

Differential Evolution with an Individual-Dependent Mechanism

Lixin Tang, *Senior Member, IEEE*, Yun Dong, and Jiyin Liu

Abstract—Differential evolution is a well-known optimization algorithm that utilizes the difference of positions between individuals to perturb base vectors and thus generate new mutant individuals. However, the difference between the fitness values of individuals, which may be helpful to improve the performance of the algorithm, has not been used to tune parameters and choose mutation strategies. In this paper, we propose a novel variant of differential evolution with an individual-dependent mechanism that includes an individual-dependent parameter setting and an individual-dependent mutation strategy. In the individual-dependent parameter setting, control parameters are set for individuals according to the differences in their fitness values. In the individual-dependent mutation strategy, four mutation operators with different searching characteristics are assigned to the superior and inferior individuals, respectively, at different stages of the evolution process. The performance of the proposed algorithm is then extensively evaluated on a suite of the 28 latest benchmark functions developed for the 2013 Congress on Evolutionary Computation special session. Experimental results demonstrate the algorithm’s outstanding performance.

Index Terms—Differential evolution, global numerical optimization, individual-dependent, mutation strategy, parameter setting.

I. INTRODUCTION

Differential Evolution (DE), proposed by Storn and Price [1] in 1995, is an efficient population-based global searching algorithm for solving optimization problems [2]–[4]. Over the years, different variants of DE have been developed to solve complicated optimization problems in a wide range of application fields, such as auction [5], decision-making [6], neural network training [7], chemical engineering [8], robot control [9], data clustering [10], gene regulatory network [11], nonlinear system control [12], and aircraft control [13].

DE is a typical evolutionary algorithm (EA) which employs strategies inspired by biological evolution to evolve a popula-

tion. Throughout this paper, we suppose that DE is used for solving minimization problems, and that the objective function can be expressed as: $f(\mathbf{x})$, $\mathbf{x} = (x^1, \dots, x^D) \in R^D$. We take the objective function value of each solution as its fitness value in DE. Note that with this setting a solution with a lower fitness value is a better solution. Some previous studies (e.g., [6][7]) also used such settings, while [2][3] used objective function only without defining fitness. To solve the problem, the classic DE process starts from an initial population of NP individuals (vectors) in the solution space, with each individual representing a feasible solution to the problem. At each generation g , the individuals in the current population are selected as parents to undergo mutation and crossover to generate offspring (trial) individuals. Each individual $\mathbf{x}_{i,g}$ ($i = 1, 2, \dots, NP$) in the population of current generation is chosen once to be a parent (target individual) for crossover with a mutant individual $\mathbf{v}_{i,g}$ obtained from a mutation operation in which the base individual is perturbed by a scaled difference of several randomly selected individuals. The offspring individual $\mathbf{u}_{i,g}$ generated from the crossover contains genetic information obtained from both the mutant individual and the parent individual. Each element $u_{i,g}^j$ ($j = 1, 2, \dots, D$) of $\mathbf{u}_{i,g}$ should be restricted within the corresponding upper and lower boundaries. Otherwise, it will be reinitialized within the solution space. The mutation and crossover operations of classic DE are illustrated in Fig. 1. The fitness value (objective function value) of the offspring individual $\mathbf{u}_{i,g}$ is then compared with the fitness value of the corresponding parent individual $\mathbf{x}_{i,g}$, and the superior individual is chosen to enter the next generation. Then, the new population is taken as the current population for further evolution operations. This continues until specific termination conditions are satisfied. In the final generation, the best individual will be taken as the solution to the problem.

There are only a few DE control parameters that need to be set: the population size NP , the mutation factor (scale factor) F , and the crossover probability (crossover rate) CR . Different parameter settings have different characteristics. In addition, the strategies used for each operation in DE, especially the mutation strategies, can vary to obtain diverse searching features that fit different problems. Therefore, the ability of DE to solve a specific problem depends heavily on the choice of strategies [4], and the setting of control parameters [14], [15]. Inappropriate configurations of mutation strategies and control parameters can cause stagnation due to over exploration, or can cause premature convergence due to over exploitation. Exploration can make the algorithm search every promising

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Lixin Tang is with The Logistics Institute, Liaoning Key Laboratory of Manufacturing System and Logistics, Northeastern University, Shenyang, 110819, China (e-mail: lixintang@mail.neu.edu.cn).

Yun Dong is with State Key Laboratory of Synthetical Automation for Process Industry, The Logistics Institute, Northeastern University, Shenyang, 110819, China (e-mail: dydexter@hotmail.com).

Jiyin Liu is with School of Business and Economics, Loughborough University, Leicestershire LE11 3TU, UK (e-mail: J.Y.Liu@lboro.ac.uk).

solution area with good diversity, while exploitation can make the algorithm execute a local search in some promising solution areas to find the optimal point with a high convergence rate.

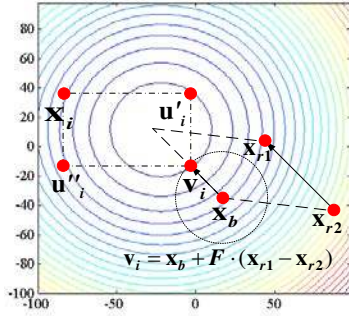


Fig. 1. The 2-D plot of evolution operation of classic DE.

Therefore, choosing strategies and setting parameters aimed at getting a good balance between the algorithm’s effectiveness (solution quality) and efficiency (convergence rate) have always been subjects of research.

In the evolution process of a DE population, superior individuals and inferior individuals play different roles. The former guide the searching direction, and the latter maintain population diversity. Generally, in the solution space, better solutions are more likely to be found in the neighborhoods of superior individuals or in areas relatively far from inferior individuals. Unfortunately, these differences have not been reflected in the control parameter setting and mutation strategy selection in classic DE and its variants.

In this paper, a novel **DE** variant (**IDE**) with an **individual-dependent** mechanism is presented. The new mechanism in IDE includes an individual-dependent parameter (IDP) setting and an individual-dependent mutation (IDM) strategy. The IDP setting first ranks individuals based on their fitness values and then determines the parameter values of the mutation and crossover operations for each individual based on its rank value. In IDP, superior individuals tend to be assigned with smaller parameter values so as to exploit their neighborhoods in which better solutions are likely contained, while inferior individuals tend to be assigned with larger parameter values so as to explore further areas in the solution space. The IDM strategy assigns four mutation operators with different searching characteristics for superior and inferior individuals at different stages of the iteration process. Further, the IDM strategy introduces perturbations to the difference vector by employing diverse elements generated from the solution space. In response to the decreased diversity of the population, we propose to increase the proportions of the explorative mutation operator and the perturbations following an exponential function. Extensive experiments are carried out to evaluate the performance of IDE by comparing it with five IDE variants, five state-of-the-art DE variants, ten up-to-date DE variants, and three other well-known EAs on the latest 28 standard benchmark functions listed in the CEC 2013 contest.

The remainder of this paper is organized as follows. In Section II, the related works on DE mutation strategy selecting and control parameter setting are reviewed. After the development of the IDP setting and the IDM strategy, the complete procedure of IDE is presented in Section III. In

Section IV, experiment results are reported to demonstrate the effectiveness of IDE. Section V gives conclusions and indicates possible future work.

II. LITERATURE REVIEW

Over the past decades, researchers have developed many different mutation strategies [16], [17]. It has been shown that some of them are fit for global search with good exploration ability and others are good at local search with good exploitation ability [3]. For example, mutation strategies with two difference vectors (e.g., DE/rand/2) can increase the population diversity compared to strategies with a single difference vector (e.g., classic DE/rand/1), while mutation strategies taking the best individual of the current generation in the base vector (e.g., DE/best/1 and DE/current-to-best/1) can strengthen exploitive search and so speed up convergence.

However, to improve algorithm robustness, exploration and exploitation must be simultaneously combined into the evolution strategy. Therefore, the *single-mutation operator* strategies with composite searching features (such as BDE [18], DEGL [19], JADE [20], ProDE [21], BoRDE [22], and TDE [23]) and the *multi-mutation operators* strategies with different searching features (such as SaDE [24], [25], TLBSaDE [26], CoDE [27], EPSDE [28],[29], SMADE [30], jDE_{soo} [31], and SPSRDEMMS [32]) were proposed. Epitropakis *et al.* [18] linearly combined an explorative and an exploitive mutation operator to form a hybrid approach (BDE) with an attempt to balance these two operators. DEGL, proposed by Das *et al.* [19], combines global and local mutant individuals to form the actual mutant individuals with a weight coefficient in each generation. In JADE, proposed by Zhang and Sanderson [20], an optional external archive is combined with a mutation strategy DE/current-to-*p*best/1 that utilizes historical information to direct population searching. The individuals in the neighborhood of the target individual are selected to participate in the mutation operation in ProDE, proposed by Epitropakis *et al.* [21]. To obtain both good diversity and fast convergence rate, Lin *et al.* [22] proposed a DE variant with a *best of random* mutation strategy (BoRDE), in which the individual with the best fitness value among several randomly chosen individuals is selected as the base vector in the mutation operation. Fan and Lampinen [23] introduced a trigonometric mutation operation to form TDE (trigonometric mutation differential evolution), in which the searching direction of each new mutant individual is biased to the best among three different individuals randomly chosen in the mutation. Each of the four given effective trial vector generation strategies (mutation and crossover operations) is selected to be implemented according to a self-adaptive probability in SaDE, proposed by Qin *et al.* [25]. In addition to a mutation strategy pool, a teaching and learning mechanism is employed by TLBSaDE, i.e., a new variant of SaDE, to generate the mutant individuals [26]. Wang *et al.* [27] proposed CoDE in which three mutation strategies are implemented in parallel to create three new mutant individuals for crossover with the target individual before selecting one to enter the next generation. Mallipeddi *et al.* [28] proposed EPSDE, in which a set of mutation strategies along with a set of parameter values compete to generate offspring. Zhao *et al.* [29] modified

EPSDE by incorporating an SaDE type learning scheme. SMADE, proposed in [30], makes use of a multiple mutation strategy consisting of four different mutation operators and selects one operator via a roulette-wheel selection scheme for each target individual in current generation. Researchers in [31] proposed a variant of jDE, i.e., jDE_{soo} (jDE for single objective optimization), which concurrently applies three different DE strategies in three sub-populations. In SPSRDEMMS [32], one mutation operator is selected from DE/rand/1 and DE/best/1 to generate the mutant individual according to the population size gradually reduced with iteration progresses. A ranking-based mutation operator is introduced in Rank-DE [33] where the base and terminal (guiding) individuals in mutation operators are proportionally selected according to their ranking values in current generation.

With respect to parameter setting methods, we can classify them into three categories: *constant*, *random*, and *adaptive* (including *self-adaptive*). In *constant* parameter setting, such as that used in classic DE, parameters are preset before the search and kept invariant during the entire iteration process. Storn and Price [2] stated that it is not difficult to choose control parameters for obtaining good results. In their opinion, a promising range of NP is between $5D$ and $10D$, where D is the dimension of the individual, 0.5 represents a reasonable value of F , and 0.1 is a first choice for CR for general situations and 0.9 for situations in which quick solutions are desired. However, based on the results of tests on four benchmark functions, Gämperle *et al.* [15] concluded that DE performance depends heavily on the setting of control parameters. The researchers stated that a promising range of NP is between $3D$ and $8D$, an efficient initial value for F is 0.6, and a promising range for CR is [0.3, 0.9]. In [34], Rönkkönen *et al.* suggested that a reasonable range of NP is between $2D$ and $40D$, that F should be sampled between 0.4 and 0.95 (and that 0.9 offered a compromise between exploration and exploitation), and that CR should be drawn from the range (0.0, 0.2) if the problem is separable, or [0.9, 1] if the problem is both non-separable and multimodal. They set $F = 0.9$, $CR = 0.9$, and $NP = 30$ for all experimental functions in the CEC 2005 contest benchmark suite. In CoDE [27], each trial vector generation strategy randomly selects one parameter setting from a pool consisting of three *constant* parameter settings. OXDE, proposed in [35], employs a new orthogonal crossover operator to improve the searching ability of classic DE with $F = 0.9$, $CR = 0.9$, and $NP = D$. In [36], DE-APC randomly assigns F value and CR value from two preset *constant* sets F_{set} and CR_{set} , respectively, to each individual. The diversity of the conclusions reached by these researchers indicates the number of different claims on the DE control parameter setting. It is impossible that one *constant* parameter setting fits all problems, instead, effective *constant* parameters should be problem-dependent.

To avoid manually tuning parameters, researchers have developed some techniques to automatically set the parameter values, one of which is *random* parameter setting. Linear variation, probability distribution, and specified heuristic rules are usually employed to generate the diverse parameters in *random* parameter setting. For example, Das *et al.* [37] presented two ways to set F in DE, i.e., random and time

varying. In the random way, F is set to be a random real number from the range (0.5, 1); in the time varying way, F is linearly reduced within a given interval. In SaDE [25], the value of parameter F is randomly drawn from a normal distribution $N(0.5, 0.3)$ for each target individual in the current population. Abbass [38] generated F from the standard normal distribution $N(0, 1)$. CR in [39] is generated from a normal distribution $N(0.5, 0.15)$. CR is set to be $[2^{1/(n\alpha_e)}]^{-1}$ in DEcfbLS [40], where n is the dimension of the problem and α_e is the inheritance factor [41]. The *random* setting can improve the exploration ability by increasing searching diversity.

Another automatic parameter setting method focuses on the adaptation of control parameters. In *adaptive* parameter setting, the control parameters are adjusted according to the feedback from the searching process [42], [43], or undergo evolutionary operation [38], [44]. Incorporating the individuals of successive generations and relative objective function values as inputs, Liu and Lampinen [42] employed a fuzzy logic controller to tune the parameters adaptively in FADE (fuzzy adaptive differential evolution). A self-adaptive DE (jDE) proposed by Brest *et al.* [43] assigns the values from the ranges [0.1, 1.0] and [0.0, 1.0] in an adaptive manner with probabilities τ_1 and τ_2 to F and CR , respectively, for each mutation and crossover operation. In JADE [20], according to the historical successful information of parameters, F is generated by a Cauchy distribution, and CR is sampled from a normal distribution for each individual at each generation. SHADE [45] is an improved version of JADE which employs a different success-history based mechanism to update F and CR . SaDE [25] adaptively adjusts CR values following a normal distribution with the mean value depending on the previous successful CR values. The parameters in [29] are gradually self-adapted by learning from the success history. In [46], for each individual, control parameters is selected adaptively from a set of 12 different DE parameter settings with a probability depending on the corresponding success rate. Instead of the single one value of F to one individual, PVADE, presented in [47], adopts a scaling factor vector F_m , calculated by a diversity measure of the population in each dimension level. The mutation and crossover rates of the evolutionary algorithms [38], [44], proposed based on DE, are self-adapted by the DE mutation operation.

We have observed that the existing mutation strategies and control parameter setting methods reviewed above are used at the population level, i.e., all individuals in the current population are treated identically without consideration of the differences in their fitness values. Consideration of this difference may be helpful for finding better solutions in the next generation. We therefore propose a new difference-based mechanism in which the control parameters and mutation operators are set to each individual according the information on its fitness value in the current generation to improve the DE performance in both convergence rate and diversity.

III. THE PROPOSED IDE

In essence, the purposes of DE mutation operations and control parameters are to determine the searching direction and the size of the searching area, respectively. In this section, we

first discuss the influences of the control parameters on DE and give the IDP setting method. Then, we investigate the convergence features of DE with different mutation operators and propose the IDM strategy. Finally, we present the complete

number of local optima is huge, and its second best local optimum is far from the global optimum [48]. The function is very difficult to optimize and is a good candidate for studying the ability to jump out of local optima. The Rotated Schaffers F7 Function (c) is multimodal, non-separable, asymmetrical, and has a huge number of local optima. It is very suitable for investigating the exploration ability. The Rotated Expanded Saffer’s F6 Function (d) is multimodal, non-separable, and asymmetrical. Through it, the exploitation ability can be examined. All these benchmark functions are minimization problems.

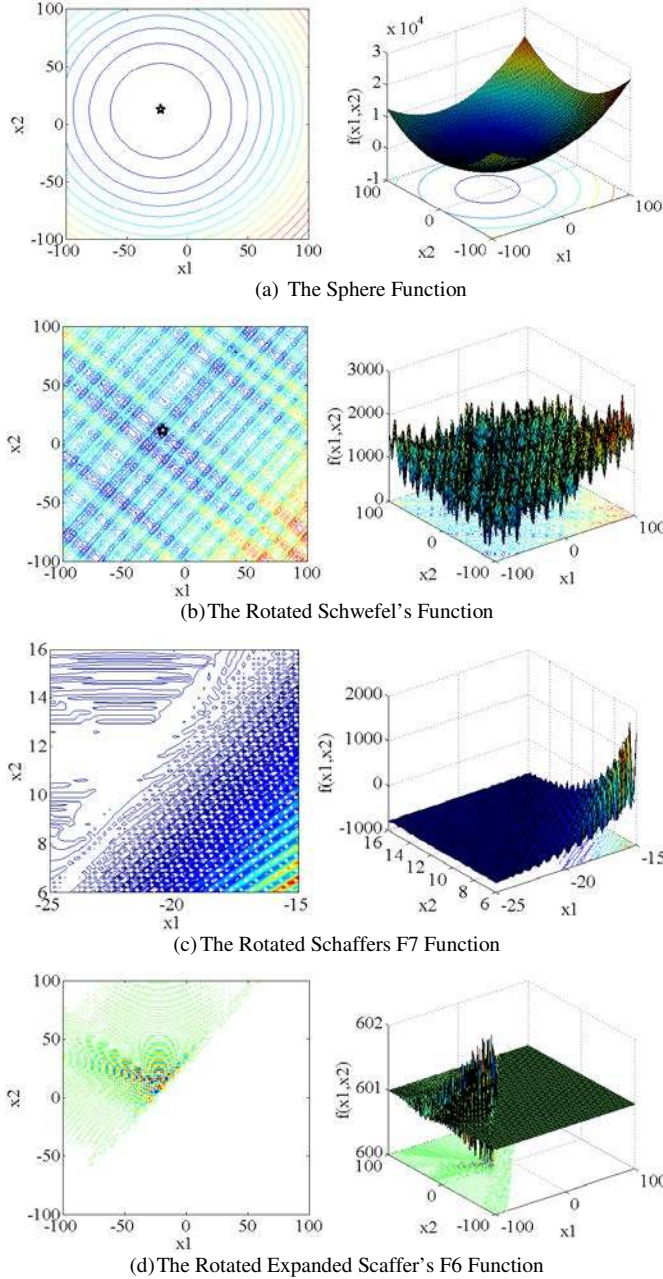


Fig. 2. The contour maps and the 3-D maps of four benchmark functions for the pilot experiments.

IDE procedure with these new strategies.

Specifically, to demonstrate the validity of the proposed strategies in this section, four typical functions introduced in the CEC 2013 benchmark suite [48] are employed to run the pilot experiments. The contour maps and the 3-D (three-dimensional) maps for 2-D benchmark functions are plotted in Fig. 2. The Sphere Function (a) is unimodal, continuous, differentiable, and separable. It is the benchmark for studying the convergence features. The Rotated Schwefel’s Function (b) is multimodal, rotated, non-separable, and asymmetrical. Its

A. Individual-Dependent Parameter Setting

From the illustration of the evolution operation of classic DE in Fig. 1, we can observe that the scale factor F is the parameter that controls the size of the searching area around the base individual \mathbf{x}_b , and the crossover rate CR indicates the probability of inheriting elements from the mutant individual \mathbf{v}_i in the process of constructing the trial individual \mathbf{u}_i .

We look at the effects of the control parameters in two cases, i.e., the unimodal Sphere Function and the multimodal Rotated Schwefel’s Function. For the Sphere Function expressed in Fig. 2 (a), it can be seen from the diagram that the individuals with better (smaller) fitness values have shorter distances to the global optimum in the center (marked by a black star) of concentric circles, whereas individuals with worse (larger) fitness values have longer distances. This suggests that to find better solutions, for superior base individuals, the mutation operations should exploit the searching area with a relatively small radius by employing a relatively small F value, and for inferior base individuals, they should jump out of the neighborhood area to explore more promising areas by using a relatively large value of scale factor. In terms of crossover, the offspring individuals should inherit more elements from the corresponding parent (target) individuals with a smaller CR value when the parent individuals are superior. In contrast, if the parent individuals are far away from the optimum, more promising offspring individuals are likely to be obtained by accepting more mutant elements with a larger CR value.

Based on this analysis, we propose to set the parameters F and CR in accordance with the differences between individuals’ fitness values. In other words, we propose that parameter setting should follow a general principle that the parameters for individuals with higher fitness values are larger, and vice versa. Using this principle, specific individual-dependent parameter setting can be devised. Two natural schemes are given below:

1) A rank-based scheme

Re-index all individuals in the current population in ascending order of their fitness (objective function) values, i.e., individual \mathbf{x}_i is the i th most superior one. The control parameter F_b associated with base individual \mathbf{x}_b and CR_i associated with target individual \mathbf{x}_i can be set using (1) and (2), respectively.

$$F_b = \frac{b}{NP} \quad (1)$$

$$CR_i = \frac{i}{NP} \quad (2)$$

2) A value-based scheme

Denote f_i as the fitness value of individual x_i in the current population. F_b and CR_i can be set as follows.

$$F_b = \frac{f_b - f_L + \delta_L}{f_U - f_L + \delta_L} \quad (3)$$

$$CR_i = \frac{f_i - f_L + \delta_L}{f_U - f_L + \delta_L} \quad (4)$$

Where f_L and f_U are the minimum and maximum fitness values, respectively, in the current population, and δ_L is the absolute value of the difference between the minimum fitness value and the second minimum (different from *the* minimum value) in the searching history up to the current population. Note that there may be more than one solution with the minimum fitness value, and the second minimum value has to be different from this minimum. The inclusion of δ_L prevents the parameters to be set to 0. Note also that it is not necessary to use the same scheme to set F and CR .

The situation for multimodal functions is more complicated than that for unimodal functions. We take as an example a typical multimodal case in Fig. 2 (b), i.e., the Rotated Schwefel’s Function. As we can observe, superior individuals are not always close to the global minimum (marked by a black star) because many local minima spread all over the searching space and confuse the search. In fact, relative to the superior individuals, the inferior individuals may be closer to the global minimum. Based on this observation, we randomize the parameters using a normal distribution with the mean specified to the original value and the standard deviation specified to 0.1. Denote a random number from a normal distribution by $randn(mean, std)$ [20]. Then, the IDP setting can be modified as follows.

$$F'_b = randn(F_b, 0.1) \quad (5)$$

$$CR'_i = randn(CR_i, 0.1) \quad (6)$$

With the randomization, the control parameter values near their mean values maintain search efficiency, while the parameter values away from those improve search diversity. If the parameter value drawn from the normal distribution is beyond the range of (0, 1), it will be ignored and a new value will be drawn until the parameter value is within the range.

To verify the idea of IDP setting, we run a pilot experiment on the four benchmark functions introduced above. The dimension of the problems (D) and the population size (NP) are set to 30 and 100, respectively. Based on the strategy DE/rand/1/bin, DEs with different parameter settings are applied to optimize the benchmark functions. These include $[F = 0.5/CR = 0.9]$ [2], $[F = 0.6/CR = 0.5]$ [15], $[F = 0.7/CR = 0.2]$ [34], the parameter setting in SaDE [25] (denoted by pSaDE), and the IDPs presented above. Four versions of IDP are tested. We use two letters to indicate the IDP parameter setting schemes, the first for F and the second for CR . For example, IDP_RV means that F is set using the rank-based scheme and CR is set using the

value-based scheme. For all pilot experiments, the maximum function evaluations (MaxFES) is set to 300,000 (i.e., the

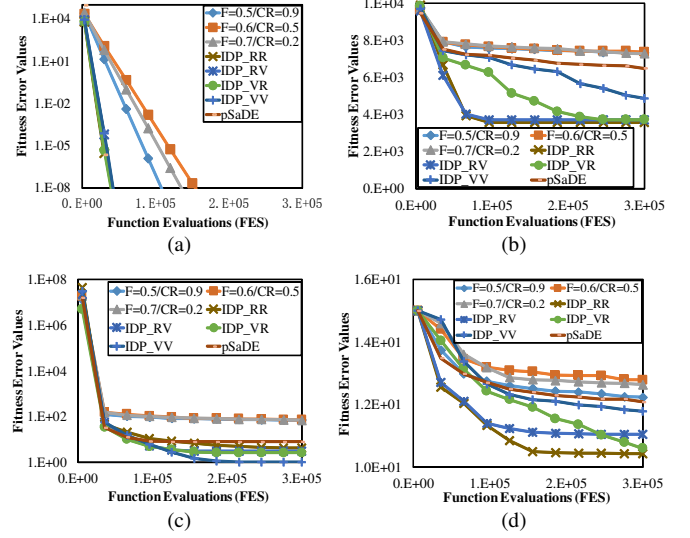


Fig. 3. Convergence curves of DEs with different parameter settings on four 30-D benchmark functions: (a) The Sphere Function, (b) The Rotated Schwefel’s Function, (c) The Rotated Schaffers F7 Function, and (d) The Rotated Expanded Scaffer’s F6 Function.

iteration number g_{max} is $3,000 = \text{MaxFES}/NP$) and the fitness error value of the best individual is sampled every 30,000 FES. For convenient illustration, the convergence curves of different DEs on four problems are plotted in Fig. 3. The horizontal axis is the number of FES, and the vertical axis is the average of the fitness error values over 51 [48] independent runs.

The parameters generated by the value-based scheme adjust the size of the searching area more precisely, and the parameters generated by the rank-based scheme are uniformly distributed in the range [0, 1]. The diagrams clearly show that the IDP settings outperform other parameter settings in all cases. Among the four IDPs, IDP_RR achieves the best performance and is selected as the parameter setting in IDE.

A recently proposed DE variant Rank-DE [33] employs a similar ranking-based scheme to select some individuals in mutation operators. This is different from IDE, which uses the scheme to calculate the values of the control parameters. The comparison of these two algorithms is carried out in Section IV.

B. Individual-Dependent Mutation Strategy

Mutation is an operation for obtaining the mutant individuals in the area around the base individual. In the mutation operator of classic DE, the base individual serves as the center point of the searching area, the difference vector sets the searching direction, and the scale factor controls the movement step. Considering the mutation and crossover strategies used, the evolutionary operation of DE can be denoted using a four-parameter notation **DE/base/differ/cross** [3]. There are several widely used mutation strategies with different kinds of base vectors and different numbers of difference vectors, e.g., DE/rand/1, DE/best/1, DE/current-to-best/1, DE/rand/2, and DE/best/2. The single base vector mutation strategy DE/best/

differ performs better in convergence rate, since the mutation operation is implemented as a local search around the best

iteration process. These results suggest that a better performance may be obtained by using a composite base vector

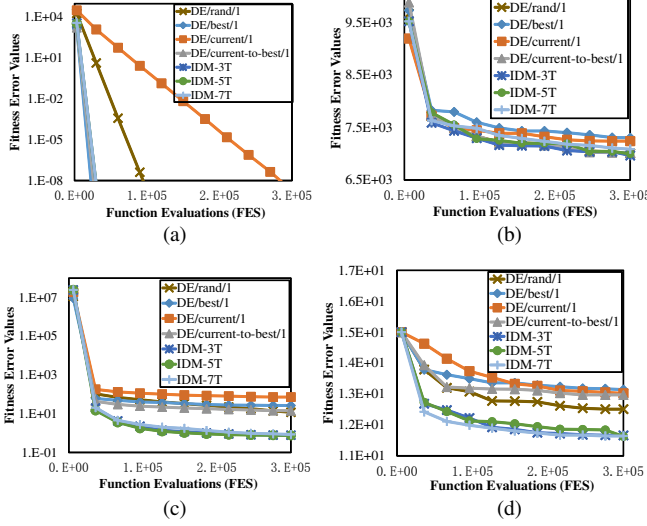


Fig. 4. Convergence curves of DEs with different mutation strategies on four 30-D benchmark functions: (a) The Sphere Function, (b) The Rotated Schwefel’s Function, (c) The Rotated Schaffers F7 Function, and (d) The Rotated Expanded Scaffer’s F6 Function.

individual. However, it is very easy to be trapped in local minima, leading to premature convergence. On the contrary, the single base vector mutation strategy DE/current/differ, which uses the target (current) individual as the base vector, has a high diversity and performs better in global searching ability. In this case, without the best individual guiding the evolution, the algorithm searches the solution space sufficiently but slowly and aimlessly. Therefore, the strategy DE/rand/differ, in which the base vector is randomly selected from the current population at each generation, can be considered as a balance between DE/best/differ and DE/current/differ. As for the operator DE/current-to-best/1, it can be employed as a mixed strategy that combines a current individual and a best individual as the **origin** (start) individual and the **guiding** (terminal) individual, respectively, to form a composite base vector. To clearly define the mutation operators with composite base vectors in this paper, we denote them as DE/**origin**-to-**guiding**/differ, where “origin” and “guiding” are to be specified.

To illustrate the searching characteristics of these four mutation strategies, i.e., DE/rand/1, DE/best/1, DE/current/1, and DE/current-to-best/1, we use the same four benchmark functions and experiments configuration above, and we set $F = 0.5$ and $CR = 0.5$. The convergence curves are plotted in Fig. 4.

The experiment results demonstrate that, among the four, DE/best/1 is the fastest strategy in unimodal function, but also the most unstable strategy in multimodal functions due to premature convergence. While a good diversity enables DE/current/1 to avoid premature convergence, its convergence rate is poor. DE/current-to-best/1 does not achieve the best performance in convergence rate or in population diversity, but it can locate the global optimum faster than DE/current/1, and it can escape from local minima with better diversity than DE/best/1. DE/rand/1 is a robust strategy with strong performance in the multimodal functions, especially at the later

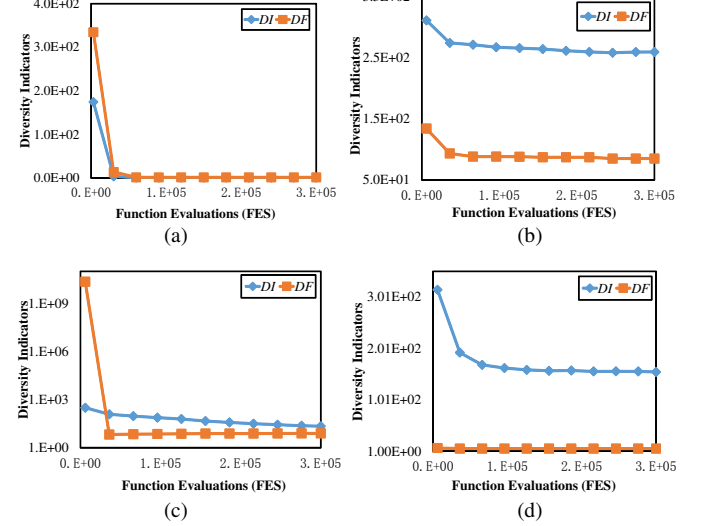


Fig. 5. The curves of the diversity of individuals (*DI*) and the diversity of fitness (*DF*) values on four 30-D benchmark problems: (a) The Sphere Function, (b) The Rotated Schwefel’s Function, (c) The Rotated Schaffers F7 Function, and (d) The Rotated Expanded Scaffer’s F6 Function.

that integrates a diversity element and a rapidity element, and by incorporating a random individual in the mutation operation.

In addition, from the convergence curves plotted in Fig. 3 and Fig. 4, we can observe that most algorithms perform more effectively with a high convergence rate in the earlier stage of the searching process relative to the later stage, especially for multimodal functions. At the later stage, the algorithms are easily trapped in local optimal solutions due to poor population diversity. To investigate the variation of the diversity of the population, we apply the classical DE (DE/rand/1/bin with $F = 0.5$ and $CR = 0.5$) to optimize the four benchmark functions and observe the diversities of individuals and fitness values in each generation. We define the diversity indicators for each generation as the standard deviations of the individuals and of their fitness values. They are denoted as *DI* and *DF*, respectively, and can be calculated as follows.

$$DI = \frac{1}{NP} \sqrt{\sum_{i=1}^{NP} \left\| \mathbf{x}_i - \frac{1}{NP} \sum_{j=1}^{NP} (\mathbf{x}_j) \right\|^2} \quad (7)$$

$$DF = \frac{1}{NP} \sqrt{\sum_{i=1}^{NP} \left(f(\mathbf{x}_i) - \frac{1}{NP} \sum_{j=1}^{NP} f(\mathbf{x}_j) \right)^2} \quad (8)$$

The curves of diversity indicators *DI* and *DF* are plotted in Fig. 5. The curves show that *DI* and *DF* decrease gradually as the iteration continues. In other words, the diversity of the population becomes poorer with the algorithm iteration. This is the inevitable trend of algorithm convergence. However, if the algorithm has not yet focused on the neighborhood of the global optimal solution at the later stage of the searching process, it is very hard to jump out of the local minima without good exploration ability. Meanwhile, the difference between the superior individuals and the inferior individuals are

insignificant when they gather together around the best solution found so far at the later stage.

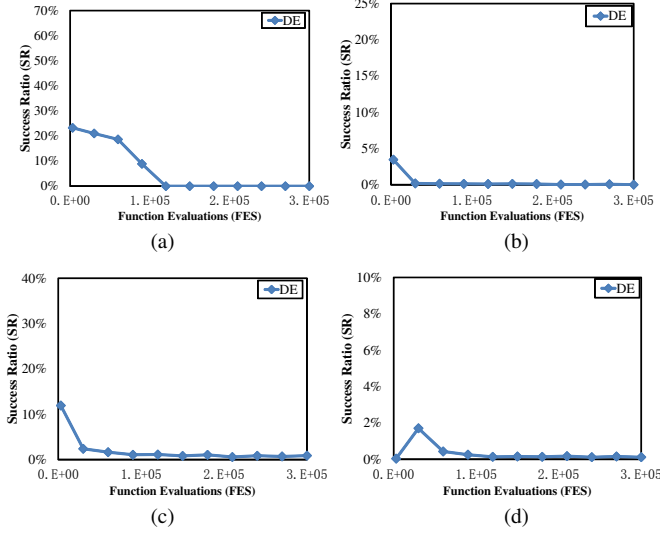


Fig. 6. The success ratio curves of classic DE on four 30-D benchmark problems: (a) The Sphere Function, (b) The Rotated Schwefel's Function, (c) The Rotated Schaffers F7 Function, and (d) The Rotated Expanded Scaffer's F6 Function.

Considering the analysis above, we first adopt the “current” individual as the origin individual (DE/current-to-**guiding**/1) for the purpose of diversity at the earlier stage, and we then employ the “rand” individual as the origin individual (DE/rand-to-**guiding**/1) to accelerate the convergence rate at the later stage. We combine these origin individuals according to their different fitness values with other specified individuals as the guiding ones to form the composite base vectors to guide the searching direction. To utilize the fitness information of the origin individuals, we first use the re-index result in the IDP setting to classify the individuals in the population into two sets, i.e., a superior set S and an inferior set I , and then choose the guiding individuals for the origin individuals in different sets. The set S contains a proportion of individuals in the generation with the best rankings. Only with the proper direction will the searching of the population be more efficient. For individuals in S , because better solutions tend to be found in their neighborhoods, an omnidirectional local search should be implemented. We therefore employ DE/**origin**-to-rand/1 to generate the mutant individuals when the corresponding origin individuals are superior. For individuals in I , we employ relatively better individuals to guide their searching directions and thus present a mutation operator DE/**origin**-to-better/1.

This new mutation strategy can be expressed as follows.

$$\mathbf{v}_{i,g} = \mathbf{x}_{o,g} + \begin{cases} F_o \cdot (\mathbf{x}_{r_1,g} - \mathbf{x}_{o,g}) + F_o \cdot (\mathbf{x}_{r_2,g} - \mathbf{x}_{r_3,g}) & i \in S \\ F_o \cdot (\mathbf{x}_{better,g} - \mathbf{x}_{o,g}) + F_o \cdot (\mathbf{x}_{r_2,g} - \mathbf{x}_{r_3,g}) & i \in I \end{cases} \quad (9)$$

$$0 \neq r_1 \neq r_2 \neq r_3$$

Where o is the index of the origin individual which is the current individual ($o = i$) at the earlier stage of the iteration process, and a random individual at the later stage of the

process, according to the previous analysis. Indexes r_1 , r_2 , and r_3 are randomly selected from the range $[1, NP]$ and are different from each other and from the target index i . $better$ is the index of the better individual randomly selected from the superior individual set S in the current generation.

Now, the issue is how to select one generation index threshold g_t between 1 and g_{max} to divide the iteration process into two stages, i.e., the earlier and the later, to determine the specified origin individuals $\mathbf{x}_{o,g}$ in (9). From the convergence curves plotted in Fig. 3 and Fig. 4, we can observe that an algorithm has different convergence rates on different problems with different difficulty degrees. Therefore, g_t varies for different problems. To further express the convergence process, the success ratio (SR) curves of classic DE on solving four 30-D problems are plotted in Fig. 6. The success ratio of each generation g is defined by

$$SR_g = \frac{NS_g}{NP}, \quad (10)$$

where NS_g is the number of offspring individuals that can successfully enter the next generation $g+1$. Because SR tends to decrease continually from a relative larger value as the iteration progresses, it can be employed as an indicator to identify whether the earlier stage ends. Generally, we can say that an algorithm enters the later stage of the convergence process when SR_g equals to zero for a given number of consecutive generations T . For the Sphere Function (a) and the Rotated Schwefel's Function (b), SR can decrease to near zero after a number of iterations with efficient searching. However, for the Rotated Schaffers F7 Function (c) and Rotated Expanded Scaffer's F6 Function (d), the value of SR at the later stage is close to but always larger than zero until the end of iteration. Therefore, an auxiliary generation index threshold G_T and a success ratio threshold SR_T are introduced into IDM to help select the generation index threshold g_t as follows.

$$g_t = \text{Min}\{g' \mid SR_{g'} \leq SR_T, \forall g' \in [g'-T, g']\} \quad (11)$$

$$g' = T + 1, \dots, g_{max}$$

Where g and g' are the generation indexes, and T is set to $1000D/NP$. In (11), SR_T is 0 before G_T+1 , and SR_T is 0.1 after G_T . The value of G_T is determined in the next pilot experiment.

Further, in response to the decreased population diversity, we propose a proportion model to gradually increase the proportion of individuals in S as the algorithm progresses. The proportion of superior individuals in the population is set as the following exponential function of the generation index g .

$$ps = 0.1 + 0.9 \times 10^{5(g/g_{max}-1)} \quad (12)$$

This function is plotted in Fig. 7, where the x axis denotes the iteration process ($x = g/g_{max}$), and the y axis is the proportion of individuals. At any point of the iteration process, the proportion of superior individuals in the population is the height of ps , and the proportion of inferior individuals is represented by the distance between ps and $y = 1$. With the proportion model, at the beginning of the iteration, most mutant individuals are

generated by DE/current-to-better/1 with good diversity. And

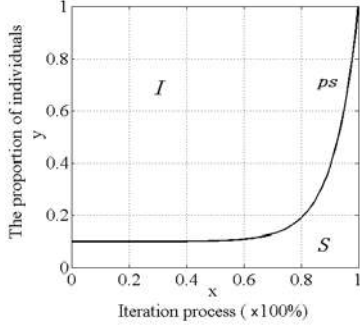


Fig. 7. A proportion model for the classification of individuals in the IDM strategy.

DE/current-to-rand/1 is employed to exploit the neighborhoods of the superior individuals. As the evolution progresses, an increasing number of random individuals are employed to guide the searching and maintain the diversity. Since the differences between the individual fitness values become smaller at the later stage of evolution, most individuals can be regarded as superior, and DE/rand/2 can be utilized to avoid trapping individuals into the local minima with a maximum of diversity. For the remaining, inferior individuals, DE/rand-to-better/1 is employed to accelerate the convergence.

To further enhance the global searching ability of the algorithm, we introduce perturbations in the difference vectors with small probability to help the base individuals move out of the local area. Combining the different components described above, the IDM strategy can be presented as follows.

$$\mathbf{v}_{i,g} = \mathbf{x}_{o,g} + \begin{cases} F_o \cdot (\mathbf{x}_{r_1,g} - \mathbf{x}_{o,g}) + F_o \cdot (\mathbf{x}_{r_2,g} - \mathbf{d}_{r_3,g}) & i \in S \\ F_o \cdot (\mathbf{x}_{better,g} - \mathbf{x}_{o,g}) + F_o \cdot (\mathbf{x}_{r_2,g} - \mathbf{d}_{r_3,g}) & i \in I \end{cases} \quad (13)$$

$o \neq r_1 \neq r_2 \neq r_3$

The indexes o , r_1 , r_2 , and r_3 are selected in the same way as in (9). $\mathbf{d}_{r_3,g}$ is a disturbed individual derived from the current population with possible elements randomly taken from the entire solution space. Each element of $\mathbf{d}_{r_3,g}$ is determined in the following way.

$$d_{r_3,g}^j = \begin{cases} L^j + rand(0,1) \cdot (U^j - L^j), & \text{if } (rand_i^j(0,1) < p_d) \\ x_{r_3,g}^j, & \text{otherwise} \end{cases} \quad (14)$$

Where the probability factor of disturbance p_d is set to be $0.1 \times ps$, L^j and U^j are the lower and the upper bound values of the j th element. To conclude IDM, we list the mutation operators for different individuals at different stages of iteration in Table I. The notation “(p)” denotes the perturbations introduced to difference vectors. It can be summarized that, in the new strategy, the **origin** individuals are current and random individuals at earlier ($g \leq g_t$) and later stages ($g > g_t$), respectively. Additionally, the **guiding** individuals are random individuals and better individuals relative to the superior and inferior **origin** individuals, respectively.

To verify the effectiveness of the IDM strategy, we take the same functions above to compare the performances of three

IDMs (denoted by IDM-3T, IDM-5T, and IDM-7T) with

TABLE I
THE MUTATION OPERATORS IN IDM STRATEGY

Generation Index	Target Individual	Mutation Operator
$g \leq g_t$	superior	DE/current-to-rand/1(p)
$g \leq g_t$	inferior	DE/current-to-better/1(p)
$g > g_t$	superior	DE/rand/2(p)
$g > g_t$	inferior	DE/rand-to-better/1(p)

different G_T values (i.e., 3T, 5T, and 7T) and the four previous mutation strategies with the same control parameter configuration ($F = 0.5$, $CR = 0.5$), and add the corresponding convergence curves in Fig. 4.

As the diagrams illustrate, IDMs obtain the best performance in multimodal cases. For unimodal cases, even though the perturbations weaken the convergence rate, the IDMs achieve a competitive performance. Three IDMs have similar performances, and IDM-5T is taken as the mutation strategy of IDE. Combining different origin individuals with corresponding guiders at different stages of the searching process, the new strategy simultaneously improves diversity and accelerates convergence. Moreover, with the perturbations, the IDM strategy is better able to jump out of the local minima to search for the global minimum in multimodal cases.

C. The Complete Procedure of the Proposed IDE

Incorporating the novel IDP setting and IDM strategy introduced above, we can now present the whole IDE, following the classic DE framework.

1) Initialization

The initialization of IDE is the same as in classic DE. Generate the initial population and set up the relevant parameters: NP and g_{max} ($g_{max} = \text{MaxFES}/NP$).

2) Mutation

For each generation g , all individuals are re-indexed in ascending order of their fitness (objective function) values and classified into two sets via (12). Then, the mutant individuals are generated by IDM strategy as (13).

The value of the scale factor is dependent on the origin individual $\mathbf{x}_{o,g}$ in the base vector and is derived from the normal distribution in (5) with a mean value calculated by (1), i.e., rank-based scheme.

3) Crossover

In our approach, the binary crossover operation in classic DE is adopted to generate the trial individuals. The formula of the crossover operation is expressed as Step 2.3 in Algorithm 1.

The value of the crossover rate is dependent on the target individual $\mathbf{x}_{i,g}$ and derived from the normal distribution in (6) with a mean value calculated by (2), i.e., rank-based scheme. Reinitialize the corresponding components of trial individuals that violate the boundary constraints.

Algorithm 1 Pseudo-code for the IDE

Step 1: Initialization

Set up the maximum generation number g_{max} , generation index $g = 0$ and randomly initialize a population of NP individuals $\mathbf{P}_g = \{\mathbf{x}_{1,g}, \dots, \mathbf{x}_{NP,g}\}$ with $\mathbf{x}_{i,g} = \{x_{i,g}^1, \dots, x_{i,g}^D\}$ and each individual is uniformly distributed in the range $[L, U]$ with $i = \{1, 2, \dots, NP\}$.

Step 2: Evolution Iteration

WHILE the termination criterion is not satisfied
DO

Step 2.1: Rearrangement

Re-index the individuals of current population in ascending order according to their fitness (objective function) values, classify them into two sets: the superior (S) and the inferior (I) using the proportion model.

Step 2.2: Mutation Operation

FOR $i = 1$ TO NP

Randomly choose four different individuals $\mathbf{x}_{o,g}$, $\mathbf{x}_{r1,g}$, $\mathbf{x}_{r2,g}$ and $\mathbf{x}_{r3,g}$ from current population. Set $o = i$ when $g \leq g_t$. Use rank-based IDP strategy to generate the F_o for the individual $\mathbf{x}_{o,g}$, as:

$$F_o = \text{randn}\left(\frac{o}{NP}, 0.1\right).$$

Generate mutant vector $\mathbf{v}_{i,g}$ via the IDM strategy as:

$$\mathbf{v}_{i,g} = \mathbf{x}_{o,g} + \begin{cases} F_o \cdot (\mathbf{x}_{r1,g} - \mathbf{x}_{o,g}) + F_o \cdot (\mathbf{x}_{r2,g} - \mathbf{d}_{r3,g}) & i \in S \\ F_o \cdot (\mathbf{x}_{better,g} - \mathbf{x}_{o,g}) + F_o \cdot (\mathbf{x}_{r2,g} - \mathbf{d}_{r3,g}) & i \in I \end{cases}$$

$$o \neq r_1 \neq r_2 \neq r_3.$$

END FOR

Step 2.3: Crossover Operation

FOR $i = 1$ TO NP

Employ rank-based IDP strategy to generate

$$CR_i = \text{randn}\left(\frac{i}{NP}, 0.1\right) \text{ for the target individual } \mathbf{x}_{i,g}.$$

Generate trial vector $\mathbf{u}_{i,g}$ through binomial crossover as follow.

FOR $j = 1$ TO D

$$u_{i,g}^j = \begin{cases} v_{i,g}^j, & \text{if } (\text{rand}_i^j(0,1) \leq CR_i \text{ or } j = j_{\text{rand}}) \\ x_{i,g}^j, & \text{otherwise} \end{cases}$$

IF $(u_{i,g}^j < L^j \text{ or } u_{i,g}^j > U^j)$

$$u_{i,g}^j = L^j + \text{rand}_i^j(0,1) \cdot (U^j - L^j)$$

END IF

END FOR

END FOR

Step 2.4: Selection Operation

Evaluate the trial vector $\mathbf{u}_{i,g}$

FOR $i = 1$ TO NP

$$\mathbf{x}_{i,g+1} = \begin{cases} \mathbf{u}_{i,g}, & \text{if } (f(\mathbf{u}_{i,g}) \leq f(\mathbf{x}_{i,g})) \\ \mathbf{x}_{i,g}, & \text{otherwise} \end{cases}$$

END FOR

Step 2.5: Increase the Generation Count

$g = g + 1$

END WHILE

4) Selection

As in classic DE, after comparing each target individual with a corresponding trial individual, the individual with the smaller fitness value will enter the next generation.

The pseudo-code of IDE is expressed in Algorithm 1.

IV. EXPERIMENTATION

In this section, extensive experiments are carried out to evaluate the IDE performance. We employ the latest 28 test functions (including 5 unimodal functions and 23 multimodal functions) in the CEC 2013 benchmark suite. Please refer to literature [48] for complete information and details about the CEC 2013 benchmark suite.

We present the experiment results in four subsections. First, in Section IV-A, we evaluate several IDEs with different strategy configurations through the problems suite to further verify the effectiveness of the proposed strategies. In Section IV-B, we compare the performance of IDE against five state-of-the-art DE variants. Subsequently, we evaluate the performance of IDE against ten up-to-date DE variants in Section IV-C. In Section IV-D, the comparison is performed between IDE and three other well-known EAs. All the evaluation experiments are implemented by MATLAB 7.8 and SPSS 21 on a personal computer with the Intel 2.83GHz CPU, 4 GB memory, and Windows 7 operating system.

The dimensionality of the problems are 10, 30, and 50 [48], and the corresponding population sizes for IDE are set to 50, 100, and 200, respectively, which are commonly used and suggested in the literature ([15], [34], and [49]). To have a reliable and fair comparison, the recommended parameter configurations (including the values of NP , F , CR , and other additional parameters) are set for all competitor algorithms as introduced in their original papers.

For each algorithm to be tested, we use \mathbf{x}^* and \mathbf{x}' to indicate the known optimum solution and the best solution obtained once the search stops after $10^4 \times D$ function evaluations [48], respectively. Therefore, the fitness error value $F(\mathbf{x}') - F(\mathbf{x}^*)$ is employed to evaluate the algorithms' performance, and the values smaller than $1.0E-08$ are taken as zero. Unless otherwise noted, each algorithm is run 51 times [48] in all instances to obtain the numerical results. The mean error (denoted by Mean) of the 51 runs and the corresponding standard deviation (denoted by Std) are calculated and presented in a number of tables. Due to space limitation, these tables are omitted in the main text of this paper. However, they can be found in the supplementary file of the paper. In the supplementary file, according to the mean error value, we have highlighted the best performance for each benchmark function by shading the background of the cell.

To get a statistical conclusion of the experimental results, the two-sided Wilcoxon rank sum test [50], [51] is applied to assess the significance of the performance difference between IDE and each competitor. Specifically, the null hypothesis in all pairs is that the observations of solutions obtained by both algorithms compared are independent and identically

distributed. The value of significance level α is set to be 5% (0.05). When the null hypothesis is rejected, we mark those cases with “+” and “-” to indicate that the competitor algorithm exhibits superior performance relative to IDE and that IDE performs better with significant difference, respectively. We mark cases with “=” if there is no statistically significant difference between the performances of compared algorithms. In addition, to have a more direct evaluation of the performance of these algorithms, the numbers of the three kinds of statistical significance cases (-/=+) and the number of best results (Number of Best abbreviated as NoB) obtained by the corresponding algorithm for all functions in each test group are listed at the bottom of the numerical results tables. The convergence curves in terms of the mean error values of the best solutions of each algorithm for three multimodal functions used previously with $D = 30$ are expressed. To plot the curves, the fitness error values are sampled after $(0.01, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0) \times \text{MaxFES}$ for each run [48]. The curves of the 30-D Sphere Function are not considered here because most algorithms can easily find the global optimum solution within a few sampling points.

A. Evaluation on the strategies in IDE

The new variant DE proposed in this paper includes two core components: IDP and IDM strategies. In this subsection, IDE is compared with its five variants with different configurations to identify the benefits from the IDP and IDM components.

First, to evaluate the IDP setting, we use IDP-r(F, CR), IDP-r(F), and IDP-r(CR) to denote the IDE variants which assign random values uniformly selected from (0,1) for the parameters in parentheses. In other words, the values of control parameters in IDP-r() are no longer associated with the rankings of corresponding individuals.

Second, for the validation of the IDM strategy, we denote the IDE variant without perturbations and the IDE variant with the mutation strategy of classic DE by IDEwo(p) and IDEwoIDM, respectively.

The detailed numerical results for the comparisons of these IDEs are listed in Tables I - III in the supplementary file. To show the performance clearly, we summarize the number of the best results graphically in Fig. 8 (a) and list statistical significance results of the comparison between each of the IDE variants and the proposed IDE in Table II. From the histogram in Fig. 8 (a), we can observe that IDE achieves the best results in 12, 18, and 15 cases for the 10-D, 30-D, and 50-D problems, respectively. Regarding the total number of the best results obtained by algorithms in three different dimensional groups, the variants IDP-r(F) and IDP-r(CR) yield the best results in 22 (=11+6+5) and 25 (=10+9+6) cases, respectively, which are more than the number obtained by IDP-r(F, CR), i.e., 17 (=6+6+5). Additionally, from the Tables I - III in the supplementary file we can see that IDP-r(F) and IDP-r(CR) achieve better mean values than IDP-r(F, CR) in most problems, especially high dimensional cases. It is also clear that, IDEwo(p)

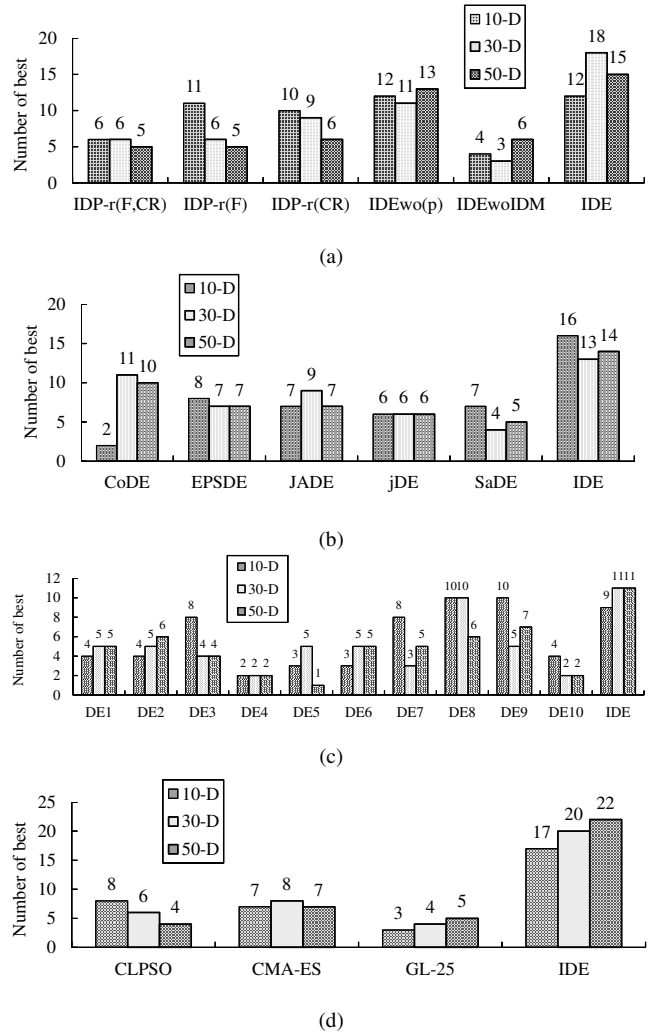


Fig. 8. Number of cases on which each algorithm performs the best in the comparison between different variants of IDE (a), the comparison between IDE with five state-of-the-art DEs (b), the comparison between IDE with ten up-to-date DEs (c), and the comparison between IDE with three EAs (d).

performs much better (36=12+11+13) than IDEwoIDM (13 cases). In the comparison results of statistically significant difference listed in Table II, for 10-D problems, it is clear that IDE outperforms the other IDE variants with significant difference in 13, 9, 6, 3, and 23 cases, and it achieves the performance similar to IDP-r(F, CR), IDP-r(F), IDP-r(CR), and IDEwo(p) in most cases. However, relative to these variants, the performance superiority of IDE becomes gradually more significant with the increase of the problems' dimension. For the 30-D problems, IDE performs significantly better than IDP-r(F, CR), IDP-r(F), IDP-r(CR), IDEwo(p), and IDEwoIDM on 20, 20, 16, 6, and 23 functions, respectively. For the 50-D problems, these figures are 19, 19, 17, 4, and 17, respectively. Furthermore, from the convergence curves plotted in Fig. 9 (a) - (c), we can observe that IDP-r(F) and IDP-r(CR) always converge faster than IDP-r(F, CR), and IDEwo(p) outperforms IDEwoIDM on these functions. Despite the fact that IDEwo(p) and IDP-r(CR) achieve better solutions in cases (a) and (c), respectively, there is no statistically significant difference between them and IDE.

TABLE II
COMPARISON RESULTS OF STATISTICALLY SIGNIFICANT DIFFERENCES OF IDE WITH ALL COMPETITORS ON 10-D, 30-D, AND 50-D PROBLEMS

Algorithms	Dimensions of the Benchmark Functions								
	10-D			30-D			50-D		
	-	=	+	-	=	+	-	=	+
IDP-r(<i>F,CR</i>)	13	15	0	20	8	0	19	6	3
IDP-r(<i>F</i>)	9	15	4	20	7	1	19	8	1
IDP-r(<i>CR</i>)	6	22	0	16	9	3	17	8	3
IDEwo(p)	3	22	3	6	22	0	4	22	2
IDEwoIDM	23	5	0	23	5	0	17	10	1
CoDE	23	5	0	11	9	8	14	6	8
EPSDE	11	13	4	18	5	5	17	6	5
JADE	14	8	6	12	9	7	14	8	6
jDE	19	7	2	16	7	5	19	5	4
SaDE	18	8	2	19	6	3	18	4	6
DE1	15	9	4	14	7	7	14	6	8
DE2	19	4	5	19	4	5	16	6	6
DE3	17	4	7	21	4	3	20	4	4
DE4	18	6	4	23	3	2	21	4	3
DE5	17	8	3	16	8	4	20	2	6
DE6	19	7	2	17	5	6	16	6	6
DE7	15	7	6	18	6	4	15	6	7
DE8	16	4	8	17	5	6	16	5	7
DE9	9	11	8	12	6	10	11	7	10
DE10	20	7	1	23	5	0	24	4	0
CLPSO	16	7	5	23	5	0	24	3	1
CMA-ES	20	3	5	19	4	5	18	4	6
GL-25	22	6	0	24	4	0	23	4	1

B. Comparison with state-of-the-art DE Variants

In this subsection, we compare the proposed IDE with five state-of-the-art DE variants that have been reported to have good performance.

- 1) CoDE: the DE with composite mutation strategies and parameters [27];
- 2) EPSDE: the DE with an ensemble of parameters and mutation strategies and an SaDE type learning strategy [29];
- 3) JADE: the DE with adaptive control parameters and optional external archive [20];
- 4) jDE: the DE with self-adaptive control parameters [43];
- 5) SaDE: the DE with adaptive strategy [25].

The experimental results of Number of Best are expressed in Fig. 8 (b). Tables IV - VI in the supplementary file report the experimental results for these DE variants in 10-D, 30-D, and 50-D problems, respectively. From the diagram we can observe that for the 10-D problems, IDE obtains the best results in 16

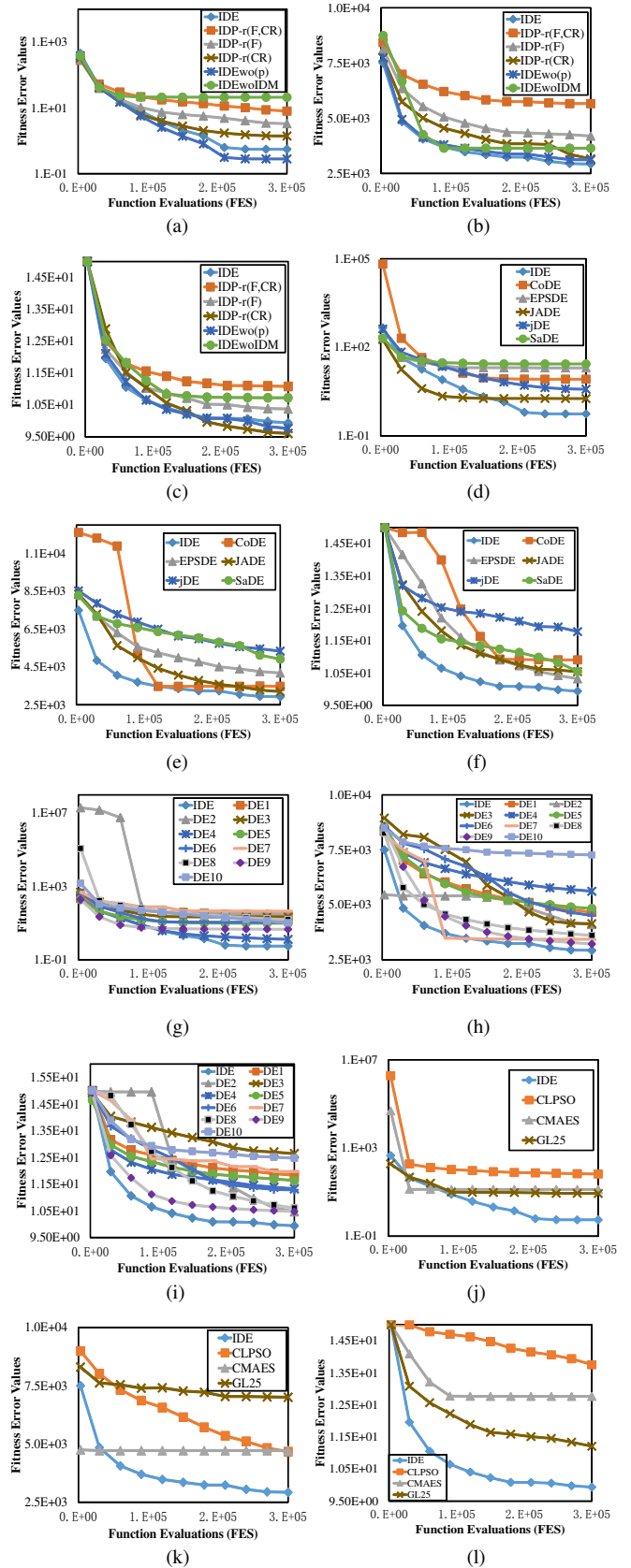


Fig. 9. Convergence curves of different variants of IDE (a)-(c), different DEs in Subsection IV-B (d)-(f), different DEs in Subsection IV-C (g)-(i), and IDE and different EAs in Subsection IV-D (j)-(l) on three 30-D problems: The Rotated Schaffers F7 Function, The Rotated Schwefel’s Function, and The Rotated Expanded Scaffer’s F6 Function, respectively.

cases, while CoDE, DPSDE, JADE, jDE, and SaDE achieve the best results for 2, 8, 7, 6, and 7 functions, respectively. IDE keeps this obvious advantage in both 30-D and 50-D problems. Moreover, on the 10-D problems the IDE solution is significantly superior to those of CoDE, EPSDE, JADE, jDE, and SaDE on 23, 11, 14, 19, and 18 functions, respectively, as shown in Table II. The comparative results in the reverse direction are only 0, 4, 6, 2, and 2 respectively. For the 30-D and 50-D problems, even though the performance differences between IDE and CoDE are smaller than those for the 10-D problems, the cases of equal performances increase. Additionally, the advantages of IDE over the other DE variants are similar to those for the 10-D problems. From the convergence curves of IDE and state-of-the-art DEs plotted in Fig. 9 (d) - (f), we can observe that the best results for the three typical multimodal problems are obtained by IDE.

C. Comparison against up-to-date DE Variants

In this subsection, IDE is compared with nine up-to-date DE variants which are all published on the proceedings of CEC 2013 and one recently proposed Rank-DE.

- 1) b6e6rl: the variant of adaptive DE with twelve competing strategies [46];
- 2) SMADE: the DE with super-fit multicriteria strategy [30];
- 3) DE-APC: the DE with automatic parameter configuration [36];
- 4) PVADE: the DE with population's variance-based adaptive strategy [47];
- 5) jDE_{soo}: the variant of jDE [31];
- 6) SPSRDEMMS: the structured population size DE with multiple mutation strategies [32];
- 7) DEcfbLS: the DE with concurrent fitness based local search [40];
- 8) TLBSaDE: the DE with teaching and learning best strategy [26];
- 9) SHADE: the adaptive DE with success-history based scheme [45];
- 10) Rank-DE: the improved version of classic DE with ranking-based mutation operator [33].

For the purpose of a simplified presentation, we denote the ten DE variants listed above by DE1 - DE10, respectively. Tables VII - IX in the supplementary file report the experimental results for these DE variants in 10-D, 30-D, and 50-D problems, respectively. From the NoB diagram in Fig. 8 (c) and the statistical results in Table II, we can observe that for the 10-D problems the proposed IDE yields the best results for 9 of the 28 functions, and performs significantly better than the ten up-to-date DEs on 15, 19, 17, 18, 17, 19, 15, 16, 9, and 20 functions, respectively. When counting the insignificant cases, IDE performs better than or the same as these DEs on 24, 23, 21, 24, 25, 26, 22, 20, 20, and 27 functions, respectively. The comparison results on the 30-D and 50-D problems are similar to those on the 10-D problems, with the proposed algorithm performing even better. From the results, we can see that IDE obtains the best results for 11 cases of the 30-D problems and for 11 cases of the 50-D problems, respectively. While these

figures for the latest DEs are fewer than 11 and 8 cases. Of the 28 functions for the 30-D problems, IDE performs better than or the same as the other ten on 21, 23, 25, 26, 24, 22, 24, 22, 18, and 28 functions. For 50-D problems, these figures are 20, 22, 24, 25, 22, 22, 21, 21, 18, and 28. Note that in the convergence curves in Fig. 9 (g) - (i), the convergence performance of IDE is the best among these DEs for the three typical functions.

D. Comparison with non-DE Evolutionary Algorithms

IDE is further compared with three other evolutionary algorithms.

- 1) CLPSO: the comprehensive learning particle swarm optimizer [52];
- 2) CMA-ES: the evolution strategies with completely derandomized self-adaptation [53];
- 3) GL-25: the global and local real-coded genetic algorithms with parent-centric crossover operators [54].

In CLPSO, introduced by Liang *et al.* in 2006 [52], the best historical information of each particle is utilized to update the corresponding velocity vector. Hansen and Ostermeier in 2001 [53] proposed CMA-ES, a powerful variant of evolution strategy (ES). Garcia-Martinez *et al.* in 2008 [54] presented GL-25, which integrates the global and local search abilities to construct a kind of real-coded genetic algorithm. In our experiments, for all non-DE algorithms, the associated control parameters are set in accordance with their original papers.

The experimental results on the 10-D, 30-D, and 50-D problems are listed in Tables X - XII, respectively, in the supplementary file. Fig. 8 (d) provides the results of NoB. For the 10-D problems, IDE achieves the best results in 17 cases, while CLPSO, CMA-ES, and GL-25 achieve the best results in 8, 7, and 3 cases, respectively. IDE significantly outperforms these three EAs on 16, 20, and 22 of the 28 functions, and performs worse on far fewer functions, as shown in Table II. In addition, IDE shows similar or even better comparative performance for the 30-D and 50-D problems. Similar to the results of the previously described comparisons, IDE performs best in convergence rate as expressed in Fig. 9 (j) - (l).

E. Discussion on IDE

For each origin individual in the composite base vector and for each target individual, the IDP setting assigns control parameters based on the differences between fitness values such that the better individuals tend to be assigned relatively smaller values of parameters (both F and CR). Even though the individuals' fitness values and their distance from the optimum is less correlated, especially in multimodal cases, the better individuals are more likely to be found in the neighborhoods close to the superior individuals and in the areas relatively far away from the inferior individuals.

As is evident in the results shown in Subsection IV-A, in most cases, IDE with the IDP setting performs better than IDP-r(F) and IDP-r(CR), both of which achieve a similar performance and obtain better results relative to the variant IDP-r(F, CR). With the individual-dependent scheme, IDM

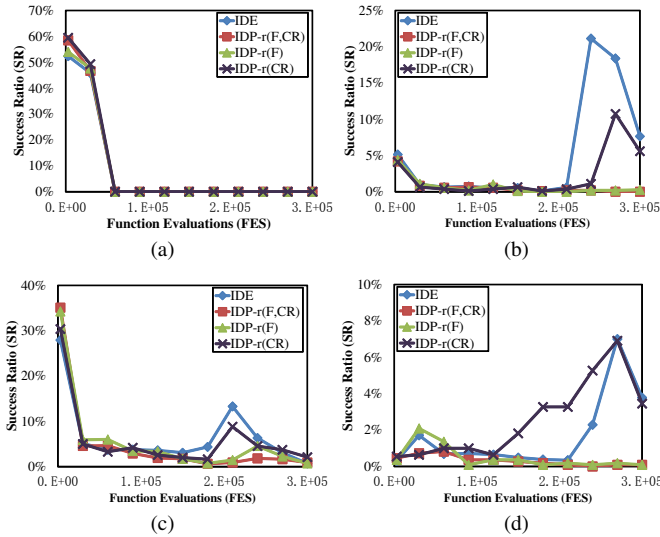
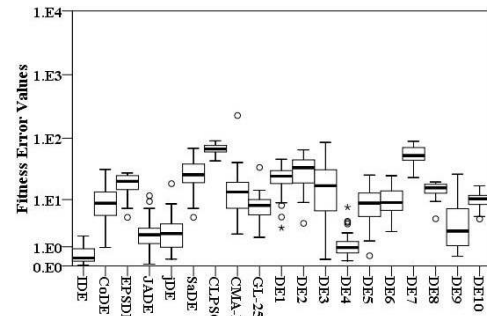


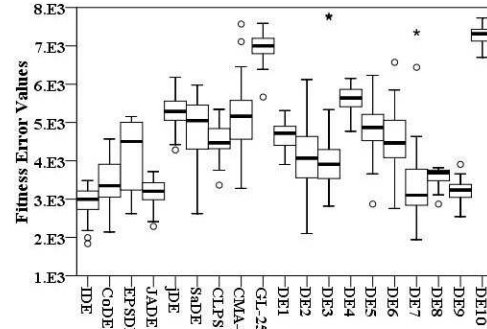
Fig. 10. The success ratio curves of IDE on four 30-D benchmark problems: (a) The Sphere Function, (b) The Rotated Schwefel’s Function, (c) The Rotated Schaffers F7 Function, and (d) The Rotated Expanded Scaffer’s F6 Function.

strategy selects the diversity mutation operators and the rapidity mutation operators for superior individuals and inferior individuals, respectively. Employing the operators with different searching abilities, IDMwo(p) can find better solutions, relative to IDEwoIDM. To further diversify the population, noise elements are introduced in IDM to perturb the difference vectors. Even though IDMwo(p) converges faster than IDE in a few unimodal problems, the latter performs better in multimodal cases. Moreover, the IDE beat all competitor algorithms in the comparison of statistically significant differences.

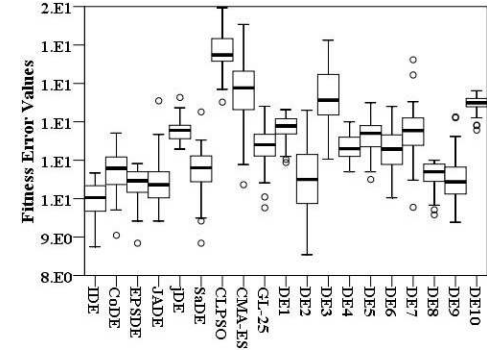
We plot the success ratio curves of IDEs with different parameter settings on four 30-D pilot functions in Fig. 10. Compared to the SR curves of classic DE expressed in Fig. 6, it is clear that, at the earlier stage, a larger SR value speeds up convergence in the unimodal case (a), and at the later stage, an increased SR improves the searching effectiveness in the multimodal cases (b)-(d). More specifically, IDE and IDP-r(CR) achieve increased SR after the transition of mutation operators from the earlier stage to the later stage of the searching process. The generation index threshold vales g_t of IDE on 10-D, 30-D, and 50-D problems are summarized in Table XIII of the supplementary file. We note that the g_t of the functions F1, F5 (except for 50-D), F6 (for 10-D), F21, and F28 (except for 50-D) is smaller than the corresponding G_T . In these functions, the SR values decrease to zero before G_T generations in the cases that finding the global minimum or that falling into the local minima. Because functions F2, F4, F7 - F9, F11 - F20, F22, and F23 have similar g_t values ($\approx G_T + T$) in each dimension group, it can be assumed that in these cases SR values decrease below SR_T before or at generation G_T . For other functions, IDE maintains a relatively good SR from start to generation g_t . Different problems have different g_t values due to different difficulty degrees. Furthermore, to illustrate the distribution of the results of each algorithm, the box plots of fitness error values of all the algorithms on three 30-D multimodal functions in the pilot experiment are depicted in Fig. 11. From the plots,



(a) The 30-D Rotated Schaffers F7 Function



(b) The 30-D Rotated Schwefel’s Function



(c) The 30-D Rotated Expanded Scaffer’s F6 Function

Fig. 11. Comparison results between IDE with other algorithms on three 30-D functions.

we can see that IDE performs more consistently than other algorithms on these problems.

V. CONCLUSION

According to the literature, many researches have focused on tuning the control parameters and designing the mutation strategies of DE to improve the algorithm performance. However, during the iteration process, most of these methods fail to consider the differences of individuals when assigning the control parameters and selecting the mutation operators.

Generally, the better solutions tend to be found in the neighborhoods of the superior individuals and in the searching areas relatively far away from the inferior individuals. In this paper, we proposed the individual-dependent mechanism to improve the performance of DE by setting the parameters and choosing the mutation strategies based on differences in individuals’ fitness values. At each generation, the individuals

in the current population are classified into two categories, i.e., the superior and the inferior, according to their fitness values. Two new IDP setting schemes, namely, the rank-based scheme and the value-based scheme, are employed to calculate the control parameter values for each individual. Then, to generate promising mutant individuals, the proposed IDE employs a new IDM strategy. In IDM, for the purpose of balancing diversity with rapidity, the random individuals and the better individuals are employed to guide the searching directions of the superior individuals and the inferior individuals, respectively. In addition, the current and the random individuals are taken as the origin individuals in the composite base vectors at two different stages of the iteration. To the best of our knowledge, this represents the first attempt to modify DE using the information derived from the differences between the fitness values of individuals.

To evaluate the performance of the proposed algorithm, extensive experiments were carried out on the latest 28 test functions in the CEC 2013 benchmark suite. Considering the No Free Lunch theorem [55], there is no algorithm that can obtain the best performance for all benchmark problems. In comparison with 18 excellent algorithms, IDE achieves both significantly superior and inferior performances, but clearly the superior outweighs the inferior.

As a continuation of this research, we are investigating the discrete version of differential evolution based on the individual-dependent scheme. We are also identifying opportunities to solve practical optimization problems.

The source codes in MATLAB for the competitor algorithms in Subsection IV-B (five state-of-the-art DEs) and IV-D (three other EAs) can be downloaded from the website <http://dces.essex.ac.uk/staff/qzhang/> [27], and the MATLAB codes of the benchmark functions suite and the detailed raw result data of the first nine up-to-date DEs in Subsection IV-C are available on <http://www.ntu.edu.sg/home/epnsugan/> [48]. The supplementary file of this paper can be downloaded from Tang’s homepage: <http://tli.neu.edu.cn/>.

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Supplementary File

Lixin Tang, *Senior Member, IEEE*, Yun Dong, and Jiyin Liu

This document includes the supplemental materials for the paper titled “Differential Evolution with an Individual-Dependent Mechanism.”

APPENDIX

A. Numerical Results

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Lixin Tang is with Liaoning Key Laboratory of Manufacturing System and Logistics, The Logistics Institute, Northeastern University, Shenyang, 110819, China (e-mail: lixintang@mail.neu.edu.cn).

Yun Dong is with State Key Laboratory of Synthetical Automation for Process Industry, The Logistics Institute, Northeastern University, Shenyang, 110819, China (e-mail: dydexter@hotmail.com).

Jiyin Liu is with School of Business and Economics, Loughborough University, Leicestershire LE11 3TU, UK (e-mail: J.Y.Liu@lboro.ac.uk).

TABLE I
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN IDE AND IDE VARIANTS OVER THE 10-DIMENSIONAL CEC 2013 BENCHMARK SET

10-D	IDP-r(F,CR)	IDP-r(F)	IDP-r(CR)	IDEwo(p)	IDEwoIDM	IDE
	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std
F ₁	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00
F ₂	3.05E+01 -	3.80E+03 -	2.68E+01 -	1.54E-06 +	4.46E+05 -	6.55E-06
	8.41E+01	6.64E+03	8.33E+01	4.52E-06	5.08E+05	1.53E-05
F ₃	2.24E+00 =	2.51E+01 -	6.47E-01 =	6.83E-01 =	1.03E+07 -	3.45E-01
	2.88E+00	7.08E+01	1.89E+00	1.90E+00	1.76E+07	1.24E+00
F ₄	1.42E-02 -	1.54E+01 -	6.91E-04 =	1.41E-08 +	3.97E+03 -	5.49E-06
	4.67E-02	2.24E+01	1.72E-03	3.75E-08	2.71E+03	1.29E-05
F ₅	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00 =	1.59E-01 -	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00	5.27E-01	0.00E+00
F ₆	3.57E+00 =	6.31E+00 -	6.24E+00 =	8.92E-01 +	7.68E+00 -	4.04E+00
	4.95E+00	4.86E+00	4.95E+00	2.96E+00	4.15E+00	4.88E+00
F ₇	2.23E-02 -	3.04E-03 =	1.61E-03 -	1.68E-03 =	5.25E+00 -	7.77E-04
	3.25E-02	8.16E-03	1.50E-03	3.30E-03	3.54E+00	9.66E-04
F ₈	2.03E+01 =	2.04E+01 =	2.03E+01 =	2.03E+01 =	2.03E+01 =	2.03E+01
	6.07E-02	7.77E-02	5.86E-02	7.04E-02	6.26E-02	9.40E-02
F ₉	1.48E+00 -	1.16E+00 =	9.87E-01 =	9.32E-01 =	3.33E+00 -	8.66E-01
	1.06E+00	9.51E-01	1.26E+00	9.16E-01	1.00E+00	6.94E-01
F ₁₀	2.90E-02 =	3.07E-02 =	2.80E-02 =	2.28E-02 =	3.28E-01 -	3.00E-02
	2.83E-02	4.66E-02	1.25E-02	1.89E-02	1.66E-01	1.82E-02
F ₁₁	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00 =	1.54E+00 -	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00	1.63E+00	0.00E+00
F ₁₂	4.77E+00 =	3.44E+00 +	4.25E+00 =	4.70E+00 =	1.53E+01 -	4.92E+00
	1.53E+00	1.36E+00	1.27E+00	1.48E+00	6.11E+00	1.62E+00
F ₁₃	6.20E+00 =	4.46E+00 =	4.39E+00 =	6.42E+00 =	2.40E+01 -	5.17E+00
	3.20E+00	2.40E+00	1.90E+00	4.15E+00	6.51E+00	3.01E+00
F ₁₄	2.59E-01 =	1.59E-01 +	5.33E-01 =	4.02E+00 -	4.93E+00 -	3.74E-01
	9.31E-02	9.58E-02	1.02E+00	4.47E+00	5.62E+00	6.61E-01
F ₁₅	6.31E+02 -	3.61E+02 =	5.16E+02 =	3.66E+02 =	6.74E+02 -	4.15E+02
	1.22E+02	1.63E+02	1.99E+02	1.45E+02	2.19E+02	1.47E+02
F ₁₆	8.68E-01 -	7.41E-01 -	9.09E-01 -	5.27E-01 -	5.06E-01 =	5.43E-01
	1.70E-01	2.50E-01	1.92E-01	1.36E-01	3.54E-01	1.41E-01
F ₁₇	1.01E+01 =	1.01E+01 =	1.01E+01 =	1.01E+01 =	1.05E+01 -	1.01E+01
	3.22E-03	6.23E-03	6.72E-03	8.24E-03	3.53E-01	6.13E-03
F ₁₈	2.48E+01 -	1.89E+01 -	1.82E+01 -	1.47E+01 =	1.82E+01 -	1.47E+01
	1.80E+00	3.47E+00	2.91E+00	1.18E+00	3.69E+00	1.51E+00
F ₁₉	4.91E-01 -	3.00E-01 =	3.21E-01 =	3.96E-01 -	4.59E-01 -	2.93E-01
	6.64E-02	8.74E-02	1.01E-01	1.07E-01	1.72E-01	6.36E-02
F ₂₀	2.20E+00 -	1.99E+00 =	1.60E+00 =	1.90E+00 =	2.91E+00 -	1.64E+00
	4.87E-01	5.63E-01	5.24E-01	4.07E-01	6.45E-01	3.62E-01
F ₂₁	4.00E+02 =	4.00E+02 =	4.00E+02 =	4.00E+02 =	4.00E+02 =	3.96E+02
	5.96E-14	5.96E-14	5.96E-14	5.96E-14	6.80E-09	2.80E+01
F ₂₂	2.33E+01 =	6.75E+00 =	1.64E+01 =	3.39E+01 -	6.59E+01 -	9.15E+00
	3.30E+01	5.64E+00	2.91E+01	3.65E+01	6.52E+01	5.82E+00
F ₂₃	8.57E+02 -	3.51E+02 +	3.95E+02 =	4.20E+02 =	9.10E+02 -	4.03E+02
	2.12E+02	1.74E+02	2.66E+02	2.01E+02	2.85E+02	1.87E+02
F ₂₄	2.00E+02 -	2.00E+02 -	1.93E+02 -	2.01E+02 =	2.08E+02 -	1.98E+02
	1.52E-03	1.04E-03	2.66E+01	2.93E+00	5.24E+00	1.34E+01
F ₂₅	2.00E+02 =	2.00E+02 =	2.00E+02 =	2.00E+02 =	2.04E+02 -	2.00E+02
	4.22E-03	3.21E-03	2.77E-04	2.43E-05	3.65E+00	2.02E-05
F ₂₆	1.34E+02 =	1.12E+02 +	1.13E+02 =	1.31E+02 =	1.22E+02 -	1.20E+02
	3.82E+01	2.91E+01	2.89E+01	4.44E+01	2.65E+01	3.48E+01
F ₂₇	3.23E+02 -	3.09E+02 -	3.18E+02 =	3.00E+02 =	3.16E+02 -	3.02E+02
	4.12E+01	3.02E+01	4.05E+01	2.45E-04	2.96E+01	1.40E+01
F ₂₈	3.00E+02 =	3.00E+02 =	2.82E+02 =	3.00E+02 =	2.82E+02 =	2.88E+02
	0.00E+00	0.00E+00	6.03E+01	0.00E+00	6.03E+01	4.75E+01
NoB	6	11	10	12	4	12
-	13	9	6	3	23	
=	15	15	22	22	5	
+	0	4	0	3	0	

TABLE II
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN IDE AND IDE VARIANTS OVER THE 30-DIMENSIONAL CEC 2013 BENCHMARK SET

30-D	IDP-r(F,CR)	IDP-r(F)	IDP-r(CR)	IDEwo(p)	IDEwoIDM	IDE
	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std
F ₁	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.52E-04 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 1.17E-03 = 0.00E+00				
F ₂	2.97E+05 - 6.48E+05 - 1.41E+05 + 2.04E+05 = 2.04E+06 - 2.42E+05	1.76E+05 - 1.80E+05 - 7.54E+04 + 9.51E+04 = 1.13E+06 - 1.40E+05				
F ₃	2.19E+06 - 3.38E+06 - 1.79E+06 - 1.04E+05 - 2.22E+07 - 2.08E+04	2.84E+06 - 3.11E+06 - 1.95E+06 - 3.44E+05 - 2.29E+07 - 1.46E+05				
F ₄	8.28E+01 = 3.11E+02 + 8.06E+01 + 7.92E+02 = 7.81E+03 - 9.75E+02	4.28E+01 = 1.60E+02 + 3.41E+01 + 5.03E+02 = 1.96E+03 - 3.26E+02				
F ₅	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 9.21E-03 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 2.07E-02 = 0.00E+00				
F ₆	2.11E+01 - 2.45E+01 - 9.55E+00 = 4.03E+00 = 4.08E+01 - 5.00E+00	2.44E+01 - 2.58E+01 - 6.75E+00 - 2.95E+00 = 2.20E+01 - 2.82E+00				
F ₇	8.01E+00 - 3.31E+00 - 1.40E+00 - 2.80E-01 = 1.90E+01 - 5.55E-01	1.26E+01 - 4.01E+00 - 1.30E+00 - 2.36E-01 = 1.65E+01 - 5.07E-01				
F ₈	2.09E+01 = 2.10E+01 - 2.10E+01 - 2.09E+01 = 2.09E+01 = 2.09E+01	3.54E-02 = 4.49E-02 - 4.13E-02 - 4.37E-02 = 3.13E-02 = 4.78E-02				
F ₉	2.85E+01 - 1.68E+01 = 2.10E+01 - 1.81E+01 = 1.74E+01 = 1.76E+01	4.68E+00 - 5.87E+00 = 2.94E+00 - 3.66E+00 = 3.16E+00 = 3.39E+00				
F ₁₀	5.98E-02 - 2.05E-01 - 1.11E-01 - 3.90E-02 = 1.78E+00 - 3.42E-02	1.52E-02 - 7.36E-02 - 8.87E-02 - 2.10E-02 = 4.06E+00 - 1.47E-02				
F ₁₁	0.00E+00 = 0.00E+00 = 0.00E+00 = 5.16E+00 - 1.03E+01 - 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 2.84E+00 - 4.13E+00 = 0.00E+00				
F ₁₂	8.40E+01 - 3.51E+01 - 3.42E+01 - 2.98E+01 = 5.22E+01 - 2.73E+01	7.91E+00 - 9.19E+00 - 8.27E+00 - 6.11E+00 = 8.83E+00 - 4.59E+00				
F ₁₃	1.04E+02 - 5.78E+01 = 6.63E+01 - 4.96E+01 = 1.02E+02 - 5.13E+01	1.36E+01 - 8.71E+00 = 1.83E+01 - 1.35E+01 = 2.62E+01 - 1.14E+01				
F ₁₄	5.85E+02 - 6.28E+01 - 4.23E+01 - 1.94E+02 - 1.29E+02 - 2.34E+01	1.41E+02 - 1.53E+01 - 3.79E+01 - 1.25E+02 - 1.26E+02 - 3.18E+01				
F ₁₅	5.66E+03 - 4.19E+03 - 3.16E+03 - 3.12E+03 = 3.68E+03 - 2.93E+03	3.91E+02 - 3.30E+02 - 5.91E+02 = 4.03E+02 = 4.25E+02 - 3.88E+02				
F ₁₆	2.09E+00 - 1.91E+00 - 1.79E+00 - 1.18E+00 = 2.06E+00 - 1.12E+00	2.13E-01 - 2.80E-01 - 3.00E-01 - 2.24E-01 = 3.22E-01 - 1.67E-01				
F ₁₇	4.66E+01 - 3.27E+01 - 3.96E+01 - 3.14E+01 = 3.39E+01 - 3.13E+01	1.28E+00 - 4.22E-01 - 2.55E+00 - 4.65E-01 = 1.88E+00 - 3.80E-01				
F ₁₈	1.59E+02 - 1.11E+02 - 9.32E+01 - 6.71E+01 = 7.27E+01 = 6.48E+01	1.22E+01 - 1.31E+01 - 2.06E+01 - 1.12E+01 = 1.23E+01 = 9.65E+00				
F ₁₉	4.12E+00 - 1.89E+00 - 2.04E+00 - 1.93E+00 - 1.79E+00 - 1.14E+00	3.68E-01 - 3.00E-01 - 9.47E-01 - 2.84E-01 - 5.96E-01 - 1.63E-01				
F ₂₀	1.11E+01 - 1.04E+01 - 9.60E+00 = 9.76E+00 = 1.10E+01 - 9.94E+00	2.81E-01 - 4.34E-01 - 9.93E-01 - 4.67E-01 = 5.61E-01 - 4.97E-01				
F ₂₁	3.26E+02 = 3.43E+02 = 3.43E+02 = 3.65E+02 - 3.41E+02 = 3.17E+02	5.81E+01 = 8.48E+01 = 8.48E+01 = 7.50E+01 - 7.08E+01 = 6.01E+01				
F ₂₂	5.00E+02 - 1.46E+02 - 1.30E+02 - 1.50E+02 = 1.82E+02 - 1.21E+02	7.10E+01 - 9.93E+00 - 8.44E+00 - 2.36E+01 - 9.63E+01 - 4.39E+00				
F ₂₃	5.80E+03 - 4.30E+03 - 3.30E+03 = 3.02E+03 = 3.86E+03 - 3.28E+03	2.23E+02 - 4.00E+02 - 5.09E+02 - 5.39E+02 = 6.86E+02 - 3.80E+02				
F ₂₄	2.06E+02 - 2.06E+02 - 2.06E+02 - 2.00E+02 = 2.28E+02 - 2.00E+02	3.27E+00 - 3.31E+00 - 5.71E+00 - 2.54E-01 = 8.45E+00 - 3.60E-01				
F ₂₅	2.10E+02 - 2.11E+02 - 2.05E+02 - 2.24E+02 = 2.66E+02 - 2.14E+02	1.61E+01 - 1.82E+01 - 1.28E+01 - 2.28E+01 = 8.12E+00 - 2.09E+01				
F ₂₆	2.00E+02 = 2.00E+02 - 2.00E+02 + 2.00E+02 = 2.00E+02 - 2.00E+02	5.30E-03 = 3.54E-03 - 3.12E-03 + 4.56E-03 = 3.59E-02 - 6.39E-03				
F ₂₇	3.59E+02 - 3.61E+02 - 3.57E+02 - 3.05E+02 = 6.37E+02 - 3.06E+02	3.36E+01 - 2.39E+01 - 2.72E+01 - 5.23E+00 = 1.06E+02 - 5.37E+00				
F ₂₈	3.00E+02 = 3.00E+02 = 3.00E+02 = 3.00E+02 = 3.00E+02 = 3.00E+02	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00				
NoB	6	6	9	11	3	18
-	20	20	16	6	23	
=	8	7	9	22	5	
+	0	1	3	0	0	

TABLE IV
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN IDE AND STATE-OF-THE-ART DES OVER THE 10-DIMENSIONAL CEC 2013 BENCHMARK SET

10-D	CoDE	EPSDE	JADE	jDE	SaDE	IDE
	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std
F ₁	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00
F ₂	5.21E+03 -	4.10E-02 =	0.00E+00 +	9.43E+02 -	9.23E+03 -	6.55E-06
	4.31E+03	1.00E-01	0.00E+00	2.81E+03	1.66E+04	1.53E-05
F ₃	1.33E+06 -	4.56E+01 =	7.66E+01 -	1.01E+00 -	1.27E+01 -	3.45E-01
	8.48E+06	9.51E+01	2.74E+02	1.88E+00	4.64E+01	1.24E+00
F ₄	1.51E+01 -	0.00E+00 +	7.66E+01 +	3.06E-02 -	3.81E+01 -	5.49E-06
	4.86E+01	0.00E+00	5.47E+02	6.12E-02	1.28E+02	1.29E-05
F ₅	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00	0.00E+00
F ₆	6.54E+00 -	0.00E+00 +	6.16E+00 -	8.85E+00 -	3.90E+00 -	4.04E+00
	4.55E+00	0.00E+00	4.79E+00	2.95E+00	4.80E+00	4.88E+00
F ₇	2.14E+01 -	5.82E-03 -	2.26E+00 -	2.07E-02 -	3.74E-02 -	7.77E-04
	1.71E+01	5.24E-03	4.58E+00	3.93E-02	7.20E-02	9.66E-04
F ₈	2.04E+01 -	2.03E+01 =	2.03E+01 =	2.03E+01 =	2.03E+01 =	2.03E+01
	1.45E-01	5.14E-02	1.05E-01	7.66E-02	7.61E-02	9.40E-02
F ₉	4.07E+00 -	5.35E+00 -	3.68E+00 -	1.47E+00 -	1.42E+00 -	8.66E-01
	1.47E+00	6.00E-01	1.08E+00	1.10E+00	9.15E-01	6.94E-01
F ₁₀	2.39E-01 -	2.62E-02 =	2.34E-02 +	5.57E-02 -	3.96E-02 =	3.00E-02
	1.83E-01	1.10E-02	2.06E-02	2.69E-02	2.54E-02	1.82E-02
F ₁₁	1.11E+00 -	0.00E+00 =	1.95E-02 =	0.00E+00 =	0.00E+00 =	0.00E+00
	1.32E+00	0.00E+00	1.39E-01	0.00E+00	0.00E+00	0.00E+00
F ₁₂	1.60E+01 -	4.91E+00 =	5.57E+00 -	6.99E+00 -	6.42E+00 -	4.92E+00
	7.76E+00	9.80E-01	2.42E+00	2.58E+00	2.50E+00	1.62E+00
F ₁₃	2.67E+01 -	5.31E+00 =	9.26E+00 -	9.43E+00 -	7.68E+00 -	5.17E+00
	1.28E+01	1.17E+00	5.39E+00	4.10E+00	4.38E+00	3.01E+00
F ₁₄	2.17E+01 -	1.67E-02 +	1.42E-01 +	9.39E-02 +	2.08E-02 +	3.74E-01
	3.77E+01	2.81E-02	7.50E-02	4.77E-01	3.23E-02	6.61E-01
F ₁₅	8.92E+02 -	5.62E+02 -	4.32E+02 =	7.38E+02 -	6.89E+02 -	4.15E+02
	3.01E+02	1.97E+02	1.66E+02	2.48E+02	2.22E+02	1.47E+02
F ₁₆	9.33E-01 =	9.92E-01 -	9.00E-01 -	1.14E+00 -	1.10E+00 -	5.43E-01
	7.17E-01	1.42E-01	3.34E-01	2.04E-01	1.77E-01	1.41E-01
F ₁₇	1.05E+01 -	9.79E+00 +	9.73E+00 +	9.94E+00 +	1.01E+01 +	1.01E+01
	2.11E+00	1.85E+00	1.98E+00	1.29E+00	3.10E-03	6.13E-03
F ₁₈	2.53E+01 -	2.23E+01 -	1.56E+01 -	2.82E+01 -	2.65E+01 -	1.47E+01
	8.75E+00	1.83E+00	2.05E+00	4.26E+00	4.41E+00	1.51E+00
F ₁₉	6.06E-01 -	2.71E-01 =	2.59E-01 +	3.26E-01 -	5.94E-01 -	2.93E-01
	1.63E-01	2.93E-02	4.34E-02	6.45E-02	9.08E-02	6.36E-02
F ₂₀	3.36E+00 -	2.10E+00 -	2.58E+00 -	2.40E+00 -	2.40E+00 -	1.64E+00
	5.13E-01	2.46E-01	4.94E-01	3.22E-01	4.38E-01	3.62E-01
F ₂₁	3.86E+02 =	3.94E+02 =	3.96E+02 =	3.75E+02 =	4.00E+02 =	3.96E+02
	5.67E+01	3.66E+01	2.80E+01	7.17E+01	0.00E+00	2.80E+01
F ₂₂	1.32E+02 -	1.10E+01 =	2.90E+01 =	1.40E+01 =	2.65E+01 =	9.15E+00
	9.70E+01	4.42E+00	4.53E+01	2.35E+01	2.63E+01	5.82E+00
F ₂₃	1.04E+03 -	1.03E+03 -	5.94E+02 -	7.67E+02 -	6.74E+02 -	4.03E+02
	3.13E+02	1.43E+02	2.03E+02	2.59E+02	3.19E+02	1.87E+02
F ₂₄	2.11E+02 -	2.17E+02 -	2.02E+02 -	1.98E+02 -	1.94E+02 -	1.98E+02
	4.74E+00	1.40E+00	1.08E+01	2.30E+01	2.17E+01	1.34E+01
F ₂₅	2.06E+02 -	2.18E+02 -	2.06E+02 -	2.03E+02 -	1.99E+02 -	2.00E+02
	1.80E+01	2.01E+00	5.61E+00	2.96E+00	1.12E+01	2.02E-05
F ₂₆	1.60E+02 -	1.94E+02 -	1.56E+02 -	1.37E+02 -	1.11E+02 -	1.20E+02
	5.61E+01	1.87E+01	6.72E+01	4.30E+01	1.93E+01	3.48E+01
F ₂₇	4.17E+02 -	4.67E+02 -	3.47E+02 -	3.26E+02 -	3.04E+02 -	3.02E+02
	8.81E+01	2.01E+01	8.24E+01	6.16E+01	1.96E+01	1.40E+01
F ₂₈	3.16E+02 =	2.93E+02 =	3.06E+02 =	2.88E+02 =	2.92E+02 =	2.88E+02
	9.41E+01	3.65E+01	5.79E+01	4.75E+01	3.92E+01	4.75E+01
NoB	2	8	7	6	7	16
-	23	11	14	19	18	
=	5	13	8	7	8	
+	0	4	6	2	2	

TABLE V
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN IDE AND STATE-OF-THE-ART DES OVER THE 30-DIMENSIONAL CEC 2013 BENCHMARK SET

30-D	CoDE	EPSDE	JADE	jDE	SaDE	IDE
	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std
F ₁	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00
F ₂	7.44E+04 + 3.97E+04	2.19E+04 + 1.03E+04	6.39E+03 + 4.58E+03	1.41E+05 + 8.27E+04	3.65E+05 + 2.07E+05	2.42E+05 - 1.40E+05
F ₃	2.56E+06 - 5.79E+06	4.51E+03 - 8.22E+03	2.10E+05 - 1.22E+06	1.68E+06 - 2.55E+06	1.25E+07 - 1.96E+07	2.08E+04 - 1.46E+05
F ₄	1.89E-01 + 5.57E-01	4.52E-01 + 1.04E+00	7.61E+03 - 1.54E+04	1.73E+01 + 1.63E+01	3.01E+03 - 1.42E+03	9.75E+02 - 3.26E+02
F ₅	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00
F ₆	2.43E+00 + 7.07E+00	8.91E+00 - 7.91E-01	2.59E+00 + 7.93E+00	1.36E+01 - 4.82E+00	2.91E+01 - 2.82E+01	5.00E+00 - 2.82E+00
F ₇	1.02E+01 - 6.60E+00	2.00E+01 - 6.14E+00	2.53E+00 - 2.21E+00	3.05E+00 - 3.08E+00	2.99E+01 - 1.46E+01	5.55E-01 - 5.07E-01
F ₈	2.08E+01 + 1.91E-01	2.09E+01 + 3.76E-02	2.09E+01 = 9.60E-02	2.09E+01 = 5.50E-02	2.09E+01 = 5.84E-02	2.09E+01 = 4.78E-02
F ₉	1.42E+01 + 2.81E+00	3.14E+01 - 1.81E+00	2.66E+01 - 1.62E+00	2.42E+01 - 6.33E+00	1.82E+01 - 2.65E+00	1.76E+01 = 3.39E+00
F ₁₀	3.16E-02 - 1.70E-02	5.12E-02 - 2.50E-02	3.61E-02 = 2.51E-02	4.18E-02 = 2.17E-02	3.02E-01 = 1.35E-01	3.42E-02 - 1.47E-02
F ₁₁	1.95E-02 - 1.39E-01	0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00	1.37E-01 - 3.46E-01	0.00E+00 - 0.00E+00
F ₁₂	3.68E+01 - 9.50E+00	4.20E+01 - 4.84E+00	2.42E+01 + 4.39E+00	6.04E+01 - 9.26E+00	4.81E+01 - 1.27E+01	2.73E+01 - 4.59E+00
F ₁₃	7.59E+01 - 2.70E+01	6.56E+01 - 1.03E+01	4.50E+01 + 1.40E+01	9.42E+01 - 1.53E+01	1.02E+02 - 2.25E+01	5.13E+01 - 1.14E+01
F ₁₄	3.51E+02 = 5.71E+02	1.89E-01 + 8.46E-02	2.69E-02 + 2.40E-02	1.22E-03 + 4.95E-03	9.04E-01 + 9.87E-01	2.34E+01 + 3.18E+01
F ₁₅	3.44E+03 - 5.98E+02	4.18E+03 - 9.02E+02	3.18E+03 - 3.21E+02	5.29E+03 - 4.21E+02	4.74E+03 - 9.72E+02	2.93E+03 - 3.88E+02
F ₁₆	3.96E-01 + 2.79E-01	2.27E+00 - 2.44E-01	1.97E+00 - 6.50E-01	2.39E+00 - 3.01E-01	2.21E+00 - 2.90E-01	1.12E+00 - 1.67E-01
F ₁₇	3.07E+01 + 1.86E+00	3.04E+01 + 2.88E-14	3.04E+01 + 8.04E-15	3.04E+01 + 7.95E-12	3.05E+01 + 3.33E-02	3.13E+01 + 3.80E-01
F ₁₈	6.37E+01 - 1.21E+01	1.29E+02 - 7.28E+00	7.67E+01 - 6.32E+00	1.63E+02 - 1.32E+01	1.26E+02 - 4.92E+01	6.48E+01 - 9.65E+00
F ₁₉	1.59E+00 - 4.21E-01	1.74E+00 - 1.31E-01	1.43E+00 - 1.14E-01	1.63E+00 - 1.82E-01	4.10E+00 - 1.01E+00	1.14E+00 - 1.63E-01
F ₂₀	1.07E+01 - 5.10E-01	1.03E+01 - 5.08E-01	1.04E+01 - 5.66E-01	1.18E+01 - 2.72E-01	1.07E+01 - 6.17E-01	9.94E+00 - 4.97E-01
F ₂₁	2.95E+02 + 8.66E+01	2.63E+02 + 4.90E+01	2.99E+02 = 6.54E+01	2.73E+02 + 7.42E+01	3.26E+02 + 8.06E+01	3.17E+02 = 6.01E+01
F ₂₂	2.24E+02 - 2.80E+02	2.02E+02 - 6.21E+01	9.44E+01 + 2.80E+01	1.22E+02 + 2.72E+01	1.14E+02 + 1.42E+01	1.21E+02 + 4.39E+00
F ₂₃	3.69E+03 - 5.91E+02	6.15E+03 - 4.81E+02	3.38E+03 = 3.19E+02	5.28E+03 = 5.11E+02	5.03E+03 - 9.93E+02	3.28E+03 - 3.80E+02
F ₂₄	2.21E+02 - 8.40E+00	2.89E+02 - 3.58E+00	2.12E+02 - 1.10E+01	2.15E+02 - 9.95E+00	2.26E+02 - 7.25E+00	2.00E+02 - 3.60E-01
F ₂₅	2.55E+02 - 6.56E+00	2.96E+02 - 2.25E+00	2.72E+02 - 1.43E+01	2.51E+02 - 1.09E+01	2.66E+02 - 1.23E+01	2.14E+02 - 2.09E+01
F ₂₆	2.00E+02 = 3.43E-03	3.40E+02 = 7.25E+01	2.22E+02 = 5.26E+01	2.08E+02 = 3.41E+01	2.00E+02 = 8.77E-03	2.00E+02 = 6.39E-03
F ₂₇	6.08E+02 - 9.71E+01	1.19E+03 - 4.33E+01	7.10E+02 - 2.54E+02	6.53E+02 - 2.16E+02	6.18E+02 - 7.16E+01	3.06E+02 - 5.37E+00
F ₂₈	3.00E+02 = 1.07E-13	3.00E+02 = 0.00E+00	3.00E+02 = 0.00E+00	3.00E+02 = 6.43E-14	3.00E+02 = 0.00E+00	3.00E+02 = 0.00E+00
NoB	11	7	9	6	4	13
-	11	18	12	16	19	
=	9	5	9	7	6	
+	8	5	7	5	3	

TABLE VI
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN IDE AND STATE-OF-THE-ART DES OVER THE 50-DIMENSIONAL CEC 2013 BENCHMARK SET

50-D	CoDE	EPSDE	JADE	jDE	SaDE	IDE
	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std
F ₁	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00
F ₂	5.31E+05 + 1.84E+05	1.51E+05 + 6.66E+04	3.59E+04 + 2.09E+04	8.63E+05 + 2.59E+05	8.20E+05 + 2.59E+05	1.68E+06 + 4.23E+05
F ₃	1.34E+07 - 2.96E+07	2.31E+06 - 2.28E+06	1.40E+05 + 3.48E+05	2.81E+06 - 3.75E+06	7.36E+07 - 6.08E+07	1.38E+05 - 1.85E+05
F ₄	5.80E-01 + 5.70E-01	6.12E+02 + 4.09E+02	1.48E+04 + 2.88E+04	1.67E+04 - 9.17E+03	4.60E+03 - 1.42E+03	6.85E+03 + 1.10E+03
F ₅	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00
F ₆	4.34E+01 + 3.61E-11	3.46E+01 + 3.84E+00	4.34E+01 + 6.82E-14	4.52E+01 + 9.51E-01	5.81E+01 - 2.27E+01	4.34E+01 - 2.62E-04
F ₇	1.50E+01 - 5.94E+00	4.23E+01 - 5.54E+00	6.08E+00 - 2.47E+00	8.77E+00 - 4.16E+00	4.89E+01 - 9.77E+00	3.18E+00 - 1.55E+00
F ₈	2.16E+01 - 7.35E-02	2.11E+01 - 3.03E-02	2.11E+01 - 3.73E-02	2.11E+01 - 3.36E-02	2.11E+01 - 3.29E-02	2.11E+01 - 2.44E-02
F ₉	2.44E+01 + 4.88E+00	6.69E+01 - 2.92E+00	5.40E+01 - 1.88E+00	5.72E+01 - 2.67E+00	3.94E+01 - 4.54E+00	3.56E+01 - 5.54E+00
F ₁₀	2.96E-02 + 1.74E-02	7.75E-02 - 3.07E-02	3.83E-02 = 3.00E-02	3.30E-02 + 2.10E-02	3.09E-01 - 1.71E-01	4.38E-02 - 2.17E-02
F ₁₁	3.72E+01 - 2.13E+01	0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00	2.24E+00 - 2.43E+00	0.00E+00 - 0.00E+00
F ₁₂	6.62E+01 - 1.74E+01	1.52E+02 - 1.98E+01	7.81E+01 - 9.06E+00	1.63E+02 - 1.75E+01	1.24E+02 - 2.19E+01	6.89E+01 - 8.82E+00
F ₁₃	1.51E+02 - 3.35E+01	2.14E+02 - 1.63E+01	1.29E+02 = 2.26E+01	2.43E+02 - 2.09E+01	2.45E+02 - 4.35E+01	1.34E+02 - 2.28E+01
F ₁₄	4.47E+03 - 2.75E+03	2.41E+02 = 3.01E+02	2.85E+01 + 3.05E+00	1.01E+02 = 1.75E+01	9.54E+00 + 1.75E+01	1.17E+02 + 8.38E+01
F ₁₅	6.57E+03 - 8.19E+02	7.61E+03 - 1.49E+03	8.88E+03 - 4.00E+02	1.11E+04 - 6.14E+02	9.04E+03 - 2.09E+03	6.54E+03 - 5.91E+02
F ₁₆	1.12E+01 - 2.49E+00	3.14E+00 - 3.41E-01	2.80E+00 - 7.45E-01	3.28E+00 - 2.82E-01	2.99E+00 - 3.07E-01	1.59E+00 - 2.36E-01
F ₁₇	1.50E+02 - 4.55E+01	5.08E+01 + 0.00E+00	5.09E+01 + 2.01E-02	5.52E+01 + 7.77E-01	5.12E+01 + 3.82E-01	5.92E+01 + 1.41E+00
F ₁₈	1.49E+02 + 1.28E+02	3.24E+02 - 1.60E+01	2.02E+02 - 1.18E+01	3.37E+02 - 2.30E+01	1.73E+02 - 8.45E+01	1.68E+02 + 1.27E+01
F ₁₉	4.23E+01 - 2.26E+01	5.70E+00 - 3.47E-01	4.07E+00 - 1.72E-01	4.26E+00 - 2.58E-01	1.03E+01 - 2.68E+00	2.24E+00 - 3.66E-01
F ₂₀	2.38E+01 - 1.85E+00	1.96E+01 - 9.21E-01	1.98E+01 - 5.09E-01	2.19E+01 - 3.38E-01	2.02E+01 - 9.94E-01	1.93E+01 - 4.47E-01
F ₂₁	4.84E+02 + 4.26E+02	4.95E+02 + 3.50E+02	8.97E+02 + 3.62E+02	3.27E+02 + 3.20E+02	9.18E+02 - 2.96E+02	7.32E+02 - 3.82E+02
F ₂₂	5.08E+03 - 2.56E+03	1.40E+03 - 4.88E+02	8.09E+01 - 5.80E+01	2.08E+02 - 7.72E+01	2.21E+01 + 4.87E+00	6.88E+01 + 2.03E+01
F ₂₃	7.13E+03 - 1.26E+03	1.37E+04 - 4.87E+02	8.96E+03 - 5.56E+02	1.09E+04 - 5.63E+02	8.75E+03 - 2.15E+03	7.32E+03 - 6.92E+02
F ₂₄	2.38E+02 - 9.47E+00	3.79E+02 - 3.75E+00	2.21E+02 - 8.20E+00	2.51E+02 - 2.50E+01	2.78E+02 - 9.38E+00	2.02E+02 - 1.14E+00
F ₂₅	2.97E+02 + 1.15E+01	3.81E+02 - 3.38E+00	3.61E+02 - 1.69E+01	3.27E+02 - 2.74E+01	3.44E+02 - 1.13E+01	3.03E+02 - 1.09E+01
F ₂₆	2.41E+02 - 6.73E+01	4.70E+02 - 5.32E+00	2.67E+02 - 9.48E+01	2.43E+02 - 8.92E+01	2.61E+02 - 8.73E+01	2.23E+02 - 4.46E+01
F ₂₇	9.34E+02 - 9.94E+01	2.10E+03 - 2.41E+01	1.22E+03 - 3.74E+02	1.43E+03 - 2.42E+02	1.17E+03 - 9.89E+01	3.58E+02 - 3.30E+01
F ₂₈	4.00E+02 = 0.00E+00	4.00E+02 = 0.00E+00	4.00E+02 = 0.00E+00	4.00E+02 = 0.00E+00	5.35E+02 = 6.75E+02	4.00E+02 = 0.00E+00
NoB	10	7	7	6	5	14
-	14	17	14	19	18	
=	6	6	8	5	4	
+	8	5	6	4	6	

TABLE VII
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN IDE AND UP-TO-DATE DES OVER THE 10-DIMENSIONAL CEC 2013 BENCHMARK SET

10-D	DE1	DE2	DE3	DE4	DE5	DE6	DE7	DE8	DE9	DE10	IDE
	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std
F ₁	0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00
F ₂	1.82E-04 1.26E-03	+ 0.00E+00 0.00E+00	+ 0.00E+00 0.00E+00	+ 1.90E-02 1.34E-01	+ 1.72E+03 1.69E+03	- 6.89E+02 1.01E+03	- 1.01E+02 6.09E+02	- 0.00E+00 0.00E+00	+ 0.00E+00 0.00E+00	+ 5.60E+05 3.05E+05	- 6.55E-06 1.53E-05
F ₃	3.94E-01 1.48E+00	= 2.48E-01 1.23E+00	+ 0.00E+00 0.00E+00	+ 2.17E-01 9.02E-01	= 1.61E+00 2.96E+00	= 5.97E+00 1.74E+01	- 1.14E+00 2.00E+00	- 9.58E-01 5.73E-01	- 1.27E-01 8.75E-01	+ 1.66E+01 2.86E+01	- 3.45E-01 1.24E+00
F ₄	0.00E+00 1.06E-08	+ 0.00E+00 0.00E+00	+ 0.00E+00 0.00E+00	+ 1.26E+03 2.78E+03	- 1.24E-01 3.76E-01	- 3.88E-02 7.80E-02	- 8.19E-01 4.57E+00	- 0.00E+00 0.00E+00	+ 0.00E+00 0.00E+00	+ 5.28E+03 1.78E+03	- 5.49E-06 1.29E-05
F ₅	0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00
F ₆	4.23E+00 4.86E+00	= 5.41E+00 4.76E+00	= 0.00E+00 0.00E+00	+ 3.27E+00 4.63E+00	+ 8.50E+00 3.30E+00	= 8.66E+00 3.16E+00	+ 1.35E+00 3.38E+00	+ 0.00E+00 0.00E+00	+ 7.89E+00 3.90E+00	- 7.84E+00 3.80E+00	- 4.04E+00 4.88E+00
F ₇	2.96E-03 6.35E-03	- 2.27E+00 4.45E+00	- 4.62E-04 2.85E-03	+ 2.67E-02 1.49E-01	+ 9.48E-01 3.25E+00	- 1.87E-01 2.71E-01	- 8.71E-01 8.21E-01	- 4.54E-01 1.55E-01	- 3.26E-03 4.50E-03	- 1.07E-03 1.06E-03	- 7.77E-04 9.66E-04
F ₈	2.04E+01 7.82E-02	- 2.03E+01 1.03E-01	= 2.04E+01 7.94E-02	- 2.04E+01 8.97E-02	= 2.03E+01 7.55E-02	= 2.03E+01 8.16E-02	= 2.03E+01 1.12E-01	+ 2.02E+01 4.03E-02	+ 2.04E+01 8.86E-02	= 2.03E+01 5.66E-02	= 2.03E+01 9.40E-02
F ₉	1.78E+00 1.85E+00	= 2.29E+00 7.19E-01	- 5.16E+00 3.68E+00	- 1.90E+00 2.02E+00	= 2.75E+00 1.38E+00	- 2.73E+00 1.11E+00	- 3.54E+00 1.09E+00	- 4.28E+00 3.31E-01	- 3.39E+00 7.28E-01	- 5.66E+00 1.97E+00	- 8.66E-01 6.94E-01
F ₁₀	3.51E-02 2.51E-02	= 1.42E-02 9.58E-03	+ 4.39E-02 2.70E-02	- 5.70E-02 3.29E-02	- 7.10E-02 3.48E-02	- 1.03E-01 6.23E-02	- 3.29E-02 1.71E-02	= 4.88E-03 3.70E-03	+ 1.20E-02 8.90E-03	- 4.70E-01 8.03E-02	- 3.00E-02 1.82E-02
F ₁₁	0.00E+00 0.00E+00	= 9.75E-02 2.96E-01	- 0.00E+00 0.00E+00	= 4.98E+00 3.04E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 1.95E-02 1.38E-01	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00	= 0.00E+00 0.00E+00
F ₁₂	8.07E+00 2.23E+00	- 7.80E+00 4.10E+00	- 6.42E+00 3.11E+00	- 7.69E+00 3.59E+00	- 6.11E+00 3.23E+00	= 7.58E+00 2.78E+00	- 6.15E+00 1.88E+00	- 5.44E+00 6.46E-01	- 3.14E+00 9.64E-01	+ 2.43E+01 3.46E+00	- 4.92E+00 1.62E+00
F ₁₃	9.57E+00 3.38E+00	- 1.21E+01 6.40E+00	- 1.05E+01 6.47E+00	- 9.52E+00 5.15E+00	- 7.81E+00 4.78E+00	- 1.10E+01 5.39E+00	- 1.19E+01 4.39E+00	- 5.67E+00 1.78E+00	= 3.77E+00 1.83E+00	= 2.19E+01 4.14E+00	- 5.17E+00 3.01E+00
F ₁₄	7.10E-02 6.31E-02	+ 3.64E+00 4.39E+00	- 5.59E+01 2.34E+01	- 1.51E+02 8.04E+01	- 5.02E-02 5.67E-02	+ 8.33E-02 7.18E-02	+ 1.84E-02 3.10E-02	+ 1.61E+00 6.24E-01	- 4.90E-03 1.68E-02	+ 3.86E+01 2.91E+01	- 3.74E-01 6.61E-01
F ₁₅	6.99E+02 1.70E+02	- 7.36E+02 2.60E+02	- 8.20E+02 3.60E+02	- 8.71E+02 1.31E+02	- 8.40E+02 2.31E+02	- 8.31E+02 3.07E+02	- 5.27E+02 1.38E+02	- 5.61E+02 6.10E+01	- 4.21E+02 1.13E+02	= 1.33E+03 1.72E+02	- 4.15E+02 1.47E+02
F ₁₆	9.48E-01 2.46E-01	- 4.04E-01 3.14E-01	+ 9.49E-01 1.93E-01	- 9.09E-01 1.85E-01	- 1.10E+00 2.32E-01	- 1.19E+00 2.31E-01	+ 2.79E-01 1.99E-01	+ 7.75E-01 8.84E-02	- 7.08E-01 2.10E-01	- 1.15E+00 1.87E-01	- 5.43E-01 1.41E-01
F ₁₇	1.01E+01 1.24E-14	+ 1.03E+01 1.55E-01	- 1.01E+01 2.18E-02	+ 1.59E+01 2.89E+00	- 9.92E+00 1.40E+00	+ 1.01E+01 8.63E-03	+ 9.80E+00 1.51E+00	= 1.05E+01 9.50E-02	+ 1.01E+01 0.00E+00	+ 1.01E+01 1.46E-02	+ 1.01E+01 6.13E-03
F ₁₈	2.49E+01 4.70E+00	- 2.46E+01 4.68E+00	- 2.05E+01 7.70E+00	- 2.76E+01 3.05E+00	- 2.77E+01 5.38E+00	- 2.29E+01 6.45E+00	- 1.65E+01 2.66E+00	- 1.90E+01 1.08E+00	- 1.69E+01 1.52E+00	- 3.43E+01 3.89E+00	- 1.47E+01 1.51E+00
F ₁₉	3.38E-01 4.09E-02	- 3.95E-01 1.25E-01	- 7.87E-01 2.55E-01	- 6.42E-01 1.51E-01	- 3.20E-01 1.04E-01	- 3.19E-01 7.38E-02	= 2.90E-01 6.21E-02	- 4.82E-01 4.72E-02	- 3.44E-01 4.85E-02	- 1.16E+00 1.99E-01	- 2.93E-01 6.36E-02
F ₂₀	2.31E+00 2.95E-01	- 2.65E+00 4.48E-01	- 2.56E+00 4.70E-01	- 2.35E+00 4.09E-01	- 2.72E+00 4.84E-01	- 2.51E+00 3.79E-01	- 2.56E+00 4.01E-01	- 2.59E+00 2.05E-01	- 2.16E+00 3.48E-01	- 2.73E+00 2.26E-01	- 1.64E+00 3.62E-01
F ₂₁	3.83E+02 6.17E+01	- 3.83E+02 5.50E+01	+ 2.96E+02 2.77E+01	+ 3.69E+02 7.28E+01	+ 3.51E+02 8.95E+01	+ 3.92E+02 3.89E+01	- 4.00E+02 4.55E-13	= 1.65E+02 5.48E+01	+ 4.00E+02 0.00E+00	= 3.92E+02 3.92E+01	= 3.96E+02 2.80E+01
F ₂₂	1.98E+01 2.51E+01	- 4.93E+01 5.33E+01	- 3.45E+02 1.35E+02	- 2.62E+02 1.16E+02	- 9.19E+01 2.93E+01	- 6.62E+01 4.21E+01	- 3.08E+01 1.89E+01	- 1.01E+02 1.65E+01	- 4.84E+00 6.14E+00	+ 3.15E+02 1.47E+02	- 9.15E+00 5.82E+00
F ₂₃	7.05E+02 2.00E+02	- 5.78E+02 3.16E+02	- 1.01E+03 4.39E+02	- 9.04E+02 2.16E+02	- 8.11E+02 2.20E+02	- 9.47E+02 2.73E+02	- 6.56E+02 1.59E+02	- 7.95E+02 1.19E+02	- 4.61E+02 1.77E+02	= 1.37E+03 1.82E+02	- 4.03E+02 1.87E+02
F ₂₄	2.04E+02 3.48E+00	- 2.02E+02 1.76E+01	- 2.18E+02 7.32E+00	- 2.05E+02 1.36E+01	- 2.09E+02 1.37E+01	- 2.04E+02 1.96E+01	- 1.13E+02 2.19E+01	+ 1.75E+02 2.01E+01	+ 1.93E+02 2.44E+01	- 1.98E+02 9.83E+00	- 1.98E+02 1.34E+01
F ₂₅	2.00E+02 1.30E+01	- 2.02E+02 1.91E+00	- 2.19E+02 6.91E+00	- 2.04E+02 3.73E+00	- 2.10E+02 4.28E+00	- 2.05E+02 1.61E+01	- 1.82E+02 3.70E+01	- 2.09E+02 1.46E+01	- 2.00E+02 6.96E-01	- 2.00E+02 1.42E-04	- 2.00E+02 2.02E-05
F ₂₆	1.55E+02 4.60E+01	- 1.26E+02 3.69E+01	- 2.00E+02 0.00E+00	- 1.84E+02 3.50E+01	- 1.93E+02 4.33E+01	- 1.69E+02 3.80E+01	- 1.10E+02 1.31E+01	- 1.09E+02 2.30E+00	- 1.33E+02 4.32E+01	= 1.33E+02 1.88E+01	- 1.20E+02 3.48E+01
F ₂₇	3.25E+02 6.19E+01	= 3.37E+02 5.23E+01	- 4.95E+02 6.58E+01	- 3.77E+02 9.29E+01	- 4.94E+02 5.20E+01	- 4.73E+02 4.65E+01	- 3.90E+02 2.97E+01	- 4.06E+02 5.57E+00	- 3.00E+02 1.45E-08	= 3.00E+02 0.00E+00	= 3.02E+02 1.40E+01
F ₂₈	2.92E+02 3.88E+01	= 3.17E+02 6.87E+01	- 2.92E+02 3.88E+01	= 2.88E+02 4.71E+01	= 2.88E+02 4.71E+01	= 2.84E+02 5.38E+01	= 2.41E+02 9.11E+01	+ 9.61E+01 1.94E+01	+ 3.00E+02 0.00E+00	= 3.00E+02 0.00E+00	= 2.88E+02 4.75E+01
NoB	4	4	8	2	3	3	8	10	10	4	9
-	15	19	17	18	17	19	15	16	9	20	
=	9	4	4	6	8	7	7	4	11	7	
+	4	5	7	4	3	2	6	8	8	1	

TABLE VIII
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN IDE AND UP-TO-DATE DES OVER THE 30-DIMENSIONAL CEC 2013 BENCHMARK SET

30-D	DE1	DE2	DE3	DE4	DE5	DE6	DE7	DE8	DE9	DE10	IDE	
	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	
F ₁	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00
F ₂	7.00E+04 + 4.37E+04	0.00E+00 + 0.00E+00	1.75E+05 + 1.32E+05	2.12E+06 + 1.54E+06	1.29E+05 + 9.59E+04	1.02E+05 + 5.25E+04	1.99E+05 + 1.07E+05	6.73E+03 + 2.52E+03	9.00E+03 + 7.40E+03	8.48E+07 + 1.37E+07	2.42E+05 + 1.40E+05	
F ₃	4.36E+03 + 1.35E+04	9.82E+03 + 4.94E+04	3.21E+06 + 1.18E+07	1.65E+03 + 2.80E+03	9.84E+06 + 1.84E+07	1.10E+07 + 1.38E+07	2.11E+06 + 4.64E+06	3.91E+01 + 6.82E+01	4.02E+01 + 2.11E+02	5.29E+02 + 1.47E+03	2.08E+04 + 1.46E+05	
F ₄	1.81E-02 + 2.85E-02	0.00E+00 + 0.00E+00	2.20E-01 + 5.97E-01	1.70E+04 + 2.82E+03	1.97E+04 + 1.25E+04	2.41E+00 + 3.26E+00	3.82E+02 + 5.12E+02	2.34E+00 + 1.97E+00	1.92E-04 + 2.98E-04	4.19E+04 + 5.12E+03	9.75E+02 + 3.26E+02	
F ₅	0.00E+00 + 0.00E+00	0.00E+00 + 0.00E+00	0.00E+00 + 0.00E+00	1.40E-07 + 1.84E-07	1.50E-08 + 1.15E-08	0.00E+00 + 0.00E+00	0.00E+00 + 0.00E+00	0.00E+00 + 0.00E+00	0.00E+00 + 0.00E+00	0.00E+00 + 0.00E+00	0.00E+00 + 0.00E+00	
F ₆	5.25E+00 + 9.80E+00	2.67E+00 + 7.85E+00	9.35E+00 + 2.04E+00	8.29E+00 + 5.76E+00	7.93E+00 + 7.51E+00	1.75E+01 + 1.13E+01	7.08E+00 + 4.17E+00	1.04E-02 + 2.12E-02	5.96E-01 + 3.69E+00	1.52E+01 + 2.65E-01	5.00E+00 + 2.82E+00	
F ₇	2.44E+01 + 8.87E+00	3.25E+01 + 1.61E+01	2.18E+01 + 1.87E+01	1.29E+00 + 1.20E+00	9.82E+00 + 6.44E+00	1.10E+01 + 6.12E+00	5.68E+01 + 1.66E+01	2.34E+00 + 3.32E+00	4.60E+00 + 5.33E+00	1.03E+01 + 2.92E+00	5.55E-01 + 5.07E-01	
F ₈	2.09E+01 + 4.68E-02	2.10E+01 + 4.80E-02	2.09E+01 + 5.19E-02	2.09E+01 + 4.77E-02	2.09E+01 + 4.47E-02	2.10E+01 + 5.04E-02	2.09E+01 + 9.44E-02	2.08E+01 + 5.09E-02	2.07E+01 + 1.74E-01	2.09E+01 + 6.86E-02	2.09E+01 + 4.78E-02	
F ₉	2.86E+01 + 1.14E+00	2.23E+01 + 3.57E+00	3.07E+01 + 9.32E+00	6.30E+00 + 3.24E+00	2.10E+01 + 7.11E+00	2.50E+01 + 3.50E+00	2.40E+01 + 2.86E+00	2.69E+01 + 3.88E+00	2.75E+01 + 1.75E+00	3.96E+01 + 1.06E+00	1.76E+01 + 3.39E+00	
F ₁₀	1.91E-02 + 1.32E-02	1.84E-02 + 1.34E-02	6.42E-02 + 4.77E-02	2.16E-02 + 1.34E-02	7.91E-02 + 4.31E-02	5.40E-02 + 3.98E-02	2.01E-02 + 1.73E-02	1.62E-02 + 6.86E-03	7.69E-02 + 3.54E-02	1.36E+00 + 2.51E-01	3.42E-02 + 1.47E-02	
F ₁₁	0.00E+00 + 0.00E+00	1.09E+01 + 4.18E+00	3.08E+00 + 4.45E+00	5.84E+01 + 1.10E+01	0.00E+00 + 0.00E+00	0.00E+00 + 0.00E+00	5.85E-02 + 2.34E-01	0.00E+00 + 0.00E+00	0.00E+00 + 0.00E+00	1.03E+02 + 7.28E+00	0.00E+00 + 0.00E+00	
F ₁₂	8.36E+01 + 1.28E+01	5.72E+01 + 1.70E+01	3.17E+01 + 8.43E+00	1.15E+02 + 1.13E+01	4.28E+01 + 1.56E+01	4.26E+01 + 1.35E+01	5.42E+01 + 8.80E+00	4.99E+01 + 3.45E+00	2.30E+01 + 3.70E+00	1.88E+02 + 1.11E+01	2.73E+01 + 4.59E+00	
F ₁₃	1.14E+02 + 1.38E+01	1.28E+02 + 3.50E+01	7.55E+01 + 2.63E+01	1.31E+02 + 1.23E+01	7.08E+01 + 2.36E+01	7.98E+01 + 2.07E+01	1.01E+02 + 1.86E+01	8.58E+01 + 8.57E+00	5.03E+01 + 1.32E+01	1.92E+02 + 8.91E+00	5.13E+01 + 1.14E+01	
F ₁₄	2.37E-02 + 2.47E-02	1.33E+02 + 1.27E+02	3.84E+03 + 3.81E+02	3.20E+03 + 4.34E+02	1.33E+00 + 1.34E+00	3.26E+00 + 6.07E+00	3.29E+01 + 1.35E+01	3.07E+01 + 1.13E+01	3.18E-02 + 2.31E-02	4.56E+03 + 2.29E+02	2.34E+01 + 3.18E+01	
F ₁₅	4.66E+03 + 3.36E+02	4.10E+03 + 8.47E+02	4.14E+03 + 1.07E+03	5.61E+03 + 3.15E+02	4.83E+03 + 5.92E+02	4.51E+03 + 7.30E+02	3.43E+03 + 1.08E+03	3.61E+03 + 2.05E+02	3.22E+03 + 2.61E+02	7.27E+03 + 2.63E+02	2.93E+03 + 3.88E+02	
F ₁₆	1.98E+00 + 3.82E-01	1.31E-01 + 7.57E-02	2.46E+00 + 4.41E-01	2.39E+00 + 2.63E-01	2.28E+00 + 3.65E-01	2.33E+00 + 3.59E-01	7.27E-01 + 8.93E-01	1.48E+00 + 2.06E-01	9.13E-01 + 1.84E-01	2.48E+00 + 3.13E-01	1.12E+02 + 1.67E-01	
F ₁₇	3.04E+01 + 4.11E-05	3.48E+01 + 1.52E+00	5.92E+01 + 5.51E+00	1.02E+02 + 1.16E+01	3.04E+01 + 4.42E-04	3.04E+01 + 7.51E-03	3.53E+01 + 1.14E+00	3.25E+01 + 6.96E-01	3.04E+01 + 0.00E+00	1.34E+02 + 7.47E+00	3.13E+01 + 3.80E-01	
F ₁₈	1.72E+02 + 1.33E+01	8.33E+01 + 2.06E+01	6.04E+01 + 9.71E+00	1.82E+02 + 1.19E+01	1.23E+02 + 1.83E+01	1.05E+02 + 2.95E+01	7.94E+01 + 1.10E+01	7.68E+01 + 7.12E+00	7.25E+01 + 5.53E+00	2.19E+02 + 1.08E+01	6.48E+01 + 9.65E+00	
F ₁₉	1.84E+00 + 1.45E-01	2.55E+00 + 5.18E-01	2.30E+00 + 6.18E-01	5.40E+00 + 8.02E-01	1.10E+00 + 2.83E-01	1.20E+00 + 1.88E-01	1.50E+00 + 1.74E-01	2.67E+00 + 2.28E-01	1.36E+00 + 1.19E-01	1.29E+01 + 1.09E+00	1.14E+00 + 1.63E-01	
F ₂₀	1.18E+01 + 3.21E-01	1.05E+01 + 8.07E-01	1.26E+01 + 7.33E-01	1.13E+01 + 3.24E-01	1.16E+01 + 4.36E-01	1.13E+01 + 5.59E-01	1.17E+01 + 6.52E-01	1.06E+01 + 3.62E-01	1.05E+01 + 5.98E-01	1.25E+01 + 2.23E-01	9.94E+00 + 4.97E-01	
F ₂₁	2.97E+02 + 8.47E+01	3.27E+02 + 8.65E+01	2.67E+02 + 6.52E+01	3.19E+02 + 6.20E+01	2.94E+02 + 8.21E+01	2.85E+02 + 6.87E+01	3.36E+02 + 9.78E+01	2.67E+02 + 4.71E+01	3.09E+02 + 5.59E+01	2.79E+02 + 4.10E+01	3.17E+02 + 6.01E+01	
F ₂₂	1.23E+02 + 1.61E+01	1.79E+02 + 4.50E+01	4.56E+03 + 6.02E+02	2.50E+03 + 3.82E+02	5.16E+01 + 5.72E+01	7.66E+01 + 4.83E+01	2.56E+02 + 9.13E+01	2.90E+02 + 1.21E+02	9.81E+01 + 2.50E+01	4.92E+03 + 2.98E+02	1.21E+02 + 4.39E+00	
F ₂₃	5.01E+03 + 4.02E+02	4.22E+03 + 8.74E+02	4.18E+03 + 9.12E+02	5.81E+03 + 4.99E+02	4.61E+03 + 5.38E+02	4.89E+03 + 8.07E+02	3.59E+03 + 4.99E+02	4.34E+03 + 3.53E+02	3.51E+03 + 4.07E+02	7.54E+03 + 2.64E+02	3.28E+03 + 3.80E+02	
F ₂₄	2.52E+02 + 1.37E+01	2.32E+02 + 2.57E+01	2.92E+02 + 1.88E+01	2.02E+02 + 1.38E+00	2.48E+02 + 7.40E+00	2.53E+02 + 8.89E+00	2.64E+02 + 9.15E+00	3.03E+02 + 2.64E+00	2.05E+02 + 5.24E+00	2.01E+02 + 3.35E-01	2.00E+02 + 3.60E-01	
F ₂₅	2.75E+02 + 1.74E+01	2.78E+02 + 9.90E+00	2.99E+02 + 6.79E+00	2.30E+02 + 2.06E+01	2.60E+02 + 6.79E+00	2.64E+02 + 8.26E+00	2.83E+02 + 5.79E+00	2.96E+02 + 1.99E+00	2.59E+02 + 1.95E+01	3.14E+02 + 3.10E+00	2.14E+02 + 2.09E+01	
F ₂₆	2.10E+02 + 3.90E+01	2.15E+02 + 5.25E+01	3.28E+02 + 5.42E+01	2.18E+02 + 3.97E+01	2.58E+02 + 6.89E+01	2.00E+02 + 4.86E-03	2.00E+02 + 6.62E-03	2.00E+02 + 0.00E+00	2.02E+02 + 1.47E+01	2.06E+02 + 1.21E+00	2.00E+02 + 6.39E-03	
F ₂₇	1.01E+03 + 7.37E+01	6.47E+02 + 1.37E+02	1.19E+03 + 1.85E+02	3.26E+02 + 1.13E+01	7.22E+02 + 8.60E+01	8.88E+02 + 9.10E+01	9.38E+02 + 5.75E+01	1.19E+03 + 1.19E+02	3.88E+02 + 1.08E+02	5.66E+02 + 1.70E+02	3.06E+02 + 5.37E+02	
F ₂₈	3.00E+02 + 0.00E+00	3.88E+02 + 3.23E+02	3.00E+02 + 0.00E+00	3.00E+02 + 3.22E-05	3.00E+02 + 3.80E-04	3.00E+02 + 0.00E+00	3.00E+02 + 0.00E+00	2.96E+02 + 0.00E+00	3.00E+02 + 0.00E+00	3.00E+02 + 0.00E+00	3.00E+02 + 0.00E+00	
NoB	5	5	4	2	5	5	3	10	5	2	11	
-	14	19	21	23	16	17	18	17	12	23		
=	7	4	4	3	8	5	6	5	6	5		
+	7	5	3	2	4	6	4	6	10	0		

TABLE IX
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN IDE AND UP-TO-DATE DES OVER THE 50-DIMENSIONAL CEC 2013 BENCHMARK SET

50-D	DE1	DE2	DE3	DE4	DE5	DE6	DE7	DE8	DE9	DE10	IDE	
	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	Mean/Std	
F ₁	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 2.93E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 3.08E-08 - 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00 = 0.00E+00
F ₂	3.23E+05 + 1.54E+05	0.00E+00 + 0.00E+00	3.60E+05 + 1.66E+05	2.04E+05 + 7.60E+04	6.05E+05 + 2.43E+05	5.65E+05 + 2.54E+05	6.55E+05 + 3.74E+05	1.68E+05 + 2.82E+04	2.66E+04 + 1.12E+04	3.92E+08 + 4.90E+07	1.68E+06 + 4.23E+05	
F ₃	8.61E+06 - 2.30E+07	3.81E+05 + 1.35E+06	6.98E+06 + 1.25E+07	7.48E+06 - 7.52E+06	4.78E+07 - 6.79E+07	4.44E+07 - 4.51E+07	2.20E+08 - 2.14E+08	7.08E+05 - 3.56E+05	8.80E+05 - 1.94E+06	6.28E+09 - 1.02E+09	1.38E+05 + 1.85E+05	
F ₄	2.32E-01 + 3.09E-01	0.00E+00 + 0.00E+00	1.53E+00 + 1.40E+00	2.20E+02 + 9.49E+01	8.34E+04 - 1.54E+04	5.18E+00 + 4.69E+00	1.21E+03 + 1.94E+03	6.58E+02 + 1.74E+02	1.61E-03 + 1.40E-03	8.79E+04 + 7.55E+03	6.85E+03 - 1.10E+03	
F ₅	0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00	1.39E-03 - 1.85E-03	2.43E-06 - 1.13E-06	0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00	3.82E-06 - 7.36E-07	0.00E+00 = 0.00E+00	
F ₆	4.34E+01 + 0.00E+00	4.30E+01 + 6.28E+00	3.90E+01 + 1.52E+00	7.36E+01 - 2.77E+01	4.30E+01 + 3.67E+00	4.37E+01 + 1.10E+00	4.34E+01 + 4.97E-14	4.07E+01 + 6.89E+00	4.28E+01 + 5.47E+00	4.51E+01 + 1.87E-01	4.34E+01 - 2.62E-04	
F ₇	8.26E+01 - 1.54E+01	4.32E+01 - 1.66E+01	3.66E+01 - 1.59E+01	2.07E+01 - 9.07E+00	2.94E+01 - 1.28E+01	3.17E+01 - 9.11E+00	1.05E+02 - 9.53E+00	4.96E+01 - 5.26E+00	2.33E+01 - 9.23E+00	9.10E+01 - 6.02E+00	6.85E+03 - 1.55E+00	
F ₈	2.11E+01 = 4.61E-02	2.11E+01 = 3.85E-02	2.11E+01 = 3.08E-02	2.11E+01 = 3.50E-02	2.11E+01 = 3.80E-02	2.11E+01 = 4.19E-02	2.11E+01 = 9.52E-02	2.11E+01 = 2.68E-02	2.11E+01 = 1.67E-01	2.09E+01 + 4.39E-02	2.11E+01 = 2.44E-02	
F ₉	5.67E+01 - 2.54E+00	4.36E+01 - 4.06E+00	6.09E+01 - 1.65E+01	2.60E+01 + 3.02E+00	5.33E+01 - 9.68E+00	5.14E+01 - 4.98E+00	4.71E+01 - 3.17E+00	6.09E+01 - 1.64E+00	5.54E+01 - 1.96E+00	7.19E+01 - 1.90E+00	3.56E+01 - 5.54E+01	
F ₁₀	3.54E-02 - 1.83E-02	2.47E-02 + 1.48E-02	6.71E-02 - 4.14E-02	5.99E-01 - 3.39E-01	1.47E-01 - 7.58E-02	5.86E-02 - 3.85E-02	3.21E-02 = 1.67E-02	1.76E-02 + 6.78E-03	7.37E-02 + 3.64E-02	3.63E+02 - 5.06E+01	4.38E-02 - 2.17E-02	
F ₁₁	0.00E+00 = 0.00E+00	4.81E+01 - 1.49E+01	3.44E+01 - 1.44E+01	1.68E+02 - 4.05E+01	1.95E-02 - 1.38E-01	0.00E+00 = 0.00E+00	4.64E+00 - 4.38E+00	0.00E+00 = 0.00E+00	0.00E+00 = 0.00E+00	2.83E+02 - 1.17E+01	0.00E+00 = 0.00E+00	
F ₁₂	1.89E+02 - 2.38E+01	1.57E+02 - 4.52E+01	5.96E+01 - 1.68E+01	2.57E+02 - 2.23E+01	9.72E+01 - 2.53E+01	8.78E+01 - 2.16E+01	1.34E+02 - 3.55E+01	1.20E+02 - 8.10E+00	5.86E+01 + 1.10E+01	4.17E+02 - 1.52E+01	6.89E+01 - 8.82E+00	
F ₁₃	2.53E+02 - 3.05E+01	3.35E+02 - 5.63E+01	1.55E+02 - 3.55E+01	3.06E+02 - 2.75E+01	1.76E+02 - 2.34E+01	1.59E+02 - 2.63E+01	2.47E+02 - 4.87E+01	2.19E+02 - 1.72E+01	1.45E+02 - 1.93E+01	4.20E+02 - 1.31E+01	1.34E+02 - 2.28E+01	
F ₁₄	3.65E-02 + 2.04E-02	3.41E+02 + 2.05E+02	9.96E+03 - 4.28E+02	7.34E+03 - 5.77E+02	8.01E+00 - 6.69E+00	2.07E+01 + 1.33E+01	2.31E+02 - 8.64E+01	8.06E+02 - 1.53E+02	3.45E-02 + 1.91E-02	1.04E+04 - 3.31E+02	1.17E+02 - 8.38E+01	
F ₁₅	9.27E+03 - 4.53E+02	8.54E+03 - 9.77E+02	9.34E+03 - 3.30E+03	1.25E+04 - 5.55E+02	9.48E+03 - 1.05E+03	9.11E+03 - 1.03E+03	6.25E+03 + 1.40E+03	7.69E+03 - 2.84E+02	6.82E+03 - 4.36E+02	1.41E+04 - 3.29E+02	6.54E+03 - 5.91E+02	
F ₁₆	2.30E+00 - 6.35E-01	8.96E-02 + 4.24E-02	3.24E+00 - 3.69E-01	3.39E+00 - 3.19E-01	3.13E+00 - 3.91E-01	2.95E+00 - 6.29E-01	1.63E+00 - 1.37E+00	1.80E+00 - 1.98E-01	1.28E+00 + 2.05E-01	3.37E+00 - 2.39E-01	1.59E+00 - 2.36E-01	
F ₁₇	5.08E+01 + 6.39E-14	6.57E+01 + 5.27E+00	1.72E+02 - 1.57E+01	2.38E+02 - 2.19E+01	5.08E+01 + 3.21E-01	5.08E+01 + 2.42E-02	6.58E+01 - 2.31E+00	7.95E+01 - 1.79E+00	5.08E+01 + 0.00E+00	3.42E+02 - 1.24E+01	5.92E+01 - 1.41E+00	
F ₁₈	3.28E+02 - 3.80E+01	1.93E+02 - 3.46E+01	1.05E+02 + 1.40E+01	3.87E+02 - 1.80E+01	2.18E+02 - 3.08E+01	1.91E+02 - 5.27E+01	1.57E+02 + 2.09E+01	1.81E+02 - 7.56E+00	1.37E+02 + 1.28E+01	4.61E+02 - 1.09E+01	1.68E+02 - 1.27E+01	
F ₁₉	3.43E+00 - 1.86E-01	5.43E+00 - 1.07E+00	5.08E+00 - 1.79E+00	2.12E+01 - 4.72E+00	2.24E+00 - 5.41E-01	2.05E+00 + 3.30E-01	2.95E+00 - 2.89E-01	7.57E+00 - 4.73E-01	2.64E+00 - 2.80E-01	3.20E+01 - 1.30E+00	2.24E+00 - 3.66E-01	
F ₂₀	2.15E+01 - 3.82E-01	1.92E+01 = 8.86E-01	2.23E+01 = 8.95E-01	2.07E+01 - 4.03E-01	2.15E+01 - 4.27E-01	2.06E+01 - 8.17E-01	2.17E+01 - 8.51E-01	1.93E+01 - 3.52E-01	1.93E+01 = 7.62E-01	2.26E+01 = 2.31E-01	1.93E+01 - 4.47E-01	
F ₂₁	4.60E+02 + 4.06E+02	8.46E+02 + 3.43E+02	6.81E+02 = 4.20E+02	9.65E+02 = 1.42E+02	8.24E+02 = 3.97E+02	6.06E+02 = 4.38E+02	5.24E+02 + 3.98E+02	3.12E+02 + 2.43E+02	8.45E+02 = 3.59E+02	4.55E+02 = 3.53E+02	7.32E+02 = 3.82E+02	
F ₂₂	3.60E+01 - 2.42E+01	3.39E+02 - 2.24E+02	1.06E+04 - 4.86E+02	7.72E+03 - 8.38E+02	3.10E+01 - 3.85E+01	3.94E+01 + 2.94E+01	6.89E+02 + 1.50E+02	2.59E+03 - 3.78E+02	1.33E+01 + 7.05E+00	1.09E+04 + 3.70E+02	6.88E+01 - 2.03E+01	
F ₂₃	9.78E+03 - 5.28E+02	9.89E+03 - 1.90E+03	9.09E+03 - 3.19E+03	1.18E+04 - 1.46E+03	9.48E+03 - 1.01E+03	9.26E+03 - 1.01E+03	7.77E+03 - 2.18E+03	9.68E+03 = 3.95E+02	7.63E+03 = 6.51E+02	1.47E+04 - 3.88E+02	7.32E+03 - 6.92E+02	
F ₂₄	3.33E+02 - 1.52E+01	3.00E+02 - 1.20E+01	3.84E+02 - 7.90E+00	2.78E+02 - 1.81E+01	2.89E+02 - 1.19E+01	3.11E+02 - 1.42E+01	3.31E+02 - 7.40E+00	3.98E+02 - 2.25E+00	2.34E+02 - 1.00E+01	3.09E+02 - 7.90E+00	2.02E+02 - 1.14E+00	
F ₂₅	3.64E+02 - 2.07E+01	3.68E+02 - 1.36E+01	3.83E+02 - 3.96E+00	3.54E+02 - 1.70E+01	3.17E+02 - 1.08E+01	3.35E+02 - 1.27E+01	3.60E+02 - 9.94E+00	3.79E+02 - 2.85E+00	3.40E+02 - 3.06E+01	4.23E+02 - 3.81E+00	3.03E+02 - 1.09E+01	
F ₂₆	3.28E+02 = 1.20E+02	2.91E+02 = 9.70E+01	4.09E+02 = 4.74E+01	3.47E+02 = 5.95E+01	3.97E+02 = 2.33E+01	2.87E+02 = 1.09E+02	2.00E+02 = 3.37E-02	2.01E+02 + 1.70E+00	2.58E+02 = 8.00E+01	3.31E+02 = 5.07E+01	2.23E+02 - 4.46E+01	
F ₂₇	1.73E+03 - 1.06E+02	1.18E+03 - 1.67E+02	2.14E+03 - 4.54E+01	1.11E+03 - 1.17E+02	1.16E+03 - 1.22E+02	1.53E+03 - 1.44E+02	1.55E+03 - 9.50E+01	2.17E+03 - 3.18E+01	9.36E+02 - 3.04E+02	2.07E+03 - 4.32E+01	3.58E+02 - 3.30E+01	
F ₂₈	4.00E+02 = 0.00E+00	1.07E+03 = 1.27E+03	6.97E+02 = 8.29E+02	4.62E+02 = 4.35E+02	9.43E+02 = 1.17E+03	7.54E+02 = 9.69E+02	4.00E+02 = 1.94E-10	4.00E+02 = 0.00E+00	4.58E+02 = 4.09E+02	4.00E+02 = 1.01E-05	4.00E+02 = 0.00E+00	
NoB	5	6	4	2	1	5	5	6	7	2	11	
-	14	16	20	21	20	16	15	16	11	24		
=	6	6	4	4	2	6	6	5	7	4		
+	8	6	4	3	6	6	7	7	10	0		

TABLE X
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN CLPSO, CMA-ES, GL-25 AND IDE OVER THE 10-DIMENSIONAL CEC 2013 BENCHMARK SET

10-D	CLPSO	CMA-ES	GL-25	IDE
	Mean/Std	Mean/Std	Mean/Std	Mean/Std
F ₁	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00
F ₂	7.05E+05 -	0.00E+00 +	3.22E+05 -	6.55E-06
	5.05E+05	0.00E+00	2.57E+05	1.53E-05
F ₃	2.72E+05 -	1.25E-01 +	8.08E+05 -	3.45E-01
	4.19E+05	8.84E-01	1.80E+06	1.24E+00
F ₄	3.58E+03 -	0.00E+00 +	1.33E+03 -	5.49E-06
	1.91E+03	0.00E+00	1.42E+03	1.29E-05
F ₅	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00
F ₆	2.52E+00 +	6.35E+00 -	6.06E+00 -	4.04E+00
	3.72E+00	4.74E+00	4.72E+00	4.88E+00
F ₇	7.37E+00 -	1.35E+05 -	2.08E+00 -	7.77E-04
	5.67E+00	8.00E+05	2.46E+00	9.66E-04
F ₈	2.04E+01 -	2.11E+01 -	2.04E+01 =	2.03E+01
	7.72E-02	4.46E-01	6.57E-02	9.40E-02
F ₉	4.05E+00 -	1.41E+01 -	3.42E+00 -	8.66E-01
	8.82E-01	3.64E+00	1.03E+00	6.94E-01
F ₁₀	2.87E-01 -	1.75E-02 +	2.87E-01 -	3.00E-02
	1.21E-01	1.64E-02	2.53E-01	1.82E-02
F ₁₁	5.85E-02 =	1.91E+02 -	3.81E+00 -	0.00E+00
	2.36E-01	2.61E+02	2.10E+00	0.00E+00
F ₁₂	9.39E+00 -	3.20E+02 -	9.14E+00 -	4.92E+00
	2.98E+00	3.19E+02	3.69E+00	1.62E+00
F ₁₃	1.41E+01 -	2.40E+02 -	1.20E+01 -	5.17E+00
	5.96E+00	3.30E+02	5.45E+00	3.01E+00
F ₁₄	8.87E+00 +	1.77E+03 -	2.79E+02 -	3.74E-01
	2.95E+01	4.29E+02	2.00E+02	6.61E-01
F ₁₅	5.67E+02 -	1.83E+03 -	9.12E+02 -	4.15E+02
	1.91E+02	4.01E+02	4.43E+02	1.47E+02
F ₁₆	5.83E-01 =	2.42E-01 +	1.24E+00 -	5.43E-01
	1.81E-01	1.71E-01	1.88E-01	1.41E-01
F ₁₇	1.02E+01 =	1.04E+03 -	1.71E+01 -	1.01E+01
	7.32E-02	4.09E+02	4.58E+00	6.13E-03
F ₁₈	2.11E+01 -	1.01E+03 -	3.18E+01 -	1.47E+01
	2.84E+00	3.19E+02	4.57E+00	1.51E+00
F ₁₉	2.61E-01 =	1.01E+00 -	8.99E-01 -	2.93E-01
	8.32E-02	4.19E-01	3.17E-01	6.36E-02
F ₂₀	2.79E+00 -	3.84E+00 -	2.33E+00 -	1.64E+00
	4.76E-01	5.25E-01	6.33E-01	3.62E-01
F ₂₁	2.88E+02 +	3.83E+02 =	4.00E+02 =	3.96E+02
	1.21E+02	6.24E+01	0.00E+00	2.80E+01
F ₂₂	4.46E+01 -	2.21E+03 -	2.02E+02 -	9.15E+00
	5.04E+01	4.88E+02	1.79E+02	5.82E+00
F ₂₃	7.42E+02 -	2.27E+03 -	4.85E+02 =	4.03E+02
	1.94E+02	4.51E+02	2.85E+02	1.87E+02
F ₂₄	1.42E+02 +	3.89E+02 -	2.01E+02 -	1.98E+02
	3.46E+01	1.96E+02	1.41E+01	1.34E+01
F ₂₅	1.92E+02 +	2.49E+02 -	2.01E+02 -	2.00E+02
	3.19E+01	6.32E+01	8.74E-01	2.02E-05
F ₂₆	1.22E+02 -	2.47E+02 -	1.25E+02 -	1.20E+02
	2.16E+01	1.37E+02	3.51E+01	3.48E+01
F ₂₇	3.25E+02 -	3.45E+02 -	3.02E+02 =	3.02E+02
	3.53E+01	5.60E+01	2.71E+00	1.40E+01
F ₂₈	2.50E+02 =	1.59E+03 -	3.00E+02 =	2.88E+02
	8.60E+01	1.40E+03	0.00E+00	4.75E+01
NoB	8	7	3	17
-	16	20	22	
=	7	3	6	
+	5	5	0	

TABLE XI
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN CLPSO, CMA-ES, GL-25 AND IDE OVER THE 30-DIMENSIONAL CEC 2013 BENCHMARK SET

30-D	CLPSO	CMA-ES	GL-25	IDE
	Mean/Std	Mean/Std	Mean/Std	Mean/Std
F ₁	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00
F ₂	1.82E+07 -	0.00E+00 +	7.00E+06 -	2.42E+05
	4.77E+06	0.00E+00	2.48E+06	1.40E+05
F ₃	2.20E+08 -	7.89E+02 =	3.07E+06 -	2.08E+04
	1.31E+08	3.07E+03	3.19E+06	1.46E+05
F ₄	2.57E+04 -	0.00E+00 +	2.90E+03 -	9.75E+02
	4.06E+03	0.00E+00	1.87E+03	3.26E+02
F ₅	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00
F ₆	2.64E+01 -	2.07E+00 +	2.96E+01 -	5.00E+00
	7.42E+00	7.17E+00	2.24E+01	2.82E+00
F ₇	6.92E+01 -	1.12E+07 -	8.23E+00 -	5.55E-01
	1.12E+01	8.01E+07	4.69E+00	5.07E-01
F ₈	2.10E+01 -	2.15E+01 -	2.10E+01 -	2.09E+01
	5.27E-02	8.07E-02	4.84E-02	4.78E-02
F ₉	2.76E+01 -	4.55E+01 -	2.53E+01 -	1.76E+01
	1.67E+00	8.11E+00	3.17E+00	3.39E+00
F ₁₀	2.18E+00 -	1.50E-02 +	1.39E-01 -	3.42E-02
	4.22E-01	1.19E-02	1.03E-01	1.47E-02
F ₁₁	0.00E+00 =	4.83E+01 -	2.55E+01 -	0.00E+00
	0.00E+00	1.41E+01	8.85E+00	0.00E+00
F ₁₂	1.06E+02 -	4.94E+02 -	1.07E+02 -	2.73E+01
	1.15E+01	8.39E+02	5.26E+01	4.59E+00
F ₁₃	1.49E+02 -	1.38E+03 -	1.40E+02 -	5.13E+01
	1.64E+01	1.44E+03	4.60E+01	1.14E+01
F ₁₄	1.82E+01 -	5.54E+03 -	3.35E+03 -	2.34E+01
	6.33E+00	6.04E+02	9.61E+02	3.18E+01
F ₁₅	4.55E+03 -	5.12E+03 -	6.98E+03 -	2.93E+03
	4.18E+02	8.64E+02	3.38E+02	3.88E+02
F ₁₆	1.96E+00 -	1.01E-01 +	2.48E+00 -	1.12E+00
	3.07E-01	5.88E-02	3.29E-01	1.67E-01
F ₁₇	3.15E+01 =	4.28E+03 -	1.10E+02 -	3.13E+01
	2.75E-01	8.11E+02	3.47E+01	3.80E-01
F ₁₈	1.86E+02 -	4.11E+03 -	2.01E+02 -	6.48E+01
	1.35E+01	7.74E+02	1.07E+01	9.65E+00
F ₁₉	1.35E+00 -	3.46E+00 -	6.07E+00 -	1.14E+00
	3.53E-01	9.99E-01	2.30E+00	1.63E-01
F ₂₀	1.38E+01 -	1.28E+01 -	1.13E+01 -	9.94E+00
	5.12E-01	8.43E-01	5.04E-01	4.97E-01
F ₂₁	2.87E+02 =	3.08E+02 =	3.00E+02 =	3.17E+02
	2.78E+01	8.65E+01	5.88E+01	6.01E+01
F ₂₂	1.43E+02 -	7.03E+03 -	2.15E+03 -	1.21E+02
	2.69E+01	6.84E+02	9.82E+02	4.39E+00
F ₂₃	5.44E+03 -	6.79E+03 -	6.75E+03 -	3.28E+03
	4.14E+02	8.47E+02	9.38E+02	3.80E+02
F ₂₄	2.72E+02 -	7.49E+02 -	2.06E+02 -	2.00E+02
	6.57E+00	6.43E+02	3.07E+00	3.60E-01
F ₂₅	2.96E+02 -	3.14E+02 -	2.48E+02 -	2.14E+02
	5.43E+00	1.62E+02	2.73E+01	2.09E+01
F ₂₆	2.02E+02 -	4.62E+02 -	2.00E+02 -	2.00E+02
	6.19E-01	4.22E+02	6.18E-02	6.39E-03
F ₂₇	7.77E+02 -	5.86E+02 -	4.38E+02 -	3.06E+02
	3.14E+02	1.81E+02	6.78E+01	5.37E+00
F ₂₈	3.00E+02 =	1.56E+03 -	3.00E+02 =	3.00E+02
	3.10E-05	3.72E+03	0.00E+00	0.00E+00
NoB	6	8	4	20
-	23	19	24	
=	5	4	4	
+	0	5	0	

TABLE XII
EXPERIMENTAL RESULTS OF THE COMPARISON BETWEEN CLPSO, CMA-ES, GL-25 AND IDE OVER THE 50-DIMENSIONAL CEC 2013 BENCHMARK SET

50-D	CLPSO	CMA-ES	GL-25	IDE
	Mean/Std	Mean/Std	Mean/Std	Mean/Std
F ₁	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00
F ₂	5.47E+07 -	0.00E+00 +	1.36E+07 -	1.68E+06
	1.16E+07	0.00E+00	8.26E+06	4.23E+05
F ₃	6.15E+09 -	7.32E+03 +	4.45E+07 -	1.38E+05
	2.05E+09	2.92E+04	5.64E+07	1.85E+05
F ₄	6.07E+04 -	0.00E+00 +	2.56E+03 +	6.85E+03
	7.29E+03	0.00E+00	1.63E+03	1.10E+03
F ₅	0.00E+00 =	0.00E+00 =	0.00E+00 =	0.00E+00
	0.00E+00	0.00E+00	0.00E+00	0.00E+00
F ₆	4.73E+01 -	4.36E+01 +	4.47E+01 -	4.34E+01
	4.61E-01	7.95E-01	7.40E-01	2.62E-04
F ₇	1.09E+02 -	2.58E+01 -	3.00E+01 -	3.18E+00
	8.19E+00	1.14E+01	5.03E+00	1.55E+00
F ₈	2.11E+01 -	2.15E+01 -	2.11E+01 =	2.11E+01
	3.61E-02	7.99E-02	3.46E-02	2.44E-02
F ₉	5.56E+01 -	7.58E+01 -	5.26E+01 -	3.56E+01
	2.36E+00	8.73E+00	3.34E+00	5.54E+00
F ₁₀	3.03E+01 -	1.87E-02 +	1.41E-01 -	4.38E-02
	5.14E+00	1.47E-02	2.35E-01	2.17E-02
F ₁₁	4.26E-05 -	1.37E+02 -	4.97E+01 -	0.00E+00
	2.22E-05	2.84E+02	1.34E+01	0.00E+00
F ₁₂	3.45E+02 -	2.48E+03 -	2.46E+02 -	6.89E+01
	2.42E+01	1.52E+03	1.27E+02	8.82E+00
F ₁₃	3.91E+02 -	3.47E+03 -	3.22E+02 -	1.34E+02
	1.87E+01	1.39E+03	8.19E+01	2.28E+01
F ₁₄	1.35E+02 =	8.58E+03 -	6.48E+03 -	1.17E+02
	2.05E+01	1.11E+03	2.74E+03	8.38E+01
F ₁₅	1.05E+04 -	8.84E+03 -	1.37E+04 -	6.54E+03
	4.79E+02	9.11E+02	3.74E+02	5.91E+02
F ₁₆	3.00E+00 -	5.23E-02 +	3.33E+00 -	1.59E+00
	3.37E-01	1.84E-02	3.00E-01	2.36E-01
F ₁₇	6.22E+01 -	7.10E+03 -	1.83E+02 -	5.92E+01
	1.31E+00	1.31E+03	5.09E+01	1.41E+00
F ₁₈	4.36E+02 -	7.19E+03 -	4.11E+02 -	1.68E+02
	1.48E+01	1.06E+03	2.28E+01	1.27E+01
F ₁₉	3.66E+00 -	6.22E+00 -	1.12E+01 -	2.24E+00
	6.13E-01	1.21E+00	2.88E+00	3.66E-01
F ₂₀	2.36E+01 -	2.22E+01 -	2.15E+01 -	1.93E+01
	4.43E-01	1.07E+00	4.12E-01	4.47E-01
F ₂₁	5.31E+02 +	7.45E+02 =	9.05E+02 -	7.32E+02
	2.39E+02	3.75E+02	3.30E+02	3.82E+02
F ₂₂	3.68E+02 -	1.25E+04 -	4.45E+03 -	6.88E+01
	1.58E+02	1.27E+03	1.56E+03	2.03E+01
F ₂₃	1.21E+04 -	1.16E+04 -	1.38E+04 -	7.32E+03
	6.60E+02	9.26E+02	4.42E+02	6.92E+02
F ₂₄	3.51E+02 -	1.71E+03 -	2.19E+02 -	2.02E+02
	7.23E+00	1.09E+03	5.60E+00	1.14E+00
F ₂₅	3.92E+02 -	4.13E+02 =	3.41E+02 -	3.03E+02
	6.74E+00	1.69E+02	1.59E+01	1.09E+01
F ₂₆	2.06E+02 -	8.11E+02 -	2.01E+02 -	2.23E+02
	9.17E-01	8.79E+02	2.97E-01	4.46E+01
F ₂₇	1.50E+03 -	8.22E+02 -	7.09E+02 -	3.58E+02
	5.59E+02	1.30E+02	1.51E+02	3.30E+01
F ₂₈	4.00E+02 -	3.65E+03 -	4.00E+02 =	4.00E+02
	1.63E-02	6.01E+03	0.00E+00	0.00E+00
NoB	4	7	5	22
-	24	18	23	
=	3	4	4	
+	1	6	1	

TABLE XIII
THE GENERATION INDEX THRESHOLD VALES OF IDE ON 10-D, 30-D, AND 50-D PROBLEMS

Functions	Dimensions / G_T Values		
	10-D/1000	30-D/1500	50-D/1250
F1	391	762	933
F2	1638	1798	1498
F3	1837	2840	2313
F4	1531	1798	1498
F5	447	980	1344
F6	785	2992	2498
F7	1568	1828	1499
F8	1195	1783	1493
F9	1745	1797	1498
F10	1082	1190	1660
F11	1038	1798	1498
F12	1033	1871	1498
F13	1305	1798	1498
F14	1228	1797	1498
F15	1315	1797	1498
F16	1187	1790	1494
F17	1198	1797	1498
F18	1230	1797	1498
F19	1247	1798	1498
F20	1196	1796	1498
F21	383	1049	1173
F22	1311	1798	1498
F23	1353	1796	1498
F24	1733	2255	2020
F25	1844	2326	1548
F26	1107	1808	1604
F27	1295	2280	1868
F28	559	1175	1445