Determination of the size of the dust torus in H0507+164 through optical and infrared monitoring

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ABSTRACT

The time delay between flux variations in different wavelength bands can be used to probe the inner regions of active galactic nuclei (AGN). Here, we present the first measurements of the time delay between optical and near-infrared (NIR) flux variations in H0507+164, a nearby Seyfert 1.5 galaxy at z=0.018. The observations in the optical V-band and NIR J, H and K_s bands carried over 35 epochs during the period October 2016 to April 2017 were used to estimate the inner radius of the dusty torus. From a careful reduction and analysis of the data using cross-correlation techniques, we found delayed responses of the J, H and K_s light curves to the V-band light curve. In the rest frame of the source, the lags between optical and NIR bands are found to be $27.1^{+13.5}_{-12.0}$ days (V vs. J), $30.4^{+13.9}_{-12.0}$ days (V vs. H) and $34.6^{+12.1}_{-9.6}$ days (V vs. K_s). The lags between the optical and different NIR bands are thus consistent with each other. The measured lags indicate that the inner edge of dust torus is located at a distance of 0.029 pc from the central UV/optical AGN continuum. This is larger than the radius of the broad line region of this object determined from spectroscopic monitoring observations thereby supporting the unification model of AGN. The location of H0507+164 in the τ - M_V plane indicates that our results are in excellent agreement with the now known lag-luminosity scaling relationship for dust in AGN.

Key words: galaxies: active - galaxies: Seyfert - (galaxies:) quasars: individual (H0507+164)

1 INTRODUCTION

Active Galactic Nuclei (AGN) are among the most luminous objects in the Universe that produce very high luminosity in a very concentrated volume, powered by the accretion of matter onto super-massive black hole (SMBH) located at the centers of galaxies. According to the unified model of AGN, a dusty torus that surrounds the central SMBH, the accretion disk and the broad line region (BLR) play a key role in the identification of Seyfert galaxies, a category of AGN, into Seyfert 1 and Seyfert 2 galaxies (Antonucci 1993). Evidence

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for their presence is seen in the broad band spectral energy distribution (SED) of AGN, such as the presence of the big blue bump in the optical-UV wavelength region, which is a signature of the accretion disk (Czerny & Elvis 1987; Malkan & Sargent 1982; Shields 1978) and a bump in the IR region (Sanders et al. 1989; Barvainis 1987; Kobayashi et al. 1993) which is a signature of the presence of the dusty torus.

The torus, which obscures the central engine, is the dominant source of IR radiation in most of the AGN. It is not easy to spatially resolve the components of the AGN such as the BLR and torus by any current imaging techniques. The IR radiation of AGN coming from the torus that extends in size from sub-pc to pc size scales (Kishimoto et al. 2011a) could in principle be resolvable using IR interferometric observations. However, such interferometric observations as of today are in a minority (Kishimoto et al. 2011b;

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Burtscher et al. 2013) and limited by the current diameters of optical/IR telescopes. Alternatively, the extent and nature of the torus can be studied via the technique of reverberation mapping (Blandford & McKee 1982). This technique relies on the flux variability of AGN, which has been known since their discovery. The continuum emission from AGN is believed to arise from the accretion disk and it is expected to vary over a range of time scales from hours to days. The variations in the continuum flux are observed at a later time in the fluxes of their broad emission lines. Similarly, there is also delayed response of the IR continuum emission (from the torus) to the changes in the optical continuum from the central AGN, which indicates that the NIR continuum and UV/optical continuum emission are causally connected. This delay between the optical and IR variation when measured can give the radius of the inner most hot dust torus $r_{\text{dust}} =$ $\tau \times c$, where c is the speed of light and τ is the time delay between optical and IR variations. This method of measuring the delayed response of the IR emission relative to the optical emission and consequently determine the size of the torus is referred to as dust reverberation mapping (DRM).

Studies of DRM in few Seyfert galaxies (Minezaki et al. 2004; Suganuma et al. 2006; Koshida et al. 2014) have led to the establishment of a correlation between the inner radius of the dust torus and the UV luminosity as $r_{\rm dust} \propto L^{0.5}$ (Kishimoto et al. 2007). Also, Kishimoto et al. (2007) established a relation between the sublimation radius ($R_{\rm sub}$) which is defined as the radius at which dust particle sublimates and the dust grain size (a) as

$$R_{\rm sub} = 1.3 \left(\frac{L_{UV}}{10^{46} \rm erg s^{-1}} \right)^{0.5} \left(\frac{T_{\rm sub}}{1500 K} \right)^{-2.8} \left(\frac{a}{0.05 \mu \rm m} \right)^{-0.5} \rm pc$$
(1)

Considering sublimation temperature $(T_{\rm sub})$ to be the dust temperature $T_{\rm dust}=1700~{\rm K}$ which was evaluated from the NIR colors of the variable flux component for Seyfert 1 galaxies (Tomita et al. 2006; Koshida et al. 2014) and grain size $a=0.1\mu{\rm m}$, the sublimation radius from equation 1 can be written as $\log R_{\rm sub}/{\rm pc}=-0.80+0.5\log(L_V/10^{44}~{\rm erg~s^{-1}})$, where $L_{UV}=6\,L_V$ (Kishimoto et al. 2007). This is in excellent agreement with the relation of $\log r_{\rm dust}/{\rm pc}=-0.88+0.5\log(L_V/10^{44}~{\rm erg~s^{-1}})$ obtained by a linear regression fit to the reverberation mapping data of a few Seyfert galaxies by Koshida et al. (2014). Thus, DRM observations using the K-band in the infrared region can define the inner radius of the dust torus for an AGN.

The emission line lag (e.g., Watson et al. 2011; Haas et al. 2011; Czerny et al. 2013) and dust reverberation lag (e.g., Oknyanskij et al. 1999; Oknyanskij & Horne 2001; Hönig 2014; Yoshii et al. 2014; Hönig et al. 2017) have been proposed to serve as standard candles. However, the later shows a stronger correlation between lag and luminosity than former and needs only photometric monitoring making it preferable for standard candle although the emission line lags can be measured up to $z \sim 4$ (see Watson et al. 2011). Unfortunately, only handful number of objects has dust lag measurement (Suganuma et al. 2006; Pozo Nuñez et al. 2014; Koshida et al. 2014), which motivated Hönig et al. (2017) to carry out a large dust reverberation mapping (DRM) program, "VEILS" (VISTA Extragalactic Infrared Legacy Survey) to use dust lag as standard candle for cosmology and constrain cosmological parameters. The "VEILS" survey will target about 1350 Seyfert 1 galaxies in the redshift range 0.1 < z < 1.2, however, missing the objects in the local universe which are crucial in determining the normalization parameter of the AGN distance moduli (see Hönig et al. 2017). Thus, dust reverberation mapping of local AGN will not only allow to estimate the extent of the torus, dust morphology and verify orientation dependent unification model but also help to estimate the normalization constant of the Hubble function.

To complement the VEILS program, in the nearby Universe, we are carrying out monitoring observations of a carefully selected sample of AGN with redshift less than 0.1 as part of our long term project called REMAP (REverberation Mapping of AGN Program). Observations towards this project has been carried out using the 2 m Himalayan Chandra Telescope at Hanle, India. Such a systematic study in conjunction with VEILS will serve as an excellent database to probe the complex interplay between optical continuum and dust emission in AGN. Here, we present the results of DRM monitoring of one local (z = 0.018) Seyfert 1.5 galaxy H0507+164. The structure of this paper is as follows. In section 2 we briefly describe the observation and data reduction processes. The analysis is presented in section 3. The results are discussed in section 4 followed by the summary in section 5. For the cosmological parameters we assumed $H_0 = 73$ km ${\rm s}^{-1}{\rm Mpc}^{-1}$, $\Omega_m = 0.27$ and $\Omega_{\lambda} = 0.73$ (Koshida et al. 2014).

2 OBSERVATION AND DATA REDUCTION

2.1 The Sample

The sample of sources for our DRM project were drawn from Bentz & Katz (2015) that have BLR lag from spectroscopic reverberation observations. From this list, we have selected only those sources that are accessible for observations using the 2m Himalayan Chandra Telescope (HCT) located at Hanle and operated by the Indian Institute of Astrophysics¹. In this paper, we present the result of the first source monitored for DRM using the HCT, namely H0507+164, a local Seyfert 1.5 galaxy at z = 0.018 with RA = 05:10:45.5 and DEC = +16:29:56. It is bright with an optical g band magnitude of 10 mag from the SIMBAD database². It has a black hole mass of $9.62^{+0.33}_{-3.73} \times 10^6 M_{\odot}$ deduced from spectroscopic reverberation observations (Stalin et al. 2011). It is detected in the NRAO/VLA Sky Survey (NVSS³) with a flux density of 6 ± 0.5 mJy at 1.4 GHz. However, it is radio quiet with a radio loudness parameter, R (ratio of flux density in the radio-band at 1.4 GHz to the optical V-band flux density) of 2.26 ± 0.26 .

2.2 Observations

The observations were carried out for a total of 35 epochs during the period October 2016 to April 2017 using HCT The telescope is a Ritchey-Chretien system with an f/9 beam. The optical observations were carried out using the Himalayan Faint Object Spectrograph and Camera

¹ http://www.iiap.res.in/centres/iao

² http://simbad.u-strasbg.fr/simbad/

³ http://www.cv.nrao.edu/nvss/NVSSlist.shtml

(HFOSC) mounted at the Cassegrain focus and equipped with a $2K \times 4K$ SiTe CCD system. This CCD has a readout noise and gain of 4.8 electrons/ADU and 1.22 electrons respectively. The observations were carried out in binned mode using only the central 2K × 2K region. Each pixel of the CCD in this mode corresponds to $0.3 \times 0.3 \text{ arcsec}^2$, and for the imaging observations reported here has a field of view of 10 \times 10 $\rm arcmin^2.$ The typical exposure time in $V\textsc{-}\mathrm{band}$ is about 50 seconds. The IR observations in J, H and K_s bands were done subsequently to the V-band observations at each epoch were carried out using the TIFR Near Infrared Spectrometer (TIRSPEC) mounted on one of the side ports of HCT (Ninan et al. 2014). The detector used in TIRSPEC is a 1024 \times 1024 HgCdTe array with a pixel size of 18 μm covering a field of view of 5×5 arcmin². It has a readout noise and gain of 25 electrons and 6 electrons/ADU respectively. The IR observations were performed in dithered mode consisted of five exposures each of 20 sec at three dither positions for each of three IR filters namely J, H and K_s . Apart from the science frames, sky regions were also observed in the same dithering pattern as the object to generate master sky frame.

2.3 Data reduction

The optical data reduction was done using IRAF (Image Reduction and Analysis Facility⁴) and MIDAS (Munich Data Analysis System⁵). For image reduction, we followed the standard procedure, such as bias & dark subtraction and flat-fielding. After removing the cosmic rays, the optical frames were aligned and then combined using imalign and imcombine tasks in IRAF for each day. Point spread function (PSF) photometry was carried out on the combined images using the daophot and allstar packages in MIDAS to find the instrumental magnitudes of the object and the comparison stars present in the CCD frames. The observed V-band image is shown in Figure 1.

Reduction of the NIR images was performed using TIR-SPEC NIR Data Reduction Pipeline (Ninan et al. 2014) for each band. The pipeline subtracts the dark obtained for the same exposure time as the science exposures and then uses twilight flats for flat fielding and produce final combined images. PSF photometry on the combined images was carried out by using MIDAS to get the instrumental magnitudes.

The object appears as a point source in our optical and IR data, thereby, making it difficult to model the host galaxy from the observed data and remove its contribution to the measured brightness. Therefore, subtraction of the host galaxy contribution to the measured brightness of the source was not carried out. Also, we have not corrected the observed flux values for galactic extinction. These effects will be small and a constant fraction of the measured flux values, thus having negligible effects on the cross-correlation analysis.

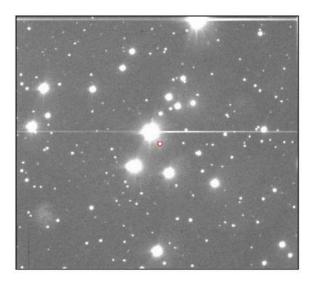


Figure 1. Observed V-band image of H0507+164. The integration time is 50 seconds and each side is 10 arcmin. The target source is shown with a circle.

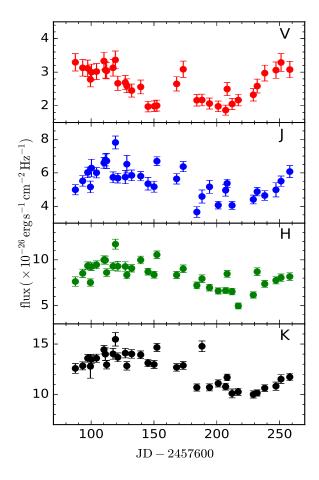


Figure 2. The light curves of H0507+164 in $V,\,J,\,H,\,Ks$ -bands for the period from October 2016 to February 2017. The NIR light curves were corrected for the contamination of emission from the accretion disk.

 $^{^4}$ IRAF is operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.

 $^{^5\,}$ MIDAS is the trade-mark of the European Southern Observatory

Table 1. Log of observations and results of photometry. Here JD is in days, the fluxes in different bands and their associated errors are in units of 10^{-26} erg s⁻¹ cm⁻² Hz⁻¹.

| JD_V | F_V | σ_V | JD_J | F_J | σ_J | JD_H | F_H | σ_H | JD_{K_s} | F_{K_s} | σ_{K_s} |
|-----------------|-------|------------|-----------------|-------|------------|-----------------|--------|------------|---------------------|-----------|----------------|
| 2457687.4272 | 3.295 | 0.260 | 2457687.4429 | 4.994 | 0.302 | 2457687.4374 | 7.628 | 0.517 | 2457687.4316 | 12.582 | 0.490 |
| 2457693.2663 | 3.129 | 0.247 | 2457693.2765 | 5.519 | 0.312 | 2457693.2819 | 8.521 | 0.457 | 2457693.2875 | 12.835 | 0.399 |
| 2457697.2763 | 3.115 | 0.246 | 2457697.2802 | 6.027 | 0.313 | 2457697.2858 | 9.339 | 0.432 | 2457697.2950 | 13.585 | 0.387 |
| 2457699.4455 | 2.784 | 0.221 | 2457699.4277 | 5.161 | 0.346 | 2457699.4219 | 7.520 | 0.399 | 2457699.4164 | 12.783 | 1.174 |
| 2457700.2714 | 2.999 | 0.238 | 2457700.2536 | 6.287 | 0.521 | 2457700.2473 | 9.262 | 0.429 | 2457700.2416 | 13.473 | 0.386 |
| 2457704.2750 | 3.019 | 0.238 | 2457704.2595 | 6.008 | 0.305 | 2457704.2541 | 9.459 | 0.428 | 2457704.2486 | 13.589 | 0.403 |
| 2457710.2058 | 3.331 | 0.262 | 2457710.2274 | 6.596 | 0.317 | 2457710.2219 | 9.989 | 0.455 | 2457710.2165 | 14.439 | 0.422 |
| 2457711.3872 | 3.064 | 0.241 | 2457711.3110 | 6.768 | 0.357 | 2457711.3051 | 9.962 | 0.447 | 2457711.2986 | 13.995 | 0.621 |
| 2457712.3179 | 3.041 | 0.240 | 2457712.3339 | 6.710 | 0.453 | 2457712.3279 | 8.612 | 0.415 | 2457712.3219 | 12.946 | 0.416 |
| 2457717.4375 | 3.129 | 0.247 | 2457717.4540 | 5.734 | 0.324 | 2457717.4488 | 9.297 | 0.441 | 2457717.4435 | 14.027 | 0.536 |
| 2457719.2792 | 3.365 | 0.265 | 2457719.3544 | 7.811 | 0.384 | 2457719.3489 | 10.171 | 0.543 | 2457719.3433 | 15.470 | 0.668 |
| 2457721.2253 | 2.668 | 0.212 | 2457721.2420 | 5.685 | 0.289 | 2457721.2364 | 9.295 | 0.526 | 2457721.2308 | 13.682 | 0.440 |
| 2457727.1733 | 2.690 | 0.213 | 2457727.1922 | 5.747 | 0.394 | 2457727.1868 | 9.270 | 0.518 | 2457727.1812 | 14.099 | 0.472 |
| 2457728.4147 | 2.596 | 0.206 | 2457728.3990 | 6.519 | 0.523 | 2457728.3928 | 8.346 | 0.411 | 2457728.3874 | 12.835 | 0.422 |
| 2457732.2453 | 2.451 | 0.194 | 2457732.2619 | 5.852 | 0.318 | 2457732.2559 | 9.073 | 0.401 | 2457732.2499 | 14.018 | 0.423 |
| 2457739.4652 | 2.560 | 0.205 | 2457739.4483 | 5.804 | 0.276 | 2457739.4421 | 9.983 | 0.415 | 2457739.4363 | 13.936 | 0.382 |
| 2457745.2972 | 1.974 | 0.158 | 2457745.2543 | 5.352 | 0.374 | 2457745.2485 | 8.704 | 0.364 | 2457745.2420 | 13.121 | 0.365 |
| 2457750.3023 | 1.985 | 0.158 | 2457750.0752 | 5.175 | 0.327 | 2457750.0811 | 8.368 | 0.371 | 2457750.0890 | 12.969 | 0.394 |
| 2457752.3102 | 2.004 | 0.162 | 2457752.3535 | 6.695 | 0.262 | 2457752.3476 | 10.556 | 0.411 | 2457752.3415 | 14.664 | 0.403 |
| 2457768.0595 | 2.651 | 0.213 | 2457768.0408 | 5.642 | 0.307 | 2457768.0331 | 8.345 | 0.385 | 2457768.0276 | 12.681 | 0.376 |
| 2457773.3053 | 3.086 | 0.243 | 2457773.2892 | 6.372 | 0.302 | 2457773.2830 | 9.025 | 0.413 | 2457773.2769 | 12.876 | 0.389 |
| 2457784.1059 | 2.163 | 0.173 | 2457784.1302 | 3.666 | 0.316 | 2457784.1220 | 7.208 | 0.372 | 2457784.1136 | 10.684 | 0.355 |
| 2457788.2195 | 2.171 | 0.173 | 2457788.2422 | 4.591 | 0.392 | 2457788.2362 | 7.938 | 0.422 | 2457788.2302 | 14.780 | 0.528 |
| 2457794.2058 | 2.065 | 0.164 | 2457794.2221 | 5.169 | 0.386 | 2457794.2160 | 6.960 | 0.363 | 2457794.2104 | 10.702 | 0.350 |
| 2457801.1541 | 1.982 | 0.158 | 2457801.1683 | 4.076 | 0.226 | 2457801.1626 | 6.604 | 0.338 | 2457801.1568 | 11.091 | 0.356 |
| 2457807.0827 | 1.868 | 0.149 | 2457807.0662 | 4.963 | 0.350 | 2457807.0598 | 6.646 | 0.314 | 2457807.0538 | 10.771 | 0.339 |
| 2457808.2595 | 2.497 | 0.197 | 2457808.2429 | 5.374 | 0.244 | 2457808.2372 | 8.461 | 0.369 | 2457808.2315 | 11.685 | 0.324 |
| 2457812.2031 | 2.052 | 0.166 | 2457812.1793 | 4.063 | 0.238 | 2457812.1733 | 6.533 | 0.356 | 2457812.1673 | 10.096 | 0.439 |
| 2457817.1344 | 2.169 | 0.173 | _ | _ | _ | 2457817.1214 | 4.961 | 0.317 | 2457817.0465 | 10.255 | 0.356 |
| 2457829.0926 | 2.326 | 0.186 | 2457829.0757 | 4.414 | 0.261 | 2457829.0698 | 6.161 | 0.344 | 2457829.0639 | 9.997 | 0.359 |
| 2457832.1700 | 2.586 | 0.206 | 2457832.1545 | 4.882 | 0.251 | 2457832.1483 | 8.705 | 0.425 | 2457832.1470 | 10.143 | 0.306 |
| 2457838.1930 | 2.972 | 0.235 | 2457838.1716 | 4.650 | 0.287 | 2457838.1656 | 7.371 | 0.374 | 2457838.1601 | 10.626 | 0.333 |
| 2457847.1147 | 3.061 | 0.243 | 2457847.1010 | 4.989 | 0.422 | 2457847.0918 | 7.763 | 0.389 | 2457847.0861 | 10.814 | 0.411 |
| 2457851.1541 | 3.289 | 0.265 | 2457851.1399 | 5.507 | 0.306 | 2457851.1344 | 8.052 | 0.399 | 2457851.1289 | 11.519 | 0.436 |
| 2457858.1201 | 3.078 | 0.244 | 2457858.1044 | 6.078 | 0.356 | 2457858.0989 | 8.170 | 0.414 | 2457858.0933 | 11.727 | 0.373 |

2.4 Subtraction of the accretion disk component from the NIR bands

The observed NIR fluxes are dominated by emission from the torus due to re-processing of the central UV/optical emission by the hot dust. However, it is contaminated by variable flux from the accretion disk component (Tomita et al. 2006; Kishimoto et al. 2008; Lira et al. 2011). This would make the time lag calculated by cross correlation analysis between the optical and IR light curves shorter than the actual lag of the dust-torus emission (Koshida et al. 2014). Thus, to get the true time lag, between optical and NIR flux variations, the contribution of accretion disk to the measured NIR fluxes needs to be removed. We estimated the contribution of the accretion disk in the J, H, Ks-bands in each of the epochs of observations by considering a power-law spectrum of the accretion disk following Koshida et al. (2014) and given by

$$f_{\rm NIR, disk}(t) = f_V(t) \left(\frac{\nu_{\rm NIR}}{\nu_V}\right)^{\alpha_\nu}$$
 (2)

where, $f_V(t)$ is the V-band flux at time 't', ν_V and $\nu_{\rm NIR}$ are effective frequencies of V-band and NIR bands respectively and α_{ν} is the power-law index. At any given epoch, the ob-

servations in the optical and each of the NIR bands differ by less than 300 seconds, and therefore, for the purpose of removing the contribution of accretion disk to each of the NIR bands, they were considered as simultaneous observations. To calculate $f_{\rm NIR, disk}(t)$, we assumed power-law index α_{ν} to be equal to 1/3 following Koshida et al. (2014). AGN do show spectral variability with a bluer-when-brighter behavior (Meusinger et al. 2011) which demands adoption of a time dependent α_{ν} to correct for the contribution of accretion disk emission to NIR. Our single optical V-band observations hinder determination of α_{ν} for each epoch of our observations. Use of single α_{ν} might have some effect on the corrected J-band fluxes, however, it will have negligible effect on the corrected K_s -band flux values.

Prior to the calculation and subsequent subtraction of the accretion disk component from the observed NIR fluxes, the observed instrumental magnitudes were converted to apparent magnitudes via differential photometry of few stars in the field whose apparent magnitudes were taken from the SIMBAD database. The apparent magnitudes were then corrected for Galactic extinction taken from the NASA/IPAC

Extragalactic database (NED⁶). These magnitudes were then converted into fluxes and the contribution of accretion disk evaluated using equation 2 were subtracted. The final fluxes thus obtained were used to generate optical and NIR light curves for further analysis. The errors in the final flux values in different filters were obtained through propagation of errors during the various steps of flux determination.

3 ANALYSIS

3.1 Light curves

The light curves of H0507+164 in optical V-band and NIR J, H and K_s bands are shown in Figure 2. As the source is radio-quiet, not much contamination to the observed flux variations is expected from the jet of the source. The variability nature of the source was characterized using the normalized excess variance (Edelson et al. 2002; Vaughan et al. 2003; Rani et al. 2017) defined as

$$F_{\rm var} = \frac{\sqrt{S^2 - \delta^2}}{\langle f \rangle} \tag{3}$$

Here $\langle f \rangle$, S^2 , δ are the mean flux, variance and mean error respectively for N observations and are given as

$$\langle f \rangle = \frac{1}{N} \sum_{i=1}^{N} f_i \tag{4}$$

$$S^{2} = \frac{1}{N-1} \sum_{i=1}^{N} (f_{i} - \langle f \rangle)^{2}$$

$$\tag{5}$$

$$\delta^2 = \frac{1}{N} \sum_{i=1}^{N} \delta_i^2, \tag{6}$$

(7)

where f_i and δ_i are the flux and error for the i^{th} measurement respectively. The uncertainties in the F_{var} are evaluated following Edelson et al. (2002) and given as

$$\operatorname{err}(F_{\operatorname{var}}) = \sqrt{\left(\sqrt{\frac{1}{2N}} \frac{\delta^2}{\langle f \rangle^2 F_{\operatorname{var}}}\right)^2 + \left(\sqrt{\frac{\delta^2}{N}} \frac{1}{\langle f \rangle}\right)^2} \tag{8}$$

In addition to calculating F_{var} we also calculated the ratio R_{max} between the maximum and minimum flux in the light curves. The results of variability analysis are given in Table 2. It is noticed that $F_{\rm var}$ in the optical V-band and NIR J and H-bands are similar, while the F_{var} in K_s band is lower than that in the other bands. An anti-corelation between variability amplitude and wavelength has been found recently based on analysis of NIR variability of a large sample of AGN by Sánchez et al. (2017). Also, compared to the optical bands, amplitude of NIR variation is expected to be smaller (Enya et al. 2002). Though our data do not reveal a clear anti-correlation of variability amplitude with wavelength as found recently (Sánchez et al. 2017), the F_{var} in the NIR bands are lower than of the optical V-band as expected (Enya et al. 2002). Therefore, the low amplitude of variations seen in the K_s band do not point to any inherent bias in the K_s band data.

Table 2. Variability statistics in $VJHK_s$ bands in observer's frame. Here, $\lambda_{\rm eff}$ is the effective wavelength in Angstroms. The average values $(\langle f \rangle)$ and the standard deviation σ of the $VJHK_s$ light curves

| are | in | units | of | 10^{-26} | $erg s^{-1}$ | ${\rm cm}^{-2}$ | Hz^{-1} . |
|-------|----|-----------------------|---------------------|------------|---------------------|-----------------|----------------------|
| Filte | er | $\lambda_{	ext{eff}}$ | $\langle f \rangle$ | σ | $F_{ m var}$ | R_{\max} | |
| | | | | | | | - |
| V | | 5510 | 2.66 | 0.48 | 0.159 ± 0.005 | 1.801 | |
| J | | 12200 | 5.56 | 0.89 | 0.149 ± 0.003 | 2.131 | |
| H | | 16300 | 8.39 | 1.36 | $0.154 {\pm} 0.002$ | 2.360 | |
| K_s | | 21900 | 12.56 | 1.56 | 0.119 ± 0.001 | 1.548 | |

3.2 Cross-Correlation Analysis

Our observations indicate that the source H0507+164 show flux variations in the optical and NIR bands enabling us to test for the presence/absence of time delay between flux variations in different bands. To calculate the time lag between the variations in the optical V-band emission from the accretion disk and the IR emission from the torus, we employed two well-known methods, namely the interpolated cross-correlation function (ICCF; Gaskell & Sparke 1986; Gaskell & Peterson 1987) and the discrete correlation function (DCF; Edelson & Krolik 1988). In this work, crosscorrelation analysis was performed between the V-band light curve and each of the NIR $(J, H \text{ and } K_s)$ light curves. Figure 3 shows the result of the cross-correlation analysis between V and J (upper panel), V and H (middle panel), V and K_s (lower panel). In each panel, the solid line shows the crosscorrelation function (CCF) obtained by ICCF method, and the data points with error bars are those obtained by DCF method. Both ICCF and DCF are found to be in excellent agreement. The autocorrelation function (ACF) is also plotted for V-band (dashed-dot) and corresponding NIR band (dashed) in different panels. The ACFs show zero lag as expected, but the CCFs show an overall shift along the positive lag indicating that NIR continuum lags behind the optical V-band emission. The amount of lag can be estimated either by the lag corresponding to the peak of the CCF (τ_{peak}) or by the lag corresponding to the centroid of CCFs ($\tau_{\rm cent}$). The later has been found to be a better representative of the lag, particularly in cases when the light curves are either noisy and/or have less number of points (Peterson et al. 1998). The centroids of the CCF was calculated as

$$\tau_{\text{cent}} = \frac{\sum_{i} \tau_{i} \text{CCF}_{i}}{\sum_{i} \text{CCF}_{i}}.$$
(9)

To quantify the lag, we have used here the centroid of the CCF, which is evaluated by considering all the points that are within 60 per cent of the maximum of the CCF. This cut off was selected so as to have sufficient cross-correlation coefficients for the centroid determination.

The uncertainties in the derived lag were evaluated using a model-independent Monte Carlo simulation based on the flux randomization (FR) and random subset selection (RSS) described in Peterson et al. (1998) with the additional improvement as suggested by Wandel et al. (1999) and summarized by Peterson et al. (2004). In each Monte Carlo iteration, we first randomly took N independent points from a parent light curve of N data points regardless of whether any point has previously been selected. The new light curve

⁶ https://ned.ipac.caltech.edu/

after RSS method contains M data points. To take into account the uncertainty in the measured flux values, we then randomly modified the fluxes of the M data points by adding the uncertainties of the measured flux multiplied with a random Gaussian value. For each Monte Carlo iteration, we computed the CCF of the modified light curve and calculated the $\tau_{\rm cent}$ using the points within 60 per cent of the CCF peak. This process was repeated for 20,000 iterations retaining only those CCF having peak value > 0.5 so that the cross correlation result is significant. We built the cross correlation centroid distribution (CCCD), which is shown by the histogram plot in each panel of Figure 3. The median of the CCCD is taken as a representation of the lag. Since the distribution has a non-Gaussian shape, we calculated uncertainties within 68 % confidence interval around the median value.

The result of the Monte Carlo simulation using different CCF analysis method is given in Table 3. The centroid lag obtained using DCF method was calculated for different bin sizes and the results are found to be consistent within error bars. The lags obtained by ICCF method are also given in Table 3 which agrees well with the DCF values within error bars. Though the time delays obtained from both DCF and ICCF agree with each other, for all further analysis we consider the lag obtained using the DCF with a bin size of $\Delta \tau = 5$ days as the typical sampling of our light curves is about 5 days. Based on this we find the rest frame (corrected for the redshift) time lags of $27.1^{+13.5}_{-12.0}$ days between V and J bands, $30.4^{+13.9}_{-12.0}$ days between V and H bands and $34.6^{+12.1}_{-9.6}$ days between V and K_s bands. Though there is an indication of wavelength dependent lag which increases with wavelength, because of the larger error bars, we conclude that within errors, the derived lags are consistent with each other. Considering only V and K_s light curves, we obtained a lag of $34.6^{+12.1}_{-9.6}$ days where Ks band variation lagging the V-band variations. This lag is larger than the lag of $3.01^{+0.42}_{-1.84}$ days obtained between the optical and emission line flux variations from optical spectroscopic monitoring observations (Stalin et al. 2011) and in agreement with what is expected from the unification model of AGN. Using this time delay we infer that the inner edge of the dusty torus is at a distance of $\approx 0.029^{+0.010}_{-0.008}$ pc from the central UV/optical AGN continuum source.

4 DISCUSSION

4.1 Infrared lag and central luminosity correlation

Using the rest frame time lag, the inner radius of the dusty torus in H0507+164 was found to be 0.029 pc. Similar measurements of the radius of the dust torus in about two dozen AGN are available in the literature based on DRM observations (see Koshida et al. 2014, and the references therein). These sources are shown in Figure 4 as empty circles in the lag - luminosity place. Also, shown in the same Figure is the location of the source H0507+164 indicated by a filled circle. The best-fitted regression line $\log \Delta \tau = -2.11 - 0.2 M_V$ of Koshida et al. (2014) which was based on a systematic and homogeneous analysis of DRM data of 17 Seyfert 1 galaxies is shown by a dashed line. Our lag measurement of H0507+164 is in excellent agreement with the lag expected

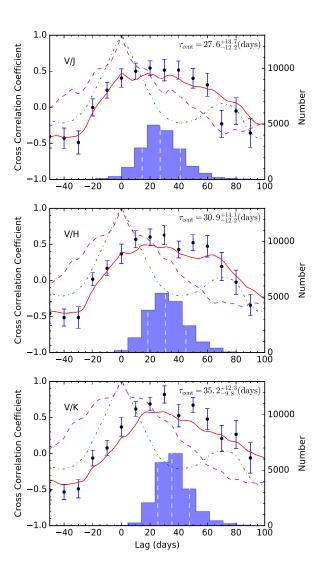


Figure 3. The CCF of V vs. J (top), V vs. H (middle) and V vs. K (bottom) is shown. In each panel, the solid line shows the ICCF, points with error bars show the DCF obtained using $\Delta \tau = 5$ days and the corresponding distribution of the $\tau_{\rm cent}$ obtained using 20,000 Monte Carlo Simulations. The dashed-dot line shows the ACF of V-band light curve and the dashed line shows the ACF of corresponding NIR band light curve. The value of $\tau_{\rm cent}$ obtained using Monte Carlo simulation is noted in each panel.

for its luminosity and closely follows the dust lag-optical luminosity correlation of $\Delta \tau_{\rm dust} \propto L^{0.5}$.

4.2 Structure of the BLR and the Dust Torus

Stalin et al. (2011) carried out spectroscopic reverberation observations of BLR of H0507+164 and estimated a lag between the optical/UV continuum and the H β line emission of $3.01^{+0.42}_{-1.84}$ days in the rest frame of the object. Our DRM observations for the same object in different NIR wavelengths together with the result obtained by Stalin et al. (2011) provide important information about the structure of the BLR and the dust torus of H0507+164. The BLR lag is found to be smaller than the dust-lag (lag between V-band and K_s -band) which is as expected from the unified scheme of

| Bands | | | DCF ($\Delta \tau$ in days) | | | ICCF |
|-----------|--|--|------------------------------|---|--|---|
| | 2 | 3 | 4 | 5 | 6 | |
| V-J | $31.1_{-15.0}^{+16.5} \\ 33.9_{-14.8}^{+17.4} \\ 39.2_{-12.3}^{+14.9}$ | $28.6_{-13.8}^{+15.4} \\ 32.0_{-13.6}^{+15.4} \\ 37.6_{-11.1}^{+13.1}$ | $28.0^{+15.1}_{-12.2}$ | $27.6_{-12.2}^{+13.7} 30.9_{-14.1}^{+14.1} 35.2_{-9.8}^{+12.3}$ | $27.3_{-12.0}^{+15.1}$ $31.9_{-12.6}^{+13.6}$ $36.3_{-10.7}^{+12.1}$ | $20.7_{-11.0}^{+13.5}$ $25.1_{-11.0}^{+12.4}$ $26.2_{-11.0}^{+9.0}$ |
| V-H | $33.9_{-14.8}^{+17.4}$ | $32.0_{-13.6}^{+15.4}$ | $32.8^{+15.7}_{-14.0}$ | $30.9_{-12.2}^{+14.1}$ | $31.9_{-12.6}^{+13.6}$ | $25.1_{-11.0}^{+12.4}$ |
| $V - K_s$ | $39.2^{+14.9}_{-12.3}$ | $37.6^{+13.1}_{-11.1}$ | $36.7^{-14.0}_{-10.7}$ | $35.2^{+12.3}_{-9.8}$ | $36.3^{+12.1}_{-10.7}$ | $30.2^{+9.0}_{-7.9}$ |

Table 3. Values of τ_{cent} and their associated error in days as obtained by DCF (for various bin size $(\Delta \tau)$) and ICCF methods.

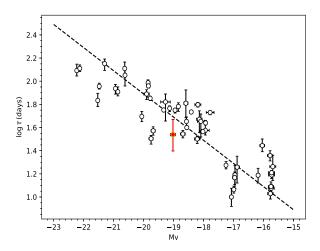


Figure 4. Dust lag-luminosity relationship using the data of Koshida et al. (2014). The filled circle corresponds to the lag between the V and K_s bands determined for

H0507+164 which lies close to the regression line (dashed line), obtained by Koshida et al. (2014). The lag times were corrected for the time dilation effect using the object redshift.

AGN. Though there are indications of a wavelength dependent lag in our multi-wavelength data reported here, they are not statistically significant due to the large errors in their lags. From an analysis of a sample of 17 Seyfert galaxies, Koshida et al. (2014) found that dust reverberation radius of their sample is 4-5 times larger than their BLR radius and typically a factor 2 smaller than their interferometric radius. Similarly, the BLR radius observed by reverberation mapping is smaller than the same observed by NIR interferometry (see Petrov et al. 2012). Such difference is expected as the reverberation mapping is a response weighted radius originating from the compact region, while the interferometric radius is flux weighted sensitive to the flux coming from the outer region (Kishimoto et al. 2007). However, there are exceptions. For the source Mrk 335 (Du et al. 2014) NGC 4151 (Bentz et al. 2006) and NGC 4593 (Barth et al. 2013), the dust radius (Koshida et al. 2014) is about 10 times larger than the BLR radius. Such varied differences between the mean dust radius and BLR radius known in AGN will hint for variable dust emission (Koshida et al. 2009; Schnülle et al. 2015). To establish this, we need more precise measurements of dust radius for a large sample of AGN. Our ongoing multi-band DRM project on a larger sample will help to understand dust geometry.

5 CONCLUSION

We have presented the first measurements of the time delays between optical and NIR bands. This is based on optical Vand NIR J, H and K_s bands observations spanning a time period of about 170 days. Significant variations have been observed in all bands. The rest frame lags between V-band and NIR bands are found to be $27.1_{-12.0}^{+13.5}$ days (V vs. J), $30.4_{-12.0}^{+13.9}$ days (V vs. H) and $34.6_{-9.6}^{+12.1}$ days (V vs. K_s). From the present analysis it is difficult to probe the existence of different lag between V and J, V and H and V and K_s , solely due to the large errors in the determined lags because of the limited amount of data analysed here. The presence of wavelength dependent lags if any can be established only with the accumulation of good quality monitoring data over a long period of time. It is likely that a combined analysis of the data would reduce the error in the lag between optical and NIR (Schnülle et al. 2015). Given the limited number of observations in the present work, we have not attempted a combined analysis.

Using the rest frame lag between V and Ks-band, we found that the inner radius of the dust torus is at a distance of 0.029 pc, from the central UV/optical continuum source. As expected from the unified model of AGN the dust inner radius is larger than the BLR radius known for this source from spectroscopic reverberation monitoring observations. Our estimate of $R_{\rm dust}$ and the V-band absolute magnitude is in good agreement with the dust lag-optical central luminosity relationship found by Koshida et al. (2014) from a large sample of AGN.

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