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Dielectronic and Trielectronic Recombination Rate Coefficients of

Be-Like Ar¹⁴⁺

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ABSTRACT

Electron-ion recombination of Be-like ⁴⁰Ar¹⁴⁺ has been measured by employing the 17 electron-ion merged-beams method at the cooler storage ring CSRm. The measured 18 19 absolute recombination rate coefficients for collision energies from 0 to 60 eV are presented, covering all dielectronic recombination (DR) resonances associated with 20 $2s^2 \rightarrow 2s^2p$ core transitions. In addition, strong trielectronic recombination (TR) 21 resonances associated with $2s^2 \rightarrow 2p^2$ core transitions were observed. Both DR and TR 22 processes lead to series of peaks in the measured recombination spectrum, which have 23 been identified by the Rydberg formula. Theoretical calculations of recombination rate 24 25 coefficients were performed using the state-of-the-art multi-configuration Breit-Pauli (MCBP) atomic structure code AUTOSTRUCTURE to compare with the experimental 26 results. The plasma rate coefficients for DR+TR of Ar¹⁴⁺ were deduced from the 27 measured electron-ion recombination rate coefficients in the temperature range from 28 10³ to10⁷ K, and compared with calculated data from the literature. The experimentally-29 derived plasma rate coefficients are 60% larger and 30% lower than the previously 30 recommended atomic data for the temperature ranges of photoionized plasmas and 31 collisionally-ionized plasmas, respectively. However, good agreement was found 32 between experimental results and the calculations by (Gu 2003) and (Colgan et al. 33 2003). The plasma rate coefficients deduced from experiment and calculated by the 34 current AUTOSTRUCTURE code show agreement that is better than 30% from 10^4 35 to10⁷ K. The present results constitute a set of bench-mark data for use in astrophysical 36 modeling. 37

38 *Keywords:* atomic data – atomic processes - plasmas

1. INTRODUCTION

It has been estimated that more than 90% of the visible matter in the universe is in 40 plasma state (Müller 2008). Astrophysical plasmas can be divided into two main classes, 41 i) the collisionally ionized plasma formed in stars, supernova remnants and galaxies, 42 43 and ii) photoionized plasmas formed in the sources such as planetary nebulae, X-ray 44 binaries and active galactic nuclei. Various types of reactions take place in astrophysical plasmas, such as electron collision excitation, electron impact ionization, and electron-45 ion recombination (Savin 2007). Emission features originating from these plasmas are 46 essential in deducing the properties of the plasmas, such as temperature, density and 47 elemental abundances (Beiersdorfer 2003; Kallman & Palmeri 2007). Electron-ion 48 recombination processes such as radiative recombination (RR) and dielectronic 49 50 recombination (DR) contribute substantially to the line emission for photoionized plasmas. In addition, the ionization balance of a plasma is determined by the relative 51 rates of ionization and recombination. 52

In order to understand astrophysical plasmas, space-based observatories, such as 53 54 Chandra and XMM-Newton, have been launched to observe x-ray emission from various astrophysical objects (Paerels & Kahn 2003). All the observed emission and 55 absorption lines have to be explained by plasma modelling, and most of the input atomic 56 data for these plasma models are from theory. However, many theories cannot calculate 57 the DR rate coefficients with sufficient precision and have large uncertainties especially 58 59 at low energies due to sensitivity in the positioning of resonances. As a result, precise electron-ion recombination data from experiment are required to explain the 60 astrophysical observations and to benchmark the theory. With these data, information 61 pertaining to these astrophysical objects, such as the structure, elemental composition, 62 63 energy balance, and temperature distribution, can be investigated (Kallman & Palmeri 64 2007).

The importance of DR in a plasma was recognized for the first time by Burgess in 65 66 1964 (Burgess 1964). Since then, DR is considered as an important process in atomic physics and plasma physics. DR experiments on highly charged ions employing the 67 electron-ion merged beams technique have been developed for more than two decades 68 69 at heavy ion storage rings, i.e., the TSR at MPIK in Heidelberg (Schippers 2015), the ESR at GSI in Darmstadt (Brandau & Kozhuharov 2012), Germany, and the CRYRING 70 at MSL in Stockholm, Sweden (Schuch & Böhm 2007). The main cooler storage ring 71 (CSRm) equipped with an electron cooler provides an ideal research platform for 72 electron-ion recombination experiments of highly charged ions at heavy ion research 73

facility in Lanzhou (Huang et al. 2017). More details about DR experiments at storage
rings can be found in the recent reviews of (Brandau & Kozhuharov 2012; Brandau et
al. 2015; Müller 2008; Schippers 2015) and in the references cited therein. Recent
reviews of experimental DR measurements for astrophysics application have been
given by (Schippers 2012).

79 Argon is one of the most abundant heavy elements in the universe and also in the solar system. The emission lines from argon have already been observed and were used 80 for plasma diagnostics (Dere et al. 2001). In addition, Be-like argon has been observed 81 in hot solar plasmas where the temperature is $\sim 10^6$ K (Bhatia & Landi 2008). The 82 intensity ratios of the emission lines from Ar¹⁴⁺ were used to diagnose coronal plasmas 83 84 (Landi et al. 2001; Saloman 2010). Therefore, investigating the recombination of Be-85 like Ar will provide very useful information for astrophysics. It is noted that the emission lines from highly charged argon have been investigated at an electron beam 86 ion trap EBIT (Lepson et al. 2003; Träbert et al. 2000). Here, we present absolute rate 87 coefficients for electron-ion recombination of Be-like argon from an experiment at the 88 main cooler storage ring CSRm and from theoretical calcuations using the 89 90 AUTOSTRUCTURE code.

For Be-like Ar¹⁴⁺, the experimental electron-ion collision energy range was 0-60 eV.
The most significant recombination channels in this energy range are

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$$\begin{aligned}
\text{Ar}^{13+}(2s^2 \cdot S_0) + e &\to \\
& \left\{ \begin{array}{l} \text{Ar}^{13+}[2s^2nl], \ \text{RR}; \\ \text{Ar}^{13+}[2s2p(^{3}P_{0,1,2})nl], \ n \ge 10, \ \text{DR}; \\ \text{Ar}^{13+}[2s2p(^{1}P_{1})nl], \ n \ge 7, \ \text{DR}; \\ \text{Ar}^{13+}[2p^{2}(^{3}P_{0,1,2}; ^{1}D_{2}; ^{1}S_{0})nl], \ n \ge 6, \ \text{TR}; \end{array} \right\} \end{aligned} \tag{1}$$

where RR, DR, and TR denote radiative, dielectronic, and trielectronic recombination, 94 95 respectively. In RR, a free electron is captured into a bound state of the ion and a photon is emitted. DR is a two-step process, a doubly excited intermediate state is formed 96 through a resonant process involving capture of a free electron and simultaneous 97 excitation of a bound electron, then the doubly excited state decays via photon emission 98 99 such that the charge state of the recombined ion is stablized. In the case of TR, the capture is associated with the excitation of two core electrons to higher levels, and 100 completed when the triply excited intermediate level decays by photon emmision. The 101 excitation energies of the core electrons and lifetimes associated with $\Delta N = 0$ (Here N 102 103 is the principal quantum number of the transition core electron) DR and TR are listed in Table 1. 104

Table 1. Excitation energies and lifetimes for $\Delta N=0$ of Be-like Ar¹⁴⁺ levels. Numbers in brackets denote powers of 10. The data cited from NIST is from the reference (Kramida et al. 2015).

	Energy		Lifetime
Level	NIST	(Wang et al. 2015)	
_	(eV)	(eV)	(s)
$1s^2 2s^2 {}^1S_0$	0.00000	0.00000	∞
$1s^2 2s 2p {}^3P_0$	28.3530	28.3604	4.2[6] ^a
$1s^2 2s 2p {}^3P_1$	29.2429	29.2509	3.436[-07]
$1s^2 2s 2p {}^3P_2$	31.3283	31.3383	1.543[-02]
$1s^2 2s 2p P_1$	56.0630	56.0704	1.070[-10]
$1s^2 2p^2 {}^3P_0$	75.0000	75.0125	1.432[-10]
$1s^2 2p^2 {}^3P_1$	76.2776	76.2740	1.369[-10]
$1s^2 2p^2 {}^3P_2$	77.9000	77.9070	1.345[-10]
$1s^2 2p^2 {}^1D_2$		85.4889	4.789[-10]
$1s^2 2p^2 {}^1S_0$	104.224	104.196	6.9199[-11]

^alifetime associated with E1M1 two photon transition taken from (Fritzsche, Surzhykov, &
Volotka 2015)

Storage-ring electron-ion recombination experiments have been performed on a 111 number of Be-like ions emphazising different physical topics. Astrophysical data needs 112 were specifically addressed with DR studies of C^{2+} , N^{3+} , O^{4+} (Fogle et al. 2005), F^{5+} 113 (Ali et al. 2013), Ne⁶⁺ (Orban et al. 2008), Mg⁸⁺, (Schippers et al. 2004), Si¹⁰⁺ 114 (Bernhardt et al. 2016; Orban et al. 2010), and Fe²²⁺ (Savin et al. 2006). Other topics 115 were trielectronic recombination of Cl¹³⁺ (Schnell et al. 2003) and hyperfine-induced 116 transition rate measurements with Ti^{18+} (Schippers et al. 2007) and S^{12+} (Schippers et 117 al. 2012). In addition, the Be-like ions Ge^{28+} (Orlov et al. 2009) and Xe^{50+} (Bernhardt 118 et al. 2015) were employed to test QED and electron-electron correlation effects. It is 119 noted that the significance of TR was first observed for Be-like Cl¹³⁺ (Schnell, et al. 120 2003) and subsequently confirmed for several ions from this isoelectronic sequence. 121 For Be-like Mg, a distinct contribution from TR in the form of several sharp peaks was 122 also found (Schippers, et al. 2004). Toward higher Z ions, some TR resonance features 123 appear in the recombination spectrum of Ti¹⁸⁺ (Schippers, et al. 2007) whereas in case 124 of Fe²²⁺ only one clear peak could be attributed to TR (Savin, et al. 2006). 125 Here, we report the first measurement of the electron-ion recombination spectrum of 126

Be-like Ar. The paper is structured as follows: The experimental method and the data
analysis are presented in Section 2. In Section 3, we give a brief description of the
theoretical method used by AUTOSTRUCTURE. In Section 4, the experimental results,

including merged-beam DR rate coefficients, and also plasma rate coefficients, are
presented and compared to currently available results in the literature. A conclusion is
given in section 5.

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2. EXPERIMENT AND DATA ANALYSIS

Measurements were performed at the main cooler storage ring (CSRm) at the Institute of Modern Physics (IMP) in Lanzhou, China. A detailed description of the experimental setup and method for DR experiments at the CSRm has already been given in the literature (Huang et al. 2015; Huang, et al. 2017). Here, we will only briefly describe the electron-ion recombination experiment with Be-like Ar¹⁴⁺at the CSRm.

In the experiment ⁴⁰Ar¹⁴⁺ ions were produced from an Electron Cyclotron Resonance 139 (ECR) ion source (Zhao et al. 2017) and accelerated to a beam energy of 6.928 MeV/u 140 by a Sector Focused Cyclotron (SFC), and then were injected into the CSRm. The 141 stored ion current was typically \sim 50 μ A. The beam lifetime was about 50 seconds. The 142 electron cooler at the CSRm was employed to cool the ion beam, and was also used as 143 an electron target in the measurement. During the experiment, the ion beam was merged 144 145 with the electron beam over an effective interaction length of L= 4.0 m in the cooler section. The electron beam was adiabatically expanded from the magnetic field of 125 146 mT at the electron-gun section to 39 mT at the electron-cooling section, thus a colder 147 electron beam was generated and a higher experimental resolution could be realized. 148 The diameter of the electron beam was measured to be ~50 mm at the cooling section, 149 with typical electron densities being $n_e = 1.1 \times 10^6$ cm⁻³. 150

151 During the measurement, the injected ion beam was first electron-cooled for several seconds in order to decrease the diameter and the momentum spread of the ion beam. 152 Then the electron energy detuning system added a bias voltage to the cathode voltage 153 154 of the electron cooler to scan the electron beam energy according to a preset timing sequence (Meng et al. 2013). This provided a nonzero relative kinetic energy between 155 electrons and ions. Downstream of the electron cooler, the recombined ions were 156 separated from the primary ion beam in the first bending magnet and detected by a 157 movable scintillator particle detector with nearly 100% efficiency (Wen et al. 2013). 158 During the measurement, a DC current transformer (DCCT) was used to monitor the 159 160 ion beam current in real time. Ion and electron beam position monitors (BPM) were utilized to monitor the relative positions of the ion beam and the electron beam in the 161 cooling section. All of the DR measurements were performed under the condition of 162 keeping the electron beam and ion beam parallel along the axis of the cooler. In addition, 163 164 a Schottky pick-up was employed to monitor the revolution frequency and the

momentum spread of the ion beam, and to correct the experimental data in the off-linedata analysis (Wu et al. 2013).

167 In the DR experiments at heavy ion storage rings, the recombination rate coefficients 168 α can be deduced from the background subtracted recombination counting rate *R* at a 169 relative energy E_{rel} between electron and ion by (Bernhardt et al. 2011):

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$$\alpha(E) = \frac{R}{N_i n_e (1 - \beta_e \beta_i)} \cdot \frac{C}{L}$$
(2)

where N_i is the number of stored ions, n_e is the density of electron beam, $\beta_e = v_e/c$ and $\beta_i = v_{ion}/c$ are the velocities of electron beam and ion beam, *L* is length of the effective interaction section, and *C* is the circumference of the storage ring.

174 **3. THEORY**

For a better understanding of the measured electron-ion recombination spectrum, a 175 theoretical calculation using the distorted-wave collision package AUTOSTRUCTURE 176 (Badnell 2011) was performed to calculate recombination cross-sections and rate 177 coefficients. AUTOSTRUCTURE is a versatile code that is able to calculate energy 178 levels, oscillator strengths, radiative/autoionization rates, and many other quantities 179 using semi-relativistic kappa-averaged wavefunctions. The underlying theory 180 implemented by AUTOSTRUCTURE for DR is well documented, however, we discuss 181 it briefly here. For a target ion $X_{\nu}^{(Q)}$ with a residual charge Q, and initial state ν , 182 colliding with an electron and recombining into an ion $X_f^{(Q-1)}$ with final state f, the 183 partial DR cross section σ_{fv}^Q , energy averaged over a bin width ΔE_c , can be expressed 184 185 as

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$$\sigma_{f\nu}^Q(E_c) = \frac{(2\pi a_0 I_H)^2 \tau_0}{E_c} \sum_j \frac{\omega_j}{2\omega_\nu} \frac{\sum_l A_{j\to\nu,E_cl}^a A_{j\to\ell}^r}{\sum_h A_{j\to h}^r + \sum_{m,l} A_{j\to m,E_cl}^a},$$
(3)

where ω_{ν} and ω_{i} are the statistical weights for the N - and (N + 1) - electron 187 states respectively. The A^r and A^a are the radiative and autoionization rates 188 respectively, and E_c is the energy of the continuum electron with angular momentum 189 l, fixed by the position of the resonances. I_H is the ionization energy of the hydrogen 190 atom, k_B is the Boltzmann constant, and $(2\pi a_0)^2 \tau_0 = 2.6741 \times 10^{-32} \text{cm}^2 \text{s}$. The 191 sum over l covers the angular momentum quantum numbers of the Rydberg electron. 192 The sum over i covers all autoionization states. Lastly, the sum over h and m193 represents the total radiative and autoionization widths respectively. 194

For the N –electron core configurations, we included $2s^2$, 2s2p, and $2p^2$, and for 195 the (N+1)-electron, we included $2s^22p$, $2s2p^2$, and $2p^3$. No promotions from $1s^2$ 196 are included, and are hence omitted from the configuration list. For the recombined 197 Rydberg electron, radiative/autoionization rates were calculated explicitly for principal 198 quantum numbers n = 3 up to n = 100, after which the rates were calculated for 199 200 quasi-logarithmically spaced values of n up to n = 1000. Interpolation was then used to obtain the remaining n. For each n, we calculated radiative/autoionization rates 201 202 for sufficiently many angular momentum quantum numbers l so as to numerically converge the total DR rate coefficient to <1% over the temperature range 203 $Q^2(10-10^6)$ K. 204

In order to compare with the experimentally-derived electron-ion recombination rate coefficients on the one hand and to calculate the plasma rate coefficient on the other hand, the calculated recombination cross section $\sigma(\upsilon)$ has to be convoluted with the appropriate electron-velocity distribution to obtain the rate coefficients,

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$$\alpha(E) = \langle \upsilon \sigma \rangle = | \upsilon \sigma(\upsilon) f(\upsilon) d^3 \upsilon$$
 (4)

where $f(\upsilon)$ is the electron-velocity distribution. In case of the merged-beams rate coefficient, it is a flattened Maxwellian (Kilgus et al. 1992) that is characterized by the longitudinal and transverse temperatures T_{\parallel} and T_{\perp} with respect to the propagation direction of the electron beam. In case of the plasma rate coefficient, $f(\upsilon)$ is an isotropic Maxwellian characterized by the electron temperature T_e of the plasma.

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4. RESULTS AND DISCUSSION

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4.1 Merged-beams DR rate coefficients

The DR spectra of Be-like 40 Ar¹⁴⁺ obtained from the DR experiment at the CSRm and from the AUTOSTRUCTURE calculations are compared and shown in Figure 1. The measured spectrum covers the whole energy range of DR resonances associated from $2s \rightarrow 2p$ ($\Delta N=0$) core excitations. In the recombination spectrum, the resonance positions of each Rydberg state can be well approximated by the Rydberg formula:

$$E_{res} = E_{exc} - I_H \left(\frac{Q}{n}\right)^2$$
(5)

where E_{exc} is the core excitation energy of the ions, which is taken from the NIST database. I_H is the ionization energy of the hydrogen atom, and Q is the charge state of the target ion. The associated Rydberg resonance series of the doubly excited intermediate levels $2s2p({}^{1}P_{1})nl$ and $2s2p({}^{3}P_{J})nl$ are indicated by vertical bars. In Figure

1 the experimental energy scale was recalibrated by a factor of 1.06 to achieve 227 agreement with the known $2s2p({}^{1}P_{1})nl$ series limit at 56.063 eV. As shown in Figure 2, 228 by fitting the first 13 resonance peaks at relative energy below 0.5 eV with a flattened 229 Maxwellian function each (Kilgus, et al. 1992), the longitudinal and transversal 230 electron temperatures were obtained, yielding $k_B T_{\parallel} = 2.40(6)$ meV and $k_B T_{\perp} = 11.91(87)$ 231 meV, respectively. The peak fit results are listed in Table 2. The numbers in parentheses 232 denote the uncertainties obtained from the fit and correspond to one standard deviation. 233 From the fit, it is concluded that the experimental energy resolution is less than 0.07 eV 234 full width at half maximum at relative energies around 0.2 eV. 235



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Figure 1. Electron-ion recombination rate coefficients of Be-like argon as a function of relative 237 collision energy. The energy scale of the experimental spectrum (connected filled circles) was 238 recalibrated by a factor of 1.06 to achieve agreement with the known 2s2p (¹P₁) nl series limit 239 at 56.063 eV. Four $\Delta N = 0$ DR series associate with $2s^2 \rightarrow 2s2p$, 1P_1 , ${}^3P_{0,1,2}$ core excitations and 240 parts of five $\Delta N = 0$ TR series $(2s^2 \rightarrow 2p^2, {}^{1}S_0, {}^{1}D_2, {}^{3}P_{0,1,2})$ can be observed. The corresponding 241 242 resonance positions are indicated by short bars in different colors. The calculated DR and TR rate coefficients are shown by the gray area and the blue area, respectively. The sum of the 243 244 theoretical DR and TR contribution is shown as a solid red line. This curve accounts for the 245 experimental field-ionization cutoff (see text). The orange line from 45 eV to 60 eV is the theoretical result including the full DR resonance strength up to $n_{max}=1000$, called the field-246 ionization-free recombination rate coefficient. 247



Figure 2. Peak fit (the solid pink line) to the experimental low-energy DR rate coefficient (black filled symbols). In the fit 13 δ -like resonances were convoluted with a flattened Maxwellian electron-energy distribution which is characterized by the temperatures T_{\parallel} and T_{\perp} in longitudinal and transversal direction, respectively, with respect to the electron beam propagation direction. The fit resulted in $k_{\rm B}T_{\parallel}$ =2.40(6) meV and $k_{\rm B}T_{\perp}$ =11.91(87) meV. The individual peaks are shown as dashed pink lines. The fitted resonance energies and strengths are given in Table 2.

256	Table 2. Results of the peak fits to the experimental merged-beams DR rate coefficient at
257	electron-ion collision energy below 3 eV (see Figure 2). The numbers in parentheses denote the
258	uncertainties obtained from the fit and correspond to one standard deviation.

Resonance energy (eV)	Resonance strength	
	$(10^{-18} \text{ cm}^2 \text{ eV})$	
0.08269(84)	10.57(15)	
0.14436(88)	13.32(15)	
0.23232(94)	17.78(17)	
0.3173(14)	8.25(17)	
0.629(18)	0.57(12)	
0.805(21)	0.56(12)	
1.091(17)	11.51(17)	
1.2786(63)	0.44(16)	
1.450(18)	3.46(53)	
1.6524(62)	17.27(41)	
1.8005(85)	6.19(65)	
2.1714(74)	2.58(12)	
2.5327(52)	3.81(12)	

In the experiment, the recombined ions have to travel through a toroidal magnet,

three quadrupole magnets and a dipole magnet before their detection. The electric field

arising from these **magnetic fields can ionize** the recombined ions in high-*n* Rydberg levels. As a result, the ions recombining into states with the outer electron having a principal quantum number $n > n_{cutoff}$ will be field-ionized in the sperating dipole magnet and cannot be detected. The critical quantum number n_{cutoff} for field ionization of an ion in a magnetic field can be estimated from the formula (Fogle, et al. 2005)

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$$n_{cutoff} \simeq \left(6.2 \times 10^8 \, V/cm \frac{Q^3}{v_i B}\right)^{1/4} \tag{6}$$

where *Q* is the charge state of the ion, v_i is the ion velocity, and *B* is the magnetic field strength. In the present experiment the estimated cutoff quantum number in the charge separating dipole magnet is n_{cutoff} =74. The field-ionization effect can be seen at the series limits of $2s2p({}^{1}P_{1})nl$ around 55 eV in Figure 1. Compared with the $2s2p({}^{1}P_{1})nl$ series, the $2s2p({}^{3}P_{J})nl$ series limits were not observed in the DR spectra.

To fully understand the measured electron-ion recombination rate coefficients a 272 convolution of the calculated DR resonance cross sections with the velocity distribution 273 of the electron beam was performed by AUTOSTRUCTURE as described in Section 3. 274 275 The gray area shows the theoretical DR rate coefficients with taking field ionization into account. It turns out that the resonance peaks around 0.5 eV, 4 eV and 11 eV cannot 276 be fully identified by considering only the $2s2p({}^{1}P_{1})nl$ and $2s2p({}^{3}P_{J})nl$ DR series 277 (Figure 1). These peaks can be attributed to TR associated $2s^2 \rightarrow 2p^2$ (1S_0 , 1D_2 , ${}^3P_{0,1,2}$) 278 core double-excitations as revealed by a separate calculation of TR contributions. The 279 280 calculated TR rate coefficients is shown as the blue shaded area in Figure 1. The sum of the calculated DR and TR rate coefficients is shown as a solid red line. This curve 281 account for field ionization, i.e, it contains contribution of recombination resonance 282 from Rydbergy levels up to 150 by taken into account of time-of-flight survival 283 probabilities for n, as described in (Schippers et al. 2001). An additional calculation 284 285 including DR and TR contributions from capture into Rydberg states up to $n_{max}=1000$ from 45 eV to 60 eV is shown in Figure 1 as a solid orange line, called the field-286 ionization-free electron-ion recombination rate coefficient. Agreement between 287 calculated results and experimental rate coefficients was found that better than 30% for 288 the whole energy range. However, there is a discrepancy in resonance positions and 289 290 intensity at energy less than 0.5 eV. It is due to electron-electron correlation effects. The intensity of resonances at 11 eV and 23 eV is not well produced by 291 AUTOSTRUCTURE, either. 292

It should to be noted that, Be-like ions are known to have long-lived 2s2p $^{3}P_{J}$ levels (J=0, 1, 2) which might be present in the ion beams used for the experiment. For Be-

like ${}^{40}\text{Ar}^{14+}$ ion which has zero nuclear spin, the lifetimes of energy levels of $2s2p({}^{3}P_{1})$ 295 and $2s2p({}^{3}P_{2})$ are very short (as listed in Table 1) and these two metastable levels will 296 not survive as the measurements were performed after several seconds of electron-297 cooling. However, the lifetime of metastable level ${}^{3}P_{0}$ is very long and can only decay 298 by E1M1 two-photon transition. As a result, ions in the metastable state of ${}^{3}P_{0}$ are 299 expected to have been present in the ion beam during the experiment. In order to 300 determine the rate coefficient for the ground level of the ion, the contribution from the 301 metastable level should be considered. However, in case of the Be-like Ar¹⁴⁺ there is 302 an unknown fraction of metastable ions in the primary beam. As described in (Orban, 303 et al. 2008), ion beams extracted from ECR ion sources showed a decreasing percentage 304 305 of metastable content with increasing charge along the Be-like isoelectronic sequence. The metastable contents amount to 60%, 40%, 35%, 14% and 10% for C²⁺, N³⁺, O⁴⁺, 306 Ne⁵⁺ and Si¹⁰⁺ ion beams, respectively (Orban, et al. 2008; Orban, et al. 2010). Since 307 we have also used an ECR ion source in this experiment, we estimated the maximum 308 metastable contents amount to be 5% in the case of Be-like Ar^{14+} in our experiment. In 309 addition, a separate calculation of electron-ion recombination for 2s2p (³P₀) metastable 310 ions by AUTOSTRUCTURE was performed. In the range of the $\Delta N=0$ DR resonances, 311 the calculation showed very weak metastable DR resonant strengths and its contribution 312 can be safely neglected. However, at high temperature the metastable contribution to 313 314 the plasma rate coefficient becomes comparable with that from the ground because of 315 the strong 2p-3d promotion.

The uncertainty of the experimental recombination rate coefficients is estimated to be about 30% (at a one-sigma confidence level), including 5% uncertainty of the estimated metastable content of the Ar^{14+} ions, an uncertainty of 15% due to combination of counting statistics, electron and ion beam currents, and interaction length, and an uncertainty of 20% due to the electron density distribution profile and also the position of the ion beam in this profile.

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4.2 Plasma recombination rate coefficients

As mentioned above, storage ring measured electron-ion recombination rate coefficients are different from the plasma rate coefficients which were used for astrophysics modelling. In contrast to the very narrow velocity spread of the electron beam in a storage ring experiment, the electrons in astrophysical plasmas have a much broader and isotropic Maxwellian velocity spread. Therefore, the plasma rate coefficient can be obtained by convoluting the DR cross section $\sigma(E)$ with a Maxwell-Boltzmann distribution characterized by the plasma electron temperature T_e (see Eq. 4,

with $E = m_e v^2/2$ and electron rest mass m_e). At electron-ion energies $E >> k_B T_{\perp}$ the DR 330 cross section $\sigma(E)$ can be obtained as $\alpha(E)/\nu$ where $\alpha(E)$ denotes the measured merged-331 beams rate coeffcient. At lower energies the influence of the experimental energy 332 spread becomes noticeable and, consequently, a different approach for the derivation 333 of the plasma rate coefficient has to be applied. Here, this concerns about the four 334 335 lowest-energy resonances from Table 2. In particular, the lowest-energy resonance appears at an energy lower than $k_{\rm B}T_{\perp}$. For these resonances, the DR cross section as 336 obtained from the peak fit was used in the convolution procedure following the 337 procedure laid out by (Schippers, et al. 2004). 338

The experimentally-derived and theoretically calculated plasma rate coefficients as a 339 340 function of electron temperature are shown in Figure 3 as the solid red line and the shortdashed red line, respectively. Both lines account for the field-ionization effect discussed 341 above. The theoretically calculated DR and TR contributions are shown in Figure 3 by 342 the black dashed line and the blue dot-dashed line, respectively. In order to compare the 343 experimental result to different theoretical models, the experimental recombination rate 344 coefficient from 45 eV to 60 eV was replaced by the AUTOSTRUCTURE calculation 345 including recombination into states up to $n_{max}=1000$ (the solid orange line in Figure 1). 346 Such a derived field-ionization-free plasma rate coefficient is shown as a gray shaded 347 area in Figure 3. It should be noted that the contribution from recombination into 348 349 resonance levels with n > 1000 was considered very small and can be safely neglected.

The temperature range is from 10^3 K to 10^7 K in Figure 3. It includes the ranges of 350 photoionized and collisionally ionized plasmas for Be-like Ar. The boundaries of these 351 352 temperature ranges are displayed by vertical dashed bars. These mark the temperatures where the fractional abundance of Be-like Ar is 10% of its maximum value (Bryans, 353 Landi, & Savin 2009; Kallman & Bautista 2001). At a temperature of 10³ K the TR 354 355 contribution is a factor of four larger than the DR contribution. In the temperature range of photoionized plasmas, the TR contribution to the total plasma rate coefficient 356 amounts to 10%. Finally, agreement of better than 30% for the whole temperature range 357 is found between the present experimentally-derived rate coefficients and the current 358 AUTOSTRUCTURE calculations. 359



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Figure 3. Plasma rate coefficients of Be-like Ar^{14+} as a function of the electron temperature. The 361 solid red line is the experimentally-derived $\Delta N = 0$ DR and TR rate coefficients. The theoretical 362 results deduced from the AUTOSTRUCTURE code for $\Delta N = 0$ DR and for TR are shown as a 363 dotted black line and a dash-dotted blue line, respectively. The calculated sum of DR and TR 364 is shown as a short-dashed red line. The experimentally-derived field-ionization-free plasma 365 rate **coefficient is** shown as gray area. The approximate temperature ranges where Ar^{14+} is 366 expected to form in photoionized plasmas and collisionally ionized plasmas are indicated by 367 vertical dashed bars and associated arrows (Bryans, et al. 2009; Kallman & Bautista 2001). 368

In order to compare with other recommended theoretical data in the literature and to make convenient use of the presently measured results in plasma modeling, the $\Delta N=0$ resonant plasma rate coefficients were fitted with the function

$$\alpha(T_e) = T_e^{-3/2} \sum_i c_i \times \exp(-\frac{E_i}{kT_e})$$
(7)

The fit parameters of c_i and E_i are listed in Table 3, and reproduce the data within

374 2% at $\sim 10^3$ K and better than 1% up to 10^7 K.

Table 3. Fitted coefficients for the RR-subtracted $\Delta N=0$ DR+TR rate coefficients from Figure 376 3 for two different values of n_{cutoff} and $n_{\text{max}}=1000$ (field-ionization free). The units of c_i and E_i 377 are 10^{-3} cm³ s⁻¹ K^{3/2} and eV, respectively.

No.	<i>n</i> cutoff		$n_{max}=$	1000
i	C_i	E_i	C_i	E_i
1	0.254	0.12	0.244	0.115
2	0.580	0.28	0.590	0.278
3	3.74	3.47	3.77	3.45
4	5.17	1.43	5.14	1.43
5	14.3	12.42	14.38	12.45
6	23.39	31.84	23.13	31.95

In Figure 4, the experimentally-derived field-ionization-free plasma rate coefficients 378 including DR and TR are compared with the theoretical data from the literature. The 379 temperature ranges where Ar¹⁴⁺ forms in collisionally ionized plasmas and 380 photoionized plasmas are indicated by vertical dashed bars as same as shown in Figure 381 382 3. Among the literature data, only the theoretical calculations from (Colgan, et al. 2003) and (Gu 2003) provide plasma rate coefficients at low temperatures. The calculations 383 of (Colgan, et al. 2003) used AUTOSTRUCTURE and (Gu 2003) used FAC code. It 384 should be noted that the plot of (Colgan, et al. 2003) as shown in Figure 4 is fitted by 385 using the revised fit on the website of ADAS (Badnell 2009). The other calculations 386 vielded plasma rate coefficients only at temperatures higher than 10^4 K. 387

At a temperature of 10^4 K, the calculated plasma rate coefficients from (Colgan, et al. 2003) and (Gu 2003) are 30% lower than experimental data. In the temperature range around 2×10^5 K, where Be-like Ar is expected to be abundant in photonionized plasmas, the calculated plasma rate coefficients from (Colgan, et al. 2003; Gu 2003; Romanik 1988) are 30% lower than the experimental results, and the data from (Mazzotta et al. 1998; Shull & Van Steenberg 1982) are about 60% lower than experimental data.

At a temperature of about 3×10^6 K where Ar^{14+} is **supposed** to be abundant in 394 collisionally ionized plasmas, the theoretical data of (Gu 2003) are 25% lower than the 395 experimental results. The calculated data from (Colgan, et al. 2003), (Mazzotta, et al. 396 1998), (Romanik 1988) and (Shull & Van Steenberg 1982) is 30%, 15%, 80%, and 30% 397 higher than the experimental data. Above 6×10^6 K, the calculation of (Gu 2003) is about 398 25% lower than the experimental data, but the calculations of (Colgan, et al. 2003; 399 Mazzotta, et al. 1998; Romanik 1988; Shull & Van Steenberg 1982) are all more than 400 30% higher than the experimental data. It should be noted that the calculation of (Gu 401 402 2003) shown in Figure 4 only included transitions for $\Delta N=0$, and the data from (Colgan, et al. 2003; Mazzotta, et al. 1998; Romanik 1988; Shull & Van Steenberg 1982) shown 403 in Figure 4 included the transitions for $\Delta N=0$ and $\Delta N=1$. As a result, DR through 404 excitation of the 2s electron to higher shells ($\Delta N > 0$ DR) and also through excitation 405 of a 1s electron which is not included in the experimental data could be the reason for 406 407 this discrepancy. It should be noted that better than 2% between the current calculation by AUTOSTRUCTURE code (as shown in Figure 3 as a short-dashed red line) and the 408 data from (Colgan, et al. 2003) is found if only taking into account of $\Delta N=0$ core 409 electron excitation. In a short summary, agreement within about 35% was found 410

411 between experimentally-derived plasma rate coefficients and theoretical calculations





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Figure 4. Comparison of field-ionization-free resonant plasma recombination rate coefficients 414 with theoritical calculated results of Be-like Ar. Full squares show rate coeficients by (Colgan, 415 et al. 2003). Calculations by (Gu 2003) and (Mazzotta, et al. 1998) are shown by full triangles 416 and full circles, respectively. Rate coefficients of (Romanik 1988) and (Shull & Van Steenberg 417 418 1982) are shown by full diamonds and stars, respectively. Temperature ranges where the Belike Ar concentration is higher than 10% of its maximum abundance in photoionized and 419 collisionally ionized plasmas are shown by vertical dashed bars as in Figure 3 (Bryans, et al. 420 421 2009; Kallman & Bautista 2001).

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5. CONCLUSIONS

Electron-ion recombination rate coefficients of Be-like Ar¹⁴⁺ forming into B-like 423 Ar^{13+} were derived from a measurement performed by employing the electron-ion 424 merged-beams method at the cooler storage ring CSRm. No previous experimental 425 results were available for this ion. The resonances associated with dielectronic 426 $(2s^2 \rightarrow 2s^2p)$ and trielectronic $(2s^2 \rightarrow 2p^2) \Delta N=0$ recombination within the energy range 427 of 0-60 eV were investigated and identified by application of the Rydberg formula. 428 429 Agreement in terms of DR resonance positions and strengths was found better than 10% and 30%, respectively, between the experimental recombination rate coefficient and the 430 newly calculated results using the distorted wave code AUTOSTRUCTURE. The TR 431 resonance positions and strenghts were also reproduced by the AUTOSTRUCTURE 432 433 calculation.

For use in plasma modelling, the plasma recombination rates coefficient was deduced from the merged-beams recombination rate coefficients. The temperature range of this plasma rate coefficient is from 10^3 to 10^7 K. This range comprises the temperatures

where the ions are abundant both in photoionized and collisionally ionized plasmas. 437 The experimentally-derived plasma rate coefficient was compared with the calculated 438 data from existing literature. At the temperature range of photoionized plasmas, the 439 experimentally-derived rate coefficient is still up to 30% larger than the more recent 440 results of (Gu 2003), (Romanik 1988) and (Colgan, et al. 2003). For temperatures 441 higher than 10⁶ K, the experimentally derived plasma rate coefficients are lower than 442 the calculated data from the literature except for (Gu 2003) which only showed $\Delta N=0$ 443 core electron excitation. Agreement of better than 30% for the whole temperature range 444 was found between the present experimentally-derived plasma rate coefficients and the 445 calculated results from AUTOSTRUCTURE. Our data thus provide a stringent 446 benchmark for Ar¹⁴⁺ recombination data used in astrophysical modelling. 447

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