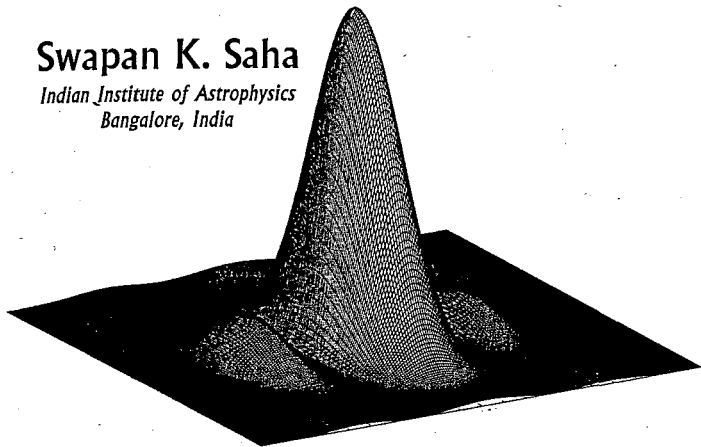


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**Diffraction-Limited
Imaging with
Large and Moderate
Telescopes**

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