Determination of the Charged Pion Form Factor at $Q^2=1.60$ and 2.45 (GeV/c)²

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The ¹H(e, $e'\pi^+$)n cross section was measured at four-momentum transfers of $Q^2 = 1.60$ and 2.45 GeV^2 at an invariant mass of the photon nucleon system of W=2.22 GeV. The charged pion form factor (F_{π}) was extracted from the data by comparing the separated longitudinal pion electroproduction cross section to a Regge model prediction in which F_{π} is a free parameter. The results indicate that the pion form factor deviates from the charge-radius constrained monopole form at these values of Q^2 by one sigma, but is still far from its perturbative Quantum Chromo-Dynamics prediction.

A fundamental challenge in nuclear physics is the description of hadrons in terms of the constituents of the underlying theory of strong interactions, quarks and gluons. Properties such as the total charge and magnetic moments are well described in a constituent quark framework, which effectively takes into account quark-gluon interactions. However, charge and current distributions, which are more sensitive to the underlying dynamic processes, are not well described.

Hadronic form factors provide important information about hadronic structure. The coupling of a virtual photon to structureless particles is completely determined by their charge and magnetic moments. However, for composite particles one must account for the internal structure, which is accomplished by momentum transfer dependent functions. Examples of these functions are the electromagnetic form factors, which describe the distribution of charge and current.

One of the simplest hadronic systems available for study is the pion, whose valence structure is a bound state of a quark and an antiquark. The electromagnetic structure of a spinless particle such as the pion is parameterized by a single form factor. The pion charge form factor, F_{π} , can be calculated in perturbative Quantum Chromo-Dynamics (pQCD) in the limit of very large values of four-momentum transfer squared, Q^2 [1]:

$$F_{\pi}\left(Q^{2}\right) = 8\pi \; \frac{\alpha_{s} \; f_{\pi}^{2}}{Q^{2}} \quad (Q^{2} \to \infty), \tag{1}$$

where α_s is the strong coupling constant. The normalization is fixed by the pion decay constant, f_{π} , which is determined from the weak decay of the pion $(\pi \rightarrow \mu + \nu_{\mu})$. At low values of Q^2 , Vector Meson Dominance models provide a reasonable description of F_{π} . Due to the pion's simple $\bar{q}q$ valence structure, the transition from "soft" (nonperturbative) to "hard" (perturbative) physics is expected to occur at significantly lower values of Q^2 for F_{π} than for the nucleon form factors [2].

The form factor of the pion is well determined up to $Q^2 = 0.28 \text{ GeV}^2$ by elastic $\pi - e$ scattering experiments [3], from which the charge radius has been extracted. Extending the measurement of F_{π} to larger values of Q^2 requires the use of pion electroproduction from a nucleon target. The pion exchange (t-pole) process, in which a virtual photon couples to a virtual pion inside the nucleon, dominates the longitudinal pion electroproduction cross section, σ_L , at small values of the Mandelstam variable t. There σ_L exhibits a characteristic t-dependence and is proportional to F_{π}^2 .

Experimental values of F_{π} have previously been determined at CEA and Cornell [4, 5], DESY [6, 7], and recently at Jefferson Lab [8]. Most of the high Q^2 data have come from experiments at Cornell covering a range of values in Q^2 between 0.28 and 9.77 GeV². In these experiments F_{π} was extracted from the longitudinal cross sections, which were isolated by subtracting a model of the transverse contribution from the unseparated cross sections. Pion electroproduction data were also obtained at DESY for a value of Q^2 of 0.7 GeV², at an invariant mass of the photon nucleon system of W=2.19 GeV, and longitudinal and transverse cross sections were extracted using the Rosenbluth separation method. In 1997, Jefferson Lab provided the first high precision pion electroproduction data for F_{π} for values of Q^2 between $Q^2=0.6$ and 1.6 GeV² at W=1.95 GeV [8]. For an updated analysis of these data see reference [9]. These data give a precise determination of σ_L with a significant improvement in the experimental uncertainty. The results presented here extend the Q^2 range to 2.45 GeV² and address questions of model dependence in the extraction of F_{π} .

The experiment described here was carried out in Hall C at Thomas Jefferson National Accelerator Facility (Jefferson Lab). Pion electroproduction cross sections were measured from hydrogen and deuterium targets. The data were taken at two beam energies for each of the two values of Q^2 at W=2.22 GeV. Charged pions were detected in the High Momentum Spectrometer (HMS), while the scattered electrons were detected in the Short Orbit Spectrometer (SOS). Both spectrometers include two drift chambers for track reconstruction and scintillator arrays for triggering. A detailed description of the Jefferson Lab Hall C spectrometers can be found in reference [10].

In order to select electrons in the SOS, a gas Čerenkov detector containing Freon-12 at atmospheric pressure was used in combination with a lead-glass calorimeter. Positively charged pions were identified in the HMS using an aerogel Čerenkov detector with refractive index of 1.03 [11]. In the case of pion production at negative polarity, electrons were rejected using a gas Čerenkov detector containing C_4F_{10} at 0.47 atm. Any remaining contamination from real electron-proton coincidences was eliminated with a coincidence time cut of ±1 ns. Background from alumininum target cell walls (2-4% of the yield) and random coincidences (~1%) were subtracted from the charge normalized yields. The exclusive neutron fi-



FIG. 1: Representative example of the measured cross sections, $\frac{d^2\sigma}{dtd\phi}$ as a function of ϕ at $Q^2 = 1.6 \ GeV^2$ for two values of ϵ . The curves shown represent the model cross section used in the Monte Carlo simulation.

nal state was selected with a cut on the reconstructed missing mass. The relevant electroproduction kinematic variables Q^2 , W and t were reconstructed from the measured spectrometer quantities. Experimental yields were calculated after correcting for several inefficiencies, the dominant sources being particle tracking efficiency (3-4%), pion absorption (4.8%), and computer dead time (1-11%). The net uncertainty in these corrections is dominated by the uncertainty in the absorption of the pions (~2%).

The unpolarized pion electroproduction cross section can be written as the product of a virtual photon flux factor and a virtual photon cross section,

$$\frac{d^5\sigma}{d\Omega_e dE'_e d\Omega_\pi} = J\left(t, \phi \to \Omega_\pi\right) \Gamma_v \frac{d^2\sigma}{dt d\phi},\tag{2}$$

where $J(t, \phi \to \Omega_{\pi})$ is the Jacobian of the transformation from $dtd\phi$ to $d\Omega_{\pi}$, ϕ is the azimuthal angle between the scattering and the reaction plane, and $\Gamma_v = \frac{\alpha}{2\pi^2} \frac{E'_e}{E_e} \frac{1}{Q^2} \frac{1}{1-\epsilon} \frac{W^2 - M^2}{2M}$ is the virtual photon flux factor. The virtual photon cross section can be expressed in terms of contributions from transversely and longitudinally polarized photons,

$$2\pi \frac{d^2 \sigma}{dt d\phi} = \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \sqrt{2\epsilon(1+\epsilon)} \frac{d\sigma_{LT}}{dt} \cos\phi (3) + \epsilon \frac{d\sigma_{TT}}{dt} \cos2\phi.$$

Here, $\epsilon = \left(1 + 2\frac{|\mathbf{q}^2|}{Q^2}\tan^2\frac{\theta}{2}\right)^{-1}$ is the virtual photon polarization, where \mathbf{q}^2 is the square of the three-momentum transferred to the nucleon and θ is the electron scattering angle. The individual components in equation 3 were

determined from a simultaneous fit to the ϕ dependence of the measured cross sections, $\frac{d^2\sigma}{dtd\phi}$, at two values of ϵ . A representative example as a function of ϕ is shown in Figure 1.

The separated cross sections are determined at fixed values of W, Q^2 and t, common for both high and low values of ϵ . However, the acceptance covers a range in these quantities, thus the measured yields represent an average over that range. Note that each t-bin has a different average value of Q^2 , W. In order to minimize errors resulting from averaging, the experimental cross sections were calculated by comparing the experimental yields to a Monte Carlo simulation of the experiment. To account for variations of the cross section across the acceptance the simulation uses a ${}^{1}\text{H}(e,e'\pi^{+})n$ model based on pion electroproduction data. In addition, the Monte Carlo includes a detailed description of the spectrometers, multiple scattering, ionization energy loss, pion decay, and radiative processes. The separated cross sections, σ_L and σ_T , are shown in Figure 2.

The uncertainty in the separated cross sections has both statistical and systematic sources. The statistical uncertainty in $\sigma_T + \epsilon \sigma_L$ ranges between 1 and 2%. Systematic uncertainties that are uncorrelated between high and low ϵ points are amplified by a factor of $1/\Delta\epsilon$ in the L-T separation. Correlated systematic uncertainties propagate directly into the separated cross sections. Uncertainties in the scattering kinematics and beam energy were parameterized using data from the over-constrained ¹H(e, e'p) reaction. Beam energy and spectrometer momenta were determined to 0.1% while the spectrometer angles were determined to ≈ 0.5 mrad. The spectrometer acceptance was verified to better than 2% by comparing e - p elastic scattering data to a global parameterization [12]. The uncorrelated systematic uncertainty is dominated by acceptance (0.6-1.1%) resulting in a total uncorrelated uncertainty of 0.9 to 1.2%. The correlated systematic uncertainty is mainly due to radiative corrections (2%), pion absorption (2%), and pion decay (1%)resulting in a total correlated uncertainty of 3.5%. A third category of systematic uncertainties consists of uncertainties that differ in size between ϵ points, but may influence the t-dependence at a fixed value of ϵ in a correlated way. The "t-correlated" uncertainty is dominated by acceptance (0.6%), kinematics (0.8-1.1%) and model dependence (1.1-1.3%) resulting in a partially correlated uncertainty of 1.8 and 1.9%.

In order to determine F_{π} , the experimental results for σ_L are compared to a Regge model calculation by Vanderhaeghen, Guidal and Laget (VGL) [13]. In this approach, pion electroproduction is described as the exchange of Regge trajectories for π - and ρ -like particles. Since most model parameters are fixed by pion photoproduction data, F_{π} and the $\pi \rho \gamma$ transition form factor are the only free parameters. Both form factors are parameterized by a monopole form, $[1+Q^2/\Lambda_i^2]^{-1}$, but the cutoff



FIG. 2: Separated cross sections, σ_L and σ_T at central values of $Q^2 = 1.60$ (2.45) GeV². Note that the average values of W and Q^2 are different for each -t-bin. The error bar indicates statistical and uncorrelated systematic uncertainty in both ϵ and -t combined in quadrature. The error band denote the correlated part of the systematic uncertainty by which all data points move collectively. The curves denote VGL Regge calculations for σ_L (solid line) and σ_T (dashed line) with values of $\Lambda_{\pi}^2 = 0.513$ (0.491) GeV² and $\Lambda_{\rho}^2 = 1.1$ GeV². The discontinuities in the σ_L curve result from the different average values of W and Q^2 for the various t-bins.

$Q^2 (\text{GeV}^2)$	F_{π}
1.60	$0.243 {\pm} 0.012$
2.45	$0.167 {\pm} 0.010$

TABLE I: Extracted values for F_{π} at a value of W=2.22GeV. The error on F_{π} combines statistical and experimental systematic uncertainties in quadrature.

parameter, Λ_{ρ}^2 , is not as well constrained as the pion cutoff parameter, Λ_{π}^2 . Varying Λ_{ρ}^2 between 0.6 and 2.1 GeV² changes σ_T by 13% (30%) at Q^2 of 1.60 (2.45), but has little influence on σ_L . Thus, F_{π} can be determined in a one parameter fit from a comparison of the longitudinal experimental cross section to the one predicted from the Regge model.

A comparison of our data to the VGL prediction is shown in Figure 2. The *t*-dependence of the longitudinal cross section is well described at both central values of Q^2 . However, the transverse cross section is underpredicted systematically. The value of F_{π} was determined from a least squares fit of the Regge model prediction to the data, and the resulting values are shown in Table I.

The extraction of F_{π} from σ_L relies on the dominance of the pion exchange term. To test the pole dom-



FIG. 3: Pion form factor as extracted in this work. Also shown are $e-\pi$ elastic data from CERN, and earlier pion electroproduction data from DESY and Jefferson Lab. The earlier Jefferson Lab data are taken from reference [9]. The data point at $Q^2 = 1.60 \text{ GeV}^2$ from [9] has been shifted from its central value for visual representation. The curves are from a Dyson-Schwinger equation (solid, [17]), QCD sum rules (dotted, [14]), dispersion relations with QCD constraint (dashed, [15]), and from a pQCD calculation (dashed-dotted, [18]).

inance the longitudinal π^-/π^+ ratios in ²H were examined. Since the pole term is purely isovector this ratio is expected to be close to unity and a significant deviation from unity would indicate the presence of an isoscalar background. The preliminary analysis of the longitudinal π^-/π^+ ratios is consistent with unity.

In Figure 3, our results are shown along with results from CERN, DESY, earlier Jefferson Lab data, and some representative calculations. Comparing the result at $Q^2 = 1.60 \text{ GeV}^2$ to the earlier Jefferson Lab data point at a lower value of W allows for a direct test of the theoretical model dependence. A higher value of W allows for a measurement at smaller values of -t, at closer proximity to the pion pole. The data are consistent with the previous Jefferson Lab F_{π} measurement at a value of $Q^2 = 1.60 \text{ GeV}^2$ and suggest a small model uncertainty due to fitting the VGL model to the data. The data indicate a one sigma deviation from a monopole form factor that yields the measured charge radius. That form factor is up to $Q^2 = 2.5 \text{ GeV}^2$ indistinguishable from the solid curve in Figure 3. Various models provide a good description of the measured values for F_{π} up to $Q^2=1.60$ GeV^2 . The data are well described by the calculation of Nesterenko and Radyushkin [14], in which a QCD sum rule framework for the soft contribution to F_{π} as well as an asymptotically dominant hard gluon exchange term is used. The dispersion relation calculation by Geshkenbein [15] also agrees well with the data. The data are also reasonably well described by the Dyson-Schwinger calculation by Maris and Tandy, which is based on the Bethe-Salpeter equation with dressed quark and gluon propagators. All parameters in the latter calculation are determined without the use of F_{π} data [16, 17]. Perturbative QCD calculations of which one is shown in Figure 3 give values of $Q^2 F_{\pi}$ around 0.10 GeV² in the region of our measurements.

In summary, we have measured separated ${}^{1}\text{H}(\text{e},\text{e}'\pi^{+})\text{n}$ cross sections at values of $Q^{2}=1.60$ and 2.45 GeV² at W=2.22 GeV. The charged pion form factor was extracted from the separated longitudinal cross section using a Regge model. The data are consistent with the previous Jefferson Lab result at $Q^{2} = 1.60$ GeV². The data deviate by one sigma from a monopole form factor obeying the measured charge radius, but are still far from the values expected from pQCD calculations.

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