

# Differential Evolution Algorithm with Application to Optimal Operation of Multipurpose Reservoir

Dattatray Gangaram Regulwar<sup>1</sup>, Sumant Anant Choudhari<sup>2</sup>, Pallakury Anand Raj<sup>3</sup>

<sup>1</sup>*Department of Civil Engineering, Government College of Engineering,  
Aurangabad, India*

<sup>2</sup>*Research Scholar, National Institute of Technology, Warangal, India*

<sup>3</sup>*Department of Civil Engineering, National Institute of Technology, Warangal, India*

*E-mail: {dgregulwar, sumantchoudhari}@rediffmail.com, a\_raj\_p@yahoo.co.in*

*Received March 12, 2010; revised April 7, 2010; accepted May 4, 2010*

## Abstract

This paper includes an application of Differential Evolution (DE) for the optimal operation of multipurpose reservoir. The objective of the study is to maximize the hydropower production. The constraints for the optimization problem are reservoir capacity, turbine release capacity constraints, irrigation supply demand constraints and storage continuity. For initializing population, the upper and lower bounds of decision variables are fixed. The fitness of each vector is evaluated. The mutation and recombination is performed. The control parameters, *i.e.*, population size, crossover constant and the weight are fixed according to their fitness value. This procedure is performed for the ten different strategies of DE. Sensitivity analysis performed for ten strategies of DE suggested that, De/best/1/bin is the best strategy which gives optimal solution. The DE algorithm application is presented through Jayakwadi project stage-I, Maharashtra State, India. Genetic algorithm is utilized as a comparative approach to assess the ability of DE. The results of GA and ten DE strategies for the given parameters indicated that both the results are comparable. The model is run for dependable inflows. Monthly maximized hydropower production and irrigation releases are presented. These values will be the basis for decision maker to take decisions regarding operation policy of the reservoir. Results of application of DE model indicate that the maximized hydropower production is  $30.885 \times 10^6$  kwh and the corresponding irrigation release is 928.44 Mm<sup>3</sup>.

**Keywords:** Optimization, Hydropower Production, Differential Evolution, Reservoir Operation

## 1. Introduction

Water for drinking purpose, for use in industry, irrigation and hydropower production, is main factor for hindering developments in many parts of the globe. Hence, proper management of available water resources is essential. Reservoir operation forms an important role in water resources development. Yeh [1] reviewed reservoir management and operation models. Algorithms and methods surveyed include linear programming (LP), dynamic programming (DP), nonlinear programming (NLP), and simulation. Oliveira and Loucks [2] have presented operating rules for multireservoir systems by using genetic search algorithms. Simulation was used to evaluate each policy by computing performance index for a given flow series. Wardlaw and Sharif [3] have presented several alternative formulations of a genetic algorithm for reser-

voir system. Later on, multi-reservoir systems optimization has been studied by Sharif and Wardlaw [4]. Nagesh Kumar *et al.* [5] have studied optimal reservoir operation for hydropower production which involved constrained nonlinear optimization. Earlier to that Srinivasa Raju and Nagesh Kumar [6] have discussed application of genetic algorithms for irrigation planning. GA was used to determine optimal cropping pattern for maximizing benefits for an irrigation project. Regulwar and Anand Raj [7] have presented A Multi objective, Multireservoir operation model for maximization of irrigation releases and hydropower production using Genetic Algorithm. A monthly Multi Objective Genetic Algorithm Fuzzy Optimization (MOGAFUOPT) model has been developed. From the relationships developed amongst irrigation releases, hydropower production and level of satisfaction, a three dimensional (3-D) surface covering the whole

range of policies has been developed.

Storn [8] has represented a heuristic approach for minimizing nonlinear and non differentiable continuous space function. The proposed method which requires few control variables is robust, easy to use and lends itself very well to parallel computation. Lampinen [9] has proposed differential evolution algorithm for handling nonlinear constraint functions. Differential Evolution (DE) algorithms claimed to be very efficient when they are applied to solve multimodal optimal control problems (Lopez Cruz *et al.* [10]). Differential evolution was used for the optimization of non-convex Mixed Integer Nonlinear Programming (MINLP) problems. The results of DE were compared with simplex, simulated annealing and genetic algorithm (Babu and Angira [11]). Vasan and Srinivasaraju [12] have demonstrated application of differential evolution to Bilaspur project in Rajasthan, India. The objective was to determine suitable cropping pattern for maximum benefits. Ranjithan [13] has presented the role of evolutionary computation in environmental and water resources systems analysis and discussed various methods such as Simulated Annealing, Tabu Search, GA, Evolutionary strategies, Particle swarm and Ant colony optimization. Janga Reddy and Nagesh Kumar [14] have studied Multi Objective Differential Evolution (MODE) with an application to a reservoir system optimization. The evolutionary operators used in differential evolution algorithms are very much suitable for problems having interdependence among the decision variables. Vasan and Komaragiri Srinivasa Raju [15] have demonstrated the applicability of DE to a case study of Mahi Bajaj Sagar project (MBSP), India. Ten different strategies of DE were employed to assess the ability of DE for solving higher dimensional problems as an alternative methodology for irrigation planning. The results were compared with LP.

In Genetic Algorithm (GA) low mutation rate is required to get global optimum [16]. The low mutation rate may get trouble with problems having interdependent relationships between variables and may require more number of function evaluations [17]. In reservoir operation the interdependence relationship may exist among decision variables. Interdependencies among variables can be tackled by properly rotating the co-ordinate system of the given function as it is done in Differential Evolution. DE has all properties necessary to handle complex problems with interdependencies between parameters [18]. DE maintains correlated self-adopting mutation step sizes in order to make timely progressive optimization. There is interdependence among variables therefore the evolutionary operators of DE are suitable to tackle these problems. This paper presents the applicability of DE for determining operation policies of a multipurpose reservoir.

## 2. Methodology

Differential evolution is a recent evolutionary optimization technique. It is simple, faster convergent and robust. The main difference between GA and DE is that GA depends on crossover while DE uses mutation as primary search mechanism. DE uses weighted differences between solution vectors to perturb the population. Unlike genetic algorithms, no binary coding of the population members is necessary. The general convention used for different variants of DE is DE/a/b/c. Here DE is for Differential evolution, 'a' is a string which denotes the vector to be perturbed, 'b' denotes the number of difference vectors taken for perturbation of 'a' and 'c' is the crossover method. According to Price and Storn [19] different strategies of DE are DE/rand/1/bin, DE/best/1/bin, DE/best/2/bin, DE/rand/2/bin, DE/rand-to-best/1/bin, DE/rand/1/exp, DE/best/1/exp, DE/best/2/exp, DE/rand/2/exp, and DE/rand-to-best/1/exp.

DE holds  $D$ -dimensional real valued vectors of  $Np$  population in pair. The current population  $P_x$ , includes vectors  $\mathbf{x}_{i,g}$  added or created randomly or by comparison with other vectors.

$$\begin{aligned} P_{x,g} &= (\mathbf{x}_{i,g}) \quad i = 0, 1, \dots, Np-1, \quad g = 0, 1, \dots, g_{\max}, \\ \mathbf{x}_{i,g} &= (x_{j,i,g}) \quad j = 0, 1, \dots, D-1. \end{aligned} \quad (1)$$

The index,  $g = 0, 1, \dots, g_{\max}$ , shows the generation of a vector. A population index  $i$  is assigned to each vector which ranges from 0 to  $Np-1$ . The index 'j' indicates parameter within vector ranges from 0 to  $D-1$ . After initialization, an intermediary population  $P_{v,g}$ , of  $Np$  mutant vectors,  $\mathbf{v}_{i,g}$  produced by random mutation.

$$\begin{aligned} P_{v,g} &= (\mathbf{v}_{i,g}) \quad i = 0, 1, \dots, Np-1, \quad g = 0, 1, \dots, g_{\max}, \\ \mathbf{v}_{i,g} &= (v_{j,i,g}) \quad j = 0, 1, \dots, D-1. \end{aligned} \quad (2)$$

Each vector in the current population is then recombined with a mutant to produce a trial population,  $P_u$  of  $Np$  trial vectors,  $\mathbf{u}_{i,g}$

$$\begin{aligned} P_{u,g} &= (\mathbf{u}_{i,g}) \quad i = 0, 1, \dots, Np-1, \quad g = 0, 1, \dots, g_{\max}, \\ \mathbf{u}_{i,g} &= (u_{j,i,g}) \quad j = 0, 1, \dots, D-1. \end{aligned} \quad (3)$$

During crossover, trial vectors overwrite the mutant population, so a single array can hold both populations. Then the cost of the trial vector is compared with the cost of the target vector, the vector having low cost will go into the next generation.

### 2.1. Case Study

The Jayakwadi project stage-I is taken as a case study. It is built across river Godavari, in Maharashtra State, India. The gross storage of reservoir is  $2909 \times 10^6 \text{ m}^3$  and live

storage is  $2171 \times 10^6 \text{ m}^3$ . Total installed capacity for power generation is 12.0 MW (Pumped storage plant). Irrigable command area is 1416.40 km<sup>2</sup>. The schematic representation of the physical system showing Jayakwadi project stage-I is shown in **Figure 1**. Monthly historical flow data for 73 years is collected and 75% dependable monthly flows are estimated using the Weibull plotting position formula. The inflow, irrigation demand, turbine capacity are presented in **Table 1**.

### 2.2. Model Formulation

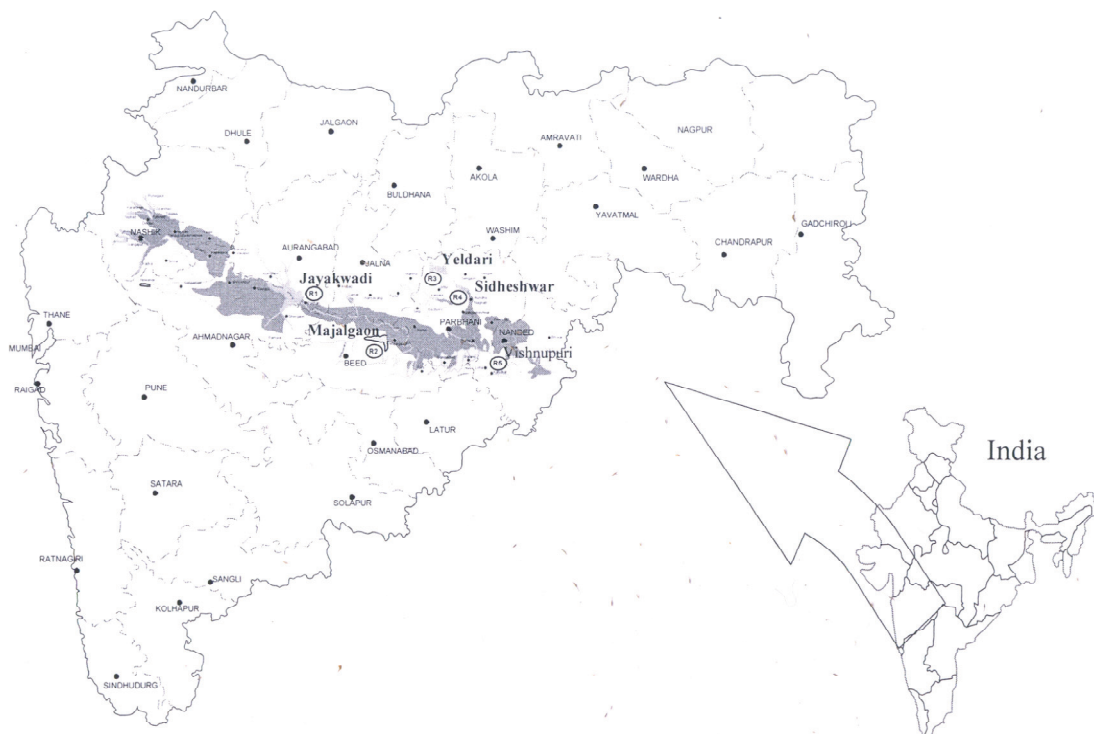
The objective of the study is to maximize the hydro-power production and present operation policy of a case study reservoir. Mathematically it can be expressed as:

$$\text{Max } Z = \sum_{t=1}^{12} P_t \tag{4}$$

where  $P_t$  = Hydropower produced in kwh during month 't'. If the monthly releases for hydropower ( $RP$ ) are

**Table 1. Inflow, irrigation demand and power demand.**

Sr no.	Months	Maximum irrigation demand in Mm <sup>3</sup>	Turbine Capacity in Mm <sup>3</sup>	75% dependable inflow in Mm <sup>3</sup>
1.	June	18.55	33.96	148.762
2.	July	26.7	33.96	408.25
3.	August	25.43	33.96	610.66
4.	September	85.79	33.96	600.0
5.	October	267.86	33.96	287.75
6.	November	228.74	33.96	196.46
7.	December	210.88	33.96	125.53
8.	January	230.34	33.96	37.65
9.	February	85.23	33.96	21.462
10.	March	70.06	33.96	19.562
11.	April	85.49	33.96	25.5
12.	May	58.20	33.96	46.587
	<b>Total</b>	<b>1393.27</b>	<b>407.52</b>	<b>2528.173</b>



**Figure 1. Sketch showing Jayakwadi project stage-1, Maharashtra state, India.**

expressed in  $\text{Mm}^3$ , head (h) in meters, then power produced P in KW hours for a 30 day month is given by  $P = 2725 \times (\text{RP}) \times (\text{h})$ . The model is subjected to the following constraints.

### 2.2.1. Releases into Turbine and Capacity Constraints

The releases into turbines for power production, should be less than or equal to the flow through turbine capacity (TC) for all the months. Also, power production in each month should be greater than or equal to the firm power (FP). These constraints can be written as:

$$RP(t) \leq TC \quad \forall \quad t = 1, 2, 3, \dots, 12. \quad (5)$$

$$RP(t) \geq FP \quad \forall \quad t = 1, 2, 3, \dots, 12. \quad (6)$$

### 2.2.2. Irrigation Supply-Demand Constraints

The releases into canals for irrigation (RI) should be less than or equal to the maximum irrigation demand ( $ID_{\max}$ ) for all the months. Also, the releases into the canals for irrigation should be greater than or equal to the minimum irrigation demand ( $ID_{\min}$ ). The irrigation release-demand constraint, can, therefore be written as:

$$RI(t) \leq ID_{\max}(t) \quad \forall \quad t = 1, 2, 3, \dots, 12. \quad (7)$$

$$RI(t) \geq ID_{\min}(t) \quad \forall \quad t = 1, 2, 3, \dots, 12. \quad (8)$$

### 2.2.3. Reservoir Storage-Capacity Constraints

The storage in the reservoirs (S) should be less than or equal to the maximum storage capacity (SC) and greater than or equal to the minimum storage capacity ( $S_{\min}$ ) for all months. These constraints can be written as:

$$S(t) \leq SC \quad \forall \quad t = 1, 2, 3, \dots, 12. \quad (9)$$

$$S(t) \geq S_{\min} \quad \forall \quad t = 1, 2, 3, \dots, 12. \quad (10)$$

### 2.2.4. Reservoir Storage-Continuity Constraints

This constraint relate to the turbine releases (RP), irrigation releases (RI), release for drinking and industrial water supply (RWS) which is taken as a constant, reservoir storage (S), inflows into the reservoirs (IN), Losses from the reservoirs for all months. The losses from the reservoirs are taken as function of storage as given by Loucks *et al.* [20]. Let  $A_0$  is reservoir water surface area corresponding to the dead storage volume and  $e_t$  is evaporation rate corresponding to the time period t (in depth units).  $A_a$  is the reservoir water spread area per unit volume of active storage. Then the actual evaporation during the time period 't' is given by

$$\text{Evaporation loss} = A_0 e_t + A_a e_t \frac{(S_t + S_{t+1})}{2}$$

$$\text{Put } a_t = \frac{A_a e_t}{2} = 0.5 A_a e_t \quad \text{then,}$$

$$\text{Evaporation loss} = A_0 e_t + a_t (S_t + S_{t+1})$$

Then the hydrologic continuity constraint can be written as:

$$(1 + a_t)S(t+1) = (1 - a_t)S(t) + IN(t) - RP(t) - RI(t) - SP(t) - WS(t) - FCR(t) + \beta RP(t) - A_0 e_t \quad (11)$$

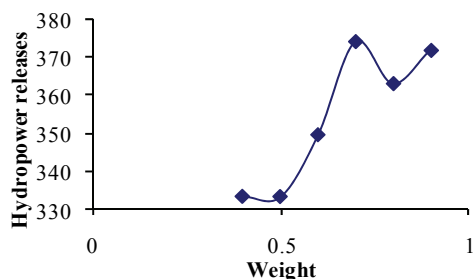
## 3. Results and Discussion

Differential Evolution (DE) has ten strategies. The model is run with DE parameters, *i.e.*, crossover constant and weight for each strategy. The population is fixed by running the model for different population sizes in combination with crossover constants and weight. For deciding crossover constant and weight for each strategy, the model is run for different crossover constants, *i.e.*, 0.7, 0.75, 0.8, 0.85, 0.9, 0.95 with the combination of weight ranging from 0.2 to 0.9 with the increment of 0.05. For every combination fitness is calculated and compared with population. Based on this approach population is fixed as 400. For getting optimal solution, generation is fixed as 500. The DE parameters, *i.e.*, crossover constants and weight are decided for each strategy and presented in **Table 2**. The relationships between weight and hydropower releases corresponding to crossover constant are presented graphically in **Figures 2 to 11**. By considering these DE parameters, the optimization model is run and optimized values of objective function are presented for all strategies in **Table 2**. The random seed should be greater than one. So for seed also the model is run for various seed values, *i.e.*, 1 to 90, and 77 is fixed from the comparison of results.

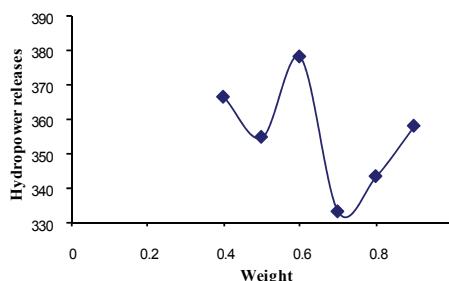
**Table 2** presents comparison of strategies of DE. In this table, the crossover constant, weight, optimal hydropower production and annual irrigation releases are presented corresponding to each strategy. The comparison of strategies for maximum objective function value is shown graphically in **Figure 12**. From the **Table 2**, it is clear that the strategy number 6, *i.e.*, DE/best/1/bin gives the optimal results. For this strategy, the DE parameters are crossover 0.85, and weight 0.9. The optimized hydropower production is worked out to be  $30.89 \times 10^6$  kwh. The release for irrigation corresponding to the optimal fitness of objective function is  $928.44 \text{ Mm}^3$ . Monthly optimal releases for irrigation are shown graphically in **Figure 13**. Monthly optimal hydropower production is shown graphically in **Figure 14**. For comparison of DE results, the genetic algorithm approach is utilized in this study. The proposed reservoir operation model is solved using GA. Stochastic remainder selection; one point crossover and binary mutation are used as GA operators in this study. For selection of population size, crossover probability, mutation probability and optimal generations, a thorough sensitivity analysis is carried out. The system performance is estimated by taking crossover probability between 0.6 to 1.0 with a increment of 0.05 and mutation probabilities between 0.4 to 0.001 with a decrement of 0.1 up to 0.01 and then the decrement is taken as 0.001. The population size is var-

**Table 2. Comparison of strategies of differential evolution.**

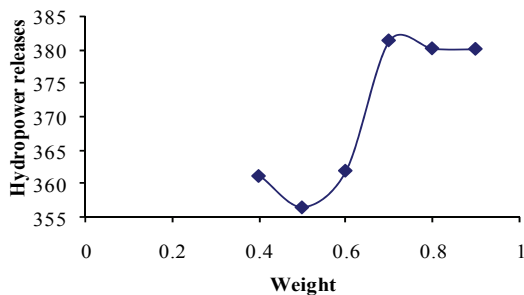
Sr. No.	Strategy	CR	F	Annual hydropower produced kwh	Annual Irrigation releases Mm <sup>3</sup>
1	DE/best/1/exp	0.85	0.70	29651500	927.271
2	DE/rand/1/exp	0.95	0.70	30365652	827.383
3	DE/rand-to-best/1/exp	0.80	0.90	27208474	872.191
4	DE/best/2/exp	0.95	0.50	29268860	976.005
5	DE/rand/2/exp	0.85	0.60	29380314	881.820
6	DE/best/1/bin	0.85	0.90	30885738	928.442
7	DE/rand/1/bin	0.95	0.80	28513356	853.046
8	DE/rand-to-best/1/bin	0.85	0.90	27368522	862.894
9	DE/best/2/bin	0.85	0.90	29247944	906.402
10	DE/rand/2/bin	0.95	0.80	30099228	947.816



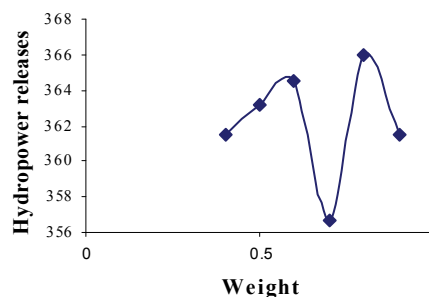
**Figure 2. Relationship between weight and strategy No. 1 for crossover 0.85.**



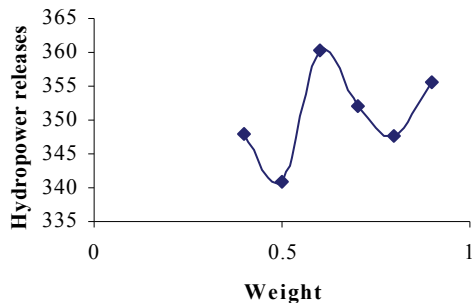
**Figure 5. Relationship between weight and strategy No. 4 for crossover 0.95.**



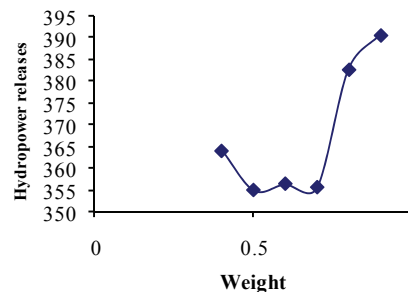
**Figure 3. Relationship between weight and strategy No. 2 for crossover 0.95.**



**Figure 6. Relationship between weight and strategy No. 5 for crossover 0.85.**



**Figure 4. Relationship between weight and strategy No. 3 for crossover 0.8.**



**Figure 7. Relationship between weight and strategy No. 6 for crossover 0.85.**

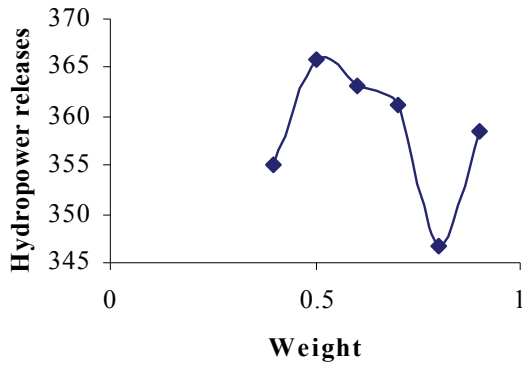


Figure 8. Relationship between weight and strategy No. 7 for crossover 0.95.

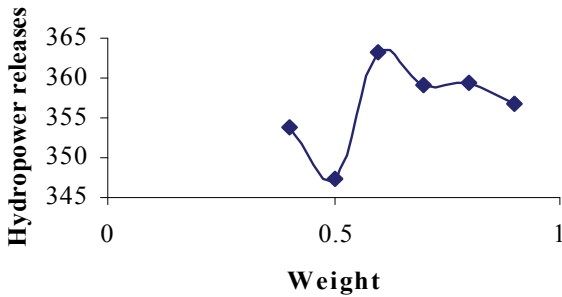


Figure 9. Relationship between weight and strategy No. 8 for crossover 0.85.

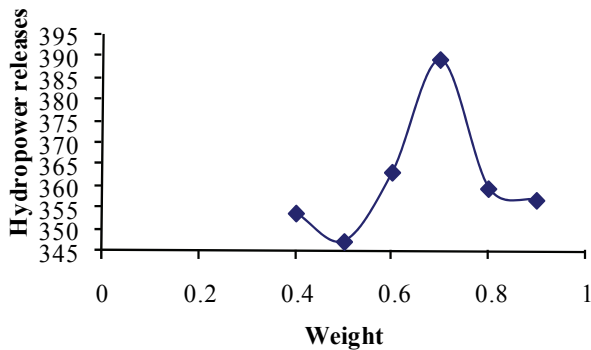


Figure 10. Relationship between weight and strategy No. 9 for crossover 0.85.

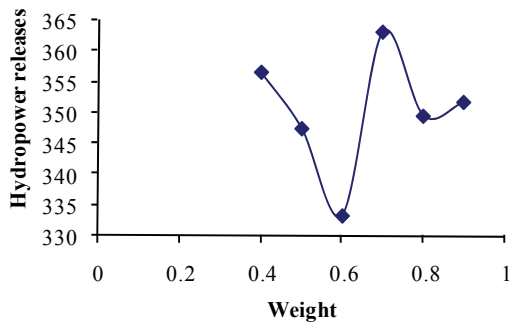


Figure 11. Relationship between weight and strategy No. 10 for crossover 0.95.

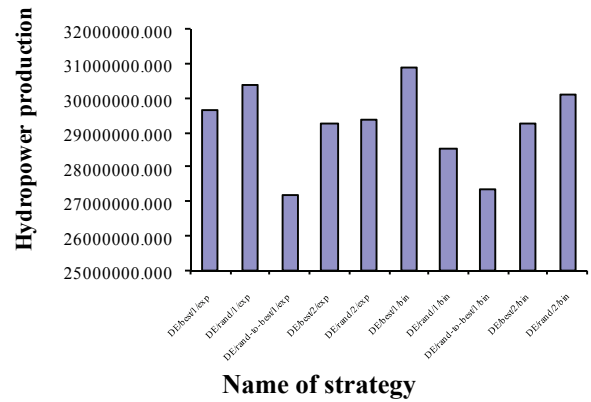


Figure 12. Comparison of strategies.

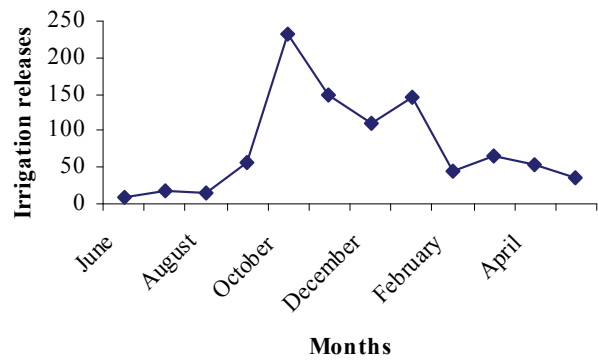


Figure 13. Optimal releases for irrigation (DE/best/1/bin).

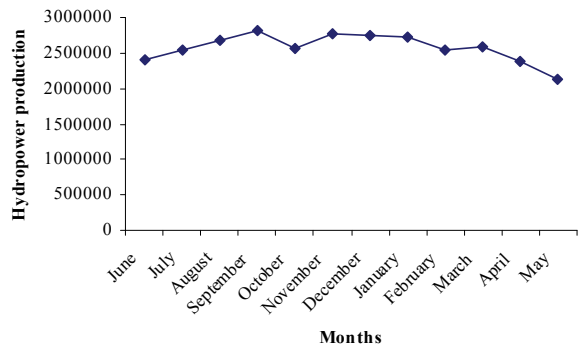


Figure 14. Optimal hydropower production (DE/best/1/bin).

ied from 50 to 150 and generation from 20 to 500. Based on the system performance the optimal population size and optimal number of generations are 100 and 500 respectively. For crossover probability of 0.95 and mutation probability of 0.01, the maximization is achieved. The monthly optimized irrigation releases and hydropower production by using GA are obtained and presented in **Table 3**. The comparison of DE and GA results for irrigation releases and hydropower production are presented for best strategy in the same table. Also **Table 4** represents the monthly optimal irrigation releases obtained by DE strategies and GA. **Table 5** represents the

**Table 3. Comparison of optimal releases for irrigation and hydropower production by DE and GA.**

Month	Release for irrigation	Release for irrigation	Hydropower produced	Hydropower produced
	Mm <sup>3</sup> By DE	Mm <sup>3</sup> By GA	× 10 <sup>6</sup> kwh By DE	× 10 <sup>6</sup> kwh By GA
June	9.65	14.20	2.405	2.581
July	16.58	16.94	2.552	2.548
August	13.47	16.63	2.671	2.571
September	55.10	58.14	2.811	2.56
October	232.55	178.05	2.575	2.562
November	148.90	146.51	2.776	2.576
December	109.42	145.18	2.738	2.571
January	144.63	129.31	2.717	2.552
February	44.38	55.59	2.544	2.559
March	64.87	48.87	2.577	2.564
April	52.12	54.67	2.384	2.572
May	36.76	38.09	2.137	2.553
TOTAL	928.442	902.19	30.887	30.769

**Table 4. Irrigation releases obtained by the DE strategies and GA in Mm<sup>3</sup>.**

Month	DE1	DE2	DE3	DE4	DE5	DE6	DE7	DE8	DE9	DE10	GA
June	9.7	9.7	9.7	9.7	9.7	9.7	9.7	9.7	9.7	9.7	14.20
July	16.6	16.6	16.6	16.6	16.6	16.6	16.6	16.6	16.6	16.6	16.94
August	13.5	13.5	13.5	13.5	13.5	13.5	13.5	13.5	13.5	13.5	16.63
September	57.4	34.8	56.2	56.2	52.3	55.1	49.7	46.3	72.9	62.5	58.14
October	232.6	138.9	162.4	162.4	138.8	232.6	140.6	162.4	162.4	162.4	178.05
November	148.9	149.6	157.9	209.1	151.7	148.9	160.3	193.9	118.5	117.9	146.51
December	109.4	127.9	109.3	109.3	85.4	109.4	123.2	109.3	85.4	109.3	145.18
January	134.9	145.2	145.8	211.8	195.1	144.6	147.7	151.9	176.6	223.7	129.31
February	51.9	44.3	34.6	51.9	74.5	44.4	52.7	34.6	74.5	34.6	55.59
March	63.1	64.9	53.2	67.4	46.0	64.9	55.6	66.9	63.6	67.8	48.87
April	44.5	34.7	74.8	44.5	62.0	52.1	34.7	34.7	56.0	74.8	54.67
May	44.5	47.4	38.3	23.7	36.4	36.8	48.9	23.2	56.8	55.0	38.09
Total	927.0	827.4	872.2	976.0	881.8	928.4	853.0	862.9	906.4	947.8	902.19

DE1 DE/best/1/exp, DE2 DE/rand/1/exp, DE3 DE/rand-to-best/1/exp, DE4 DE/best/2/exp, DE5 DE/rand/2/exp, DE6 DE/best/1/bin, DE7 DE/rand/1/bin, DE8 DE/rand-to-best/1/bin, DE9 DE/best/2/bin, DE10 DE/rand/2/bin

**Table 5. Hydropower production obtained by the DE strategies and GA in kwh (× 10<sup>6</sup>).**

Month	DE1	DE2	DE3	DE4	DE5	DE6	DE7	DE8	DE9	DE10	GA
June	2.41	2.42	2.11	2.35	2.32	2.40	2.37	2.29	2.41	2.30	2.58
July	2.35	2.52	2.18	2.52	2.48	2.55	2.23	2.17	2.57	2.80	2.55
August	2.61	2.61	2.14	2.26	2.51	2.67	2.56	2.19	2.41	2.53	2.57
September	2.36	2.72	2.02	2.73	2.67	2.81	2.16	2.08	2.78	2.87	2.56
October	2.86	2.58	2.54	2.53	2.82	2.58	2.53	2.46	2.79	2.63	2.56
November	2.76	2.83	2.48	2.72	2.76	2.78	2.01	2.41	2.62	2.65	2.58
December	2.80	2.36	2.46	2.29	2.23	2.74	2.71	2.23	2.36	2.41	2.57
January	2.69	2.62	2.38	2.48	2.68	2.72	2.32	2.56	2.67	2.79	2.55
February	2.63	2.45	1.99	2.36	2.22	2.54	2.52	2.32	2.44	2.26	2.56
March	1.79	2.58	2.41	2.38	2.46	2.58	2.55	2.13	2.62	2.19	2.56
April	2.21	2.45	2.41	2.36	2.00	2.38	2.40	2.44	1.85	2.37	2.57
May	2.18	2.22	2.08	2.27	2.23	2.14	2.15	2.09	1.73	2.30	2.55
Total	29.65	30.37	27.21	29.27	29.38	30.89	28.51	27.37	29.25	30.10	30.77

monthly optimal hydropower production by DE strategies and GA. **Tables 4** and **5** gives exhaustive comparison of all DE strategies and GA for irrigation releases and hydropower production. This comparison among all strategies of DE and GA provides applicability of differential evolution for optimal operation of multi-purpose reservoir.

#### 4. Conclusions

In the present study a multipurpose reservoir in Godavari River sub basin in Maharashtra State, India is considered. A multiobjective operation model for maximization of hydropower production is proposed using differential evolution algorithm. Results of application of DE model indicate that the maximized hydropower production is  $30.885 \times 10^6$  kwh and the corresponding irrigation release is 928.44 Mm<sup>3</sup>. From the results it can be seen that the monthly maximized irrigation release and hydropower production can be the basis for decision maker to take decision for reservoir operation. Genetic algorithm is utilized as a comparative approach. The results of GA and different DE strategies for irrigation releases and hydropower production show that both the results are close and comparable. Therefore it can be said that DE can be used as an alternative methodology for optimal operation of multipurpose reservoir. Differential evolution algorithm works with numerical values. Therefore highly complex objective functions do not introduce any difficulties and even discontinuous functions are acceptable. From the results, it can be said that the DE can be effectively applied to multi-objective operation problem and the reservoir can be operated for optimal reservoir releases for irrigation and hydropower production after meeting the other demands from the reservoir.

#### 5. Acknowledgements

The authors are thankful to Rainer Storn, K. Price and J. Lampinen for their guidance during the work. Also, the authors are thankful to Command Area Development Authority, Aurangabad, Maharashtra state, India for providing necessary data for the analysis.

#### 6. References

- [1] W. W.-G. Yeh, "Reservoir Management and Operations Models: A State-of-the-Art Review," *Water Resources Research*, Vol. 21, No. 12, 1985, pp. 1797-1818.
- [2] R. Oliveira and D. P. Loucks, "Operating Rules for Multi-Reservoir Systems," *Water Resource Research*, Vol. 33, No. 4, 1997, pp. 839-852.
- [3] R. Wardlaw and M. Sharif, "Evaluation of Genetic Algorithm for Optimal Reservoir System Operation," *Journal of Water Resource, Planning and Management*, Vol. 125, No. 1, 1999, pp. 25-33.
- [4] M. Sharif and R. Wardlaw, "Multireservoir Systems Optimization Using Genetic Algorithms: Case Study," *Journal of Computer in Civil Engineering*, Vol. 14, No. 4, 2000, pp. 255-263.
- [5] D. Nagesh kumar, A. Kumar and K. S. Raju, "Application of Genetic Algorithms for Optimal Reservoir Operation," *Proceedings of X World Water Congress*, Melbourne, 2000.
- [6] K. S. Raju and D. Nagesh Kumar, "Irrigation Planning Using Genetic Algorithms," *Water Resource Management*, Vol. 18, No. 2, 2004, pp. 163-176.
- [7] D. G. Regulwar and P. A. Raj, "Development of 3-D Optimal Surface for Operation Policies of a Multireservoir in Fuzzy Environment Using Genetic Algorithm for River Basin Development and Management," *Water Resource and Management*, Vol. 22, No. 5, 2008, pp. 595-610.
- [8] R. Storn and K. Price, "Differential Evolution a Simple Evolution Strategy for Fast Optimization," *Dr Dobb's Journal*, Vol. 22, No. 4, 1997, pp. 18-24.
- [9] J. Lampinen, "Multiconstraint Nonlinear Optimization by Differential Evolution Algorithm," *Technical Report*, Lappeenranta University of Technology, Laboratory of Processing, 1999. <http://www.lut.fi/~jlampine/debiblo.htm>
- [10] I. L. Lopez Cruz, L. G. Van Willigenburg and G. Van Straten, "Efficient Differential Evolution Algorithms for Multimodal Optimal Control Problems," *Journal of Applied Soft Computing*, Vol. 3, No. 2, 2003, pp.97-122.
- [11] B. V. Babu and R. Angira, "A Differential Evolution Approach for Global Optimization of MINLP Problems," *Proceedings of 4th Asia Pasific conference on Simulated Evolution and Learning (SEAL2002)*, Vol. 2, Singapore, 2002, pp. 880-884.
- [12] A. Vasani and K. Srinivasa Raju, "Optimal Reservoir Operation Using Differential Evolution," *International Conference on Hydraulic Engineering: Research and Practice (ICON-HERP-2004)*, Indian Institute of Technology Roorkee, India, 2004.
- [13] S. R. Ranjithan, "Role of Evolutionary Computation in Environmental and Water Resources Systems Analysis," *Journal of Water Resources Planning and Management*, ASCE, Vol. 131, No. 1, 2005, pp.1-2.
- [14] M. J. Reddy and D. N. Kumar, "Multiobjective Differential Evolution with Application to Reservoir System Optimization," *Journal of Computing in Civil Engineering*, ASCE, Vol. 21, No. 2, 2007, pp.136-146.
- [15] A. Vasani and K. S. Raju, "Application of Differential Evolution for Irrigation Planning: An Indian Case Study," *Water Resources Management*, Vol. 21, No. 8, 2007, pp. 1393-1407.
- [16] D. E. Goldberg, "Genetic Algorithms in Search, Optimization and Machine Learning," Addison-Wesley, Reading, Massachusetts, 1989.
- [17] R. Salomon, "Re-Evaluating Genetic Algorithm Performance under Coordinate Rotation of Benchmark Func-



tions: A Survey of Some Theoretical and Practical Aspects of Genetic Algorithms," *Biology Systems*, Vol. 39, No. 3, 1996, pp. 263-278.

- [18] K. V. Price, "An Introduction to Differential Evolution, New Ideas in Optimization," McGraw-Hill, London, 1999, pp. 79-108.
- [19] K. Price and R. Storn, "Home Page of Differential Evolution," 2005. <http://www.icsi.Berkeley.edu/~storn/code.html>
- [20] D. P. Loucks, J. Stedinger and D. Haith, "Water Resources Systems Planning and Analysis," Prentice-Hall, Eaglewood Cliffs, New Jersey, 1981.

## Appendix: Notation

The following symbols are used in this paper

RP(t): Monthly releases for power generation during month t

TC: Flow corresponding to maximum capacity of turbine

FP: Flow corresponding to firm power.

RI(t): Releases for irrigation during month t.

IDmax(t): Maximum irrigation requirement of command area during month t.

IDmin (t): Minimum irrigation requirement of command area during month t

S(t): Storage volume in the reservoir during month t

SC: Maximum storage volume of reservoir

Smin: Dead storage volume of reservoir

SP(t): Spills during month t

FCR(t): Feeder Canal Releases during month t

$\beta$ : Constant.

NP: Number of Population

CR: Crossover Constant

F: Weight