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Design and Control of Grid Connected PWM Rectifiers by Optimizing Fractional Order PI Controller using Water Cycle Algorithm

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ABSTRACT In this paper water cycle algorithm based fractional order PI controller (FOPI) is proposed for virtual flux oriented control of three phase grid connected PWM rectifier. FOPI controller makes the PWM rectifier control more robust due to the fractional behavior. Fractional order controllers have additional degree of freedom and so wider range of parameters is available to provide better control and robustness in the plant. The optimization and design of FOPI controller is done using water cycle algorithm (WCA). WCA is an optimization method inspired by monitoring the water cycle operation and flow of water bodies like streams and rivers in the direction of sea. The performance of FOPI controllers are optimized and designed using WCA technique leading to WCA-PI and WCA-FOPI controllers. The system is tested using MATLAB/Simulink. The simulation results verify the better performance of WCA-FOPI in terms of settling time, rise time, peak overshoot and Total Harmonic Distortion (THD) of grid current. A robustness measurement with line filter parametric variations and non ideal supply voltage (unbalance and distorted supply voltage) is carried out. The WCA-FOPI demonstrates more robustness as compared to WCA-PI. Simulation findings validate the WCA-FOPI controller outcomes as compared to WCA-PI in terms of control effect and robustness.

INDEX TERMS PWM rectifier, VFOC, Water cycle algorithm, FOPID controller, fractional calculus

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I. INTRODUCTION

The power electronics converters are being used at all levels in power systems using renewable energy sources. The most commonly used power converter topology is the three phase voltage source converter. This converter is popular due to its capability to operate either as a rectifier or inverter. In rectifier mode, it is more commonly called as PWM rectifier. PWM rectifiers have been an ideal choice among different power quality improved rectifiers. The attractive features of these rectifies are better control of dc voltage, nearly unity power factor operation (grid voltage and current in same phase) and less harmonic content in grid current. The need for advanced control techniques of active rectifiers is felt by the researchers. One of the popular control method known as voltage oriented control (VOC) provides the active and reactive power control indirectly. Although VOC provides satisfactory response, however the operation is largely affected by the chosen current controller [1]. In VOC method, the ac side currents are transformed into active and reactive components and compared with reference currents respectively. The PI controllers are used to track the reference. Modulator block is used to generate gate signals. Fine tuning of PI controller is necessary to get satisfactory steady and dynamic response.

Another method which is simple to implement is known as direct power control (DPC) method. In this method without using inner current control loops, the active and reactive power is brought near reference values. Therefore the coordinate transformations are not needed [2]. The error in powers (active and reactive both)along with hysteresis controller and a switching logic table are used to produce the PWM signals Therefore no modulating blocks are required in DPC. So the performance of DPC depends on the accurate calculation or measurement of active and reactive power [2]. However hysteresis regulators ensure good dynamic behavior, but the drawback with DPC is not getting constant switching frequency. Another downside is requirement of high sampling frequency. The behavior of hysteresis regulators used in DPC causes the variable switching pattern of the semiconductor devices used in the converter [3]. The use of space vector pulse width modulation technique can be used to obtain constant switching frequency with DPC [1, 4]. The VOC and DPC methods can be applied based on voltage estimation using virtual flux and are called as virtual flux based VOC (VFOC) and virtual flux based DPC (VFDPC) methods.

PID controllers are well known for use in control applications in industry due to simple configuration. However in order to get high performance, tuning is necessary [5]. The unfolding of fractional calculus has shown the way towards changeover from classical PID controllers to fractional order PID (FOPID) controllers. The differential equations are of non-integer order in FOPID. A comparison of integer order and fractional order controllers is done for real life objects. The fractional order controllers

are found better and require less control effort than integer order controllers in industrial problems [6]. The author has explained the benefits, execution and commercial uses of FOPID controllers. The changeover from integer order controllers to fractional order controllers can be implemented globally. It can provide more tuning flexibility and better design specifications. Future focus should be to evolve the tools and directions so as to implement the transition to FOPID controllers [7]. The author has used FOPID in hybrid renewable power plant for the purpose of integration through a voltage source inverter. The power quality of the injected power is improved as compared to classical PID controller. The fractional order controller is less sensitive to variations in load and parameters, which means more freedom in choosing controller parameters. This allows us to pick out economical electronic components for the plant [8]. FOPID is used for grid integrated PV system to inject active and reactive power individually. The power quality of injected power is improved using FOPI controller during irradiation and load changes [9]. FOPID controller is used for stability control in a magnetic levitation system. The Maglev system model is designed in MATLAB/Simulink using first principle, which can be used for other applications. The fractional order controller demonstrated extremely better response compared to integer order controller [10]. The author has used FOPID controller in hybrid shunt active power filter to compensate harmonics and reactive power. The system is implemented under unbalance supply and with unbalanced load conditions. The developed system is economical, not complex, easy to implement and effective to eliminate the load generated harmonics [11]. A FOPID controller is designed for a DC-DC boost converter under different operating conditions. The simulation and experimental results show better response in terms of overshoot and recovery time using fractional order controller compared to integer order controller. The author suggested that fractional order controllers can be applied in step down and buck-boost DC-DC converters using the same formulations [12]. FOPID controller is applied to three phase induction motors to reduce the harmonic current, vibration, and noise. The controller design is based on the motor parameters [13]. A FOPID based on fuzzy is used in automatic governor control and tuned using imperialist competitive method. The simulation is implemented for isolated and interconnected systems. The FOPID controller is compared with other existing controllers. The system with FOPID is found to be robust against parameters and load variations [14].

As classical PID controllers need tuning of parameters, same is applicable to FOPID controllers as well. Several tuning methods can be found in literature to tune the parameters of PID controllers [15]. To achieve optimal tuning meta-heuristic methods prove to be better than methods such trial and errors based approach and Ziglernichols method. Cuckoo search algorithm is used in [16] to



tune the parameters of PID controller of an AVR system to improve the response. The simulation results validate better control action of cuckoo search (CS) algorithm compared to particle swarm optimization (PSO) and artificial bee colony (ABC) method. Kidney-inspired method is used in [17] to tune the parameters of PID controller of an AVR system to improve the transient response. The peak overshoot, rise time, settling time are reduced and steady state error is eliminated. The optimization methods used for PID controllers can also be used to tune the parameters of FOPID controllers. FOPID controllers offer much better adaptive behavior due to its five parameters available for tuning. The tuning algorithm for FOPID controllers are reviewed in [7]. The different methods have been applied for tuning of FOPID controller parameters in the literature such as simulated annealing, genetic algorithm, chaotic ant grey wolf optimization, particle swarm, swarm optimization, slap swarm algorithm, colliding bodies optimization, tabu search based algorithm, continuous state transition, moth flame, fire-fly and other meta-heuristic algorithms [7]. FOPID controllers are applied to AVR systems in many research papers and different optimization techniques have been used to tune the controller parameters. Chaotic ant swarm (CAS) algorithm is used to tune the parameters of FOPID controller in an AVR system. The objective function is to improve the transient response and reduce the steady state error. The simulation results verify the better performance of CAS-FOPID controller under model uncertainties also [18]. The author has used FOPID controller for AVR in [19] to improve multiobjective functions. The three objectives optimized are integral of absolute error (IAE), absolute steady-state error, and settling time. A multi-objective external optimization (MOEO) technique is proposed to achieve the multiobjective optimization. The Simulated Annealing (SA) method is used in an AVR system to tune the parameters of FOPID controller. The cost function is minimized using the SA method. The results indicated good control action and robustness against model uncertainties The [20]. employment of fraction calculus in power system has been studied in the areas of voltage control, automatic governor control and damping control [21]. The prospects of FOPID controllers in power converter applications are not explored until recently.

In this paper water cycle algorithm based fractional order PI controller (FOPI) is proposed for virtual flux oriented control of three phase grid connected PWM rectifier. FOPI controller makes the PWM rectifier control more robust due to the fractional behavior. Fractional order controllers have additional degree of freedom and so wider region of parameters is available to provide better control and robustness in the plant. One FOPI controller is used in the outer voltage loop and two FOPI current controllers in the inner current loops. The classical PI controllers are also used for comparison purpose. The optimization and design of both PI and FOPI controller is done using water cycle algorithm (WCA) technique leading to WCA-PI and WCA- FOPI controllers. The simulation results verify the better performance of WCA-FOPI in terms of less settling time, rise time, peak overshoot and Total Harmonic Distortion (THD) of grid current. A robustness measurement with filter parametric variations and non ideal supply voltage (unbalance and distorted supply voltage) is carried out. The WCA-FOPI demonstrates more robustness as compared to WCA-PI. Simulation findings validate the WCA-FOPI controller outcomes as compared to WCA-PI in terms of control effect and robustness.

The highlights of the current work are to:

- Develop a Simulink model of a VFOC based PWM rectifier.
- Design and optimize the WCA-PI controller for inner and outer loop controls.
- Design and optimize the WCA-FOPI controller for inner and outer loop controls.
- Estimate and compare the control actions of WCA-PI and WCA-FOPI controllers under balanced supply voltage conditions.
- Estimate and compare the control actions of WCA-PI and WCA-FOPI controllers under parametric variations.
- Estimate and compare the control actions of WCA-PI and WCA-FOPI controllers under unbalanced and distorted supply voltage conditions.

This research paper is divided into eight parts. The model of the rectifier and VFOC algorithm is explained in part II. The fractional order PID controller is discussed in part-III. The part IV presents the water cycle algorithm. Part V presents the MATALB simulation results and part-VI deals with the conclusion.

II. PWM RECTIFIER AND VFOC ALGORITHM

The three phase PWM rectifier circuit is shown in Fig.1.Six IGBT switches have been used in the bridge configuration. The line filter with resistance R and inductance L is connected on the input side. The line currents are labeled as i_a , i_b , i_c and the three phase ac voltages as E_a , E_b , E_c . The DC side of the converter is represented by of a filter C and a load resistance R_L . The load voltage and current are V_{dc} and I_L respectively. S_a , S_b and S_c are the switching state of the converter.

Applying the Kirchhoff's voltage law in Fig.1:

$$\begin{bmatrix} E_a \\ E_b \\ E_c \end{bmatrix} = R \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix} + L \frac{d}{dt} \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix} + \begin{bmatrix} v_a \\ v_b \\ v_c \end{bmatrix}$$
(1)

$$\frac{dv_c}{dt} = S_a i_a + S_b i_b + S_c i_c \tag{2}$$

The pole phase voltage of the rectifier is represented by the equation (3) to (5):

$$v_{an} = (2S_a - (S_b + S_c))\frac{V_{dc}}{3}$$
(3)
$$v_{bn} = (2S_b - (S_a + S_c))\frac{V_{dc}}{3}$$
(4)

Design and Control of Grid Connected PWM Rectifiers by Optimizing Fractional Order PI Controller using Water Cycle Algorithm

(5)



$$v_{cn} = \left(2S_c - (S_a + S_b)\right)\frac{v_{dc}}{3}$$

The co-ordinates transformation from three phases (abc) to stationary coordinates $(\alpha - \beta)$ is done using the following equation.

$$\begin{bmatrix} x_{\alpha} \\ x_{\beta} \end{bmatrix} = \frac{2}{3} \begin{bmatrix} 1 & -1/2 & -1/2 \\ 0 & \sqrt{3}/2 & \sqrt{3}/2 \end{bmatrix} \begin{bmatrix} x_{\alpha} \\ x_{b} \\ x_{c} \end{bmatrix}$$
(6)



FIGURE 1. PWM Rectilfer.

The VFOC algorithm based on voltage oriented control without ac line voltage sensor is applied. The voltage is estimated as in [3]. The FOPI controllers are used in place of traditional PI controllers in inner current loop and outer voltage loop. The parameters of FOPID controllers are optimized and designed using water cycle algorithm.



FIGURE 2. VFOC Scheme using WCA optimized FOPI controllers.

III. FRACTION ORDER PID CONTROLLER

In recent times, fraction order calculus has gained attention and applications have been explored in the field of control system [22-24]. Fractional order calculus can represent better and accurate model of real system as compared to classical integer theory.

The analysis of fractional order differential equations is given in [25-26]. The study on FOPID controllers is focused in the academic and commercial fields. The

VOLUME XX, 2021

benefits of FOPID controllers are moreover attractive in electrical, mechanical and electromechanical system models exhibiting characteristics of real materials and also in rheological features of rocks and more. The derivative and integral order is integer in classical PID controller, whereas in FOPID controller they are fractional.

The idea of FOPID was put forward by Podlunby in year 1997. It was found by Podlunby that FOPID controllers can perform better than PID controllers. The structure of FOPID is represented by $PI^{\lambda}D^{\mu}$ in [23-24]. The λ and μ are fraction numbers. The Fig.3 illustrates the schematic of FOPID controller.



FIGURE 3. FOPID Controller

The control action of FOPID controller can be represented equation (7) :

$$u(t) = K_p e(t) + K_i D^{-\lambda} e(t) + K_d D^{\mu} e(t)$$
(7)

The λ and μ are random real numbers. In case of classical PID controller these values are equal to one.

The equation (7) can be written in s-domain as:

$$u(s) = \left(K_p + \frac{K_i}{s\lambda} + K_E S^{\mu}\right)e(s)$$
(8)

The control domain of PID and FOPID can be shown by Fig.4.



FIGURE 4. FOPID and PID Controller domain

The major benefit of FOPID controller is to increase in performance of non linear and dynamic systems; and have less sensitivity to changes in parameters of the system. However the challenges involved are the design and implementation cost. The FOPID controller requires five parameters to be optimized whereas PID controller needs to optimize only three parameters. Hence the design of FOPID controller is more challenging than PID controller. Although being more technically advantageous, the IEEE Access

implementation cost and cost benefits obtained from FOPID controller needs further investigation. The prospects of FOPID controllers in power converter applications are not explored until recently. The employment of fraction calculus in power system has been studied in the areas of voltage control, automatic governor control and damping control.

The design and tuning of controller parameters is very crucial part in a control system. Usually trial and error procedure is used to tune the parameters of a PID controller. The controller parameters obtained by this method is time consuming and the parameters obtained may not be the finest one. Optimization techniques are sought after as it required less time and gives optimal values of parameters [27]. Particle swarm optimization (PSO) is used in [28-30] to tune the fractional order controllers. Atom search optimization (ASO) method is used for tuning of FOPID controller and to control the frequency automatically in a hybrid power system [31]. The ASO method is quite simple to apply and based on the theory of atomic motion behavior and can be used in to find optimal solution in broad range of applications. An advanced design of ASO method is ChASO. This method is established on the basis of logistic map chaotic pattern and better solution is obtained by avoiding local minima stagnancy. The ChASO is used by the author in [32] to control the speed of dc motor. Adaptive Colliding Bodies Optimization (ACBO) method has been used for tuning of FOPID in [27] for robotic control. Some others optimization techniques such as Tabu search, harmony search, grey wolf optimization, Quantum bacterial foraging have been used in literature [33-36].

IV. WATER CYCLE ALGORITHM

Water cycle algorithm (WCA) is based on imitation of nature inspired water cycle process and describes how the water flow from high mountain ranges through rivers, streams and merges into sea. The rain water is collected in streams and rivers and finds way towards the sea. This water is converted into vapors and cause cloud formation. The clouds on condensation let out the water back by means of rain drops or snowfall and get collected in streams and rivers. The WCA follows the water cycle approach by irregularly created rain drops. The rain drops can be characterized by an array and leads to the optimal solution of a problem. The sea is called the lowest point as the water finally gets collected into the sea through rivers and streams. The sea or rivers or streams are considered as rain drops by this algorithm. Where sea is the finest rain drop, as it has least objective function value (for minimization). Thereafter, rivers having values nearest to the best objective value are chosen. Rivers proceed on the way to sea and streams proceed towards rivers or move to sea. The water cycle algorithm finds new solution as water move to the sea. The rivers move towards sea and vaporization of sea water takes place. In case all rivers approach the fitness values same as sea, then it means complete vaporization has

happened. So the rain starts again and hence completion of water cycle. If a stream moving into a river discovers better value of cost function then the direction of flow is reversed (position of stream and river is interchanged).

A stream is specified by a matrix A as below:

$$A_i = [A_1 A_2 A_3 A_4 \dots, A_N]$$
(9)

If total number of streams is considered of size N_{pop} , then the whole population comprising of sea plus rivers can be expressed by arbitrarily formed matrix of dimensions $N_{POP} \times N$ as below:



The N_{POP} is the population size and N is the design variable. The defined designed variables in the matrix can be real values (floating type). The cost of every stream (each row is a stream) considering the cost function can found as below.

$$C_i = Cost_i = f(A_1^i, A_2^i, \dots, A_N^i)$$

$$i = 1, 2, 3 \qquad N_{\text{non}}$$

$$(11)$$

Now the best stream (which has least cost or most fitness) is picked as the rivers and sea. The best stream is recognized as the sea. So, Nsr is the sum of number of rivers and one sea. The remaining population i.e N_{stream} is recognized as streams moving to rivers or merging straight into sea. This can be represented by the following equations:

$$N_{sr} = Number \ of \ rivers + 1(sea) \tag{12}$$

$$N_{stream} = N_{POP} - N_{sr} \tag{13}$$

The stream population moving to sea and river can be expressed by

$$Population \ of \ streams = \begin{bmatrix} S_1 \\ S_2 \\ S_3 \\ \vdots \\ S_{N_{stream}} \end{bmatrix}$$
$$= \begin{bmatrix} A_1^1 & A_2^1 & A_3^1 & \dots & A_N^1 \\ A_1^2 & A_2^2 & A_3^2 & \dots & A_N^2 \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ A_1^{N_{stream}} & A_2^{N_{stream}} & A_3^{N_{stream}} & \vdots & A_N^{N_{stream}} \end{bmatrix}$$
(14)

Design and Control of Grid Connected PWM Rectifiers by Optimizing Fractional Order PI Controller using Water Cycle Algorithm



Now the number of streams moving to rivers and sea can be found as:

$$NS_n = round \left\{ \left| \frac{C_n}{\sum_{n=1}^{N_{sr}} C_n} \right| \times N_{streams} \right\}$$
(15)

Where
$$n = 1,2,3,...,N_{sr}$$

 $C_n = Cost_n - Cost_{N_{sr+1}}, \quad n = 1,2,3,...,N_{sr}$ (16)

 N_{sr} is the count of streams, which moves to specified sea and rivers. Fig.5 represents the streams flow to a specified river with the connection line.

The new positions of streams and rivers are proposed in following equations:

$$\vec{A}_{stream}(t+1) = \vec{A}_{stream}(t) + rand \\ \times C\left(\vec{A}_{sea}(t) - \vec{A}_{stream}(t)\right) \quad (17)$$

$$A_{stream}(t+1) = A_{stream}(t) + rand$$
$$\times C\left(\vec{A}_{river}(t) - \vec{A}_{stream}(t)\right)$$
(18)

$$\vec{A}_{river}(t+1) = \vec{A}_{river}(t) + rand \\ \times C\left(\vec{A}_{sea}(t) - \vec{A}_{river}(t)\right)$$
(19)

where, t is marked as iteration index and rand is steadily distributed number between zero and one. The updating equation (17) depicts the movement of stream towards the sea, equation (18) represents the movement of stream to the rivers and equation (19) is representing movement of rivers towards the sea. If the solution of any stream is found to be superior to connected river, then the positions of them are interchanged. So, the following iteration appraise stream as river and river as stream. However the same is applicable to a river and sea.

The next step is evaporation which results into precipitation. This step prevents hasty convergence to local optima. For this river and streams should be in the neighborhood of sea. The equation (20) checks weather evaporation followed by rain will occur or not in a river or stream

$$if \|\vec{A}_{sea}^{t} - \vec{A}_{river_{j}}^{t}\| < d_{max} \text{ or } rand < 0.1$$
(20)
Where $j = 1, 2, 3, \dots, N_{sr} - 1$

Where d_{max} is very small quantity and is near zero. This value determines the search depth close to the sea. The higher value will increase the search intensity whereas smaller one decreases the search intensity.

The value of d_{max} decreases after each iteration as per the following equation.

$$d_{max}(t+1) = d_{max}(t) - \frac{d_{max}(t)}{Max. iteration}$$

$$Where t = 1,2,3, \dots, Max. iteration.$$
(21)

Once evaporation activity is fulfilled then raining procedure is applied. The new rain drops from streams fall at distinct

VOLUME XX, 2021

positions. The position on newly set up streams can be calculated using the equation below.

 $A_{stream}^{new} = LB + rand \times (UB - LB)$ (22) Where UB is the upper bound and LB is the lower bound specified by the system. The flowchart of the WCA is shown in Fig.6.



FIGURE 5. Schematic diagram showing (a) Flow of streams into a particular river; (b) WCA optimization procedure.

As described above in this section, the sea or rivers or streams are considered as rain drops by the WCA and the rain drops are characterized by an array. The sea is the finest rain drop, as it has least objective function value (for minimization). The parameters of PI and FOPI controller are tuned by the water cycle algorithm. The problem variables in the VFOC scheme of PWM rectifier are K_P, K_I for PI controller whereas K_P, K_I and λ for FOPI controllers. So, these variables are defined as stream (rain drops) array. The cost function is integral time absolute error (ITAE). The selected population size is 50. The LB is taken as zero and UB is selected as 20.The value of d_{max} is taken as 1e⁻¹⁶.The outer loop PI controller parameters obtained by WCA are K_P=0.4048 and K_I=20. The inner loop PI

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parameters obtained by WCA are K_P =0.2179, K_I =11.7736.The outer loop FOPI parameters obtained by WCA are K_P =0.3713, K_I =1.9075 and λ =1.0006. The inner loop FOPI parameters obtained by WCA are K_P =17.593, K_I =14.04 and λ =0.7942.



V. SIMULATION RESULTS

The proposed method of VFOC using WCA-PI and WCA-FOPI is verified using Matlab with Simulink and Fomcon toolbox. "The FOMCON toolbox for MATLAB is a fractional-order calculus based toolbox for system modeling and control design. The approximation implemented in the toolbox is the most commonly used Recursive Approximation (ORA)."The Oustaloup approximation order is set to 5 and frequency range is taken as (0.001, 1000) for the purpose of approximation. The

simulation study is done under three conditions. In the first case, the simulation is performed with three phase balanced and ideal supply. In second case, it is implemented with line filter parametric uncertainties. The value of line filter resistance and inductance is decreased. And in the third case, the performance of the rectifier is evaluated under unbalanced and distorted supply conditions.

A. PROPOSED VFOC SCHEME WITH BALANCED SUPPLY

The VFOC method using WCA-PI and WCA-FOPI controllers is simulated using MATLAB/Simulink. A three grid supply line voltage of 415V is given to the input terminals of the rectifier and dc reference voltage is set to 600V. The line filter parameters are 0.001Ω and 3 mH. A full resistive load of 10kW is connected across the capacitor. The simulation results using WCA-PI controller are shown in Fig. 7-8.







Design and Control of Grid Connected PWM Rectifiers by Optimizing Fractional Order PI Controller using Water Cycle Algorithm



FIGURE 8. Phase a voltage and current at unity pf and frequency spectrum of line current generated by WCA-PI Under balanced three supply

The current scale is zoomed in five times to improve the visibility in Fig.8 (a). These figures demonstrate that the dc side voltage is 600V, power factor is close to unity and THD of supply phase current is 7.54%.

The simulation results using WCA-FOPI are shown in Fig. 9-10. The current scale is zoomed in five times to improve the visibility in Fig.10 (a). These figures demonstrate that the dc side voltage is 600V, power factor is close to unity and THD of grid phase current is 1.49%.



FIGURE 9. Performance of WCA-FOPI controller under balanced three phase supply (a) DC Link voltage three-phase voltage supply. (b) Three phase currents



FIGURE 10. Phase a voltage and current at unity pf and frequency spectrum of line current generated by WCA-FOPI under balanced three supply

VOLUME XX, 2021

Fig. 11 shows the comparison dc link voltage of WCA-PI and WCA-FOPI controllers. It can be observed that settling time of FOPI controller is less than the PI controller, so FOPI controller improved the stability of the system. The peak overshoot is 660V using WCA-PI controller and it is 600 V using WCA-FOPI controller. The rise time is 0.02 sec using WCA-FOPI and using 0.042 using WCA-PI controller. At the same the THD of phase current is 7.54% with WCA-PI and 1.49% with WCA-FOPI controller. The FOPID controller provides better control of non linear system which results into less current harmonics with WCA-FOPI than WCA-PI controller. It can be concluded that the control action in terms of rise time, peak-overshoot and harmonic content is better using WCA-FOPI controller. The Fig.12 shows the convergence characteristics of WCA-PI and WCA-FOPI controllers. This figure demonstrates that the WCA-FOPI converges fast than WCA-PI.

A step change in load is applied at from 10kW to 15 kW at 0.1 sec and then from 15kW to 20 kW at 0.15 sec. The load disturbance characteristics of output voltage are overlapped in the both cases as shown in Fig.13 It is observed that both WCA-PI and WCA-FOPI provide same type of behavior under load disturbances. The load voltage is restored to reference voltage when load is increased to 15 kW. But when the load is increased to 20 kW, the load voltage does not reach set point using WCA-PI and WCA-FOPI.

The Fig.14 shows the effect of controller saturation on the output dc voltage. A step change in reference voltage is applied at 0.1 sec from 600V to 700V. The output response in WCA-PI is delayed more than WCA-FOPI controller. The output voltage settles to reference voltage of 700V at 0.14 sec in case of WCA-FOPI and at 0.18 sec in case of WCA-PI controller. The Fig.15 shows the reference sine waveform for generating PWM. The noise present in the modulating waveform of WCA-PI and WCA-FOPI is reflected into the response of the rectifier. The bode plot of outer voltage loop is given in Fig.16. The gain margins are 48.908dB and 44.5278 dB using WCA-FOPI and WCA-PI controllers respectively. The phase margin with WCA-PI controller is 110.14 and 98.01 using WCA-PI controller. The WCA-FOPI has more gain and phase margin compared to WCA-PI controller.



FIGURE 11. The DC link voltage using WCA-PI and WCA-FOPI controllers under balanced three phase supply

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Design and Control of Grid Connected PWM Rectifiers by Optimizing Fractional Order PI Controller using Water Cycle Algorithm



FIGURE 12. Convergence characteristics of WCA-PI and WCA-FOPI



FIGURE 13. Load disturbance characteristics of WCA-PI and WCA-FOPI





FIGURE 14. Controller under saturation in WCA-PI and WCA-FOPI

FIGURE 15. Reference sine waveform for pwm signal generation for (a) WCA-PI (b) WCA-FOPI



FIGURE 16. Bode plot of the outer voltage loop with WCA-PI and WCA-FOPI

B. PROPOSED VFOC SCHEME UNDER PARAMETRIC UNCERTAINTIES

The VFOC method using both types of controllers under parametric variation is simulated using MATLAB/Simulink. A three grid line voltage of 415V is Voltage is set to 600V. The line filter parameters are reduced to 0.0008Ω and 2.8 mH. The filter inductor parameters are changed uniformly in all three phases. A

full resistive load of 10kW is connected. The simulation results are shown in Fig. 17-19. The current scale is zoomed in five times to improve the visibility in Fig.18 (a) and Fig.19(a). The comparison of dc voltage tracking using both types of controllers is shown in Fig.17.The peak overshoot using WCA-PI is more than using WCA-FOPI controller. The rise time is smaller with WCA-FOPI than WCA-PI controller. The power factor close to unity is achieved using both types of controllers. Moreover the THD using WCA-PI controller is increased to 8.44% and using WCA-PI controller is 1.59%. So, it be concluded that WCA-FOPI controller provides better control effect as compared to WCA-PI controller under parametric variations also. It can be summarized that WCA-FOPI provides more robustness against parametric uncertainties.







Phase a voltage and current at unity pf and frequency FIGURE 18. line current generated by WCA-PI under parametric spectrum of variations



parametric variations

C. PROPOSED VFOC SCHEME USING FOPI UNDER UNBALANCE AND DISTORTED SUPPLY

The VFOC method using both types of controllers under unbalance supply voltage is simulated using MATLAB/Simulink. A three grid line voltage of 415V is given to the input terminals of the rectifier and dc reference voltage is set to 600V. The line filter parameters are 0.001Ω and 3 mH. A full resistive load of 10kW is connected across the capacitor. The simulation results can be seen in Fig. 20-23. The unbalance is due to different voltage of

three phases. The THD of phase a supply voltage is 11.79% as shown in Fig.21.

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FIGURE 20. The DC link voltage using WCA-PI and WCA-FOPI controllers under unbalanced and distorted three phase supply



FIGURE 21. Frequency spectrum of phase a supply voltage



Three phase voltage and current at unity pf and frequency FIGURE 22 spectrum of line current generated by WCA-PI under unbalanced and distorted three phase supply

The comparison of dc voltage tracking using both types of controllers is shown in Fig.20. The peak overshoot using WCA-PI is 1050V and 800 V using WCA-FOPI controller.

VOLUME XX, 2021

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The settling time is smaller with WCA-FOPI than WCA-PI controller. The power factor close to unity is achieved using both types of controllers. Moreover the THD using WCA-PI controller is increased to 7.95% and using WCA-PI controller is 1.63%. However both types of controllers draw balanced supply current during unbalanced and distorted supply conditions. It can be validated that WCA-FOPI demonstrates more robustness against supply disturbances.



FIGURE 23. Three phase voltage and current at unity pt and frequency spectrum of line current generated by WCA-FOPI under unbalanced and distorted three phase supply

A comparison of THD and peak overshoot obtained by using both type controllers under different conditions is done in table I. It can be concluded from the table that the WCA-FOPI controller provides more robustness and better control effect than the WCA-PI controller.

D. SENSITIVITY ANALYSIS

Considering the base case of balanced supply conditions in section V(A), a sensitivity analysis is carried out to prospect the effectiveness of the proposed controller with -26.67% change in line filter inductance value, 25% voltage sag in phase a to create unbalance. The results are shown in Fig.23-24.

The value of inductance of line filter is reduced by 26.67% (2.2 mH) as compared to base case. The THD of grid current is increased to 12.35 % and 1.91% in the case of WCA-PI and WCA-FOPI respectively. For a change of the line filter value by -26.67%, the THD of grid current increased by 63.79% for WCA-PI and 28.18% for WCA-FOPI controllers. The FOPI controller is found to be less sensitive to parametric variation of line filter. The voltage of phase a is reduced by 25% as compared to base case and other phases voltage is kept to normal value. The line current THD increased to 12.66% and 1.63% for WCA-PI

and WCA-FOPI respectively. For a change in input voltage of 25%, the change in THD of grid current is 67.9% for WCA-PI controller and 2.515% for WCA-FOPI controller. Therefore, the WCA-FOPI ifs found to be less sensitive to input voltage variations. It can be concluded that WCA-FOPID controller is more robust to parametric variations and supply disturbances.



FIGURE 23. Ffrequency spectrum of line current with line filter inductance L=2.2 mH (a) WCA-PI (b) WCA-FOPI







TABLE I. Comparison of THD and Peak overshoot		
Control effect	WCA-PI	WCA-FOPI
THD under ideal supply	7.54%	1.49%
THD under parametric uncertainties	8.44%	1.59%
THD under Non ideal supply voltage	7.95%	1.63%
Peak-overshoot under ideal supply	660V	600V
Peak-overshoot under Parametric	650V	600V
uncertainties		
Peak-overshoot under Non ideal supply	1050V	800V
voltage		

VI. CONCLUSION

A water cycle algorithm based fractional order PI controller is proposed to implement virtual flux oriented control scheme in three phase PWM rectifier. Water cycle based fractional order PI (WCA-PI) and integer order PI (WCA-PI) controllers are designed and optimized. WCA is an optimization method inspired by monitoring the water cycle operation and flow of water bodies like streams and rivers in the direction of sea. The fractional order controllers have additional degree of freedom and provide more robust control effect. The major benefit of FOPID controller is to increase in performance of non linear and dynamic systems; and having less sensitivity to changes in parameters of the system. The rectifier is operated under three conditions; a) balanced supply conditions, b) parametric uncertainties, c) and distorted supply unbalance conditions. The simulation results verify the better performance of WCA-FOPI in terms of settling time and stability, rise time, peak overshoot and Total Harmonic distortion of grid current under balance supply conditions. The WCA-FOPI converges faster than WCA-PI. The both types of observed controllers same response under load disturbances. The input line filter parameters are changed to evaluate the performance under parametric uncertainties. The value of inductance and resistance is reduced. A more robust response is recorded with WCA-FOPI. Moreover under unbalance and distorted supply, both types of controllers give balanced supply currents. However, the peak overshoot, settling time and THD of grid current are increased under unbalance and distorted supply voltage. But the WCA-FOPI is found to be better and more robust in these evaluation parameters. The simulation findings validate the WCA-FOPI controller outcomes as compared to WCA-PI in terms of control effect and robustness.

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