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Published in: Monthly Notices of the Royal Astronomical Society

DOI: 10.1111/j.1365-2966.2009.16078.x

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Document Version Publisher's PDF, also known as Version of record

Publication date: 2010

Link to publication in University of Groningen/UMCG research database

Citation for published version (APA): Tashiro, H., Aghanim, N., Langer, M., Douspis, M., Zaroubi, S., & Jelic, V. (2010). Detectability of the 21-cm CMB cross-correlation from the epoch of reionization. *Monthly Notices of the Royal Astronomical* Society, 402(4), 2617-2625. https://doi.org/10.1111/j.1365-2966.2009.16078.x

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Detectability of the 21-cm CMB cross-correlation from the epoch of reionization

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Accepted 2009 November 19. Received 2009 November 19; in original form 2009 August 12

ABSTRACT

The 21-cm line fluctuations and the cosmic microwave background (CMB) are powerful probes of the epoch of reionization of the Universe. We study the potential of the cross-correlation between 21-cm line fluctuations and CMB anisotropy to obtain further constraints on the reionization history. We analytically compute the 21-cm cross-correlation with the CMB temperature anisotropy and polarization, and we calculate the signal-to-noise ratio (S/N) for its detection with *Planck* together with LOw Frequency ARray (LOFAR), Murchison Widefield Array (MWA) and Square Kilometer Array (SKA). We find, on the one hand, that the 21-cm cross-correlation signal with CMB temperature from the instant reionization can be detected with an S/N of \sim 2 for LOFAR and \sim 10 for SKA. On the other hand, we confirm that the detection of the 21-cm cross-correlation with CMB polarization is practically infeasible.

Key words: cosmic microwave background – cosmology: theory – large-scale structure of Universe.

1 INTRODUCTION

The measurement of 21-cm line of neutral hydrogen from high redshifts is eagerly awaited as a probe of the epoch of reionization (EoR). During the EoR, the first collapsed objects heat and ionize the intergalactic medium (IGM). Therefore, the epoch and the process of reionization are tightly related to the evolution of cosmological structure and the formation of the first objects (Barkana & Loeb 2001; Ciardi & Ferrara 2005; Fan, Carilli & Keating 2006). The 21-cm fluctuations are sensitive to the density, temperature and ionized fraction of IGM. Studying the 21-cm tomography tells us about the physics of IGM gas and structure formation during the EoR (Madau, Meiksin & Rees 1997; Tozzi et al. 2000; Ciardi & Madau 2003; Furlanetto, Zaldarriaga & Hernquist 2004), and several 21-cm experiments are recently designed and built [e.g. MWA,¹ LOw Frequency ARray (LOFAR),² Square Kilometer Array (SKA)³].

The 21-cm cross-correlation with other complementary probes is expected to provide additional information other than their respective autocorrelations. Besides, the cross-correlation has an advantage for observations of 21-cm fluctuations whose signal is weak, because it suffers from foregrounds and systematic effects less than the autocorrelations. The cross-correlation between the 21-cm line and the cosmic microwave background (CMB) has been studied by many authors. On large scales ($\ell \sim 100$), the 21-cm fluctuations cross-correlate with the CMB Doppler temperature anisotropies which are due to the motions of ionized baryons (Alvarez et al. 2006; Adshead & Furlanetto 2007). Because the maximum amplitude of the cross-correlation between the 21-cm fluctuations and CMB temperature anisotropies from reionization between the 21-cm fluctuations and CMB temperature anisotropies from reionization bubbles arises (Cooray 2004; Salvaterra et al. 2005; Slosar, Cooray & Silk 2007; Jelic et al. 2009). Salvaterra et al. (2005) showed that these two signals are anticorrelated on the scale corresponding to the typical size of an ionized bubble. Tashiro et al. (2008) studied the 21-cm cross-correlation with CMB *E*-mode polarization on large scales. They have shown that the peak of the cross-correlation spectrum reaches its maximum value when the average ionized fraction of the universe is about half as shown in the case of the 21-cm cross-correlation with the CMB Doppler temperature, and there is a damping that depends on the duration of reionization. The cross-correlation between the 21-cm means that the peak of the cross-correlation spectrum reaches is adamping that depends on the duration of reionization. The cross-correlation between the 21-cm cross-correlation with the CMB Doppler temperature, and there is a damping that depends on the duration of reionization. The cross-correlation between the 21-cm cross-correlation with the CMB Doppler temperature, and there is a damping that depends on the duration of reionization.

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¹ http://web.haystack.mit.edu/array/MWA

² http://www.lofar.org

³ http://www.skatelescope.org

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fluctuations and high-redshift galaxy distribution has also the potential to probe the EoR (Furlanetto & Lidz 2007; Wyithe & Loeb 2007; Lidz et al. 2009). On large scales, the 21-cm and galaxy distributions are anticorrelated, while on scales smaller than the typical size of an ionized bubble, these fields become roughly uncorrelated. Therefore, the cross-correlation between the 21-cm fluctuations and high-redshift galaxy distributions provides access to the evolution of the typical scale of the ionized bubble.

In this paper, we investigate the detectability of the cross-correlation between the 21-cm fluctuations and CMB by performing a signalto-noise ratio (S/N) analysis. Particularly, we focus on the cross-correlation on large scales and we discuss the detectability of the signals and the sensitivity to the reionization properties by *Planck* and LOFAR which will release useful data for the cross-correlation in the near future. This article is organized as follows. In Section 2, we give a short description of the S/N analysis. In Section 3, we provide analytic form of the cross-correlation between the 21-cm fluctuations and the CMB anisotropy which include both CMB temperature anisotropy and CMB *E*-mode polarization. In Section 4, we show the angular power spectrum of the cross-correlation. In Section 5, we evaluate the the S/N of the cross-correlation and discuss the detectability by upcoming observations. Section 6 is devoted to the conclusions. Throughout the paper, we use *Wilkinson Microwave Anisotropy Probe* (*WMAP*) 5-year values for the cosmological parameters, i.e. h = 0.73 ($H_0 = h \times 100 \text{ km s}^{-1}$ Mpc⁻¹), $T_0 = 2.725 \text{ K}$, $h^2 \Omega_b = 0.0223$ and $h^2 \Omega_m = 0.128$ (Komatsu et al. 2009) for a flat cosmology.

2 SIGNAL-TO-NOISE RATIO ANALYSIS

In order to investigate the detection level of the signals, a useful tool is the S/N analysis. The S/N analysis not only can give the prospective detection level for the observations but also allows us to compute the optimal observational properties for an arbitrary detection level.

In order to evaluate S/N, first, we must estimate the error of the power spectrum of the cross-correlation. For simplicity, we assume that CMB, 21-cm fluctuations and instrumental noise are Gaussian and the foregrounds and noise of 21-cm fluctuations and CMB anisotropy are not correlated. Under these assumption, the error of the power spectrum of the cross-correlation can be rewritten as (Knox 1995)

$$\Delta C_{\ell}^{2} = \frac{1}{(2\ell+1)f_{\rm sky}\Delta\ell} \left[(C_{\ell}^{21-\alpha})^{2} + (C_{\ell}^{\alpha} + N_{\ell}^{\alpha})(C_{\ell}^{21} + N_{\ell}^{21}) \right], \tag{1}$$

where the superscript 21 stands for 21-cm fluctuations and the superscript α stands for *D*, the CMB Doppler anisotropy, or *E*, the *E*-mode polarization, and C_{ℓ} and N_{ℓ} are the signal from the EoR and the noise power spectrum, respectively. In equation (1), Δl is the size of bins within which the power spectrum data are averaged over $l - \Delta l/2 < l < l + \Delta l/2$, and f_{sky} is the sky fraction common to the two cross-correlated signals. In this paper, we consider *Planck* as CMB observation, which is almost full sky. Therefore, f_{sky} corresponds to the sky fraction of 21-cm observations which is of the order of a few per cent at most.

From equation (1), we can obtain the total S/N for the 21-cm cross-correlation as

$$\left(\frac{S}{N}\right)^2 = f_{\rm sky} \sum_{\ell=\ell_{\rm min}}^{\ell_{\rm max}} (2\ell+1) \frac{|C_{\ell}^{21-\alpha}|^2}{|C_{\ell}^{21-\alpha}|^2 + (C_{\ell}^{21}+N_{\ell}^{21})(C_{\ell}^{\alpha}+N_{\ell}^{\alpha})}.$$
(2)

In the next section, we discuss the cross-correlation signal from reionization and we explicit the noise power spectrum in Section 5.1.

3 FORMALISM OF THE CROSS-CORRELATION

The angular power spectrum of the cross-correlation between 21-cm fluctuations and CMB has been obtained by Alvarez et al. (2006) and Tashiro et al. (2008). Here, we recall the analytic form of the cross-correlation with CMB Doppler temperature anisotropy and *E*-mode polarization and give a short description for our reionization model.

3.1 21-cm line fluctuations

The observed brightness temperature of the 21-cm lines in a direction \hat{n} and at a frequency ν is given as in Madau et al. (1997) by

$$T_{21}(\hat{\boldsymbol{n}};\nu) = \frac{\tau_{21}}{(1+z_{\rm obs})} (T_{\rm s} - T_{\rm CMB}) [\eta_{\rm obs}, \hat{\boldsymbol{n}}(\eta_0 - \eta_{\rm obs})], \tag{3}$$

where T_{CMB} is the CMB temperature and T_s is the spin temperature given by the ratio of the number density of hydrogen in the excited state to that of hydrogen in the ground state. The conformal time η_{obs} is associated with the redshift z_{obs} and $\nu = \nu_{21}/(1 + z_{\text{obs}})$ with ν_{21} being the frequency corresponding to the 21-cm wavelength. The optical depth for the 21-cm line absorption τ_{21} is

$$\tau_{21} = \frac{3c^3\hbar A_{10}x_{\rm H}n_{\rm H}}{16kv_{21}^2T_{\rm s}H(z)},\tag{4}$$

where $n_{\rm H}$ is the hydrogen number density and $x_{\rm H}$ is the fraction of neutral hydrogen, which is written as a function of the ionized fraction $x_e = 1 - x_{\rm H}$.

According to equations (3) and (4), the observed brightness temperature of the 21-cm lines will reflect baryon density fluctuations, $\delta_b \equiv (\rho_b - \bar{\rho}_b)/\bar{\rho}_b$, and fluctuations of the neutral hydrogen fraction, $\delta_H \equiv (x_H - \bar{x}_H)/\bar{x}_H$, where ρ_b is the baryon density and the symbols with an overline (⁻) represent the background values. We can rewrite equation (3) in the linear approximation:

$$T_{21}(\hat{\boldsymbol{n}}; \nu) = [1 - \bar{x}_e(1 + \delta_x)](1 + \delta_b)T_0 \approx [(1 - \bar{x}_e)(1 + \delta_b) + \bar{x}_e\delta_x]T_0,$$
(5)

where \bar{x}_e and δ_x are the average and the fluctuations of the ionized fraction, respectively, which are $\bar{x}_e = 1 - \bar{x}_H$ and $\delta_x = -\delta_H$ in the linear approximation, and T_0 is a normalization temperature factor given by

$$T_0 = 23 \left(\frac{\Omega_b h^2}{0.02}\right) \left[\left(\frac{0.15}{\Omega_m h^2}\right) \left(\frac{1+z_{obs}}{10}\right) \right]^{1/2} \left(\frac{T_s - T_{CMB}}{T_s}\right) \text{mK.}$$
(6)

The spin temperature is determined by three couplings with CMB, gas and Ly α photons. Before the reionization, T_s is set by the balance between the couplings with CMB and gas. Then, after gas is heated by stars and quasi-stellar objects and the reionization starts, T_s becomes much larger than the CMB temperature mainly by the Ly α coupling (Ciardi & Madau 2003). In this paper, since we focus on 21-cm signals from the EoR, we assume $T_s \gg T_{CMB}$ in order to obtain T_0 .

The 21-cm line fluctuation map at a frequency ν can be described by

$$\delta T_{21}(\hat{\boldsymbol{n}};\nu) = T_0 \sum_{\ell} \int \frac{\mathrm{d}k^3}{(2\pi)^3} \sqrt{4\pi (2\ell+1)} \left[(1-\bar{x}_e)(1+F\mu^2)\delta_{\mathrm{b}} - \bar{x}_e \delta_x \right] j_\ell [k(\eta_0 - \eta_{\mathrm{obs}})] Y_\ell^0(\hat{\boldsymbol{n}}), \tag{7}$$

where we take the Fourier expansion of δ_b and δ_x with Rayleigh's formula. We also introduced the factor $(1 + F\mu^2)$ to account for the enhancement of the fluctuation amplitude due to the redshift distortion (Kaiser effect) on the 21-cm line fluctuations, $\mu = \hat{k} \cdot \hat{n}$ and $F = d \ln g/d \ln a$ with g(a) the linear growth factor of baryon fluctuations (Bharadwaj & Ali 2004).

3.2 CMB anisotropy

As reionization proceeds, the coupling of CMB photons and free electrons by Thomson scattering becomes strong again. As a result, Thomson scattering during reionization produces secondary CMB temperature anisotropy and polarization.

In the CMB temperature, the main generation mechanisms at the EoR are the Doppler effect for first-order anisotropic fluctuations and the kinetic Sunyaev–Zel'dovich effect for the second order. While the former is dominant on large scales ($\ell < 1000$), the latter dominates on small scales ($\ell > 1000$). In the following, we focus on the computation of the cross-correlation power spectrum on large scales ($\ell \sim 100$). We therefore consider only the Doppler anisotropy and neglect the kinetic Sunyaev–Zel'dovich effect, although, by making this hypothesis, we underestimate the CMB temperature anisotropy generated during reionization at $\ell \sim 1000$.

The Doppler anisotropy of the CMB temperature produced during the EoR is given by $T_{\rm D}(\hat{n}) = -T_{\rm cmb} \int_0^{\eta_0} d\eta \dot{\tau} e^{-\tau} \hat{n} \cdot \mathbf{v}_{\rm b}(\hat{n}, \eta)$, where $\dot{\tau}$ is the differential optical depth for Thomson scattering $\tau(\eta)$ in conformal time $\dot{\tau} = n_{\rm e}\sigma_{\rm T}a$ with the electron number density $n_{\rm e}$, the cross-section of Thomson scattering $\sigma_{\rm T}$ and the scale factor *a* normalized to the present epoch. The continuity equation for baryons gives the peculiar velocity of baryons $\mathbf{v}_{bk} = -i(\mathbf{k}/k^2)\dot{\delta}_{bk}$, where the dot represents the derivative with respect to conformal time. Finally, the Doppler anisotropy is thus given by

$$T_{D}(\hat{\boldsymbol{n}}) = T_{\text{CMB}} \int_{0}^{\eta_{0}} \mathrm{d}\eta \, \dot{\boldsymbol{\tau}} e^{-\boldsymbol{\tau}} \int \frac{\mathrm{d}^{3}k}{(2\pi)^{3}} \frac{\dot{\delta}_{\text{b}}}{k^{2}} \sum_{\ell} \sqrt{4\pi (2\ell+1)} (-i)^{\ell} \frac{\partial}{\partial \eta} j_{\ell} [k(\eta_{0}-\eta)] Y_{\ell}^{0}(\hat{\boldsymbol{n}}), \tag{8}$$

where as above we have taken the Fourier expansion of δ_b with Rayleigh's formula.

During reionization, CMB polarization is produced from the quadrupole component of CMB temperature anisotropy by Thomson scattering. The CMB polarization can be decomposed into E and B modes with electric- and magnetic-like parities, respectively. We focus on the dominant modes generated by scalar perturbations. According to the Boltzmann equations for CMB, the scalar perturbations produce only E modes which are given by (Hu & White 1997)

$$E(\hat{\boldsymbol{n}}) = \sum_{\ell \mid m} (-i)^{\ell} \sqrt{\frac{4\pi}{2\ell+1}} \int \frac{\mathrm{d}^{3}k}{(2\pi)^{3}} E_{\ell}^{(0)} Y_{\ell}^{m}(\hat{\boldsymbol{n}}),$$
(9)

$$\frac{E_{\ell}^{(0)}(\eta_{0},k)}{2\ell+1} = -\frac{3}{2}\sqrt{\frac{(\ell+2)!}{(\ell-2)!}} \int_{0}^{\eta_{0}} \mathrm{d}\eta \,\dot{\tau} e^{-\tau} P^{(0)} \frac{j_{\ell}[k(\eta_{0}-\eta)]}{[k(\eta_{0}-\eta)]^{2}},\tag{10}$$

where $P^{(0)}$ is the m = 0 source term due to Thomson scattering. It is related to the initial gravitational potential Φ_0 via the transfer function $D_{\rm E}(k, \eta)$, $P^{(0)} = D_{\rm E}(k, \eta) \Phi_0$; this is detailed in the appendix of Tashiro et al. (2008).

3.3 Cross-correlation between 21 cm and CMB

The angular power spectrum is defined as the average of the spherical harmonic coefficients $a_{\ell m}$ over the $(2\ell + 1)$ *m*-values, $C_{\ell} = \sum_{m} \langle |a_{\ell m}|^2 \rangle / (2\ell + 1)$, where the $a_{\ell m}$ are defined for an arbitrary sky map $f(\hat{\boldsymbol{n}})$ as $f(\hat{\boldsymbol{n}}) = \sum_{\ell m} a_{\ell m} Y_{\ell}^m$.

From equations (7) and (8), the cross-correlation between the 21-cm line fluctuations and the CMB Doppler temperature anisotropy can be written as

$$C_{\ell}^{21-D}(z_{obs}) = -\frac{2}{3\pi} \int_{0}^{\infty} k^{2} dk \int_{0}^{\eta_{0}} d\eta \left[4\overline{x}_{H}(z_{obs}) D_{b}(k, \eta_{obs}) k^{2} P_{\Phi}(k) - 3\overline{x}_{e}(z_{obs}) P_{x\Phi} \right] \\ \times j_{\ell} [k(\eta_{0} - \eta_{obs})] j_{\ell} [k(\eta_{0} - \eta)] \frac{\partial}{\partial \eta} \dot{\tau} e^{-\tau} \dot{D}_{b}(k, \eta),$$
(11)

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where P_{Φ} and $P_{x\Phi}$ are the power spectra of the initial gravitational potential and the cross-correlation between the gravitational potential and the fluctuations of the ionized fraction, respectively. The function $D_{b}(k, \eta)$ relates δ_{b} to the initial gravitational potential Φ_{0} as $\delta_{b}(k, \eta) = k^{2}D_{b}(k, \eta)\Phi_{0}(k)$, and we have set $F\langle\mu^{2}\rangle = 1/3$ for the matter-dominated epoch. We can simplify equation (11) by using the approximation for $\ell \gg 1: 2\int_{0}^{\infty} dk P(k)j_{l}(kr)/\pi \approx P(k = l/r)\delta(r - r')/l^{2}$. We finally obtain

$$\ell^2 C_{\ell}^{21-\mathrm{D}}(z_{\mathrm{obs}}) = -\frac{1}{3} \left(\frac{\ell}{r_{\mathrm{obs}}}\right)^2 \left[4\overline{x}_{\mathrm{H}}(z_{\mathrm{obs}}) D_{\mathrm{b}}(k,\eta_{\mathrm{obs}}) \left(\frac{\ell}{r_{\mathrm{obs}}}\right)^2 P_{\Phi}\left(\frac{\ell}{r_{\mathrm{obs}}}\right) - 3\overline{x}_e(z_{\mathrm{obs}}) P_{x\Phi}\left(\frac{\ell}{r_{\mathrm{obs}}},z_{\mathrm{obs}}\right) \right] \frac{\partial}{\partial \eta'} \dot{\tau} e^{-\tau} \dot{D}_{\mathrm{b}}(k,\eta)|_{\eta=\eta_{\mathrm{obs}}}.$$
 (12)

Equation (12) involves two terms. One involves P_{Φ} and is the homogeneous ionization term. The other term involves $P_{x\Phi}$ and is the bias term. The homogeneous term corresponds to the anticorrelation part of the signal. In overdense regions, the 21-cm emission is strong due to the large amounts of hydrogen ($\delta_{21} > 0$); while the CMB temperature is lower due to the Doppler shift ($\delta_{Doppler} < 0$). The bias term in turn shows the positive correlation part of the signal. In overdense regions, ionizing sources are numerous and the quantity of neutral hydrogen is small. Therefore, the 21-cm emission in overdense regions is weaker than the background emission ($\delta_{21} < 0$).

The cross-correlation between 21-cm line fluctuations and E modes was studied in detail by Tashiro et al. (2008). We provide here the basic equation:

$$C_{\ell}^{E-21} = -\frac{3}{\pi} T_0 \sqrt{\frac{(\ell+2)!}{(\ell-2)!}} \int dk \int d\eta k^2 \dot{\tau} e^{-\tau} D_E(k,\eta) \left[\frac{4}{3} (1-\bar{x}_e) P_{\Phi\delta_b} - \bar{x}_e P_{x\Phi}\right] \frac{j_\ell [k(\eta_0 - \eta_{obs})] j_\ell [k(\eta_0 - \eta)]}{[k(\eta_0 - \eta)]^2},\tag{13}$$

where $P_{\Phi\delta_b}$ is the power spectrum of the cross-correlation between the gravitational potential and the baryon density fluctuations. According to the cosmological linear perturbation theory (e.g. Kodama & Sasaki 1984), the power spectrum $P_{\Phi\delta_b}$ can be written in terms of the initial power spectrum of the gravitational potential P_{Φ} as $P_{\Phi\delta_b} = k^2 D_b(k, \eta) P_{\Phi}$. The function $D_E(k, \eta)$ exhibits an oscillatory behaviour and it can be decomposed as well into a homogeneous ionization and a bias terms. However, their signs depend on D_E .

3.4 Reionization model

Cross-correlations between 21 cm and CMB in equations (12) and (13) involve two power spectra P_{Φ} and $P_{x\Phi}$. While P_{Φ} is computed using the WMAP cosmological parameters, $P_{x\Phi}$ depends on the reionization process. Although the latter is not well known, we can reasonably expect that ionizing sources are formed in dense regions and that they ionize the surrounding medium with an efficiency that depends on the density of the medium. Therefore, we can distinguish two possible cases: one where ionized fluctuations and matter overdensities coincide, and the other where ionized fluctuations and matter density are antibiased (e.g. Benson et al. 2001). Following Alvarez et al. (2006), we assume that the fluctuations of the ionized fraction are associated with the matter density contrast using the Press–Schechter description (Press & Schechter 1974). As a result, the power spectrum $P_{x\Phi}$ is given by

$$\bar{x}_e P_{x\Phi} = -\bar{x}_H \ln \bar{x}_H (\bar{b}_h - 1 - f) D_m (k, \eta) k^2 P_{\Phi}, \tag{14}$$

where $D_{\rm m}$ is the transfer function of matter (both dark and baryonic) and $\bar{b}_{\rm h}$ is the average bias of dark matter haloes more massive than the minimum mass of the source of ionizing photons $M_{\rm min}$ given by

$$\bar{b}_{\rm h} = 1 + \sqrt{\frac{2}{\pi}} \frac{e^{-\delta_c^2/2\sigma^2(M_{\rm min})}}{f_{\rm coll}\sigma(M_{\rm min})},\tag{15}$$

where $\sigma(M)$ is the variance of the density fluctuations smoothed with a top-hat filter of the scale corresponding to a mass M and f_{coll} is the fraction of matter collapsed into haloes with $M > M_{min}$. In this paper, we choose M_{min} such that the halo virial temperature is $T_{vir}(M_{min}) = 10^4$ K. This choice corresponds to the assumption that the ionizing sources form in dark matter haloes where the gas cools efficiently via atomic cooling. The parameter f describes the reionization regime we are interested in. For f = 0, we are in the 'photon-counting limit' case where recombinations are not important and where the progress of the reionization depends on the number of ionizing photons only. The overdense regions contain more collapsed objects which are sources of ionizing photons. Therefore, in this case, ionization in overdense regions is easier than in underdense regions. On the contrary, f = 1 indicates the 'Strömgren limit' case where ionization is balanced by recombination. Although the overdense regions contain more sources of ionizing photons, the recombination rate in overdense regions is higher than in underdense regions. Hence, overdense regions in the f = 1 case have a lower ionized fraction than in the f = 0 case (for details, see Alvarez et al. 2006).

Finally, in order to calculate the cross-correlation, we need the evolution of the mean ionized fraction for which we use a simple parametrization based on two key quantities, the reionization redshift (defined as the redshift at which the ionized fraction equals 0.5), z_{re} , and the reionization duration, Δz :

$$\bar{x}_e(z) = \frac{1}{1 + \exp[(z - z_{\rm re})/\Delta z]}.$$
(16)

4 CROSS-CORRELATION POWER SPECTRUM

In the left-hand panel of Fig. 1, we show the power spectrum of the cross-correlation between the 21-cm line fluctuations and the Doppler anisotropy. For this computation, we set the reionization redshift and duration as $z_{re} = 10$, $\Delta z = 0.1$ and we take $z_{obs} = 10$. We explore both

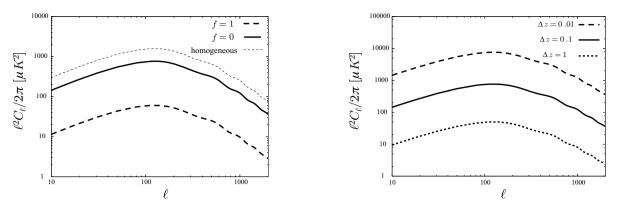


Figure 1. The cross-correlation between 21-cm fluctuations and CMB Doppler temperature anisotropy. In the left-hand panel, we show the dependence on the reionization model. We set $z_{re} = 10$, $\Delta z = 0.1$ and $z_{obs} = 10$. The solid line represents the f = 0 case where we do not take into account the recombinations. The dashed line is for the f = 1 case where recombinations and ionizations are balanced. The thin dotted line represents the homogeneous term where we do not consider the fluctuations of the ionized fraction δ_x . In the right-hand panel, the dependence on the reionization duration is shown for $z_{re} = 10$, f = 0 and $z_{obs} = 10$. The dashed, solid and dotted lines are for $\Delta z = 0.01$, 0.1 and 1, respectively.

the photon-counting-limit case (f = 0) and the Strömgren-limit case (f = 1). In both cases, the cross-correlation has a positive sign. As mentioned earlier, more fluctuations are produced in the photon-counting-limit case than in the Strömgren-limit case. The amplitude of the power spectrum with f = 0 is thus larger than that with f = 1.

The cross-correlation signal has two different contributions with opposite signs as shown in Section 3.3. One is associated with the bias term and the other is with the homogeneous term. For reference, we plot the homogeneous ionization part as the thin line in the left-hand panel of Fig. 1. At high redshifts (z > 15), since the average bias is high, the bias part dominates the homogeneous part as shown in the model of Alvarez et al. (2006) where they have taken $z_{re} = 15$ and $z_{obs} = 15$. However, at low redshifts (z < 15), since the bias is of the order of 1, the bias term is comparable to the homogeneous part. Therefore, in our reionization model where $z_{re} = 10$ and $z_{obs} = 10$, cancellation occurs in the total signal. Subsequently, the total amplitude of the cross-correlation ends up smaller than that in the homogeneous ionization part.

The right-hand panel of Fig. 1 exhibits the dependence of the cross-correlation power spectrum on the reionization duration for the case with $z_{re} = 10$, $z_{obs} = 10$ and f = 0. When the reionization time is fixed, the shorter the duration the larger the amplitude of the power spectrum. As a matter of fact, long duration of the reionization increases the integration range over η in equation (11) and thus causes cancellation of the correlation due to phase gap between the density and velocity fluctuations. Note that, according to Alvarez et al. (2006), the instantaneous reionization gives an infinite signal (equation 12). However, equation (12) is obtained using the Limber approximation which is no more valid in a short duration reionization. We therefore perform an exact calculation of the cross-correlations from equation (11).

The cross-correlation between 21-cm line fluctuations and CMB *E*-mode polarization was studied in detail in Tashiro et al. (2008). The angular power spectrum depends on the polarization source term $P(k_{obs})$, namely the quadrupole term of the CMB, at z_{obs} where k_{obs} satisfies $k_{obs} = \ell/(\eta_0 - \eta_{obs})$. Accordingly, the angular power spectrum exhibits its first peak at a multipole $\ell < 10$ which corresponds to the angular separation of the quadrupole at z_{obs} . The free streaming of the quadrupole at redshifts higher than z_{obs} produces oscillations at higher ℓ modes ($\ell > 10$). These oscillations are increasingly damped by larger reionization durations Δz . In addition and similarly to the cross-correlation between 21-cm line fluctuations and CMB Doppler temperature anisotropy, the parameter *f* affects the amplitude of the cross-correlation with the *E* modes. The *f* = 0 case produces more fluctuations than the *f* = 1 case, and thus a larger overall amplitude.

5 DETECTION OF THE CROSS-CORRELATION SIGNALS

For computation of the S/N, evaluating the noise power is crucial. Especially, the estimation of the experimental noise power spectrum for each observation strategy is an important factor of the noise power spectrum. Here, we introduce the parametrization of the experimental noise for the various planned observation: LOFAR, MWA and SKA. Then, we calculate the S/N for the 21-cm cross-correlation with CMB Doppler temperature and CMB *E*-mode polarization which are given by equations (12) and (13), respectively.

5.1 Noise power spectrum

In order to evaluate the noise power spectrum, we neglect the foregrounds. Under this assumption, the noise power spectrum of the signal from reionization consists of the experimental noise power spectrum and of the power spectrum of primary CMB.

For the CMB observation, we consider the *Planck* configuration. In this case, compared with the CMB signal, the experimental noise is very small on scales of interest. Therefore, we neglect the experimental noise power spectrum. This assumption gives the noise for the CMB Doppler temperature anisotropy as $N_{\ell}^{D} = C_{\ell}^{T}$ and for *E*-mode polarization from reionization as $N_{\ell}^{E} = C_{\ell}^{E}$, where C_{ℓ}^{E} is the primary CMB *E* modes.

For the 21-cm fluctuations, the dominant signal of the 21-cm line on large scales is that of reionization. Therefore, we can assume that the noise spectra of the 21-cm fluctuations consist of the experimental noise power spectra only. According to Zaldarriaga, Furlanetto &

Table 1. The current designs of 21-cm experiments. The estimated $\sqrt{N_{100}}$ is computed for the observation wavelength which corresponds to $z_{obs} = 10$.

	$f_{\rm sky}$	$\Delta \nu$ (MHz)	<i>t</i> _{obs}	$A/T ({ m m}^{2}/{ m K})$	D (Km)	$\sqrt{N_{100}}(\mu K)$
MWA	0.02	6	1000 h	13	1.5	5600
LOFAR-1	0.0024	1	800 h	108	2	1200
LOFAR-3	0.007	1	1500 h	108	2	900
SKA	0.009	1	1 month	1000	1	140
super SKA	0.018	1	1 month	1000	1	70

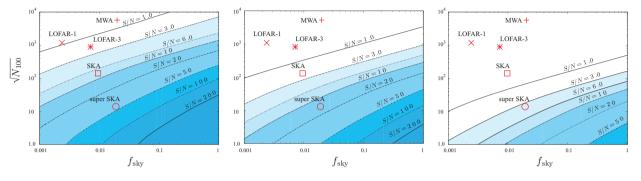


Figure 2. S/N of the 21-cm cross-correlation with the CMB Doppler anisotropy for different reionization durations. In all the panels, the S/N is given as a function of the sky fraction f_{sky} and the normalized noise power spectrum N_{100} . In all the panels, we set $z_{obs} = 10$ and $z_{re} = 10$. From left to right, the reionization durations are set to $\Delta z = 0.01, 0.1$ and 0.5.

Hernquist (2004), the power spectrum of the experimental noise of the 21-cm observations at a wavelength λ cm is given by

$$\frac{\ell^2 N_\ell^{21}}{2\pi} = \left(\frac{\ell}{100}\right)^2 N_{100},\tag{17}$$

where N_{100} is a normalized noise power spectrum which is written as

$$N_{100} = \frac{1}{t_{\rm obs}\Delta\nu} \left(\frac{100\ell_{\rm max}}{2\pi} \frac{\lambda^2}{A/T}\right)^2.$$
(18)

Here, Δv is the bandwidth, t_{obs} is the total integration time, A/T is the sensitivity (an effective area divided by the system temperature) and $\ell_{max} = 2\pi \frac{D}{\lambda}$ is the maximum multipole associated with the length of the baseline *D*. In Table 1, we summarize the main characteristics of the present designs of MWA (Bowman, Morales & Hewitt 2006; Lidz et al. 2008), LOFAR (Jelić et al. 2008) and SKA (Alvarez et al. 2006) and calculate $\sqrt{N_{100}}$ for the observation wavelength corresponding to an observing redshift $z_{obs} = 10$ matching the present reionization limits. In the table, LOFAR-1 and LOFAR-3 stand for two cases – one with a single observed field, LOFAR-1, and the second with the three observed fields, LOFAR-3. For reference, we consider an ideal experiment which we refer to as 'super SKA' with a sensitivity 10 times that of SKA and a field of view twice as large as SKA's.

5.2 Results

We calculate the S/N for the cross-correlation between 21-cm fluctuations and the CMB Doppler temperature anisotropy (Fig. 2) and CMB E modes (Fig. 3) for a reionization model with $z_{re} = 10$ and different reionization durations. In both figures, we show the dependence of S/N on f_{sky} and N_{100} . From left to right, Δz is set to 0.01, 0.1 and 0.5. In these two-parameter-space figures, we show the positions of the current experimental designs for 21-cm observations (see also Table 1). Fig. 2 shows that the cross-correlation between *Planck* and LOFAR, in its present configuration, is only sensitive to an 'instantaneous' reionization (with $\Delta z = 0.01$). If the quantity N_{100} , expressing the instrumental noise of LOFAR, were reduced by a factor of 10 (by improving the sensitivity T/A or increasing the observation field and S/N > 5 for multi observation fields. As shown in Section 4, the longer the duration of reionization Δz , the smaller the amplitude of the cross-correlation. As a result, LOFAR becomes insensitive to the reionization signal for $\Delta z = 0.1$ whereas SKA sees the S/N decreasing from S/N = 8 when $\Delta z = 0.01$ to S/N = 2.5 when $\Delta z = 0.1$. When the reionization is longer, $\Delta z = 0.5$, the cross-correlation signal is detected only by an ideal experiment like 'super SKA'.

Fig. 3 shows that the cross-correlation signal is detected only by an ideal experiment like 'super SKA' with at most S/N = 1.0. We show, in Fig. 4, the cross-correlation power spectrum between 21 cm and CMB *E* modes with the errors estimated from equation (1). As mentioned previously, increasing the duration of reionization damps the power at high ℓ s. At those scales, the noise due to CMB signal dominates the cross-correlation signal making it very difficult to probe the duration of reionization (see Fig. 4). As a result, the S/N does not depend on Δz as shown in Fig. 3.

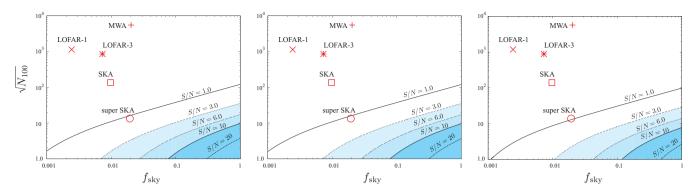


Figure 3. S/N of the 21-cm cross-correlation with the CMB *E* modes for different reionization durations. In all the panels, the S/N is given as a function of the sky fraction f_{sky} and the normalized noise power spectrum N_{100} . In all the panels, we set $z_{obs} = 10$ and $z_{re} = 10$. From left to right, the reionization durations are set to $\Delta z = 0.01, 0.1$ and 0.5.

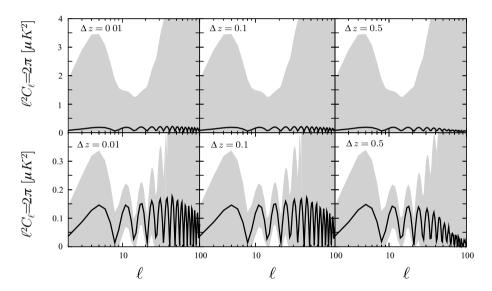


Figure 4. The 21-cm and *E*-mode cross-correlation signal with the estimated errors. We set $z_{obs} = 10$, $z_{re} = 10$ and f = 0. From left to right, we take $\Delta z = 0.01$, 0.1 and 0.5. The top panels show the cross-correlation error for SKA and the bottom panels are for super *SKA*. The cross-correlation signal is the solid line and the error regions are represented as the grey zone in each panel.

The amplitude of the cross-correlation gradually increases as the redshift z_{obs} goes down. The signal reaches its maximum value at $z_{obs} = z_{re}$ where the ionized fraction is about one-half. Tracing this evolution in the cross-correlation signal with future radio-interferometer observations may possibly constrain the duration of reionization. This is illustrated in Fig. 5, where we show the cross-correction with the estimated error at different redshifts in the ideal case of super *SKA* for two different reionization durations, $\Delta z = 0.1$ and 0.5. We show that the signal from the instantaneous reionization $\Delta z = 0.01$ vanishes before or after the redshift z_{re} , whereas the signal from a longer duration, $\Delta z = 0.5$, does not disappear.

In the estimation of the S/N of the cross-correlation, the autocorrelation for each observation is the ultimate source of noise as shown in equation (2). We therefore calculate the highest S/N attainable, i.e. in the full sky survey (the sky fraction is a multiplicative factor), and we plot the resulting S/N as a function of N_{100} in Fig. 6. For this computation, we set $z_{obs} = 10$, $z_{re} = 10$ and f = 0. The amplitude of the 21-cm cross-correlation with the CMB Doppler anisotropy depends on the reionization duration. Therefore, the critical value of N_{100} , where the 21-cm autocorrelation-term (C_{ℓ}^{21}) dominates the 21-cm experimental noise (N_{ℓ}^{21}), depends as well on the reionization duration. The critical value for $\Delta z = 0.01$ is $N_{100} \sim 1.0$ and that for $\Delta z = 1.0$ is $N_{100} \sim 0.1$. Since the 21-cm cross-correlation with the CMB Doppler anisotropy has a sufficiently high amplitude and a peak at large scales, it can be detected by present or planned experiments (Fig. 6, left-hand panel). For the 21-cm cross-correlation with the CMB *E*-mode polarization, although the long duration of reionization damps the power at high ℓ s, the noise which dominates the cross-correlation signal at these scales makes it difficult to probe the duration. Therefore, the difference due to the duration does not prominently appear in the right-hand panel of Fig. 6. The critical value of N_{100} is same for different reionization durations (the critical value is $N_{100} \sim 1.0$). Regardless of the duration of reionization, the signal of the cross-correlation can be detected with an S/N larger than 10.

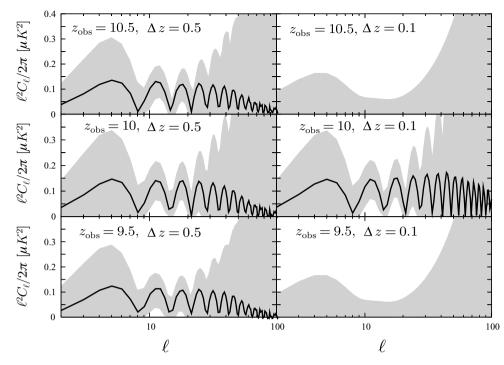


Figure 5. The 21-cm and *E*-mode cross-correlation signal with the estimated errors, for SKA, at different observing redshifts. We set $z_{re} = 10$ and f = 0 with $\Delta z = 0.5$ and 0.1 in the left- and right-hand panels, respectively. From top to bottom, we set $z_{obs} = 10.5$, 10 and 9.5. The cross-correlation signal is shown as the solid line and the errors are represented as the grey zone in each panel.

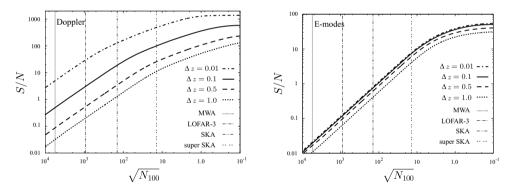


Figure 6. The S/N as a function of N_{100} for the ideal full sky survey. We set $z_{re} = 10$, f = 0 and $z_{obs} = 10$. The dashed–dotted, solid, dashed and dotted lines are for $\Delta z = 0.01$, 0.1, 0.5 and 1, respectively. The vertical lines represent the normalized noise power spectra for each observation. The left-hand panel shows the S/N for the 21-cm cross-correlation with the CMB Doppler anisotropy, and the right-hand panel is for the 21-cm cross-correlation with *E*-mode polarization.

6 CONCLUSION

We have investigated the detection level of the cross-correlation between 21-cm fluctuations and large scale CMB anisotropy from the EoR. We have evaluated the S/N for the 21-cm cross-correlation with both the Doppler temperature anisotropy and the *E*-mode polarization. During the EoR, CMB anisotropies are also produced by patchy reionization and Ostriker–Vishniac effect. These anisotropies also cross-correlate with 21-cm fluctuations, on small scales (Cooray 2004; Salvaterra et al. 2005; Slosar et al. 2007; Jelic et al. 2009). However, on such scales, the CMB anisotropy is contaminated by other secondary effects from galaxy clusters, e.g. Sunyaev–Zeld'vich effect, which has a cross-correlation with 21-cm fluctuations (Slosar et al. 2007). The detection of the cross-correlation signal from EoR at small scales is beyond the scope of the present study. We will address this issue in a forthcoming paper.

For the cross-correlation between the 21-cm fluctuations and the CMB Doppler anisotropy produced during the EoR, the amplitude of the spectrum depends on the reionization duration. Short durations imply high amplitude of the cross-correlation, and consequently large S/N. The cross-correlation between *Planck* and LOFAR, in its present configuration, is sensitive to an 'instantaneous' reionization (with $\Delta z = 0.01$) only. If the instrumental noise of LOFAR were reduced by a factor of 10, LOFAR could detect the cross-correlation signal from the instantaneous reionization with S/N ~ 3 for single observation field and S/N ~ 5 for multi observation field. Moreover, an ideal experiment with a sensitivity 10 times better and a field of view twice as big as that of SKA can detect the signal from the reionization with $\Delta z = 0.5$.

For the cross-correlation between the 21-cm fluctuations and the CMB *E*-mode polarization, the angular power spectrum is damped on small scales by the reionization duration. On those scales, the noise from the primordial CMB polarization dominates the cross-correlation signal and makes the measurement of the cross-correlation insensitive to the reionization duration. However, instead of the measurement of the damping, the signal detection over several frequencies by an ideal experiment 10 times more sensitive than SKA may give constraints on the reionization duration.

ACKNOWLEDGMENTS

HT is supported by the Belgian Federal Office for Scientific, Technical and Cultural Affairs through the Interuniversity Attraction Pole P6/11.

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