]. These circuits are in step-up voltage mode. By adding numbers of proposed switching-capacitor cells, different step-up voltage conversion ratio can be obtained without adding any other active switches. Current spike problem of the conventional switched-capacitor converter is improved. Figs. 1–3 show the double, triple, and n-mode step-up voltage conversions ratio, respectively. After detailed perusal and circuits comparison, the general switching-capacitor cell for step-up the voltage conversion ratio was found (Fig. 4).

II. PRINCIPLES OF STEP-UP SWITCHED-CAPACITOR RESONANT CONVERTERS

The triple-mode switched-capacitor resonant circuit is like a two double-mode switched-capacitor resonant converters combined together. Similar to double-mode circuit, when Q_2 is turned on while Q_1 is turned off, C_{1a} and L_r are connected in series resonance through D_{1a} . C_{1a} is charged from source V_S . Both C_{2a} and C_{2b} are very large capacitors for keeping the voltage to be constant. C_{2a} is like another voltage source with its voltage equals to $2V_S$. C_{2a} discharges to C_{1b} through D_{1b} while C_{1b} and L_r are connected in series resonance. When Q_1 is turned on while Q_2 is turned off, V_S and C_{1a} are connected in series resonance with L_r and their polarities are in same direction and add up. Since C_{1a} has a dc component

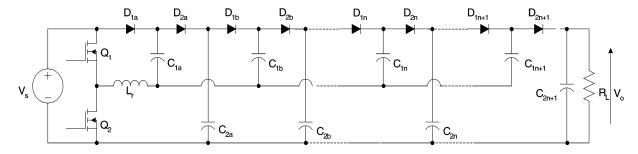


Fig. 3. *n*-mode of switched-capacitor resonant converter.

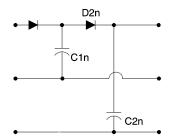


Fig. 4. Proposed switching-capacitor cell.

equal to V_S . They charge C_{2a} so that the voltage across C_{2a} equals to $2V_S$. C_{1b} and L_r are connected in series resonance as well with V_S in the same direction of polarity. C_{1b} has a dc component equal to $2V_S$. V_S and C_{1b} release energy to the load together. C_{1a} is not necessary equal to C_{1b} , but is usually made them equal in order to ensure zero-current switching can be controlled easily. The voltage conversion ratio of the converter is 3. Actually, C_{2a} can be considered to be another output with voltage conversion ratio equal to 2 so that this circuit can be a multiple output circuit.

III. MATHEMATICAL ANALYSIS

The computer simulation waveforms of the triple-mode circuit using the parameters of $(V_s=40~\rm V,~C_{1a}~\rm and~C_{1b}=0.22~\mu F, C_{2a}~\rm and~C_{2b}=0.22~\mu F, L_r=1~\mu H,$ output power = 100 W) are shown in Fig. 5(a) and (b). For analyzing the circuit, it would be divided into four states in each switching period. Fig. 6(a)–(d) shows the equivalent circuits of the triple mode switched-capacitor resonant coverter for the four states.

A. State $I[t_0 \text{ to } t_1]$

 Q_2 is turned on and Q_1 is turned off in this state. C_{1a} and L_r resonate together with V_S while C_{1b} and L_r resonate together with C_{2a} . They all start resonating at t_0 from the current equal to zero in sinusoidal manner. Since the current increases gradually at t_0, Q_2 is turned on under zero-current switching condition. They stop resonating when the current reaches zero again at t_1 by the reverse biased D_{1a} and D_{1b} . Let $L_r = L$ and $C_{1a} = C_{1b} = C$. Assume that C_{2a} and C_{2b} are large enough to keep the voltage to be constant, and the circuit is lossless, the equations of this state can be derived by classical circuit equation

$$v_{C1a} = V_S - \frac{3}{4} I_o T_S \omega_0 Z_0 \cos \omega_0 (t - t_0)$$
 (1)

$$i_{Lr} = \frac{3}{4} I_o T_S \omega_0 \sin \omega_0 (t - t_0) \tag{2}$$

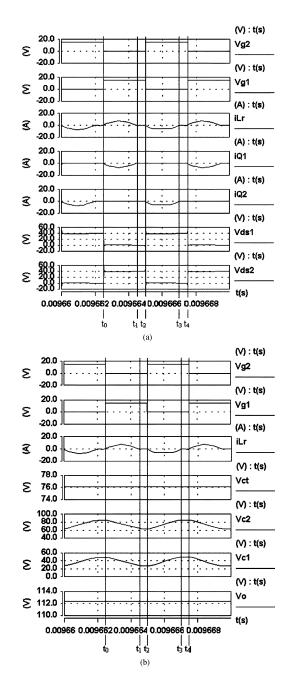


Fig. 5. Simulation waveforms of triple-mode switched-capacitor resonant converter. $V_{\rm ds}$ and $V_{\rm g}$ stand for the drain-source and gain voltages of the Mosfet. $V_{\rm ct}$ is the interim voltage developed on the capacitor C_{2b} .

$$v_{C1b} = 2V_S - \frac{3I_o T_S \omega_0 Z_0}{4} \cos \omega_0 (t - t_0)$$
 (3)

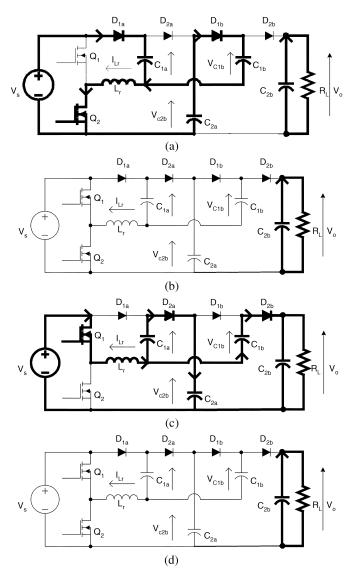


Fig. 6. Equivalent circuits of the triple-mode switched-capacitor resonant converter. (a) State I. (b) State II. (c) State III. (d) State IV.

where

$$\omega_0 = \frac{1}{\sqrt{2LC}} \tag{4}$$

$$Z_0 = \sqrt{\frac{L}{2C}}. (5$$

B. State II $[t_1 \text{ to } t_2]$

Both Q_2 and Q_1 are still turned off in this state. The resonance stops at t_1 . The inductor current is equal to zero. The voltages of C_{1a} , C_{1b} , and C_{2a} are unchanged. C_{2b} discharges to the load. At t_2, Q_1 is turned on and Q_2 is turned off. Hence, Q_2 is turned off under zero-current condition. The equations of this state are

$$v_{C1a} = V_S + I_o T_S \omega_0 Z_0 \tag{6}$$

$$v_{C1b} = 2V_S + \frac{I_o T_S \omega_0 Z_0}{2} \tag{7}$$

$$i_{Lr} = 0. (8)$$

C. State III $[t_2 \text{ to } t_3]$

 Q_1 is turned on and Q_2 is turned off in this state. L_r and C_{1a} resonate in series together and connected with source V_s to C_{2a} while L_r resonates with C_{1b} and connected together to C_{2b} and the load. Similar to State I, the resonant currents are in sinusoidal manner. They increase from zero at t_2 gradually so that zero-current turn-on of Q_1 is achieved. The current reaches zero at t_3 . The resonance stops by the reverse biased diodes D_{2b} and D_{2a} . The equations of this state are

$$v_{C1a} = V_S + \frac{3}{4} I_o T_S \omega_0 Z_0 \cos \omega_0 (t - t_2)$$
 (9)

$$i_{Lr} = -\frac{3}{4}I_o T_S \omega_0 \sin \omega_0 (t - t_2) \tag{10}$$

$$v_{C1b} = 2V_S + \frac{3I_o T_S \omega_0 Z_0}{4} \cos \omega_0 (t - t_2). \tag{11}$$

D. State IV $[t_3 \text{ to } t_4]$

In this state, both Q_1 and Q_2 are still turned off. Similar to State III, the resonance stops at t_3 . The instantaneous inductor current is equal to zero. The voltage of C_{1a} and C_{1b} is unchanged. C_{2b} discharge to the load again. At t_4, Q_2 is turned on and Q_1 is turned off. Hence, Q_1 is turned off in zero-current condition. The equations of this state are

$$v_{C1a} = V_S - I_o T_S \omega_0 Z_0 \tag{12}$$

$$v_{C1a} = V_S - I_o T_S \omega_0 Z_0$$
 (12)
 $v_{C1b} = 2V_S - \frac{I_o T_S \omega_0 Z_0}{2}$ (13)

$$i_{Lx} = 0. (14)$$

The voltage conversion ratio has been derived by using balancing of the input and output energies. Also with the condition of continuity of the inductor current and capacitor voltages, the conversion ratio has been proved to be 3 and the coefficients of [(1)-(3),(6)-(7),(9)-(10),(12)-(13)] has been derived as shown above.

IV. GENERALIZED EQUATIONS OF CONVERTERS

The voltage across $C_{1a}, C_{1b}, C_{1c}, \ldots$ are denoted by V_{Ci} where $i = a, b, c, \dots$ Also define $\varphi(i) = 1, 2, 3, 4 \dots$ for $i = a, b, c, d, \dots$ respectively. All the resonant capacitor currents also pass through L_r . Hence, for an n-mode, there are $n-1C_1$ capacitors. Their general equations of an n-mode converter can be described as follows.

A. State $I[t_0-t_1]$

$$v_{C_i} = \varphi(i)V_s - \frac{n\pi I_0 T_S Z_o}{2T_0}\cos\omega_0(t - t_0)$$
 (15)

$$i_L = \frac{n\pi I_0 T_S}{2T_0} \sin \omega_0 (t - t_0) \tag{16}$$

where

$$\omega_0 = \sqrt{\frac{1}{L_r n C_1}} = \frac{2\pi}{T_o} \tag{17}$$

$$Z_0 = \sqrt{\frac{L_r}{nC_1}}. (18)$$

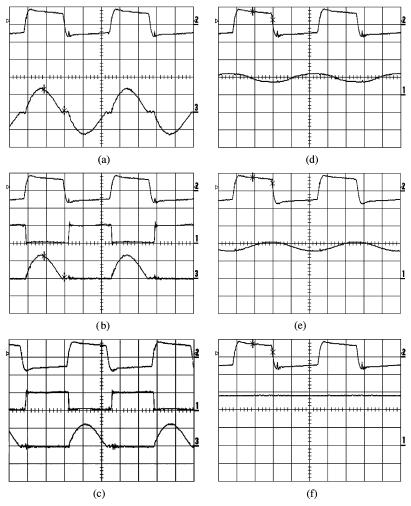


Fig. 7. Measured waveforms of triple-mode switched-capacitor resonant converter (time base: $5~\mu s$ /div). (a) Upper trace: Gate signal of Q_1 , 20 V/div, Lower trace: I_L , 5 A/div. (b) Upper trace: Gate signal of Q_1 , 20 V/div, Middle trace: V_{ds} of Q_1 , 40 V/div, Lower trace: Q_1 current, 5 A/div. (c) Upper trace: Gate signal of Q_2 , 20 V/div, Middle trace: V_{ds} of Q_2 , 40 V/div, Lower trace: Q_2 current, 5 A/div. (d) Upper trace: Gate signal of Q_1 , 20 V/div, Lower trace: V_{C1a} , 40 V/div. (e) Upper trace: Gate signal of Q_1 , 20 V/div, Lower trace: Output Voltage, 40 V/div.

B. In State II $[t_1-t_2]$

$$v_{C_i} = \varphi(i)V_s + \frac{n\pi I_0 T_S Z_0}{2T_0}$$
(19)

$$i_L = 0. (20)$$

C. In State III $[t_2-t_3]$

$$v_C = \varphi(i)V_s + \frac{n\pi I_0 T_S Z_o}{2T_0} \cos \omega_o(t - t_2)$$
 (21)

$$i_L = -\frac{n\pi I_0 T_S}{2T_0} \sin \omega_o (t - t_2).$$
 (22)

D. In State IV $[t_3-t_4]$

$$v_C = \varphi(i)V_s - \frac{n\pi I_0 T_S Z_o}{2T_0}$$
 (23)

$$i_L = 0. (24)$$

It could also be noted that the voltage rating of the transistors Q_1 and Q_2 are equal to V_s . The voltage ratings of all the diodes are also approximately equal to V_s .

V. DESIGN

The design of a triple-mode converter is simple and can be shown in the following steps.

1) Define the specification

 $V_s = 40 \text{ V}, P_o = 100 \text{ W}, \text{ switching frequency} = 215 \text{ kHz}.$

2) The period of resonant frequency is chosen to be less than the period of switching frequency so that a zero-current switching can be naturally achieved. Usually

$$T_o = 0.9T_s$$
.

This gives the switching frequency $f_o = 240 \text{ kHz}.$

3) The ripple voltage on the resonant capacitor C_{1a} and C_{1b} must be small compared to their dc level. The peak-to-peak ripple voltage is derived from (1), (3), (9), or (11))

$$\Delta v_{C1} = \frac{3}{2} I_o T_S \omega_0 Z_0.$$

A maximum voltage ripple of one-third of the dc component is allowed on the resonant capacitor. Hence, it gives $Z_o=1.51~\Omega.$

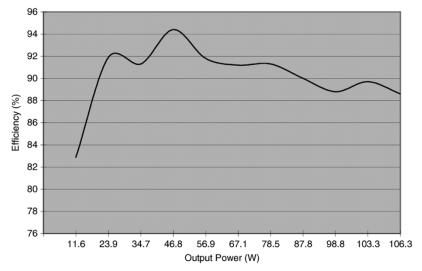


Fig. 8. Measured efficiency and output power of the triple-mode switched-capacitor resonant converter.

4) The resonant components can therefore be calculated by angular frequency and impedance from (4)–(5)

$$C_1 = \frac{1}{2Z_o\omega_0} = 0.22 \,\mu\text{F}$$

$$L_r = \frac{Z_o}{\omega_o} = 1 \,\mu\text{H}.$$

5) $C_2(C_{2a} \text{ and } C_{2b})$ is a larger capacitance and is to maintain constant voltage for each stage. Its value can be estimated by the basic capacitor ripple voltage calculation

$$\Delta V_{C2} \cdot \frac{I_0}{C_2} \left\{ \frac{\cos \theta}{f_s} \cdot \frac{1}{2f_0} \left(1 \cdot 2 \frac{\theta}{\pi} \right) \right\}$$

where $\theta = \sin^{-1}(f_s)/(\pi f_o)$ and $I_o = (P_o)/(V_o)$.

For 0.025-V ripple voltage, this gives $C_2=100~\mu\mathrm{F}$. This is to guarantee very good dc voltage on C_2 for the experiment. In fact, $10~\mu\mathrm{F}$ is good enough for practical circuit.

6) The transistor rating voltage is at least equal to V_s . The diode rating voltage is also equal to V_s but with a tolerance of ripple voltage on C_1 . Therefore, they are chosen a rating of at least 100 V.

VI. EXPERIMENTAL RESULTS

The circuit of step-up triple-mode converter shown in Fig. 2 has been tested in laboratory. The specification and component values of the prototype is as follows:

Input voltage	40V	
Output voltage	120V	
Output power	20W - 100W	
Switching frequency	215kHz	
Q ₁ and Q ₂	IRF530	
D ₁ and D ₂	MBR10100	
C _{1a} and C _{1b}	0.22μF	
C _{2a} and C _{2b}	100µF	
$L_{\rm r}$	1μН	

TABLE I
MEASURED EFFICIENCY INPUT AND OUTPUT VALUE OF TRIPLE-MODE
SWITCHED-CAPACITOR RESONANT CONVERTER

Input			Output			Efficiency
Volt(V)	I(A)	P(W)	Volt(V)	I(A)	P(W)	%
40	0.35	14	120.9	0.1	11.6	82.9
40	0.65	26	118.4	0.2	23.9	91.9
40	0.95	38	116.5	0.3	34.7	91.3
40	1.24	49.6	115.8	0.4	46.8	94.4
40	1.55	62	113.8	0.5	56.9	91.8
40	1.84	73.6	112.6	0.6	67.1	91.2
40	2.15	86	111.8	0.7	78.5	91.3
40	2.44	97.6	110.1	0.8	87.8	90
40	2.78	111.2	109.3	0.9	98.8	88.8
40	2.88	115.2	108.5	0.95	103.3	89.7
40	3	120	107.4	1	106.3	88.6

The measured waveforms at 100 W are shown in Fig. 7. The waveforms are very clean with no serious parasitic oscillation. From both Fig. 7(a) and (b), it is seen that both Q_1 and Q_2 are zero-current switching during turning on and off in a sinusoidal manner. The waveforms agree with the simulation as shown in Fig. 5 and the theoretical characteristics as shown in Sections III and IV. From the graph of characteristic of efficiency shown in Fig. 8 and Table I, it can be seen that the efficiency of the converter is around 90% at 100-W power output. It should be noted that a closed-loop voltage control is not necessary to add to the proposed converters. The voltage conversion ratio is fixed according to the topologies and varied slightly with the load as shown in Table I. The concept of these topologies is based on complete resonance energy transfer among the switching capacitors and hence the voltage conversion ratio is about fixed. They are working under a different concept as compared to the classical switched-capacitor converters.

Fig. 7(d) and (e) shows the voltage of C_{1a} and C_{1b} . It can be seen that there is a dc component of V_s and $2V_s$ on the volt-

ages of C_{1a} and C_{1b} respectively. The resonant component is small as expected. The amplitude of the resonant voltage and current have been examined and confirmed that they agree with the (1)–(11) derived, with a small deviation because of the energy loss in the circuit.

VII. CONCLUSION

This paper has introduced a family of step-up-mode resonant switched-capacitor converter including a 100-W output power triple-mode step-up experimental results. Mathematical modeling, generalized equation, computer simulation, and experiments have been presented. There is only a very small inductor providing resonance in each circuit. No large inductor is needed for energy storage. All switching devices in these circuits are under zero-current switching condition. Both switching loss and EMI have been reduced. High efficiency can then be obtained. From the experiment, it is shown that the efficiency of the converter can be around 90%. Also, current spike problem does not exist in all these circuits.

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K. K. Law received the B.Eng. degree in electrical engineering from the Hong Kong Polytechnic University, Hong Kong, in 1999.

He is an Assistant Engineer with Chevalier (H.K.) Ltd., Hong Kong. Since 2000, he has been a part-time research student at the Hong Kong Polytechnic University. His current research interests are switched-capacitor converters and power factor correction.



K. W. E. Cheng received the B.Sc. and Ph.D. degrees from the University of Bath, Bath, U.K., in 1987, and 1990, respectively.

He was a Project Leader and Principal Engineer at Lucas Aerospace Ltd., Birmingham, U.K. He joined the Hong Kong Polytechnic University, Hong Kong, in 1997, where he is now a Professor and the Director of the Power Electronics Research Centre. His research interest is in all the aspects of power electronics and drives. He has published seven books and more than 200 papers in international journals and

conferences.

Dr. Cheng received the IEE Sebastian Z De Ferranti Premium Award for Best Paper in 1995, the Outstanding Consultancy Award in 2000, and the Merit Award of Best Teacher of the Hong Kong Polytechnic University, in 2003.



Y. P. Benny Yeung was born in Hong Kong in 1974. He received the B.Eng. degree (Hons.) and Ph.D. degree in electrical engineering from The Hong Kong Polytechnic University, Hong Kong, in 1998 and 2004, respectively.

His principle research interests include soft-switching of switched-mode power supplies and switched reluctance motor drives.