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# Detection of Effective Porosity and Permeability Zoning in an Iranian Oil **Field Using Fractal Modeling**

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# ABSTRACT

Identification and delineation of different zones in oil fields are among the fundamental tasks in petroleum explorations. Fractal methods are useful tools for such purposes. The aim of this paper is to conduct a comparative study of Concentration-Area (C-A) and Number-Size (N-S) fractal models to separate effective porous and permeable zones based on core logging samples collected from one of the oilfields in southern Iran. However, permeability and porosity threshold values were calculated based on the C-A and N-S log-log plots. A comparison between the C-A and N-S fractal results showed that the C-A method is more compatible with reality, and it is capable of separating permeable and porous zones in this oilfield.

Keywords : Concentration-area (C-A); Effective porosity; Number-size (N-S); Permeability; Southern Iran

## 1. Introduction

Several studies have tried to estimate petroleum reservoir properties, such as permeability and porosity, based on well logging, seismic, or production data [1-3]. The purpose of petrophysical studies is to determine the zoning in a reservoir formation. Porosity, water and hydrocarbon saturations, and permeability are important parameters which should be examined in petrophysical assessments to understand the quality of the reservoir [2-3]. Different methods have been proposed for the interpretation and determination of these parameters, specifically effective porosity and permeability. These methods include Resevoir Quality Index (RQI) and Flow Zone Index (FZI) [2-4]. The modeling of permeability and effective porosity is important for improving the production of an oilfield. Furthermore, these parameters are important in reservoir modeling and simulation, as they influence the rate of hydrocarbon production, ultimate recovery, optimal placement of wells, pressure, and fluid contact evaluation [3-6]. Thus, proper determination of permeability and effective porosity is of paramount importance since they affect the economy of the whole venture of development and operation of an oilfield.

Detection of different zones for effective porosity and permeability in a studied oilfield is an important aim for petroleum exploration. Several methods have been proposed to explain it properly. Moving averages and probability plots are among the most traditional and easy ways to use statistical methods for characterizing the effective porosity and permeability zoning in a petroleum reservoir [5]. Statistical methods are only applicable to cases where exploratory data follow a normal or lognormal distribution, and they define thresholds as the sum of the mean and standard deviations. However, the normal distribution does not provide the only possible model of data distribution. Therefore, traditional methods based on classical statistics may fail to recognize the zones in a studied area [5-6].

These limitations can be solved using fractal and multifractal modelings. Fractal geometry is an important non-linear mathematical technique that was first introduced by Mandelbrot (1983) and has been applied in different fields of geosciences since the 1980s [7-14]. One of the main applications of fractal geometry is calculating the threshold and separating different zones (porous and permeable zones in this scenario) based on the difference between their fractal dimensions [15-18]. Additionally, several fractal methods have been developed and applied in geochemical explorations, such as Number-Size (N-S) by Mandelbrot (1983), Concentration-Area (C-A) by Cheng et al. (1994), Concentration-Distance (C-D) by Li et al. (2003), and Concentration-Volume (C-V) by Afzal et al. (2011). The detection and description of zone properties, including effective porosity and permeability, can be conducted using fractal methods. Fractal models have already been used to investigate either the permeability or porosity of oil shale samples [19-24]. Fractals are considered by a scaling law, which relates two variables: the scale factor and the object being measured. This scaling relationship is described by a power-law function that, in turn, explains the inherent physical characteristics of the object being analyzed, such as porosity and permeability [16, 25-27]. Different geological processes can be explained based on variations in fractal dimensions obtained from the analysis of relevant data. On the other hand, regionalized variables, such as porosity and permeability, can be interpreted by fractal geometry based on self-similarity and data complexity [25, 28-29]. According to the limited size of the dataset and the close extension of the study area, the N-S and C-A methods are suitable for the current research. In this study, the N-S and C-A fractal models were applied for the separation of porous and permeable zones in an oil reservoir of southern Iran.

### 2. Methodology

#### 2.1. Number-size (N-S) fractal model

The N-S model, originally established by Mandelbrot (1983), can be utilized to describe the distribution of geochemical populations without pre-processing the data. The N-S method was developed by Agterberg

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(1995), Zuo et al. (2009), Deng et al. (2010), Hassanpour and Afzal (2013), and Afzal et al. (2016). This model shows that there is a relationship between desirable attributes and their cumulative number of samples. The model is expressed by the following equation [25]:

 $N(\geq \rho)=F\rho^{-D}$ 

Where,  $\rho$  represents regionalized variables (such as porosity and permeability),  $N(\geq \rho)$  denotes the cumulative number of samples with concentration values greater than or equal to  $\rho$ , F is a capacity constant, and D shows the scaling exponent or the fractal dimension of the distribution of the studied regionalized variable. Fractal dimensions can be positive, negative, complex, or fuzzy values. Based on the multifractal model proposed by Agterberg (1995), a power-law frequency model has been proposed to describe the N-S relationship according to the frequency distribution of element concentrations and the cumulative number of samples with those attributes [11, 14, 29-33].

According to Mandelbrot (1983), plotting the cumulative number against concentration in the log-log coordinates of  $N(\ge \rho)$  versus log  $\rho$ , which represents straight line segments with different slopes -D corresponds to various concentration intervals. This method is suitable for low volume datasets, such as this case study.

#### 2.2. Concentration-area (C-A) fractal model

The C-A model is developed based on the relationship between the obtained results and the exploratory data plus their surface area. Its advantages include easy implementation and the ability to compute quantitative thresholds for different zones [3, 9-10, 32, 34-37]. The C-A method, originally proposed by Cheng et al. (1994), is based on a simple empirical set of equations, which will be shortly presented. The C-A fractal model has the following general form:

 $A(\rho \le \upsilon) \infty \rho^{-\alpha 1}; A(\rho \ge \upsilon) \infty \rho^{-\alpha 2}$ 

Where,  $\rho$  and  $A(\rho)$  reveal the studied attributes such as porosity/permeability and area with concentration values greater than the contour value  $\rho$ , respectively. Also,  $\upsilon$  represents the threshold values for this attribute, and  $-\alpha 1$  and  $-\alpha 2$  are fractal dimensions that are greater than zero [18, 26, 36, 38]. Fractal dimensions are calculated from the slopes of the straight lines in a log-log plot of  $A(\rho)$  versus  $\rho$ .

Cheng et al. (1994) used two methodologies to calculate  $A(\rho)$ , as follows: (1)  $A(\rho)$  is the area enclosed by contour level q on a contour map (e.g., porosity and permeability in this scenario), resulting from the estimation of raw data using a weighted moving average method such as ordinary kriging; and (2)  $A(\rho)$  are the values derived via box-counting

of original values. By box-counting, one superimposes a grid with cells on the studied area. The  $A(\rho)$  of a given q is equal to the number of cells multiplied by the cell area with concentration values greater than  $\rho$ . The average concentration values are utilized for those boxes containing more than one sample. Area-concentration  $[A(\rho)]$  with concentrations greater than  $\rho$  usually represents a power-law relationship [9-10]. The breaks between straight-line segments on this plot and the corresponding values of  $\rho$  have been used as threshold values to discriminate values into different components, showing various factors, especially geological processes [39].

## 3. Results and Discussion

#### 3.1. Dataset

The dataset comprises the physical properties of 364 core logging samples collected from a drilling borehole in an oilfield in southern Iran. The available data were recorded from horizontal and vertical core samples at 20cm intervals, and included effective porosity and permeability from depths 3500 m to 3700 m. The samples were analyzed under ambient, 800 psi, 3000 psi, and 6000 psi pressure circumstances. The N-S and C-A fractal methods were performed to detect porous and permeable zones in the oilfield. The data were gridded and estimated by the Ordinary Kriging (OK) method. The estimated data were used for fractal analysis through the C-A fractal method.

#### 3.2. C-A application

The C-A log-log plots were generated for porosity and permeability at 800 psi, 3000 psi, and 6000 psi (Figs. 1 and 2). Permeability had six populations at ambient, 3000, and 6000 psi, but five populations at 800 psi. There was a multifractal nature for permeability and porosity in this area, based on different log-log plots, as depicted in Figs. 1 and 2. The major permeable zones at ambient, 800, 3000, and 6000 psi commenced from 138, 60.25, 54.95, and 47.86 md, respectively. These zones with high permeability values are located in the NE and SW parts of the area, as depicted in Figs. 3 and 4. Porosity populations were delineated based on the C-A log-log plots (Fig. 2), with the main porous zones beginning from 13-14%. There are seven populations for porosity ambient and six populations for others, as depicted in Fig. 2. Based on the fractal modeling, porous zones are situated in the SW and NE parts of the studied region, as displayed in Figs. 5 and 6. The threshold values for permeability and porosity are indicated in Table 1.



Fig. 1. The permeability log-log plots based on the C-A fractal model of the estimated data: (a) permeability at ambient; (b) permeability at 800 psi; (c) permeability at 3000 psi; and (d) permeability at 6000 psi.



Fig. 2. The porosity log-log plots based on the C-A fractal model of the estimated data: (a) porosity at ambient; (b) porosity at 800 psi; (c) porosity at 3000 psi; and (d) porosity at 6000 psi.



Fig. 3. Permeable zones distribution maps based on the C-A fractal method: (a) permeability at ambient; (b) permeability at 800 psi.



**Fig. 4.** Permeable zones distribution maps based on the C-A fractal method: (a) permeability at 3000 psi; (b) permeability at 6000 psi.





Fig. 5. Porous zones distribution maps based on the C-A fractal method: (a) porosity at ambient; (b) porosity at 800 psi.





Fig. 6. Porous zones distribution maps based on the C-A fractal method: (a) porosity at 3000 psi; (b) porosity at 6000 psi.

Table 1	. Thres	hold	valı	ues of	permea	ble	e and	porous	s zone	s in	the	studied	area
	d	efine	ed fi	rom tl	ne C-A fi	rac	tal n	nodel (l	Figs. 1	and	2).		

Qualification	Permeable & porous zones	Permeability range (md)	Porosity range (%)
	Background	<56.23	<5.48
	Weakly	56.23-100	5.48-7.28
Ambient	Moderately	100-138.04	7.28-8.69
	Highly	138.04-151.36	8.69-10.96
	Extremely	151.36-229.09	10.96-14.45
	Background	<18.62	<6.76
	Weakly	18.62-43.65	6.76-9.55
800 psi	Moderately	43.65-60.25	9.55-11.25
	Highly	60.25-173.78	11.25-13.8
	Extremely	173.78-241.5	13.8-16.6
	Background	<10.23	<6.61
	Weakly	10.23-19.5	6.61-8.34
3000 psi	Moderately	19.5-42.66	8.34-10.72
	Highly	42.66-54.95	10.72-13.12
	Extremely	54.95-162.18	13.12-16.22
	Background	<12.3	<6.17
	Weakly	12.3-27.54	6.17-8.36
6000 psi	Moderately	27.54-40.74	8.36-13.18
	Highly	40.74-47.86	13.18-14.13
	Extremely	47.86-158.49	14.13-15.49

#### 3.3. N-S implementation

The N-S method was conducted on the pre-treatment data without any estimations. The log-log plots of porosity and permeability were established under various conditions at 800 psi, 3000 psi, 6000 psi, and ambient (Figs. 7 and 8). Accordingly, the obtained results indicate that permeability at 800 psi, 3000 psi, and 6000 psi has five populations, but seven populations under an ambient condition. The highly permeable zones from the N-S fractal at ambient, 800 psi, 3000 psi, and 6000 psi began from 199.53, 158.49, and 100 md, respectively. As revealed in Figs. 9 and 10, these permeable zones with high values at 800 psi, 3000 psi, and 6000 psi are located in the NE, while under the ambient condition, they exist in the SW parts of the area. Based on the porosity log-log plots derived from the N-S fractal method, six populations under the ambient condition, five populations at 800 psi and 3000 psi, and four populations at 6000 psi were identified. Also, the obtained results suggest that the highly porous zones from the N-S method are located in the SW and NE of the area (Figs. 11 and 12). The high values of the porous zones from the N-S fractal started from 15-16%. Finally, the threshold values of porosity and permeability are provided in Table 2.





Fig. 7. The permeability log-log plots based on the N-S fractal model of data: (a) permeability at ambient; (b) permeability at 800 psi; (c) permeability at 3000 psi; and (d) permeability at 6000 psi.



Fig. 8. The porosity log-log plots based on the N-S fractal model of data: (a) porosity at ambient; (b) porosity at 800 psi; (c) porosity at 3000 psi; and (d) porosity at 6000 psi.





Fig. 9. Permeable zones distribution maps based on the N-S fractal method: (a) permeability at ambient; (b) permeability at 800 psi.



Fig. 10. Permeable zones distribution maps based on the N-S fractal method: (a) permeability at 3000 psi; (b) permeability at 6000 psi.



Fig. 11. Porous zones distribution maps based on the N-S fractal method: (a) porosity at ambient; (b) porosity at 800 psi.



Fig. 12. Porous zones distribution maps based on the N-S fractal method: (a) porosity at 3000 psi; (b) porosity at 6000 psi.

Table 2.	Threshold values of	the permeable	and porous	zones in the	studied area
	defined from	the N-S fractal	model (Figs	s 7 and 8)	

Qualification	Permeable & porous zones	Permeability range (md)	Porosity range (%)
	Background	<4.77	<4.68
	Weakly	4.77-15.14	4.68-10
Ambient	Moderately	15.14-64.56	10-13.18
	Extremely	64.56-199.53 199.53-794.33	13.18-16.6 16.6-20.89
	Background	<0.16	<4.79
	Weakly	0.16-6.17	4.79-8.91
800 psi	Moderately	6.17-25.12	8.91-15.85
	Extremely	25.12-158.49 158.49-389.04	15.85-19.95 19.95-31.5
	Background	<0.23	<4.9
	Weakly	0.23-3.98	4.9-11.22
3000 psi	Moderately	3.98-18.62	11.22-16.22
	Extremely	Permeability range (md)         Porosity r (%)           <4.77	16.22-20.42 20.42-31.1
	Background	<0.5	<6.31
	Weakly	0.5-2.69	6.31-15.85
6000 psi	Moderately	2.69-19.95	15.85-22.39
	Extremely	19.95-100	22.39-30.8

#### 3.4. Correlation between fractal results and actual values

Carranza (2011) presented an analytical technique for the calculation of overlaps or spatial correlation between two binary models. Therefore, according to the overlaps between the numbers of cells in the fractal model and the cells existing in the conventional model (e.g., geological, actual, or standard models), a log-ratio matrix was established as Table 3.

**Table 3.** The log-ratio matrix to compare the performance of fractal modeling results with the conventional model (reality). A, B, C, and D represent the number of voxels in overlaps between classes in the binary geological model and the binary results of fractal models [40]

	the billary	results of fractal filodels	[40].			
	Conventional model (Reality)					
		Inside zone	Outside zone			
Fractal model	Inside zone	True positive (A)	False positive (B)			
	Outside zone	False negative (C)	True negative (D)			
		Overall accuracy (OA	A = (A+D)/(A+B+C+D)			

Where, (A) denotes the number of voxels that exist either in the fractal model or the conventional model; (B) represents the number of voxels in the fractal model but not available in the geological model; (C)

is the number of voxels embedded in the conventional model but not found in the fractal model; (D) is the number of voxels existing neither in the fractal nor in the conventional model; and (OA) is the main criterion for the evaluation of coincidence between the fractal results and the actual values. An intersection operation between a fractal zone model (porosity and permeability, in this scenario) and different zones in the conventional model was performed to obtain the number of cells corresponding to each of the four classes of overlapping zones, as shown in Table 5. In this study, porous and permeable zones were compared with standard zones presented by Tiab and Donaldson (2004) [41].

# 3.5. Comparison between permeability fractal results and actual results

A comparison between N-S and C-A permeability fractal results was performed using the log-ratio matrix. A standard range of permeability (50-150 md) was chosen for the conventional model [41]. Further, permeability fractal ranges in different conditions were selected considering their threshold values. As depicted in Tables 4-7, it can be concluded that the C-A fractal method has greater accuracy and is closer to reality. The OAs obtained by the C-A are higher than those by the N-S modeling for different ranges. The OAs resulting from the C-A model are higher than 96% in various zones, but these values for the N-S method are between 90%-95%, as depicted in Tables 4-7. The difference between C-A and N-S modeling is near to 10% and 7% for permeability at 3000 psi and 6000 psi, respectively (Tables 6-7).

Table 4. Comparison between the results de	rived from the N-S and C-A fractal
models (permeability <b>under</b> th	e ambient condition).

(P				).	
		Stand	ard (50-15	0 md)	
		Inside	zone	Outsi	de zone
N-S fractal I	nside zone	Α	14	В	7
Permeability ambient	Outside zone	С	3	D	136
(64.56-199.52 md)		OA			0.9375
		Stand	lard (50-1	50 md)	
		Inside	e zone	Outsi	de zone
C-A fractal I	nside zone	А	21	В	0
Permeability ambient	Outside zone	С	59	D	1765
(100-138.04 md)		OA		0.	968022

 Table 5. Comparison between the results derived from the N-S and C-A fractal models (permeability at 800 psi)

models (permeabili	<i>cy</i> at 00.	- F /.		
	Stand	lard (50-15	50 md)	
	Insid	e zone	Outsi	de zone
N-S fractal Inside zone	Α	15	В	11
Permeability ambient Outside zone	С	0	D	236
(64.56-199.52 md)	OA		(	).958015
	Stan	dard (50-1	50 md)	
	Stan Insid	dard (50-1 le zone	50 md) Outsie	de zone
C-A fractal Inside zone	Stan Insic A	<b>dard (50-1</b> le zone 17	50 md) Outsie B	de zone
C-A fractal Inside zone Permeability ambient Outside zone	Stan Insic A C	<b>dard (50-1</b> le zone 17 8	50 md) Outsie B D	<b>de zone</b> 0 1820
C-A fractal Inside zone Permeability ambient Outside zone (100-138.04 md)	Stan Insic A C OA	<b>dard (50-1</b> le zone 17 8	50 md) Outsid B D	<b>de zone</b> 0 1820 995664



 Table 6. Comparison between the results derived from the N-S and C-A fractal models (permeability at 3000 psi).

	Stand	lard (50-15	60 md)	
	Insid	e zone	Outsie	le zone
N-S fractal Inside zo	one A	8	В	16
Permeability ambient Outsid	e zone C	9	D	229
(64.56-199.52 md)	OA		(	).90458
	Stan	dard (50-1	50 md)	
	Stan Insid	dard (50-1) le zone	50 md) Outsid	le zone
C-A fractal Inside z	Stan Insic	<b>dard (50-1</b> ) le zone 18	50 md) Outsic B	<b>le zone</b> 0
C-A fractal Inside z Permeability ambient Outsi	Stan Insic one A ide zone C	<b>dard (50-1</b> ) le zone 18 5	50 md) Outsio B D	<b>le zone</b> 0 1822

 Table 7. Comparison between the results derived from the N-S and C-A fractal models (permeability at 6000 psi).

		Stand	ard (50-15	60 md)	
		Inside	zone	Outsic	le zone
N-S fractal Ir	iside zone	Α	9	В	10
Permeability ambient	Outside zone	С	8	D	236
(64.56-199.52 md)		OA		(	).931559
		Stand	lard (50-1	50 md)	
		Insid	e zone	Outsie	le zone
C-A fractal II	nside zone	Α	21	В	2
Permeability ambient	Outside zone	С	0	D	1822
(100 128 0/ md)		01		0	00201/

#### 3.6. Comparison between porosity fractal results and actual values

The N-S and C-A fractal results for porosity zones were evaluated using the log-ratio matrix, with its conclusions exhibited in Tables 8-11. In this comparison, a range of 10-15% was assumed for the standard porosity range [41]. Porosity fractal ranges were selected based on their threshold values derived from the N-S and C-A fractal models. According to the obtained results, under the conditions of ambient, 800 psi, 3000 psi, and 6000 psi, the C-A fractal method presented a more accurate response than the N-S fractal method. The OAs derived via the C-A were higher than those found by the N-S modeling for different ranges. The OAs resulting from the C-A model were equal to 98% in different zones, but these values for the N-S model lay within the range 76%-92%, as reported in Tables 8-11. The difference between C-A and N-S modelings is 21% for 6000 psi (Tables 11). In addition, the difference for 800 psi and 3000 psi s6% and 8%, respectively (Tables 9-10).

 Table 8. Comparison between the results derived from the N-S and C-A fractal models (porosity under the ambient condition).

		Stand	ard (10 – 1	5%)	
		Inside	e zone	Outsid	e zone
N-S fractal	Inside zone	А	20	В	0
Permeability ambie	ent Outside zone	С	5	D	127
(64.56-199.52 md)		OA		0	.967105
		Stand	lard (10 –	15%)	
		Stand Insid	lard (10 – e zone	15%) Outsid	e zone
C-A fractal	Inside zone	Stand Insid	<b>lard (10 –</b> e zone 25	15%) Outsid B	le zone
C-A fractal Permeability ambie	Inside zone ent Outside zone	Stand Insid A C	<b>lard (10 –</b> e zone 25 38	<b>15%)</b> Outsid B D	e zone 0 1782

 Table 9. Comparison between the results derived from the N-S and C-A fractal models (porosity at 800 psi).

	Stand	lard (10 – 1	5%)	
	Inside	e zone	Outsic	le zone
N-S fractal Inside zone	Α	42	В	19
Permeability ambient Outside zone	С	0	D	195
(64.56-199.52 md)	OA		0	.925781
	Stan	<b>dard (10</b> – 1	15%)	
	Insid	le zone	Outsic	le zone
C-A fractal Inside zone	Α	40	В	0
C-A fractal Inside zone Permeability ambient Outside zone	A C	40 39	B D	0 1766

 Table 10. Comparison between the results derived from the N-S and C-A fractal models (porosity at 3000 psi).

	Standard (10 - 15%)				
	Insid	Inside zone		Outside zone	
N-S fractal Inside zone	Α	23	В	9	
Permeability ambient Outside zone	С	15	D	198	
(64.56-199.52 md)	OA		0.902041		
	Standard (10 – 15%)				
	Stan	dard (10 –	15%)		
	Stan Insic	dard (10 – le zone	15%) Outsid	le zone	
C-A fractal Inside zone	Stan Insic A	<b>dard (10 –</b> le zone 39	<b>15%)</b> Outsid B	le zone	
C-A fractal Inside zone Permeability ambient Outside zone	Stan Insic A C	dard (10 – le zone 39 28	<b>15%)</b> Outsid B D	le zone 0 1778	

 
 Table 11. Comparison between the results derived from the N-S and C-A fractal models (porosity at 6000 psi).

	Standard (10 – 15%)				
	Inside zone		Outside zone		
N-S fractal Inside zone	Α	36	В	56	
Permeability ambient Outside zone	С	0	D	146	
(64.56-199.52 md)	OA			0.764706	
	Standard (10 – 15%)				
	Inside zone Outside zon			a	
	Insid	e zone	Outsi	ae zone	
C-A fractal Inside zone	A	e zone 7	B	0	
C-A fractal Inside zone Permeability ambient Outside zone	A C	7 50	B D	0 1788	

# 4. Conclusion

This study was conducted on a drilling borehole of an oilfield from the south of Iran. It presented the specific use of N-S and C-A fractal methods for the separation of permeable and porous zones as a useful tool for petro-physical exploration. The advantages of these methods include simplicity and straightforward computational implementations. Both of the N-S and C-A fractal models revealed the highly porous and permeable zones. The results obtained by fractal modeling suggested that the main zones for petroleum extraction occur in the SW and NE parts of the area. The threshold values for highly permeable zones at ambient, 800 psi, 3000 psi, and 6000 psi began from 138, 60.25, 54.95, and 47.86 md based on the C-A fractal model, respectively. Also, the major permeable zones derived from the N-S fractal method at ambient, 800, 3000, and 6000 psi started from 199.53, 158.49, and 100 md in order and priority. According to the obtained porosity log-log plots, the threshold values for the major porous zones began from 14.5% as the average value for both of the C-A and N-S fractal models. A comparison between the C-A and N-S fractal results revealed that under various conditions of ambient, 800, 3000, and 6000 psi, the C-A fractal method outperforms the N-S fractal method. Consequently, the permeability and porosity results derived from the C-A fractal model has a better equivalence with the reality; therefore, it is more capable of separating the porous and permeable zones in petroleum extractions

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