

# Design and Test of an Improved Active Disturbance Rejection Control System for Water Sampling Unmanned Surface Vehicle

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## ABSTRACT

Unmanned surface vehicles (USVs) have wide application prospects in military and civil fields. Motivated by the large demand for environmental protection equipment, a water-sampling USV (WS-USV) system is designed in this study. The software and hardware of the entire system are designed and developed independently. Two water sampling modes, a manual remote control mode and remote interface automatic control mode are designed for handling emergencies. The WS-USV is propelled by twin-propellers. These propellers have many input constraints owing to their inherent structure, making the design of the controller very difficult. In this study, an improved active disturbance rejection control (ADRC) method is proposed and a saturation function is introduced to design a path-following control system for the WS-USV. This enhances the anti-disturbance ability for addressing environmental disturbances by wind, waves and currents in the water sampling process. The stability of the system is improved. The feasibility, stability and performance superiority of the control system are proven by water sampling contrast experiments.

## 1. Introduction

Approximately 70% of the earth's surface is covered by water. With the rapid development of industrialisation, the pollution of rivers, lakes, and other water resources is becoming increasingly serious [1]. Despite being a source of life, fresh water is scarce in most countries, and extremely lacking in others. To this end, all countries have actively taken necessary measures to protect rivers and lakes, so that the overall quality of the ecological water environment is improved. The efficient acquisition of water samples is not only a prerequisite for the prevention and control of water pollution, but is also the premise for improving the water environment, restoring the functions of rivers and lakes, and ensuring the safety of the water. At present, environmental monitoring authorities mainly conduct manual sampling and online sampling. Manual sampling has the disadvantages of a long collection cycle, high work intensity, low efficiency and even great potential safety hazards to human health. Online sampling is limited to collecting water samples from fixed points, and cannot be widely used in large water areas, owing to high cost and without random dynamics [2].

Owing to developments in automatic control theory and related technologies, autonomous underwater vehicles (AUVs), unmanned surface vehicles (USVs), ground robots, and unmanned aerial vehicles (UAVs) are rapidly emerging [3]. The sea, land, and air vehicles gradually tend to be integrated and unmanned [4], which has aroused the enthusiasm of scholars and researchers. Among them, USVs have been widely used in military and civilian fields [5, 6]. Different functions can be achieved by installing different modules on

USVs. A water sampling USV (WS-USV) was developed by carrying a water sampling module on a USV. Research on the control system of the WS-USV has great significance for improving the ecological environment, reducing the sampling cost, and increasing the safety of sampling personnel.

Existing research on USVs can be divided into two categories: theoretical studies of control strategies, and control system designs for the USV. In terms of theoretical research, many control methods have been used in USVs, including proportional-integral-derivative (PID) control [7, 8, 9], sliding mode control (SMC) [10, 11, 12], fuzzy control [13, 14, 15], active disturbance rejection control (ADRC) [16] and dynamic surface control (DSC) [17]. However, the above methods have limited abilities to defend against environmental forces and model uncertainties. In ref.[18], an adaptive dynamic surface trajectory tracking control method was proposed based on a neural network (NN). The model uncertainties were estimated using a radial basis function NN (RBF-NN), and the input saturation of the rudder was compensated for by an auxiliary design system. Park et al.[19] proposed a NN-based output feedback control method, and the speed of the USV was estimated by an NN observer. A path-following control method of USVs based on backstepping technology and principle of line-of-sight (LOS) navigation was proposed by Peng et al.[20]. The USV suffered from complex disturbances and speed and output constraints, which were compensated for and adjusted by an extended state observer (ESO) and reference regulator, respectively. An adaptive NN-based trajectory fault-tolerant tracking control method for a USV was proposed in ref.[21]. The NN technology was used to address model uncertainties. The adaptive method and a backstepping technique were combined to handle input saturations, disturbances, and actua-

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tor faults. A novel data-driven backstepping path-following control strategy was proposed by Weng et al.[22], in which the backstepping technology and sliding mode surface were combined to simplify the design of the controller and enhance robustness. The ESO was used to compensate for complex unknowns. In ref.[23], a fixed-time conversion control method was proposed. The dynamic model of the USV was transformed into two cascading subsystems to address actuator dead zones. A finite-time nonlinear SMC method was proposed in ref.[24]. A terminal sliding mode controller and auxiliary sliding mode controller were used to control different state areas to avoid singular problems. An adaptive NN position tracking control method was proposed by Zhang et al.[25]. The backstepping technology, NN, DSC, and SMC methods were combined to design a robust controller, in which the estimation of model parameters was avoided, and the potential for practical application was improved. A reinforcement learning (RL) controller was proposed in ref.[26], an NN-based RL method was introduced to compensate for uncertainties and disturbances. The advanced control methods mentioned above all showed superior control effects, but applying them to actual control systems requires further study and simplification.

The design of a control system is relatively slow, and there are few scholars studying this area. The ones that do mainly focus on traditional control methods [27, 28, 29, 30, 31]. For example, a LOS-based PID control strategy was proposed for an under-actuated vehicle by Caharija et al.[27]. A P-speed controller with linear feedback and PD-heading controller with linear feedback were designed for the control of an under-actuated AUV, and sea tests were conducted to verify the effectiveness and stability of the proposed control strategy and designed controller. A NN-based output feedback control method was proposed for a twin-propeller USV with input saturation by Chen et al.[28]; they designed a trajectory tracking controller for the USV. The effectiveness of the controller was verified through simulations and experiments. In ref.[29], a fuzzy PID-based trajectory tracking control system was designed for a river crab feeding boat with twin paddle wheels, and the effectiveness and reliability of the control system were validated by feeding experiments. An LOS navigation-based target enclosing strategy for USVs was proposed by Jiang et al.[30], and its feasibility was verified through simulation experiments. A control system based on the ADRC method was also designed. The effectiveness of the control strategy and stability of the control system were verified by a target enclosing experiment with two triple-propeller single-rudder USVs. A novel translation and rotation cascade control method was proposed in ref.[31]. First, the superiority of this method was verified by comparative simulation experiments. Then, a path-following controller for a twin-propeller USV was designed using this method. The feasibility of the control strategy and effectiveness of the controller were verified through experiments. A UAV sampling remote control system for mine water samples was developed by Banerjee et al.[32]. It could sample in small, isolated, and dangerous water areas, and could avoid

the dangers in traditional sampling methods. In ref.[33], a water sampling UAV was developed by designing a water sampling device and equipping it on a UAV, which improved the sampling efficiency and safety. As can be seen from the above references, there is little research and design regarding the unmanned sampling equipment urgently needed for environmental monitoring, especially in regards to the design of WS-USV systems. Motivated by the urgent demand for environmental protection equipment, and drawing on experience from improving the anti-disturbance effects of controllers used in RL, NN or other learning (optimization) methods to approximate an unknown state in theoretical research[34], an improved ADRC strategy combining traditional ADRC with extreme learning machine (ELM) is proposed in this study. The strategy considers the practical problems of the propeller (with various input and output constraints) and system stability, and a set of control systems for the WS-USV is designed by introducing a saturation function and combining it with the improved ADRC method. The control system is applied to a WS-USV for independent design and development. The effectiveness, stability, and superiority of the control method and control system are verified by water sampling contrast experiments. The main contributions of this study are as follows:

(1). A set of WS-USV systems is independently designed. To facilitate emergency treatment, a manual remote control device and remote automatic control platform are designed for the WS-USV.

(2). An improved ADRC strategy is proposed, and a WS-USV path-following control system is designed based on this control strategy.

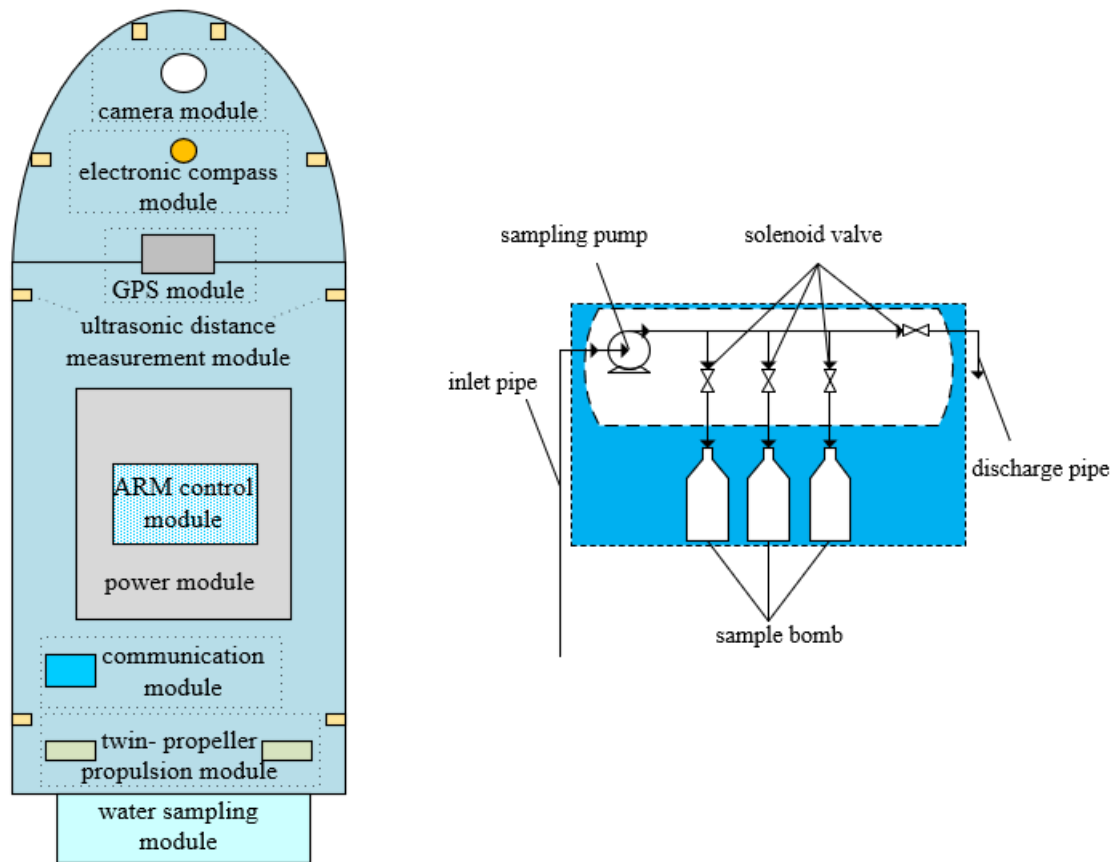
(3). Considering that the stability of the system will be greatly affected by the propeller working under extreme conditions for a long time, a saturation function is introduced in the design of the control system, to solve the multiple input constraints of the WS-USV system caused by the inherent structure of the propellers. Based on ensuring a good control effect, this function not only reduces wear, but also enhances the stability of the system.

The organisation of this paper is as follows. The hardware and software architecture is introduced in Section II. In Section III, the control strategy of the WS-USV is introduced, and the improved active disturbance rejection controller is designed. Section IV provides the water sampling experimental results. The conclusion is presented in Section V.

## **2. Framework of water-sampling unmanned surface vehicle (WS-USV) system**

### **2.1. Overall design of WS-USV system**

The overall structure of the WS-USV is shown in Fig.1. The WS-USV system consists of an onboard subsystem and onshore subsystem. The onboard subsystem includes a GPS module, electronic compass module, rotatable camera module, ultrasonic distance measurement module, wireless communication module, ARM control module, twin-propeller



**Figure 1:** Structure diagram of water-sampling unmanned surface vehicle (WS-USV).

propulsion module, power module, 4G network image transmission module and water sampling module. The water sampling module is shown in Fig.1b. The onshore subsystem consists of a wireless communication module, joystick remote control module, and remote control platform. The hull of the WS-USV is constructed with fibre-reinforced plastic, propelled by the twin-propeller at the stern of the WS-USV and steered by the rotation speed difference of the twin-propeller. A rotatable camera module is mounted on the bow, an ultrasonic distance measurement module is evenly distributed at port and starboard, the water sampling module is installed on the stern.

## 2.2. Hardware structure of the onboard subsystem

To meet the needs of various working environments and emergency situations, two control modes are designed for the WS-USV: a manual remote control sampling mode and automatic sampling mode. To reduce the risk of hardware failures caused by the switching of the two modes, the manual remote control part is developed in the remote automatic control platform. The hardware of the onboard system is centred on the ARM control module, which is the 'STM32F429IGT6' designed and produced by STMicroelectronics. The microcontroller core is the Cortex-M4 designed by ARM, and the peripherals, such as the general purpose input output (GPIO), universal synchronous/asynchronous receiver/trans-

mitter (USART), inter-integrated circuit (IIC) and serial peripheral interface are designed and produced by ST Microelectronics. Lithium battery power modules provide power for the entire onboard system. The RS232 serial interface and direct memory access (DMA) transmission mode are used, in which the ARM control module communicates with the GPS module, electronic compass module and wireless communication module. The IIC communication mode is adopted for when the ultrasonic distance measurement module communicates with the ARM control module. The ARM control module collects and centrally manages the data of the above modules, and combines it with the work task of the water sampling to produce corresponding two pulse width modulation (PWM) signals to drive the twin-propeller propulsion module to control the motion of the WS-USV. According to the sampling instructions, the water sampling module is controlled to collect water samples. The onboard wireless communication module is used for communication between the onboard and onshore subsystems. The rotatable camera module and 4G-network image transmission module are equipped for long-distance observation of the environment around the WS-USV and image target detection via image transmission. The data of the ultrasonic distance measurement module and image information are used to research collision avoidance. The hardware connections and communication modes of the WS-USV system are shown in Fig.2.

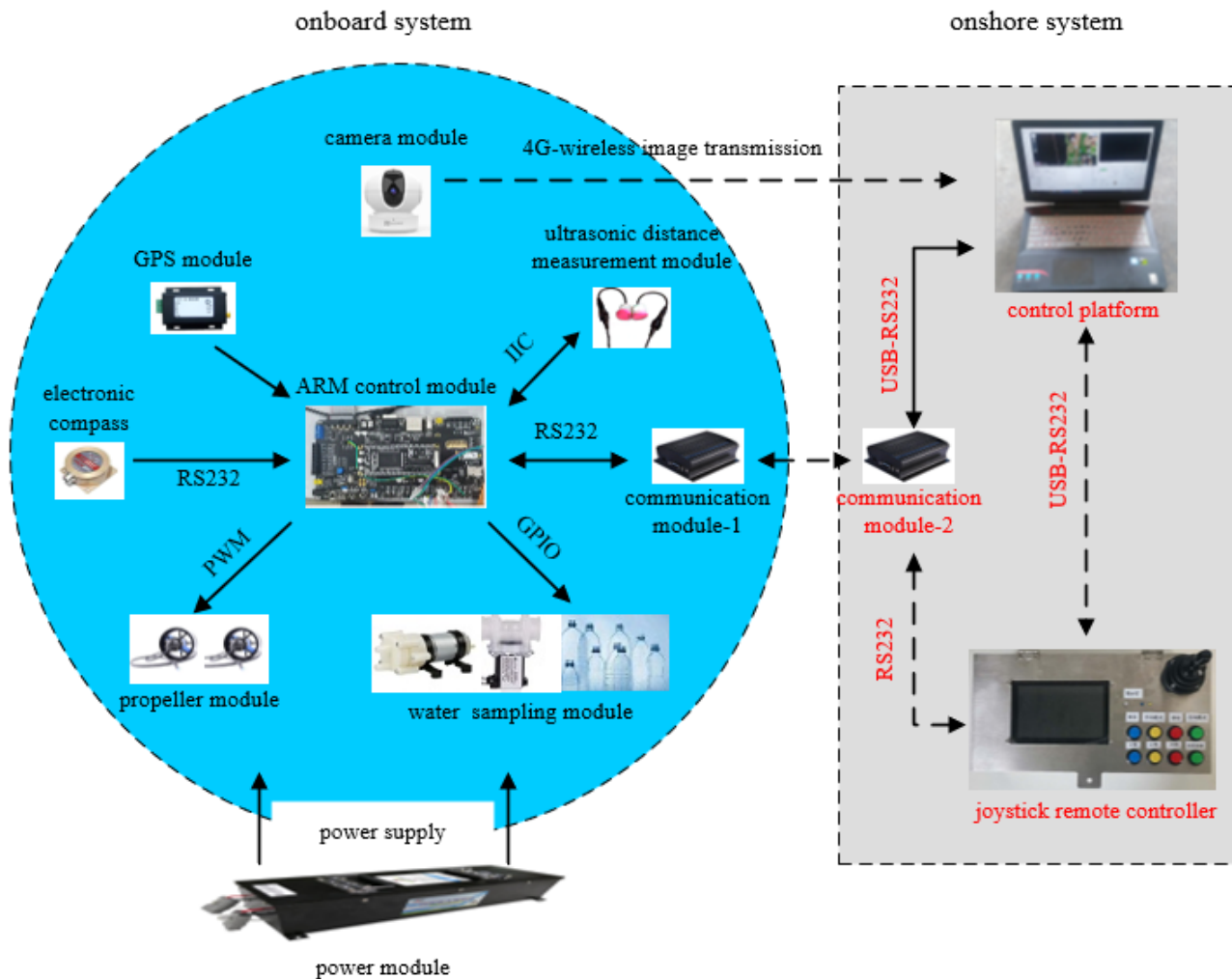


Figure 2: Hardware connections and communication modes of the WS-USV system.

## 2.3. Software development of the WS-USV system

### 2.3.1. Software design of the onboard subsystem

To ensure the portability of the system and openness of the interface, an embedded real-time uC/OS-III operating system is adopted in the onboard subsystem. The software design employs the concept that the data obtaining, processing, and sending of a module is designed as a subprogram. The software design of the onboard system is divided into two parts, the underlying bus and the configuration of peripherals (including the configuration of the drivers for the USART, IIC, DMA, GPIO, and PWM) [35]. The driver program is not only the link between the various hardware modules, but also acts as the bridge of the entire system. The driver program and corresponding control program perform data exchanges with each module, so that the onboard system can operate normally. The software structure of the onboard subsystem consists of a data acquisition module, processing module, output module, and communication module for interacting with the onshore subsystem. The acquisition module receives and incorporates GPS data, electronic compass data, ultrasonic probe data and communication module

data. The processing module decodes the GPS, electronic compass, ultrasonic probe, and communication module data, and provides joint processing thereof. The output module incorporates the outputs of the PWM, on-off instructions of the relays, and transmissions of the communication module data. The overall software workflow of the onboard system is shown in Fig.3.

### 2.3.2. Software development of joystick remote controller

The program of the joystick remote controller also follows the concept that the data obtaining, processing, and sending of a module is designed as a subprogram. The overall control program is divided into main programs and some subprograms; the subprograms are comprised of the driver programs of each module. Each verified subprogram can be embedded in the main program.

After the joystick remote controller is initialised, the data of the joystick is received through the RS232 and DMA. To avoid jitter in the WS-USV data from shaking, the data is received multiple times, the shaking data is removed by the

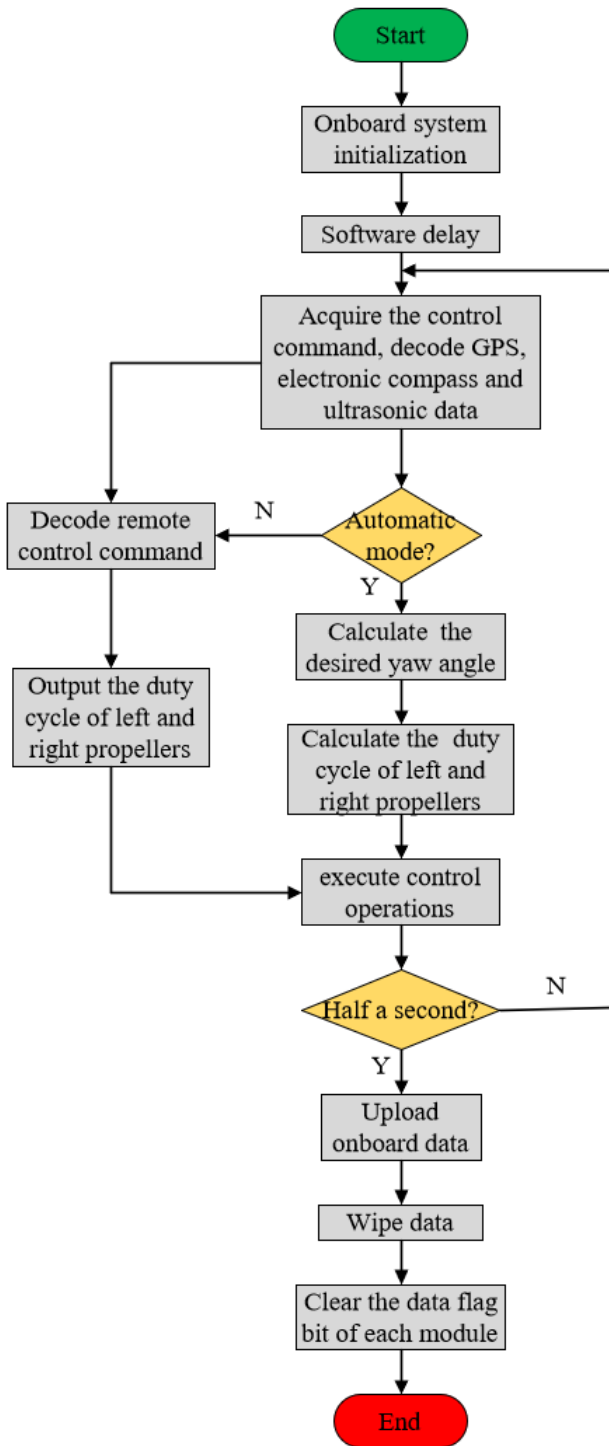


Figure 3: Workflow chart of the onboard subsystem.

median value filtering method. The filtered data is converted into corresponding control instructions. Then, by detecting whether a flag is set, it is determined whether effective data has been returned (received) from the WS-USV. If the flag is set, the data will be decoded according to the return protocol, and important data will be displayed on an LCD screen. Finally, there is confirmation of whether the status of each

key has changed, and according to the key state changes, the corresponding control instructions are sent to the WS-USV to perform the corresponding operations. The overall workflow of the joystick remote controller is shown in Fig.4.

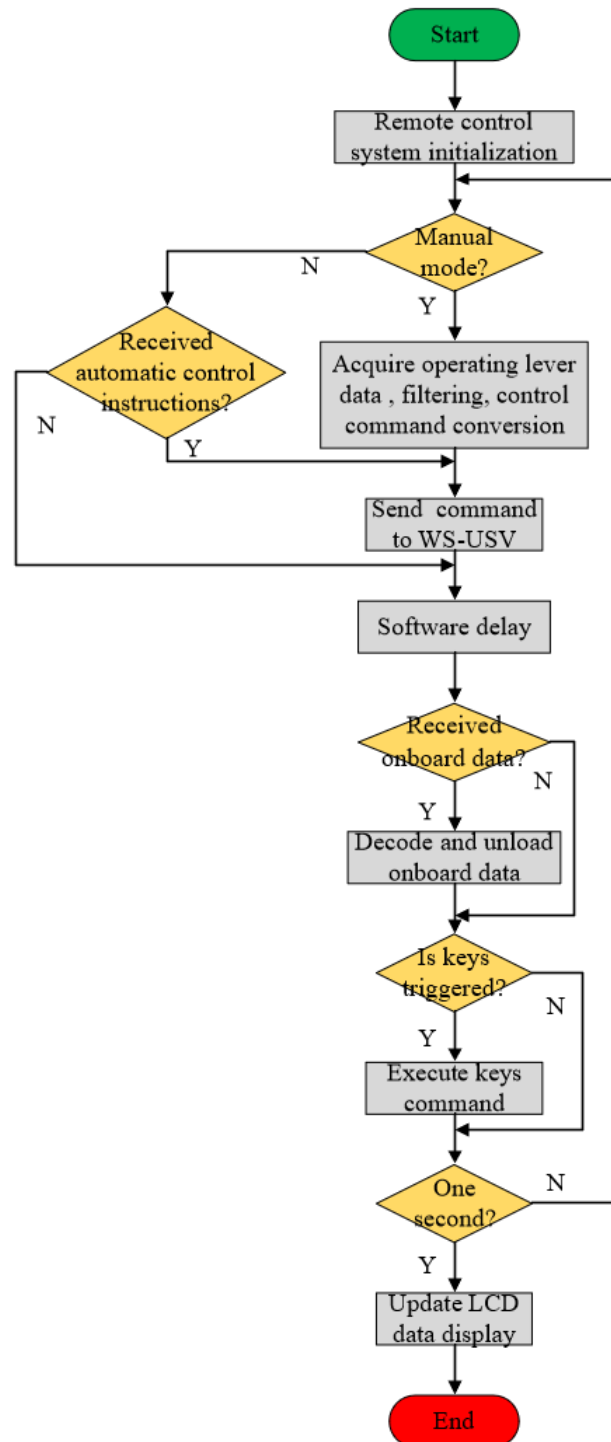


Figure 4: Workflow chart of the remote control subsystem



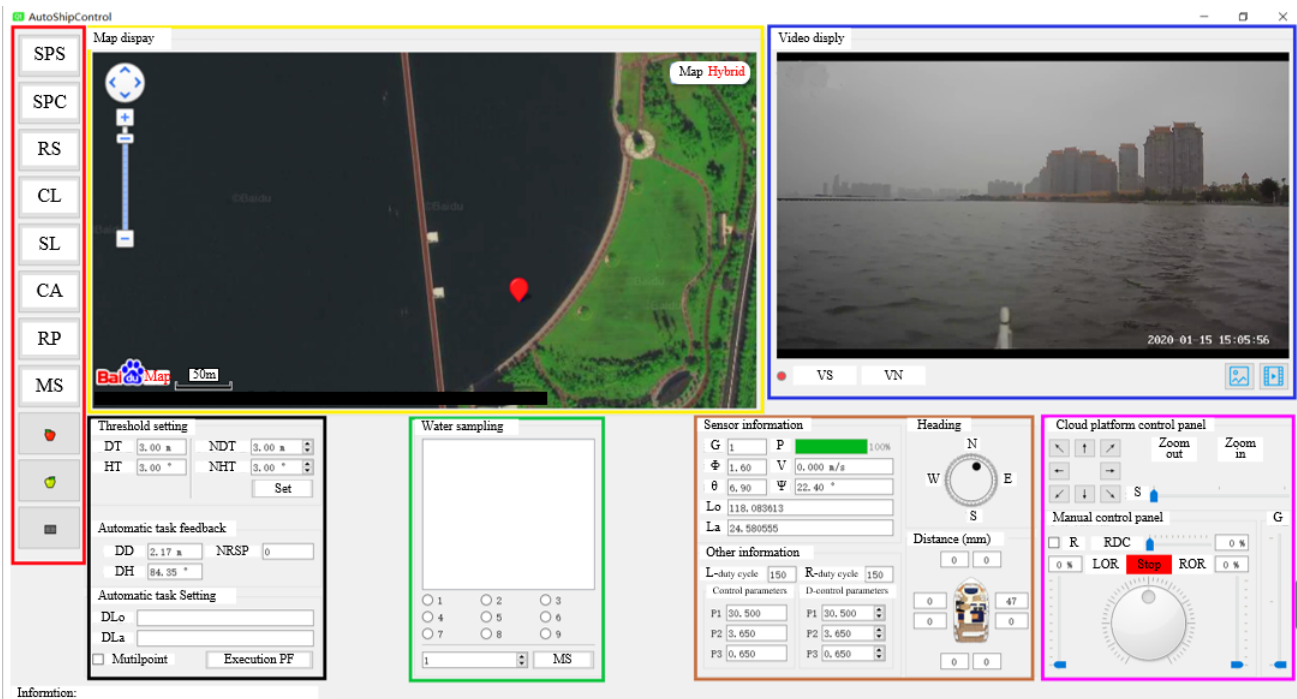


Figure 5: Human-machine interaction (HMI) of the remote control platform.

### 2.3.3. Design and development of the remote control platform

The control interface application of the remote automatic control platform is developed by QT application [36]. The human-machine interaction (HMI) of the WS-USV system is shown in Fig.5. It is divided into seven parts: auxiliary function selection zone, map display zone, automatic control operation zone, water sampling zone, video display zone, sensor parameter zone, and manual control zone.

**Auxiliary function selection zone (red zone):** This zone includes buttons for serial port setting, serial port connecting, reset sensor, clear log, storage log, chart analysis, refresh path, and mode switching. This zone is the auxiliary control function zone of the HMIs for the WS-USV. The communication between the control software and WS-USV is connected by the serial port setting button and connecting serial port button. The operation log of the WS-USV is managed using the clearing log and storage log buttons. The running real-time status information curve of the WS-USV is displayed through the chart analysis button. The sampling path of the WS-USV is updated through the refresh path button. The control mode of the WS-USV is switched by the mode switching button (i.e. to automatic control mode or manual control mode).

**Map display zone (yellow zone):** The application programming interface [37] of the Baidu Map is called to display the location and actual path of the WS-USV in real time. A point on the map can also be selected and marked as a water sampling point, which is then displayed on the map.

**Automatic control operation zone (black zone):** This zone includes three functions: threshold setting, automatic task

feedback, and automatic task setting. The threshold setting function includes setting the distance and yaw angle thresholds. The automatic task feedback function includes displaying the desired distance, desired heading, and number of remaining sampling points. The automatic task setting function includes setting the longitude and latitude of the desired sampling points, and selecting single-point sampling or multi-point sampling.

**Water sampling zone (green zone):** This zone includes two functions: automatic water sampling and manual water sampling. The automatic water sampling function is based on the desired sampling points for automatic sampling; the sampling number and completed information are shown in the panel. The manual sampling function is an alternative function, e.g., when automatic sampling is not working, the operator can manually select the number of sampling points to complete the water sampling.

**Video display zone (blue zone):** This zone includes four functions: video acquisition parameter configuration, video connection, capture current video image, and video recording. The serial number, transmission address, channel number, key, screenshot, and/or video saving path of the camera module should be configured for video acquisition. The video connection function mainly concerns the connected video acquisition module, so that the video image is displayed on the control platform. The video images can be captured by the current video image function, and are saved to the specified path by number. The video returned by the camera module can be recorded in MP4 format the video recording video function, and is saved to the same path.

**Parameter display zone (brown zone):** This zone pro-

vides a dynamic display of the WS-USV status information, including the motion status information of the WS-USV, propulsion information, and distance information between the WS-USV and obstacles. The motion status information of the WS-USV includes the position, roll, pitch, yaw, speed, and battery level. The propulsion information includes the duty cycle values of the left and right propellers, control parameters of the controller, and adjustable desired control parameters.

Manual control zone (purple zone): This zone can be divided into two parts: cloud platform control and manual control. The rotation speed, recording angle, and recording range of the camera can be adjusted by the cloud platform control. The manual control of the WS-USV includes gear adjustment, propulsion direction setting, and course adjustment.

**Remark 1.** The overall operation process (single cycle) of the onboard subsystem programs and the remote control subsystem programs are illustrated in Fig.3 and Fig.4 respectively. The half-duplex communication mode is employed for the wireless data transmission station between the onboard and onshore subsystem. The workflow of manual remote control mode for the WS-USV system is described as follows: each subsystem is initialized firstly; the manual remote control mode is set by the operator later. After receiving the information from the joystick, the remote control subsystem transmits data to the onboard subsystem through communication module. After the onboard subsystem receives the data, the follow-up process is completed according to the respective process of two subsystems. Then the important onboard data is sent back to the onboard subsystem through communication module. After remote control subsystem receives relevant data and key commands, part of the important information received is displayed in the remote control subsystem. The single process is finished and the circulation cycles until the whole task is completed.

### 3. Autonomous motion control strategy for the WS-USV

During automatic water sampling, the operator first sends the desired sampling point information to the WS-USV using the remote control platform. After receiving the water sampling instruction, the desired yaw angle and desired distance between the actual position of the WS-USV and current target sampling point are calculated; for this calculation, the motion status information is collected by the onboard sensors. Then, the controller adjusts the heading of the WS-USV according to the desired yaw angle and current yaw angle, and sails to the desired sampling point at a certain speed. It begins sampling when the WS-USV reaches the target sampling area. After sampling, the WS-USV sails to the next sampling point in the same way. Based on this sampling strategy, the motion control principle diagram for the WS-USV, as designed in this study, is shown in Fig.6.

In Fig.6,  $\psi$  represents the current yaw angle of the WS-USV as collected by the electronic compass;  $\psi_d$  denotes the

azimuth of the current position of the WS-USV and the desired position  $\psi, \psi_d \in [0^\circ, 360^\circ]$ , which are positive in the clockwise direction, when the heading point to north is  $0^\circ$ .  $d$  is the distance between the current position of the WS-USV and desired position,  $u_d$  is the set desired speed, and  $P_1$  represents the reference duty ratio at the desired speed, and  $P_2$  represents the output duty cycle of the controller.  $P_c = [P_{c1}, P_{c2}]^T$  is the converted output value, and  $P_1 = [P_{1l}, P_{1r}]^T$  is the vector consisting of the duty cycles corresponding to the desired speeds of the left and right propellers.  $P = [P_{11}, P_{22}]^T$  denotes the vector comprising the control output after conversion and applying actual engineering restrictions.

The controller in the control schematic is designed for an improved ADRC strategy, in which the duty cycle for adjusting the heading of the WS-USV is calculated from the desired yaw angle and current yaw angle of the WS-USV (as acquired by the electronic compass module). Then, as combined with the reference duty cycle of the desired speed of the WS-USV, the rotation speeds of the left and right propellers are adjusted to control the motion of the WS-USV towards the desired course. The distance between the current position of the WS-USV and current desired sampling position is used to determine whether the WS-USV has reached the desired sampling point. Until the WS-USV reaches the desired sampling area, water sampling is performed automatically. To improve the sampling efficiency, motion in a straight line between sampling points is expected. A motion control strategy for the straight line is proposed based on the principle diagram for the WS-USV, and is divided into heading guidance and heading tracking control.

#### 3.1. Heading guidance

In the process of moving the WS-USV from the current position to desired sampling position, the azimuth angle from the current position to target sampling point is taken as the desired yaw angle. The current yaw angle is acquired by the electronic compass. The yaw angle of the WS-USV is adjusted by the controller to change the rotation speed of the twin-propeller. Therefore, it can sail to the desired sampling point according to the expected heading. However, the WS-USV is disturbed by winds, waves, and currents. The guidance from the limited target points will cause the WS-USV to deviate from the desired path when tracking the desired course. To reduce control deviations, virtual target points [29] are introduced in the actual control process. Multiple virtual positions are calculated on the desired path between the current position of the WS-USV and target sampling position. The WS-USV follows the multiple virtual positions, instead of directly tracking a single target sampling point. Therefore, the motion of the WS-USV can be corrected at a regular distance. Compared with directly tracking a target sampling point, this can indirectly reduce the distance for tracking the next target position, and any deviations between the actual path and desired path caused by disturbances. Thus, the performance of the followed path is improved by this method. A schematic of the virtual target

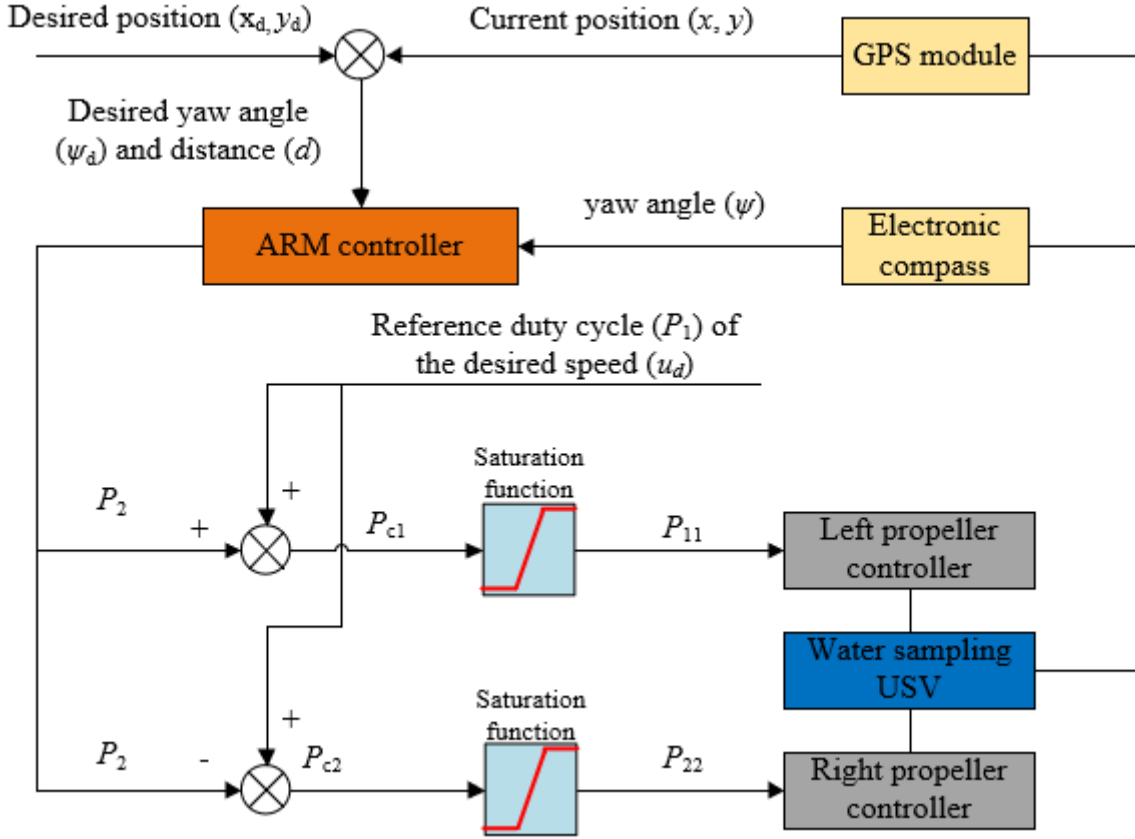


Figure 6: Control schematic of the WS-USV.

point calculation is shown in Fig.7.

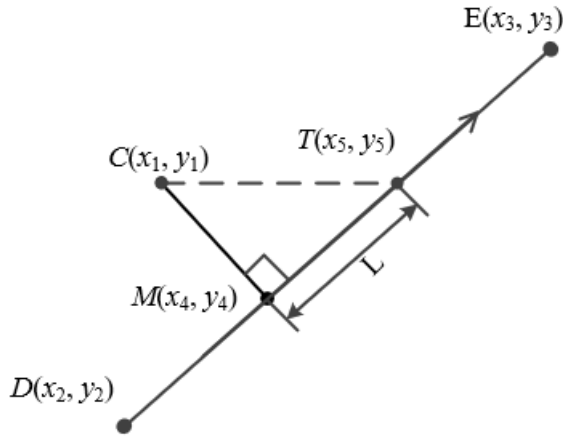


Figure 7: Schematic of the virtual position calculation [29].

In Fig.7,  $C$  represents the position of the WS-USV,  $D$  is the initial position,  $E$  is the desired position,  $T$  is the virtual position in the desired  $DE$  path,  $M$  is the projection point of the WS-USV position on the desired  $DE$  path,  $(x_i, y_i)$  is the longitude and latitude of each position ( $i = 1, 2, 3, 4, 5$ ); and  $L$  is the distance between the projection point of the WS-USV position and virtual target position on the desired  $DE$

path.

If the direction of line  $CE$  is taken as the guidance direction for the WS-USV, the WS-USV will have a larger deviation from the desired path of the line  $DE$ . However, if point  $T$  is taken as the first virtual target point, the direction of line  $CT$  is taken as the guiding direction until the WS-USV reaches the area of point  $T$ , and then continues to track the next virtual target point. Until the WS-USV reaches the area of the desired sampling point  $E$ , there is a superior path-following performance using this method. The longitude and latitude coordinates of point  $T$  are calculated as follows:

1. Calculate the longitude and latitude coordinates of the projection point  $M$  as follows:

$$\begin{cases} x_4 = \frac{(x_3-x_2)^2 x_1 + (y_3-y_2)^2 x_2 + (x_1-x_2)(x_3-x_2)(y_3-y_2)}{(x_2-x_3)^2 + (y_2-y_3)^2} \\ y_4 = \frac{(y_3-y_2)^2 y_1 + (x_3-x_2)^2 y_2 + (x_1-x_2)(x_3-x_2)(y_3-y_2)}{(x_2-x_3)^2 + (y_2-y_3)^2} \end{cases} \quad (1)$$

2. Define the intermediate variable  $S$ , representing the distance from the point  $M$  to the point  $E$ , and calculated as follows:

$$S = 2 \cdot R \cdot$$

$$\arcsin\left(\sqrt{\sin^2\left(\frac{(y_3-y_4)\pi}{360}\right) + \cos\left(\frac{y_3\pi}{180}\right)\cos\left(\frac{y_4\pi}{180}\right)\sin^2\left(\frac{(x_3-x_4)\pi}{360}\right)}\right)$$



(2)

Where,  $R = 6378137\text{m}$  denotes the radius of the earth.

3. The latitude and longitude coordinates of the point  $T$  can be calculated by substituting  $S$  into Eq.(3), as follows:

$$\begin{cases} x_5 = x_4 + \frac{L(x_3 - x_4)}{S} \\ y_5 = y_4 + \frac{L(y_3 - y_4)}{S} \end{cases} \quad (3)$$

In the above,  $L$  is 2–5 times the length of the WS-USV.

**Remark 2.** The distance between the virtual target point and the projection point  $L = nL_{WS-USV}$ ,  $L$  is defined as the virtual desired distance,  $L_{WS-USV}$  is the length of the WS-USV. According to the principle of line-of-sight navigation,  $n=2-5$  is chosen in this study [38].

### 3.2. Heading tracking controller

The main function of the controller is to control the WS-USV at a certain speed to follow the desired path. An improved active disturbance rejection controller is designed, as described in this section.

#### 3.2.1. Introduction of nonlinear ADRC and ELM

ADRC is a practical control method proposed by Professor Han at the end of the 20th century [39]. It is mainly composed of a tracking differentiator (TD) to reduce the overshoot by arranging a transient process in the initial control state, an ESO to estimate the total disturbance, and a nonlinear state error feedback control law (NLSEF) to compensate the total disturbance by using the estimated value of ESO.

The TD part of ADRC is described as follows:

$$\begin{cases} \dot{v}_1 = v_2 \\ \dot{v}_2 = \varphi(v_1, v_2) \end{cases} \quad (4)$$

where  $v_1, v_2$  are the outputs,  $\varphi(v_1, v_2)$  is the nonlinear function.

The ESO part of ADRC is expressed as follows:

$$\begin{cases} \dot{e} = z_1 - y \\ \dot{z}_1 = z_2 - \alpha_1 e \\ \dot{z}_2 = z_3 - \alpha_2 \text{fal}(e, \alpha_1, \delta) + bu \\ \dot{z}_3 = -\alpha_3 \text{fal}(e, \alpha_2, \delta) \end{cases} \quad (5)$$

$$\text{fal}(e, a, \delta) = \begin{cases} e\delta^{a-1}, & |e| \leq \delta \\ |e|^a \text{sign}(e), & |e| > \delta \end{cases} \quad (6)$$

where the inputs of the ESO are the regulated output  $y$  and the control input  $u$  of the plant,  $e$  is the observer error,  $\alpha_1, \alpha_2, \alpha_3$

are control parameters for the output error,  $a_1$  and  $a_2$  denote the nonlinear divisor.  $\delta$  is the ESO filtering factor.  $z_1, z_2, z_3$  are the observed values of the state variables and the unknown total disturbances.

The nonlinear state error feedback (NLSEF) control law part of ADRC is as follows:

$$\begin{cases} e_1 = v_1 - z_1 \\ e_2 = v_2 - z_2 \\ u_0 = k_P \text{fal}(e_1, \epsilon_1, \delta_0) + k_D \text{fal}(e_2, \epsilon_2, \delta_0) \\ u = u_0 - \frac{z_3}{b_0} \end{cases} \quad (7)$$

where  $k_P, k_D$  are the gain parameters,  $b_0$  is the compensation factor,  $u_0$  is the amount of control before compensation,  $e_1, e_2$  are the state error and  $\epsilon_1, \epsilon_2$  are nonlinear parameters.

ELM is a fast single-hidden-layer feed-forward NN learning algorithm [40]. Its hidden layer node parameters can be randomly selected; only the number of hidden layer neurons need to be set. A unique optimal solution is obtained. The output weight of the network is a least-squared solution obtained by a minimised quadratic loss function. The parameters of the ELM need not be iterated after the determination. It is easy to use, and the calculation speed is fast. Therefore, the impetus to combine the ELM and the ADRC in practical applications is based on these merits.

The ELM algorithm is as follows. For a training data sample  $\{(x_j, t_j) | x_j \in R^d, t_j \in R^m, j = 1, 2, \dots, N\}$ , the output function expression of a single hidden layer feed-forward neural network with  $Q$  hidden layer neurons is as follows:

$$\sum_{i=1}^Q \beta_i G(\xi_i \cdot x_j + b_i) = t_j, j = 1, 2, \dots, N \quad (8)$$

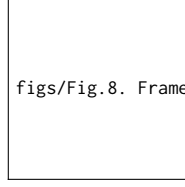
In the above,  $\xi_i$  and  $b_i$  are the hidden layer node parameters,  $\beta_i$  denotes the weight vector between the  $i$ -th hidden layer and network output, and  $G(\xi_i \cdot x_j + b_i)$  represents the hidden layer node output of the  $j$ -th hidden layer for sample  $x$ .

Eq.(8) can be abbreviated as  $H\beta = T$ . Training this network is equivalent to finding the least squares solution of the system  $H\beta = T$ .

$$\hat{\beta} = (H^T H)^{-1} H^T T \quad (9)$$

$$H(\xi_1, \dots, \xi_Q, b_1, \dots, b_Q, x_1, \dots, x_N) = \begin{bmatrix} G(\xi_1 \cdot x_1 + b_1) & \dots & G(\xi_Q \cdot x_1 + b_Q) \\ \vdots & \vdots & \vdots \\ G(\xi_1 \cdot x_N + b_1) & \dots & G(\xi_Q \cdot x_N + b_Q) \end{bmatrix}_{N \times Q} \quad (10)$$

$$\beta = \begin{bmatrix} \beta_1^T \\ \vdots \\ \beta_Q^T \end{bmatrix}_{Q \times m} \quad T = \begin{bmatrix} t_1^T \\ \vdots \\ t_N^T \end{bmatrix}_{N \times m} \quad (11)$$



**Figure 8:** Framework of improved active disturbance rejection control (ADRC) for the WS-USV.

In the above,  $H$  is the output matrix of the hidden layer, and  $G(\xi_i \cdot x_j + b_i)$  denotes the output of the  $i$ -th hidden layer neuron corresponding to input  $x_j$ . According to the ELM algorithm, the ELM network model for the improved active disturbance rejection controller for the WS-USV is as follows

Collect the output data  $\{(Z_{1i}, Z_{2i}, Z_{3i}) | Z_{1i}, Z_{2i} \in \mathbb{R}^d, Z_{3i} \in \mathbb{R}^m\}$  of the ESO, and use it as the training sample data;

determine the output function  $G(\xi_i, b_i, Z_{1i}, Z_{2i})$  of the hidden layer, and the number of hidden layer nodes  $Q$ ;

randomly generate hidden layer node parameter  $(\xi_i, b_i)$ ,  $i = 1, 2, \dots, Q$ ;

calculate the output matrix  $H$  of the hidden layer; and calculate the output weight  $\beta$  of the network, as follows

$$\beta = H^+T \quad (H^+ = (H^T H)^{-1} H^T) \quad (12)$$

The trained ELM module is embedded in the active disturbance rejection controller, and part of the output data  $(Z_{1i}, Z_{2i})$  of the ESO is taken as the input of the ELM module. Then, the output of the ELM module is connected to a feedback loop of the control object for the ESO. The active disturbance rejection controller combined with the ELM is shown in Fig.8.

### 3.2.2. Design of the improved heading ADRC

The mathematical model of WS-USV is given as follows

$$\begin{cases} \dot{\psi} = r \\ \dot{r} = bP_2 + W \\ y = \psi \end{cases} \quad (13)$$

where  $\psi$  denotes the heading of WS-USV,  $r$  is the yaw velocity,  $P_2$  is the input signal,  $y$  is the output signal,  $b$  is a position parameter,  $W$  is the total unknown dynamics.

A reference system is given as follows

$$\begin{cases} \dot{\psi}_d = r_d \\ \dot{r}_d = \varphi(\psi_d, r_d), \varphi(0, 0) = 0 \end{cases} \quad (14)$$

where  $\psi_d$  is the reference input. Assume throughout this paper that  $\varphi \in C(\mathbb{R}^2, \mathbb{R})$  such that the system (14) is globally asymptotically stable.

The tracking differentiator of improved ADRC is

$$\begin{cases} \dot{\psi}_{d1} = r_{d1} \\ \dot{r}_{d1} = f_{st}(\psi_{d1}, r_{d1}, \psi_d) \end{cases} \quad (15)$$

where  $\psi_{d1}$  denotes the reference heading of WS-USV,  $r_{d1}$  is the reference yaw velocity,  $f_{st}(\psi_{d1}, r_{d1}, \psi_d)$  is the optimal synthetic rapid control function.

The improved ESO is expressed as

$$\begin{cases} e = Z_1 - \psi \\ \dot{Z}_1 = Z_2 - \beta_1 e \\ \dot{Z}_2 = Z_3 - \beta_2 f_{al}(e, a_1, \delta_2) \\ \quad + f_{ann}(Z_1, Z_2) + b_0 P_2 \\ \dot{Z}_3 = -\beta_3 f_{al}(e, a_2, \delta_2) \end{cases} \quad (16)$$

where  $f_{ann}(Z_1, Z_2)$  is ELM function,  $Z_1, Z_2$  and  $Z_3$  are the estimated values of the WS-USV state variables by the ESO, respectively.  $a_1, a_2, \delta_2, \beta_1, \beta_2, \beta_3$  and  $b_0$  are adjustable parameters.  $e$  is the observation error.

The control law of the improved ADRC is

$$\begin{cases} e_1 = \psi_{d1} - Z_1 \\ e_2 = r_{d1} - Z_2 \\ u_0 = k_P f_{al}(e_1, a, \delta_1) + k_D f_{al}(e_2, a, \delta_1) \\ P_2 = u_0 - (Z_3 + f_{ann}(Z_1, Z_2))/b_0 \end{cases} \quad (17)$$

where  $a, k_P, k_D$  and  $\delta_1$  are the adjustable parameters,  $e_1$  and  $e_2$  are the heading error and yaw velocity error, respectively. **Assumption A1.** The total unknown dynamics  $W$  of WS-USV is continuously differentiable, bounded and its first derivative is also bounded.

**Assumption A2.**  $W$  and the solutions  $\psi, r$  of Eq.(13), satisfy  $|W| + |\psi| + |r| \leq B_0$  for a constant  $B_0 > 0$ .  $|-f_{ann}(Z_1, Z_2)| + |b - b_0| |P_2| \leq c^*$  for a constant  $c^* > 0$ .

**Assumption A3.** There exists constants  $\bar{\omega}_{1i} (i = 1, 2, 3, 4)$ ,  $\mu_{12}, \mu_{13}$  and positive define, continuous differentiable functions  $V_1, \Phi_1$ , such that

- 1)  $\bar{\omega}_{11} \|\chi\|^2 \leq V_1(\chi) \leq \bar{\omega}_{12} \|\chi\|^2, \bar{\omega}_{13} \|\chi\|^2 \leq \Phi_1(\chi) \leq \bar{\omega}_{14} \|\chi\|^2$ ;
- 2)  $\frac{\partial V_1(\chi)}{\partial \chi_1} (\chi_2 - g_1(\chi_1)) + \frac{\partial V_1(\chi)}{\partial \chi_2} (\chi_3 - g_2(\chi_1)) + \frac{\partial V_1(\chi)}{\partial \chi_3} g_3(\chi_1) \leq -\Phi_1(\chi)$ ;
- 3)  $|\frac{\partial V_1(\chi)}{\partial \chi_2}| \leq \mu_{12} \|\chi\|, |\frac{\partial V_1(\chi)}{\partial \chi_3}| \leq \mu_{13} \|\chi\|$ .

where  $\chi = (\chi_1, \chi_2, \chi_3)$ ,  $\|\cdot\|$  denotes the Euclid norm.

**Lemma 1[41].** Suppose that Assumption A1-A3 are satisfied. Then the ESO (16) is convergent.

Proof: See Appendix A.

**Assumption A4.**  $\varphi(v)$  is continuously differentiable,  $\varphi(0) = 0$ , and Lipschitz continuous with Lipschitz constant  $L_1$ :  $|\varphi(v) - \varphi(\hat{v})| \leq L_1\|v - \hat{v}\|$  for all  $v, \hat{v} \in \mathbb{R}^2$ . There exists constants  $\bar{\omega}_{2i}(i = 1, 2, 3, 4)$ ,  $\mu_{22}$  and positive define, continuous differentiable functions  $V_2, \Phi_2$ , such that

- 1)  $\bar{\omega}_{21}\|v\|^2 \leq V_2(v) \leq \bar{\omega}_{22}\|v\|^2$ ,  $\bar{\omega}_{13}\|v\|^2 \leq \Phi_2(v) \leq \bar{\omega}_{24}\|v\|^2$ ;
- 2)  $v_2 \frac{\partial V_2(v)}{\partial v_1} + \varphi(v_1, v_2) \frac{\partial V_2(v)}{\partial v_2} \leq -\Phi_2(v)$ ;
- 3)  $|\frac{\partial V_2(v)}{\partial v_2}| \leq \mu_{22}\|v\|, \forall v = (v_1, v_2) \in \mathbb{R}^2$ .

In above assumption, the continuous differentiability and Lipschitz continuity of  $\varphi(\cdot)$  imply that

$$|\frac{\partial \varphi(v)}{\partial v_i}| \leq L_1, v \in \mathbb{R}^2, i = 1, 2. \quad (18)$$

**Assumption A5.** Both  $\psi_d$  and  $\dot{\psi}_d = r_d$  are bounded in  $[0, \infty)$ , and  $\varphi(\cdot)$  is locally Lipschitz continuous, and system (15) with  $\psi_d \equiv 0$  is globally asymptotically stable.

The proof of Assumption A5 is given in the Theorem 3.1 of Ref.[42].

**Lemma 2[43].** Suppose that Assumption A1-A5 are satisfied. Then the tracking errors  $\psi_{d1} - \psi$  and  $r_{d1} - r$  are convergent.

Proof: See Appendix B.

To convert the mathematical form of the controller into C code and integrate it into the control system of a WS-USV, the improved active disturbance rejection controller must be discretised. The TD discrete algorithm is expressed as follows:

$$\begin{cases} \psi_{d1}(k+1) = \psi_{d1}(k) + T r_{d1}(k) \\ r_{d1}(k+1) = r_{d1}(k) + T f st(\psi_{d1}(k), r_{d1}(k), \psi_d(k), r, h) \end{cases} \quad (19)$$

where  $T$  denotes the sampling period of the control system,  $f st(\psi_{d1}, r_{d1}, \psi_d, r, h)$  is the optimal synthetic rapid control function,  $\psi_d$  denotes the direction angle between the current position and desired position of the WS-USV, and is the input signal of the path-following system,  $\psi_{d1}$  and  $r_{d1}$  are the states of the tracking system, and  $r$  and  $h$  are adjustable parameters used to adjust the frequency and filtering effect of the tracking differentiator.

For the second-order system, the ESO discrete algorithm

can be described as follows

$$\begin{cases} e(k) = Z_1(k) - \psi(k) \\ Z_1(k+1) = Z_1(k) + T(Z_2(k) - \beta_1 e(k)) \\ Z_2(k+1) = Z_2(k) + T(Z_3(k) - \beta_2 f al(e(k), a_1, \delta_2) + f_{ann}(Z_1, Z_2) + b_0 P_2(k)) \\ Z_3(k+1) = Z_3(k) - T \beta_3 f al(e(k), a_2, \delta_2) \end{cases} \quad (20)$$

where  $f_{ann}(Z_1, Z_2)$  is ELM function, which is described as follows

$$f_{ann}(Z_1, Z_2) = \sum_{i=1}^Q \zeta_i \left( \frac{1}{1+e^{-(\xi_{1i} Z_1 + b_i)}} + \frac{1}{1+e^{-(\xi_{2i} Z_2 + b_i)}} \right) \quad (21)$$

The discrete algorithm of the NLSEF control law is described as follows

$$\begin{cases} e_1(k) = \psi_{d1}(k) - Z_1(k) \\ e_2(k) = r_{d1}(k) - Z_2(k) \\ u_0(k) = k_P f al(e_1(k), a_1, \delta_1) + k_D f al(e_2(k), a_2, \delta_1) \\ P_2(k) = u_0 - (Z_3(k) + f_{ann}(Z_1, Z_2))/b_0 \end{cases} \quad (22)$$

In the above,  $Z_1(k)$ ,  $Z_2(k)$  and  $Z_3(k)$  are the estimation values of the ship state variables by the ESO.  $\psi(k)$  is the controlled output of the system,  $\delta_2$ ,  $\beta_1$ ,  $\beta_2$  and  $\beta_3$  are adjustable parameters.  $k_P$ ,  $k_D$ ,  $\delta_1$ ,  $a_1$  and  $a_2$  are the adjustable parameters.  $P_2(k)$  is the output value of the controller, and can be input into the propeller controller after the corresponding transformation.

$$P_c(k) = P_1(k) + P_2(k) \begin{bmatrix} -1 \\ 1 \end{bmatrix} \quad (23)$$

where  $P_c(k) = [P_{c1}(k), P_{c2}(k)]^T$  is the converted output value vector, and  $P_1(k) = [P_{1l}(k), P_{1r}(k)]^T$  is the vector consisting of the duty cycles corresponding to the desired speeds of the left and right propellers.

The WS-USV adopts a twin-propeller propulsion mode without a rudder module, and only steers through the speed difference of the twin-propeller. The relationship between the propeller speed difference and yaw moment is expressed as follows [44]

$$N_P = k(n_l - n_r)d_P \quad (24)$$

In the above,  $k$  is the conversion coefficient,  $N_P$  is the yaw moment,  $n_l$  and  $n_r$  are the rotation speeds of the left and right propellers, respectively, and  $d_P$  is the installation distance of the left and right propellers.

Owing to the structural characteristics of the propeller, it is governed by multiple input constraints. The inherent control law of the propeller is shown in Table.1, the speeds

**Table 1**  
Control law of the propeller

positive pulse width range (period 8ms)	propeller status
1.5ms	stop
1.5ms–2.2ms	forward rotation, speed increase
1.5ms–0.8ms	reverse rotation, speed increase

for forward and reverse rotation of the propeller are limited. The frequent operation of the propeller at an extreme speed will significantly increase the wear, affecting the stability of the system.

The duty cycles corresponding to the pulse width range are 1.5ms for 150, 1.5ms–2.2ms for 150–220, and 1.5ms–0.8ms for 150–80, respectively.

As the WS-USV is steered based on twin-propeller rotation speed difference, in the course of an attitude adjustment, the propeller will frequently switch between forward and reverse rotation. Even when the steering demand is large, switches from the forward maximum speed to reverse maximum speed often occur. However, this cannot be achieved in a short period of time, and has a great impact on the propellers and hardware system of the WS-USV, as well as the stability of the entire control system [45]. According to Eq.(13), the greater the rotation speed difference of the twin-propeller, the greater the yaw moment. If the steering is too fast, the tracking effect will be poor, and the tracking performance will be unstable. Considering the above engineering practice, in the design process of the controller, a saturation function is introduced to limit the amplitude and speed of the control input to reduce the adverse effects and enhance the stability of the system.

When the WS-USV is sailing forward, the calculation is as follows

$$P_{ii}(k) = \begin{cases} 200 & \text{if } P_{ci}(k) \geq 200 (i = 1, 2) \\ P_{ci}(k) & \text{if } 150 < P_{ci}(k) < 200 \\ 150 & \text{if } P_{ci}(k) \leq 150 \end{cases} \quad (25)$$

When the WS-USV is sailing backward, the calculation is as follows

$$P_{ii}(k) = \begin{cases} 100 & \text{if } P_{ci}(k) \leq 100 (i = 1, 2) \\ P_{ci}(k) & \text{if } 100 < P_{ci}(k) < 150 \\ 150 & \text{if } P_{ci}(k) \geq 150 \end{cases} \quad (26)$$

In the above,  $P(k) = [P_{11}(k), P_{22}(k)]^T$  denotes the vector consisting of the control output after conversion and engineering restrictions.

**Remark 3.** Compared with robust control methods that are based on the worst case design, the robustness of ADRC may not be as good as these methods since they are designed to achieve best possible robust performance in the presence

of the worst uncertainty. Thus, ADRC can be regarded as a “refined” robust control method. However, it provides a promising approach for trading off between the nominal performance and robustness. Above all, ADRC provides an alternative approach to widely used robust control and adaptive control methods for dealing with uncertain systems.

**Remark 4.** It is demonstrated in [46] that nonlinear ESO has better tracking performance in low frequency bands than linear ESO, but worse tracking performance in high frequency bands than linear ESO. For ship motion control, the low frequency position information of the ship and the low frequency disturbance that can cause ship position change. The high frequency signals caused by ocean disturbances need to be filtered out. From this point of view, nonlinear ESO is more suitable for the needs of state and disturbance estimation in ship motion control. Furthermore, the propeller suffers from the constraint of thrust amplitude due to the inherent characteristics. In order to alleviate the effect of amplitude limitation and improve the stability of the system, the nonlinear saturation function is introduced for the controller design. It is clear that the WS-USV is a complex nonlinear system with strong uncertainty. From this point of view, ADRC is more suitable for the controller design than LADRC.

**Remark 5.** It is shown in [47] that a NN-based ADRC has better dynamic characteristics than ADRC. In order to clarify the reason of using the ELM, we compare it with back propagation neural network (BPNN). Compared with the training speed and structure, we find that the ELM is fast in training speed and simple in structure. In the ELM training process, there is no need to adjust the number of hidden layer neurons and the only optimal solution can be obtained. The training of ELM is simplified since ELM works for generalized single-hidden layer feed-forward networks. However, BPNN has multi-layer hidden layer and the training process is complex. ELM has faster learning speed and better generalization performance. In addition, ELM is easier to be implemented in the ARM control module than BPNN.

**Remark 6.** The main work of this paper is the application of improved nonlinear ADRC to the heading control of WS-USV based on the milestone theoretical analysis of the convergence of nonlinear ADRC in [41, 42, 43]. The effectiveness and stability of the designed nonlinear heading ADRC are proved from the perspective of practice by a large number of navigation experiments of WS-USV. A brief theoretical analysis of nonlinear heading ADRC is given in Appendix A and B. For a detailed analysis of the convergence of nonlinear ADRC, authors can refer to Ref.[41, 42, 43].

## 4. Experimental and result analysis of water sampling

### 4.1. Setting of water sampling target points

The WS-USV prototype is shown in Fig.9.

Before water sampling starts, the target sampling points must be selected according to the requirements of the water sample collection. According to the principle of random





Figure 9: WS-USV prototype.

sampling, five target points were selected, i.e. the middle and four corners of the water sampling area. The latitude and longitude coordinates of the five sampling points were measured by GPS, and were sent to the WS-USV by the remote control platform. The latitude and longitude coordinates of the five desired sampling points used in this experiment are shown in Table 2.

**Table 2**  
Coordinates of water sampling points.

Sampling point number	Longitude	Latitude
1	118.083457° E	24.581749° N
2	118.083950° E	24.581277° N
3	118.083940° E	24.582722° N
4	118.082936° E	24.582699° N
5	118.083116° E	24.581123° N

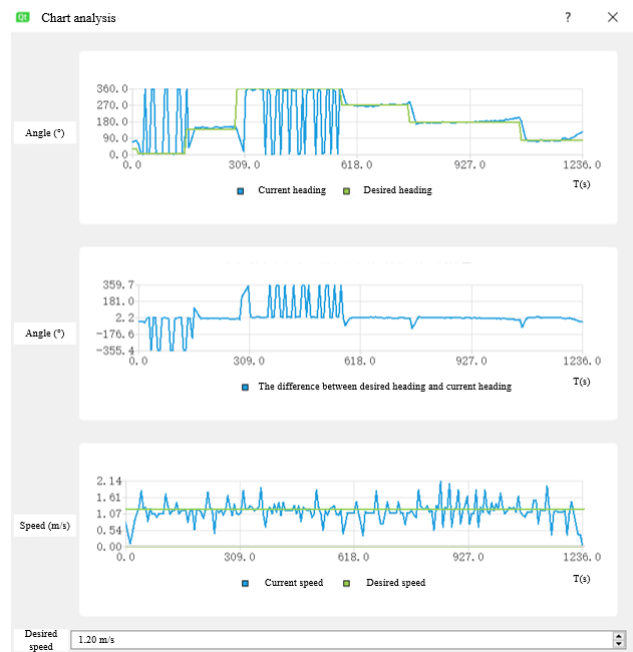
#### 4.2. Testing of automatic water sampling navigation

In this experiment, a single closed-loop control method for heading based on a constant speed was adopted to test the automatic path-following control performance, perform a real-time comparison of the current heading and desired heading in the navigation process, provide real-time recording of heading errors, and change the left and right propellers' rotation speeds to adjust the course. The traditional ADRC method path-following control performance test and improved ADRC strategy path-following control performance test were conducted in this experiment. This experiment was conducted in a sea area with a grade 4 westerly wind, and it was cloudy. In the process of the experiment, the distance threshold, yaw angle threshold, and reference speed of the WS-USV were set as 3m, 3° and 1.2m/s, respectively. The threshold meant that when the difference between the current value and desired value was less than the threshold value, the current value could be regarded as equal to the desired value. The velocity factor  $r_0$ , sampling step  $h_0$ , sampling time  $t$  and parameter  $\delta$  of the ADRC took empirical values of 3000, 0.005, 0.01 and 0.1, respectively. After many experiments, the diagram of the water sampling path and contrast

curve between the actual heading and desired heading of the WS-USV path-following controller was designed based on the ADRC technology. Its depiction in the HMI is shown in Fig.10. The control parameters  $b_0$ ,  $\beta_1$ ,  $\beta_2$ ,  $\beta_3$ ,  $k_P$  and  $k_D$  were 1.3, 85.5, 2436.75, 23149.5, 2.95 and 0.55, respectively.



a. Diagram of the water sampling path.



b. Diagram of course and speed tracking.

Figure 10: Diagram of water sampling path tracking control for the ADRC.

The same control parameters were adopted in the WS-USV path-following controller based on the ADRC method combined with ELM. The offsets  $a$  and  $b$  of the hidden layer and output layer of the ELM were 0.46 and 0.367, respectively, and the learning rate was set as 0.352. The corresponding input weights are listed in Table.3.

After ELM training, the diagram of the water sampling path and contrast curve between the actual heading and desired heading of the WS-USV path-following controller based on the ADRC strategy combined with ELM were depicted in the HMI, as shown in Fig.11.

Specification of speed and course tracking diagram: As the range of the heading collected by electronic compass

**Table 3**  
 Input weights of each neuron

Neuron number	Input weight
1	(-0.04824, 0.03983)
2	(-0.26338, -0.89235)
3	(0.31122, 0.72437)
4	(0.87640, -0.11413)
5	(0.24085, 0.09602)
6	(-0.43432, 0.13372)
7	(-0.58964, 0.36079)
8	(-0.12173, -0.25724)
9	(-0.94550, -0.84354)
10	(0.75237, -0.08730)
11	(0.22018, -0.90431)
12	(-0.59282, 0.47651)

was  $0^\circ$  to  $360^\circ$  and the desired heading corresponding to the second tracking point was  $359.74^\circ$ , there was a leap from  $360^\circ$  to  $0^\circ$  within the normal range. Thus, the difference between the actual heading and desired heading as shown in the course tracking diagram did not exceed the angle threshold range, and the course tracking was normal. Comparisons of the water sampling paths based on the traditional ADRC method and improved ADRC strategy are shown in Fig.12.

The actual headings of the WS-USV based on the traditional ADRC method and improved ADRC strategy are depicted in Fig.13. It can be seen from Fig.10-Fig.13 that the two path-following controllers (the traditional ADRC technology and the improved ADRC method) had the same desired speed in the process of multiple-point water sampling. The error between the improved ADRC water sampling path and desired path is less than the difference from the traditional ADRC method. The improved ADRC strategy yaw angle jump is smaller and more stable, where as the traditional ADRC method yaw angle oscillation is relatively large. In summary, the control system designed based on the two control methods is effective and stable, and the control performance of the improved ADRC method is slightly superior to that of the traditional ADRC technology.

The real-time duty cycles of the left and right propellers are processed by amplitude limiting and speed limiting. For example, the duty ratios correspond to the real-time speeds of the left and right propellers, as shown in Fig.14.

The duty cycle difference corresponding to the real-time rotation speed difference between the left and right propellers is shown in Fig.15. It can be seen from Fig.14 and Fig.15 that the rotation speed and rotation speed difference for the left and right propellers are kept within a limited range, and the rotation speed is kept within the maximum speed range of 0 to 71.5%. This significantly reduces the abnormal wear caused by frequent use of maximum speed, and also prevents instability in the system and running errors in the control program caused by the sudden switching from forward to reverse in the propeller. The rotation speed difference of the propellers is maintained within a proper range, which reduces the amplitude and frequency of the yaw of the WS-



a. Diagram of the water sampling path.



b. Diagram of course and speed tracking.

**Figure 11:** Diagram of water sampling path tracking control for the improved ADRC.

USV and is conducive to a stable sail. However, the performance of the WS-USV in emergency obstacle avoidance or large winds and waves will be affected by the relevant restrictive treatment. In view of this situation, a gear shift function is added to the design of the WS-USV system. All restrictions are removed by automatically shifting gears, and the maximum speed and maximum yaw moment are restored to cope with the emergency.

## 5. Conclusion

In this study, a set of WS-USV systems is designed, including a remote automatic control platform, joystick remote controller, and USV. An automatic path-following control system based on an ARM controller combined with GPS and an electronic compass is developed for a WS-USV. Aiming at practical engineering problems (such as frequent switching between extreme speed causes system instability), an improved ADRC strategy is proposed. A saturation function is

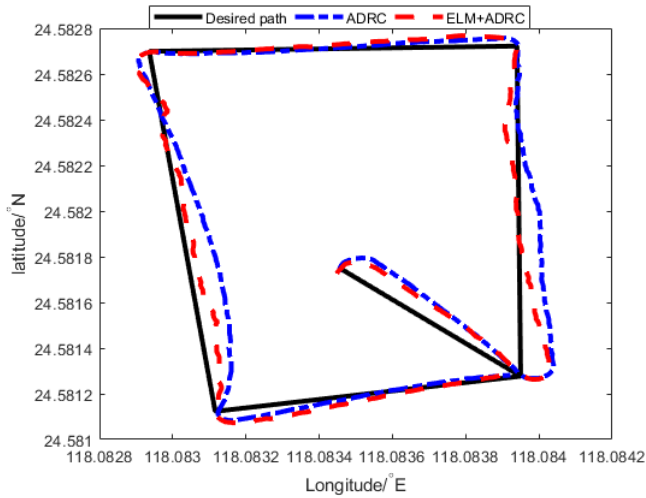


Figure 12: Water sampling paths.

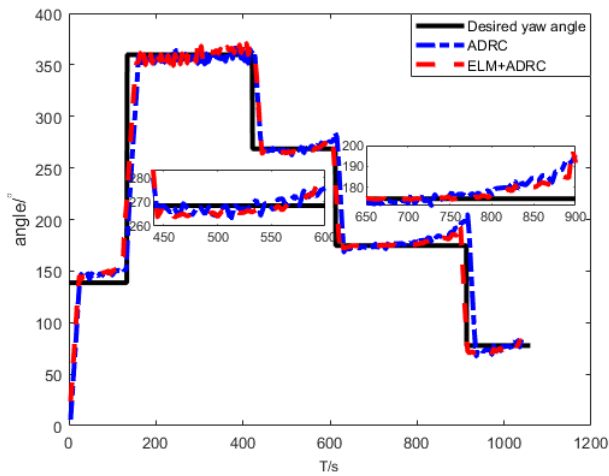


Figure 13: Desired and actual yaw angles of the WS-USV.

introduced into the controller design to address limitations regarding amplitude and rate, ensuring the stability of the control system and reducing the wear of the propeller. A constant speed and heading closed-loop control is adopted for the design of the WS-USV control system. The WS-USV comprises multi-point automatic sampling equipment with a remote controller that integrates manual remote control, key control, and important parameter displays, and a convenient remote automatic control platform providing functions for map display, manual control, video recording, parameter display, and water sampling. The feasibility and stability of the control system are verified by multi-group water sampling experiments. The comparisons of the traditional ADRC and improved ADRC indicate that the control effect of the improved ADRC is better than that of the traditional ADRC.

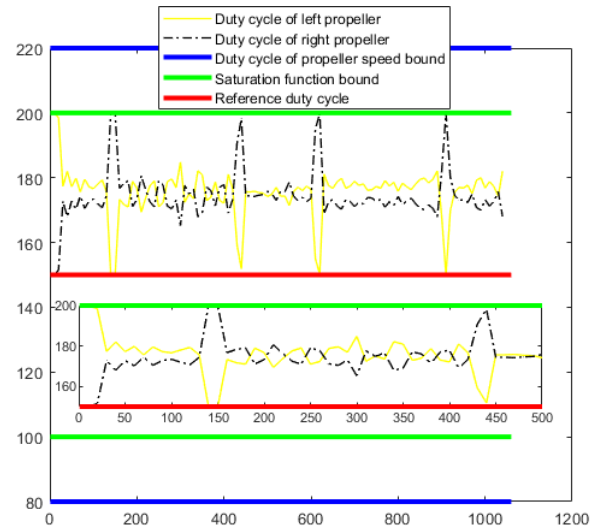


Figure 14: Duty cycles of the left and right propellers.

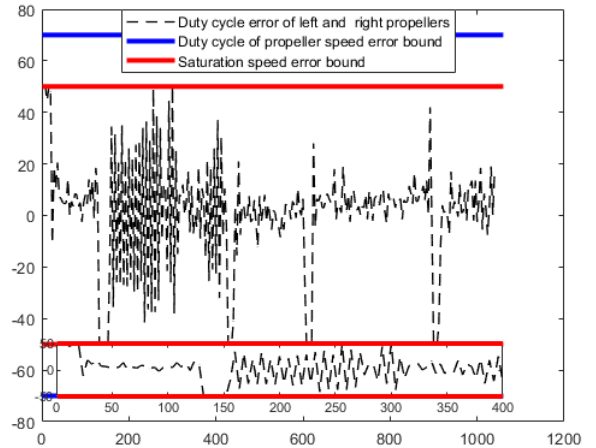


Figure 15: Duty cycle errors of the left and right propellers.

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## Appendix A

Proof of Lemma 1.

**Proof.** With an extended state variable  $x_3 = W + (b - b_0)P_2$ ,

the system (13) can be written as:

$$\begin{cases} \dot{x}_1 = \dot{\psi} = r \\ \dot{x}_2 = \dot{r} = bP_2 + W \\ \dot{x}_3 = \dot{W} + (b - b_0)\dot{P}_2 = h \\ y = x_1 = \psi \end{cases} \quad (27)$$

where  $h = \dot{W} + (b - b_0)\dot{P}_2$ .

From Assumption A1 and A2, there is a positive constant  $h^* > 0$  such that  $|\dot{W} + (b - b_0)\dot{P}_2| = |h| < h^*$  for all  $t \geq 0$ . Set

$$\begin{cases} E_1 = \psi - Z_1 \\ E_2 = r - Z_2 \\ E_3 = (W + (b - b_0)P_2) - Z_3 \\ g_1(E_1) = -\beta_1 E_1 \\ g_2(E_1) = -\beta_2 \text{fal}(E_1, a_1, \delta_2) \\ g_3(E_1) = -\beta_3 \text{fal}(E_1, a_2, \delta_2) \end{cases} \quad (28)$$

According to (24),(26) and (27), we have  $E = [E_1, E_2, E_3]^T$  satisfies

$$\begin{cases} \dot{E}_1 = E_2 - g_1(E_1) \\ \dot{E}_2 = E_3 - g_2(E_1) - f_{ann}(Z_1, Z_2) + (b - b_0)P_2 \\ \dot{E}_3 = h - g_3(E_1) \end{cases} \quad (29)$$

By Assumption A3, finding the derivative of  $V_1(E) = \frac{1}{2}E_1^2 + \frac{1}{2}E_2^2 + \frac{1}{2}E_3^2$  with respect to  $t$  along the solution  $E$  of Eq.(29).

$$\begin{aligned} \frac{d}{dt}V_1(E) &= \frac{\partial V_1(E)}{\partial E_1}(E_2 - g_1(E_1)) + \frac{\partial V_1(E)}{\partial E_2}(E_3 \\ &\quad - g_2(E_1)) - \frac{\partial V_1(E)}{\partial E_3}g_3(E_1) \\ &\quad + \frac{\partial V_1(E)}{\partial E_2}(-f_{ann}(Z_1, Z_2) \\ &\quad + (b - b_0)P_2) + \frac{\partial V_1(E)}{\partial E_3}h \\ &\leq -\Phi_1(E) + c^*\mu_{12}\|E\| + h^*\mu_{13}\|E\| \\ &\leq -\frac{\bar{\omega}_{13}}{\bar{\omega}_{12}}V_1(E) + \frac{\sqrt{\bar{\omega}_{11}}}{\bar{\omega}_{11}}(c^*\mu_{12} \\ &\quad + h^*\mu_{13})\sqrt{V_1(E)} \end{aligned} \quad (30)$$

It follows that

$$\frac{d}{dt}\sqrt{V_1(E)} \leq -\frac{\bar{\omega}_{13}}{2\bar{\omega}_{12}}\sqrt{V_1(E)} + \frac{\sqrt{\bar{\omega}_{11}}}{2\bar{\omega}_{11}}(c^*\mu_{12} + h^*\mu_{13}) \quad (31)$$

By Assumption A3 again, we have

$$\begin{aligned} \|E\| &\leq \sqrt{\frac{V_1(E)}{\bar{\omega}_{11}}} \leq \frac{\sqrt{\bar{\omega}_{11}V_1(E(t_1))}}{\bar{\omega}_{11}} e^{-\frac{\bar{\omega}_{13}}{2\bar{\omega}_{12}}(t-t_1)} \\ &\quad + \frac{c^*\mu_{12} + h^*\mu_{13}}{2\bar{\omega}_{11}} \int_{t_1}^t e^{-\frac{\bar{\omega}_{13}}{2\bar{\omega}_{12}}(t-s)} ds \leq B_* \end{aligned} \quad (32)$$

This together with (27) yields

$$\begin{aligned} |E_j| &\leq \|E\| \leq \frac{\sqrt{\bar{\omega}_{11}V_1(E(t_1))}}{\bar{\omega}_{11}} e^{-\frac{\bar{\omega}_{13}}{2\bar{\omega}_{12}}(t-t_1)} \\ &\quad + \frac{c^*\mu_{12} + h^*\mu_{13}}{2\bar{\omega}_{11}} \int_{t_1}^t e^{-\frac{\bar{\omega}_{13}}{2\bar{\omega}_{12}}(t-s)} ds \\ &\xrightarrow{t \rightarrow \infty} 0, (j = 1, 2, 3) \end{aligned} \quad (33)$$

Therefore, the ESO is convergent. The proof is complete.

## Appendix B

Proof of Lemma 2.

**Proof.** Set

$$\eta = [\eta_1, \eta_2]^T, \eta_1 = \psi_{d1} - \psi, \eta_2 = r_{d1} - r. \quad (34)$$

From (15),(17),(27) and (34), it follows that

$$\begin{cases} \dot{\eta}_1 = \eta_2 \\ \dot{\eta}_2 = -\varphi(\eta_1, \eta_2) - E_3 - [\varphi(e_1, e_2) \\ \quad - \varphi(\psi_{d1} - \psi, r_{d1} - r)] \end{cases} \quad (35)$$

By Lipschitz continuity of  $\varphi(\cdot)$  assumed in Assumption A4, we have

$$\begin{aligned} |\varphi(\psi_{d1} - Z_1, r_{d1} - Z_2) - \varphi(\psi_{d1} - \psi, r_{d1} - r)| \\ \leq L_1 \|\psi - Z_1, r - Z_2\|^T \leq L_1 \| [E_1, E_2]^T \| \end{aligned} \quad (36)$$

Under Assumption A4 and using (36), we can compute the derivative of  $V_2(\eta) = \frac{1}{2}\eta_1^2 + \frac{1}{2}\eta_2^2 = \frac{1}{2}(\psi_{d1} - \psi)^2 + \frac{1}{2}(r_{d1} - r)^2$  along the solution of (35) as follows:

$$\begin{aligned} \frac{dV_2(\eta)}{dt} &= \eta_2 \frac{\partial V_2(\eta)}{\partial \eta_1} - \{\varphi(\eta) + E_3 + [\varphi(e_1, e_2) \\ &\quad - \varphi(\psi_{d1} - \psi, r_{d1} - r)]\} \frac{\partial V_2(\eta)}{\partial \eta_2} \\ &\leq -\Phi_2(\eta) + (L + 1)\mu_{22}\|E\|\|\eta\| \\ &\leq -\frac{\bar{\omega}_{23}}{\bar{\omega}_{22}}V_2(\eta) + N_*\sqrt{V_2(\eta)}, \forall t > t_2 \end{aligned} \quad (37)$$



where  $N_*$  is some R-dependent positive constant and we used the face  $\|E\| \leq B_*$  proved in (31). It then follows that

$$\frac{d\sqrt{V_2(\eta)}}{dt} \leq -\frac{\bar{\omega}_{23}}{\bar{\omega}_{22}}V_2(\eta) + N_*, \forall t > t_2 \quad (38)$$

This together with Assumption A4 implies that for all  $t > t_2$ , that

$$\|\eta\| \leq \sqrt{\frac{V_2(\eta)}{\bar{\omega}_{21}}} \leq \frac{\sqrt{\bar{\omega}_{21}}}{\bar{\omega}_{21}}(e^{-\frac{\bar{\omega}_{23}}{\bar{\omega}_{22}}(t-t_2)}\sqrt{V_2(\eta(t_2))}) + N_* \int_{t_2}^t e^{-\frac{\bar{\omega}_{23}}{\bar{\omega}_{22}}(t-s)} ds \quad (39)$$

Since the first term of the right-hand side of (39) tends to zero as  $t$  goes to infinity, and the second term is bounded, it follows that there exist  $t_1 > t_2$  and  $\Gamma_2 > 0$  such that  $\|[\psi_{d1} - \psi, r_{d1} - r]^T\| \leq \Gamma_2$  for all  $t > t_1$ . Thus the tracking errors  $\psi_{d1} - \psi$  and  $r_{d1} - r$  are convergent. The proof is complete.

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