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# Design and Optimization of a 3-Coil Inductive Link for Efficient Wireless Power Transmission

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# Abstract

Inductive power transmission is widely used to energize implantable microelectronic devices (IMDs), recharge batteries, and energy harvesters. Power transfer efficiency (PTE) and power delivered to the load (PDL) are two key parameters in wireless links, which affect the energy source specifications, heat dissipation, power transmission range, and interference with other devices. To improve the PTE, a 4-coil inductive link has been recently proposed. Through a comprehensive circuit based analysis that can guide a design and optimization scheme, we have shown that despite achieving high PTE at larger coil separations, the 4-coil inductive links fail to achieve a high PDL. Instead, we have proposed a 3-coil inductive power transfer link with comparable PTE over its 4-coil counterpart at large coupling distances, which can also achieve high PDL. We have also devised an iterative design methodology that provides the optimal coil geometries in a 3-coil inductive power transfer link. Design examples of 2-, 3-, and 4-coil inductive links have been presented, and optimized for 13.56 MHz carrier frequency and 12 cm coupling distance, showing PTEs of 15%, 37%, and 35%, respectively. At this distance, the PDL of the proposed 3-coil inductive link is 1.5 and 59 times higher than its equivalent 2- and 4-coil links, respectively. For short coupling distances, however, 2-coil links remain the optimal choice when a high PDL is required, while 4-coil links are preferred when the driver has large output resistance or small power is needed. These results have been verified through simulations and measurements.

# Keywords

Wireless power transmission; implantable microelectronic devices; power transfer efficiency; inductive links

# I. Introduction

Inductive power transmission can be used to either continuously power up a device or temporarily recharge its batteries without any direct electrical contact between the energy source and that device. A high efficiency power amplifier (PA), connected to the main energy source on the transmitter side (Tx), often drives the primary coil, which is mutually coupled to a secondary coil on the receiver side (Rx), which is connected to the load ( $R_L$ ). The load can cover a wide range of applications from high performance and sophisticated implantable microelectronic devices (IMD) with relatively high power consumption (>100 mW), such as cochlear and retinal implants, to simple and low power radio frequency

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identification (RFID) tags that cannot use primary batteries due to their cost, size, or lifetime constraints [1]-[6].

The mutual inductance between a pair of coupled coils, M, is proportional to  $d^{-3}$ , where d is the center-to-center spacing between the coils when they are in parallel planes and perfectly aligned [5]. A key requirement in all of the above applications is to deliver sufficient power to the load with high power transfer efficiency (PTE) when d is relatively large or the coils are misaligned, i.e. when M is very small (PTE is already large enough for small d). Large PTE is meant to reduce heat dissipation within the coils, tissue exposure to AC magnetic field, which can cause additional heat dissipation in IMDs, size of the main energy source, and interference with nearby electronics to satisfy regulatory requirements [7]-[9].

Design, theoretical analysis, and geometrical optimization of the conventional 2-coil inductive links have been covered extensively in the literature over the last three decades [10]-[21]. More recently, a 4-coil power transmission link was proposed in [22] to further increase the PTE, particularly at large *d*. In the 4-coil arrangement, which schematic diagram is shown in Fig. 1a, a pair of coils is used on the Tx side, which are referred to as the driver,  $L_1$ , and primary,  $L_2$ , coils. A second pair of coils is used on the Rx side, which are referred to as the secondary,  $L_3$ , and load,  $L_4$ , coils. All of these coils are tuned at the same resonance frequency,  $f_0$ , using capacitors  $C_1 \sim C_4$ . The coils' parasitic resistances are also shown by  $R_1 \sim R_4$ . The 4-coil method has so far been adopted for transferring power to multiple small receivers, transcutaneous power transmission for  $d = 10 \sim 20$  mm, and recharging mobile devices in [23], [24], and [25], respectively. However, an in-depth comparative circuit analysis of this arrangement that can guide a design and optimization scheme for such applications is still lacking.

In this paper, we have analyzed the 4-coil inductive link utilizing the reflected load theory [5], which is more familiar to circuit designers than the coupled-mode theory used by the physicists in [26], and compared it with its conventional 2-coil counterpart. Our analysis shows that utilizing the 4-coil method increases the PTE at large d at the cost of a significant reduction in the power delivered to the load (PDL). Therefore, unless the application requires a small amount of power (10s of mW or less), a high driving voltage ( $V_s$ ) will be required, which can reduce the driver efficiency and lead to safety issues in medical applications. Instead, we have demonstrated that a 3-coil inductive power transfer link, initially proposed in [26], not only provides as high PTE as the 4-coil method but also offers a PDL that is significantly higher than both 2- and 4-coil links at large d. In the following section we have constructed a circuit-based theoretical framework to analyze and compare 2-, 3-, and 4-coil inductive links. Section III describes the design and optimization procedure for the 3- and 4-coil inductive links. Measurement results are included in section IV, followed by discussions and concluding remarks in sections V and VI, respectively.

#### II. Theory of Multiple Inductively Coupled Coils

Fig. 1b shows the simplified schematic diagram of a 2-coil inductive link. It is known that the highest PTE across this link can be achieved when both LC tanks are tuned at the same

resonance frequency,  $f_0=1/2\pi \sqrt{L_2C_2}=1/2\pi \sqrt{L_3C_3}$  [18]. The effect of the Rx side on the Tx side can be modeled at resonance by calculating the reflected impedance,

$$R_{ref} = k_{23}^2 \omega_0 L_2 Q_{3L} = k_{23}^2 R_2 Q_2 Q_{3L}, \tag{1}$$

where  $k_{23}=M_{23}/\sqrt{L_2L_3}$ ,  $Q_2 = \omega_0 L_2/R_2$ , and  $Q_{3L} = Q_3 Q_L/(Q_3+Q_L)$ , in which  $Q_3 = \omega_0 L_3/R_3$ and  $Q_L = R_L/\omega_0 L_3$  [5].  $Q_L$  is often referred to as the load quality factor, and the value for

 $M_{23}$  can be calculated from (31) in the Appendix. Hence, the primary loop can be simplified at resonance as the circuit shown in Fig. 1c. It should be noted that  $R_2$  in Fig. 1c also includes  $R_s$ , the output impedance of the driver circuitry,  $V_s$ .

To derive an equation for the PTE at resonance, we should consider that the power provided by  $V_s$  divides between  $R_2$  and  $R_{ref}$ , and the power delivered to  $R_{ref}$ , i.e. the power that is received by the secondary loop, divides between  $R_3$  and  $R_L$ , which are the only power consuming components on the Rx side. This will lead to [18]

$$\eta_{2-coil} = \frac{k_{23}^2 Q_2 Q_{3L}}{1 + k_{23}^2 Q_2 Q_{3L}} \cdot \frac{Q_M}{Q_L}.$$
(2)

Note that the first and second terms in (2) correspond to the power division between  $R_2$  and  $R_{ref}$ , and  $R_3$  and  $R_L$ , respectively.

The amount of power delivered to the load (PDL), on the other hand, can be calculated by multiplying the power provided by  $V_{s_1}$  i.e.  $V_s^2/2(R_2+R_{ref})$ , by the PTE from (2)

$$P_{L,2-coil} = \frac{V_s^2}{2R_L} \frac{k_{23}^2 Q_2 Q_{3L}}{\left(1 + k_{23}^2 Q_2 Q_{3L}\right)^2} \cdot \frac{Q_{3L}}{Q_L}.$$
(3)

The resonant energy exchange between two conductive objects has been analyzed based on the coupled-mode theory (CMT) in [28]. Utilizing this theory, the PTE between a pair of capacitively loaded conducting loops, such as  $L_2$  and  $L_3$  spaced by a certain distance, d, can be found from [26], [28]

$$\eta = \frac{1}{1 + \frac{\Gamma_3}{\Gamma_L} \left[ 1 + \frac{\Gamma_2 \Gamma_3}{K^2} \left( 1 + \frac{\Gamma_L}{\Gamma_3} \right)^2 \right]},\tag{4}$$

where  $\Gamma = \omega_0/2Q$  is the resonance width due to the loop's intrinsic loss and

 $K = \omega_0 M/2 \sqrt{L_1 L_2}$  is the coupling rate between the two loops. It can be shown that (4) will result in (2) if we substitute  $\Gamma_2 = \omega_0/2Q_2$ ,  $\Gamma_3 = \omega_0/2Q_3$ ,  $\Gamma_L = \omega_0/2Q_L$  and  $K = \omega_0 k_{23}/2$  [29].

If the simple 2-coil inductive link in Fig. 1b is extended to an *m*-coil link, in which  $1^{st}$  and  $m^{th}$  coils are connected to the energy source and load, respectively, the reflected load from the  $(j+1)^{th}$  coil to the  $j^{th}$  coil can be found from

$$R_{ref} \quad _{j,j+1} = k_{j,j+1}^2 \omega_0 L_j Q_{(j+1)L}, \qquad j = 1, 2, \dots, m-1$$
(5)

where  $k_{j,j+1}$  is the coupling coefficient between the  $j^{\text{th}}$  and  $(j+1)^{\text{th}}$  coils and all coils are tuned at the same resonance frequency,  $f_0$ .  $Q_{(j+1)L}$  is the loaded quality factor of the  $(j+1)^{\text{th}}$  coil which can be found from

$$Q_{jL} = \frac{\omega_0 L_j}{R_j + R_{ref} \quad j, j+1} = \frac{Q_j}{1 + k_{j,j+1}^2 Q_j Q_{(j+1)L}}, \ j=1, 2, \dots, m-1$$
(6)

where  $Q_j = \omega_0 L_j/R_j$  and  $R_j$  are the unloaded quality factor and parasitic series resistance of the *j*<sup>th</sup> coil,  $L_j$ , respectively. It should be noted that for the last coil, which is connected to the load in series,  $Q_{mL} = \omega_0 L_m/(R_m + R_L)$  and for the first coil, which is connected to the source,  $R_I$  also includes the source output impedance,  $R_s$ . Therefore, assuming that the coupling between non-neighboring coils is negligible, the PTE from the *j*<sup>th</sup> coil to (*j*+1)<sup>th</sup> coil can be written as

$$\eta_{j,j+1} = \frac{R_{ref}}{R_j + R_{ref}} \frac{j,j+1}{j,j+1} = \frac{k_{j,j+1}^2 Q_j Q_{(j+1)L}}{1 + k_{j,j+1}^2 Q_j Q_{(j+1)L}}.$$
(7)

Using (5), (6), and (7), the overall PTE in such a multi-coil inductive link can be found from

$$\eta_{m-coil} = \prod_{j=1}^{m-1} \eta_{j,j+1} \cdot \frac{Q_{mL}}{Q_L},$$
(8)

and the PDL from

$$P_{L,m-coil} = \frac{V_s^2}{2R_1} \frac{1}{1 + k_{12}^2 Q_1 Q_{2L}} \eta_{m-coil}.$$
(9)

For (8) and (9) to be valid, all coils should be tuned at the same resonance frequency to also achieve the highest PTE and PDL between each neighboring pair of coils [18], and maximize the PTE and PDL of the multi-coil link.

#### A. Optimal 2-Coil Power Transfer Link

The PTE profile of the 2-coil inductive link according to (2) is a monotonically decreasing function of the coils' coupling distance,  $d_{23}$ . However, for a given set of  $Q_2$ ,  $Q_3$  and  $k_{23}$  values, there is an optimal load,  $R_{L,PTE} = \omega_0 L_3 Q_{L,PTE}$ , which can maximize the PTE at that particular  $d_{23}$ .  $Q_{L,PTE}$  can be found by calculating the derivative of (2) vs.  $Q_L$  from

$$Q_{LPTE} = \frac{Q_3}{\left(1 + k_{23}^2 Q_2 Q_3\right)^{1/2}}.$$
(10)

The maximum PDL at a certain  $d_{23}$  can be achieved when the reflected impedance from (1) matches the primary coil impedance, i.e.  $R_{ref} = R_2$  [30]. It should also be noted that in this condition, the PTE is always less than 50%, because half of the power is dissipated in  $R_2$ . Thus, the coupling coefficient which maximizes PDL for a certain  $R_L$  can be found from,

$$k_{23,PDL} = \frac{1}{(Q_2, Q_{3L})^{1/2}}.$$
(11)

Alternatively, by calculating the derivative of (3) vs.  $Q_L$ , one can find the optimal load,  $R_{L,PDL} = \omega_0 L_3 Q_{L,PDL}$ , which can maximize the PDL at a particular  $d_{23}$ , where

$$Q_{L,PDL} = \frac{Q_3}{1 + k_{23}^2 Q_2 Q_3}.$$
(12)

Page 5

It is important to note that according to (10) and (12), the maximum PTE and PDL cannot be achieved simultaneously with the same  $R_L$  or  $d_{23}$ . In the 2-coil links, each of these conditions requires a specific set of  $k_{23}$ ,  $Q_2$ , and  $Q_3$ , which may not be feasible within the designated constraints. On the other hand, a multi-coil solution provides the designer with more degrees of freedom to optimize the inductive link based on either one of the above requirements. This is the basic idea behind the 3- and 4-coil inductive links, despite their potential negative impact on the size-constrained applications.

#### **B. 4-Coil Power Transfer Inductive Link**

The PTE in the 4-coil inductive link, shown in Fig. 1a, can be found by reflecting the resistive components to the left from the load coil back to the driver coil loop, one stage at a time using (5), and calculating the portion of the power that is delivered to the following stage, using (7), until it reaches  $R_L$ 

$$\eta_{4-coil} = \frac{\left(k_{12}^2 Q_1 Q_2\right) \left(k_{23}^2 Q_2 Q_3\right) \left(k_{34}^2 Q_3 Q_{4L}\right)}{\left[\left(1+k_{12}^2 Q_1 Q_2\right) \cdot \left(1+k_{34}^2 Q_3 Q_{4L}\right)+k_{23}^2 Q_2 Q_3\right] \cdot \left[1+k_{23}^2 Q_2 Q_3+k_{34}^2 Q_3 Q_{4L}\right]} \cdot \frac{Q_{4L}}{Q_L}}{Q_L}$$
(13)

To simplify this equation,  $k_{13}$ ,  $k_{14}$  and  $k_{24}$  have been neglected in comparison to coupling coefficients between neighboring coils, which are  $k_{12}$ ,  $k_{23}$  and  $k_{34}$  [24]. Using the same method, the PDL in the 4-coil inductive link can be found from

$$P_{L,4-coil} = \frac{V_s^2}{2R_1} \frac{\left(k_{12}^2 Q_1 Q_2\right) \left(k_{23}^2 Q_2 Q_3\right) \left(k_{34}^2 Q_3 Q_{4L}\right)}{\left[\left(1+k_{12}^2 Q_1 Q_2\right) \cdot \left(1+k_{34}^2 Q_3 Q_{4L}\right)+k_{23}^2 Q_2 Q_3\right]^2} \cdot \frac{Q_{4L}}{Q_L}$$

$$14)$$

The PTE between loosely coupled primary and secondary coils,  $L_2$  and  $L_3$ , is the dominant factor in determining the overall PTE of the 4-coil link at a large coupling distance,  $d_{23}$ . When  $R_L$  reflects onto  $L_3$  from  $L_4$  according to (5), it reduces the quality factor of  $L_3$  from  $Q_3 = \omega_0 L_3/R_3$  to

$$Q_{3L} = \frac{Q_3}{1 + k_{34}^2 Q_3 Q_{4L}},\tag{15}$$

based on (6). In order to maximize the PTE between  $L_2$  and  $L_3$ ,  $Q_{3L}$  in (15) should satisfy (10).  $k_{34}$  in (15) is, therefore, a key parameter in 4-coil links which allows designers to maximize the PTE for any arbitrary  $R_L$ . As mentioned in section II.A, this flexibility is not available in a 2-coil link. Similarly, the total impedance in the secondary coil reflects onto the primary coil, based on (5), and reduces the primary coil's quality factor from  $Q_2 = \omega_0 L_2/R_2$  to

$$Q_{2L} = \frac{Q_2}{1 + k_{23}^2 Q_2 Q_{3L}}.$$
(16)

From (16) and (7) it can be inferred that a strong coupling between the primary and secondary coils (i.e. a high  $k_{23}$ ) reduces  $Q_{2L}$  and consequently  $\eta_{12}$ , which is the PTE between  $L_1$  and  $L_2$ . It should also be noted that according to (16),  $Q_{2L}$  is roughly proportional to  $k_{23}^{-2}$ , where  $k_{23}$  is further proportional to  $d_{23}^{-3}$  [5]. Therefore,  $Q_{2L}$  is proportional to  $d_{23}^{6}$  implying that  $\eta_{12}$  will significantly reduce at small  $d_{23}$  if  $k_{12}$  is not

chosen large enough. This effect has been demonstrated in Fig. 2a, which shows the PTE of a 4-coil inductive link as a function of  $k_{12}$  and  $d_{23}$  for the coils used in our measurements and specified in Table I. It can be seen that for small  $k_{12}$ , near the origin, the PTE has dropped at short coupling distances due to the small  $\eta_{12}$ . Therefore, small  $Q_1$  and  $k_{12}$  will result in a significant drop in  $\eta_{12}$  at small coupling distances according to (7).

In order to avoid the above problem,  $k_{12}$  should be kept large, which according to (5) results in a large reflected load onto  $L_1$ . This can reduce the available power from the source, according to (9), unless  $V_s$  is increased. However, large  $V_s$  can cause safety issues in medical applications, and this is a major disadvantage of the 4-coil arrangement for inductive power transfer to IMDs, particularly when a high PDL is required.

Fig. 2b shows the PDL from (14) as a function of  $k_{12}$  and  $d_{23}$  for the coils in Table I. It can be seen that increasing  $k_{12}$  results in reducing the PDL when  $V_s$  is kept constant. A comparison between Figs. 2a and 2b is instructive by observing that the high PTE and high PDL areas of these surfaces do not overlap, which means that in a 4-coil inductive link there is always a compromise between the highest PTE that can be achieved while delivering sufficient power to the load without surpassing safe  $V_s$  limits. This can be seen in [25] where  $k_{12}$  has been purposely reduced to achieve a high PDL. The result of  $k_{12}$  reduction, however, is a drop in PTE from 70% to 10% in short coupling distances. Thus, considering the above issues and the size overhead, the utility of the 4-coil links in high power IMD applications is questionable.

The optimal PTE with respect to  $d_{23}$  in a 4-coil link can be found by differentiating (13) in terms of  $k_{23}$ , which gives

$$k_{23,PTE} = \left(\frac{\sqrt{1 + k_{12}^2 Q_1 Q_2} \cdot \left(1 + k_{34}^2 Q_3 Q_{4L}\right)}{Q_2 Q_3}\right)^{1/2}.$$
(17)

This equation helps designers to shift the peak of the PTE profile in Fig. 2a towards the nominal coupling distance for certain  $k_{12}$  and  $k_{34}$  values. Similarly, the optimal PDL, can be found by differentiating (14) in terms of  $k_{23}$ , which results in

$$k_{23,PDL} = \left(\frac{\left(1 + k_{12}^2 Q_1 Q_2\right) \cdot \left(1 + k_{34}^2 Q_3 Q_{4L}\right)}{Q_2 Q_3}\right)^{1/2}.$$
(18)

#### C. 3-Coil Power Transfer Inductive Link

The 3-coil inductive link circuit model, which comprises of the primary coil,  $L_2$ , on the Tx side and the secondary and load coils ( $L_3$  and  $L_4$ ) on the Rx side, has been shown in Fig. 3. The PTE of this link with no simplification can be found from

$$\eta_{3-coil} = \frac{\left(k_{23}^2 Q_2 Q_3\right) \left(k_{34}^2 Q_3 Q_{4L}\right) + k_{24}^2 Q_2 Q_{4L}}{\cos\left(\theta\right) \left(1 + k_{34}^2 Q_3 Q_{4L}\right) \sqrt{A^2 + B^2}} \cdot \frac{Q_{4L}}{Q_L}$$
(19)

where A, B, and  $\theta$  are

$$A = 1 + k_{23}^2 Q_2 Q_3 + k_{34}^2 Q_3 Q_{4L} + k_{24}^2 Q_2 Q_{4L}, B = 2 Q_2 Q_3 Q_{4L} k_{23} k_{24} k_{34}, \theta = \tan^{-1} {B / A}.$$
(20)

Also the PDL of the 3-coil inductive link can be found from

$$P_{L3-coil} = \frac{V_s^2}{2R_2} \frac{(k_{23}^2 Q_2 Q_3)(k_{34}^2 Q_3 Q_{4L}) + k_{24}^2 Q_2 Q_{4L}}{A^2 + B^2} \cdot \frac{Q_{4L}}{Q_L}.$$
(21)

If we ignore  $k_{24}$  due to large separation between  $L_2$  and  $L_4$ , then (19) can be simplified to

$$\eta_{3-coil} = \frac{\left(k_{23}^2 Q_2 Q_3\right) \left(k_{34}^2 Q_3 Q_{4L}\right)}{\left[\left(1+k_{23}^2 Q_2 Q_3+k_{34}^2 Q_3 Q_{4L}\right) \left(1+k_{34}^2 Q_3 Q_{4L}\right)\right]} \cdot \frac{Q_{4L}}{Q_L} = \eta_{23}\eta_{34}$$
(22)

where

$$\eta_{23} = \frac{k_{23}^2 Q_2 Q_{3L}}{1 + k_{23}^2 Q_2 Q_3} = \frac{k_{23}^2 Q_2 Q_3}{1 + k_{23}^2 Q_2 Q_3 + k_{34}^2 Q_3 Q_{4L}},$$
  

$$\eta_{34} = \frac{k_{34}^2 Q_3 Q_{4L}}{1 + k_{34}^2 Q_3 Q_{4L}}, \frac{Q_{4L}}{Q_L}.$$
(23)

Similarly, (21) can be simplified to

$$P_{L,3-coll} = \frac{V_s^2}{2R_2} \frac{\left(k_{23}^2 Q_2 Q_3\right) \left(k_{34}^2 Q_3 Q_{4L}\right)}{\left(1 + k_{23}^2 Q_2 Q_3 + k_{34}^2 Q_3 Q_{4L}\right)^2} \cdot \frac{Q_{4L}}{Q_L}$$
(24)

The problem with the optimal 2-coil power transfer link in section II.A was that for a given set of  $Q_2$ ,  $Q_3$ , and  $k_{23}$ , the optimal PTE could only be achieved for a certain load,  $R_{L,PTE}$ , which could be far from the nominal  $R_L$ . In the 3-coil power transfer inductive link, however,  $L_3$ ,  $L_4$  and  $M_{34}$  in Fig. 3 can play the role of an impedance matching circuit (compare with Fig. 1b), which can convert any arbitrary  $R_L$  to  $R_{L,PTE}$ . This is equivalent to having a load quality factor of  $Q_L = Q_{L,PTE}$  in the secondary loop of a 2-coil link, which was defined in (10).

This leverage in the design of the 3-coil links has been provided by  $k_{34}^2 Q_3 Q_{4L}$  term in (22)-

(24). Lowering  $k_{34}^2 Q_3 Q_{4L}$  tends to increase  $\eta_{23}$  and at the same time reduces  $\eta_{34}$  in (23), both of which affect the overall PTE in (22). To better understand the PTE variations in a 3-coil inductive link, the effects of  $k_{34}$  and  $d_{23}$  on the PTE are shown in Fig. 4a for the coils

specified in Table-I. The optimal value for  $k_{34}^2 Q_3 Q_{4L}$  that maximizes the PTE for a certain  $d_{23}$  (or  $k_{23}$ ) can be found by differentiating (22) with respect to  $k_{34}$ ,

$$k_{_{34,PTE}} = \left(\frac{1 + k_{23}^2 Q_2 Q_3}{Q_3^2 Q_{4L}^2}\right)^{1/4} = \left(\frac{\left(1 + k_{23}^2 Q_2 Q_3\right) \cdot \left(1 + R_L / R_4\right)^2}{Q_3^2 Q_4^2}\right)^{1/4}.$$
(25)

For a certain  $R_L$ , if the choice of  $k_{34}$  in the design of a 3-coil inductive link satisfies (25), then the reflected load onto the secondary loop will satisfy (10) and maximizes the PTE.

Fig. 4b shows the effects of  $k_{34}$  and  $d_{23}$  on the PDL of the 3-coil inductive link in Table-I, based on (24). It can be seen that there are optimal values for both  $k_{34}$  and  $k_{23}$ , which can maximize PDL, and in order to find them, (24) should be differentiated with respect to  $k_{34}$  and  $k_{23}$ ,

$$k_{23,PDL} = \left(\frac{1 + k_{34}^2 Q_3 Q_{4L}}{Q_2 Q_3}\right)^{1/2},$$
(26)

$$k_{34,PDL} = \left(\frac{1 + k_{23}^2 Q_2 Q_3}{Q_3 Q_{4L}}\right)^{1/2}.$$
(27)

These values result in the reflected load on to the primary coil to be equal to  $R_2$ , in order to satisfy (12) for any arbitrary  $R_L$ .

A comparison between Figs. 4 and 2 reveals a key advantage of the 3-coil links over their 4coil counterparts, which suffer from poor PDL in areas of the curve that PTE is high (see section II.B). Comparing Figs. 4a and 4b, however, shows that by proper choice of  $k_{23}$  and  $k_{34}$ , which depend on the coil values and their geometries, designers can establish 3-coil inductive power transfer links that offer both high PTE as well as high PDL. Another advantage of the 3-coil links is that they are not affected by the inefficiency between the driver and primary coils ( $\eta_{12} < 1$ ).

Fig. 5a compares the 2-coil and 3-coil links' optimal load quality factors,  $Q_{L,PTE}$ , vs.  $d_{23}$  to maximize the PTE for the coils in Table I. Three important points to learn from these curves are: 1) The 2-coil link needs an exceedingly higher  $Q_{L,PTE}$  as  $d_{23}$  increases, which may not be feasible, particularly in small coils. On the other hand, the 3-coil link satisfies the PTE optimization requirement at various distances with much smaller  $Q_{L,PTE}$ , which is quite feasible by connecting  $R_L$  in series with  $L_4$  as shown in Fig. 3. 2) The optimal  $Q_{L,PTE}$  in the 3-coil link is adjustable with  $k_{34}$  based on (25), as shown in Fig. 5b, where the optimal PTE has been maintained for the 3-coil link in a wide range of  $R_L$  (10  $\Omega - 1$  k $\Omega$ ) at  $d_{23} = 5$  cm. On the other hand, with a 2-coil link the optimal PTE has been achieved in these conditions only for a specific  $R_{L,PTE} = 200 \Omega$  that satisfies (10). 3) At small  $d_{23}$ , the 2-coil link requires smaller  $Q_{L,PTE}$ , which is relatively easy to achieve. Therefore, for short distance inductive power transmission, which is the case in most transcutaneous IMD applications, a conventional 2-coil inductive link that is properly designed can be very close to the optimal choice [20], [21].

The additional degree of freedom provided by 3- and 4-coil inductive links via  $k_{34}$  allows designers to increase the loaded quality factor of  $L_3$  ( $Q_{3L}$ ). This leads to better immunity to misalignment but at the same time higher sensitivity to carrier frequency variations or detuning in multi-coil links. Note that misalignment only happens between  $L_2$  and  $L_3$ , because  $L_1$  and  $L_2$  in 4-coil links and  $L_3$  and  $L_4$  in 3- and 4-coil links are often housed together in the Tx and Rx sides, respectively. There is also little concern about detuning of  $L_4$  and  $L_1$  because these coils have very small loaded quality factors and therefore are much less sensitive to frequency shifts.

#### III. Optimal Design of Multi-Coil Inductive Links

In this section, we extend the design and optimization procedure, which we introduced in [20] for maximizing the PTE in 2-coil wireless power transmission links to multiple coils. Either (19) or (22) can be used for the optimization of PTE in 3-coil links. However, the former can complicate the procedure, which may not be necessary if  $k_{24}$  is very small. As mentioned in [20], most of the design constraints are set by the inductive link application, and the rest of them by the coil fabrication process. For instance, in IMD applications the size of  $L_3$  depends on the IMD location in the body. Because to maximize the PTE, the outer diameter of  $L_3$ ,  $D_{o3}$ , should be increased to the largest size allowed by the application.

We have provided further details about coils designed for the IMD applications in section V. However, in this section we have chosen an inductively powered wireless neural recording system for freely behaving small animal subjects as our design and optimization example [31]. A key limitation of the current wireless neural recording systems that are developed for neuroscience applications is the need for the animal subject to carry a large payload of batteries for continuous recording over several hours or even days [32] - [34]. This may not be a major issue for larger animal subjects such as non-human primates [35], [36]. However, such a payload can affect the behavior of smaller animals such as rats and mice, which are more common in behavioral neuroscience labs due to their lower cost [37]. The goal here is to substitute the batteries by  $L_3$  and  $L_4$  in the animal headstage, and  $L_2$  at the bottom of the cage. For such an application, we chose  $D_{o3}$ ,  $d_{23}$ , and  $d_{34}$  equal to 4 cm, 12 cm, and 0.9 cm, respectively, as the starting point of this design example (see Table I).

#### A. Design Procedure

We showed in section II.C that the optimal 3-coil link can be considered as the loosely coupled  $L_2$ - $L_3$  link when the arbitrary  $R_L$  is transformed to  $R_{L,PTE}$ , utilizing  $L_4$  and  $k_{34}$  to satisfy (10). Therefore, the optimization procedure, shown in Fig. 6 flowchart, has two parts:

First,  $\eta_{23}$  is maximized in (23) by maximizing  $k_{23}^2 Q_2 Q_3$ , which requires optimizing  $L_2$  and  $L_3$  geometries like what we did for a 2-coil inductive link in [20]. Second, the geometry of  $L_4$  is optimized for  $k_{34}$  to satisfy (25), and consequently maximize  $\eta_{34}$  in (23) by maximizing  $k_{34}^2 Q_3 Q_{44}$ .

One of the decisions that should be made early on is whether the coils are lithographically defined or wire-wound. Geometrical parameters of the printed spiral coils (PSC) that affect circuit parameters such as Q and k, and consequently the PTE, are the line width (w), line spacing (s), outer diameter ( $D_o$ ), and fill factor ( $\varphi$ : the ratio between the difference and the sum of a PSC's inner and outer diameters), which are described in [20]. In wire-wound coils (WWC) made of single filament solid wires, w is the wire diameter, the number of turns (n: integer) is used instead of  $\varphi$ , and s can be twice the thickness of the wire insulation. The relationship between circuit parameters and the coil geometries in this case can be found in the Appendix. In each step of this optimization scheme, the designer should derive k, Q, and other circuit parameters from the PSC and WWC geometries using the equations presented in [20] and the Appendix, respectively. Moreover, to consider the finite quality factor of the resonance capacitors ( $C_{1-4}$ ) and the resistance of their connections to the coils, an additional 0.1  $\Omega$  was added to  $R_{1-4}$  values.

In step-1, design constraints imposed by the application and coil fabrication technology are considered. The former defines the maximum values for  $D_{o3}$  and  $D_{o4}$ , while the latter indicates the minimum line width and line spacing ( $w_{min}$ ,  $s_{min}$ ) in the case of PSC, or the wire specifications in WWC. The nominal values for  $d_{12}$ ,  $d_{23}$ ,  $d_{34}$ ,  $R_L$  and  $R_s$  are also required in this step, which are dependent on the application ( $d_{12}$  is needed only for 4-coil

links). For instance,  $d_{34}$  will depend on the implant thickness in IMD applications if  $L_3$  and  $L_4$  are going to be housed together. As mentioned earlier,  $R_s$ , which is a property of the driving circuitry, should be added to  $R_2$  and  $R_1$  in our procedure for the design of 3- and 4- coil links, respectively.

In step-2, the initial values for  $L_2 \sim L_4$  geometries are chosen, which are  $(w_2 \sim w_4, s_2 \sim s_4, \varphi_2 \sim \varphi_4, D_{o2})$  and  $(w_2 \sim w_4, s_2 \sim s_4, n_2 \sim n_4, D_{o2})$  for PSCs and WWCs, respectively. A more detailed discussion about how to choose these initial values can be found in [20].

 $L_2$  and  $L_3$  geometries are optimized in step-3 for  $\eta_{23,max}$ . In step-3.1, following the procedure in [20] provides the optimal values of  $(w_2, w_3, \varphi_2, \varphi_3, D_{o2})$  for PSCs. Running the same iterative procedure while replacing  $(\varphi_2, \varphi_3)$  with  $(n_2, n_3)$  in the Appendix provides the optimal values of  $(w_2, w_3, n_2, n_3, D_{o2})$  for WWCs. In step-3.2, values found in step-3.1 are used to sweep  $s_2$  and  $s_3$  in [20] or in the Appendix for PSCs or WWCs, respectively, such

that the resulting  $k_{23}$ ,  $Q_2$ , and  $Q_3$  maximize  $k_{23}^2 Q_2 Q_3$ . The new  $s_2$  and  $s_3$  values are then fed back into step 3.1 to improve  $\eta_{23}$  further. Steps 3.1 and 3.2 are repeated iteratively until  $s_2$  and  $s_3$  values change less than 0.1% and satisfy the condition in step-3.3.

In step-4, the geometry of  $L_4$  is optimized using  $L_2$  and  $L_3$  circuit parameters from step-3, such that the resulting  $k_{34}$ ,  $R_4$ , and  $Q_4$  satisfy (25). In step-4.1 for PSCs,  $\varphi_4$  and  $D_{o4}$  are swept in [20] for the resulting  $k_{34}$  and  $Q_4$  to maximize  $\eta_{3-coil}$  in (22). Similarly for WWCs,  $n_4$  and  $D_{o4}$  are swept for the resulting  $k_{34}$  and  $Q_4$  from the Appendix to maximize  $\eta_{3-coil}$ . In step-4.2, the new  $\varphi_4$  and  $D_{o4}$  values found in step-4.1 for PSCs are used to sweep  $s_4$  and  $w_4$  in [20] for the resulting  $k_{34}$  and  $Q_4$  to further maximize  $\eta_{3-coil}$  in (22). For WWCs,  $n_4$  and  $D_{o4}$  values from step-4.1 are used to sweep  $s_4$  and  $w_4$  in the Appendix for the resulting  $k_{34}$  and  $Q_4$  to further maximize  $\eta_{3-coil}$ . Steps 4.1 and 4.2 are repeated iteratively until  $s_4$ ,  $w_4$  and  $D_{o4}$  values change less than 0.1% and satisfy the condition in step-4.3. This step concludes the design of the 3-coil wireless power transmission link for maximum PTE, which can be further validated using field solvers, such as HFSS (Ansoft, Pittsburgh, PA).

The rest of steps in Fig. 6 are specific to 4-coil links to optimize the geometry of  $L_1$  for the highest PTE based on (13). In step-5, the initial values for  $L_1$  geometry, which are  $(w_1, s_1, \varphi_1, D_{o1})$  and  $(w_1, s_1, n_1, D_{o1})$  for the PSCs and WWCs, respectively, are chosen. Step-6 is quite similar to step-4, which determined the optimal geometry of  $L_4$ . The iterative process in steps 6.1 and 6.2, and the condition in step-6.3 will ensure  $\eta_{12,max}$  and consequently maximize  $\eta_{4-coil}$  in (13), which can be validated by field solvers.

#### **B. Design Example**

Table I summarizes the results of optimization procedure for two sets of 2-, 3- and 4-coil inductive links that operate at  $f_0 = 13.56$  MHz and deliver power to a load of  $R_L = 100 \Omega$  as efficiently as possible from a nominal coupling distance of  $d_{23} = 12$  cm. To discriminate between the losses that are specific to the inductive link and those that are related to the driver circuit, thus out of the scope of this work, we considered a small  $R_s$  of only 0.1  $\Omega$  in our optimizations to account for the driver output resistance. The effect of  $R_s$  on the PTE and PDL of the 2-, 3- and 4-coil inductive links, however, has been discussed in more details in section V. Based on the requirements of our application, the coils on the Tx side were considered overlapping hexagonal shaped PSCs, fabricated on cost effective 1.5 mm thick FR4 printed circuit boards (PCB) with 1-oz copper weight (35.6 µm thick), and those on the Rx side were considered WWCs made of magnet wire (enameled copper).

In these designs, the PCB fabrication process requires  $w_{min}$  and  $s_{min}$  to be 150 µm. Also in the case of the 4-coil design, the overlapping  $L_1$  and  $L_2$  determine  $d_{12}$  by the PCB thickness (see Fig. 9). As mentioned earlier, to limit the size of the headstage,  $D_{o3}$  and  $d_{34}$  were also

limited 4 cm and 0.9 cm, respectively. The first set of coils, designated by "optimal" in Table I, are resulted from the iterative optimization process, as shown in Fig. 6, with no additional constraints. According to the equations in section II, the optimized 3- and 4-coil inductive links can achieve PTE of 55% and 54%, respectively, compared to the 2-coil inductive link, which PTE is limited to 27.4% at  $d_{23} = 12$  cm. Despite their similarity in PTE, a key difference between the 3- and 4-coil links is that the former has a PDL of 146 mW for  $V_s = 1$  V, while the latter can only deliver 6.8 mW to the load because of the large reflected impedance,  $R_{ref}$ , onto the driver coil,  $L_1$ . The PDL of the 2-coil link in these conditions is 160 mW.

In the second set of coils, designated by "measurement", the PSC diameter on the Tx side  $(D_{o1}, D_{o2})$  was limited to 16.8 cm due to PCB fabrication constraints. The total weight of the Rx coils that are going to be mounted on the animal headstage was limited to  $W_{3,4} = 1.6$  g, which relate to the WWC geometries according to (39) in the Appendix. Hence, WWC wire diameter on the Rx side  $(w_3, w_4)$  was limited to 0.64 mm (AWG-22) to observe the headstage weight limitation. This set of coils was fabricated and used in section IV measurements.

# **IV. Simulation and Measurement Results**

Two types of setups have been used in the past for PTE measurements. In the first method, shown in Fig. 7a, a network analyzer is directly connected to the primary and secondary coils to measure the S-parameters. Then the S-parameters are converted to Z-parameters [38] to obtain,

$$Q_{2} = \frac{\operatorname{Im}(Z_{22})}{\operatorname{Re}(Z_{22})}, Q_{3} = \frac{\operatorname{Im}(Z_{33})}{\operatorname{Re}(Z_{33})}, k_{23} = \sqrt{\frac{\operatorname{Im}(Z_{23}) . \operatorname{Im}(Z_{32})}{\operatorname{Im}(Z_{22}) . \operatorname{Im}(Z_{33})}},$$
(28)

and find the PTE by substituting them in (2). This method is straightforward, but it does not involve any actual power transfer between the coils. It is bound to the assumptions and accuracy of the models within the theoretical PTE and PDL equations. It also becomes more complicated and less accurate in multi-coil links, which should be tuned at a certain resonance frequency in order to operate properly (see Fig. 1a).

In the second method, shown in Fig. 7b, a signal generator or PA drives the primary coil, tuned at  $f_0$ , and the transmitted power is calculated by directly measuring the current and voltage waveforms. The received power can also be found in the same way by probing the voltage across  $R_L$ . Even though this method is more realistic than the first one, it rapidly loses its accuracy at higher carrier frequencies, such as 13.56 MHz, due to the parasitic components introduced by measurement probes. Moreover, the oscilloscope ground connections can introduce additional complications due to ground loops and interference. Our experiments showed that using different values of R in Fig. 7b for sensing the inductive link input current could result in different values for the PTE and PDL.

We have devised a new method for PTE and PDL measurements, which seems to be more accurate particularly in multi-coil inductive links. In this method, resonance capacitors and  $R_L$  are connected to the primary and load coils, which are then considered a complete 2-port system along with the multi-coil inductive link, as shown in Fig. 7c. The network analyzer is then used to measure the S-parameters, and consequently the Z-parameters are derived, as in the first method [38]. PTE and PDL are found from 2-port equations,

$$PTE = \frac{|Z_{42}|^2}{R_L |Z_{22}|\cos(\ell Z_{22})},$$
  

$$PDL = \frac{|V_4|^2}{2R_L} = \frac{|V_2|^2}{2R_L |Z_{22}|^2} |Z_{42}|^2.$$
(29)

where  $Z_{22} = V_2/I_2$  and  $Z_{42} = V_4/I_2$  are derived when  $I_4 = 0$ . The  $I_4 = 0$  requirement in calculating Z-parameters ensures that the network analyzer loading (often 50  $\Omega$ ) on the inductive link does not affect the results. In this method, as the network analyzer sweeps a certain frequency range that includes  $f_0$ , actual power transfer does take place in the form of a small signal injected from Port-1 of the network analyzer to  $R_L$ . One can also measure the entire link power transfer efficiency all the way from the battery to the load by adding the equivalent of the source output resistance,  $R_s$ , in series with  $L_1$  in the 4-coil link and  $L_2$  in the 2- and 3-coil links.

Figs. 8a and 9a show the experimental setup for measuring the PTE and PDL of the 3- and 4-coil inductive links, respectively. These coils were fabricated based on the values listed in the "Measurement" columns of Table I, and held in parallel and perfectly aligned using non-conducting Plexiglas sheets and plastic screws to prevent power loss due to eddy currents. Figs. 8b and 9b show 3-D models of the same coils constructed in the HFSS electromagnetic field simulator for 3- and 4-coil links, respectively. In the 4-coil setup,  $k_{12}$  was adjusted for a fixed  $d_{12} = 1.5$  mm, by changing the amount of overlapping between similar  $L_1$  and  $L_2$  (see Fig. 9).  $L_3$  and  $L_4$  were also similar and provided  $k_{34} = 0.22$  at  $d_{34} = 9$  mm.

Figs. 10a and 10b compare the measured, simulated (via HFSS), and calculated (see section II) values of the PTE and PDL, respectively, vs. coupling distance,  $d_{23}$ , in 2-, 3- and 4-coil inductive links. The curves labeled as "Meas1" show the measurement results according to the method proposed in Fig. 7c, using a ZVB4 network analyzer (R&S, Germany). It can be seen that these results are in very good agreement with HFSS simulation and calculation results, labeled "Sim" and "Calc", respectively.

As an alternative, we also measured the PTE and PDL of the inductive links according to the method shown in Fig. 7b, using a class-D PA with known power efficiency ( $\eta_{PA} = 30\%$ ) and  $R = 15 \Omega$  for 2- and 3-coil links, and  $R = 500 \Omega$  for 4-coil link (due to low current levels) in three different distances of 4, 8, and 12 cm, which are labeled as "Meas2" in Fig 10. In this case the measurement results are probably less accurate because of the parasitic components added by the probes and the fact that the PA's power efficiency has some dependency on the reflected impedance onto the Tx side, which changes with  $d_{23}$ . Nonetheless they are close to the other values.

It can be seen in Fig. 10a that the 3- and 4-coil inductive link PTEs (37% and 35%, respectively) are significantly higher than the PTE of the 2-coil link (15%) at  $d_{23} = 12$  cm. At the same coupling distance, however, the 3-coil inductive link has achieved a PDL of 260 mW from  $V_s = 1$  V, which is 1.5 and 59 times higher than the PDL of 2- and 4-coil links, respectively. Despite its high PTE, the 4-coil link has only been able to deliver 4.4 mW to the load under these conditions, which may not be sufficient for most applications. It thus requires a much higher  $V_s$  (~7.7 times in this case) to become comparable to its 3-coil counterpart. It can also be seen from the 2-coil PTE profile in Fig. 10a that short and large distances have smaller PTE variation. However, there is a certain coupling distance in between where the PTE drops very rapidly. The second derivative of (2) can correlate

 $k_{23}=1/\sqrt{3Q_2Q_{3L}}$  to this distance.  $Q_2$  and  $Q_{3L}$  should preferably be maximized to move this point to larger distances.

In the 2-coil link used in our measurements,  $R_L = 100$  ohm, is connected in parallel with  $L_3$  to achieve a higher  $Q_L = 9.8$ .  $Q_{3L}$  is only 8.9 and  $R_{ref}$ , according to (1), is 0.053  $\Omega$  at  $k_{23} = 8.8 \times 10^{-3}$ . Thus, (2) estimates  $\eta_{2\text{-coil}}$  to be 13.5%. According to Fig. 5a, the optimal  $Q_L$  in this case is 65, which is much larger than the realistic 9.8 value, which can be achieved following our optimization process and applying design constraints.

On the other hand, if we consider the 3-coil inductive link and  $R_L$  in series with  $L_4$ ,  $Q_L = 0.34$  which is close to the optimal value for PTE ( $Q_L = 0.26$ ) according to Fig. 5a.  $R_{ref,34}$  is 0.56 ohm at  $k_{34} = 0.22$ , which results in  $\eta_{34} = 74.6\%$  based on (5) and (7), respectively. Therefore,  $Q_3 = 177$  is loaded to become  $Q_{3L} = 45.4$ , based on (6), and remains much higher than  $Q_{3L} = 8.9$  of the 2-coil link. Finally,  $R_{ref,23}$  is 0.28  $\Omega$  at  $k_{23} = 9 \times 10^{-3}$ , which results in  $\eta_{23} = 48.3\%$  based on (5) and (7). Finally,  $\eta_{3-coil} = 0.746 \times 0.483 \times 0.998 = 36\%$ , where 99.8% represents the division of power between  $R_4$  and  $R_L$ . In these conditions,  $Q_2 = 255$  reduces to  $Q_{2L} = 132$  based on (6).

In the case of the 4-coil link,  $R_{ref,12}$  and  $\eta_{12}$  are 41.5  $\Omega$  and 99.3% at  $k_{12} = 0.064$  based on (5) and (7), respectively, which lead to more or less the same PTE as the 3-coil link. Nonetheless, comparing the reflected loads seen by the PA in 2-, 3- and 4-coil links (0.053, 0.28, and 41.5  $\Omega$ , respectively) clearly explains the reason for low PDL in the 4-coil link.

If one is interested in calculating the overall efficiency all the way from  $V_s$  to  $R_L$ , including the driver, then  $R_s = 0.1 \Omega$  should be added to  $R_2$ ,  $R_2$ , and  $R_1$  in (2), (19), and (13) for 2-, 3- and 4-coil links, respectively, which yield PTEs of 11%, 31%, and 35%. These correspond to the PDLs of 98 mW, 187 mW, and 4.4 mW for  $V_s = 1$  V, respectively.

# V. Discussion

In Fig. 10a, the 4-coil simulated and measured PTE at small  $d_{23}$  are up to 10% lower than the calculated results. This could be because of approximating the overlapping hexagonalshaped coils in Fig. 9a with a pair of circular coils (due to their complex geometry) for calculating  $k_{12}$ . We found that for these coils, calculations give a higher  $k_{12} = 0.09$ compared to HFSS simulations,  $k_{12} = 0.064$ . This resulted in larger error at small  $d_{23}$ , where the reflected load onto  $L_2$  is larger, and a higher  $k_{12}$  can overestimate  $\eta_{12}$ . It is worth noting that the higher estimation of  $k_{12}$  also results in lower available power from the source, leading to the calculated PDL at short coupling distances to be smaller than the simulation and measurement results, as it can be seen in Fig. 10b. Another reason for the discrepancy could be a larger percentage of error in the actual coil distances and alignments at lower  $d_{23}$ .

We added the source output resistance,  $R_s$ , representing the driver loss, to  $R_I$  and  $R_2$  in 4and 2/3-coil links, respectively, to consider its effects on the optimization procedure. The  $R_s$ value, which depends on the PA design, plays an important role in optimization of the overall power efficiency,  $\eta_{ov}$ , from the energy source to the load [20]. Other key parameters that affect the PA design are the power required by the load ( $P_L$ ), source voltage ( $V_s$ ), supply voltage ( $V_{DD}$ ), transistors breakdown voltage, and safety limits for the IMD applications

[16]. The available power from source,  $P_{av}$ , can be expressed as  $V_s^2/8R_s$ , which implies that large  $V_s$  or small  $R_s$  are desired when  $P_L$  is large. In a class-E PA, zero-voltage-switching allows for high power efficiency with peak voltages across the coil and PA transistor that are 1.07 and 3.56 times  $V_{DD}$ , respectively [40]. Therefore, when the application involves large  $P_L$  in the order of 100s of mW,  $R_s$  should be reduced to levels well below 1  $\Omega$  for the PA to provide sufficient  $P_{av}$  at reasonable  $V_s$  and  $V_{DD}$  [16], [25].

To compare the effects of  $R_s$  on 2-, 3- and 4-coil inductive links optimization, including the PA losses, we have optimized our design example in Table I for different values of  $R_s$  from

0.1 to 5  $\Omega$ . It can be seen in Fig. 11 that the 4-coil link maintains its high PTE even at large  $R_s$  values due to its large reflected impedance,  $R_{ref} >> R_s$ , at the cost of very small PDL. On the other hand, for  $R_s$  values below 1  $\Omega$ , the 3-coil link offers almost the same PTE, while providing much higher PDL. Therefore, we can conclude that for the applications that require small amounts of PDL in the order of 10s of mW, a 4-coil inductive link with a weak driver provides the highest  $\eta_{ov}$  while keeping  $V_s$  within reasonable range. Because utilizing large transistors in this case to reduce  $R_s$  results in increased dynamic switching losses [18].

In order to compare the PTE and PDL of 2-, 3- and 4-coil links in IMD applications, where coil dimensions and coupling distances are smaller than the inductively powered neural recording system in our design example, we followed the procedure in section III on a set of inductive links to optimize them for a retinal implant [16], [39]. For this application, we chose  $D_{o3}$ ,  $d_{12}$ ,  $d_{23}$ ,  $d_{34}$ ,  $R_L$ ,  $R_s$ ,  $P_L$  equal to 10 mm, 0.1 mm, 10 mm, 0.1 mm, 100  $\Omega$ , 0.5  $\Omega$ , and 250 mW, respectively. We also assumed that all coils are PSC type with a microfabrication process that sets  $w_{min}$  and  $s_{min}$  at 50 µm. Table II summarizes the resulting optimal geometries for  $R_s = 0.5 \Omega$ , and Fig. 12a shows the calculated PTE and PDL for these inductive links vs. coupling distance,  $d_{23}$ . At the nominal coupling distance of  $d_{23} = 10$  mm, it can be seen from Table II that the PTE of the 4-coil link is only 4.9% higher than the 3-coil link. The PDL of the 3-coil link, however, is 11 times higher than the 4-coil link at the same distance. The 2-coil inductive link is also close to optimal in this condition, which is in agreement with the conclusion at the end of section II.C. At  $d_{23} = 20$  mm, the difference between 4- and 3- coil PTEs increases to 7.7%, while the ratio between their PDLs reaches 192!

In Fig. 12b we have compared the calculated PTE and PDL of optimized 2-, 3- and 4-coil links vs.  $R_s$ . These curves are quite instructive by showing the designer which inductive link can provide the optimal  $\eta_{ov}$ . For instance, a low power driver with  $R_s = 5 \Omega$  for a low  $P_L$  application favors a 4-coil inductive link to maintain high PTE despite its low PDL [17], [18]. The same 4-coil link at  $d_{23} = 20$  mm will require  $V_s = 30$  V with 100 V across a class-E PA transistor to deliver 250 mW to the load. On the other hand, a 3-coil inductive link, driven by a stronger class-E PA with  $R_s = 0.5 \Omega$ , will require  $V_s = 1.8$  V and imposes only 6 V across the PA transistor in the same conditions. It should be noted that with class-C or class-D PAs, a low-loss matching circuit can transform  $R_{ref} + (R_1 \text{ or } R_2)$  to the optimal load required by the PA to achieve its highest efficiency. Therefore, 3-coil inductive links can be the optimal choice for a wide range of  $R_s$  values [41].

#### VI. Conclusion

We have presented a design procedure to maximize the PTE in 2-, 3-, and 4-coil inductive links via a comprehensive analysis based on the reflected load theory. We have extended conventional 2-coil inductive link equations to a multi-coil arrangement to provide a platform for the analysis and design of the state-of-the-art power transmission inductive links. We have shown that the 3-coil inductive links can significantly improve the PTE and PDL, particularly at large coupling distances by transforming any arbitrary load impedance to the optimal impedance needed at the input of the inductive link. The coupling between  $L_3$ and  $L_4$  on the Rx side ( $k_{34}$ ), provides designers with a new degree of freedom for impedance transformation, which was not feasible in 2-coil links. We showed that the recently proposed 4-coil inductive links transform the load impedance to a very high reflected resistance across the driver coil, which limit the available power from source and drastically reduce PDL, particularly at large coupling distances. Furthermore, a set of 2-, 3-, and 4-coil links was optimized in a design example, modeled in HFSS, and fabricated using magnet wires and PCB. Measured results at 12 cm coupling distance showed PTE of 15%, 37%, and 35% for 2-, 3-, and 4-coil links, respectively. The 3-coil link, however, achieved a PDL of 1.5 and 59 times larger than its 2- and 4-coil counterparts, respectively.

# Acknowledgments

This work was supported in part by the National Institutes of Health, NIBIB, grant 1R21EB009437-01A1, and the National Science Foundation under award ECCS-824199.

# Appendix

WWCs are often modeled as distributed RLC networks including a self-inductance in series with a resistance, both of which are in parallel with the coil parasitic capacitance [19]. The relationship between these parameters ( $L_{self}$ ,  $R_{wwc}$  and  $C_P$ ) and the WWC geometries have been collected from various references and included in this Appendix.

Analytical expression for the self-inductance of a one turn circular conductive loop can be found from [42]

$$L_i = 0.5\mu_0\mu_r D_o \ln\left(\frac{D_o}{w}\right),\tag{30}$$

where  $\mu_0$  and  $\mu_r$  are the permeability of space and conductor, respectively.  $D_o$  is the diameter of the loop and w is the diameter of wire. For mutual inductance, M, a wire-wound coil can be considered a set of concentric single-turn loops with various diameters, all connected in series. Using Maxwell equations,  $M_{ij}$  between a pair of parallel single-turn circular coils at radii  $r_i = w_i/2$  and  $r_j = w_i/2$  can be found from [20]

$$M_{ij} = \frac{2\mu}{\alpha} \sqrt{r_i \cdot r_j} \left[ \left( 1 - \frac{\alpha^2}{2} \right) K\left( \alpha \right) - E\left( \alpha \right) \right], \tag{31}$$

where

$$\alpha = 2\sqrt{\frac{r_i \cdot r_j}{\left(r_i + r_j\right)^2 + d_{ij}^2}}.$$
(32)

In this equation,  $d_{ij}$  is the coupling distance between the two coils and  $i \neq j$ .  $K(\alpha)$  and  $E(\alpha)$  are the complete elliptic integrals of the first and second kind, respectively [20]. Hence, the self-inductance of a WWC can be found from

$$L_{self} = \sum_{i,j} M_{i,j} + \sum_{i} L_i.$$
(33)

To model the series parasitic resistance of the WWC, its DC resistance should be calculated from

$$R_{DC} = \frac{\rho_c}{\pi D_o^2} \cdot n. \left(2 \cdot \pi \cdot w^2\right),\tag{34}$$

where  $\rho_c$  is the resistivity of the conductive material and *n* is total number of turns. As the operating frequency increases, the skin effect increases the series resistance, which can be modeled as [43]

$$R_{wwc} \cong R_{DC} \cdot \frac{\rho_c}{\delta \cdot \pi \cdot (D_o - \delta)},\tag{35}$$

where

$$\delta = \sqrt{\frac{\rho_c}{\pi \cdot \mu \cdot f}}.$$
(36)

The parasitic capacitance between two turns of a WWC can be found from [19]

$$C_{turn} = \varepsilon_0 \varepsilon_r \int_0^{\theta_c/2} \frac{\pi \cdot D_o \cdot w/2}{\zeta + (w/2) \varepsilon_r (1 - \cos\theta) + 0.5\varepsilon_r \cdot s} d\theta$$
(37)

where  $\varsigma$  is the thickness of the insulation layer and  $\theta_e$  is the effective angle between turn *i* and turn *j* which is 90 degrees and *s* is the spacing between turns. Hence, the sum of the turn-to-turn parasitic capacitance can be approximately given by  $C_P = 2nC_{turn}$ .

Finally, considering  $R_{wwc}$  in series with  $L_{self}$  and  $C_P$  in parallel with both, the quality factor of a WWC at operating frequency,  $\omega_0$ , can be found from [20]

$$Q = \frac{\omega_0 L_{self} - \omega_0 \left( R_{wwc}^2 + \omega_0^2 L_{self}^2 \right) C_P}{R_{wwc}} \approx \frac{\omega_0 L_{self}}{R_{wwc}},$$
(38)

which is valid for low frequency and small  $C_P$ .

In certain applications the maximum weight of the WWC,  $W_{max}$ , should also be considered in the design process.  $w_{max}$ , the maximum wire diameter of an *n*-turn WWC is related to its weight according to

$$w_{\max} = \left(\frac{4W_{\max}}{\pi^2 \rho. n. D_o}\right)^{1/2},$$
 (39)

where  $\rho$  is the density of the conducting material, which is 8.96 g/cm<sup>3</sup> for copper. In (39) we have ignored the weight of the insulating material.

# Biography



**Mehdi Kiani** (S'09) received his B.S. degree at Shiraz University, Shiraz, Iran and his M.S. degree at Sharif University of Technology, Tehran, Iran in 2005 and 2008 respectively. He

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**Uei-Ming Jow** received the B.E. degree in electrical engineering from Tatung University, Taiwan, and the M.S. degree in electronics engineering from National Taiwan University of Science and Technology, Taiwan, in 1991 and 2001 respectively. From 2001 to 2006, he joined Industrial Technology Research Institute (ITRI) at Hsinchu, Taiwan, and worked in Electronics Research and Service Organization as an RF engineer. He was involved at the analysis and design of electromagnetic compatibility for high speed digital circuit as well as embedded RF circuits packaging technology. He is now working towards his PhD degree at the Georgia Institute of Technology. His main research interests are neural and bionic implants, integrated analog circuit design, and wireless implantable biomedical systems.



**Maysam Ghovanloo** (S'00–M'04–SM'10) was born in 1973 in Tehran, Iran. He received the B.S. degree in electrical engineering from the University of Tehran, Tehran, Iran, in 1994, the M.S. degree in biomedical engineering from the Amirkabir University of Technology, Tehran, Iran, in 1997, and the M.S. and Ph.D. degrees in electrical engineering from the University of Michigan, Ann Arbor, in 2003 and 2004, respectively.

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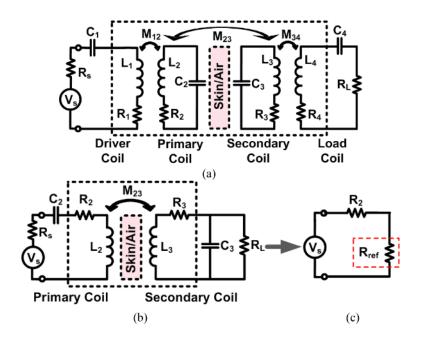
Dr. Ghovanloo is an Associate Editor of the IEEE TRANSACTIONS ON CIRCUITS AND SYSTEMS, PART-II, IEEE TRANSACTIONS ON BIOMEDICAL CIRCUITS AND SYSTEMS, and a member of the Imagers, MEMS, Medical, and Displays (IMMD) subcommittee at the International Solid-State Circuits Conference (ISSCC). He is the 2010 recipient of a CAREER award from the National Science Foundation. He has also received awards in the 40th and 41st Design Automation Conference (DAC)/ISSCC Student Design Contest in 2003 and 2004, respectively. He has organized several special sessions and was a member of Technical Review Committees for major conferences in the areas of circuits, systems, sensors, and biomedical engineering. He is a member of the Tau Beta Pi, AAAS, Sigma Xi, and the IEEE Solid-State Circuits Society, IEEE Circuits and Systems Society, and IEEE Engineering in Medicine and Biology Society.

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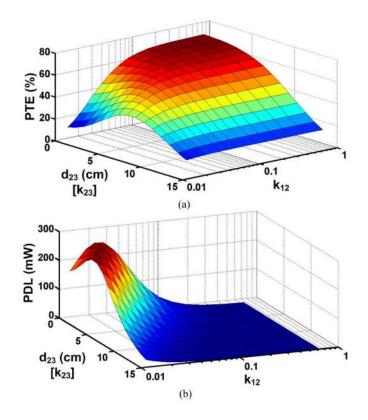
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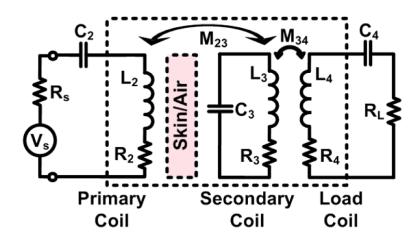
#### Fig. 1.

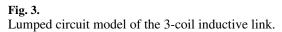
Lumped circuit models of (a) 4-coil and (b) conventional 2-coil inductive links for wireless power transfer. (c) Equivalent circuit of the reflected load on to the primary loop at resonance (for the sake of simplicity,  $R_s$ , which is a property of the driving circuitry, has been merged with  $R_2$ ).





Simulated (a) power transfer efficiency (PTE) and (b) power delivered to the load (PDL) for a 4-coil inductive link as a function of  $k_{12}$  and  $d_{23}$  when  $k_{34} = 0.22$  for the coils specified in Table I.  $V_s = 1$  V and  $R_L = 100 \Omega$ .





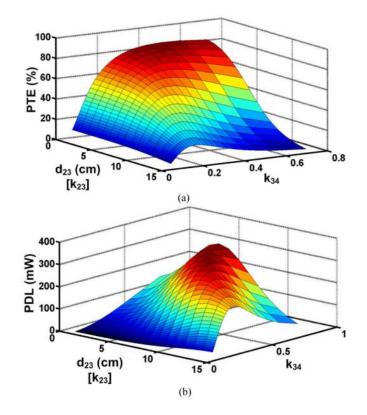
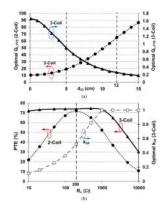


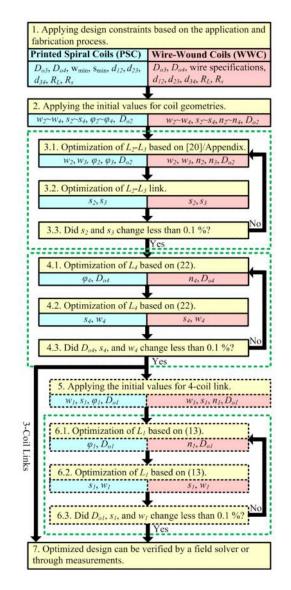


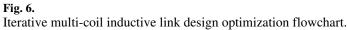
Fig. 4. Simulated (a) PTE and (b) PDL for a 3-coil inductive link as a function of  $k_{34}$  and  $d_{23}$  for the coils in Table I.  $V_s = 1$  V and  $R_L = 100 \Omega$ .

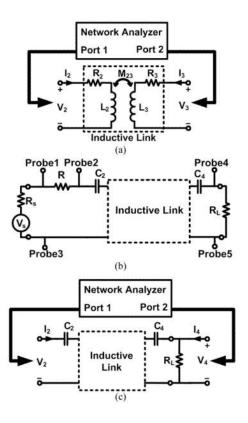


#### Fig. 5.

(a) Optimal load quality factor,  $Q_{L,PTE}$ , needed to achieve the highest PTE vs. coils' spacing in 2- and 3-coil inductive links ( $k_{34} = 0.22$ ,  $R_L = 100 \Omega$ , and other parameters from Table I). (b)  $k_{34}$  adjustments based on (25) to maintain the optimal PTE in a 3-coil link vs.  $R_L$  at  $d_{23} =$ 5 cm. The 2-coil link only reaches the optimal PTE for a specific  $R_L = 200 \Omega$  that satisfies (10).

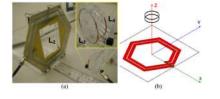






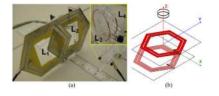
# Fig. 7.

PTE measurement setups for inductive links: (a) Conventional method using a network analyzer, (b) direct method using a signal source and current and voltage probe via oscilloscope, (c) the new method using network analyzer with all the coils tuned at the carrier frequency and  $R_L$  connected.



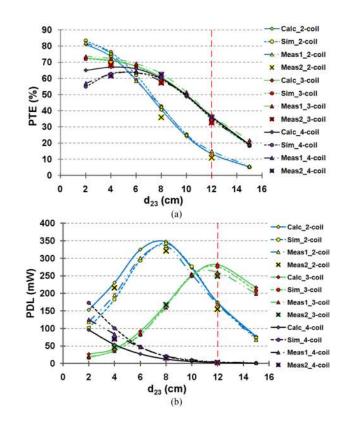
#### Fig. 8.

(a) Experimental setup for measuring the PTE and PDL in a 3-coil inductive link. (b) 3-coil inductive link model in the HFSS. Coil specifications are listed in Table I.



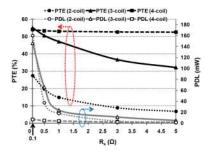
# Fig. 9.

(a) Experimental setup for measuring the PTE and PDL in a 4-coil inductive link. (b) 4-coil inductive link model in the HFSS. Coil specifications are listed in Table I.



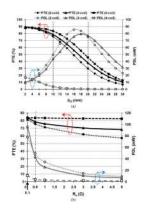
#### Fig. 10.

Comparison between measured, simulated (HFSS), and calculated (see section II) values of the (a) PTE and (b) PDL vs.  $d_{23}$  for 2-, 3-, and 4-coil inductive links specified in the "Measurement" columns of Table I ( $V_s = 1$  V).



# Fig. 11.

Calculated PTE and PDL vs. source resistance,  $R_s$ , for 2-, 3-, and 4-coil inductive links in the design example of Table I ( $V_s = 1$  V,  $d_{23} = 12$  cm).



#### Fig. 12.

(a) Comparison between calculated values of the PTE and PDL vs.  $d_{23}$  for 2-, 3-, and 4-coil inductive links specified in Table II ( $V_s = 1 \text{ V}$ ,  $R_s = 0.5 \Omega$ ). (b) Comparison between calculated values of the PTE and PDL vs.  $R_s$  for 2-, 3-, and 4-coil inductive links for the IMD example of Table II ( $V_s = 1 \text{ V}$ ,  $d_{23} = 1 \text{ cm}$ ).

Table I

Kiani et al.

Optimized Geometries for Design Examples

,		)	•			
	Domotoria	Crumbolo	2-0	2-Coil	3-Coil	3-Coil / 4-Coil
	r ar anteuers	siounic	Meas	Optim	Meas	Optim
	Inductance (μH)	$L_{j}$	-	-	- / 0.9	- / 0.18
	Outer diameter (cm)	$D_{0I}$	I	I	- / 16.8	- / 10.5
	Fill factor	Ι φ		-	- / 0.13	- / 0.14
$L_{I}$	Num. of turns	lu			- / 2	- / 1
	Line width (mm)	$W_I$			- / 8.66	- / 12
	Line spacing (mm)	$S_I$	T	I	- / 2.6	- / 35
	Quality factor	$\mathcal{Q}_{l}$	T	I	- / 255	-/131
	Inductance (µH)	$L_2$	0.9	1.2	6.0	1.2
	Outer diameter (cm)	$D_{02}$	16.8	27	16.8	27
	Fill factor	φ 2	0.13	0.28	0.13	0.28
$L_2$	Num. of turns	<sup>2</sup> u	2	2	2	2
	Line width (mm)	$W_2$	8.66	12	8.66	12
	Line spacing (mm)	$S_2$	2.6	35	2.6	35
	Quality factor	$\mathcal{Q}_2$	255	196	255	196
	Inductance (μH)	$L_{3}$	0.12	0.058	0.4	0.47
	Coil diameter (cm)	$D_{03}$			4	
1.5	Wire diameter (mm)	$W_{\mathcal{B}}$	0.64	5.68	0.64	2.2
ŗ,	Num. of turns	$n_3$	1	1	2	3
	Line spacing (µm)	$S_3$	100	100	100	100
	Quality factor	$\mathcal{Q}_3$	105.2	151.5	111	417
	Inductance (μH)	$L_4$	I	I	0.4	0.22
	Coil diameter (cm)	$D_{04}$	I.	I	4	2.8
L4	Wire diameter (mm)	$W_4$	-	I	0.64	1
	Num. of turns	$n_4$	I	I	2	2

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	Denomotone	Sumbole	2-0	2-Coil	3-Coil / 4-Coil	4-Coil
	r ar anneuer s	sioumic	Meas	Optim	Meas	Optim
	Line spacing (µm)	$S_4$	-	-	100	100
	Quality factor	$\mathcal{Q}_4$	-	-	177	142
$L_I - L_2$	$L_1$ - $L_2$ coupling distance (mm)	$d_{12}$		-	/-	- / 1.5
$L_2 - L_2$	$L_2$ - $L_3$ coupling distance (mm)	$d_{23}$			120	
$L_3 - L_4$	$L_3$ - $L_4$ coupling distance (mm)	$d_{34}$		-	6	
Powe	Power transfer efficiency (%)	h	15	27.4	37/35	55/54
Powei	Power delivered to load (mW)	DDT	170	160	260/4.4	146/6.8
	Nominal load $(\Omega)$	$R_L$			100	
Driv	Driver output resistance ( $\Omega$ )	$R_S$			0.1	
Power	Power carrier frequency (MHz)	$f_o$		1:	13.56	
LI and i	LI and $L2$ are hexagonal overlapping PSCs, while $L3$ and $L4$ are WWCs.	ng PSCs, wh	ile L3 and	l L4 are W	WCs.	

Grayed cells indicate the design constraints.

Table II

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Optimized PSC Geometries for IMD Applications

-					
	Parameters	Symbols	2-Coil	3-Coil	4-Coil
	Inductance (µH)	$L_{I}$	ı	I	0.12
	Outer diameter (mm)	$D_{0l}$	ı	I	25.2
	Fill factor	φ 1	-	ı	0.24
$L_{l}$	Num. of turns	$^{I}u$	ı	ı	2
	Line width (mm)	$W_{I}$	ı	I	2.4
	Line spacing (µm)	$S_I$	-	I	150
	Quality factor	$\mathcal{Q}_{I}$	I	I	87.4
	Inductance (µH)	$L_2$	1.57	1.22	0.6
	Outer diameter (mm)	$D_{02}$	37	43	36.5
	fill factor	φ 2	0.52	0.57	0.52
$L_2$	Num. of turns	$n_2$	8	8	5
	Line width (mm)	$w_2$	1.45	1.8	2.4
	Line spacing (µm)	$S_2$	150	150	150
	Quality factor	$\mathcal{Q}_2$	165	182	195
	Inductance (µH)	$L_{3}$	0.1	0.276	0.54
	Outer diameter (mm)	$D_{03}$		10	
	Fill factor	<i>p</i> 3	0.26	0.11	0.15
$L_3$	Num. of turns	$n_3$	3	4	6
	Line width (mm)	$W_{\mathcal{B}}$	0.65	0.27	0.18
	Line spacing (µm)	$S_3$	50	50	50
	Quality factor	$\mathcal{Q}_3$	127	159	152
	Inductance (µH)	$L_4$		0.11	0.16
	Outer diameter (mm)	$D_{04}$	-	9.1	8.8
<b>L</b> 4	Fill factor	φ 4		0.19	0.25
	Num. of turns	$n_4$	-	3	4

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	Parameters	Symbols	2-Coil	3-Coil	4-Coil
	Line width (mm)	₽M		0.46	0.4
	Line spacing (µm)	54		50	50
	Quality factor	$Q_4$		129	154
L <sub>1</sub> and	$L_1$ and $L_2$ coupling distance (nun)	$d_{12}$	ı		0.1
<sup>2</sup> and	$L_2$ and $L_3$ coupling distance (mm)	$d_{23}$		10	
L <sub>3</sub> and	$L_3$ and $L_4$ coupling distance (mm)	$d_{34}$	ı	0.1	1
Powe	Power transfer efficiency (%)	h	75.7	78.6	83.5
Powe	Power delivered to load (mW)	TAd	49.5	43.4	3.9
	Nominal load $(\Omega)$	$R_L$		100	

All coils are considered PSC type.

Power carrier frequency (MHz)

13.56

0.5

 $R_s$  $f_0$ 

Driver output resistance  $(\Omega)$ 

Grayed rows indicate the design constraints.