

Development of a Numerical Model for High-Temperature Shape Memory Alloys

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Abstract

A thermomechanical hysteresis model for a high-temperature shape memory alloy (HTSMA) actuator material is presented. The model is capable of predicting strain output of a tensile-loaded HTSMA when excited by arbitrary temperature-stress inputs for the purpose of actuator and controls design. Common quasi-static generalized Preisach hysteresis models available in the literature require large sets of experimental data for model identification at a particular operating point, and substantially more data for multiple operating points. The novel algorithm introduced here proposes an alternate approach to Preisach methods that is better suited for research-stage alloys, such as recently-developed HTSMAs, for which a complete database is not yet available. A detailed description of the minor loop hysteresis model is presented in this paper, as well as a methodology for determination of model parameters. The model is then qualitatively evaluated with respect to well-established Preisach properties and against a set of low-temperature cycled loading data using a modified form of the one-dimensional Brinson constitutive equation. The computationally efficient algorithm demonstrates adherence to Preisach properties and excellent agreement to the validation data set.

1. Introduction

In aeronautics propulsion, the transition to an all-electric engine is desirable from reliability and efficiency standpoints. By replacing conventional hydraulic actuation systems with smart material actuators in such components as valves, vanes, nozzles, it may be possible to realize substantial improvements in the overall size and weight of the engine, allowing higher efficiencies to be realized. Furthermore, the high energy output and bandwidth of such materials enable other lucrative control capabilities not previously within reach, such as active inlets, variable area nozzle control, and blade tip clearance control in the high-pressure turbine (refs. 1 to 4). In the active clearance control example, an array of actuators could be used to actively position several floating turbine shroud segments to within close proximity of the turbine blades using closed-loop control, which expand and contract during flight. In such an application, the smart material actuator must be capable of high-amplitudes of motion (~0.1 in.) amidst large bias loads (~2000 lbf) that can vary significantly during normal operation. Furthermore, such actuators must be capable of moderate bandwidths (on order of 1 Hz), be robust at elevated temperatures (i.e., long cycle life), consume minimal energy to operate, and be compact and light weight.

The particular class of smart materials known as shape memory alloys (SMAs) has emerged in several application areas including robotics, control of space-borne structures, and control of helicopter rotor blades (refs. 5 and 6). Some SMA materials, such as Nitinol, are capable of macroscopic strains up to 6 percent at stresses up to 500 MPa (ref. 7). In comparison with piezoceramics, for example, these capabilities amount to more than an order-of-magnitude higher energy output per unit density of material. Consequently, SMAs are well-suited for applications where size and weight are of high importance in actuator feasibility, as is the case with any propulsion system. Another advantage is that SMAs have similar manufacturability to conventional metals and, as such, are readily produced in structurally necessary forms: wires, rods, and sheets. Lastly, the unique thermal activation properties of SMAs give them a distinct advantage over other smart actuation methods because it is possible to circumvent potentially costly modifications to the propulsion power system that otherwise would be required (ref. 8). Because hot and cool air is often diverted from various stages in the engine in order to provide cooling to various high-temperature components, small portions of this secondary air may be actively modulated by way of a proportional valve. Therefore operation of the SMA actuator via active convective cooling may be possible in lieu of more conventional active resistance heating methods that require large power draws.

A functional drawback of SMAs is that the phase transitions that produce work are governed by hysteresis. Furthermore, with widely-available Nickel-Titanium (NiTi) alloys, phase transition temperatures and useable range of operation reside close to room temperature, rendering them infeasible for moderate- to high-temperature applications. To overcome these limitations, a Nickel-Platinum-Titanium ($\text{Ni}_{20}\text{Pt}_{30}\text{Ti}_{50}$) high-temperature shape memory alloy (HTSMA) has been recently developed at NASA Glenn Research Center. This alloy exhibits work outputs comparable to conventional NiTi alloys, but with transformation temperatures greater than 250 °C (480 °F) and oxidation rates that are less than half that of typical NiTi SMA materials (fig. 1). This is a significant advancement over conventional SMA materials, enabling the possibility for actuation in an engine's hot sections.

In partial alleviation of the hysteresis problem, HTSMA hysteresis deadband characteristics are narrower and hysteresis profiles shallower than many conventional NiTi alloys. Because it is not possible to fully eliminate inherent hysteresis, more sophisticated control strategies that guarantee stability, maximize HTSMA bandwidth, and maintain uniform response across the entire range of operation may still be required (refs 9 to 11). In any case, reliable development and evaluation of candidate actuator control systems usually require accurate models of the HTSMA. In addition, such models must be executable in a real-time environment in order for model-based control or estimation to be implemented.

Generally speaking, SMA models consist of two parts: a hysteresis model and a constitutive model. To accurately model hysteresis, minor hysteresis loops in the response trajectory must be accounted for, although inclusion of such detail substantially complicates the model and is an active area of research

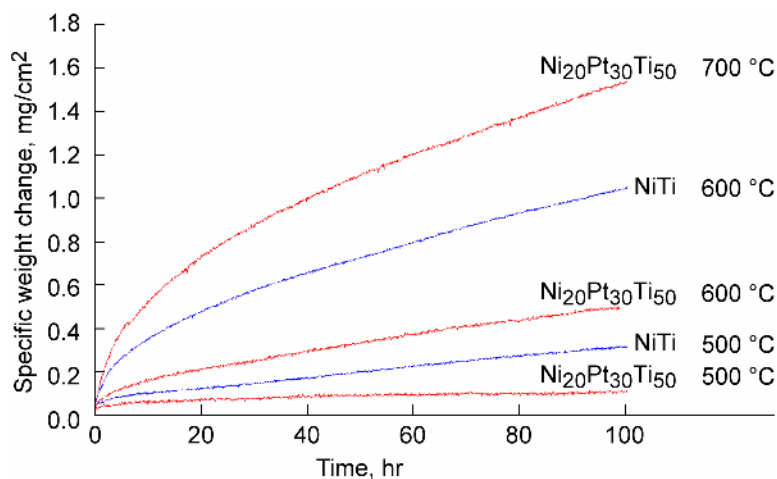


Figure 1.—Oxidation characteristics of $\text{Ni}_{20}\text{Pt}_{30}\text{Ti}_{50}$ and NiTi.

(ref. 12). It has been shown that the generalized Preisach model of hysteresis is suited for describing SMA hysteresis and obeys certain empirically-verified properties (refs. 12 to 14). The usefulness of generalized Preisach models is fully exploited only when a full database of empirical response data is available, usually in the form of probability density functions (PDFs) obtained from a population of first-order descending (FOD) curves (ref. 15). In the case of the HTSMA, however, this database does not yet exist due to the time and costs associated with conducting high temperature experiments. Furthermore, accurate constitutive models are still needed for estimation of internal SMA variables, leading to potential inaccuracies in the results. Since continuous-function PDF approximants have been shown to represent SMA behavior quite well under quasi-static situations (ref. 16), it is reasonable to adopt this approach for the HTSMA application. With these approximants, algorithmic hysteresis models that are both conceptually simple and easy to implement can be used as long as they are capable of capturing minor loop hysteresis phenomena.

Madill and Wang (ref. 16) developed an efficient algorithm for SMA control simulations to compute martensite volume fraction, an internal state variable, as temperature varies between intermediate points. However, memory of the trajectory history was limited to only the prior hysteresis loop, not every prior dominant loop, and hence violates well-established Preisach properties. Efficient, yet accurate algorithmic hysteresis models that memorize multiple prior dominant loops have been developed for electromagnetic power circuits by Casoria, et al. (ref. 17). To the authors' knowledge, however, such models have not been applied in a similar manner to shape memory alloys. Moreover, a thorough exposition of how these models were implemented has not been made widely available.

In this work, a numerical, algorithmic realization of HTSMA hysteresis is presented as an alternative to analytic generalized Preisach models based upon PDF data. In its simplicity, the algorithm offers an intuitive approach to SMA hysteresis in lieu of the 'black box' approach offered by generalized Preisach models. As such, one can directly define physical properties of the material or directly manipulate the constitutive equations as an alternative to obtaining sets of PDF identification data as new HTSMA materials become available. Although applicable to any of the several SMA constitutive models reported, the Brinson phenomenological constitutive model is chosen here because it possesses the fidelity to be applied across a wide range of stress-strain conditions (ref. 18).

The remainder of this paper is organized in the following manner. Section 3 describes the model architecture and development. In this section, the SMA constitutive equations are introduced, a modification to the transformation kinetics model is proposed, and incorporation of the minor-loop hysteresis algorithm is presented. Section 4 details experimental characterization of the HTSMA material and methodologies used in determining the necessary model parameters. The results of model validation are presented in section 5. Here, qualitative adherence to known Preisach properties and quantitative agreement to available experimental data is provided. A summary of the model's capabilities and recommended future work is given in section 6.

2. Nomenclature

A	region of austenite transformation
A_f	temperature at which austenite transformation is completed or finished
A_s	temperature at which austenite transformation starts
C	stress influence coefficient
E	modulus of elasticity
F	value of ζ_n when $d\zeta_n/dt$ changes sign
F_{min}	vector containing past minima
F_{max}	vector containing past maxima
M	region of martensite transformation

M_f	temperature at which martensite transformation is completed or finished
M_s	temperature at which martensite transformation starts
S	region of stress-induced martensite transformation
T	temperature
b	kinetic curve bias
dt	differential element of time
i	integer
f	kinetic curve describing minor loop transformation
k	integer
n	integer
Θ	coefficient of thermal expansion
Φ	kinetic curve scaling factor
Ω	phase transformation coefficient
ε	material strain
ε_L	maximum recoverable strain
ξ	total martensite fraction
ξ_S	stress-induced martensite fraction
ξ_T	temperature-induced martensite fraction
ξ_n	normalized martensite fraction
σ	applied stress
σ^{cr}	critical stress

Subscripts:

0	referring to an initial state
A	referring to austenite transformation
A^f	referring to temperature at which austenite transformation finishes
A_s	referring to temperature at which austenite transformation starts
M	referring to martensite transformation
M^f	referring to temperature at which martensite transformation is completed or finished
M_s	referring to temperature at which martensite transformation starts
S	stress-induced component
T	temperature-induced component
max	maximum value
min	minimum value
s	starting point
f	finish or final point

Superscripts:

$A \rightarrow M$	transformation from austenite to martensite
$A \rightarrow S$	transformation from austenite to stress-induced martensite
$M \rightarrow A$	transformation from martensite to austenite

$S \rightarrow A$ transformation from stress-induced martensite to austenite
 cr critical state

3. HTSMA Phenomenological Model

SMA materials generally exist in the austenite phase at high temperatures and the martensite phase at low temperatures. Functionally, drastic shape changes may arise when transitioning between these two crystallographic material phases. Large macroscopic work may accompany the resulting shape change when the parent austenite phase is higher in strength than the lower-temperature martensite phase. In such cases, the parent phase exhibits high-stiffness Hooke's law behavior while the martensite exhibits a lower-stiffness, pseudoplastic response. Transition paths are completely reversible, but are dominated by major loop hysteresis as shown in figure 2(a). Minor loop hysteresis is prevalent when transition changes occur before transformation is complete, as shown in figure 2(b); and is a more difficult phenomenon to model. The specific parameters used to model the shape memory effect are discussed in detail later in this section.

The HTSMA model consists of three parts: a transformation kinetics model describing major loop hysteresis, a generalized Preisach hysteresis algorithm relating temperature and stress to martensite fractions, and a constitutive equation relating martensite fractions to strain output under tensile loading. The various elements of the model are implemented as shown in figure 3 using MATLAB/Simulink (The Mathworks, Inc.). By adopting a modular implementation, the hysteresis model can be coupled with other models, such as heat transfer models or higher-fidelity constitutive models, depending on the particular needs facing the designer.

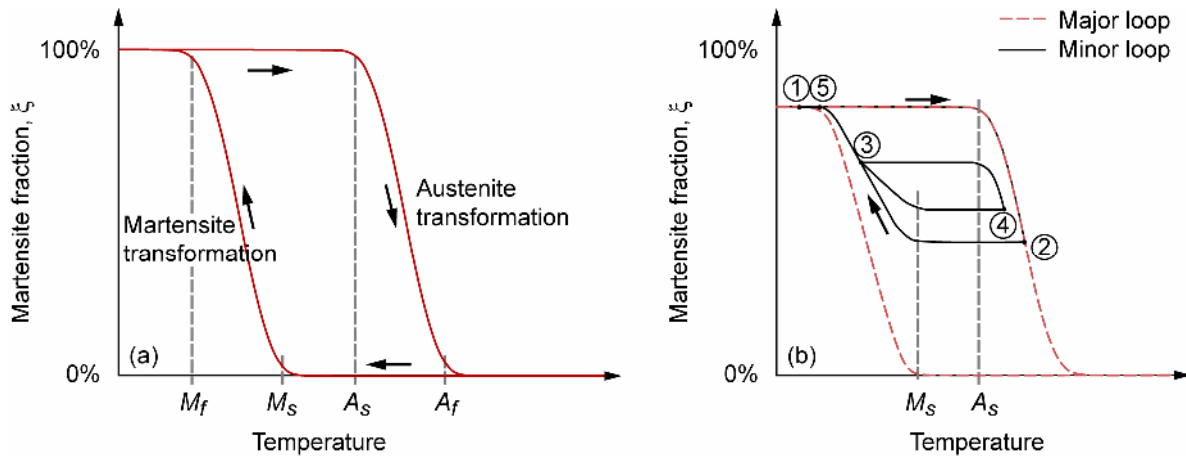


Figure 2.—Examples of: (a) major loop hysteresis, (b) minor loop hysteresis of SMA materials.

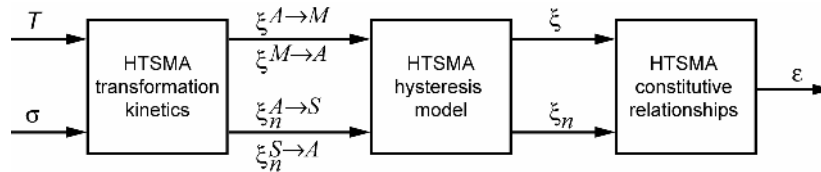


Figure 3.—Interconnection diagram of HTSMA model. $\xi^{x \rightarrow y}$ and $\xi_n^{x \rightarrow y}$ represent martensite fraction basis variables along the major loop contours; ξ and ξ_n represent the true martensite fractions with hysteresis.

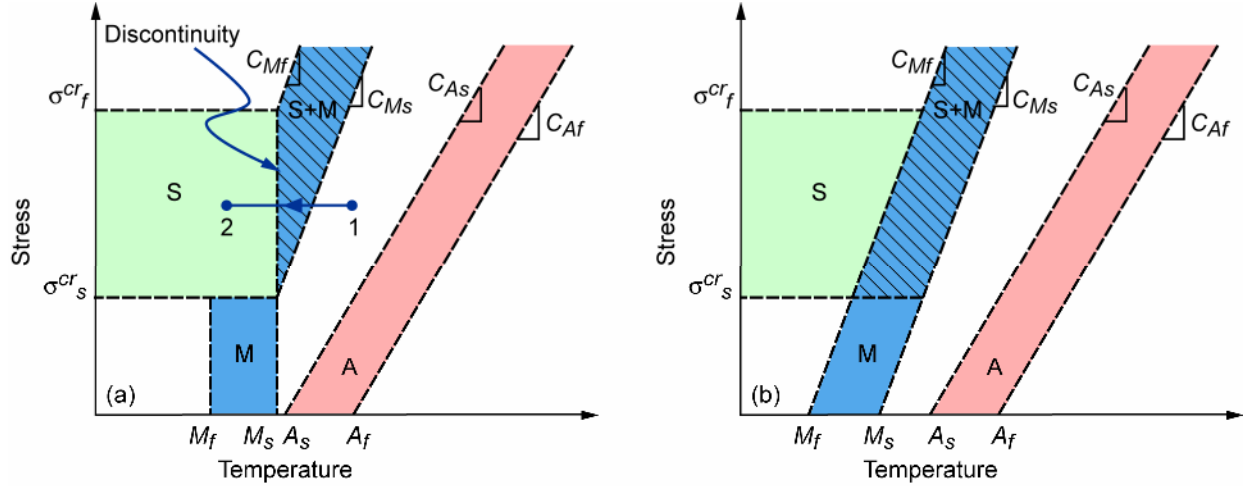


Figure 4.—Stress-temperature phase transformation diagram: (a) original Brinson model; (b) modified Brinson model.

Brinson Quasi-Static Constitutive Model

SMA actuators are typically implemented in a wire bundle arrangement due to ease of manufacture, fast heat transfer characteristics, failure redundancy, and conduciveness to resistive heating methods (ref. 19). A constitutive model based on uniaxial tensile loads representative of alloy wires is therefore an appropriate choice. Of the various phenomenological models available in the literature, none have broader applicability than the Brinson model (ref. 18) because of distinctions made between separate stress- and temperature-induced martensite fractions. This is especially important for predicting stress-related effects at low temperature.

The region where martensite transitions between its variants independent of temperature is denoted by S in the stress-temperature phase plot in figure 4(a). As stress is applied through region S , the alloy transitions from temperature-induced martensite to stress-induced martensite, causing a pseudoplastic deformation and large macroscopic strains. The thermomechanical explanation of this effect is that it is possible for multiple randomly-oriented martensite variants to coexist when martensite is in the “temperature-induced” state. In contrast, when martensite becomes completely “stress-induced,” only the variant that corresponds to the direction of the applied stress is in equilibrium. Hence, the two-way SMA energy output increases substantially with applied stress. When stress is again relieved, the martensite remains in the stress-induced state and maintains an elongated shape. Strain restoration cannot be achieved unless the material is heated to austenite, a process commonly referred to as the *shape memory effect*. Regions where austenite transformation occurs, denoted A in figure 4(a), and martensite occurs, denoted M , have an approximate linear dependence with applied stress. Variations in stress above A_f , but below the permanent martensite deformation temperature, result in complete strain recovery, known as the *pseudoelastic effect*.

The Brinson model describes the thermomechanical evolution by first separating total martensite fraction ξ into a stress-induced martensite component ξ_S and temperature-induced component ξ_T :

$$\xi = \xi_S + \xi_T \quad (1)$$

The constitutive equation relating the two martensite states and the strain ϵ , stress σ , and temperature T is as follows:

$$\sigma - \sigma_0 = E(\xi)\epsilon - E(\xi_0)\epsilon_0 + \Omega(\xi)\xi_S - \Omega(\xi_0)\xi_{S0} + \Theta(T - T_0). \quad (2)$$

Here the subscript 0 denotes the initial states, while Θ is the coefficient of thermal expansion (CTE). In addition, the modulus of elasticity, E , is non-constant and defined as,

$$E(\xi) = E_A + \xi(E_M - E_A), \quad (3)$$

with subscripts A and M referring to austenite and martensite, respectively. Furthermore, the phase transformation coefficient used in equation (2) is defined as,

$$\Omega(\xi) = -\varepsilon_L E(\xi), \quad (4)$$

where ε_L is the maximum recoverable strain.

The boundaries of the stress-induced martensite region S are defined by the starting critical stress σ_s^{cr} and the finish critical stress σ_f^{cr} . Bounding stresses for the austenite region A may be defined by

$$\sigma_{As}^{cr} = C_{As}(T - A_s) \quad (5a)$$

$$\sigma_{Af}^{cr} = C_{Af}(T - A_f) \quad (5b)$$

Similarly, the martensite region M is bounded by

$$\sigma_{Ms}^{cr} = C_{Ms}(T - M_s) \quad (6a)$$

$$\sigma_{Mf}^{cr} = C_{Mf}(T - M_f) \quad (6b)$$

The crosshatched region in figure 4(a) represents the location where the two martensite regions coincide. Here A_s , A_f , M_s , and M_f are defined as the austenite start, austenite finish, martensite start, and martensite finish temperatures, respectively, evaluated at zero stress. The stress influence coefficients C_{As} , C_{Af} , C_{Ms} , and C_{Mf} are the corresponding slopes of the transition temperature-stress boundaries. The hysteresis model describing the relationship between temperature and martensite fraction within the critical stress regions is outlined in the following sections.

Modification to Original Brinson Model

The cosine transformation kinetic approximant used to describe major loop behavior of both total and stress-induced martensite fraction was initially proposed by Liang and Rogers (ref. 20) and later modified by Brinson (ref. 21) to accommodate stress-induced martensite. For transitions from austenite to martensite, Brinson's model describing stress-induced martensite fraction encounters discontinuities in situations when temperature decreases through M_s with $\sigma_s^{cr} < \sigma < \sigma_f^{cr}$, as depicted by the path 1→2 in figure 4(a). As the kinetic equations are written, transformation of ζ_S progresses from finite slope to zero slope at a point along the kinetic curve corresponding to the instantaneous stress at M_s , instead of proceeding to the lower bound of the kinetic curve. To establish continuity, the relationship $\xi_n = \xi_S / \xi$ is introduced and hysteresis is instead described by martensite fraction ζ and normalized martensite fraction ζ_n . This substitution modifies the original phase transformation regions from those shown in figure 4(a) to those shown in figure 4(b). The modified Brinson model further enables M to be a linear function of stress (instead of stress-independent), permitting closer agreement between the model and data at stresses below σ_s^{cr} .

Transformation from austenite to martensite is represented by the following:

$$\xi^{A \rightarrow M}(\sigma, T) = \frac{1}{2} \cos \left[\pi \frac{T - M_f - \sigma C_{Mf}^{-1}}{M_s - M_f + \sigma (C_{Ms}^{-1} - C_{Mf}^{-1})} \right] + \frac{1}{2}, \quad (7a)$$

$$\xi_n^{A \rightarrow S}(\sigma, T) = \frac{1}{2} \cos \left[\pi \frac{\sigma - \sigma_f^{cr}}{\sigma_s^{cr} - \sigma_f^{cr}} \right] + \frac{1}{2}. \quad (7b)$$

The superscripts designate the direction of transformation, i.e., $A \rightarrow M$ = austenite to martensite; $A \rightarrow S$ = austenite to stress-induced martensite. The cross-hatched region in figure 4(b) represents the intersection of all non-saturated values of $\xi^{A \rightarrow M}$ and all non-saturated values of $\xi_S^{A \rightarrow S}$ (all nonzero values of $\xi_n^{A \rightarrow S}$). The only other notable difference between this model and past realizations is that independent stress influence coefficients are now applied to M_s and M_f .

For transition from $M \rightarrow A$ the transformation kinetics are represented by

$$\xi^{M \rightarrow A}(\sigma, T) = \frac{1}{2} \cos \left[\pi \frac{T - A_s - \sigma C_{As}^{-1}}{A_f - A_s + \sigma (C_{Af}^{-1} - C_{As}^{-1})} \right] + \frac{1}{2}, \quad (8a)$$

$$\xi_n^{S \rightarrow A}(\sigma, T) = F \xi^{M \rightarrow A}(\sigma, T), \quad (8b)$$

where F represents the value of ξ_n at the instant when $d\xi_n/dt$ changes sign. In figure 4(b), transformations in stress-induced martensite and total martensite to austenite are both represented by A , as equation (8) reflects. Because $\xi^{M \rightarrow A}$ and $\xi_S^{S \rightarrow A}$ are coincident, F may be thought of as a scalar on martensite fraction in determining $\xi_n^{S \rightarrow A}$. For implementation of the model, the basis variables of equations (7) and (8) are passed as inputs to the minor loop computation algorithm.

Minor Loop Algorithm

To illustrate the phenomenological behavior of minor hysteresis loops, consider trajectory 4-5 in figure 2(b). In this example, the trajectory initially follows the transition path that intersects point 3 as temperature decreases. After the intersection with 3, a new path is followed, intersecting point 1. Transition paths are dependent on prior extrema; however, as smaller loops are overtaken by larger ones, the smaller extrema are eliminated from memory. This is described succinctly by the *wiping out property* of the generalized Preisach model. Once the material reaches point 1 (also point 5), the double minor loop is closed and all extrema are eliminated from memory. An additional property, known as the *minor loop congruency property*, is required to complete the generalized Preisach model.

Within the Preisach modeling paradigm, it has been shown that reasonable approximations to the PDF can be obtained using information contained in major loop data (ref. 15). Therefore, monotonic variations in temperature during minor loop formation may be described by the major loop, which is scaled and translated based on the past history of temperature (or martensite fraction) extrema. Representing Preisach hysteresis during transition from martensite to austenite is accomplished in a piecewise manner that depends on the direction of transformation:

$$f(\sigma, T) = \begin{cases} \max \left[\Phi^{A \rightarrow M} f^{A \rightarrow M}(\sigma, T) + b^{A \rightarrow M} \right] & \text{for } df/dt > 0 \\ \min \left[\Phi^{M \rightarrow A} f^{M \rightarrow A}(\sigma, T) + b^{M \rightarrow A} \right] & \text{for } df/dt < 0 \end{cases} \quad (9)$$

where the scalars and biases are

$$\Phi^{A \rightarrow M} = \frac{F_{\min} - F_{\max}}{F_{\min}^{A \rightarrow M} - F_{\max}^{A \rightarrow M}}$$

$$\Phi^{M \rightarrow A} = \frac{F_{\min} - F_{\max}}{F_{\min}^{M \rightarrow A} - F_{\max}^{M \rightarrow A}}$$

$$b^{A \rightarrow M} = F_{\max} - \Phi^{A \rightarrow M} F_{\max}^{A \rightarrow M}$$

and

$$b^{M \rightarrow A} = F_{\min} - \Phi^{M \rightarrow A} F_{\min}^{M \rightarrow A}$$

Here f is used to represent both ζ and ζ_n , as algorithms are identical for both variables. It follows that $f^{A \rightarrow M}$ and $f^{M \rightarrow A}$ are the associated kinetic curves (for ζ_n , superscript M is replaced with S). F_{\min} contains the past n minima of f and F_{\max} contains the past n maxima of f , collected at instants when f changes sign. $F_{\min, \max}^{A \rightarrow M}$ and $F_{\min, \max}^{M \rightarrow A}$ are analogous vectors corresponding to $f^{A \rightarrow M}$ and $f^{M \rightarrow A}$.

In order to satisfy the wiping out property, the hysteresis model must discard past extrema that are smaller in magnitude than the most recent value. Each extrema vector is subject to the following conditions:

- For $i = 1, \dots, n$, if $df/dt > 0$ and $F_{\min}(i) > F_{\min}(1)$ (1 being the most recent), then
 - i. Let $F_{\min}(i) = F_{\min}(1)$
 - ii. Let $F_{\max}(i) = \min_k \{F_{\max}(k)\}$ with $k = 1, \dots, n$ and $k \neq i$

This modifier is applied to the remaining two extrema vector pairs $F_{\min}^{A \rightarrow M}$, $F_{\max}^{A \rightarrow M}$ and $F_{\min}^{M \rightarrow A}$, $F_{\max}^{M \rightarrow A}$.

- For $i = 1, \dots, n$, if $df/dt < 0$ and $F_{\max}(i) < F_{\max}(1)$ (1 being the most recent), then
 - i. Let $F_{\max}(i) = F_{\max}(1)$
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This modifier is applied to the remaining two extrema vector pairs $F_{\max}^{A \rightarrow M}$, $F_{\min}^{A \rightarrow M}$ and $F_{\max}^{M \rightarrow A}$, $F_{\min}^{M \rightarrow A}$.

In the simulation, the number of memorized loops n is set to 10 to ease computational efficiency. To eliminate the feedback path, the sign of df/dt for detection of the turn-around points is computed instead by testing the sign of $df^{A \rightarrow M}/dt$ and $df^{M \rightarrow A}/dt$. If either one changes sign, then an extremum has

been detected. The algorithm may encounter situations where small input variations or noise may cause oscillations in the extremum detector, therefore a threshold was incorporated in the detection scheme to reject these oscillations. It is known that hysteresis response approaches a linear characteristic with small driving amplitudes, thus thresholding will not compromise the model's accuracy. Within the MATLAB/Simulink environment, the hysteresis model was implemented as an Embedded MATLAB Function, which was called once every time a martensite fraction extremum is detected.

4. HTSMA Characterization

Experimentally-identified properties of the HTSMA that were used to parameterize the present model are given in table 1. Additional data and explanation of the properties are provided in reference 0. The data was collected from several forms of a Ni₃₀Pt₂₀Ti₅₀ alloy that has been identified for high-temperature actuator applications and is undergoing additional development and optimization at NASA Glenn. It should be noted, however, that material properties are highly dependent on variations in thermomechanical processing and minor deviations in composition.

TABLE I.—PHYSICAL PROPERTIES OF Ni₃₀Pt₂₀Ti₅₀

Parameter		Value		Parameter		Value	
Martensite start temperature	M_s	510	°F	M_s stress influence coefficient	C_{Ms}	0.83	ksi/°F
Martensite finish temperature	M_f	463	°F	M_f stress influence coefficient	C_{Mf}	1.44	ksi/°F
Austenite start temperature	A_s	505	°F	A_s stress influence coefficient	C_{As}	1.78	ksi/°F
Austenite finish temperature	A_f	527	°F	A_f stress influence coefficient	C_{Af}	0.83	ksi/°F
Start critical stress	σ_s^{cr}	33.4	ksi	Elastic modulus of martensite (200 °C)	E_M	10152	ksi
Finish critical stress	σ_f^{cr}	128.6	ksi	Elastic modulus of austenite (300 to 600 °C)	E_A	12328	ksi
Max. recoverable strain	ε_L	3.3	%	Coefficient of thermal expansion	Θ	1.02e-5	1/K

The Young's moduli and room temperature tensile properties in table I were specifically obtained from measurements on a 0.060-in.-diameter rod that was produced by a multiple extrusion technique from a 1-in.-diameter cast and homogenized billet, resulting in a uniform, fine-grained material. The sample is representative of the material in wire form, which is the most likely product form for actuator applications. Difficulties in measuring material modulus by direct techniques, i.e., extensometry or strain gages, arise from the extreme dependence of modulus on strain. Instead, modulus measurements were determined on the as-processed rod by an impulse frequency excitation technique.

Values for critical stresses were determined in a similar manner to Epps and Chopra (ref. 23), at approximate points where the room temperature stress-strain characteristic deviates from linear elastic regimes that correspond, in theory, to the start and finish of the stress-induced martensite transformation ($\xi_S = 0 \rightarrow 1$). In practice, the start critical stress σ_s^{cr} is an approximation to the start of the nonlinear regime and the finish critical stress σ_f^{cr} , coupled with the stress-free maximum recoverable strain ε_L , are chosen to obtain adequate model agreement to the slope of the transition region below 3 percent strain. Based on experience with conventional shape memory alloys, the material will experience reduced fatigue life at strain levels above approximately 3 percent, therefore any application utilizing these alloys should prevent strains from exceeding those levels. Since there is no practical way of measuring stress-induced martensite fraction ξ_S to make correlation with σ_f^{cr} and ε_L possible, the model-calculated value of ξ_S loses physical meaning, even with a perfect model fit. If the model is indeed exercised within the valid strain range, the overall modeling accuracy will not be compromised.

The tensile curve used to determine these parameters is shown in figure 5 with the model fit overlaid on the plot. The sample used for the experiment was a thin rod that was heat-treated at 1112 °F (600 °C) to regain the shape memory properties that were suppressed due to the significant level of hot-working in

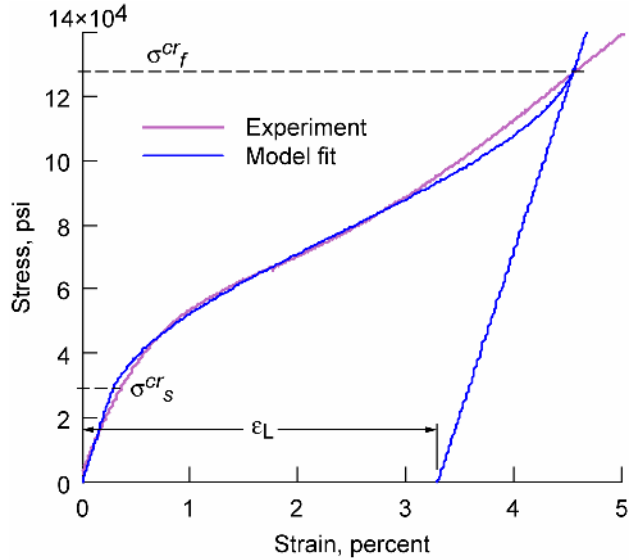


Figure 5.—HTSMA stress strain curve for a Ni₃₀Pt₂₀Ti₅₀ HTSMA and model fit at room temperature.

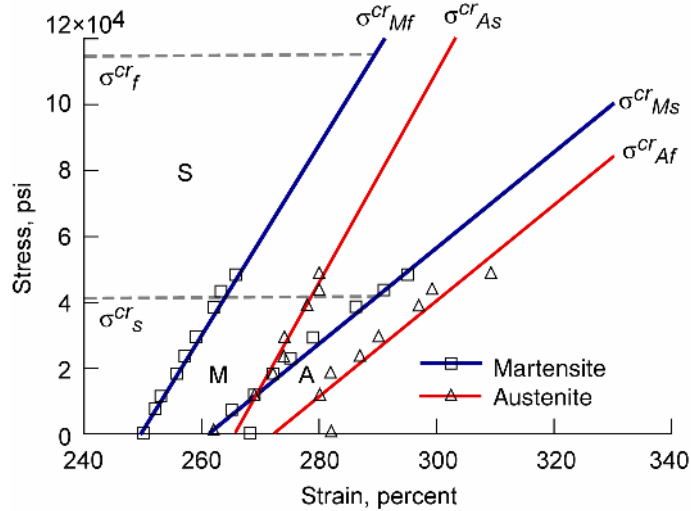


Figure 6.—Stress-temperature transformation data for a Ni₃₀Pt₂₀Ti₅₀ HTSMA and model fit.

the alloy. The tensile properties of the heat-treated rod are very similar to those for the as-processed rod (provided in table I), except for an increase in the yield strength in the heat-treated material. The linear region on the right-hand side of the model curve illustrates the material’s actual behavior when the strain is relieved following an initial stress increase past σ_f^{cr} . Note that, by decreasing the stress to zero, the value of the modeling parameter ϵ_L becomes apparent.

A plot of the phase transformation temperatures as a function of stress for the alloy is shown in figure 6, along with the fitted boundaries, using the values listed in table I. The data set was determined by measuring the strain-temperature response of the material under various levels of constant stress. These tests were performed on cast and homogenized ingots that were extruded at 2012 °F (1100 °C) at a reduction ratio of 7:1. This simple, high-temperature processing resulted in a very course grained

material. Coefficient of thermal expansion (CTE) was obtained via dilatometry testing using the same course grained rod. Figure 6 illustrates that the martensite and austenite transition temperatures have less overlap but tighter transformation bands at low stress, but larger overlap and wider transformation bands at larger stresses. Parameters in the linear stress-temperature relationships of equations (5) and (6) were adjusted to approximate the respective data for the transformation boundary regions. It should be noted that the zero-stress transition temperatures in the data were considered as outliers and were removed from the parameterization.

5. Model Evaluation

The goal of the evaluation is to validate the full model against both established hysteresis principles and a set of stress-cycled data. The modified Brinson major loop model was compared with responses with the original representation, while the minor loop hysteresis model was validated against well-established Preisach properties. The complete model was then validated against a set of stress-cycled experimental data. In each of the following simulations, the CTE was set to zero and the simulation increment was set to 1 ms.

Major Loop Simulation Tests

Major loop evaluation was conducted by cycling the internal temperature between M_f and A_f at several constant stress conditions. Figure 7 shows the result of the evaluation at the four stress conditions given in table II. It should be noted that test points 2 to 4 are considered to be in the extrapolated range of the phase plot in figure 6 and test points 3 and 4 are considered to be outside the valid strain range in figure 5. The figure highlights dependence on peak-to-peak strain on stress-induced martensite fraction. At test point 1, stress-induced martensite remains close to zero throughout the cycle, since the alloy stress is below the start critical stress σ_s^{cr} . The resulting peak-to-peak strain in figure 7, or equivalently, the difference between martensite strain and austenite strain, is 0.05 percent. At test points 2, 3, and 4, stress-induced martensite peaks at 0.33, 0.82, and 0.98, respectively, causing reversible peak-to-peak strains to grow accordingly. Due to the dependence of stress on transformation temperatures, the hysteresis curves shift to higher temperatures and decrease in slope as applied stress increases. Discontinuity in ξ_s response from the original Brinson model at the stress-independent intersection of M and S (at ~ 290 °C) is eliminated in the modified version by addition of the new variable ζ_n , as can be noted in the figure.

TABLE II.—TEST POINTS USED FOR HYSTERESIS EVALUATION

Test point	Description	Stress, ksi
1	Stress below critical region, $\sigma < \sigma_s^{cr}$	30
2	Stress within critical region, $\sigma_s^{cr} < \sigma < \sigma_f^{cr}$	70
3	Stress within critical region, $\sigma_s^{cr} < \sigma < \sigma_f^{cr}$	100
4	Stress above critical region, $\sigma > \sigma_f^{cr}$	130

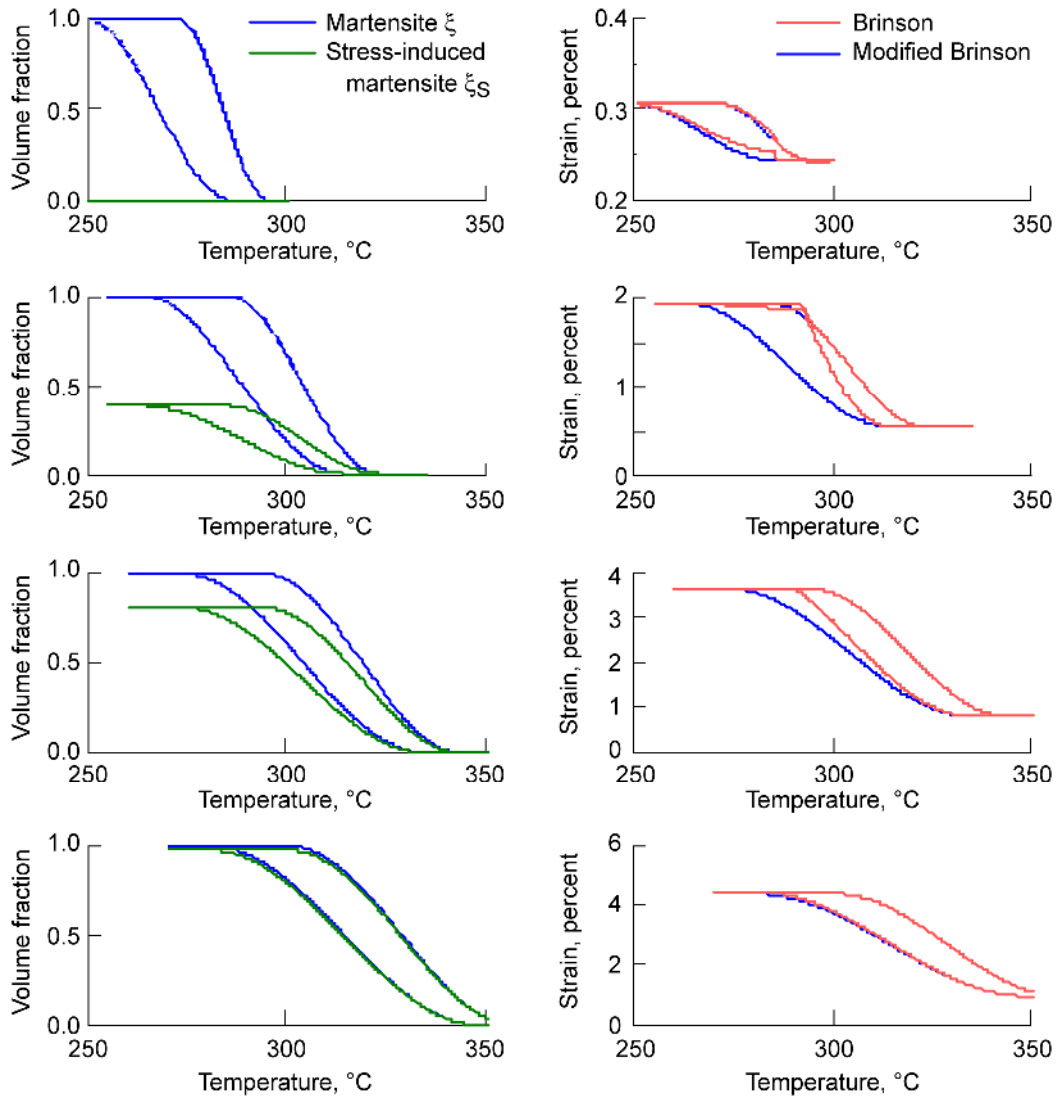


Figure 7.—Temperature-cycled major loop martensite fractions and resulting strain at test points 1 (top row) thru 4 (bottom row).

High Temperature Minor Loop Simulation Tests

The next set of tests focused on evaluating minor hysteresis loop prediction. For all temperature-cycled evaluation tests, a constant stress from test point 1 was used. The first two tests aim to verify adherence to Preisach hysteresis that is described by the following two properties: *minor loop congruency* and *wiping out* of past extrema. The second two tests illustrate the prediction capability given more complex loading profiles.

The congruency property test in figure 8 was generated from a temperature input that produces two opposing loops. The first loop occurs during transition along the $M \rightarrow A$ kinetic curve and the second occurs along the $A \rightarrow M$ curve with the same temperature reversal points as the first, designated by paths 2-3-4 and 6-7-8, respectively. It is evident from figure 8 that the correct hysteresis trajectory is developed, as the two minor loops appear to be congruent in shape. Nevertheless, the scaling factors $\Phi^{A \rightarrow M}$ and $\Phi^{M \rightarrow A}$ are slightly different between the two minor loop segments, resulting in a small discrepancy in the sizes of the two minor loops. It is important to note that, although equation (9) scales minor loop segments from major loop bases, the algorithm does not guarantee congruency of two vertically-shifted loops. To

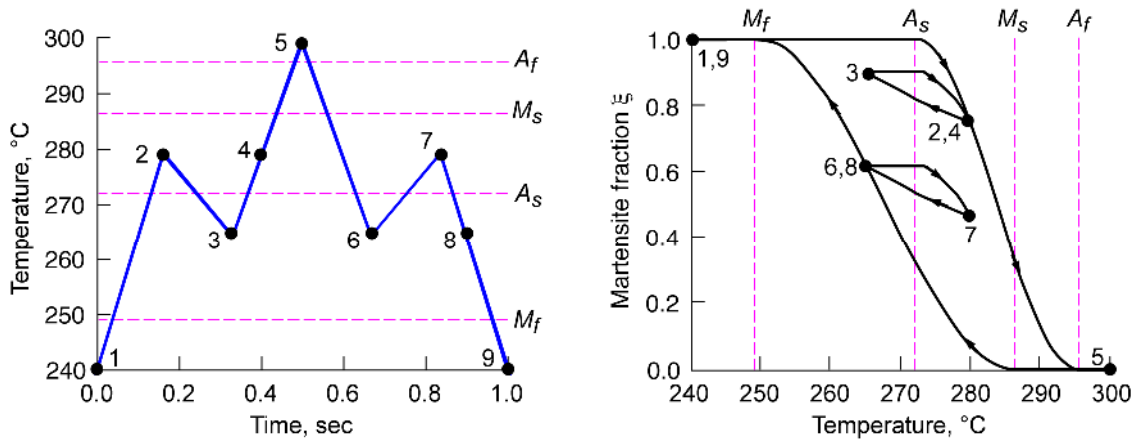


Figure 8.—Two opposing minor loops-congruency property test.

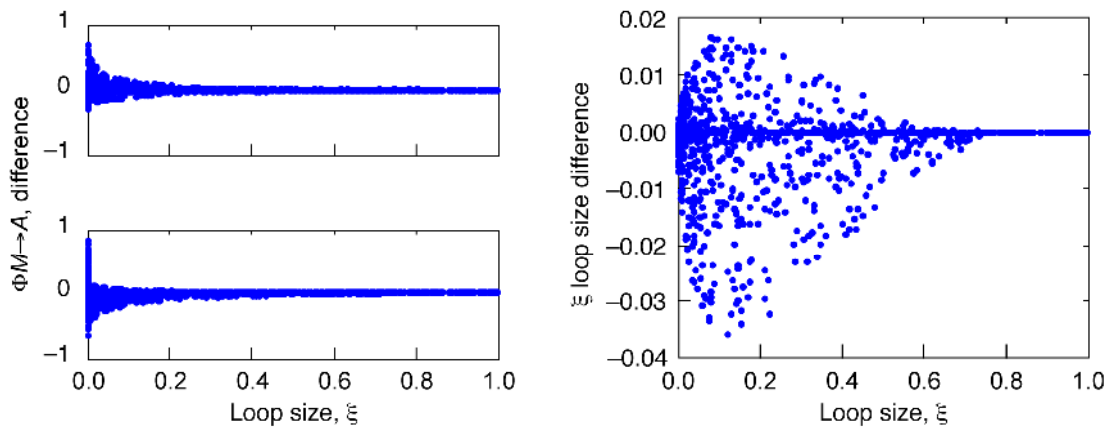


Figure 9.—Differences in scaling factors and ξ loop size between two congruent loops; data generated from congruency property test runs at 1000 random stresses and temperatures.

investigate congruency adherence further, a profile of minor loop congruency inaccuracies across the range of operation was generated by performing the congruent loop test at 1000 randomly-generated stresses and temperatures. Figure 9 shows differences between the minor loop scaling factors for the first and second loop as functions of minor loop size. The plot also shows differences between minor loop sizes between the two loops versus minor loop size for the same set of tests. Results indicate that scaling factor errors are large for small magnitude loops, but become smaller as magnitudes increase. A similar trend can be seen in the magnitude errors, however, large errors persist over a wider range of loop magnitudes. The pseudorandom nature of the errors confirms that, on average, the congruency property is satisfied. Based on the data it is hypothesized that truncation errors in the denominator of Φ in equation (9) cause differences in Φ to grow as minor loops become small. One fix to resolve this issue is to implement an amplitude threshold to prevent truncation errors from dominating the response with small loops.

In the wiping out test, shown in figure 10, a past extrema pair that makes up a minor loop must be “wiped out” when one of the two points is overtaken. The property is clearly demonstrated in the figure, as the first two decaying minor loops (path 2-3-4-5-6-7) are replicated one-for-one with the second two loops (7-3-4-5-6-7). For verification, investigating the sequence shows that both extrema from the innermost loop are indeed eliminated from memory as the second half of the trajectory begins, resulting

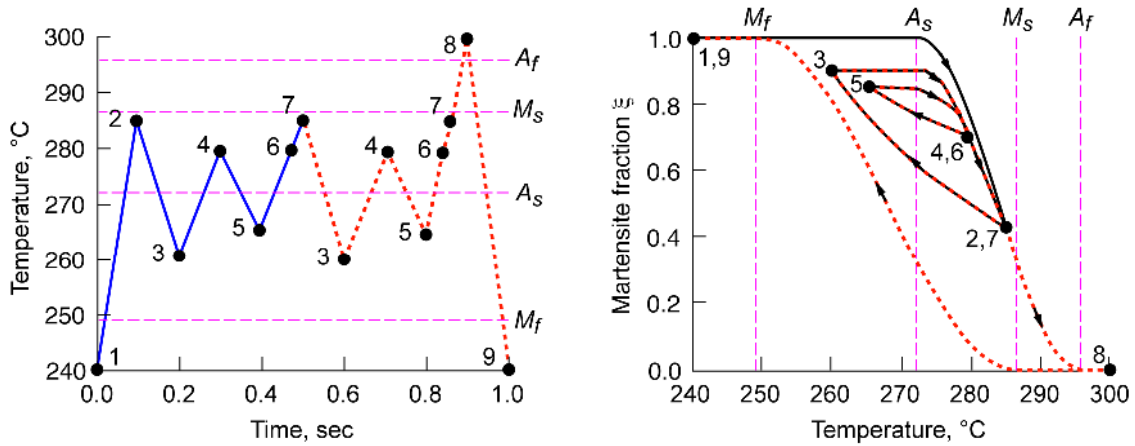


Figure 10.—Two decaying minor loops—wiping out property test. Second half of time input shown as red dotted line for clarity.

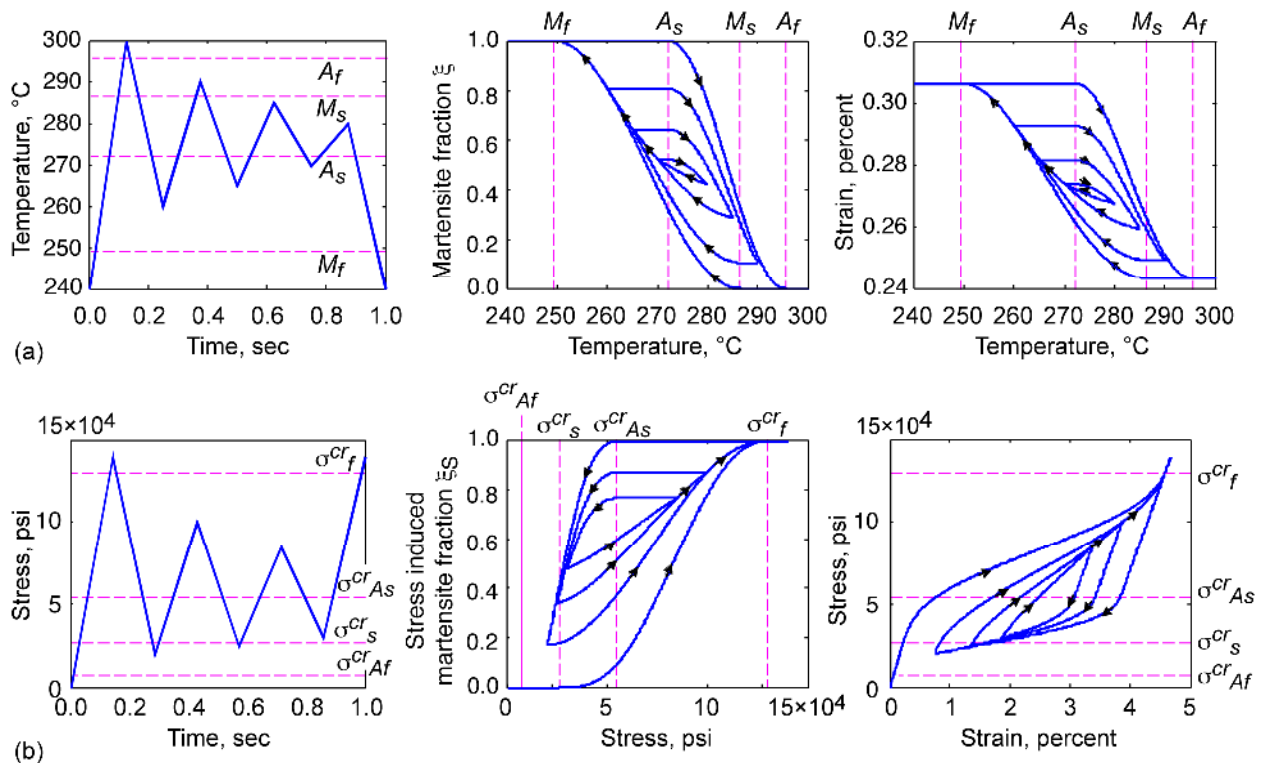


Figure 11.—(a) Three decaying minor loops—temperature cycles; (b) three decaying minor loops—stress cycles at 280 °C.

in reconstruction of the larger minor loop. It is thus concluded that the algorithm correctly adheres to the wiping out property.

Results of the multiple decaying minor loop test is shown in figure 11. These tests were performed to verify the algorithm's ability to construct minor loops given a slightly more complex input sequence. In figure 11(a), after the three decaying minor loops are developed, the martensite fraction trajectory intersects the previous three extrema as temperature is decreased in the final monotonic input segment. After each intersection, the associated extrema pair is eliminated from memory as it approaches the

martensitic kinetic curve. After the third of the extrema pair is eliminated, the martensitic kinetic curve is traced exactly.

This test also sheds light on how minor loop behavior in any hysteretic system can impact control design by virtue of the system being non-stationary. As driving amplitude decays over time, the resulting minor loops converge to a small slope. In the worst-case, if the trajectory evolves to a steady-state that is in the flat region of one of the kinetic curves (i.e., either between M_s and A_f or M_f and A_s), then this slope may approach zero. With such a severe change in input-output sensitivity, it is obvious that control stability and robustness can be significantly compromised as steady-state is reached. Such concerns have been echoed by other researchers (ref. 16), who have focused on development of robust SMA control techniques. Having multiple minor loop fidelity, the present model can capture these important effects, and hence predict stability given any compensative action.

A similar set of tests is shown in figure 11(b), except the minor loops were generated by stress cycling. As with temperature variation tests, the input-output profile follows partial recovery paths up to the last segment, during which time the trajectory eliminates the previous minor loop extrema after they are intersected. At each stress relief segment, the trajectory follows linear elastic theory described by E_M until stress drops below $\sigma_{A_s}^{cr}$, at which point strain partially recovers.

Low Temperature Stress-Cycled Minor Loop Tests

A cycled stress input test was conducted to examine the stress-strain effects at temperatures below M_f and to validate the one-way hysteresis of the model. As shown in the room temperature results in figure 12, the strain follows an irreversible path during the stress relaxation phase of the cycle, returning to linear elasticity following the turn-around points. Hysteresis loops that appear in the data during the stress relief cycle are believed to be a result of partial recovery of ζ_s as stress reaches zero, i.e., a partial two-way effect. Nevertheless, it is encouraging that the stress-strain output upon stress reversal initially follows a slope very close to E_M , as confirmed by moduli taken at the initial portions of the reversal curves in table III. It should be noted that, because the data was taken at room temperature, the average modulus more closely approximates modulus data taken on room temperature samples, a slightly larger value than the E_M at 200 °C used in the model.

TABLE III.—ELASTIC MODULI DETERMINED FROM STRESS-CYCLING TEST

Cycle number	Modulus (decreasing), ksi	Modulus (increasing), ksi
1	13437	13048
2	11034	12054
3	10616	12001
4	10267	11199
5	11202	10655
6	11894	10945
Average modulus	11529	
Mart. modulus at room temperature	12000	

In all of the phenomenological models, the two-way recovery critical stresses are in the material's compression region. The Tanaka model (ref. 24), upon which the Liang & Rogers and Brinson models are based, uses exponential relationships that are capable of preserving the continuous nature of phase transformations. However the latter's models have replaced the exponential with a piecewise continuous cosine relationship to avoid numerical convergence problems of the exponential. As shown in figure 13, the piecewise nature of the Liang & Rogers and Brinson models require that the material exhibit linear elasticity between σ_s^{cr} and $\sigma_s'^{cr}$, therefore permitting exclusion of $\sigma_s'^{cr}$ from the model. Without

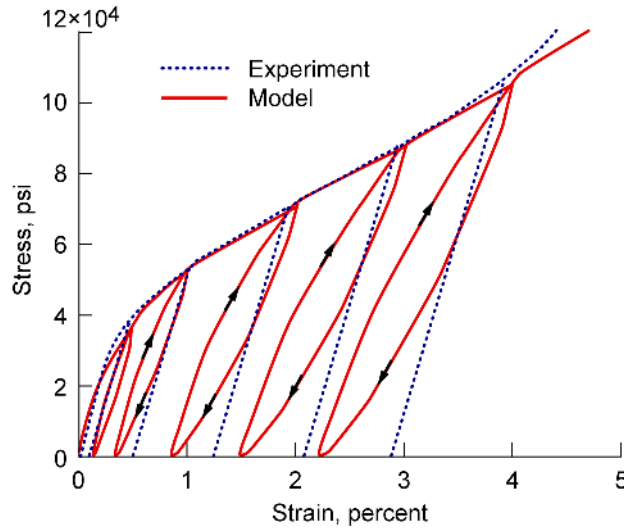


Figure 12.—Room temperature load cycling test for a $\text{Ni}_{30}\text{Pt}_{20}\text{Ti}_{50}$ HTSMA.

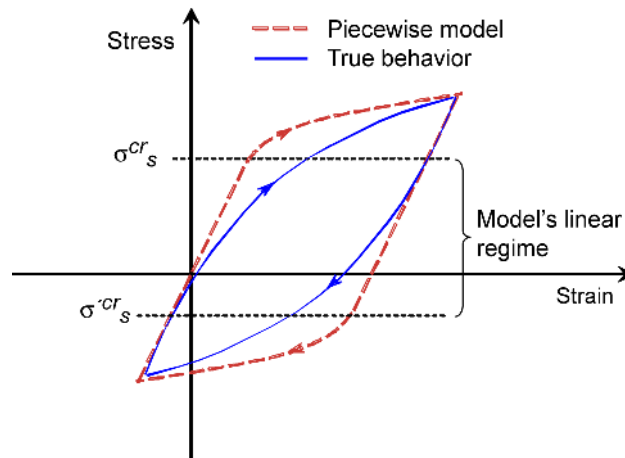


Figure 13.—Partial strain recovery model phenomenology.

substantial modification, these models are incapable of predicting these partial recovery loops due to this oversimplification of linear behavior. Although problems with the piecewise model has been acknowledged and addressed in the literature (as it also occurs with NiTi alloys) (refs. 7, 12, and 18), as yet there are no reported solutions to the issue.

6. Conclusions

In this paper, a simple, computationally efficient numerical model of a shape memory alloy material is developed. The model consists of a constitutive model with transformation kinetics and a novel minor loop hysteresis model. In the transformation kinetics relationships, Brinson's formulation was modified from original form to remove discontinuities in the response. For the hysteresis model, an algorithmic representation of hysteresis is proposed as an alternative to generalized Preisach methods that require a

database of first order descending curves to properly identify the hysteresis distribution profile. As such, the present model is conducive to simplified identification methods for new shape memory alloy (SMA) materials such as the recently-developed high-temperature SMA. The hysteresis algorithm is implemented as a modular component so that any supplemental models (i.e., heat transfer, transformation kinetics, constitutive equations) may be independently modified or freely interchanged.

The parameterized model was empirically verified to obey two established Preisach properties: the *minor loop congruency property* and the *wiping out property*. These tests were sufficient to validate the behavior of the hysteresis model itself in comparison with existing quasi-static Preisach models. More complex loading profiles were also evaluated, with the outcome that the model is well-suited for controls analysis and evaluation. Low-temperature stress cycling was validated against a set of experimental data, demonstrating agreement with the model over the operating range of interest.

As a result of this thorough evaluation of the model, insight can be gained as to the future work that may be pursued:

1. modification of amplitude thresholding to prevent noise from producing excessive errors in scaling factor;
2. inclusion of partial recovery minor loops, not captured by the present model; and
3. thorough validation against an exhaustive data set of a “benchmark” high-temperature alloy.

The present model is well adept for prototype design and evaluation of high-temperature shape memory alloy (HTSMA) actuators. Pending experimental validation, the model may also be used for proportional control system design, as a result of the inclusion of path-dependent minor hysteresis loops. It is envisaged that the model can be applied to simulate the behavior of a broad range of passive or active actuation devices utilizing HTSMA or other research-stage materials.

References

1. Pitt, D.M., Dune, J.P., White, E.V., and Garcia, E., “Wind tunnel demonstration of the SAMPSON smart inlet,” *Proceedings of SPIE International Symposium on Smart Structures and Materials*, Vol. 4332, pp. 345–356, June 2001.
2. Rey, N.M., Tillman, G., Miller, R.M., Wynosky, T., Larkin, M.J., Flamm, J.D., and Bangert, L.S., “Shape memory alloy actuation for a variable area fan nozzle,” *Proceedings of SPIE International Symposium on Smart Structures and Materials*, Vol. 4332, pp. 371–382, June 2001.
3. DeCastro, J.A. and Melcher, K.J., “A study on the requirements for fast active turbine tip clearance control systems,” AIAA Paper 2004–4176.
4. Melcher, K.M. and Kypuros, J.A., “Toward a fast-response active turbine tip clearance control,” *Proceedings of the International Symposium on Air Breathing Engines*, ISABE 2003–1102, 2003.
5. Saadat, S., Salichs, J., Noori, M., Hou, Z., Davoodi, H., Baron, I., Suzuki, Y., and Masuda, A., “An overview of vibration and seismic applications of NITI shape memory alloy,” *Journal of Smart Materials and Structures*, Vol. 11, No. 2, pp. 218–229, 2002.
6. Singh, K., Sirohi, J., and Chopra, I., “An improved shape memory alloy actuator for rotor blade tracking,” *Journal of Intelligent Material Systems and Structures*, Vol. 14, pp. 767–786, December 2003.
7. Chopra, I., “Review of state of art of smart structures and integrated systems,” *AIAA Journal*, Vol. 40, No. 11, pp. 2145–2187, 2002.
8. Lockyer, A.J., Martin, C.A., Lindner, D.K., Walia, P.S., and Carpenter, B.F., “Power system and requirements for integration of smart structures into aircraft,” *Journal of Intelligent Material Systems and Structures*, Vol. 15, pp. 305–315, April 2004.
9. Majima, S., Kodama, K., and Hasegawa, T., “Modeling of shape memory alloy actuator and tracking control system with the model,” *IEEE Transactions on Control System Technology*, Vol. 9, No. 1, pp. 54–59, 2001.

10. Ma, N. and Song, G., "Control of shape memory alloy actuator using pulse width modulation," *Journal of Smart Materials and Structures*, Vol. 12, No. 5, pp. 712–719, 2003.
11. Ma, N., Song, G., and Lee, H-J, "Position control of shape memory alloy actuators with internal electrical resistance feedback using neural networks," *Journal of Smart Materials and Structures*, Vol. 13, No. 4, pp. 777–783, 2004.
12. Sittner, P., Stalmans, R., and Tokuda, M., "An algorithm for prediction of the hysteretic responses of shape memory alloys," *Journal of Smart Materials and Structures*, Vol. 9, No. 4, pp. 452–465, 2000.
13. Mayergoyz, I.D and Friedman, G., "Generalized Preisach model of hysteresis," *IEEE Transactions on Magnetics*, Vol. 24, No. 1, pp. 212–217, 1988.
14. Hughes, D. and Wen, J.T., "Preisach modeling of piezoceramic and shape memory alloy hysteresis," *Journal of Smart Materials and Structures*, Vol. 6, No. 3, pp. 287–300, 1997.
15. Choi, B.-J., Lee, Y.-J., and Choi, B.-Y., "Fast Preisach modeling method for shape memory alloy actuators using major hysteresis loops," *Journal of Smart Materials and Structures*, Vol. 13, No. 5, pp. 1069–1080, 2004.
16. Madill, D.R. and Wang, D., "Modeling and L2-stability of a shape memory alloy position control system," *IEEE Transactions on Control System Technology*, Vol. 6, No. 4, pp. 473–481, 1998.
17. Casoria, S., Brunelle, P., and Sybille, G., "Hysteresis modeling in the Matlab/Power System Blockset," *Mathematics and Computers in Simulation*, Vol. 63, No. 3, pp. 237–248, 2003.
18. Prahlad, H. and Chopra, I., "Comparative evaluation of shape memory alloy constitutive models with experimental data," *Journal of Intelligent Material Systems and Structures*, Vol. 12, pp. 383–395, June 2001.
19. DeCastro, J.A., Melcher, K.J., and Noebe, R.D., "System-level design of a shape memory alloy actuator for active clearance control in the high pressure turbine," AIAA Paper 2005–3988.
20. Liang, C. and Rogers, C.A., "One-dimensional thermomechanical constitutive relations for shape memory material," *Journal of Intelligent Material Systems and Structures*, Vol. 1, pp. 207–234, April 1990.
21. Brinson, L.C., "One dimensional constitutive behavior of shape memory alloys: thermomechanical derivation with non-constant material functions," *Journal of Intelligent Material Systems and Structures*, Vol. 4, pp. 229–242, April 1993.
22. Noebe, R.D., Gaydosch, D., Padula, S., Garg, A., Biles, T., Nathal, M., "Properties and potential of two (Ni,Pt)Ti alloys for use as high-temperature actuator materials," *Proceedings of SPIE Smart Structures and Materials 2005: Active Materials: Behavior and Mechanics*, Vol. 5761, pp. 364–375, May 2005.
23. Epps, J. and Chopra, I., "Comparative evaluation of shape memory alloy constitutive models with test data," AIAA Paper 97–1194.
24. Tanaka, K., "A thermodynamical sketch of shape memory effect: one-dimensional tensile behavior," *Res. Mechanica*, Vol. 18, pp. 251–263, 1986.

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13. ABSTRACT (<i>Maximum 200 words</i>) A thermomechanical hysteresis model for a high-temperature shape memory alloy (HTSMA) actuator material is presented. The model is capable of predicting strain output of a tensile-loaded HTSMA when excited by arbitrary temperature-stress inputs for the purpose of actuator and controls design. Common quasi-static generalized Preisach hysteresis models available in the literature require large sets of experimental data for model identification at a particular operating point, and substantially more data for multiple operating points. The novel algorithm introduced here proposes an alternate approach to Preisach methods that is better suited for research-stage alloys, such as recently-developed HTSMAs, for which a complete database is not yet available. A detailed description of the minor loop hysteresis model is presented in this paper, as well as a methodology for determination of model parameters. The model is then qualitatively evaluated with respect to well-established Preisach properties and against a set of low-temperature cycled loading data using a modified form of the one-dimensional Brinson constitutive equation. The computationally efficient algorithm demonstrates adherence to Preisach properties and excellent agreement to the validation data set.				
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