

DiFi: Fast 3D Distance Field Computation using Graphics Hardware

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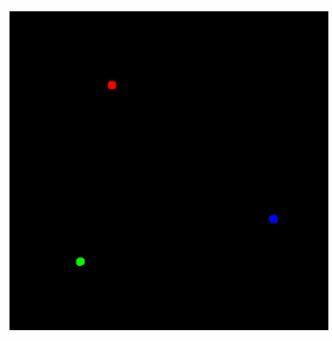
University of North Carolina at Chapel Hill

http://gamma.cs.unc.edu/DiFi

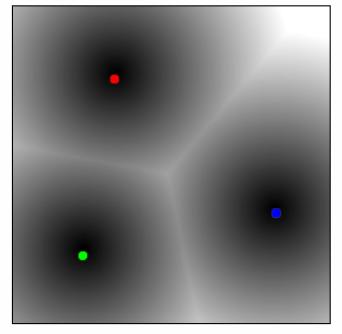


Distance Field

Given a set of geometric primitives (sites), it is a scalar field representing the minimum distance from any point to the closest site



3 point sites

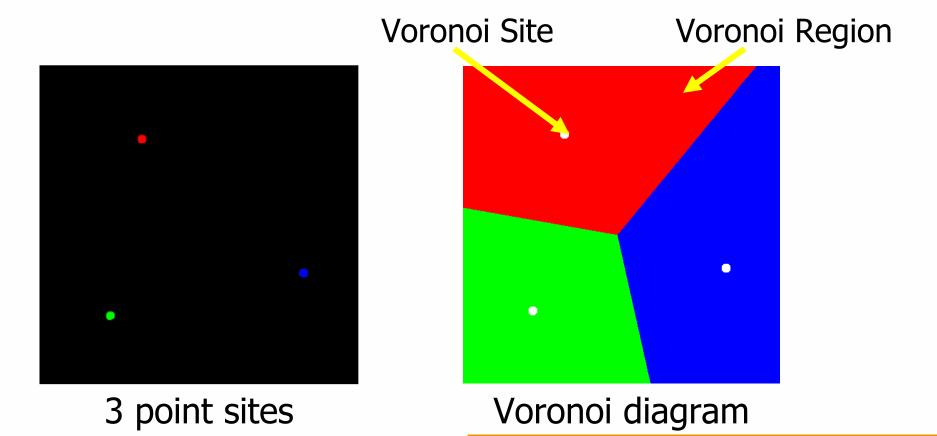


2D Distance field



Voronoi Diagram

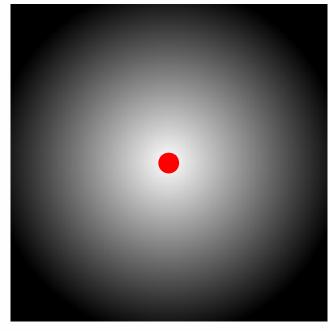
Given a collection of sites, it is a subdivision of space into cells such that all points in a cell are *closer* to one site than to any other site



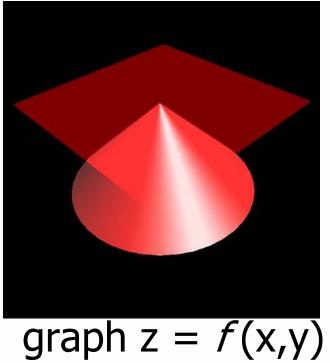


Distance Function

A scalar function $f(\mathbf{x})$ representing minimum distance from a point x to a site



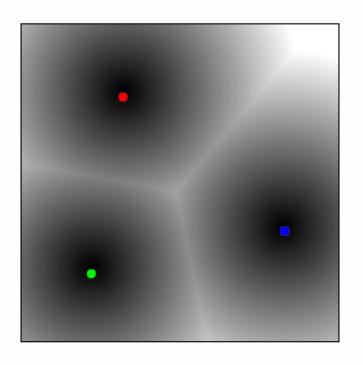
$$f(x,y) = \sqrt{x^2 + y^2}$$

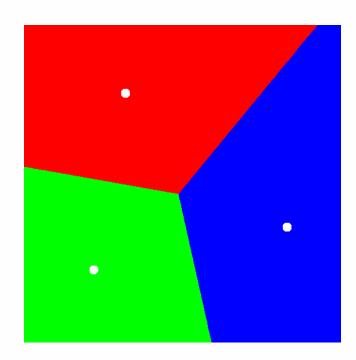




Voronoi Diagram and Distance Fields

Region where distance function contributes to final distance field = Voronoi Region







Why Should We Compute Them?

Useful in a wide variety of applications

Collision Detection Surface Reconstruction Robot Motion Planning Non-Photorealistic Rendering Surface Simplification Mesh Generation Shape Analysis



Distance field algorithm:

- Fast computation
- Applicable to complex and generic models
- No preprocessing



Outline

- Related Work
- Fast GPU based algorithm (DiFi)
- Applications and Results
- Conclusions



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Related Work

- Geometric models: Polygonal data
- Volumetric models: Image data



Related Work

- Geometric models: Polygonal data
 - Adaptive Grids [Vleugels97, Frisken00]
 - Uniform Grids [Sethian96, Hoff99, Mauch00, Sigg03, Denny03, Furhmann03]
- Volumetric models: Image data

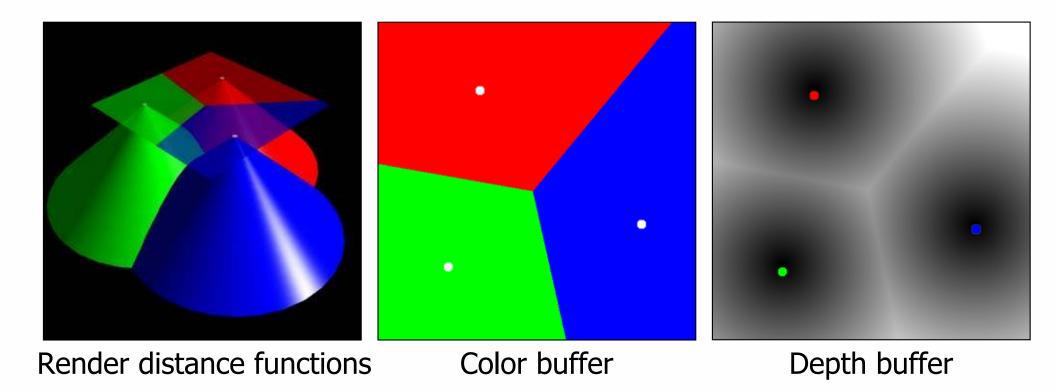


Related Work

- Geometric models: Polygonal data
- Volumetric models: Image data
 - Approximate Distance Fields [Danielsson80, Sethian96]
 - Exact Distance Fields [Mulikin92, Breen00]
 - Surveyed in [Cuisenaire99]
 - Linear time algorithms for 2D [Breu95] and k-D [Maurer03]



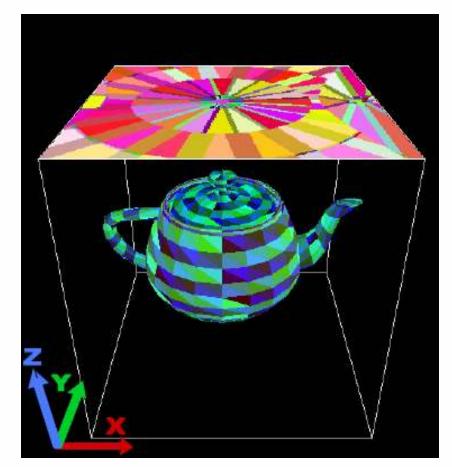
- Accelerate using graphics hardware [Hoff99]
 - Rasterization to compute distance values
 - Depth test to perform minimum operator





- Graphics hardware can generate one 2D slice at a time
- Sweep along 3rd
 dimension (Z-axis)
 computing 1 slice at a
 time

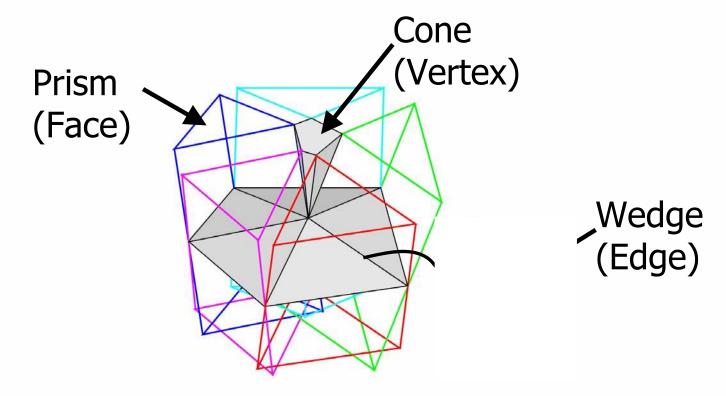
 Slow for large number of sites and high grid resolutions



3D Voronoi Diagram



 For manifold objects, Voronoi regions bounded by prisms, wedges and cones [Mauch00, Sigg03]





- Compute distance functions inside Voronoi region bounds using programmable GPU [Sigg03]
- Best suited for computation in small neighborhood of the boundary

- Not applicable to non-manifolds
- Inefficient for global computation



Contributions

- A fast 3D distance field computation algorithm
- Reduces computation using geometric properties and spatial coherence
 - Culling
 - Clamping
- Applicable to complex polygonal and image models
- No preprocessing



Outline

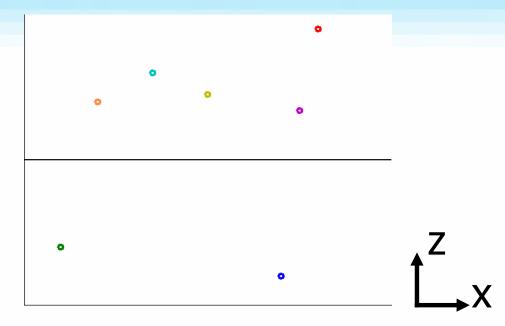
- Related Work
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 - Motivation
 - Geometric properties
 - Site classification
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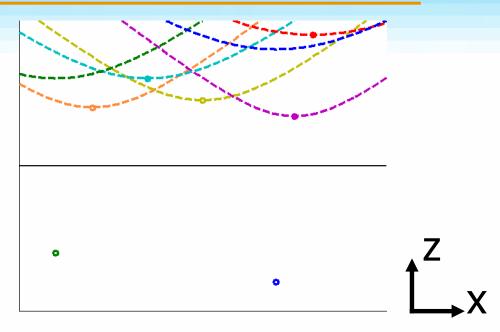
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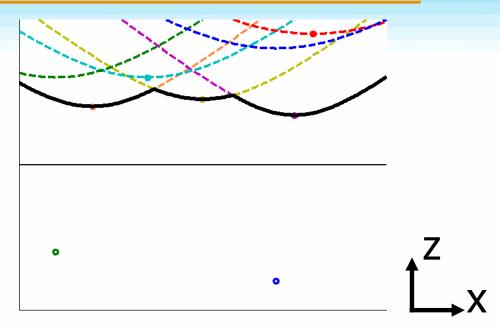




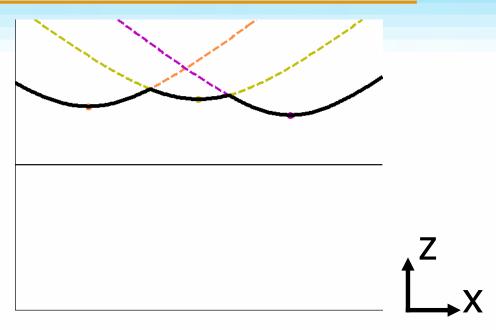




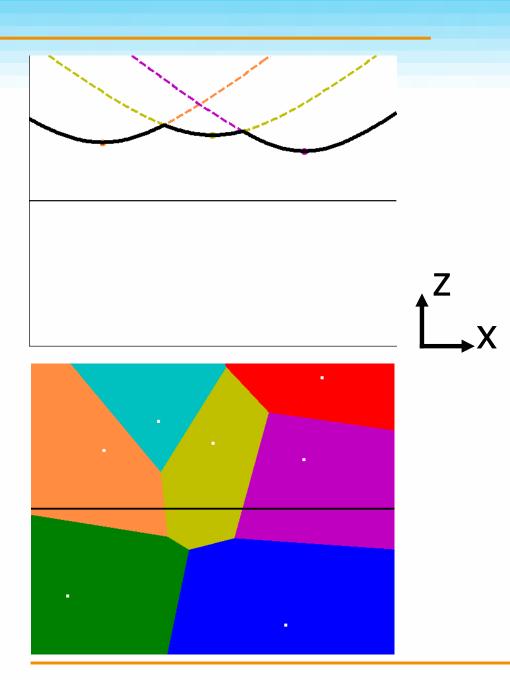






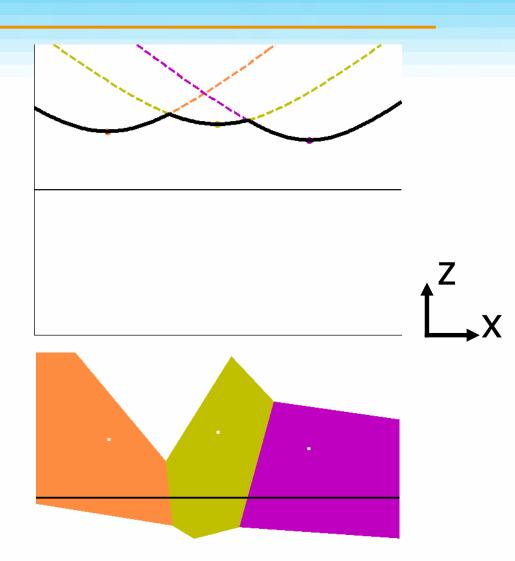








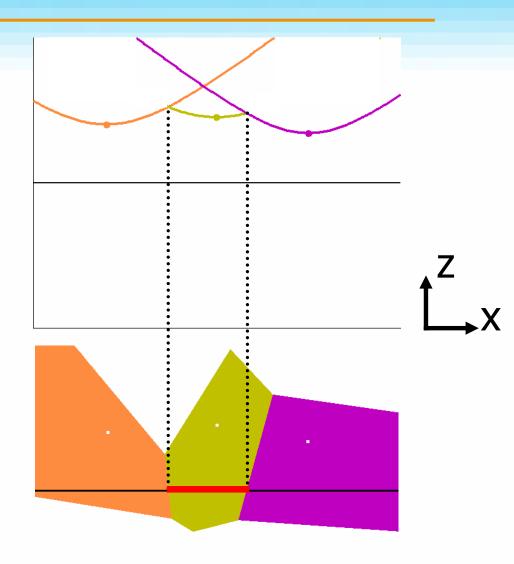
- Sites whose Voronoi regions intersect the slice contribute to distance field
 - Small number of sites contribute
 - Cull remaining sites





Motivation: Goals

- Sites whose Voronoi regions intersect the slice contribute to distance field
 - Cull remaining sites
- Compute distance function in domain where Voronoi region intersects slice
 - Clamp domain of computation





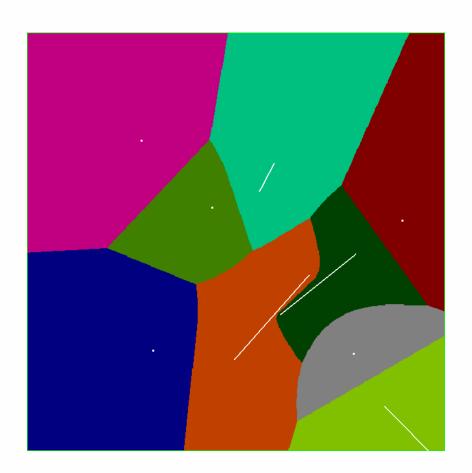
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Geometric Properties

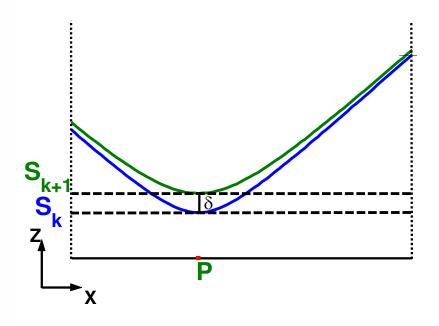
- Connectivity: Voronoi regions are connected for all L_p norms
 - Used for culling





Geometric Properties

- Connectivity: Voronoi regions are connected for all L_p norms
 Used for culling
- Coherence: Change in distance field between adjacent slices is bounded
 - Used for clamping



Distance functions for a point site P_i to adjacent slices

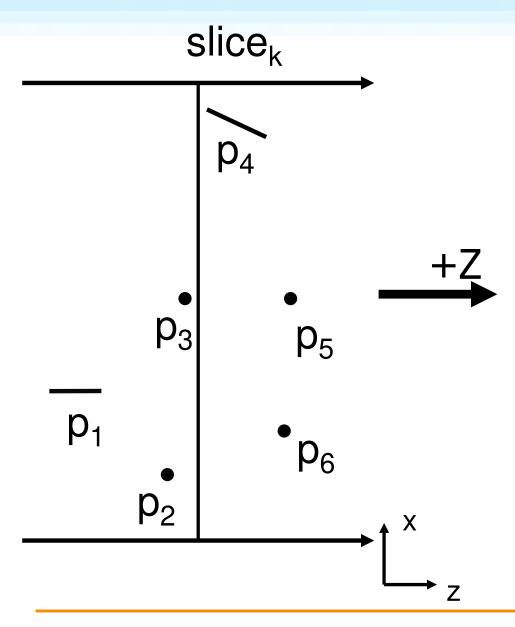


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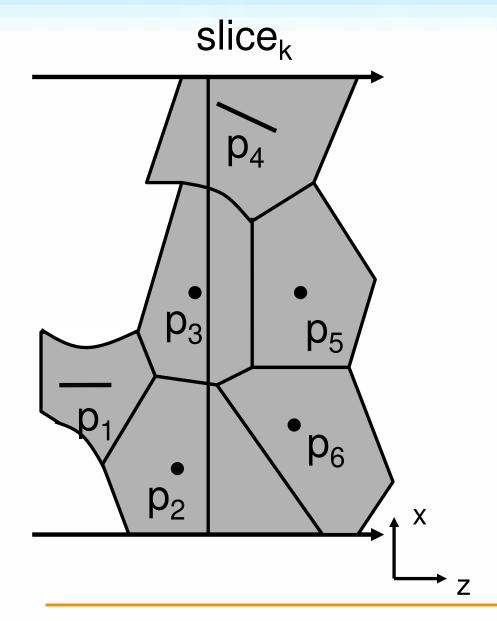


For each slice partition the set of sites



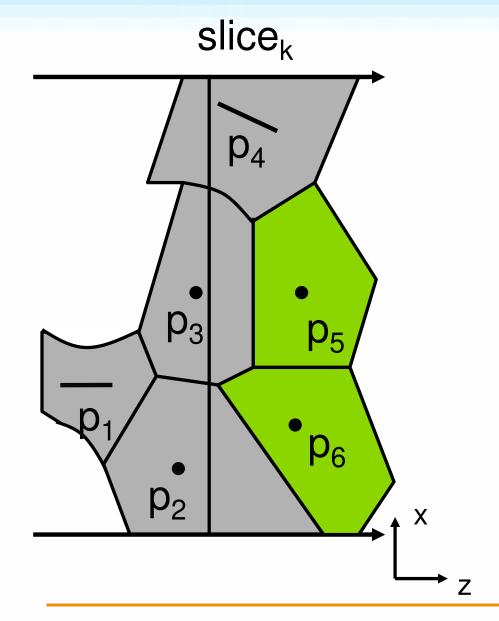


 For each slice partition the set of sites using Voronoi region bounds:



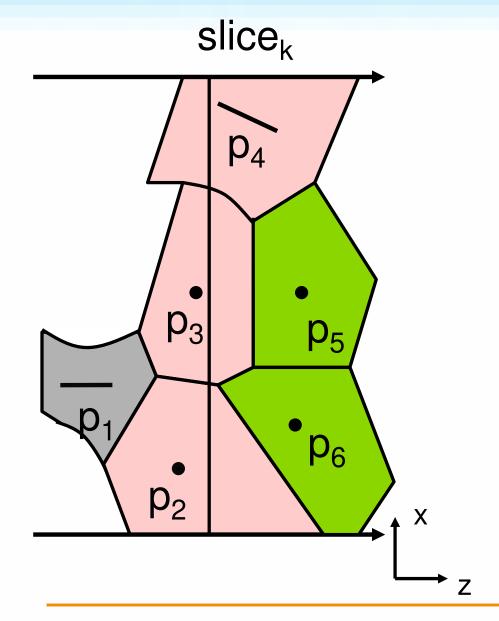


- For each slice partition the set of sites using Voronoi region bounds:
 - Approaching



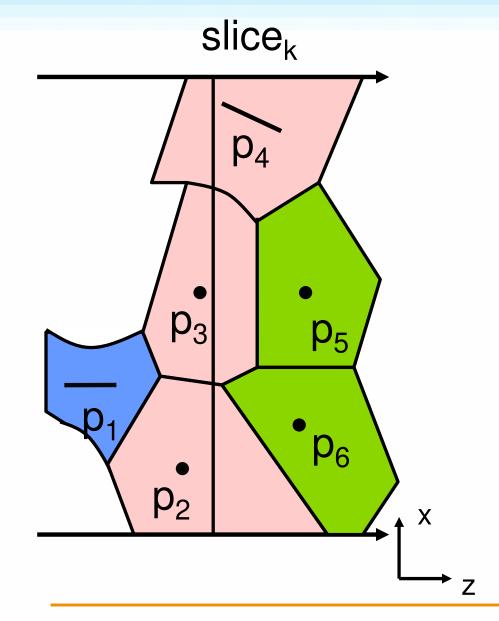


- For each slice partition the set of sites using Voronoi region bounds:
 - Approaching
 - Intersecting



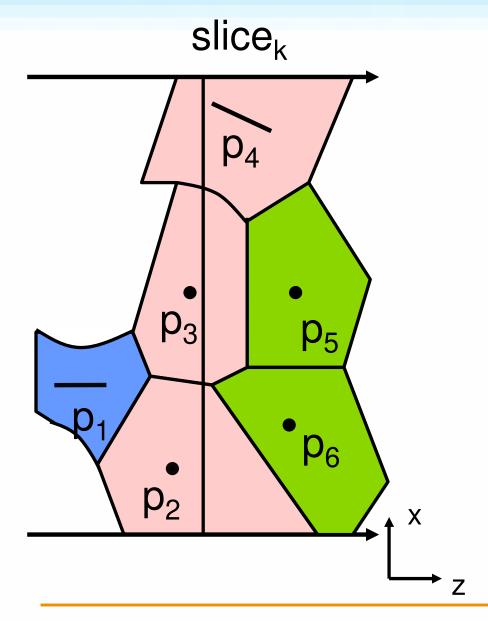


- For each slice partition the set of sites using Voronoi region bounds:
 - Approaching
 - Intersecting
 - Receding





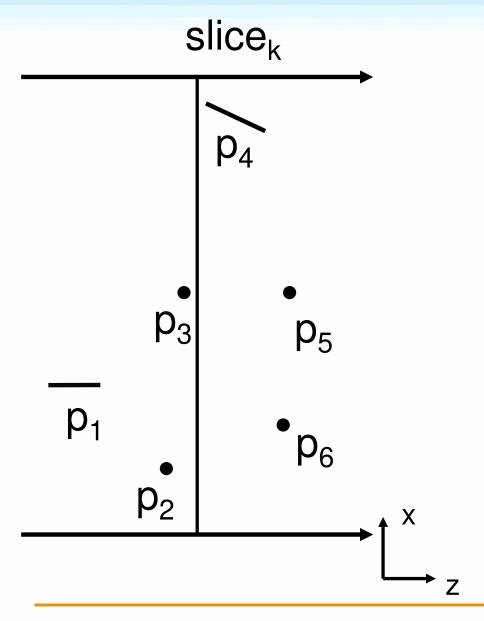
- For each slice partition the set of sites using Voronoi region bounds:
 - Approaching
 - Intersecting
 - Receding
- Only Intersecting sites contribute to distance field





Site Classification

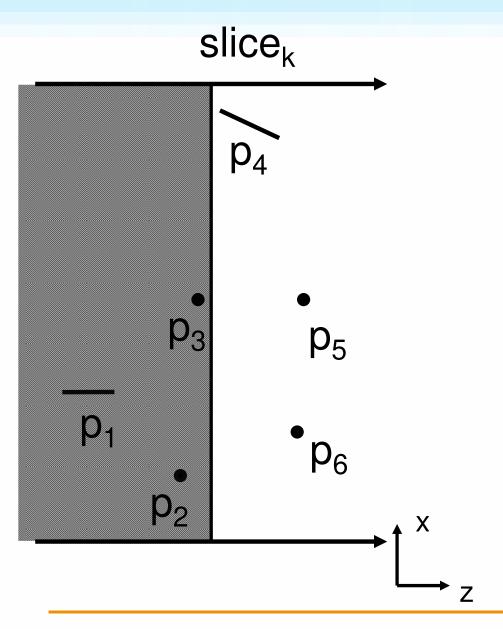
For each slice,
 also partition set
 of sites using
 sweep direction





Site Classification

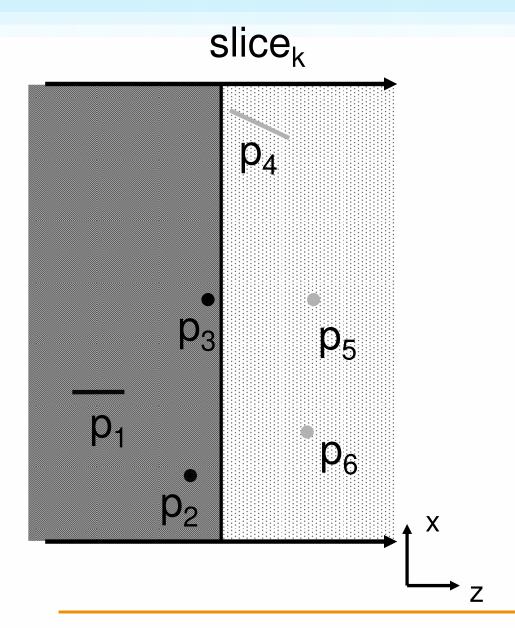
- For each slice,
 also partition set
 of sites using
 sweep direction
 - Swept





Site Classification

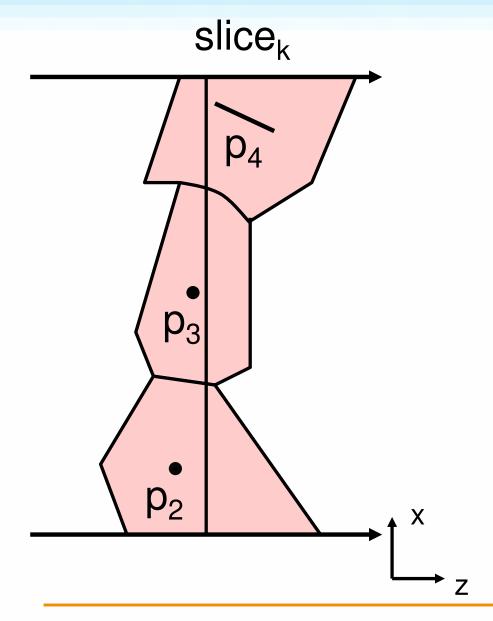
- For each slice,
 also partition set
 of sites using
 sweep direction
 - Swept
 - Unswept





Acceleration Techniques

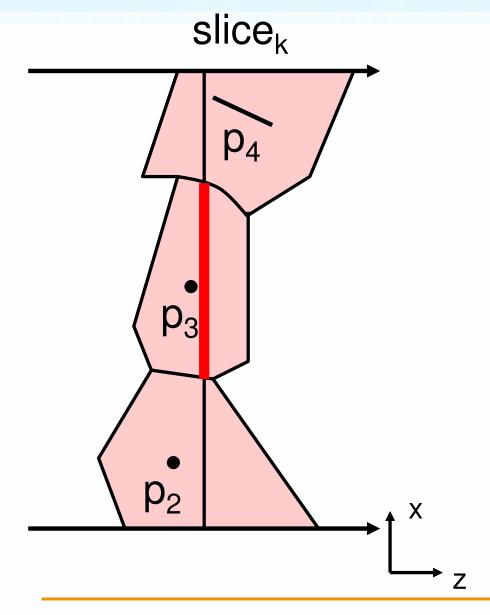
 Culling: Render distance functions for intersecting sites only





Acceleration Techniques

- Culling: Render distance functions for intersecting sites only
- Clamping: For each intersecting site, clamp domain of computation





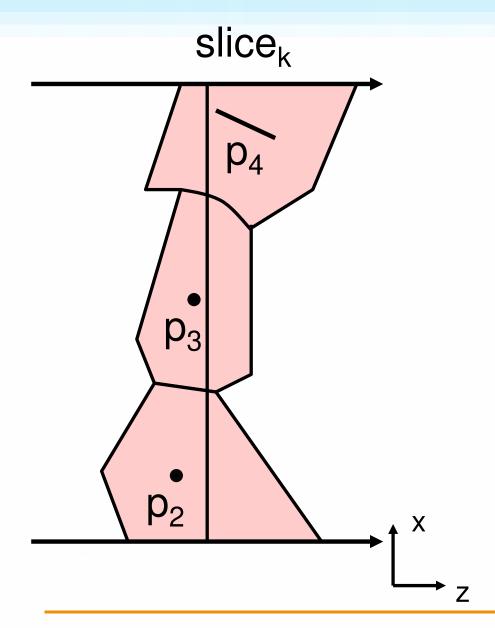
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Culling: Goal

 Render distance functions for intersecting sites only



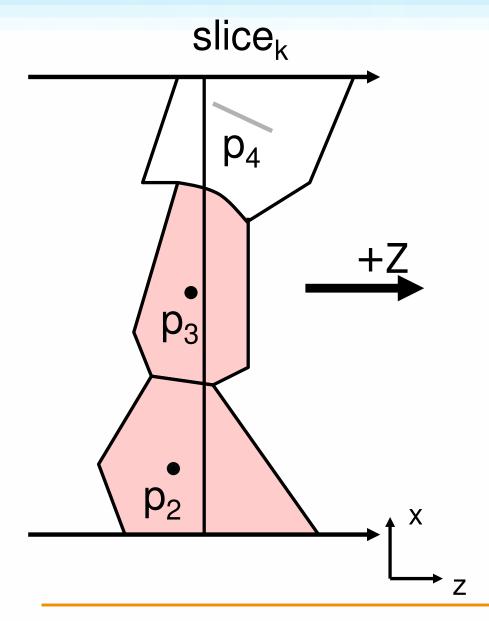


Culling: 2 Pass Algorithm

Render distance functions for

intersecting swept

sites: +Z pass



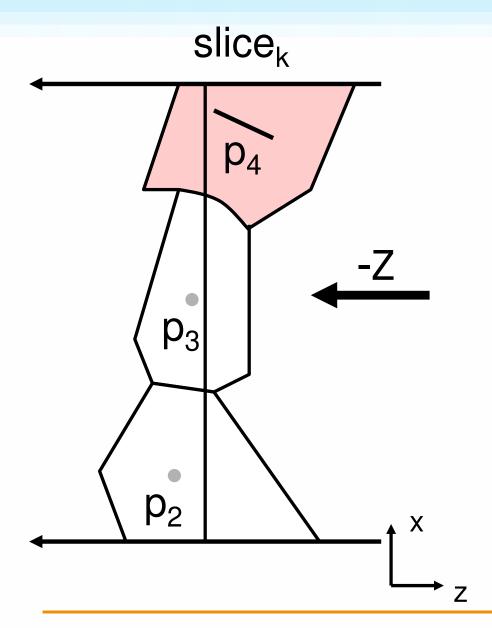


Culling: 2 Pass Algorithm

Render distance functions for

intersecting swept

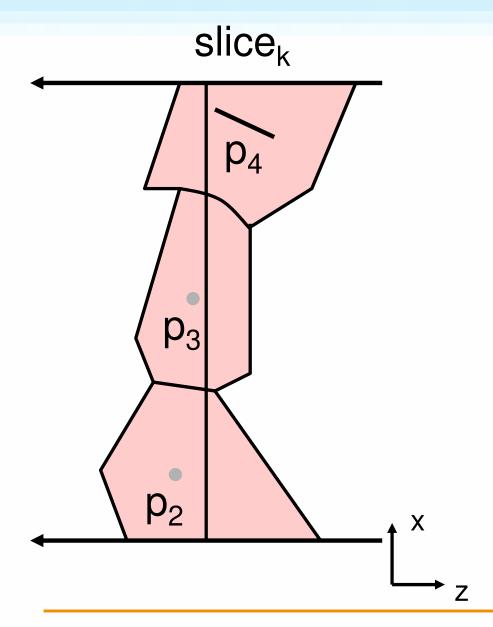
sites: -Z pass





Culling: 2 Pass Algorithm

- Render distance functions for intersecting swept sites
- Final distance field obtained after both passes



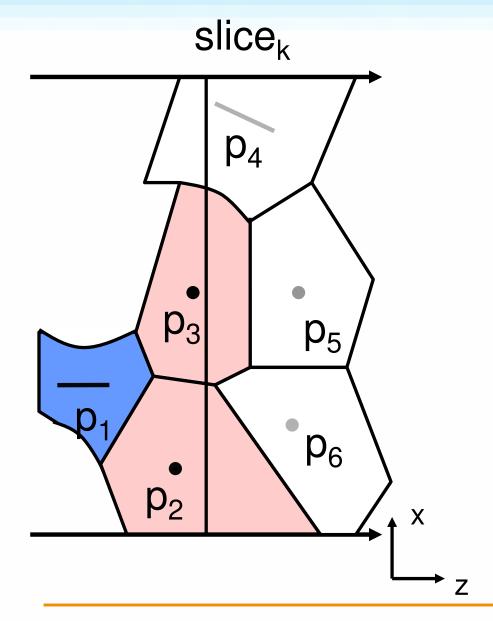


Culling

- Computing exact intersecting set = Exact Voronoi computation
- Swept set easy to compute
- Compute a set of potentially intersecting swept (PIS) sites
- Use hardware based occlusion queries to compute *PIS*

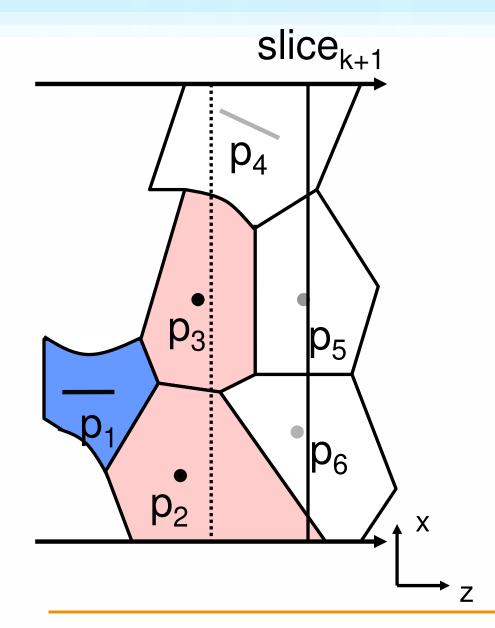


Given the
 potentially intersecting swept set for slice k



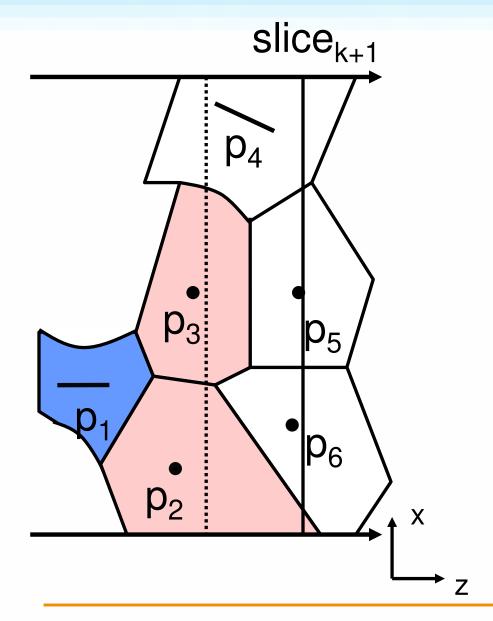


For slice k+1:



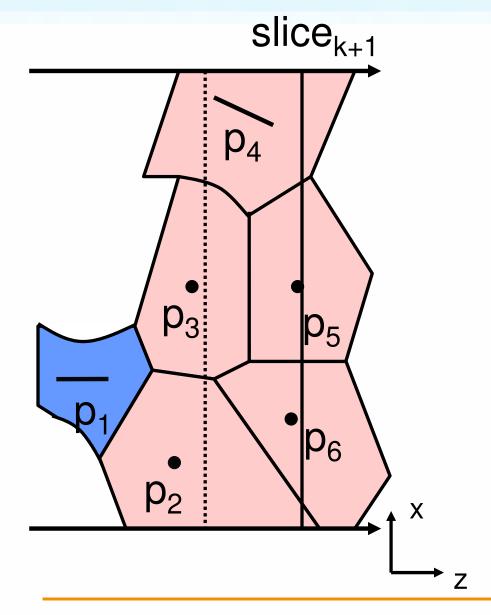


- For slice k+1:
 - Add newly swept sites to PIS



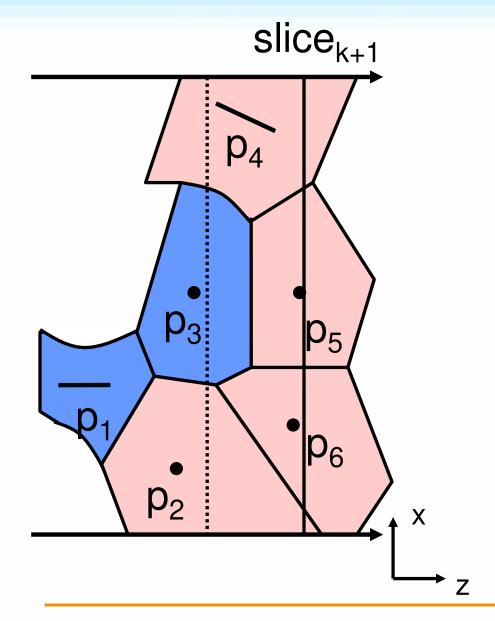


- For slice k+1:
 - Add newly swept sites to PIS
 - Draw distance functions of new PIS





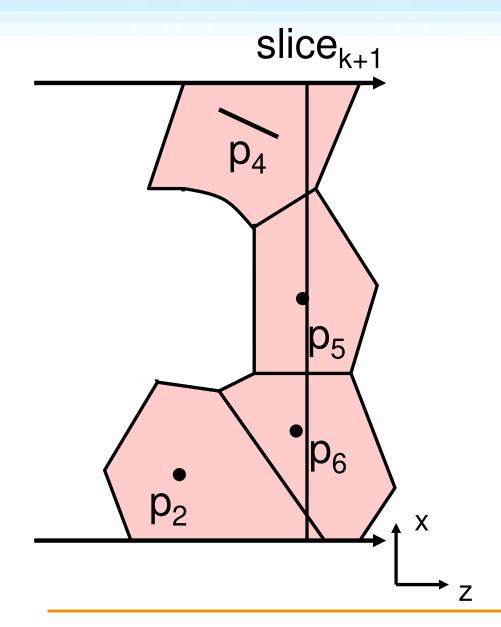
- For slice k+1:
 - Add newly swept sites to intersecting set
 - Draw distance functions of new intersecting set
 - Check visibility and update receding set





For slice k+1:

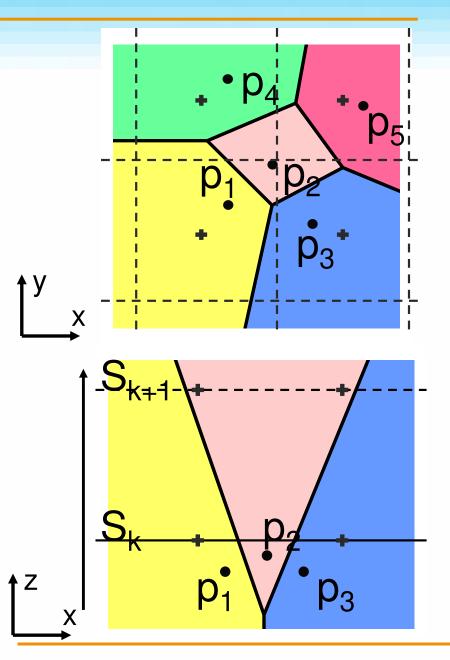
- Add newly swept sites to intersecting set
- Draw distance functions of new intersecting set
- Check visibility and update receding set
- Get final intersecting swept set for slice k+1





Culling: Conservative Sampling

- Issue: Image space occlusion query may under sample a Voronoi region
 - Wrongly classifies a site as receding
- Solution: "Grow" the Voronoi region by pixel size (details in paper)





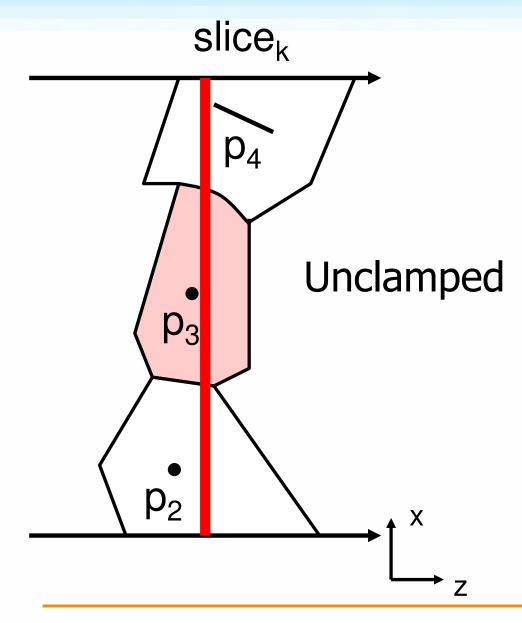
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Clamping: Goal

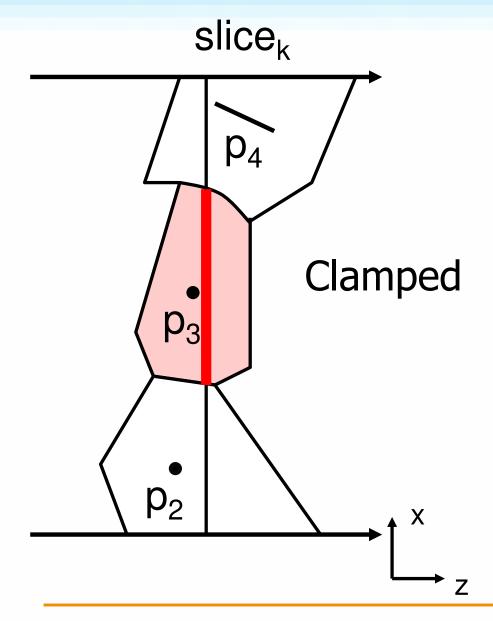
Clamping: For each intersecting site, clamp domain of computation





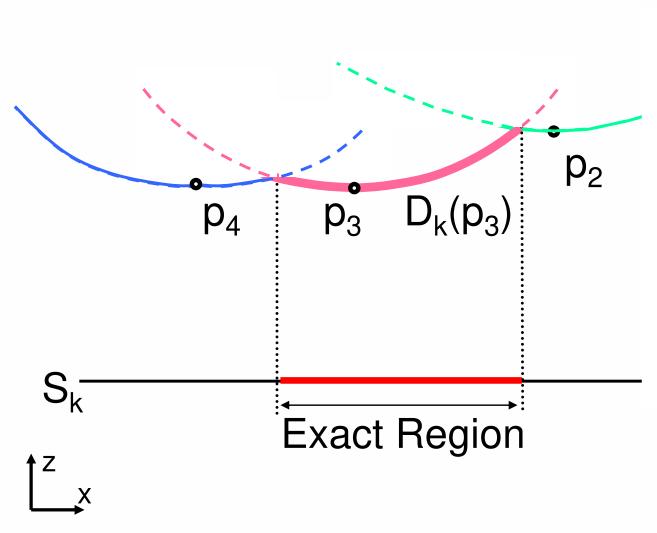
Clamping: Goal

- Clamping: For each intersecting site, clamp domain of computation
- Domain of computation = Intersection of Voronoi Region with slice



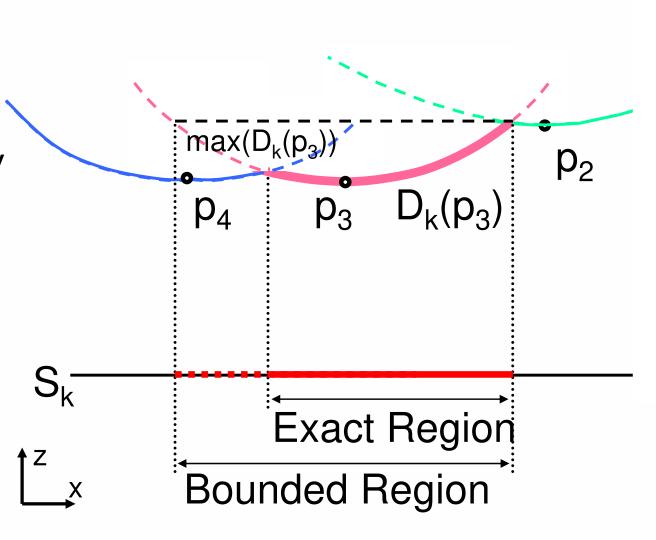


- Distance function of each site is monotonic
- The exact Voronoi region





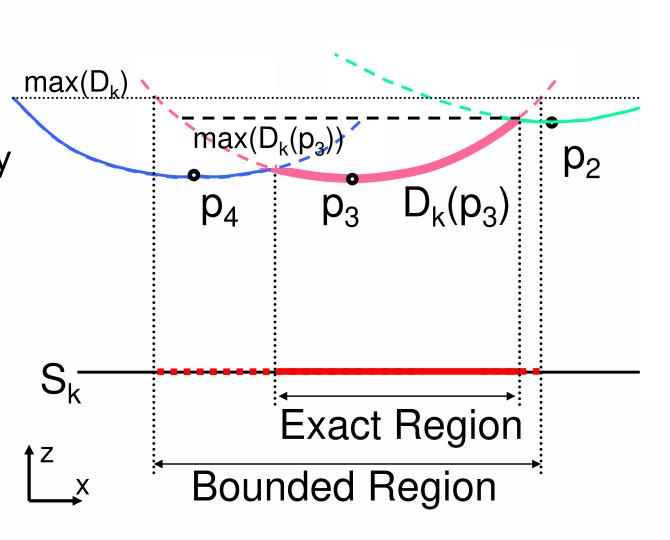
- Distance function of each site is monotonic
- The exact Voronoi region is bounded by max of distance function





Distance function of each site is monotonic

The exact Voronoi region is bounded by max of distance function, which is bounded by max of distance field, max(D_k)





Compute max(D_{k+1}) for slice k+1 incrementally using max(D_k)

Lemma: Let distance between adjacent slices be δ_z . Then change in maximum value of distance field between slices S_k and S_{k+1} is given by:

$$max(D_{k+1}) \leq max(D_k) + \delta_z$$

 \bigcirc Use max(D_{k+1}) for clamping



Clamping: Manifold Sites

- Voronoi region bounded by prisms, wedges and cones [Mauch00, Sigg03]
- For each manifold site, refine Voronoi region bounds using prism, wedge or cone bounds



Outline

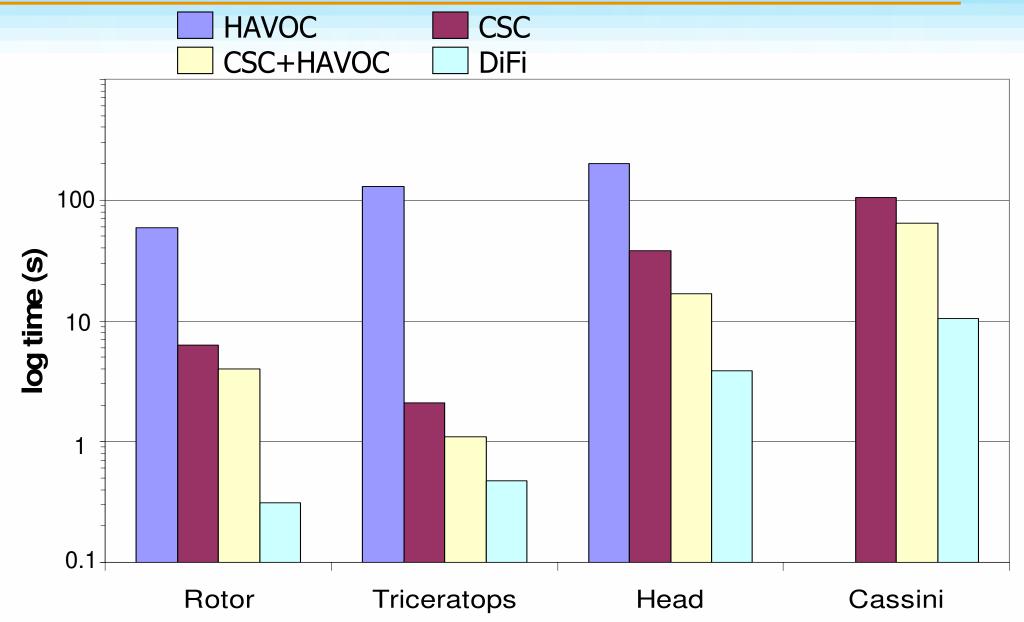
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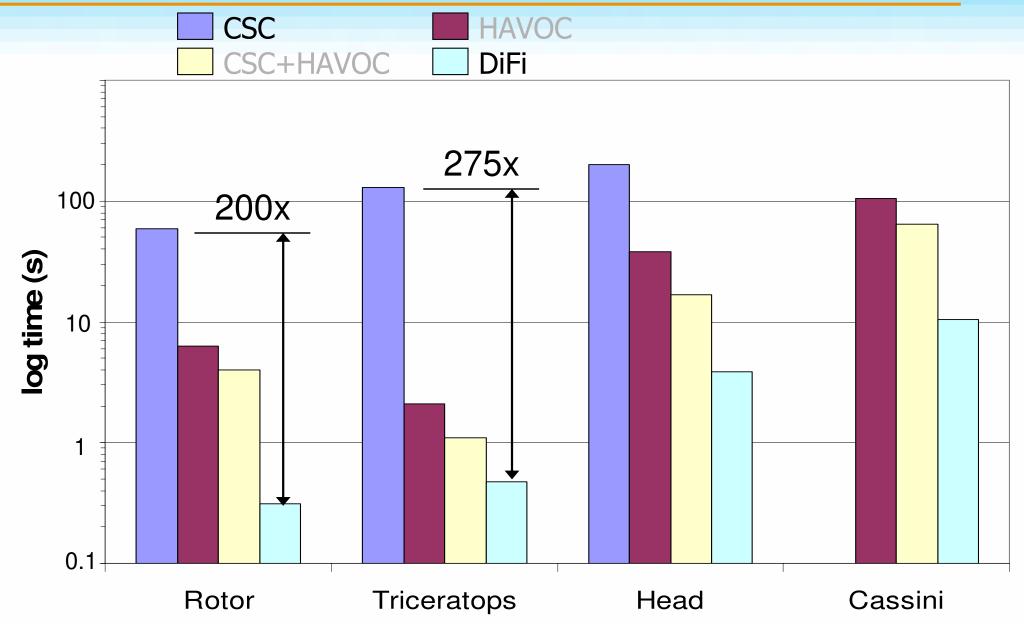
Implementation

- Pentium4 2.8Ghz, 2GB RAM
- NVIDIA GeForce FX 5900 Ultra,
 256MB Video RAM
- Windows XP, OpenGL
- HAVOC3D [Hoff99]

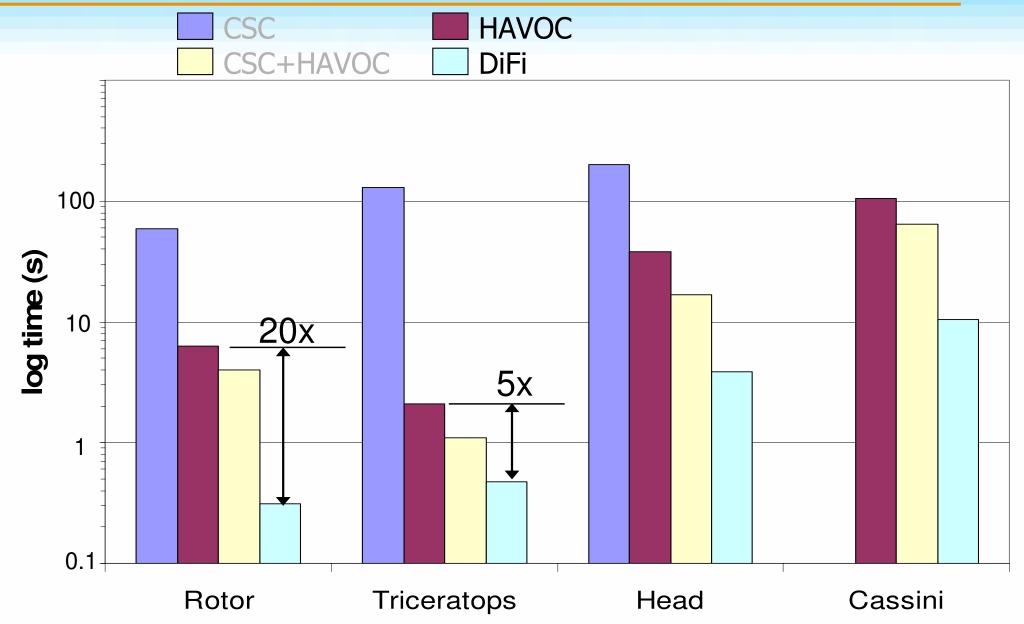




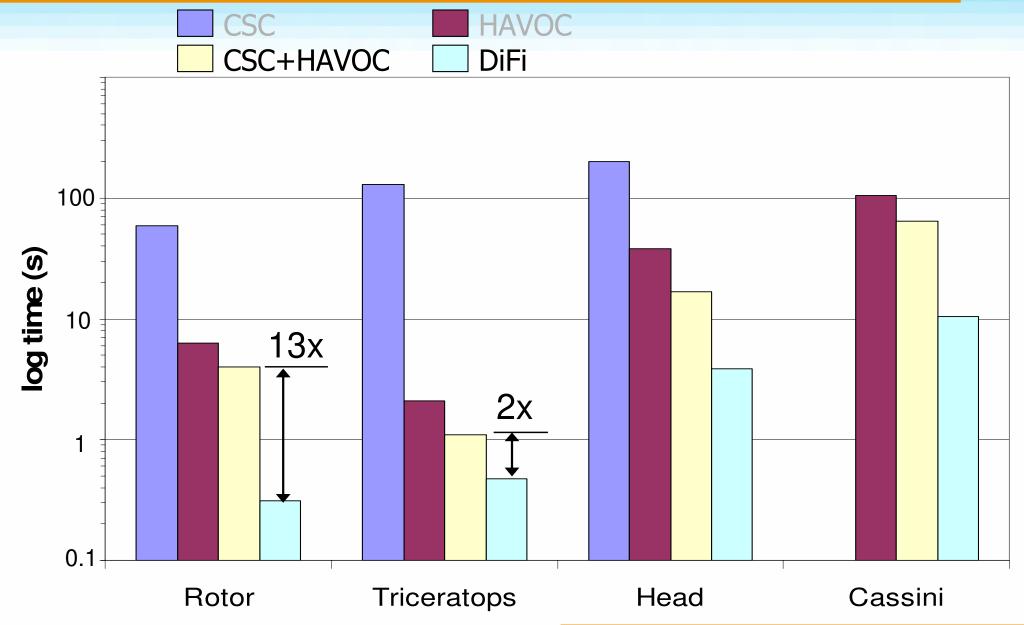




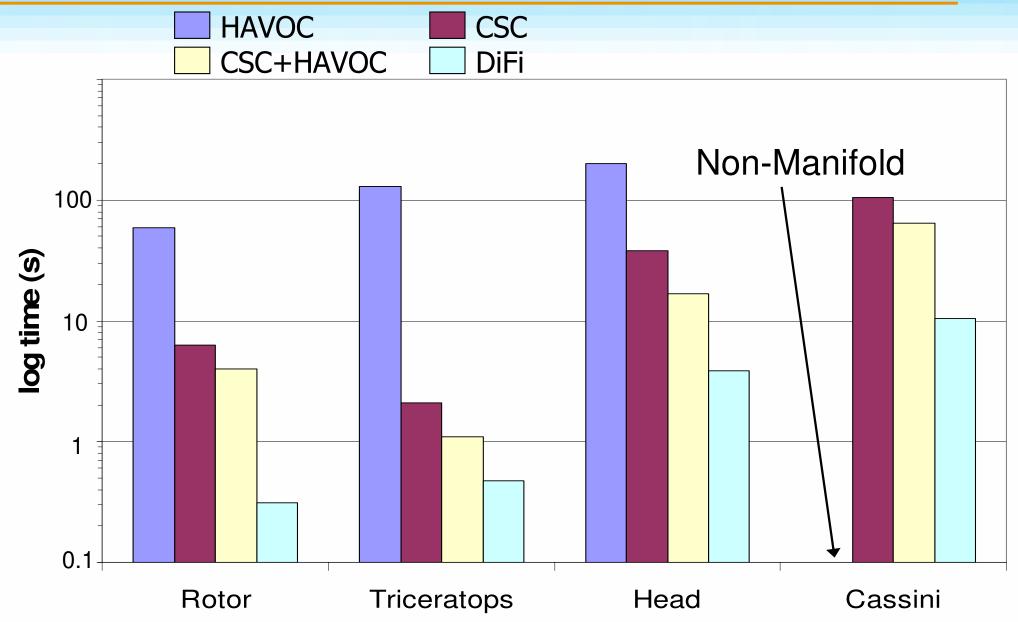






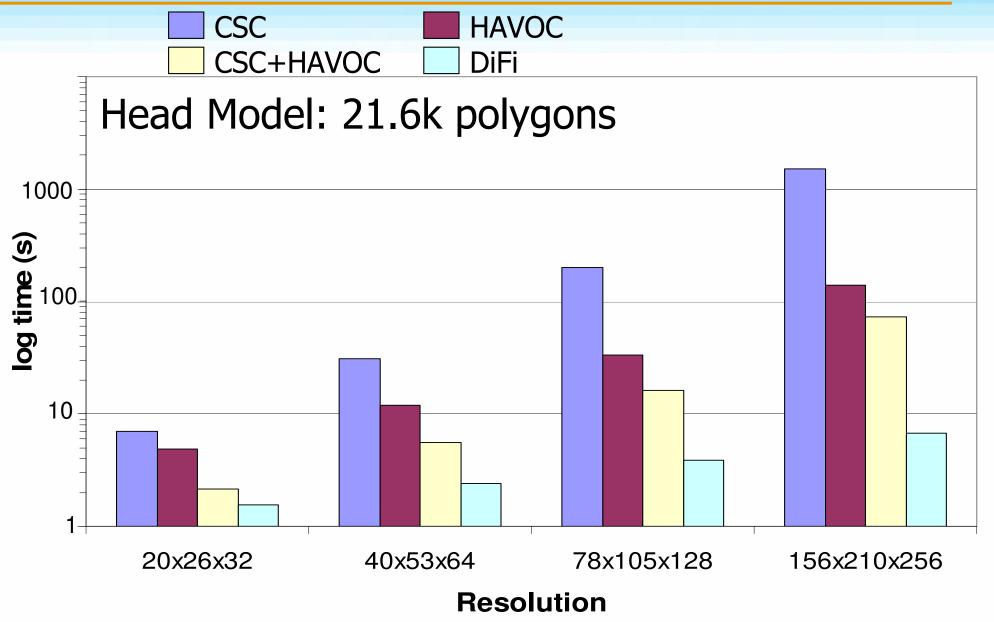








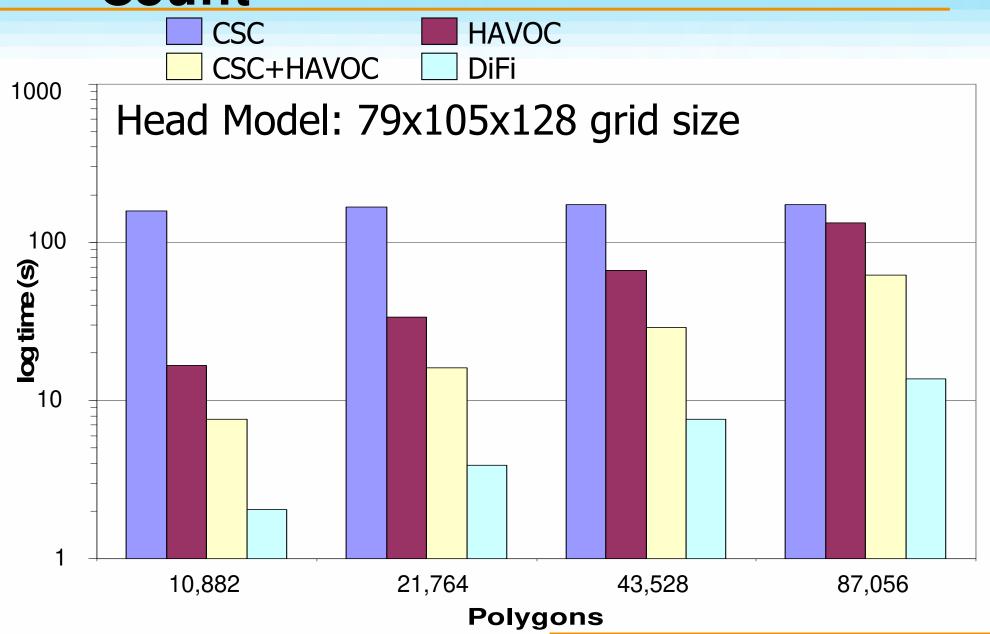
Results: Varying Resolution





Results: Varying Polygon

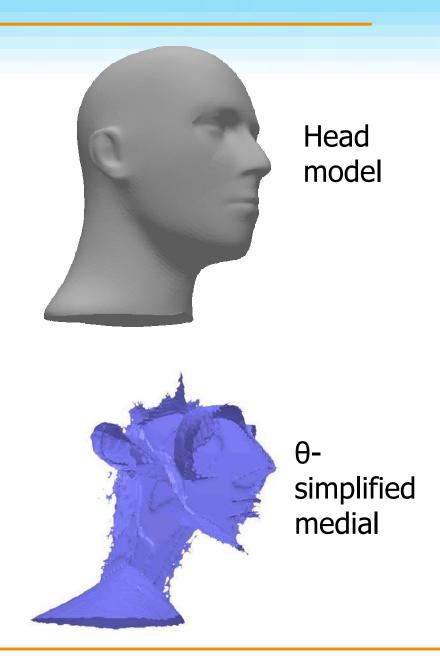
Count





Applications: Medial Axis

- Compute a simplified medial axis using gradient of distance field [Foskey03]
- Stable subset of exact medial axis





Applications: Medial Axis

Medial Axis Computation

Triceratops (5K polys)
Distance Field Cost = 0.8sec/frame



Applications: Motion Planning

- DiFi used in a constraint-based planner [Garber02]
- Voronoi diagram → Estimated path
- Distance field → Proximity queries



Live Demo

- Laptop
 - Pentium4 3.2Ghz, 2GB RAM
 - NVIDIA GeForce FX Go5700, 128MB
 Video RAM
 - Windows XP, OpenGL



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Conclusions

- A fast 3D distance field computation algorithm with an order of magnitude speedup
 - Almost interactive for complex 3D models
- Applicable to complex polygonal and image models
- No preprocessing
 - Applicable to dynamic environments



Conclusions

- Use geometric properties to reduce computations
 - Culling
 - Clamping
- Exploit spatial coherence for incremental computation
- Perform geometric tests efficiently on GPU
 - Overcome undersampling



Limitations

- Best suited for *global* distance field computation in complex environments
 - Culling involves occlusion query overhead
 - Clamping bounds depend on distribution of sites
- Computes distance field on uniform grid
 - Size limited by GPU memory
- Application may require distance field readback to CPU



Future Work

- Efficient clamping for manifold sites [Sigg03]
- Explore temporal coherence for dynamic and deformable models
- Extend to k-th order Voronoi diagrams
- Further applications like dynamic simulation, morphing and database queries



Acknowledgments

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- Mark Harris, Greg Coombe, Naga Govindaraju
- UNC GAMMA group



Questions?



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